

# Assignment 1 SENG474

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1.

for AGE:

$$\text{young} = \frac{8}{24} \cdot \left[ -\frac{2}{8} \log_2\left(\frac{2}{8}\right) - \frac{1}{2} \log_2\left(\frac{1}{2}\right) - \frac{2}{8} \log_2\left(\frac{2}{8}\right) \right] = 0.5$$

$$\text{pre-pre} = \frac{8}{24} \cdot \left[ -\frac{2}{8} \log_2\left(\frac{2}{8}\right) - \frac{5}{8} \log_2\left(\frac{5}{8}\right) - \frac{1}{8} \log_2\left(\frac{1}{8}\right) \right] = 0.4329$$

$$\text{presb} = \frac{8}{24} \left[ -\frac{1}{8} \log_2\left(\frac{1}{8}\right) - \frac{6}{8} \log_2\left(\frac{6}{8}\right) - \frac{1}{8} \log_2\left(\frac{1}{8}\right) \right] = 0.3538$$

$$\text{total} = 1.2867$$

for spectacle-prescrip

$$\text{myope} = \frac{12}{24} \left[ -\frac{2}{12} \log_2\left(\frac{2}{12}\right) - \frac{7}{12} \log_2\left(\frac{7}{12}\right) - \frac{3}{12} \log_2\left(\frac{3}{12}\right) \right] = 0.6922$$

$$\text{hyper} = \frac{12}{24} \left[ -\frac{3}{12} \log_2\left(\frac{3}{12}\right) - \frac{8}{12} \log_2\left(\frac{8}{12}\right) - \frac{1}{12} \log_2\left(\frac{1}{12}\right) \right] = 0.5944$$

$$\text{total} = 1.2866$$

for astigmatism

$$\text{No} = \frac{12}{24} \left[ -\frac{5}{12} \log_2\left(\frac{5}{12}\right) - \frac{7}{12} \log_2\left(\frac{7}{12}\right) - 0 \right] = 0.4899$$

$$\text{Yes} = \frac{12}{24} \left[ -0 - \frac{8}{12} \log_2\left(\frac{8}{12}\right) - \frac{4}{12} \log_2\left(\frac{4}{12}\right) \right] = 0.4591$$

$$\text{total} = 0.949$$

For tear-prod-rate

$$\text{reduced} \quad \frac{12}{24} \left[ \overset{\text{soft}}{0} - \overset{\text{none}}{\frac{12}{12} \log_2(1)} - \overset{\text{hard}}{0} \right] = 0$$

$$\text{normal} \quad \frac{12}{24} \left[ -\frac{5}{12} \log_2\left(\frac{5}{12}\right) - \frac{3}{12} \log_2\left(\frac{3}{12}\right) - \frac{4}{12} \log_2\left(\frac{4}{12}\right) \right] = 0.7771$$

$$\text{total} = 0.7771$$

So root is tear-prod-rate

For tear-prod-rate = reduced

Expected info: 0

tear-prod-rate = normal

age = young

$$\text{info}([2, 0, 2]) = -\frac{2}{4} \log_2\left(\frac{2}{4}\right) - 0 - \frac{2}{4} \log_2\left(\frac{2}{4}\right) = 1$$

age = pre-pr

$$\text{info}([2, 1, 1]) = -\frac{2}{4} \log_2\left(\frac{2}{4}\right) - \frac{1}{4} \log_2\left(\frac{1}{4}\right) - \frac{1}{4} \log_2\left(\frac{1}{4}\right) = 1.5$$

age = presb

$$\text{info}([1, 2, 1]) = -\frac{1}{4} \log_2\left(\frac{1}{4}\right) - \frac{1}{2} \log_2\left(\frac{1}{2}\right) - \frac{1}{4} \log_2\left(\frac{1}{4}\right) = 1.5$$

$$\text{Expected info: } 1 \cdot \frac{4}{12} + 1.5 \cdot \frac{4}{12} + 1.5 \cdot \frac{4}{12} = 1.3333$$

$$\text{spect} = \text{myope} \quad \frac{6}{12} \left[ \frac{2}{6} \log_2 \left( \frac{2}{6} \right) - \frac{1}{6} \log_2 \left( \frac{1}{6} \right) - \frac{3}{6} \log_2 \left( \frac{3}{6} \right) \right] = 0.7296$$

$$\text{hypermetrope} \quad \frac{6}{12} \left[ -\frac{3}{6} \log_2 \left( \frac{3}{6} \right) - \frac{2}{6} \log_2 \left( \frac{2}{6} \right) - \frac{1}{6} \log_2 \left( \frac{1}{6} \right) \right] = 0.7296$$

$$\text{total} = 1.4592$$

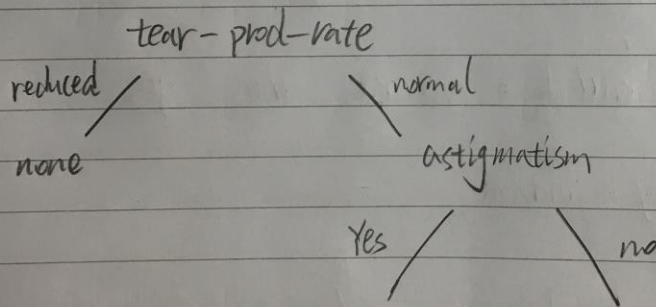
$$\text{astigmatism} = \text{no} \quad \frac{6}{12} \left[ -\frac{5}{6} \log_2 \left( \frac{5}{6} \right) - \frac{1}{6} \log_2 \left( \frac{1}{6} \right) - 0 \right] = 0.3250$$

$$\text{yes} \quad \frac{6}{12} \left[ 0 - \frac{2}{6} \log_2 \left( \frac{2}{6} \right) - \frac{4}{6} \log_2 \left( \frac{4}{6} \right) \right] = 0.4591$$

$$\text{total} = 0.7769$$

so astigmatism will be the next node

root and first level



2.  $P(\text{Yes}) = \frac{9}{14}$      $P(\text{no}) = \frac{5}{14}$

possible tests For "Yes"

outlook = sunny	$\frac{2}{5}$
overcast	$\frac{4}{4}$
rainy	$\frac{3}{5}$

temp = hot	$\frac{2}{4}$
mild	$\frac{4}{6}$
cool	$\frac{3}{4}$

humidity = high	$\frac{3}{7}$
= normal	$\frac{6}{7}$

windy = False	$\frac{6}{8}$
= True	$\frac{3}{6}$

Then: If outlook = overcast then yes

If humidity = normal

possible tests	
outlook = sunny	$\frac{2}{7}$
rainy	$\frac{2}{3}$

temp = hot	$\frac{1}{1}$
mild	$\frac{2}{2}$
cool	$\frac{3}{4}$



windy = False	$\frac{4}{4}$
= True	$\frac{2}{3}$

If humidity = normal  
and windy = False then yes

possible tests

outlook = sunny	$\frac{1}{4}$
rainy	$\frac{1}{3}$

temp = hot	0
mild	$\frac{2}{4}$
cool	0

humidity = normal	$\frac{1}{2}$
high	$\frac{1}{5}$

windy = False	$\frac{1}{4}$
True	$\frac{1}{4}$

choose mild

If temp = mild

possible tests

outlook = sunny	$\frac{1}{2}$
rainy	$\frac{1}{3}$

humidity = normal 1  
                  high  $\frac{1}{3}$

windy = False  $\frac{1}{2}$   
          True  $\frac{1}{2}$

If temp = mild and humidity = normal  
then yes

possible tests

outlook = sunny 0  
          rainy  $\frac{1}{3}$

temp = hot 0  
          mild  $\frac{1}{3}$   
          cool 0

humidity = normal 0  
          = high  $\frac{1}{3}$

windy = False  $\frac{1}{3}$   
          True 0

If outlook = rainy

possible tests

temp = hot 0  
          mild  $\frac{1}{2}$   
          cool 0

humidity = high	$\frac{1}{2}$
normal	0

windy = False	1
True	0

If outlook = rainy and windy = False  
then yes.

For "No"  
Possible tests

outlook = sunny	$\frac{3}{5}$
rainy	$\frac{2}{5}$
overcast	0

temp = hot	$\frac{2}{7}$
mild	$\frac{2}{8}$
cool	$\frac{1}{4}$

humidity = high	$\frac{4}{7}$
normal	$\frac{1}{7}$

windy = False	$\frac{2}{8}$
True	$\frac{3}{6}$

If outlook = sunny

possible tests

temp	= hot	$\frac{2}{2}$
	mild	$\frac{1}{2}$
	cool	0

humidity	= high	$\frac{2}{3}$
	normal	0

windy	= False	$\frac{2}{3}$
	True	$\frac{1}{2}$

If outlook = sunny and humidity = high  
then no

possible tests

outlook	= sunny	0
	= rainy	$\frac{2}{5}$
	= overcast	0

temp	= hot	0
	= mild	$\frac{1}{4}$
	= cool	$\frac{1}{4}$

humidity	= high	$\frac{1}{4}$
	= normal	$\frac{1}{7}$



$$\begin{array}{l} \text{windy} = \text{False} \\ \text{True} \end{array} \quad \begin{array}{l} 0 \\ \frac{2}{5} \end{array}$$

If outlook = rainy

possible tests

$$\begin{array}{l} \text{temp} = \text{hot} \\ \text{mild} \\ \text{cool} \end{array} \quad \begin{array}{l} 0 \\ \frac{1}{3} \\ \frac{1}{3} \end{array}$$

$$\begin{array}{l} \text{humidity} = \text{high} \\ \text{normal} \end{array} \quad \begin{array}{l} \frac{1}{2} \\ \frac{1}{3} \end{array}$$

$$\begin{array}{l} \text{windy} = \text{False} \\ \text{True} \end{array} \quad \begin{array}{l} 0 \\ \frac{2}{2} \end{array}$$

If outlook = rainy and windy = True  
then no.

Prism rules: If outlook = overcast then yes

If humidity = normal and windy = False then yes

If temp = mild and humidity = normal then yes

If outlook = rainy and windy = False then yes

If outlook = sunny and humidity = high then no

If outlook = rainy and windy = True then no

pre-presb, hyper, yes, reduced, ?

3.

$$P(\text{contact-lenses} = \text{soft} | E)$$

$$= \left(\frac{2+1}{8+3}\right) \cdot \left(\frac{2+1}{12+2}\right) \cdot \left(\frac{1}{12+2}\right) \left(\frac{1}{12+2}\right) / P(E) = 0.0002982 / P(E)$$

$$P(\text{contact-lenses} = \text{none} | E)$$

$$= \left(\frac{5+1}{8+3}\right) \cdot \left(\frac{8+1}{12+2}\right) \cdot \left(\frac{8+1}{12+2}\right) \cdot \left(\frac{12+1}{12+2}\right) / P(E) = 0.2093 / P(E)$$

$$P(\text{contact-lenses} = \text{hard} | E)$$

$$= \left(\frac{1+1}{8+3}\right) \cdot \left(\frac{1+1}{12+2}\right) \cdot \left(\frac{4+1}{12+2}\right) \left(\frac{1}{12+2}\right) / P(E) = 0.0006626 / P(E)$$

$$P(E) = 0.2103$$

$$P(\text{contact-lenses} = \text{soft} | E) = 0.001418$$

$$P(\text{contact-lenses} = \text{none} | E) = 0.9952$$

$$P(\text{contact-lenses} = \text{hard} | E) = 0.003151$$