

# Crash Course: Bases de Estadística y Econometría

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Informática par Economistas  
Universidad de Piura  
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*\*Nota basada en material del curso de Jonathan Roth y Peter Hull en Brown University.*

¿Así que quieres saber de machine learning? Primero las bases



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→ Es la caja de herramientas estadísticas que usamos los economistas para responder preguntas económicas usando data

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Por lo general, los economistas nos concentramos en las primeras dos, con un énfasis en preguntas causales



## ¿Por qué es difícil responder estas preguntas?

- Para preg. descriptivas: solo observamos una **muestra** de individuos, no la **población** completa
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Nuestra muestra es **aleatoriamente** seleccionada de la población
  - Por ej., los nombres de los trabajadores que vemos en la encuesta fueron sacados de un sombrero al azar donde estaban todos los posibles trabajadores
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- El peor escenario: nuestra muestra es *no representativa* de la población que nos interesa
  - Por ej., los trabajadores que son formales tenían muchas mayor probabilidad de responder la encuesta

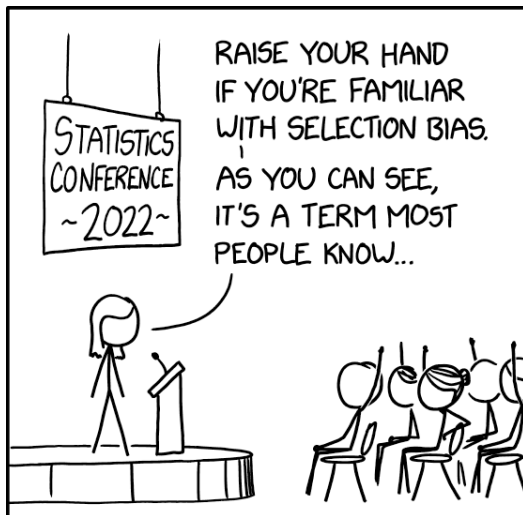


- En 1948, el Chicago Tribune escribió que Thomas Dewey ganaba a Harry Truman en la elección presidencial, basada en una encuesta a votantes



- En 1948, el Chicago Tribune escribió que Thomas Dewey ganaba a Harry Truman en la elección presidencial, basada en una encuesta a votantes
- Pero su encuesta fue por teléfono. En ese año solo la gente rica tenía teléfonos: muestra  $\neq$  población  $\rightarrow$  ¡resultados engañosos!

*Sesgo de selección* se refiere a contextos como el que mencionamos anteriormente, donde la muestra no es sacada aleatoriamente desde la población de interés



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  - Preg. Descriptiva: ¿Cuánto ganan los alumnos de UdeP después de graduarse?
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- Preg. Contrafactuales no se pueden contestar con data solamente. ¡Necesitamos supuestos para aprender de ellos!

# Splitting up the problem

- When thinking about causal Qs, it's often easier to split the problem in two
- **Identification:** what could we learn about the parameters we care about (causal effects) if we had the observable data for the entire population
  - Need to make assumptions about how observed outcomes relate to outcomes that would have been realized under different treatments
- **Statistics:** what can we learn about the full population that we care about from the finite sample that we have?
  - Need to understand the process by which our data is generated from the full population

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- The process of learning about the *parameter* from the *estimand* is called **identification**.

Teoría Económica



Parámetros

Distribución Poblacional



Estimandos

Muestra



Estimadores



Identificación



Inferencia Estadística

$$\theta = E[X_i]/E[Y_i]$$

$$E[X_i]$$

$$E[Y_i]$$

$$\sum X_i/n$$

$$\sum Y_i/n$$

## Let's add some math...

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- Observed outcome  $Y_i$  is  $Y_i(1)$  if  $D_i = 1$  and  $Y_i(0)$  if  $D_i = 0$ . ( $Y_i$  is your actual earnings)

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- We can write the observed outcome as  $Y_i = D_i Y_i(1) + (1 - D_i) Y_i(0)$

- Example sample:  $(Y_i, D_i)$  for  $i = 1, \dots, N$ . Data with earnings and where you went to school



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- Example estimator:
  - Difference in sample mean of earnings for people who went to Brown and people who went to URI:

$$\underbrace{\frac{1}{N_1} \sum_{i:D_i=1} Y_i}_{\text{Avg earnings at Brown in sample}} - \underbrace{\frac{1}{N_0} \sum_{i:D_i=0} Y_i}_{\text{Avg earnings at URI in sample}}$$

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- Example estimand:
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- Example target parameter:
  - Causal effect of Brown for Brown students:

$$\underbrace{E[Y_i(1)|D_i = 1]}_{\text{Earnings at Brown for Brown students in pop}} - \underbrace{E[Y_i(0)|D_i = 1]}_{\text{Earnings at URI for Brown students in pop}}.$$

## Why is causal identification hard?

- Thought experiment: suppose we had data on earnings for *every* Brown and URI graduate
- We can learn from the data:

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Earnings at URI for Brown Students

- Because we never see Brown students going to URI!

- One idea to solve this problem would be to assume that:

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- Why might this give us the wrong answer?
- Because Brown students may be different from URI students in other ways that would affect their earnings (regardless of where they went to college)
  - Academic ability, family background, career goals, etc.
- These differences are referred to as *omitted variables* or *confounding factors*

## What about experiments?

- The gold standard for learning about causal effects is a randomized controlled trial (RCT), aka experiment
- Suppose that the Brown and URI administration randomized who got into which college (assume these are the only 2 colleges for simplicity)
- Since college is randomly assigned, the only thing that differs between Brown and URI students is the college they went to
- Hence,

$$\underbrace{E[Y_i(0)|D_i = 1]}_{\text{Earnings at URI for Brown Students}} = \underbrace{E[Y_i(0)|D_i = 0]}_{\text{Earnings at URI for URI Students}}$$

since we've eliminated any confounding factors

## But running experiments is often hard/impossible

- Unfortunately, Brown/URI have not let us randomize who gets into which college
  - At least not yet! If you could convince them to do this, it'd make for a cool senior thesis!
- Likewise, it is difficult to convince states to randomize their minimum wages, or other policies
- In some cases, randomization is not just difficult but would be immoral
  - “What is the causal effect of spousal death on labor supply?”

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- In some cases, randomization is not just difficult but would be immoral
  - “What is the causal effect of spousal death on labor supply?”
- In this course, we'll discuss tools economists try to use when running experiments is not possible.

## Course Roadmap – Where we're going

- **Part I (~ 7 lectures): Review of probability/statistics.** This will give us a mathematical language to talk about:
  - ① *Statistical estimation/inference*: how does the sample we observe relate to the population of interest
  - ② *Identification*: how do observable features of the population relate to (causal) parameters we care about

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- **Part III (~ 7 lectures): Other “quasi-experimental” strategies:** We'll discuss other strategies for “mimicking” an experiment when it's not available, including instrumental variables (IV) and regression discontinuity (RD)

# Outline

1. Deriving Multivariate Regression and OLS
2. Regression and Causality
3. Regression Odds and Ends



## Moving Beyond One “Regressor”

- So far we've talked about regression as a way of approximating the CEF  $E[Y_i|X_i = x] \approx \alpha + x\beta$  for a single scalar  $X_i$ 
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  - In the Brown/URI example, we may want to control for high school GPA, family income, SAT, race ...
- ② We want a *nonlinear* CEF approx.: e.g.  $E[Y_i | X_i] \approx \alpha + X_i\beta + X_i^2\gamma$ 
  - We can “trick” regression into doing this by setting  $\mathbf{X}_i = (1, X_i, X_i^2)'$