

CS 2

Introduction to Programming Methods



Last Time

Dynamic programming

- how to solve optimization problems fast

Other Dynamic Prog Examples

Find min # of (minUS) coins to make an amount

- to find the solution for 13¢
 - solve for all of 1¢, 2¢, 3¢, ..., 12¢
 - choose best among {solution for i¢ + solution for 13-i¢}

Knapsack problem

- various item types of various values & weights
- one bag with limited total weight

Gene Sequence Alignment

Shortest Path

- more on this later



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Networking

Communication between computers

- web, email, streaming, etc



Telephony



Video



Music



Social networks



Location



Mail



Cloud computing



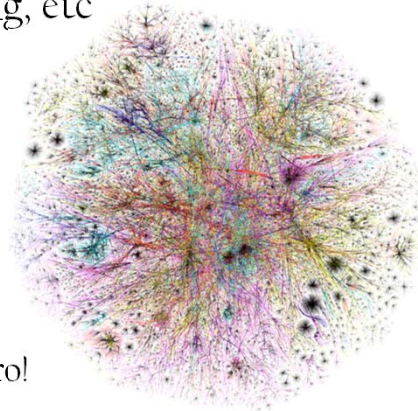
Networking

Communication between computers

- web, email, streaming, etc

Internet

- complex topology
 - computers connected
 - and routers
 - traffic directing



As usual, today is just an intro!



Addressing

Each machine has

- a globally unique address
 - IP address; 32 bits for now (www.caltech.edu: 50.18.115.211)
- and a domain name
 - easier for humans...
 - mapping from DN to IP may change dynamically
 - tree of DNS servers
 - » keep track of domains used recently

Addresses assigned by ICANN

- Marina del Rey



Circuit Switching



Used in (old) telephone network

- when a call is made, switches are activated...
- establishing a line between two phones
 - quite rigid!
 - line busy even if no one is talking over it
 - if all lines are busy, you are stuck
 - but efficient
 - if you get a line, data can be sent reliably, with no overhead
- not quite appropriate for the internet...

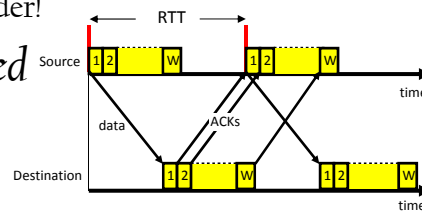


Packet switching

Basic Principles

- data split into small (numbered) packets
- each packet is sent to receiver
 - so each can actually end up using a different path
- data reassembled at the receiver
 - can be received out of order!

Can be *connection-oriented*
or *connectionless*



Connection-oriented Switching

“Virtual” Circuit Switching

- initial setup establishes route to destination
 - hops between network nodes; more on this later
- each node aware of “circuit”
 - stores connectionID to know where to forward packets
- then packets just include their connectionID
 - small header (minor overhead)
- “dedicated” line, in-order transmission
 - example: X.25, Frame-relay; also, TCP



Connectionless Switching

Datagram communication

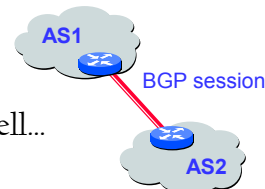
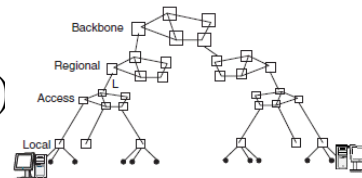
- each dispatched packet contains end address
- packets may go via different routes
 - based on target IP address
 - and which connection is active
 - routing tables dynamically updated
- example: Ethernet, IP, UDP
 - better for video conferencing or streaming
 - loss of a few packets not a showstopper



Heterogeneity of Networks

Two-level hierarchy

- Autonomous System (AS)
 - usually homogeneous domain
 - Sprint, AT&T, Verizon,...
 - shortest path routing: OSPF, IS-IS
- inter-domain
 - BGP (Border Gateway Protocol)
 - deal with inhomogeneity
 - the other protocols do not scale up well...
 - no guarantee of shortest path...



Abstraction

Networks are graphs

- extension of trees
- can be undirected
 - just a link btw nodes
- or directed
 - only in one direction
- and/or weighted
 - weight can be, e.g., RTT

Extensions of Trees

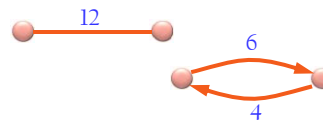
Graphs are widely used too

- dates back to Euler
- nodes and links (edges)
 - cycles allowed
 - edge can be directed or not
 - values assigned to edges too
 - "weighted" graphs
- useful in many applications
 - e.g., networks, automata, database dependencies, task scheduling (critical path analysis), even garbage collection in Java



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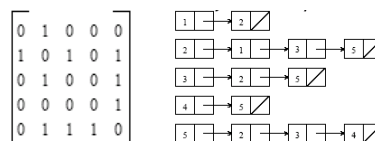
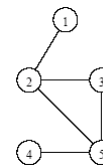
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Storing Graph Connectivity

Two basic ways of encoding graphs

- adjacency matrix
 - $M[i][j]$ indicates whether (i,j) is an edge
- linked list
 - or iterator
 - storing neighbors



Directed and/or weighted graphs?

- same deal, small changes



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Single-Source Shortest Path

Find shortest paths from a source node

- used in OSPF (careful: only non-negative weights!)

Good news: dynamic programming at work

- if R is a node on the minimal path from P to Q, knowing the latter implies knowing the minimal path from P to R
- running time: $O(E+V^2)$
 - can be made $O(E+V \log V)$ with a priority queue



Pseudocode

Vertices stored in V

Source vertex = s

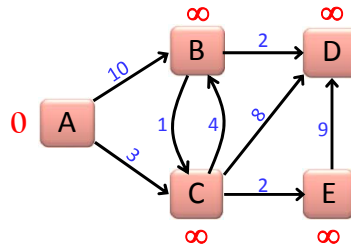
```
dist[s] ← 0                                (distance to source vertex is zero)
for all v ∈ V - {s}
  do dist[v] ← ∞                            (set all other distances to infinity)
Q ← V                                       (queue Q initially contains all vertices)
while Q ≠ ∅                                (while queue is not empty)
  do u ← mindistance(Q, dist)              (select/remove element of Q with min. distance)
  for all v ∈ neighbors[u]
    do if dist[v] > dist[u] + w(u, v)        (if new shortest path found)
      then d[v] ← d[u] + w(u, v)           (set new value of shortest path)
  remove u from Q
{if desired, add traceback code by updating, e.g., an array previous[v]}
return dist
```



Example I

Q: A B C D E

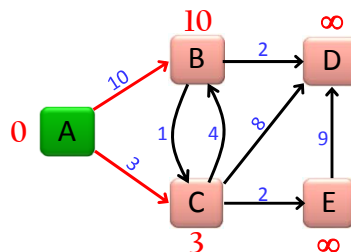
d: 0 ∞ ∞ ∞ ∞



Example II

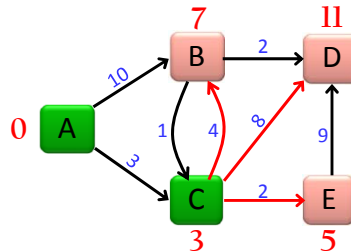
Q: A B C D E

d: 0 10 3 ∞ ∞



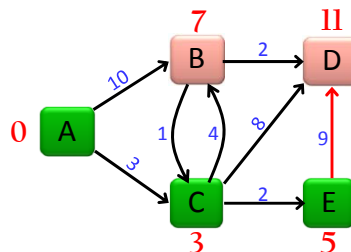
Example III

Q: A B C D E
d: 0 7 3 11 5



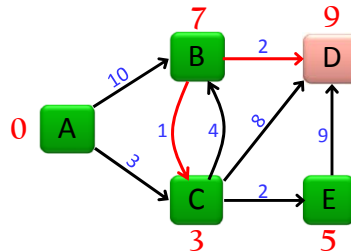
Example IV

Q: A B C D E
d: 0 7 3 11 5



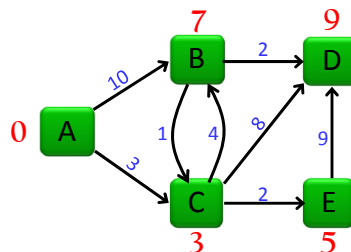
Example V

Q: A B C D E
d: 0 7 3 9 5



Example VI – The End

Q: A B C D E
d: 0 7 3 9 5



Shortest Path in a Graph

Not just good for internet communication

- mapquest/Google map
 - roads are weighted by speed limit, average traffic, ...
- epidemiology
 - “contact” network, with weight equals probability
- robot motion planning
 - if you know a map of the environment



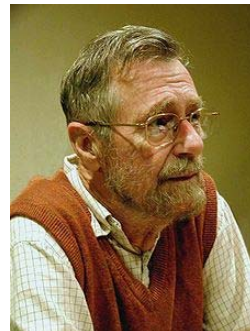
source: Wikipedia



[Edsger W. Dijkstra]

May 11, 1930 – August 6, 2002

- from theoretical physicist...
- to computer scientist
 - made a case against GOTO
 - made programming a science
 - Turing award in 1972



Graph Search

Two basic orders of search

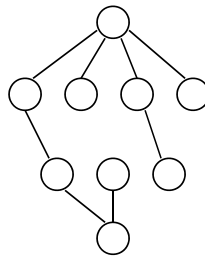
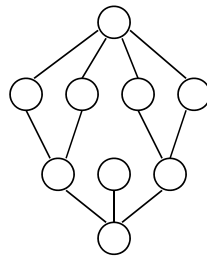
- depth first search (DFS)
 - like trees' preorder: visit node, then its neighbors
 - explore as far as possible along each branch before backtracking
- breadth first search (BFS)
 - same order as Dijkstra if equal weights
 - i.e., level by level
 - parallel version: MapReduce
 - programming model implemented in, e.g., Hadoop
 - basically, a tree of executions, then a gathering



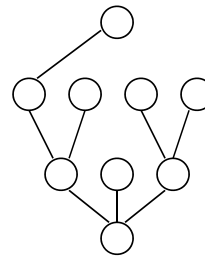
Spanning Trees

Trees assembled during search

- BFS: short and bushy
- DFS: long and stringy



BFS from top



DFS from top



Other Typical Graph Problems

All-pair shortest paths

- dyn. prog. again, called Floyd-Warshall
$$\text{shortestPath}(i, j, k) = \min(\text{shortestPath}(i, j, k-1), \text{shortestPath}(i, k, k-1) + \text{shortestPath}(k, j, k-1))$$
- if positive weights, Dijkstra's just as good
 - $O(V^3)$

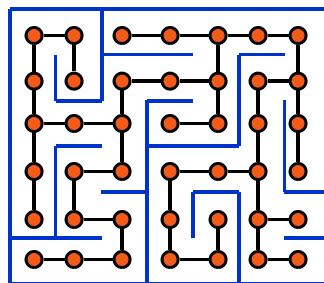
Minimum spanning tree (e.g., power lines)

- find a subgraph of graph G
 - forming a tree containing all vertices of G
 - with min sum of weights
- Prim's algorithm (same complexity as SSSP)



[Spanning Trees]

Cool way to make a maze too...



Final Words on Networking

Notion of ports

- different channels
 - IP header contains addr + port

Notion of sockets

- chat over ports
 - listen/bind,recv/send,...

Notion of layers

DNS lookup
FTP
HTTP
POP3
Telnet

UDP	53
TCP	21
TCP	80
TCP	110
TCP	23

