

Proyecto de Modelado Matemático I: Visualización 3D en VisIt

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CAFE: A NEW RELATIVISTIC MHD CODE

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ABSTRACT

We introduce CAFE, a new independent code designed to solve the equations of relativistic ideal magnetohydrodynamics (RMHD) in three dimensions. We present the standard tests for an RMHD code and for the relativistic hydrodynamics regime because we have not reported them before. The tests include the one-dimensional Riemann problems related to blast waves, head-on collisions of streams, and states with transverse velocities, with and without magnetic field, which is aligned or transverse, constant or discontinuous across the initial discontinuity. Among the two-dimensional (2D) and 3D tests without magnetic field, we include the 2D Riemann problem, a one-dimensional shock tube along a diagonal, the high-speed Emery wind tunnel, the Kelvin-Helmholtz (KH) instability, a set of jets, and a 3D spherical blast wave, whereas in the presence of a magnetic field we show the magnetic rotor, the cylindrical explosion, a case of Kelvin-Helmholtz instability, and a 3D magnetic field advection loop. The code uses high-resolution shock-capturing methods, and we present the error analysis for a combination that uses the Harten, Lax, van Leer, and Einfeldt (HLL-E) flux formula combined with a linear, piecewise parabolic method and fifth-order weighted essentially nonoscillatory reconstructions. We use the flux-constrained transport and the divergence cleaning methods to control the divergence-free magnetic field constraint.

Key words: magnetohydrodynamics (MHD) – methods: numerical – relativistic processes

1. INTRODUCTION

Models of high-energy astrophysics are closely related to relativistic fluid dynamics because most of the sources are identified with the dynamics of a gas or plasma associated with

currently most used codes. The Cactus Einstein Toolkit, a multiplatform package mounted on Cactus (Goodale et al. 2003), is capable of solving the general relativistic MHD (Mina et al. 2014). Whisky, a code that in its most sophisticated version can evolve general relativistic resistive magnetohydro-

Magnus: A New Resistive MHD Code with Heat Flow Terms

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Abstract

We present a new magnetohydrodynamic (MHD) code for the simulation of wave propagation in the solar atmosphere, under the effects of electrical resistivity—but not dominant—and heat transference in a uniform 3D grid. The code is based on the finite-volume method combined with the HLL-E and HLLC approximate Riemann solvers, which use different slope limiters like MINMOD, MC, and WENO5. In order to control the growth of the divergence of the magnetic field, due to numerical errors, we apply the Flux Constrained Transport method, which is described in detail to understand how the resistive terms are included in the algorithm. In our results, it is verified that this method preserves the divergence of the magnetic field within the machine round-off error ($\sim 1 \times 10^{-15}$). For the validation of the accuracy and efficiency of the schemes implemented in the code, we present some numerical tests in 1D and 2D for the ideal MHD. Later, we show one test for the resistivity in a magnetic reconnection process and one for the thermal conduction, where the temperature is advected by the magnetic field lines. Moreover, we display two numerical problems associated with the MHD wave propagation. The first one corresponds to a 3D evolution of a vertical velocity pulse at the photosphere–transition–corona region, while the second one consists of a 2D simulation of a transverse velocity pulse in a coronal loop.

Key words: magnetohydrodynamics (MHD) – methods: numerical – Sun: atmosphere

1. Introduction

The theory of magnetohydrodynamics—the study of interactions between magnetic fields and conductive fluids in low frequencies—is of great importance for understanding the dynamics of the plasma in the solar atmosphere (Priest & Hood 1991). Since the plasma, in this region is highly

atmosphere (Joss et al. 2012a). Complete reviews of observations of magnetohydrodynamic waves in solar regions like the corona, sunspots, prominences, coronal mass ejections, solar flares, and solar winds can be found in Nakariakov & Verwilt (2005), Khomenko & Collados (2015), Okamoto et al. (2007), Vršnak et al. (2013), Shibata & Magara (2011), and Ofman (2010), respectively.

```
(base) paula@PaulaCW:~/pron/Graphs_ASCII$ head -25 prmtttvas_1.xyzl
```

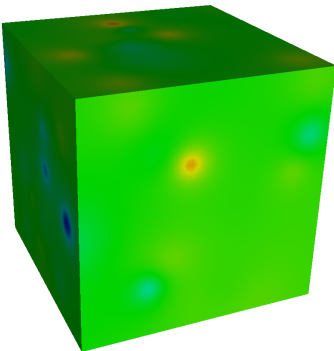
```
#line = 0.0000000000000000
```

```
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9.9999997540632175E-015 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 0.9998734590737456E-015 1.0000168665552601E-014
0.000000000000000000 -0.500000000000000000 -0.479999999999999998 3.0300707122200770E-006 9.9998734590737456E-015 1.0000168665552601E-014
1.0000000189603919E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 0.9998734590737456E-015 1.0000168665552601E-014
0.000000000000000000 -0.500000000000000000 -0.460000000000000002 3.0300707122200770E-006 9.9998734590737456E-015 1.0000168665552601E-014
1.0000003004945944E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 9.994104067192648E-015 1.0006969245196090E-014
0.000000000000000000 -0.500000000000000000 -0.440000000000000000 3.0300707122200770E-006 9.994104067192648E-015 1.0006969245196090E-014
1.000001978134284E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 9.9685720085807909E-015 1.0037413580362885E-014
0.000000000000000000 -0.500000000000000000 -0.419999999999999998 3.0300707122200770E-006 9.9685720085807909E-015 1.0037413580362885E-014
1.000011192438348E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 9.845699694818114E-015 1.0192874667451618E-014
0.000000000000000000 -0.500000000000000000 -0.400000000000000002 3.0300707122200770E-006 9.845699694818114E-015 1.0192874667451618E-014
1.0000578307609614E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 9.3024279254236336E-015 1.0917857257959950E-014
0.000000000000000000 -0.500000000000000000 -0.380000000000000000 3.0300707122200770E-006 9.3024279254236336E-015 1.0917857257959950E-014
1.000275325381139E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 7.0965887034301607E-015 1.4032098153708638E-014
0.000000000000000000 -0.500000000000000000 -0.350000000000000000 3.0300707122200770E-006 7.0965887034301607E-015 1.4032098153708638E-014
1.001209597806625E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 5.118656916139387E-015 2.6350965269109879E-014
0.000000000000000000 -0.500000000000000000 -0.330000000000000000 3.0300707122200770E-006 5.118656916139387E-015 2.6350965269109879E-014
1.0049052759414590E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 2.9173474951067055E-014 7.1208553797846292E-014
0.000000000000000000 -0.500000000000000000 -0.320000000000000001 3.0300707122200770E-006 2.9173474951067055E-014 7.1208553797846292E-014
1.0183625345000799E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 1.1690786257281141E-013 2.2151310344176631E-013
0.000000000000000000 -0.500000000000000000 -0.299999999999999999 3.0300707122200770E-006 1.1690786257281141E-013 2.2151310344176631E-013
1.0634538993932558E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 3.6783910560619354E-013 6.8471268769845656E-013
0.000000000000000000 -0.500000000000000000 -0.280000000000000003 3.0300707122200770E-006 3.6783910560619354E-013 6.8471268769845656E-013
1.2024137746702629E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 1.0231425810445261E-012 1.9968126549272344E-012
0.000000000000000000 -0.500000000000000000 -0.260000000000000001 3.0300707122200770E-006 1.0231425810445261E-012 1.9968126549272344E-012
1.5960437648388964E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 2.823440342231712E-012 5.4107167369864601E-012
0.000000000000000000 -0.500000000000000000 -0.239999999999999999 3.0300707122200770E-006 2.823440342231712E-012 5.4107167369864601E-012
2.6202149894566641E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 5.928653076908586E-012 1.3561966607367233E-011
0.000000000000000000 -0.500000000000000000 -0.210000000000000000 3.0300707122200770E-006 5.928653076908586E-012 1.3561966607367233E-011
5.06589958570060E-014 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 1.2546531168589553E-011 3.1401327920163171E-011
0.000000000000000000 -0.500000000000000000 -0.200000000000000001 3.0300707122200770E-006 1.2546531168589553E-011 3.1401327920163171E-011
1.0417398344409679E-013 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 2.4154398808382749E-011 6.7133380021864337E-011
0.000000000000000000 -0.500000000000000000 -0.179999999999999999 3.0300707122200770E-006 2.4154398808382749E-011 6.7133380021864337E-011
2.1136908974920829E-013 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 4.2387838862377795E-011 1.3259324644362160E-010
0.000000000000000000 -0.500000000000000000 -0.159999999999999998 3.0300707122200770E-006 4.2387838862377795E-011 1.3259324644362160E-010
0.0747973901447202E-013 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 6.7587161875994187E-011 2.4142843526995708E-010
0.000000000000000000 -0.500000000000000000 -0.140000000000000001 3.0300707122200770E-006 6.7587161875994187E-011 2.4142843526995708E-010
7.3425530549347846E-013 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003 9.7447395985511123E-011 4.0608248327132344E-010
0.000000000000000000 -0.500000000000000000 -0.120000000000000000 3.0300707122200770E-006 9.7447395985511123E-011 4.0608248327132344E-010
1.2282174494975776E-012 299.99983692554611 7.0897999763653063E-023 7.0897999763653063E-023 5.00000001419004654E-003
```

```
(base) paula@PaulaCW:~/pron/Graphs_ASCII$
```

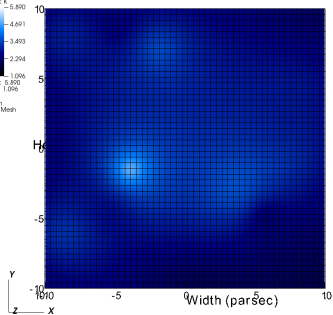
DB: example.silo
Cycle: 0

Pseudocolor
Var: pressure
Units: Pa
-5.779
-4.610
-3.442
-2.273
-1.104
Max: 5.779
Min: -1.104



DB: example.silo
Cycle: 0

Pseudocolor
Var: temp
Units: K
-5.880
-4.691
-3.493
-2.294
-1.096
Max: 5.880
Min: -1.096
Mesh
Var: Mesh



Solución 1

```
from __future__ import print_function
import os
from astropy.io import ascii

def ascii2hdf5(inputfile, outputfile, clobber=False, overwrite=True,
               verbose=False):
    """Convert a file to hdf5 using compression and path set to data"""
    if verbose:
        print('converting {} to {}'.format(inputfile, outputfile))

    tbl = ascii.read(inputfile)
    try:
        tbl.write(outputfile, format='hdf5', path='data', compression=True,
                  overwrite=overwrite)
    except:
        print('problem with {}'.format(inputfile))
        return

    if clobber:
        os.remove(inputfile)
        if verbose:
            print('removed {}'.format(inputfile))

    return
```

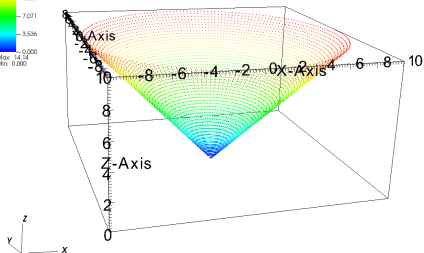
Solución 2

```
import math
n = 10000
f = open("values.3D", "wt")
f.write("x y z value\n");
for i in range(n):
    t = float(i) / float(n-1)
    angle = t * (math.pi * 2.) * 50.
    r = t * 10.
    x = r * math.cos(angle)
    y = r * math.sin(angle)
    z = t * 10.
    value = math.sqrt(x*x + y*y + z*z)
    f.write("%g %g %g %g\n" % (x,y,z,value))
f.close()
```

DB: values.3D
Cycle: 0

Mesh
Var: points

Pseudocolor
Var: value



```

import sys
import numpy as np

# Se importa el archivo con los datos correspondientes
# a las dimensiones y tiempos de las corridas
filedata = open('input_plots.par', 'r')

lines = filedata.readlines()
# Se asignan la variables del archivo filedata en
# las variables correspondientes
xmin = float(lines[1].split('=')[1])
xmax = float(lines[2].split('=')[1])
ymin = float(lines[3].split('=')[1])
ymax = float(lines[4].split('=')[1])
zmin = float(lines[5].split('=')[1])
zmax = float(lines[6].split('=')[1])
Nxx = int(lines[7].split('=')[1])
Nyy = int(lines[8].split('=')[1])
Nzz = int(lines[9].split('=')[1])
Ntt = int(lines[10].split('=')[1])
courant = float(lines[11].split('=')[1])
every3D = float(lines[14].split('=')[1])

# Se cierra el archivo
filedata.close()

# Se calculan los pasos espaciales y temporales
dx = (xmax - xmin)/float(Nxx)
dy = (ymax - ymin)/float(Nyy)
dz = (zmax - zmin)/float(Nzz)
dt = courant * min(dx,dy,dz)

```

```

# Se importa el archivo con los datos de las corridas correspondientes a las variables
# densidad, velocidad en x, y, z, presion y campo magnetico en x, y, z
f = open('primitivas_1.xyzl', 'r')

# Se crea la funcion 'extraer' para tomar determinado tiempo y variable del archivo f
def extraer(parametro):

    # Se leen las entradas para reconocer la variable y tiempo a extraer
    variable = str(parametro.split('-')[0])
    bloque = format(int(parametro.split('-')[1]), '02')

    # Se calcula el tiempo real que se esta extrayendo
    t = dt*float(bloque)*every3D

    # Se valida la infomacion acerca de la variable, el bloque de tiempo y el tiempo
    # real que se esta extrayendo
    print 'Extrayendo la variable',variable,'en el bloque',bloque,'en',t, 'segundos.'

    # Se saltan las lineas correspondientes a los tiempos anteriores al que se requiere
    skip = int((((Nyy+2)*(Nxx+1)+1)*(Nzz+1)+4)*int(bloque))
    print 'Se saltan', skip, 'lineas.'
    for a in range (0,skip+3):
        f.readline()

    # Se crea un archivo nuevo llamado por el nombre de la variable y el bloque a extraer
    w = open('%s_b%s.3D'%(variable,bloque), 'wt')
    # Se escribe el encabezado necesario para que VisIt pueda leer los archivos ASCII
    w.write('x y z %s\n'%variable);

```



```

# Se leen las lineas de la misma manera como fueron salvadas y se reescriben
# los datos requeridos en el archivo w
for i in range(0,Nzz+1):
    f.readline()
    for j in range(0,Nxx+1):
        f.readline()
        for k in range(0,Nyy+1):
            z, x, y, rho, vx, vy, vz, press, Bx, By, Bz = f.readline().split()
            if (variable == 'v'):
                v = np.sqrt(float(vx)**2+float(vy)**2+float(vz)**2)
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(v)))
            elif (variable == 'B'):
                B = np.sqrt(float(Bx)**2+float(By)**2+float(Bz)**2)
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(B)))
            elif (variable == 'rho'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(rho)))
            elif (variable == 'vx'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(vx)))
            elif (variable == 'vy'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(vy)))
            elif (variable == 'vz'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(vz)))
            elif (variable == 'press'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(press)))
            elif (variable == 'Bx'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(Bx)))
            elif (variable == 'By'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(By)))
            elif (variable == 'Bz'):
                w.write('%g %g %g %g\n' %(float(x),float(y),float(z),float(Bz)))

# Se cierran ambos archivos
w.close()
f.close()

```

```
# Se utilizan estas 3 lineas para llamar la funcion  
# e ingresar la variable y bloque a salvar desde la terminal  
method_name = sys.argv[1]  
parameter_name = sys.argv[2]  
getattr(sys.modules[__name__], method_name)(parameter_name)
```

Archivos resultantes

```
(base) paula@PaulaCW:~/prom/Graphs_ASCII$ head -25 vz_b15.3D
x y z vz
-0.5 -0.5 0 1e-14
-0.5 -0.48 0 1e-14
-0.5 -0.46 0 1e-14
-0.5 -0.44 0 1.00001e-14
-0.5 -0.42 0 1.00008e-14
-0.5 -0.4 0 1.00041e-14
-0.5 -0.38 0 1.00195e-14
-0.5 -0.36 0 1.00859e-14
-0.5 -0.34 0 1.03482e-14
-0.5 -0.32 0 1.13036e-14
-0.5 -0.3 0 1.45048e-14
-0.5 -0.28 0 2.437e-14
-0.5 -0.26 0 5.23151e-14
-0.5 -0.24 0 1.25024e-13
-0.5 -0.22 0 2.9863e-13
-0.5 -0.2 0 6.78572e-13
-0.5 -0.18 0 1.43959e-12
-0.5 -0.16 0 2.83184e-12
-0.5 -0.14 0 5.15173e-12
-0.5 -0.12 0 8.65852e-12
-0.5 -0.1 0 1.34386e-11
-0.5 -0.08 0 1.92576e-11
-0.5 -0.06 0 2.54771e-11
-0.5 -0.04 0 3.11156e-11
```

Script en bash

```
(base) paula@PaulaCW:~/prom/Graphs_ASCII$ cat myscript.sh
#!/usr/bin/env bash

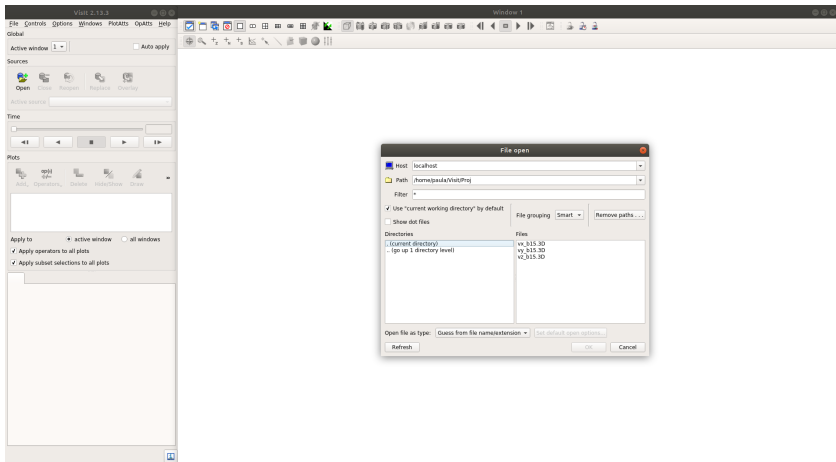
rm *.3D

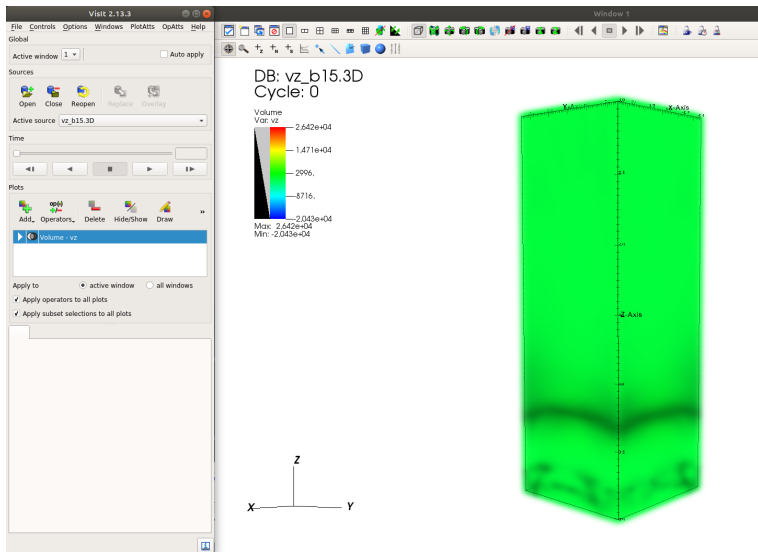
v=${1?Error: Ingrese otra variable}
b=${2?Error: Ingrese otro bloque}

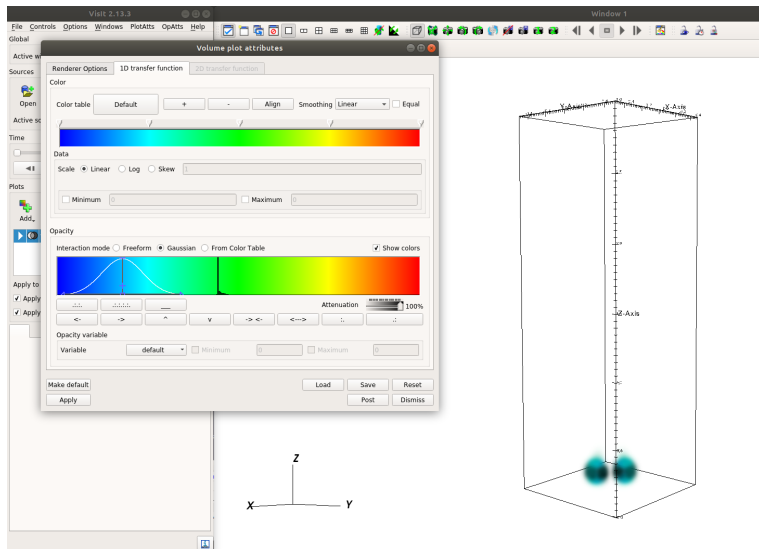
python extractor.py extraer $v-$b

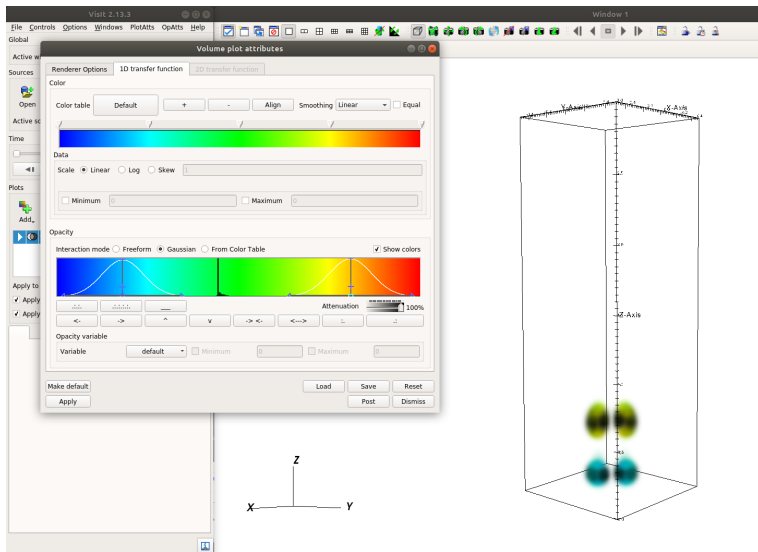
cp *.3D ../../../../../../Visit/Proj/

cd
./visit
```

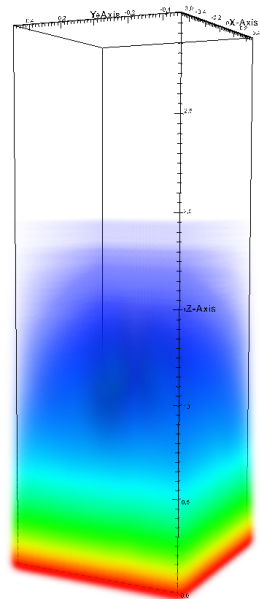
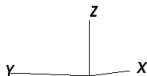
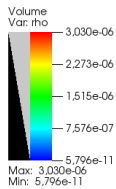




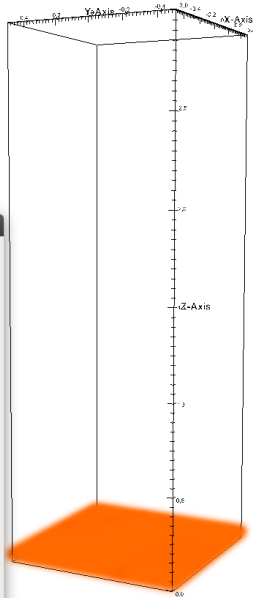
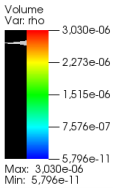




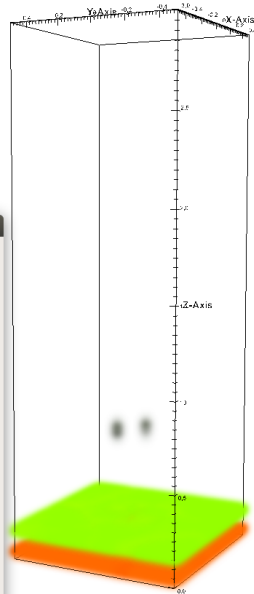
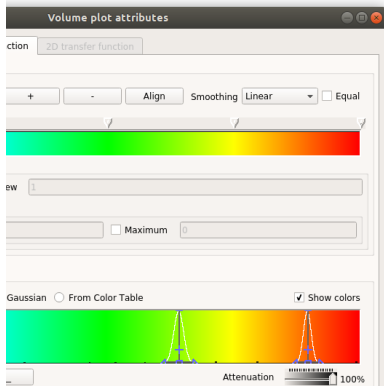
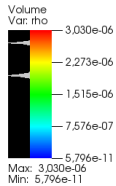
DB: rho_b30.3D
Cycle: 0



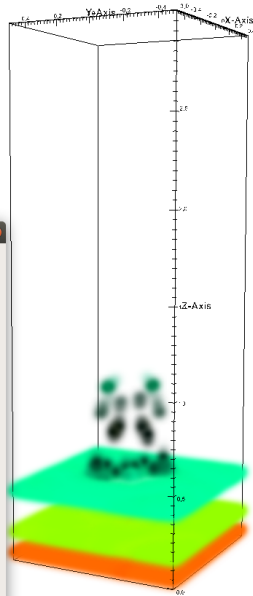
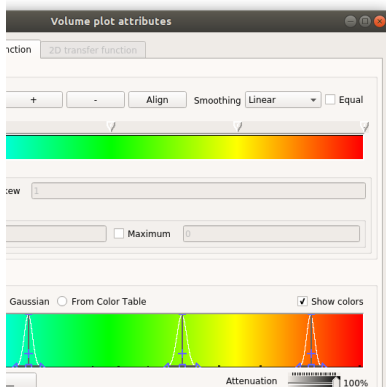
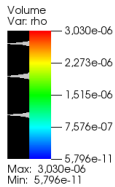
Cycle: $\bar{0}$



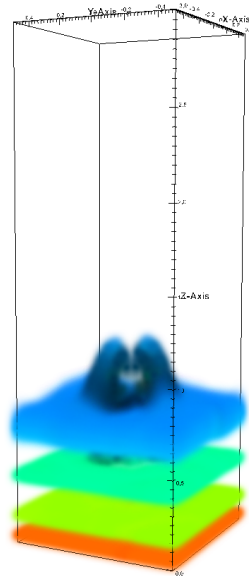
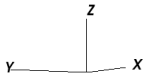
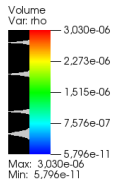
DB: rho_b30.3D
Cycle: 0



DB: rho_b30.3D
Cycle: 0



DB: rho_b30.3D
Cycle: 0



- ❶ Página oficial de VisIt
- ❷ Convertidor de ASCII a HDF5
- ❸ Generador de archivos en formato permitido

¡GRACIAS!