EE5630 Digital Signal Processing

HW#1

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Due Sunday March 8, 2020

1. (Problem 2.5 in textbook)

A causal LTI system is described by the difference equation

$$y[n] - 5y[n-1] + 6y[n-2] = 2x[n-1].$$

- (a) Determine the homogeneous response of the system, i.e., the possible outputs if x[n] = 0 for all n.
- **(b)** Determine the impulse response of the system.
- (c) Determine the step response of the system.

2. (Problem 2.30 in textbook)

If the input and output of a causal LTI system satisfy the difference equation

$$y[n] = ay[n-1] + x[n],$$

then the impulse response of the system must be $h[n] = a^n u[n]$.

- (a) For what values of a is this system stable?
- (b) Consider a causal LTI system for which the input and output are related by the difference equation

$$y[n] = ay[n-1] + x[n] - a^{N}x[n-N],$$

where *N* is a positive integer. Determine and sketch the impulse response of this system. *Hint*: Use linearity and time-invariance to simplify the solution.

- (c) Is the system in part (b) an FIR or an IIR system? Explain.
- (d) For what values of a is the system in part (b) stable? Explain.

3. (Problem 2.35 in textbook)

Consider an LTI system with frequency response

$$H(e^{j\omega}) = e^{-j\left(\omega - \frac{\pi}{4}\right)} \left(\frac{1 + e^{-j2\omega} + 4e^{-j4\omega}}{1 + \frac{1}{2}e^{-j2\omega}}\right), \quad -\pi < \omega \le \pi.$$

Determine the output y[n] for all n if the input for all n is

$$x[n] = \cos\left(\frac{\pi n}{2}\right)$$

4. (Problem 2.40 in textbook)

Determine which of the following signals is periodic. If a signal is periodic, determine its period.

(a)
$$x[n] = e^{j(2\pi n/5)}$$

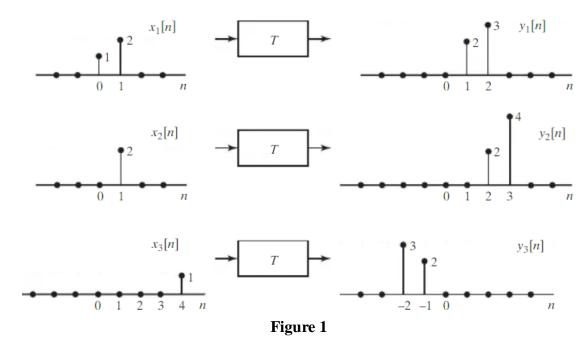
$$(b) x[n] = \sin(\pi n/19)$$

(c)
$$x[n] = ne^{j\pi n}$$

(d)
$$x[n] = e^{jn}$$

5. (Problem 2.47 in textbook)

The system T in Figure 1 is known to be *time invariant*. When the inputs to the system are $x_1[n]$, $x_2[n]$, and $x_3[n]$, the responses of the system are $y_1[n]$, $y_2[n]$, and $y_3[n]$, as shown.



- (a) Determine whether the system T could be linear.
- (b) If the input x[n] to the system T is $\delta[n]$, what is the system response y[n]?
- (c) What are all possible inputs x[n] for which the response of the system T can be determined from the given information alone?

Notice:

- 1. Each question should be in different file (.jpg .jpeg .png), and you should name those files Q1, Q2, ... Q5.
- 2. Archive all the files into a zip file. (There would be 5 files inside the zip file.)
- 3. Name the zip file as "HW1_StudentID.zip". (such as $HW1_108061xxx.zip$)