

P8130 Final Project

Abstract

Introduction (brief context and background of the problem)

Methods (data description and statistical methods)

Results

Conclusions/Discussion

```
# import necessary datasets
library(tidyverse)
library(ggplot2)
library(GGally)
library(PerformanceAnalytics)
library(performance)
library(MASS)
```

Read in dataset

```
cdi = read_csv("./cdi.csv") %>%
  janitor::clean_names()

## no missing value
cdi %>%
  dplyr::select(everything()) %>%
  summarise_all(funs(sum(is.na(.)))) %>%
  knitr::kable()
```

id	cty	state	area	pop	pop18	pop65	docs	beds	crimes	hsgrad	bagrad	poverty	unemp	pcincometotal	inc	region
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Data cleaning

First, some normalization for better comparison

```
cdi =
  cdi %>%
  mutate(crm_1000 = crimes/pop*1000, # as indicated by the project prompt
         docs_1000 = docs/pop*1000, # every 1000 people how many doctors
         beds_1000 = beds/pop*1000, # similar as above
         pop_density = pop/area, # how many people per square miles
         northeast = ifelse(region == 1, 1, 0), # region as dummy variable
         northcentral = ifelse(region == 2, 1, 0),
         south = ifelse(region == 3, 1, 0)) %>%
  dplyr::select(-id, -crimes, -area, -docs, -beds, -totalinc, -region)
```

Data Exploration

```
## summary statistics, tentative, NOT FINAL
```

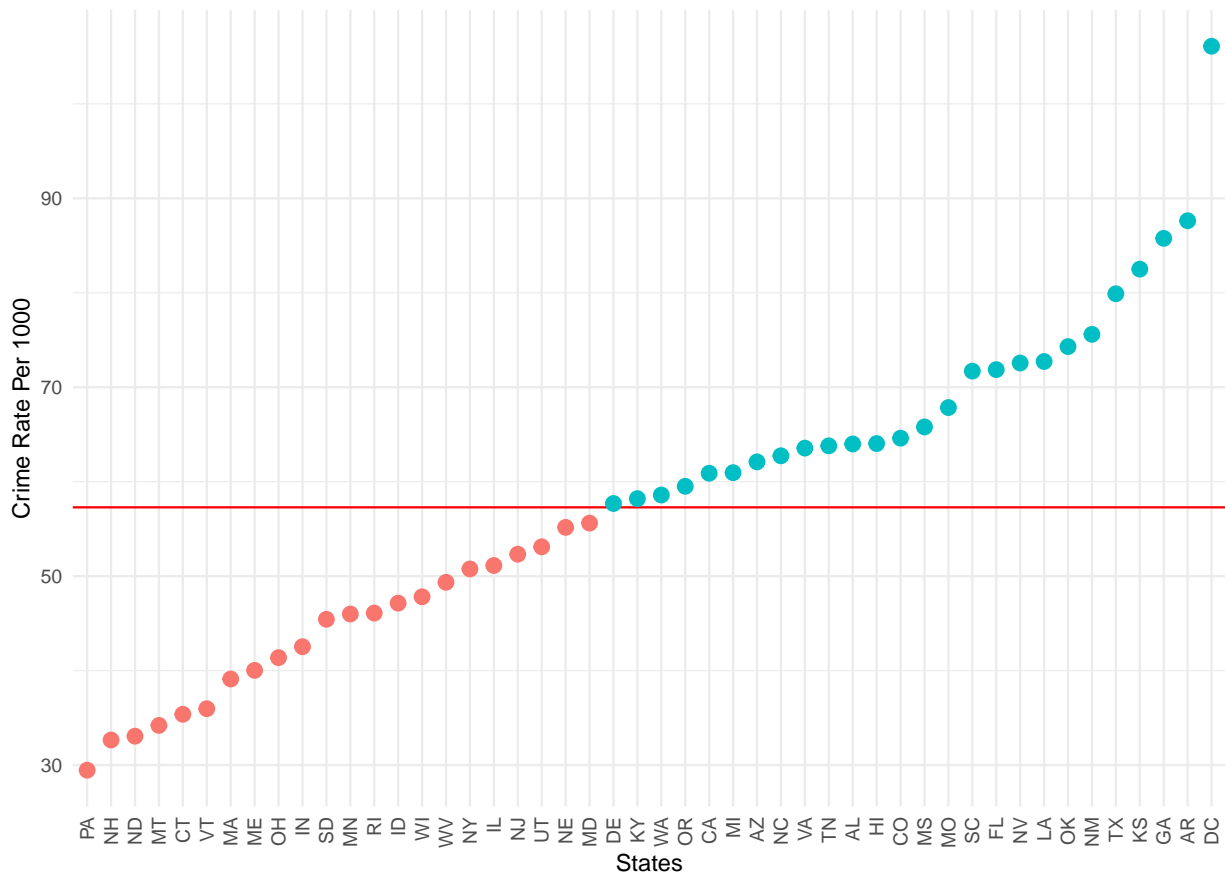
```
sum_cdi =
  cdi %>%
  dplyr::select(-c(cty, state))
summary(sum_cdi)
```

```
##      pop      pop18      pop65      hsgrad
## Min.   : 100043   Min.   :16.40   Min.   : 3.000   Min.   :46.60
## 1st Qu.: 139027   1st Qu.:26.20   1st Qu.: 9.875   1st Qu.:73.88
## Median : 217280   Median :28.10   Median :11.750   Median :77.70
## Mean   : 393011   Mean   :28.57   Mean   :12.170   Mean   :77.56
## 3rd Qu.: 436064   3rd Qu.:30.02   3rd Qu.:13.625   3rd Qu.:82.40
## Max.   :8863164   Max.   :49.70   Max.   :33.800   Max.   :92.90
##      bagrad      poverty      unemp      pcincome
## Min.   : 8.10   Min.   : 1.400   Min.   : 2.200   Min.   : 8899
## 1st Qu.:15.28   1st Qu.: 5.300   1st Qu.: 5.100   1st Qu.:16118
## Median :19.70   Median : 7.900   Median : 6.200   Median :17759
## Mean   :21.08   Mean   : 8.721   Mean   : 6.597   Mean   :18561
## 3rd Qu.:25.32   3rd Qu.:10.900   3rd Qu.: 7.500   3rd Qu.:20270
## Max.   :52.30   Max.   :36.300   Max.   :21.300   Max.   :37541
##      crm_1000      docs_1000      beds_1000      pop_density
## Min.   : 4.601   Min.   : 0.3559   Min.   : 0.1649   Min.   : 13.26
## 1st Qu.: 38.102   1st Qu.: 1.2127   1st Qu.: 2.1972   1st Qu.: 192.34
## Median : 52.429   Median : 1.7509   Median : 3.3287   Median : 335.91
## Mean   : 57.286   Mean   : 2.1230   Mean   : 3.6493   Mean   : 888.44
## 3rd Qu.: 72.597   3rd Qu.: 2.4915   3rd Qu.: 4.5649   3rd Qu.: 756.55
## Max.   :295.987   Max.   :17.0377   Max.   :19.6982   Max.   :32403.72
##      northeast      northcentral      south
## Min.   :0.0000   Min.   :0.0000   Min.   :0.0000
## 1st Qu.:0.0000   1st Qu.:0.0000   1st Qu.:0.0000
## Median :0.0000   Median :0.0000   Median :0.0000
## Mean   :0.2341   Mean   :0.2455   Mean   :0.3455
## 3rd Qu.:0.0000   3rd Qu.:0.0000   3rd Qu.:1.0000
## Max.   :1.0000   Max.   :1.0000   Max.   :1.0000
```

```
mean_crm = mean(sum_cdi$crm_1000)
cdi_state = cdi %>%
  group_by(state) %>%
  summarize(crime_rate = mean(crm_1000)) %>%
  mutate(low_high = ifelse(crime_rate>mean_crm, TRUE,FALSE))
```

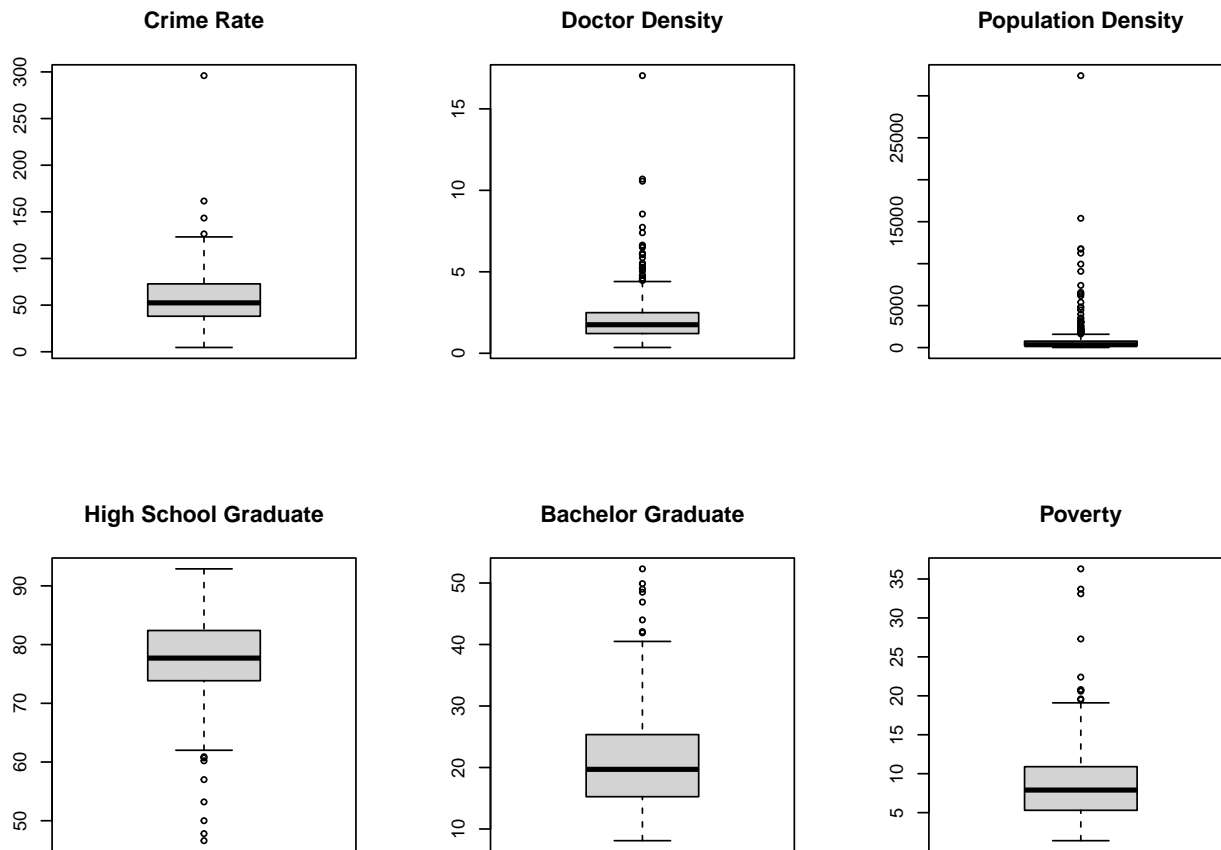
```
cdi_state %>%
  mutate(state = fct_reorder(state, crime_rate)) %>%
  ggplot(aes(x = state, y = crime_rate))+
  geom_hline(yintercept = mean_crm, color = "red")+
  geom_point(aes(color = low_high),size = 3)+
  ggtitle("Crime Rates in the US States") +
  labs(y = "Crime Rate Per 1000", x = "States") +
  theme(plot.title = element_text(hjust = 0.5),
        axis.text.x = element_text(angle = 90, vjust = 0.5, hjust= 1),
        legend.position = "none")
```

Crime Rates in the US States

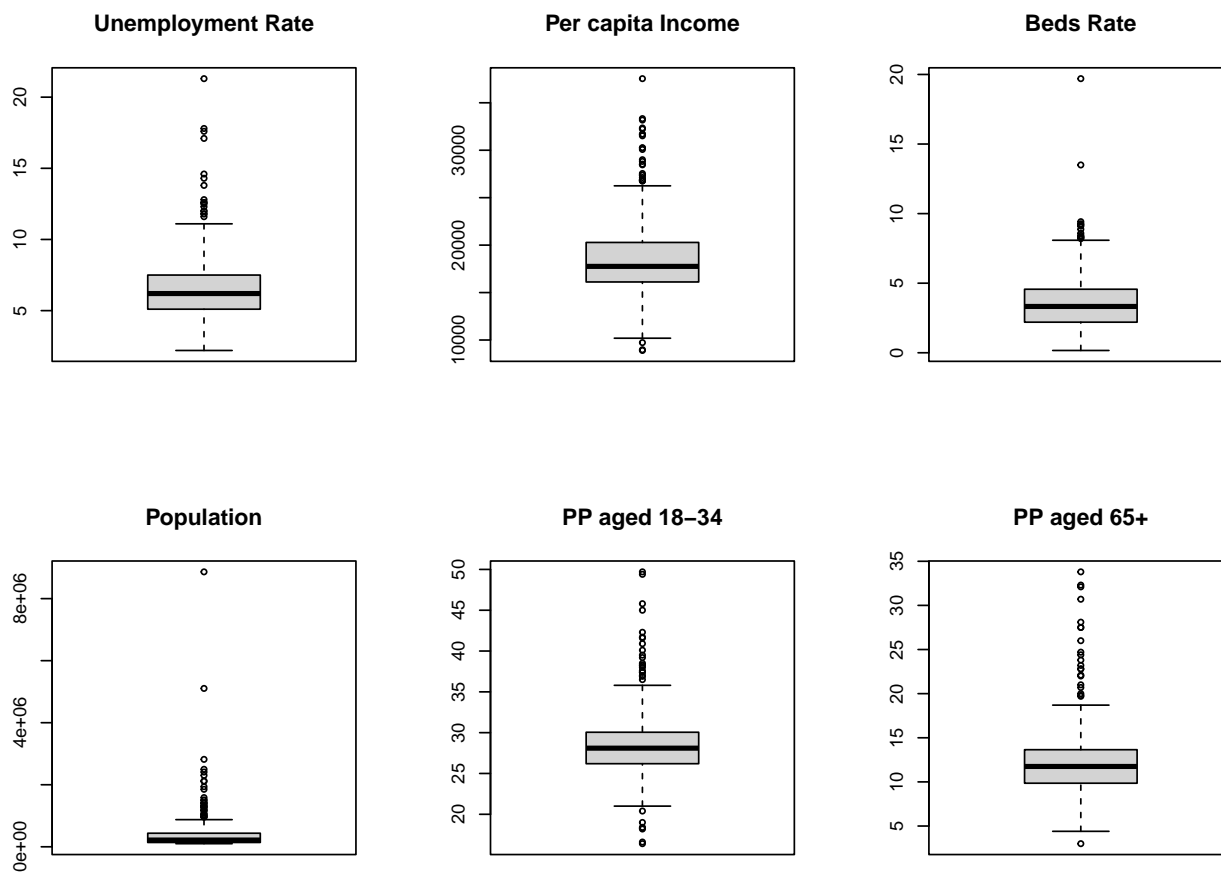


boxplot for each variable

```
par(mfrow=c(2,3))
boxplot(sum_cdi$crm_1000, main='Crime Rate')
boxplot(sum_cdi$docs_1000, main='Doctor Density')
boxplot(sum_cdi$pop_density, main='Population Density' )
boxplot(sum_cdi$hsgrad, main='High School Graduate')
boxplot(sum_cdi$bagrads, main='Bachelor Graduate')
boxplot(sum_cdi$poverty, main='Poverty')
```

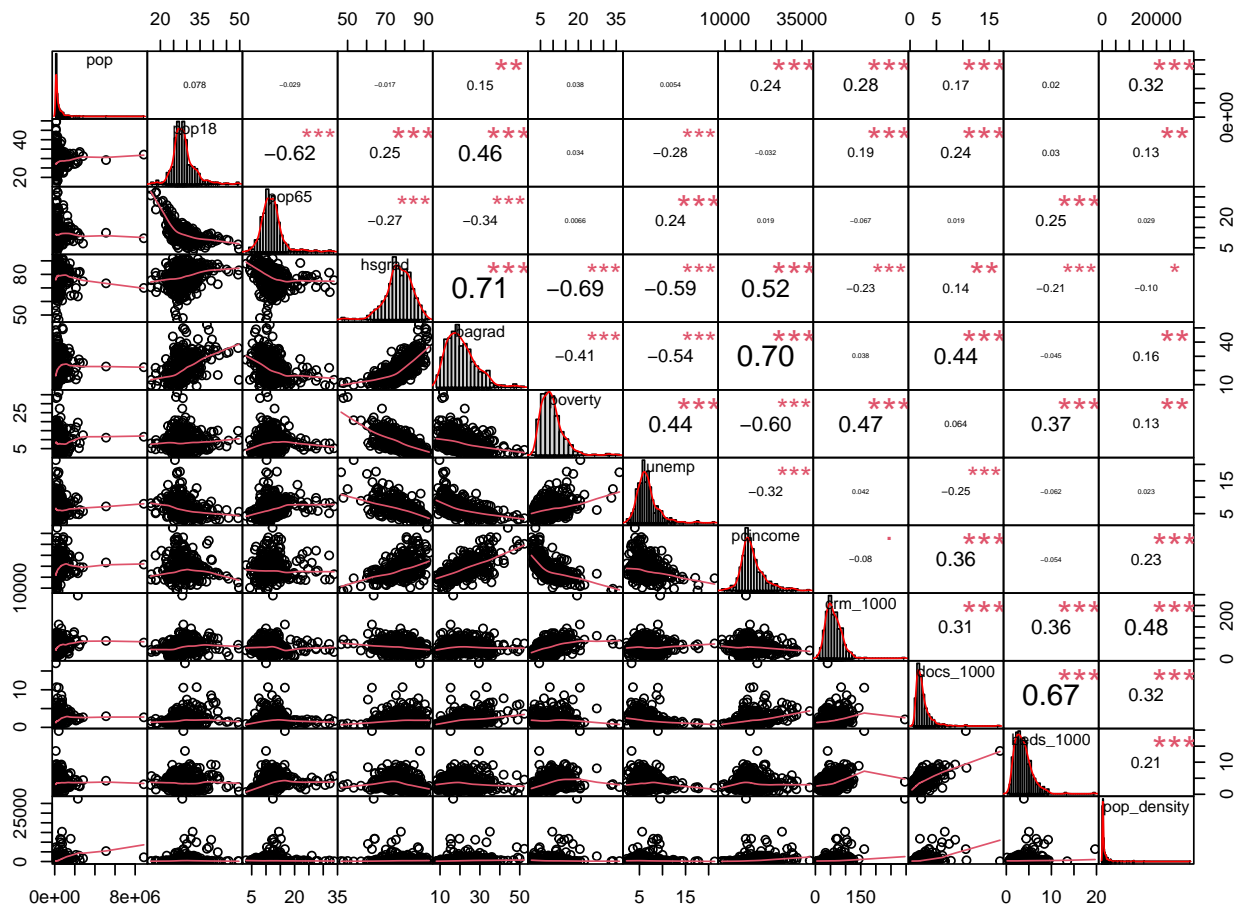


```
par(mfrow=c(2,3))
boxplot(sum_cdi$unemp, main='Unemployment Rate')
boxplot(sum_cdi$pcincome, main='Per capita Income')
boxplot(sum_cdi$beds_1000, main='Beds Rate')
boxplot(sum_cdi$pop, main='Population')
boxplot(sum_cdi$pop18, main='PP aged 18-34')
boxplot(sum_cdi$pop65, main='PP aged 65+')
```



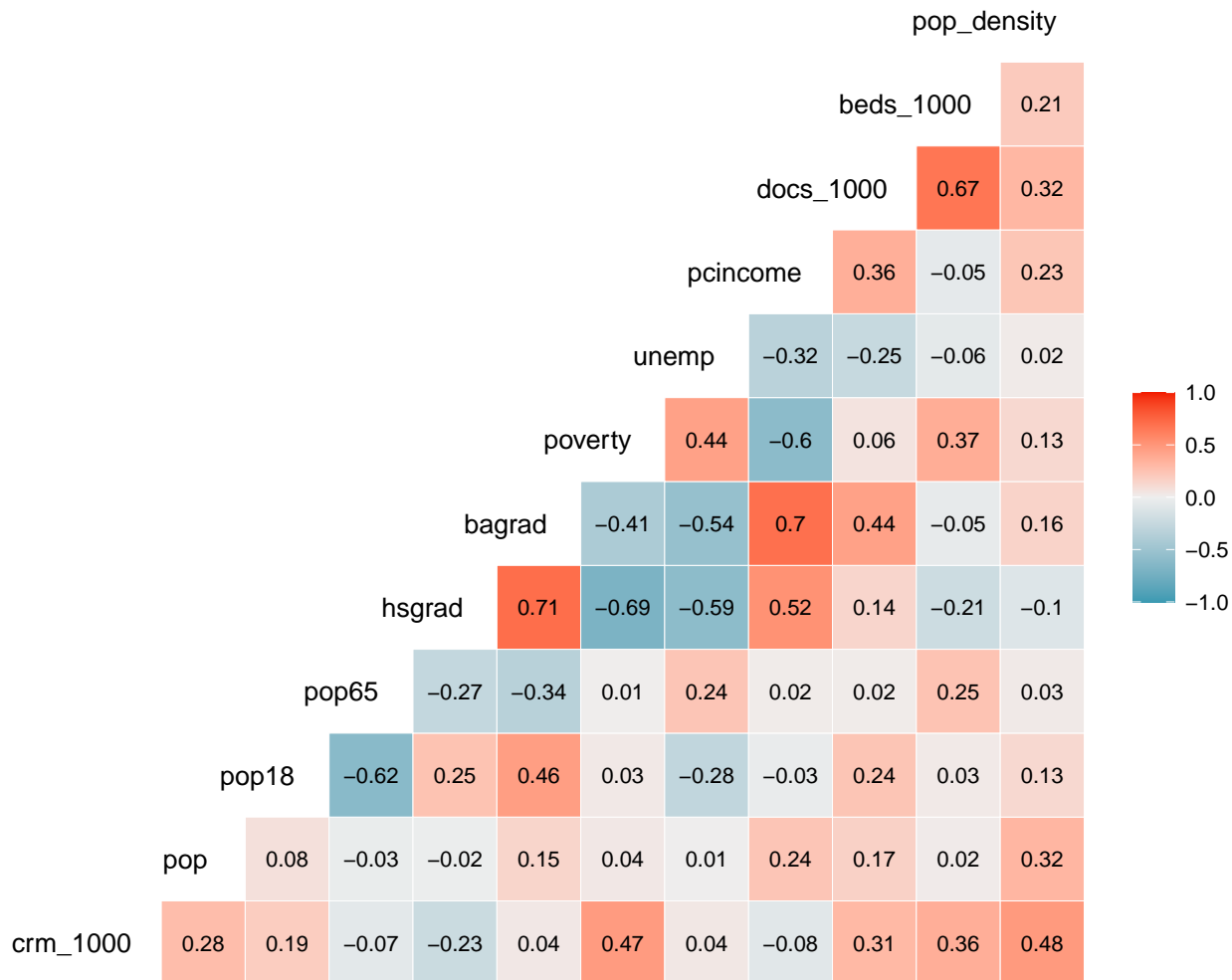
Marginal Correlation and Correlation matrix

```
corr_matrix =
  cdi %>%
  dplyr::select(-state, -cty, -northeast, -northcentral, -south) %>%
  chart.Correlation(histogram = TRUE, method = "pearson")
```



Correlation Heatmap

```
cdi %>%
  dplyr::select(-state, -cty, -northeast, -northcentral, -south) %>%
  dplyr::select(crm_1000, everything()) %>%
  ggcorr(label=TRUE, hjust = 0.9, layout.exp = 2, label_size = 3, label_round = 2)
```



Build

Model ### Full Model Let's start with the full model

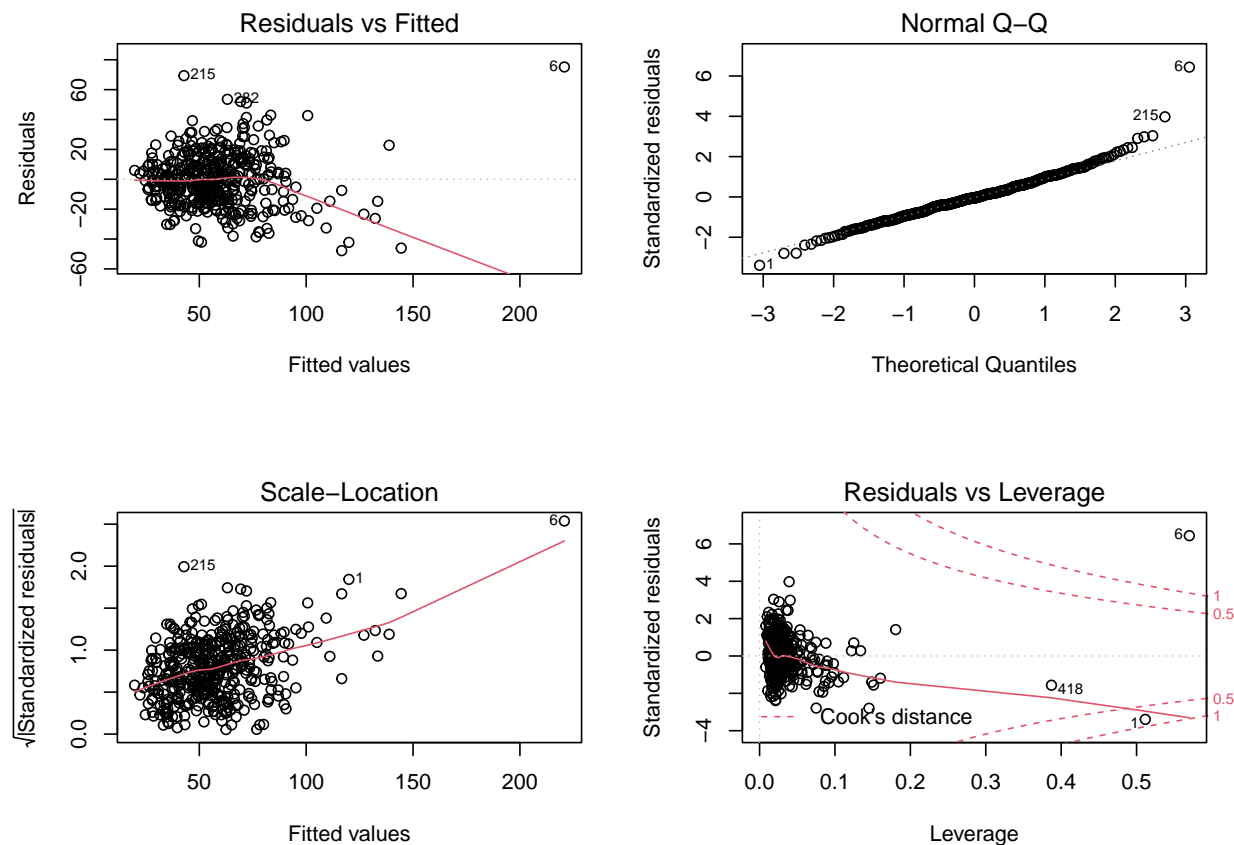
```
mult_fit = lm(crm_1000 ~ ., data = sum_cdi)
summary(mult_fit)
```

```
##
## Call:
## lm(formula = crm_1000 ~ ., data = sum_cdi)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -47.786 -11.422  -0.934  10.200  75.180
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -4.805e+01  2.770e+01  -1.734  0.083592 .
## pop          5.486e-06  1.579e-06   3.474  0.000566 ***
## pop18        6.947e-01  3.305e-01   2.102  0.036150 *
## pop65       -1.998e-01  3.055e-01  -0.654  0.513410
## hsgrad       6.143e-01  2.690e-01   2.284  0.022864 *
## bagrad      -4.835e-01  2.971e-01  -1.628  0.104327
## poverty     1.856e+00  3.864e-01   4.803  2.17e-06 ***
## unemp       6.111e-01  5.314e-01   1.150  0.250812
## pcincome    1.039e-03  4.734e-04   2.195  0.028670 *
## docs_1000   -6.634e-01  1.019e+00  -0.651  0.515556
## beds_1000    3.157e+00  7.939e-01   3.977  8.21e-05 ***
## pop_density  4.901e-03  4.537e-04  10.802  < 2e-16 ***
```

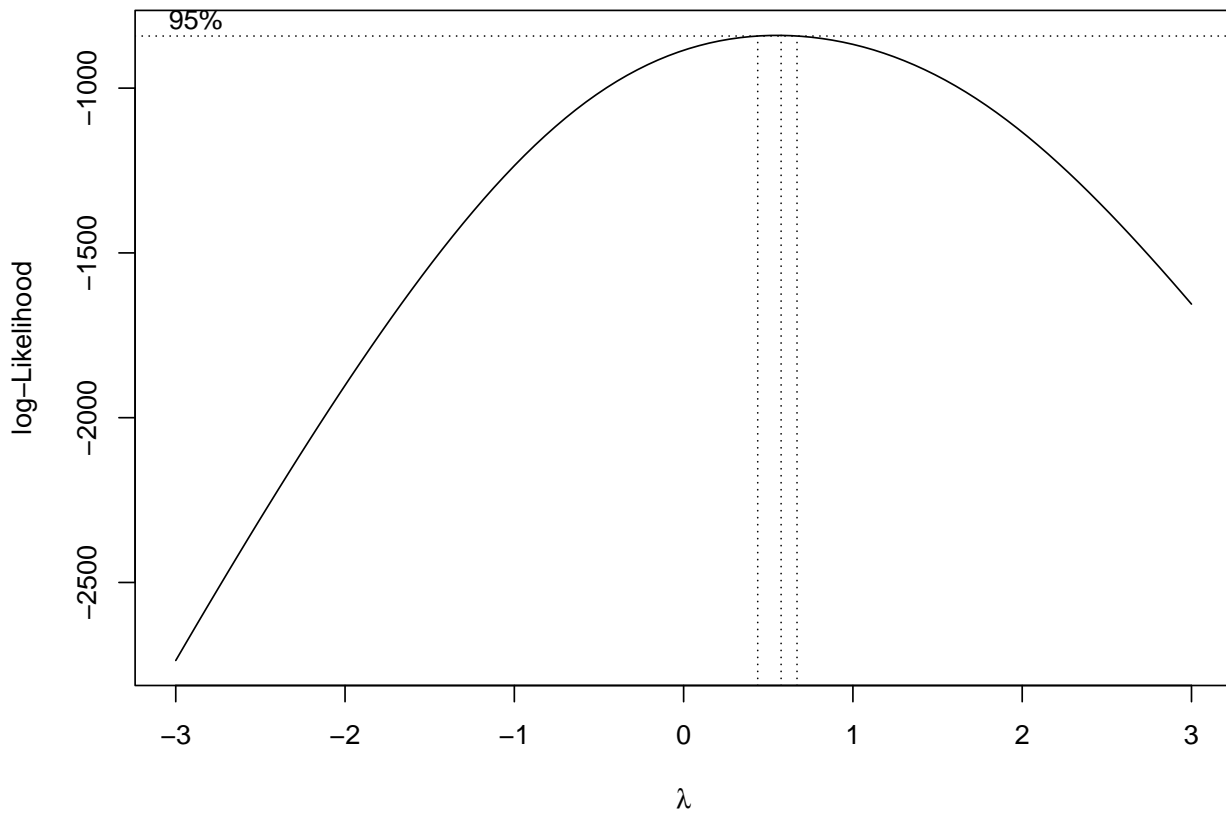
```
## northeast    -2.118e+01  3.125e+00 -6.778 4.09e-11 ***
## northcentral -1.220e+01  2.984e+00 -4.089 5.18e-05 ***
## south        6.614e+00  2.863e+00  2.310 0.021353 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 17.81 on 425 degrees of freedom
## Multiple R-squared:  0.589, Adjusted R-squared:  0.5755
## F-statistic: 43.51 on 14 and 425 DF, p-value: < 2.2e-16
```

Model diagnostics of the full model

```
par(mfrow=c(2,2))
plot(mult_fit)
```



```
# get the lambda for the transformation
bc_model = boxcox(mult_fit, lambda = seq(-3, 3, by = 0.25))
```

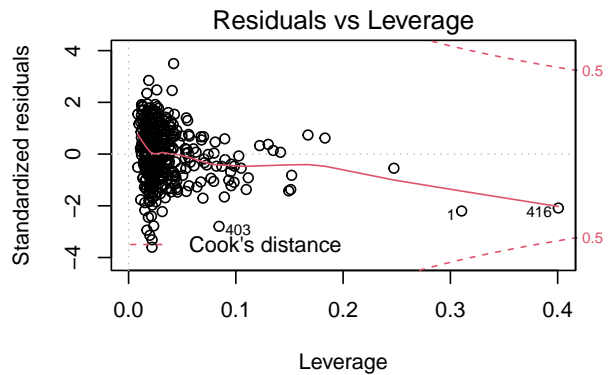
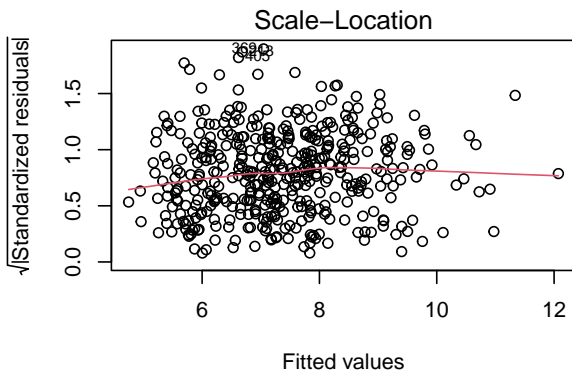
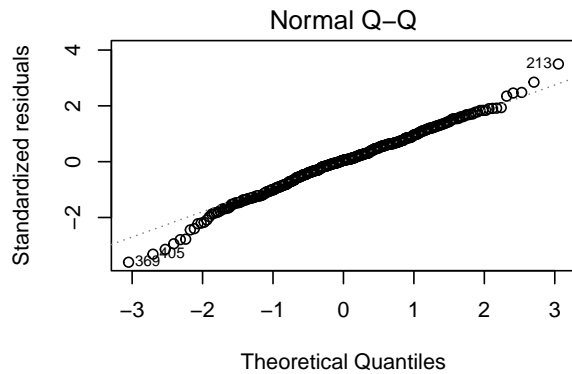
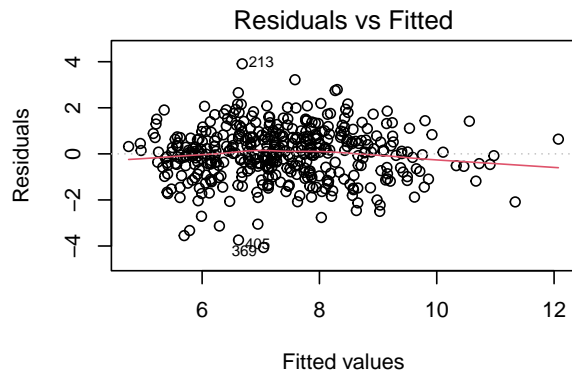
```
lamb = bc_model$x[which.max(bc_model$y)]
lamb
```

```
## [1] 0.5757576
```

~0.5, thus we applied square root to the Y. Also we get rid of the influential points. The full model is the basis of other models, thus we choose to filter the outliers out at first.

```
sum_cdi_mod = sum_cdi[-c(1,6),] # filter out outlier and store it as the new dataset
full_trans_fit = lm(sqrt(crm_1000) ~.,data = sum_cdi_mod) # refit
```

```
# check again
par(mfrow=c(2,2))
plot(full_trans_fit)
```



```
summary(full_trans_fit)
```

```
##
## Call:
## lm(formula = sqrt(crm_1000) ~ ., data = sum_cdi_mod)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.0654 -0.6625  0.0540  0.7183  3.9085
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  7.644e-02  1.786e+00   0.043  0.965879
## pop          7.281e-07  1.425e-07   5.111  4.87e-07 ***
## pop18       7.584e-02  2.159e-02   3.513  0.000491 ***
## pop65      -2.316e-04  1.965e-02  -0.012  0.990601
## hsgrad      2.583e-02  1.733e-02   1.491  0.136820
## bagrad     -3.462e-02  1.911e-02  -1.812  0.070658 .
## poverty     1.111e-01  2.492e-02   4.457  1.07e-05 ***
## unemp       4.736e-02  3.407e-02   1.390  0.165214
## pcincome    1.058e-04  3.141e-05   3.367  0.000828 ***
## docs_1000   -2.102e-02  6.581e-02  -0.319  0.749576
## beds_1000   2.286e-01  5.101e-02   4.481  9.59e-06 ***
## pop_density  8.083e-05  4.359e-05   1.854  0.064417 .
## northeast  -1.719e+00  2.008e-01  -8.565 < 2e-16 ***
## northcentral -9.851e-01  1.912e-01  -5.151  3.97e-07 ***
## south       3.042e-01  1.835e-01   1.658  0.098155 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.141 on 423 degrees of freedom
```

```
## Multiple R-squared:  0.551, Adjusted R-squared:  0.5361
## F-statistic: 37.08 on 14 and 423 DF,  p-value: < 2.2e-16
check_collinearity(full_trans_fit)
```

```
## # Check for Multicollinearity
##
## Low Correlation
##
##      Term  VIF Increased SE Tolerance
##      pop  1.00      1.00      1.00
##      pop18 2.65      1.63      0.38
##      pop65 2.07      1.44      0.48
##      hsgrad 3.28      1.81      0.31
##      bagrad 3.74      1.93      0.27
##      poverty 2.43      1.56      0.41
##      unemp  1.89      1.37      0.53
##      pcincome 1.02      1.01      0.98
##      docs_1000 2.62      1.62      0.38
##      beds_1000 3.16      1.78      0.32
##      pop_density 1.01      1.01      0.99
##      northeast 2.21      1.49      0.45
##      northcentral 2.28      1.51      0.44
##      south 2.46      1.57      0.41
```

We will just use the transformed models for the further model fits

Backward Elimination

```
multi_back = step(full_trans_fit, direction='backward')
```

```
## Start:  AIC=130.27
## sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad + bagrad + poverty +
##      unemp + pcincome + docs_1000 + beds_1000 + pop_density +
##      northeast + northcentral + south
##
##      Df Sum of Sq  RSS  AIC
## - pop65      1    0.000 550.67 128.27
## - docs_1000   1    0.133 550.81 128.37
## - unemp       1    2.516 553.19 130.26
## <none>                550.67 130.27
## - hsgrad      1    2.892 553.56 130.56
## - south       1    3.577 554.25 131.10
## - bagrad      1    4.275 554.95 131.66
## - pop_density 1    4.475 555.15 131.81
## - pcincome    1   14.762 565.43 139.85
## - pop18       1   16.064 566.74 140.86
## - poverty     1   25.858 576.53 148.37
## - beds_1000   1   26.137 576.81 148.58
## - pop         1   34.004 584.68 154.51
## - northcentral 1   34.547 585.22 154.92
## - northeast   1   95.493 646.17 198.31
##
## Step:  AIC=128.27
## sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp +
##      pcincome + docs_1000 + beds_1000 + pop_density + northeast +
##      northcentral + south
##
##      Df Sum of Sq  RSS  AIC
```

```
## - docs_1000      1      0.133 550.81 126.37
## <none>              550.67 128.27
## - unemp          1      2.550 553.22 128.29
## - hsgrad         1      2.903 553.58 128.57
## - south          1      3.583 554.26 129.11
## - bagrad         1      4.277 554.95 129.66
## - pop_density    1      4.515 555.19 129.84
## - pcincome       1     14.879 565.55 137.94
## - pop18          1     21.617 572.29 143.13
## - poverty        1     27.010 577.68 147.24
## - beds_1000      1     28.382 579.05 148.28
## - pop            1     34.067 584.74 152.56
## - northcentral   1     34.747 585.42 153.07
## - northeast      1     96.401 647.07 196.93
##
## Step:  AIC=126.37
## sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp +
##      pcincome + beds_1000 + pop_density + northeast + northcentral +
##      south
##
##              Df Sum of Sq    RSS    AIC
## <none>              550.81 126.37
## - unemp            1      2.533 553.34 126.38
## - hsgrad           1      3.010 553.82 126.76
## - south            1      3.944 554.75 127.50
## - pop_density      1      4.387 555.19 127.85
## - bagrad           1      4.988 555.79 128.32
## - pcincome         1     14.747 565.55 135.94
## - pop18            1     21.486 572.29 141.13
## - poverty          1     27.234 578.04 145.51
## - pop              1     33.948 584.75 150.57
## - northcentral     1     35.244 586.05 151.54
## - beds_1000        1     52.476 603.28 164.23
## - northeast        1     97.351 648.16 195.66
```

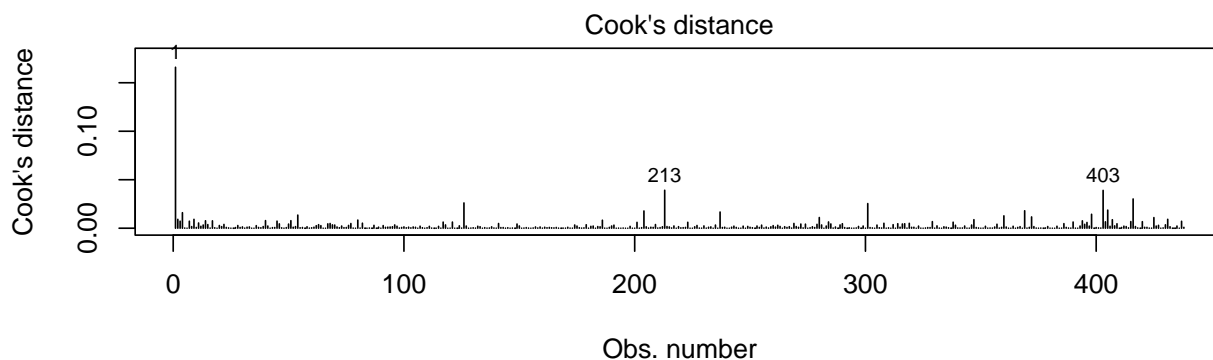
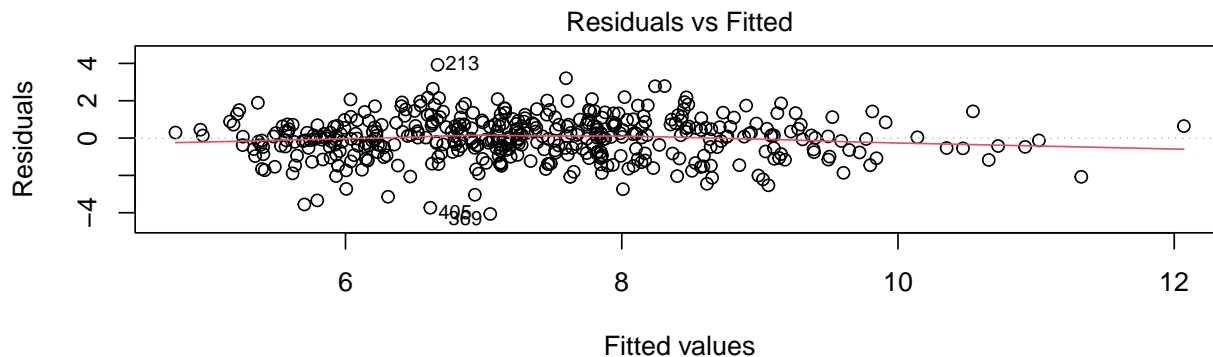
multi_back

```
##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
##      poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
##      northcentral + south, data = sum_cdi_mod)
##
## Coefficients:
## (Intercept)      pop      pop18      hsgrad      bagrad
##  9.096e-02    7.261e-07    7.546e-02    2.624e-02   -3.617e-02
##  poverty      unemp    pcincome    beds_1000    pop_density
##  1.115e-01    4.714e-02    1.048e-04    2.172e-01    7.880e-05
##  northeast  northcentral      south
## -1.711e+00  -9.731e-01    3.142e-01
```

```
sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp + pcincome + beds_1000 + pop_density +
northeast + northcentral + south, data = sum_cdi
```

Model Diagnostic

```
par(mfrow = c(2,1))
plot(multi_back, which = 1)
plot(multi_back, which = 4)
```



get rid of the outliers first

```
back_without = sum_cdi[-c(1),]
```

```
with_back = lm(sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp+
  pcincome + beds_1000 + pop_density + northeast + northcentral +
  south, data = sum_cdi)
```

```
without_back = lm(sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp+
  pcincome + beds_1000 + pop_density + northeast + northcentral +
  south, data = back_without)
```

```
summary(with_back); summary(without_back)
```

```
##
```

```
## Call:
```

```
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
##   poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
##   northcentral + south, data = sum_cdi)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max
## -4.0525 -0.7474  0.0681  0.7419  4.0605
```

```
##
```

```
## Coefficients:
```

```
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.607e-02  1.705e+00  -0.021  0.983127
## pop          3.602e-07  1.036e-07   3.476  0.000560 ***
## pop18        6.399e-02  1.869e-02   3.423  0.000679 ***
## hsgrad       3.579e-02  1.757e-02   2.037  0.042260 *
## bagrad      -3.749e-02  1.890e-02  -1.984  0.047915 *
## poverty      1.207e-01  2.483e-02   4.859  1.66e-06 ***
## unemp        4.193e-02  3.461e-02   1.211  0.226387
## pcincome     9.396e-05  3.076e-05   3.055  0.002393 **
```

```

## beds_1000      1.886e-01  3.441e-02  5.483 7.17e-08 ***
## pop_density    2.129e-04  2.957e-05  7.201 2.72e-12 ***
## northeast     -1.659e+00  2.020e-01 -8.215 2.56e-15 ***
## northcentral  -9.426e-01  1.914e-01 -4.924 1.22e-06 ***
## south         3.399e-01  1.848e-01  1.839 0.066567 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.169 on 427 degrees of freedom
## Multiple R-squared:  0.5598, Adjusted R-squared:  0.5474
## F-statistic: 45.25 on 12 and 427 DF,  p-value: < 2.2e-16

##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
##     poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
##     northcentral + south, data = back_without)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.0005 -0.7447  0.0672  0.7078  4.1414
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  4.092e-01  1.688e+00   0.242 0.808582
## pop          7.111e-07  1.438e-07   4.946 1.09e-06 ***
## pop18       6.304e-02  1.846e-02   3.415 0.000699 ***
## hsgrad      3.219e-02  1.738e-02   1.852 0.064654 .
## bagrad     -3.406e-02  1.868e-02  -1.823 0.068985 .
## poverty     1.115e-01  2.466e-02   4.521 7.99e-06 ***
## unemp       4.435e-02  3.418e-02   1.298 0.195111
## pcincome    7.916e-05  3.066e-05   2.582 0.010163 *
## beds_1000   1.945e-01  3.401e-02   5.720 2.01e-08 ***
## pop_density  1.901e-04  2.992e-05   6.353 5.42e-10 ***
## northeast  -1.653e+00  1.994e-01  -8.289 1.51e-15 ***
## northcentral -9.442e-01  1.890e-01  -4.995 8.58e-07 ***
## south       3.410e-01  1.824e-01   1.869 0.062316 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.154 on 426 degrees of freedom
## Multiple R-squared:  0.5712, Adjusted R-squared:  0.5592
## F-statistic: 47.3 on 12 and 426 DF,  p-value: < 2.2e-16
check_collinearity(without_back)

## # Check for Multicollinearity
##
## Low Correlation
##
##      Term  VIF Increased SE Tolerance
##      pop  1.00      1.00      1.00
##      pop18 1.93      1.39      0.52
##      hsgrad 3.28      1.81      0.31
##      bagrad 3.50      1.87      0.29
##      poverty 2.39      1.55      0.42
##      unemp  1.86      1.36      0.54
##      pcincome 1.03      1.01      0.98
##      beds_1000 1.45      1.20      0.69

```

```
##   pop_density 1.00          1.00          1.00
##   northeast 2.14          1.46          0.47
##  northcentral 2.18          1.48          0.46
##           south 2.39          1.55          0.42
```

Forward Selection

```
multi_forward = step(full_trans_fit, direction = 'forward')
```

```
## Start:  AIC=130.27
## sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad + bagrad + poverty +
##   unemp + pcincome + docs_1000 + beds_1000 + pop_density +
##   northeast + northcentral + south
```

```
multi_forward
```

```
##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad +
##   bagrad + poverty + unemp + pcincome + docs_1000 + beds_1000 +
##   pop_density + northeast + northcentral + south, data = sum_cdi_mod)
##
```

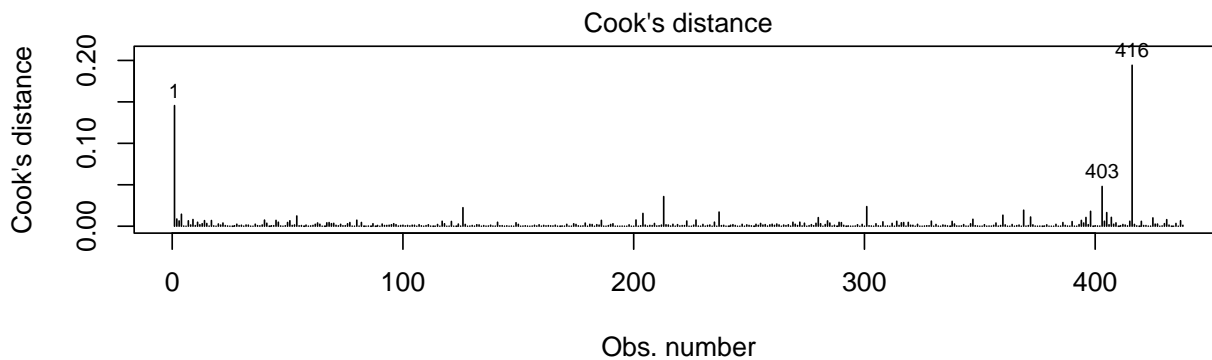
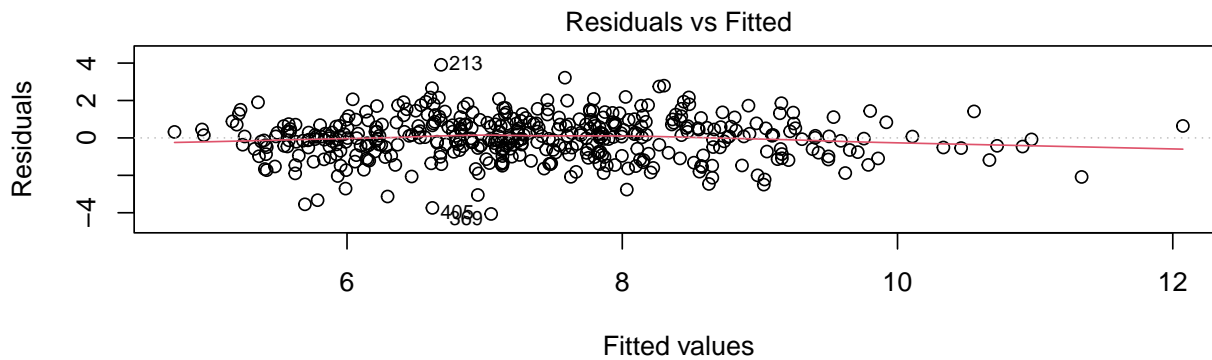
```
## Coefficients:
```

```
## (Intercept)          pop          pop18          pop65          hsgrad
##  7.644e-02      7.281e-07      7.584e-02     -2.316e-04      2.583e-02
##      bagrad      poverty      unemp      pcincome      docs_1000
## -3.462e-02      1.111e-01      4.736e-02      1.058e-04     -2.102e-02
##   beds_1000  pop_density  northeast  northcentral          south
##  2.286e-01      8.083e-05     -1.719e+00     -9.851e-01      3.042e-01
```

```
sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad + bagrad + poverty + unemp + pcincome + docs_1000 +
beds_1000 + pop_density + northeast + northcentral + south, data = sum_cdi_mod
```

Model diagnostic

```
par(mfrow = c(2,1))
plot(multi_forward, which = 1)
plot(multi_forward, which = 4)
```



```
forward_without = sum_cdi[-c(1,416),]
with_for = lm(sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad +
  bagrad + poverty + unemp + pcincome + docs_1000 + beds_1000 +
  pop_density + northeast + northcentral + south, data = sum_cdi_mod)
without_for = lm(sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad +
  bagrad + poverty + unemp + pcincome + docs_1000 + beds_1000 +
  pop_density + northeast + northcentral + south, data = forward_without)
summary(with_for); summary(without_for)
```

```
##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad +
##   bagrad + poverty + unemp + pcincome + docs_1000 + beds_1000 +
##   pop_density + northeast + northcentral + south, data = sum_cdi_mod)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.0654 -0.6625  0.0540  0.7183  3.9085
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  7.644e-02  1.786e+00   0.043  0.965879
## pop          7.281e-07  1.425e-07   5.111  4.87e-07 ***
## pop18        7.584e-02  2.159e-02   3.513  0.000491 ***
## pop65       -2.316e-04  1.965e-02  -0.012  0.990601
## hsgrad       2.583e-02  1.733e-02   1.491  0.136820
## bagrad      -3.462e-02  1.911e-02  -1.812  0.070658 .
## poverty      1.111e-01  2.492e-02   4.457  1.07e-05 ***
## unemp        4.736e-02  3.407e-02   1.390  0.165214
## pcincome     1.058e-04  3.141e-05   3.367  0.000828 ***
## docs_1000   -2.102e-02  6.581e-02  -0.319  0.749576
```



```

## beds_1000      2.286e-01  5.101e-02  4.481 9.59e-06 ***
## pop_density    8.083e-05  4.359e-05  1.854 0.064417 .
## northeast     -1.719e+00  2.008e-01  -8.565 < 2e-16 ***
## northcentral  -9.851e-01  1.912e-01  -5.151 3.97e-07 ***
## south         3.042e-01  1.835e-01  1.658 0.098155 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.141 on 423 degrees of freedom
## Multiple R-squared:  0.551, Adjusted R-squared:  0.5361
## F-statistic: 37.08 on 14 and 423 DF,  p-value: < 2.2e-16

##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad +
##     bagrad + poverty + unemp + pcincome + docs_1000 + beds_1000 +
##     pop_density + northeast + northcentral + south, data = forward_without)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.9836 -0.7387  0.0681  0.7275  4.1006
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  5.096e-01  1.807e+00   0.282  0.77810
## pop          7.197e-07  1.445e-07   4.981 9.25e-07 ***
## pop18        6.204e-02  2.154e-02   2.881  0.00417 **
## pop65       -5.352e-03  1.989e-02  -0.269  0.78798
## hsgrad       3.100e-02  1.752e-02   1.770  0.07747 .
## bagrad      -3.114e-02  1.937e-02  -1.608  0.10860
## poverty     1.088e-01  2.528e-02   4.303 2.10e-05 ***
## unemp       4.639e-02  3.455e-02   1.343  0.18009
## pcincome     8.118e-05  3.105e-05   2.614  0.00926 **
## docs_1000   -4.578e-02  6.636e-02  -0.690  0.49065
## beds_1000   2.239e-01  5.172e-02   4.329 1.87e-05 ***
## pop_density  1.926e-04  3.017e-05   6.384 4.56e-10 ***
## northeast  -1.671e+00  2.031e-01  -8.227 2.40e-15 ***
## northcentral -9.769e-01  1.939e-01  -5.037 7.00e-07 ***
## south       3.169e-01  1.862e-01   1.702  0.08948 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.157 on 423 degrees of freedom
## Multiple R-squared:  0.5718, Adjusted R-squared:  0.5576
## F-statistic: 40.34 on 14 and 423 DF,  p-value: < 2.2e-16

check_collinearity(without_for)

## # Check for Multicollinearity
##
## Low Correlation
##
##      Term  VIF Increased SE Tolerance
##      pop  1.00      1.00      1.00
##      pop18 2.61      1.62      0.38
##      pop65 2.06      1.43      0.49
##      hsgrad 3.31      1.82      0.30
##      bagrad 3.73      1.93      0.27
##      poverty 2.49      1.58      0.40

```

```
##          unemp 1.89          1.37          0.53
##          pcincome 1.02          1.01          0.98
##          docs_1000 2.76          1.66          0.36
##          beds_1000 3.32          1.82          0.30
##          pop_density 1.00          1.00          1.00
##          northeast 2.21          1.49          0.45
##          northcentral 2.28          1.51          0.44
##          south 2.47          1.57          0.41
```

Both direction

```
multi_both = step(full_trans_fit, direction = "both")
```

```
## Start:  AIC=130.27
## sqrt(crm_1000) ~ pop + pop18 + pop65 + hsgrad + bagrad + poverty +
##          unemp + pcincome + docs_1000 + beds_1000 + pop_density +
##          northeast + northcentral + south
##
##          Df Sum of Sq    RSS    AIC
## - pop65          1      0.000 550.67 128.27
## - docs_1000       1      0.133 550.81 128.37
## - unemp           1      2.516 553.19 130.26
## <none>                        550.67 130.27
## - hsgrad          1      2.892 553.56 130.56
## - south            1      3.577 554.25 131.10
## - bagrad           1      4.275 554.95 131.66
## - pop_density      1      4.475 555.15 131.81
## - pcincome         1     14.762 565.43 139.85
## - pop18            1     16.064 566.74 140.86
## - poverty          1     25.858 576.53 148.37
## - beds_1000        1     26.137 576.81 148.58
## - pop              1     34.004 584.68 154.51
## - northcentral     1     34.547 585.22 154.92
## - northeast        1     95.493 646.17 198.31
##
## Step:  AIC=128.27
## sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp +
##          pcincome + docs_1000 + beds_1000 + pop_density + northeast +
##          northcentral + south
##
##          Df Sum of Sq    RSS    AIC
## - docs_1000       1      0.133 550.81 126.37
## <none>                        550.67 128.27
## - unemp           1      2.550 553.22 128.29
## - hsgrad          1      2.903 553.58 128.57
## - south            1      3.583 554.26 129.11
## - bagrad           1      4.277 554.95 129.66
## - pop_density      1      4.515 555.19 129.84
## + pop65            1      0.000 550.67 130.27
## - pcincome         1     14.879 565.55 137.94
## - pop18            1     21.617 572.29 143.13
## - poverty          1     27.010 577.68 147.24
## - beds_1000        1     28.382 579.05 148.28
## - pop              1     34.067 584.74 152.56
## - northcentral     1     34.747 585.42 153.07
## - northeast        1     96.401 647.07 196.93
##
```

```
## Step: AIC=126.37
## sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp +
##      pcincome + beds_1000 + pop_density + northeast + northcentral +
##      south
```

```
##
##           Df Sum of Sq    RSS    AIC
## <none>                550.81 126.37
## - unemp             1     2.533 553.34 126.38
## - hsgrad            1     3.010 553.82 126.76
## - south             1     3.944 554.75 127.50
## - pop_density       1     4.387 555.19 127.85
## + docs_1000         1     0.133 550.67 128.27
## - bagrad            1     4.988 555.79 128.32
## + pop65             1     0.000 550.81 128.37
## - pcincome          1    14.747 565.55 135.94
## - pop18             1    21.486 572.29 141.13
## - poverty           1    27.234 578.04 145.51
## - pop               1    33.948 584.75 150.57
## - northcentral      1    35.244 586.05 151.54
## - beds_1000         1    52.476 603.28 164.23
## - northeast         1    97.351 648.16 195.66
```

```
multi_both
```

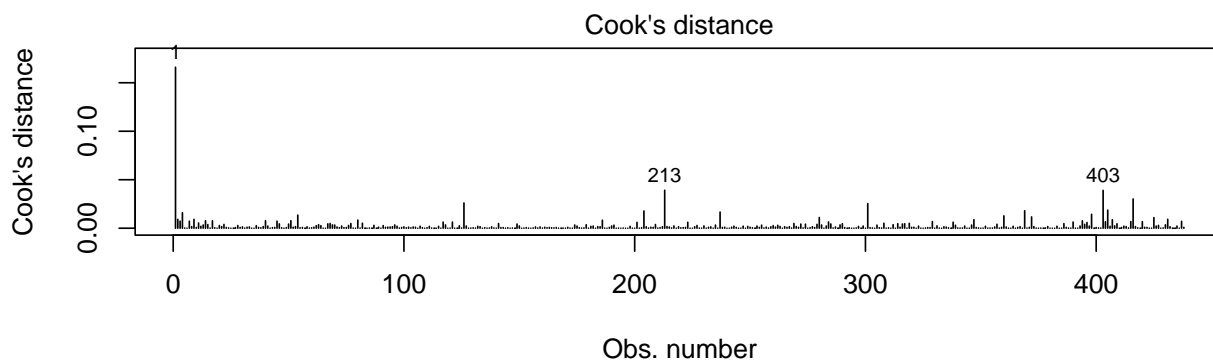
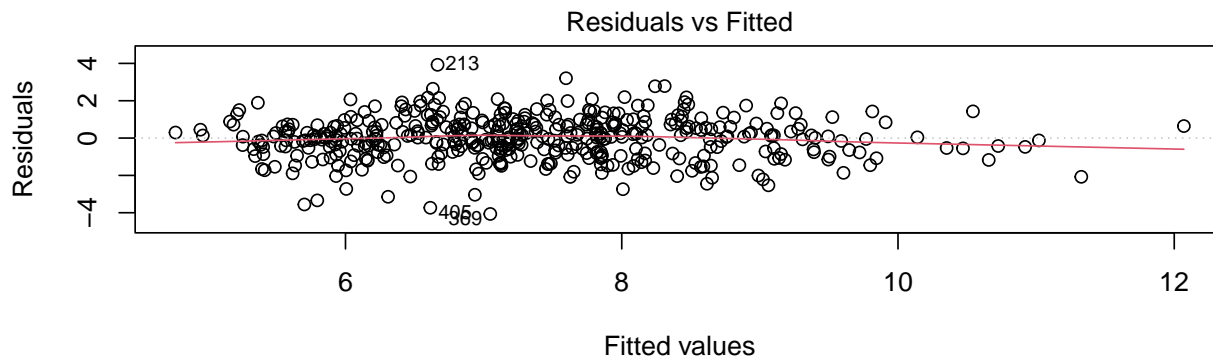
```
##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
##      poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
##      northcentral + south, data = sum_cdi_mod)
```

```
## Coefficients:
## (Intercept)      pop      pop18      hsgrad      bagrad
##  9.096e-02    7.261e-07    7.546e-02    2.624e-02   -3.617e-02
##  poverty      unemp      pcincome      beds_1000    pop_density
##  1.115e-01    4.714e-02    1.048e-04    2.172e-01    7.880e-05
##  northeast  northcentral      south
## -1.711e+00  -9.731e-01    3.142e-01
```

```
sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad + poverty + unemp + pcincome + beds_1000 + pop_density +
northeast + northcentral + south, data = sum_cdi_mod
```

Model diagnostic

```
par(mfrow = c(2,1))
plot(multi_both, which = 1)
plot(multi_both, which = 4)
```



```
both_without = sum_cdi[-c(1),]
```

```
with_both = lm(sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
  poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
  northcentral + south, data = sum_cdi_mod)
without_both = lm(sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
  poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
  northcentral + south, data = both_without)
summary(with_both); summary(without_both)
```

```
##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
##   poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
##   northcentral + south, data = sum_cdi_mod)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.0662 -0.6619  0.0502  0.7174  3.9254
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  9.096e-02  1.667e+00   0.055  0.956516
## pop          7.261e-07  1.419e-07   5.118  4.69e-07 ***
## pop18        7.546e-02  1.853e-02   4.072  5.57e-05 ***
## hsgrad       2.624e-02  1.722e-02   1.524  0.128270
## bagrad      -3.617e-02  1.844e-02  -1.962  0.050439 .
## poverty     1.115e-01  2.432e-02   4.584  6.01e-06 ***
## unemp        4.714e-02  3.372e-02   1.398  0.162867
## pcincome     1.048e-04  3.108e-05   3.373  0.000811 ***
## beds_1000    2.172e-01  3.414e-02   6.363  5.12e-10 ***
```

```

## pop_density 7.881e-05 4.283e-05 1.840 0.066502 .
## northeast -1.711e+00 1.974e-01 -8.667 < 2e-16 ***
## northcentral -9.731e-01 1.866e-01 -5.215 2.88e-07 ***
## south 3.142e-01 1.801e-01 1.744 0.081807 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.138 on 425 degrees of freedom
## Multiple R-squared: 0.5509, Adjusted R-squared: 0.5382
## F-statistic: 43.45 on 12 and 425 DF, p-value: < 2.2e-16

##
## Call:
## lm(formula = sqrt(crm_1000) ~ pop + pop18 + hsgrad + bagrad +
## poverty + unemp + pcincome + beds_1000 + pop_density + northeast +
## northcentral + south, data = both_without)
##
## Residuals:
## Min 1Q Median 3Q Max
## -4.0005 -0.7447 0.0672 0.7078 4.1414
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.092e-01 1.688e+00 0.242 0.808582
## pop 7.111e-07 1.438e-07 4.946 1.09e-06 ***
## pop18 6.304e-02 1.846e-02 3.415 0.000699 ***
## hsgrad 3.219e-02 1.738e-02 1.852 0.064654 .
## bagrad -3.406e-02 1.868e-02 -1.823 0.068985 .
## poverty 1.115e-01 2.466e-02 4.521 7.99e-06 ***
## unemp 4.435e-02 3.418e-02 1.298 0.195111
## pcincome 7.916e-05 3.066e-05 2.582 0.010163 *
## beds_1000 1.945e-01 3.401e-02 5.720 2.01e-08 ***
## pop_density 1.901e-04 2.992e-05 6.353 5.42e-10 ***
## northeast -1.653e+00 1.994e-01 -8.289 1.51e-15 ***
## northcentral -9.442e-01 1.890e-01 -4.995 8.58e-07 ***
## south 3.410e-01 1.824e-01 1.869 0.062316 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.154 on 426 degrees of freedom
## Multiple R-squared: 0.5712, Adjusted R-squared: 0.5592
## F-statistic: 47.3 on 12 and 426 DF, p-value: < 2.2e-16
check_collinearity(without_both)

## # Check for Multicollinearity
##
## Low Correlation
##
## Term VIF Increased SE Tolerance
## pop 1.00 1.00 1.00
## pop18 1.93 1.39 0.52
## hsgrad 3.28 1.81 0.31
## bagrad 3.50 1.87 0.29
## poverty 2.39 1.55 0.42
## unemp 1.86 1.36 0.54
## pcincome 1.03 1.01 0.98
## beds_1000 1.45 1.20 0.69
## pop_density 1.00 1.00 1.00

```

##	northeast	2.14	1.46	0.47
##	northcentral	2.18	1.48	0.46
##	south	2.39	1.55	0.42