

The language of the computers

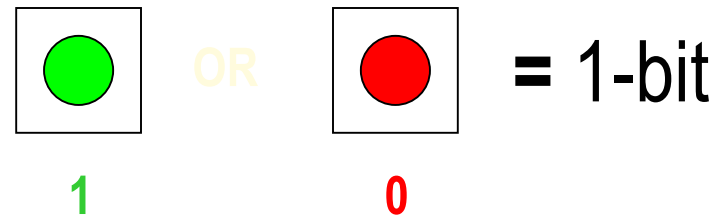
CMPT-2!X

The Language of the Computers

Computer (binary) arithmetic

Digital computers use two states

- 0 and 1 = Binary System
- Bi in Latin is 2



Binary system

- 0 and 1 = Binary System

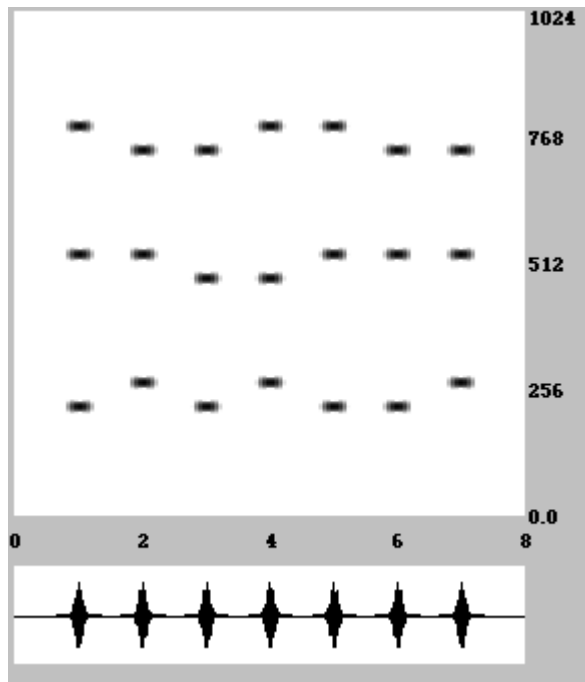
➤ 0 = OFF, 1 = ON

➤ 0 = Down, 1 = Up

➤ 0 = 0 volts, 1 = 5 volts

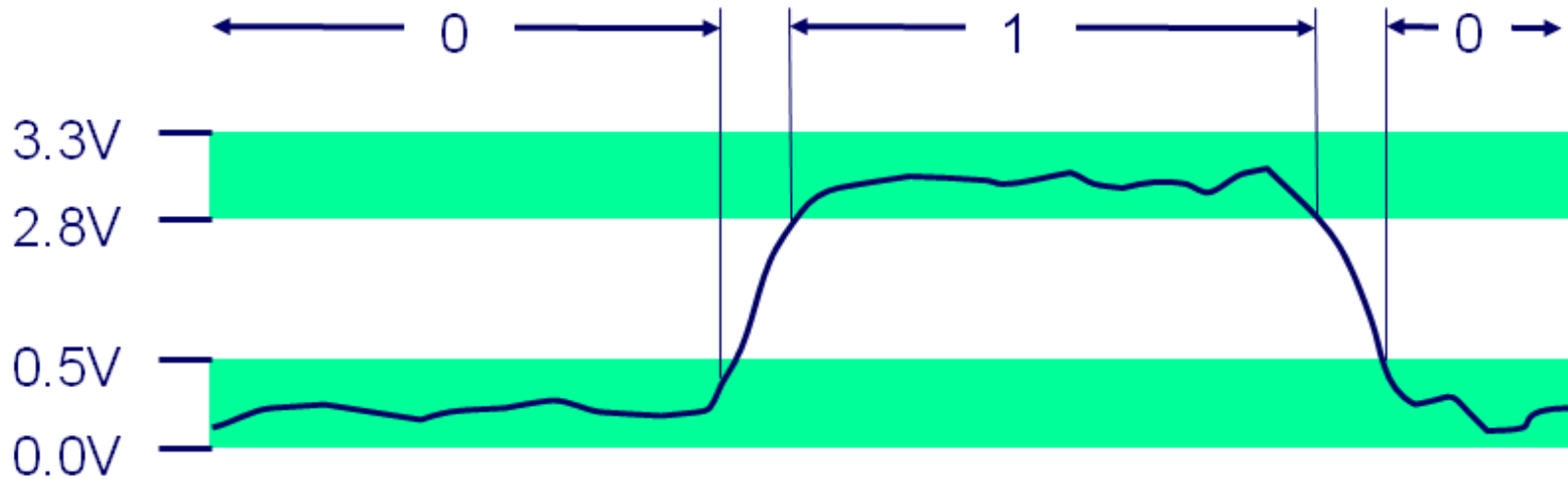


Actual Binary signal or sequence

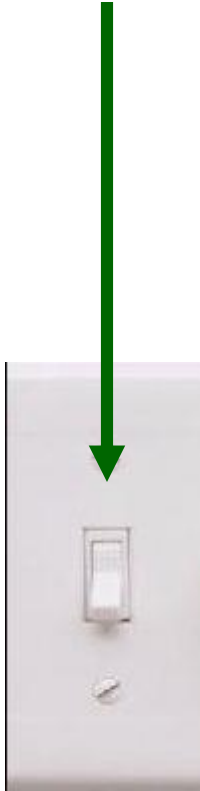


<http://www.uwec.edu>

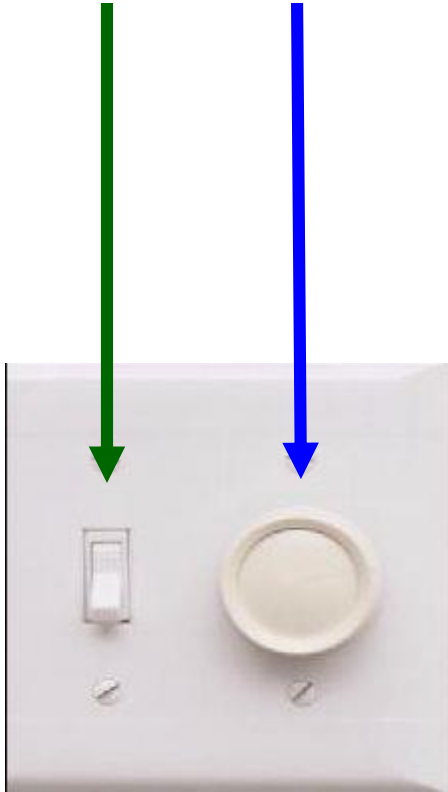
It is all voltage ... electricity



Digital ... Binary



Digital & Analog ... analogy



Number systems

- Decimal
- Binary
- Octal
- Hexadecimal.

Binary System

- Binary numbers: base₂
 $\{0, 1\}$

Octal System

- Binary numbers: base₂

{0, 1}

- Octal numbers: base₈

{0 1 2 3 4 5 6 7}

Hex System

- Binary numbers: base₂

{0, 1}

- Octal numbers: base₈

{0 1 2 3 4 5 6 7}

- Hexadecimal numbers: base₁₆

{0 1 2 3 4 5 6 7 8 9 A B C D E F}

Binary 1...0...1

```
0010011110111101111111111100000
101011111011111100000000000010100
101011111010010000000000000100000
101011111010010100000000000100100
10101111101000000000000000011000
10101111101000000000000000011100
10001111101011100000000000011100
10001111101110000000000000011000
00000001110011100000000000011001
00100101110010000000000000000001
00101001000000010000000001100101
10101111101010000000000000011100
00000000000000000111100000010010
00000011000011111100100000100001
0001010000100000111111111110111
10101111101110010000000000011000
00111100000001000001000000000000
10001111101001010000000000011000
00001100000100000000000011101100
00100100100001000000010000110000
```

Decimal (Base-10) ... Binary (Base-2)

Decimal (Base 10)	Binary (Base 2)
0	0
1	1
2	10
3	11
4	100
5	101
6	110
7	111
8	1000
9	1001
10	1010
11	1011
1000	1111101000

Number conversions

- Our aim is to learn how to convert:
- Decimal numbers to Binary numbers and back
- $(xxxx)_{10} \longleftrightarrow (yyyy)_2$

Number with Base-10 (Decimal)

- NumberWithBase₁₀

$$\blacktriangleright (9 \quad 5 \quad 3)_{10}$$

$$= 900 \quad +50 \quad +3$$

$$= 9*100 \quad +5*10 \quad +3*1$$

$$= 9*10^2 \quad +5*10^1 \quad +3*10^0$$

Multiply by the proper power of 10

- NumberWithBase₁₀

$$\blacktriangleright (9 \quad 5 \quad 3)_{10}$$

$$= 900 \quad +50 \quad +3$$

$$= 9*100 \quad +5*10 \quad +3*1$$

$$= 9*10^2 \quad +5*10^1 \quad +3*10^0$$

We multiply each digit by the appropriate power of 10

Convert binary number to decimal number

- NumberWithBase₁₀

➤ (953)₁₀

$$= 9 * 10^2 + 5 * 10^1 + 3 * 10^0$$

- Convert: From base-2 to base-10

$$- (\textcolor{red}{1} \textcolor{gray}{1} \textcolor{teal}{1} 0)_2 = (?)_{10}$$

Convert binary number to decimal number

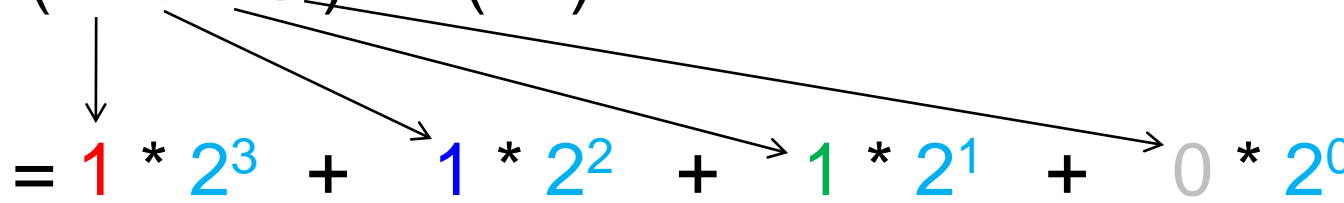
- NumberWithBase₁₀

➤ $(953)_{10}$
 $= 9 * 10^2 + 5 * 10^1 + 3 * 10^0$

- Convert: From base-2 to base-10

➤ $(\textcolor{red}{1} \textcolor{blue}{1} \textcolor{green}{1} 0)_2 = (?)_{10}$

$= \textcolor{red}{1} * \textcolor{blue}{2}^3 + \textcolor{blue}{1} * \textcolor{blue}{2}^2 + \textcolor{green}{1} * \textcolor{blue}{2}^1 + 0 * \textcolor{blue}{2}^0$



We multiply each binary digit by the appropriate power of 2

Perform the simple arithmetic operations

- NumberWithBase₁₀

➤ $(953)_{10}$

$$= 9 * 10^2 + 5 * 10^1 + 3 * 10^0$$

- Convert: From base-2 to base-10

➤ $(\textcolor{red}{1} \textcolor{blue}{1} \textcolor{green}{1} \textcolor{gray}{0})_2 = (?)_{10}$

$$= \textcolor{red}{1} * \textcolor{blue}{2}^3 + \textcolor{blue}{1} * \textcolor{blue}{2}^2 + \textcolor{green}{1} * \textcolor{blue}{2}^1 + \textcolor{gray}{0} * \textcolor{blue}{2}^0$$

$$= 8 + 4 + 2 + 0$$

$$= 12 + 2$$

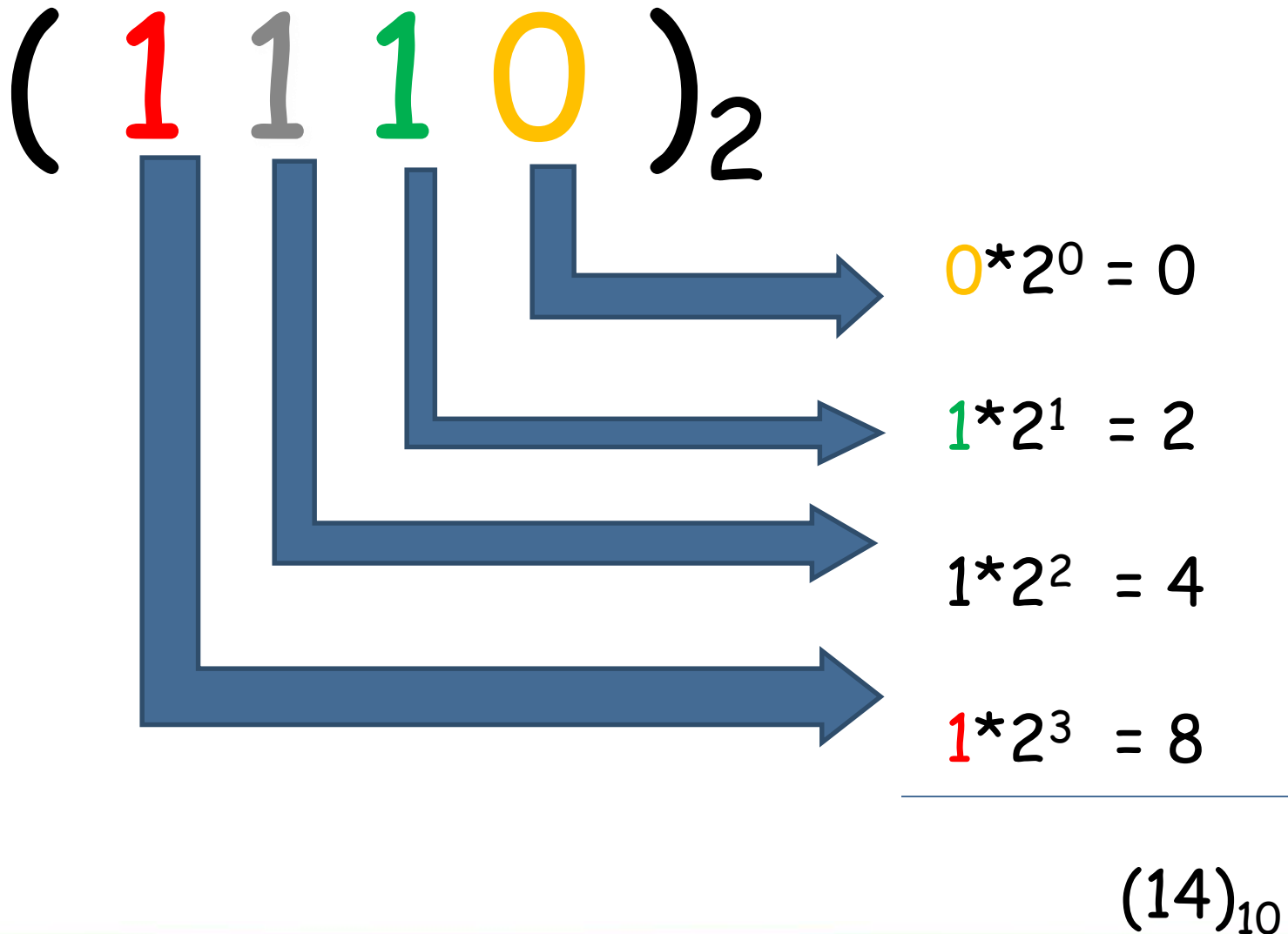
$$= (14)_{10}$$

The result

The result

- $(\textcolor{red}{1} \textcolor{blue}{1} \textcolor{green}{1} 0)_2 = (14)_{10}$

Another view



Another example

Convert: From base₂ to base₁₀

$$\blacktriangleright (1\ 1\ 0\ 1\ 1)_2$$

$$= 1 * 2^4 + 1 * 2^3 + 0 * 2^2 + 1 * 2^1 + 1 * 2^0$$

$$= 16 + 8 + 0 + 2 + 1$$

$$= (27)_{10}$$

\blacktriangleright Therefore the result is: $(1\ 1\ 0\ 1\ 1)_2 = (27)_{10}$

One more example

$$\begin{aligned} \blacktriangleright (1\ 0\ 1\ 1)_2 &= (?)_{10} \\ &= 1*2^3 + 0*2^2 + 1*2^1 + 1*2^0 \\ &= 8 + 0 + 2 + 1 \\ &= (11)_{10} \end{aligned}$$

\blacktriangleright Therefore the result is: $(1\ 0\ 1\ 1)_2 = (11)_{10}$

Convert: From base-10 \Rightarrow base-2

The inverse ...

Binary to Decimal, use **multiplications**

Decimal to Binary, use **divisions**

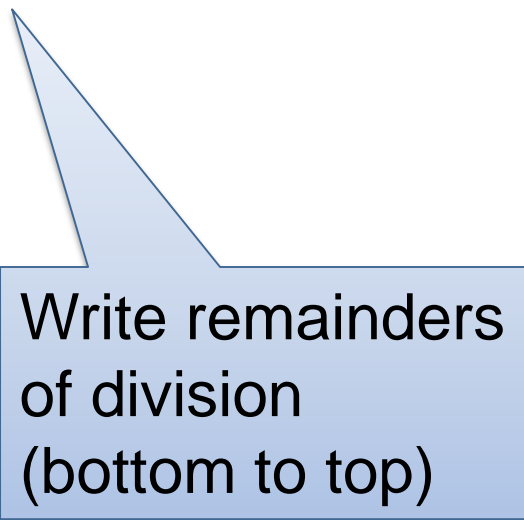
Convert: From base-10 \Rightarrow base-2

- $(27)_{10} = (?)_2$
- Divide decimal 27 by 2
 - $27 / 2 = 13$ remainder 1
 - $13 / 2 = 6$ remainder 1
 - $6 / 2 = 3$ remainder 0
 - $3 / 2 = 1$ remainder 1
 - $1 / 2 = 0$ remainder 1

When the result of the division is ZERO. We stop

The result ...

- $(27)_{10} = (?)_2$
- Divide decimal 27 by 2
 - $27 / 2 = 13$ remainder 1
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Write remainders
of division
(bottom to top)

The result ...

- $(27)_{10} = (?)_2$

Write remainders of
division (bottom to top)

- Divide decimal 27 by 2

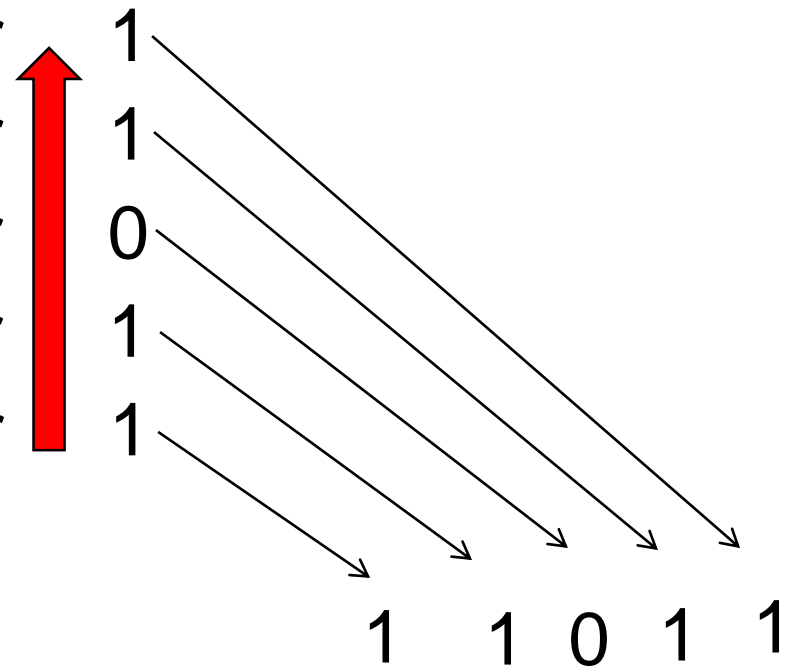
- $27 / 2 = 13$ remainder

- $13 / 2 = 6$ remainder

- $6 / 2 = 3$ remainder

- $3 / 2 = 1$ remainder

- $1 / 2 = 0$ remainder



The result

- $(27)_{10} = (11011)_2$

Another example

- $(28)_{10} = (?)_2$
- Divide decimal 28 by 2
 - $28 / 2 = 14$ remainder 0
 - $14 / 2 = 7$ remainder 0
 - $7 / 2 = 3$ remainder 1
 - $3 / 2 = 1$ remainder 1
 - $1 / 2 = 0$ remainder 1

When the result of the division is ZERO. We stop

Another example ...

- $(28)_{10} = (?)_2$

Write remainders of
division (bottom to top)

- Divide decimal 28 by 2

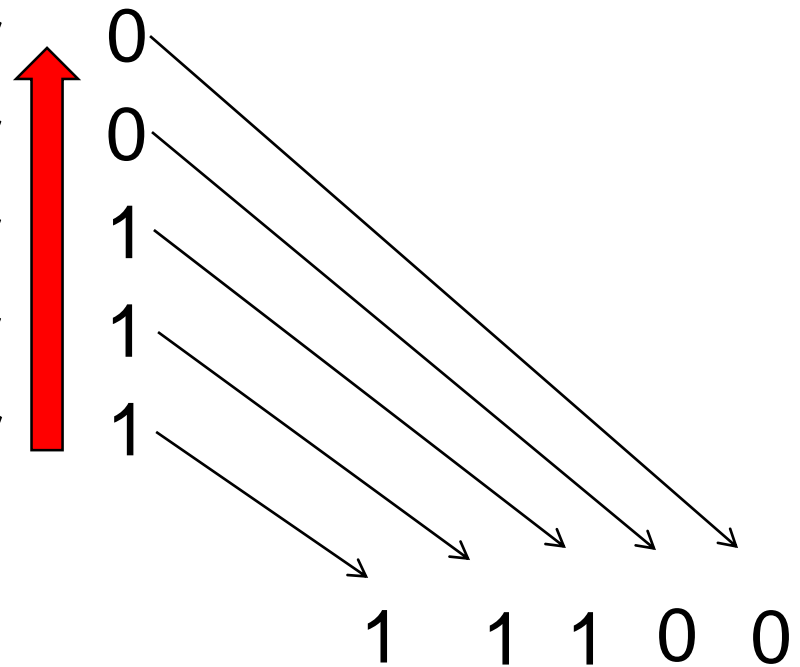
- $28 / 2 = 14$ remainder

- $14 / 2 = 7$ remainder

- $7 / 2 = 3$ remainder

- $3 / 2 = 1$ remainder

- $1 / 2 = 0$ remainder



The result

- $(28)_{10} = (11100)_2$

Conclusion: Binary and Decimal conversion

1. Converting a binary (base-2) to decimal (base-10), form the appropriate sum of powers in base “2”
2. Converting a decimal integer (base-10) to binary (base-2), divide by “2”, use the remainders as coefficients. Collect the coefficients bottom-top.