Computational and Differential Geometry 2022-1



MIDTERM ASSIGNMENT 3

April 22, 2022

Indicaciones generales

- 1. Fecha de publicación: 22 de abril de 2022.
- 2. Fecha de entrega: 29 de abril de 2022 hasta las 23:55.
- 3. Único medio de entrega: https://e-aulas.urosario.edu.co.
- 4. Formato de entrega: módulo y driver (main.py) en Python 3.
- 5. Importante: no use acentos ni deje espacios en los nombres de los archivos que cree.
- 6. La actividad debe realizarse individualmente.
- 7. Los grupos pueden consultar sus ideas con los profesores para recibir orientación; sin embargo, la solución y detalles del ejercicio debe realizarlos **individualmente**. Cualquier tipo de fraude o plagio es causa de anulación directa de la evaluación y correspondiente proceso disciplinario.
- 8. El grupo de trabajo debe indicar en su entrega de la solución a la actividad cualquier asistencia que haya recibido.
- 9. El grupo no debe consultar ninguna solución a la actividad que no sea la suya.
- 10. El grupo no debe intentar ocultar ningún código que no sea propio en la solución a la actividad (a excepción del que se encuentra en las plantillas).
- 11. Las entregas están sujetas a herramientas automatizadas de detección de plagio en códigos.
- 12. e-aulas se cerrará a la hora acordada para el final de la evaluación. La solución de la actividad debe ser subida antes de esta hora. El material entregado a través de e-aulas será calificado tal como está. Si ningún tipo de material es entregado por este medio, la nota de la evaluación será 0.0.

Introduction

So you've decided to spend your undergraduate internship at a robot motion planning company. The company is widely known for their expertise in the control of the sailing of autonomous cargo ships. These crewless vessels transport either containers or bulk cargo over navigable waters with little or no human interaction. See Figure 1. Unfortunately, the last project on autonomous cargo ships of the company has presented some problems related to the self-navigation system and help is needed getting it back up again.

Given that you're a savvy intern with wide knowledge on algorithms and data structures, your boss has assigned to you fixing the project problem(s). Solving the issues with the self-navigation system of an autonomous cargo ship requires the implementation of a brand new interface. This piece of software will be plugged into the rest of the software developed by other colleagues in the company.

Problem

Your job is then to provide a computational application that offers different options of autonomous ship sailing (motion) planning. The functionality required evaluates aspects of autonomous ship navigation within a fleet: a group of ships. These aspects include global and local properties such as nearest and farthest ships, analysis of potential collisions, and drawing maps of the fleet.

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Figure 1: Schematic view of how the motion planning of autonomous cargo ships work.

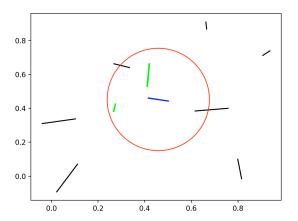
The application must be implemented as a class with a collection of methods and a driver, coded in Python 3. We will treat the ships on the map as a line segment (x_i, x_f, y_i, y_f) of the coordinates for the bow (x_f, y_f) and the stern (x_i, y_i) , and treat its location as the mean point of the bow and stern coordinates. We will measure all distances using the standard Euclidean norm in the plane. The methods must satisfy the following specifications:

- 1. Nearest ships. Communication between ships has a finite range. A ship has to know to which ships send information relevant to the navigation route. Given the location of a vessel (point in the plane), find and report the s closest ships to the location using the Euclidean distance. If there is more than s closest to the location of the vessel, report only s of them, choosing them randomly.
- 2. Avoiding collisions. As the ships navigate, they need to take into account if there are other vessels within some distance so maneuvers can be performed and collisions be avoided. Find and return whether there are any ships within a ball of radius r and center given by the location of a ship. Notice that because the ships are segments and not points you must perform a range search using the coordinates of both stern and bow.
- 3. Partner lookup. Knowing where the nearest ship is located within a fleet is also of interest to autonomous vessels. This piece of information is relevant in case of attack, emergency, etc. Every vessel in a fleet must have another vessel that is closest to it. Find all the closest-pair of locations of ships within the fleet. You must always be able to find a closest-pair to every ship regardless of their distance.
- 4. Operation radius. This number offers information regarding the range or scope of operation of the whole fleet and how far and how fast it can react to an event during navigation. Find and report the approximate radius of the circle that encloses all the ships in the fleet. You must consider that the ships are extended objects and *not* treat them as points in the plane. Your solution, however, can be approximate but close to the true smallest enclosing circle.

The class should be named AutonFleet. You have the freedom to choose its attributes so redundant computation is avoided as much as possible. Notice that two trees must be constructed: one that considers vessels as locations and another that considers them as segments. Extra methods may be implemented if necessary. Start by analyzing their prototype, then implement them, and finally, test them.

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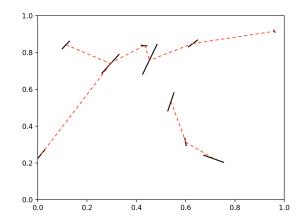


Figure 2: Solution of the 'avoiding collisions' and 'partner lookup' problems for a 10-ship fleet. *Left*: Given the radius of the circle (red) and a ship (blue) report all ships completely contained inside the circle (green). *Right*: Closest-pair of ships within the fleet. Given a ship (black), the (red) dashed line displays its closest-pair.

The solution to each problem must generate a plot clearly *showing and labeling* the answer; you may also print extra information to the terminal with further details. See Figure 2 for details. Regarding input data, randomly generate around 10–200 points in the interval $R = [0, 1] \times [0, 1]$.

Strategy

Let us now analyze how to proceed. The input to the problem is the segments, saved in the format (x_i, x_f, y_i, y_f) in the input files, that represents each vessel in the fleet, so you need to read the coordinates and appropriately keep the information. Next, remembering what you learned in Computational Geometry, you know that you need to build a computational model of the fleet so that you can efficiently process information about navigation and implement the functionality discussed above. A good candidate geometric model is a k-d tree, which is a geometric data structure that partitions space. Other pieces of information might also be relevant to keep nearby.

With this understanding, we now have a clear picture of how to proceed with the construction of the class. You may also want to keep in mind the range searching, the nearest-neighbor and the closest-pair of points problems, which can be efficiently solved in two dimensions using k-d trees.

See Exercise 5.13 from the Dutch book for other details.

References

M. de Berg, O. Cheong, M. van Kreveld, and M. Overmars. *Computational Geometry: Algorithms and Applications*. Third edition. Springer-Verlag, 2008.