



Data Structures

Let's solve a maze!



**Before we start: A few
words about outlines**



Outlines

- Get thoughts out *before* writing code
 - Can revise after writing code
 - Makes code more readable
 - Does *not* replace function headers or comments
- Pseudocode versus paragraphs
 - Pseudocode makes it easier to translate to code
 - Either case, should be able to understand the algorithm from reading it
- Pseudocode
 - Should be the “English” version of your code—copying code is as useful as reading the code itself.
 - Helper functions called should be explained

Quick aside: Why you should care

- *"This is just CS2 busywork."*
 - Data structures are fundamental to CS; you'll have to know them to take future CS classes.
- *"The libraries are already written, so I don't have to know how they work."*
 - What if a library isn't available?
 - What if you need special functionality?
- *"I only need to know one data structure, and I can apply it to every situation."*
 - That's the whole point of this week's assignment...
 - Using the right data structure can improve performance

There are so many out there!

This week, we'll be working with stacks and queues, but there are lots more...

Linked lists

Sets

Hash tables

Graphs

Trees

Arrays



New topic: Binary search trees
as a simple data structure



Search trees (and why)

To find an element in a linked list, we must visit consecutive list elements until we find what we want. Not true for search trees!

BST: Average $O(\log n)$

LL: Average $O(n)$

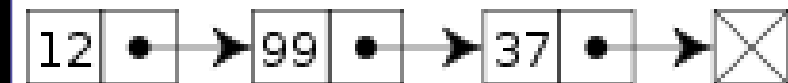
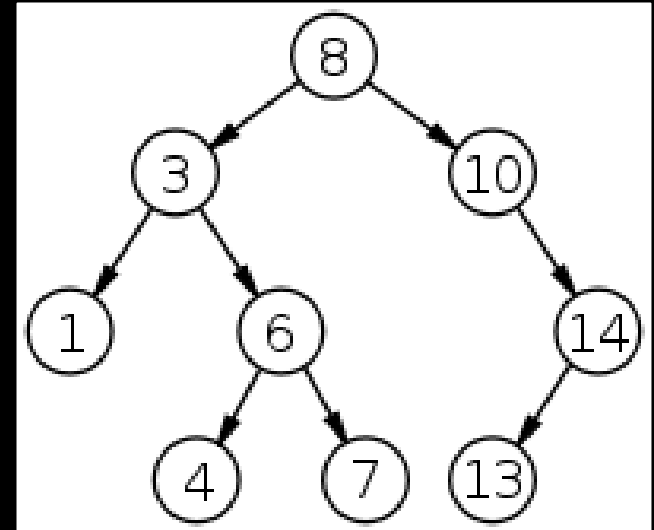
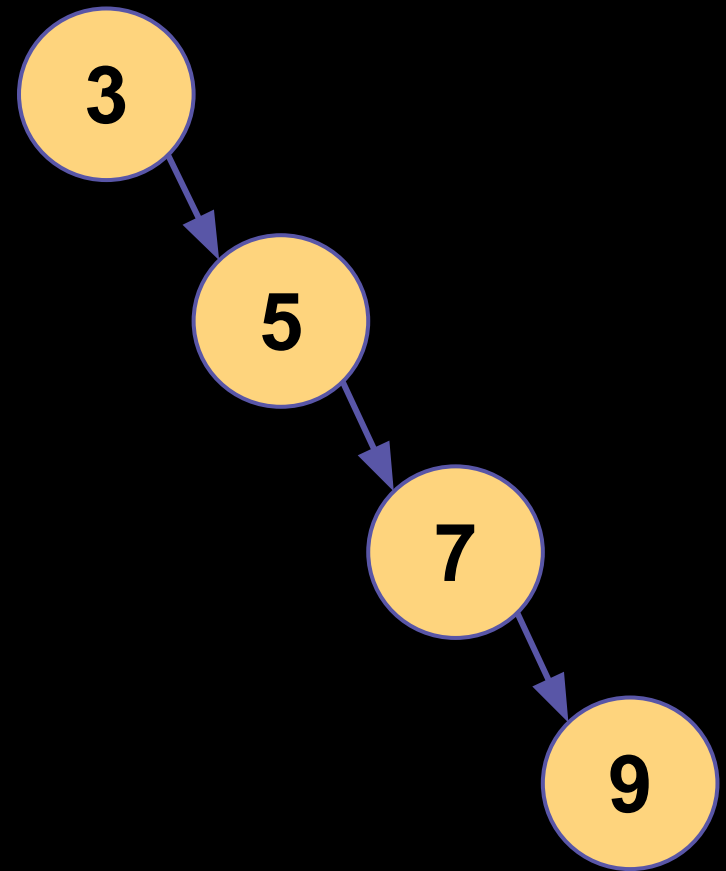


Image credit: Wikipedia

Search trees (and why)

Balance is important!
If the BST is poorly constructed, it effectively becomes a linked list, and our average search time increases.

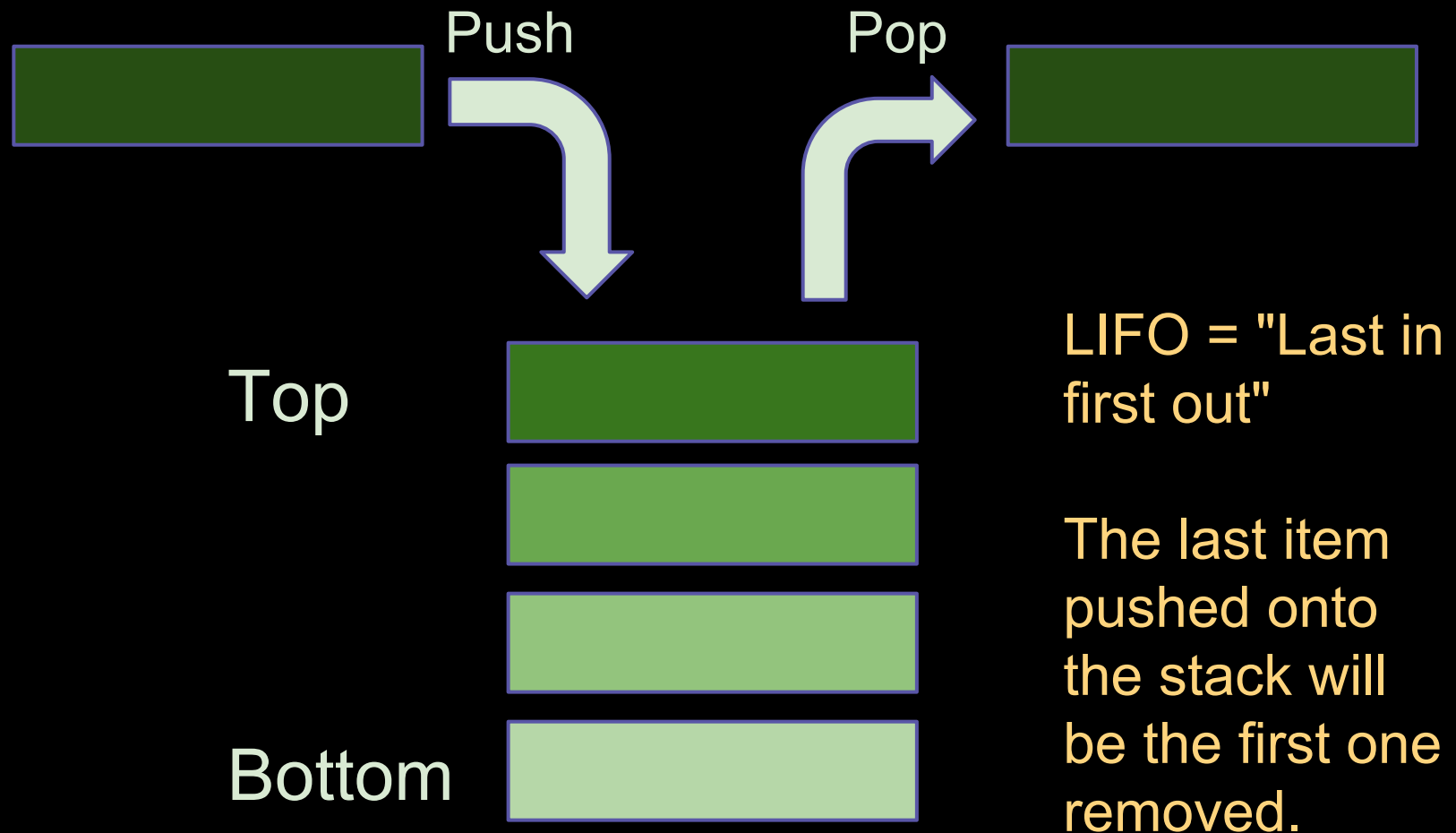




New topics: Stacks and
queues; search algorithms



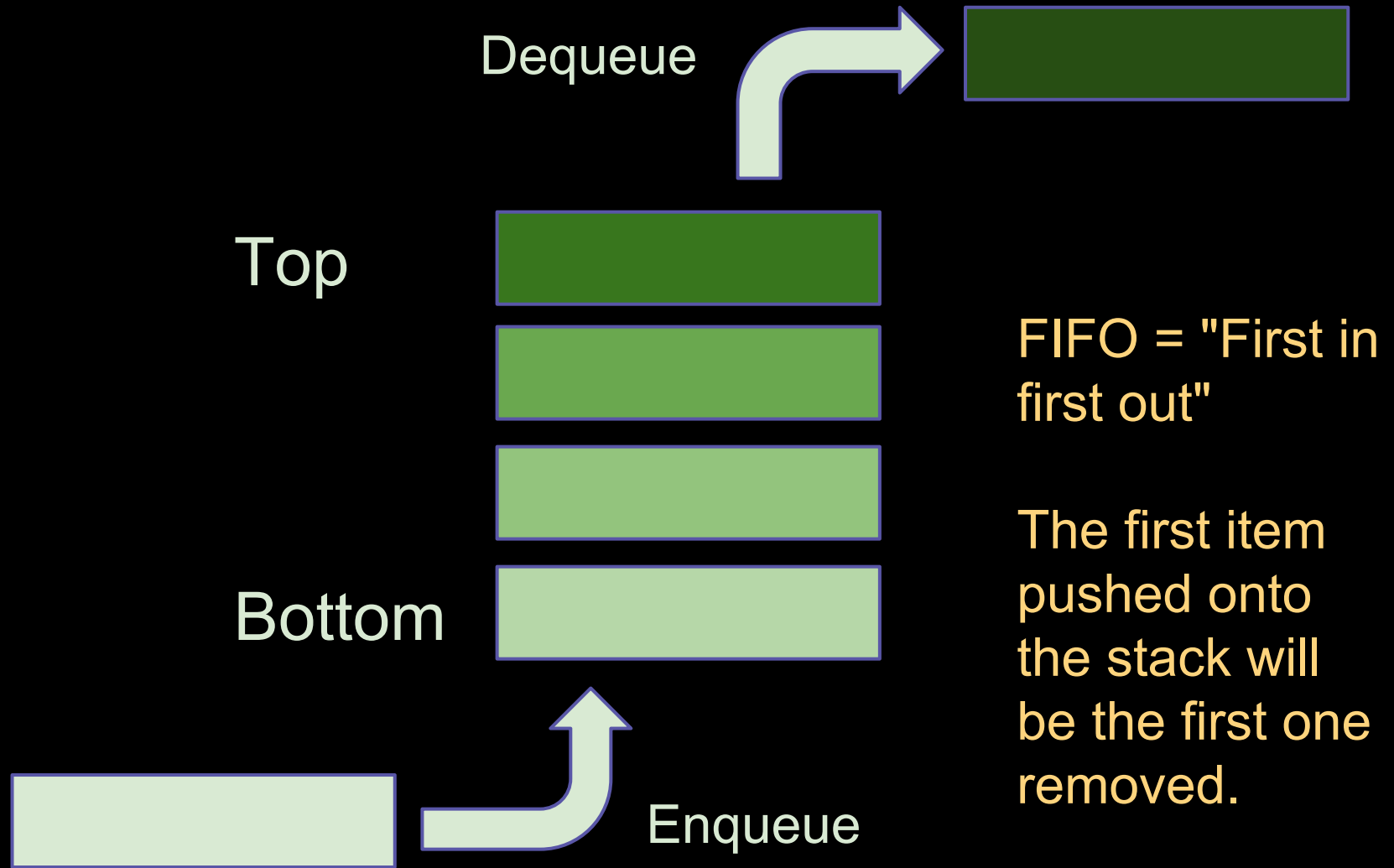
Basics of the stack



Stacks: Implementation details

- What happens if you pop from an empty stack?
- How do you handle adding the first item?
- How do you know when the stack is empty?
- One way to manage a stack:
 - Keep a pointer to the top of the stack
 - Each item stores a pointer to the item below it
- Remember LIFO: Add and remove items from the top of the stack.

Basics of the queue



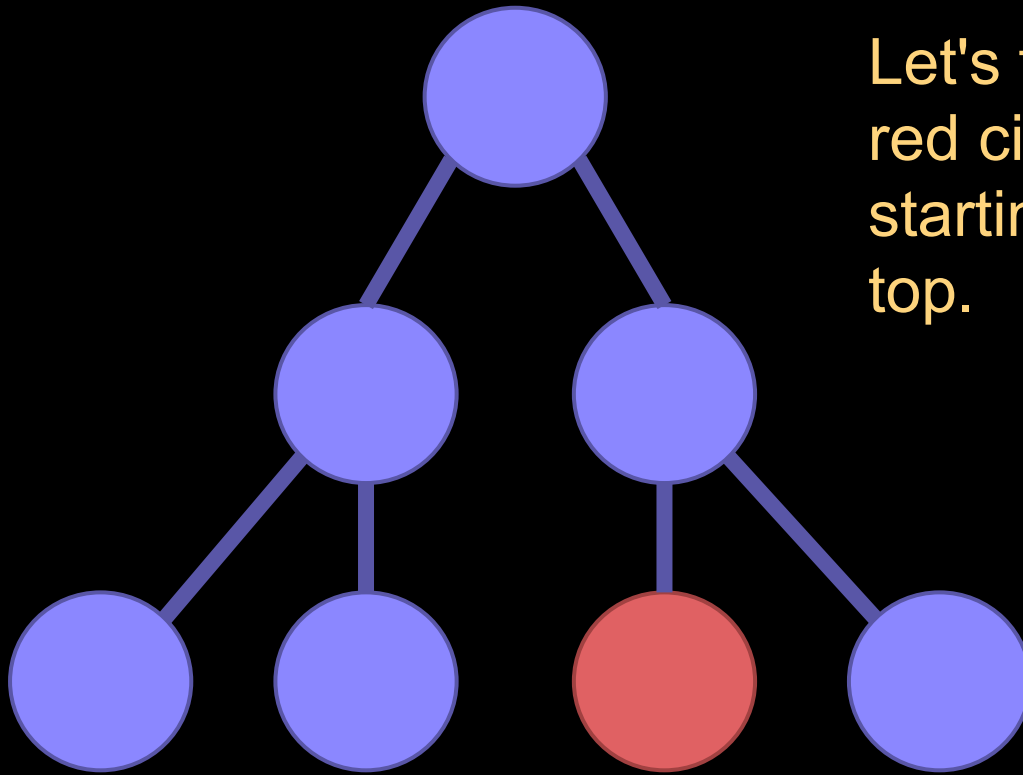
Queues: Implementation details

- What happens if you dequeue from an empty queue?
- How do you handle adding the first item?
- How do you know when the queue is empty?
- One way to manage a queue:
 - Keep a pointer to the front and rear of the queue
 - Each queue item stores a pointer to the next item in the queue
- Remember FIFO: Add new items to the rear, and remove items from the front.

Introducing the depth-first search (DFS)

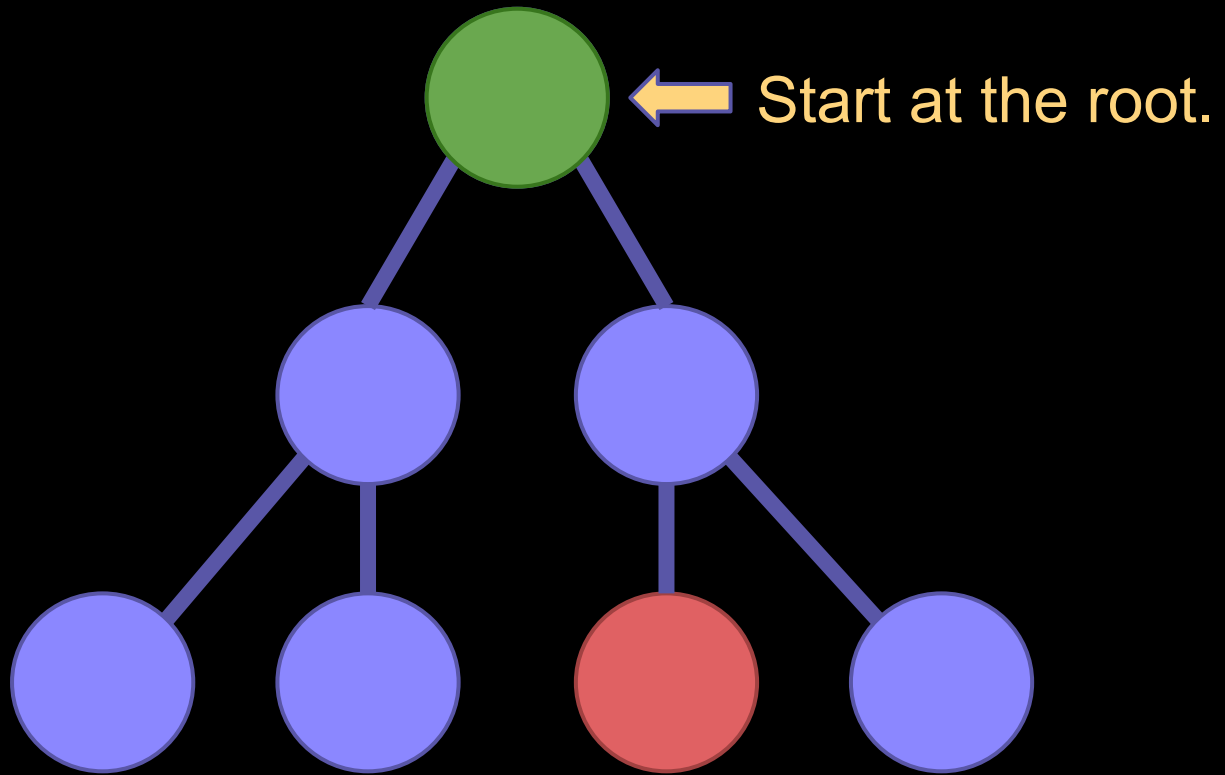
- DFS searches as far as possible along a branch before backtracking.
- From any node, we move to the first unvisited child node until we can go no further (i.e. the node we have found has no children).
- Then backtrack until we hit a node with unvisited children and repeat the process.

Solve something easy with DFS



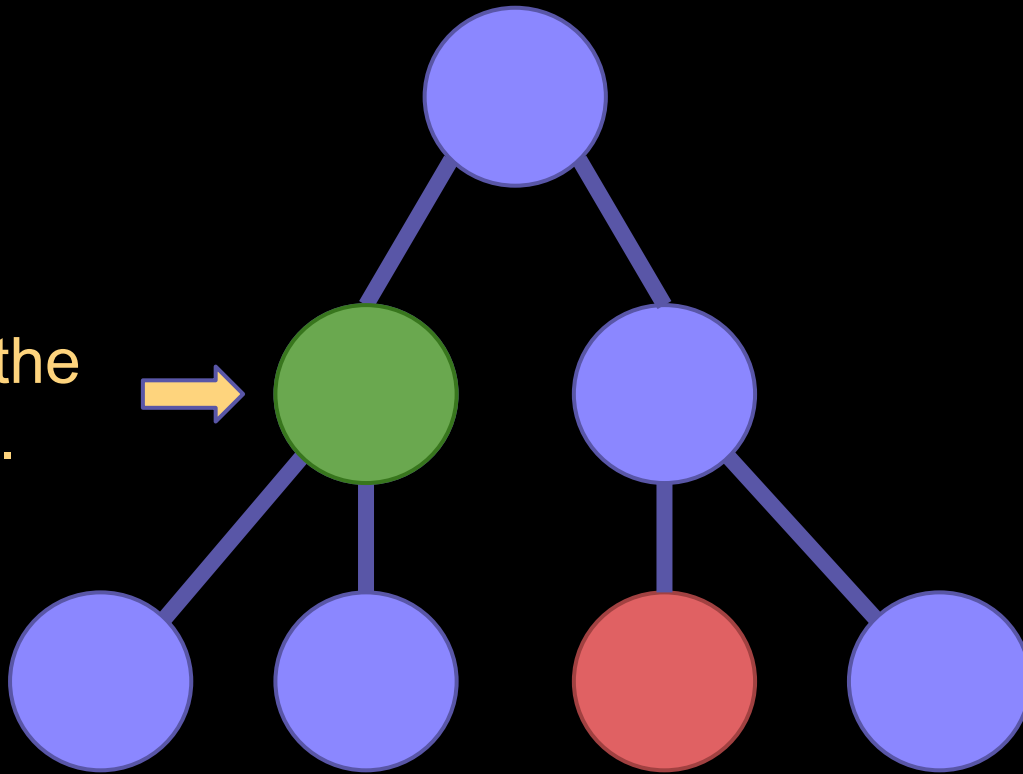
Let's find the
red circle,
starting at the
top.

Solve something easy with DFS



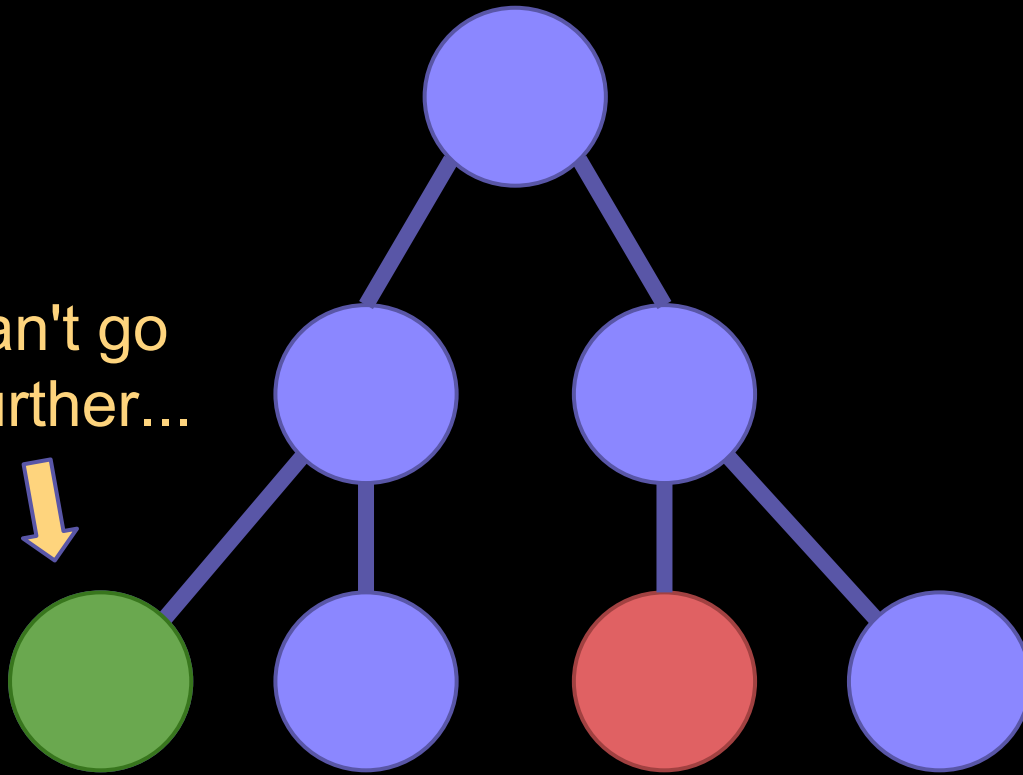
Solve something easy with DFS

Move to the
first child.



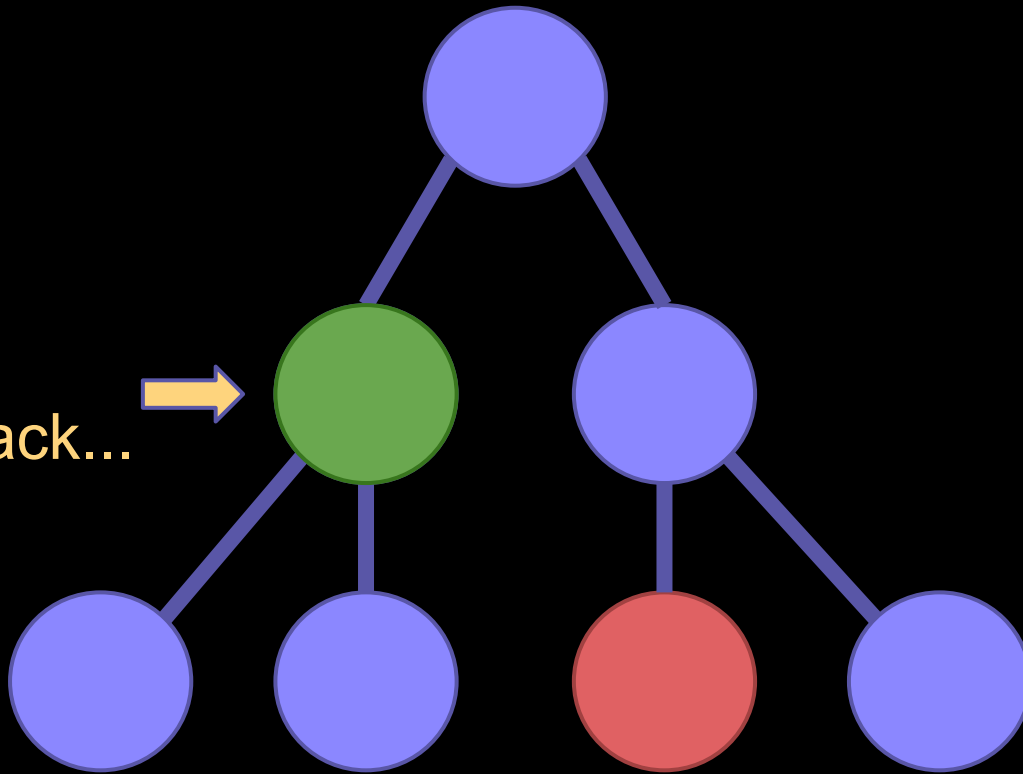
Solve something easy with DFS

We can't go
any further...

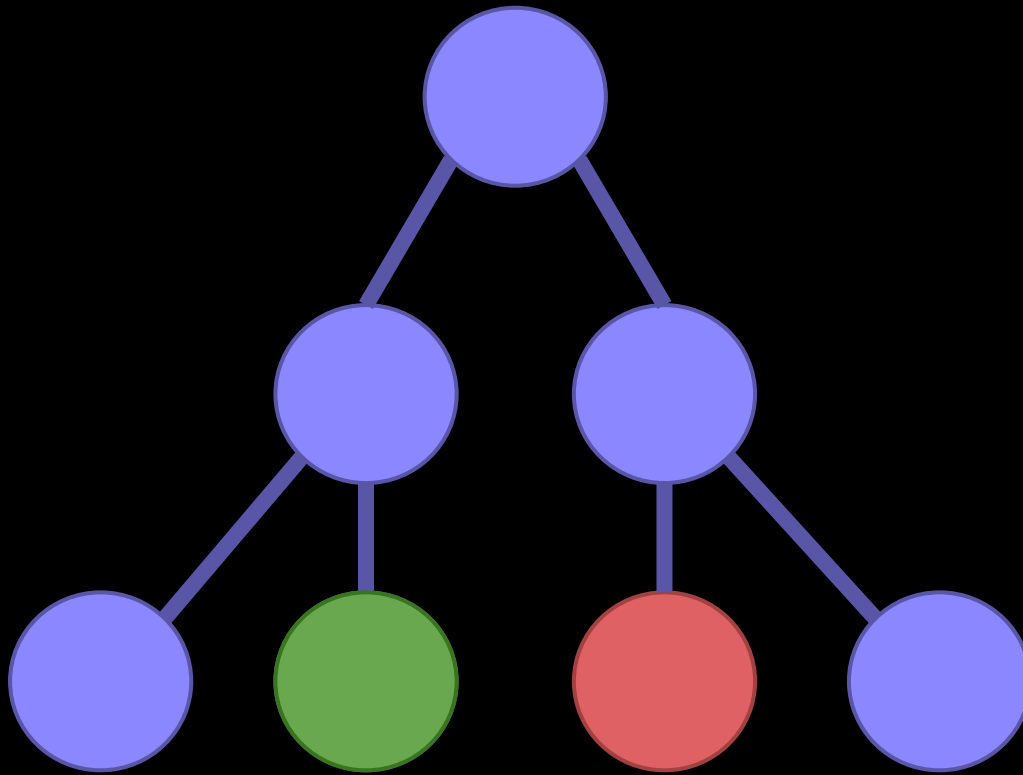


Solve something easy with DFS

... so
backtrack...



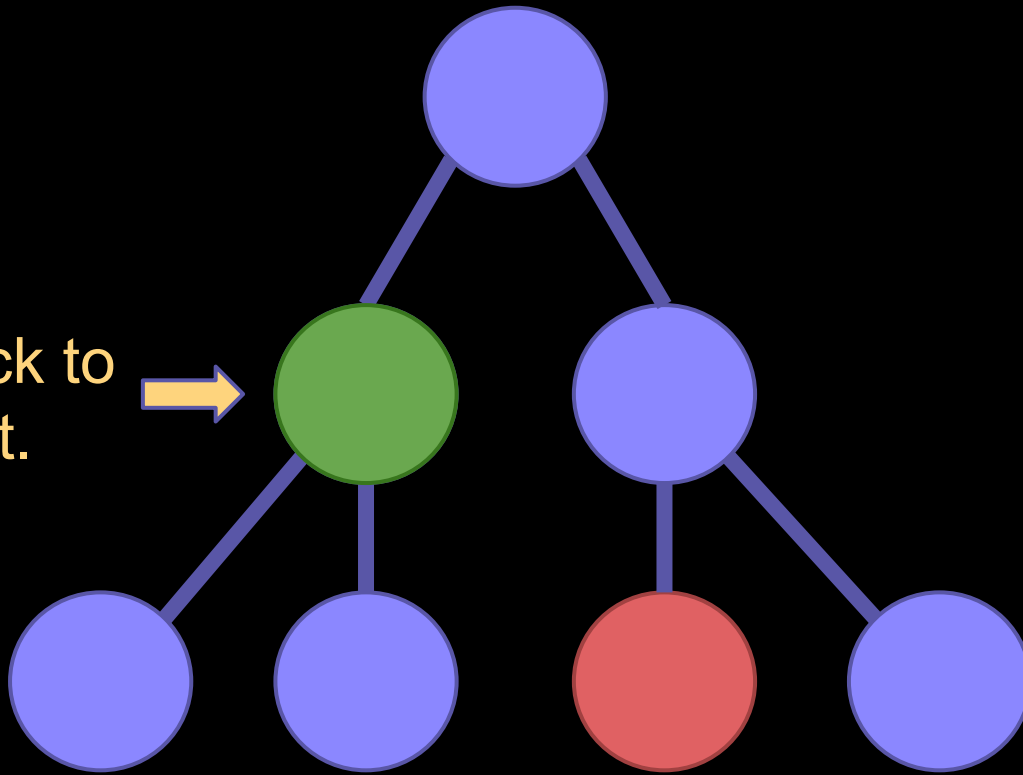
Solve something easy with DFS



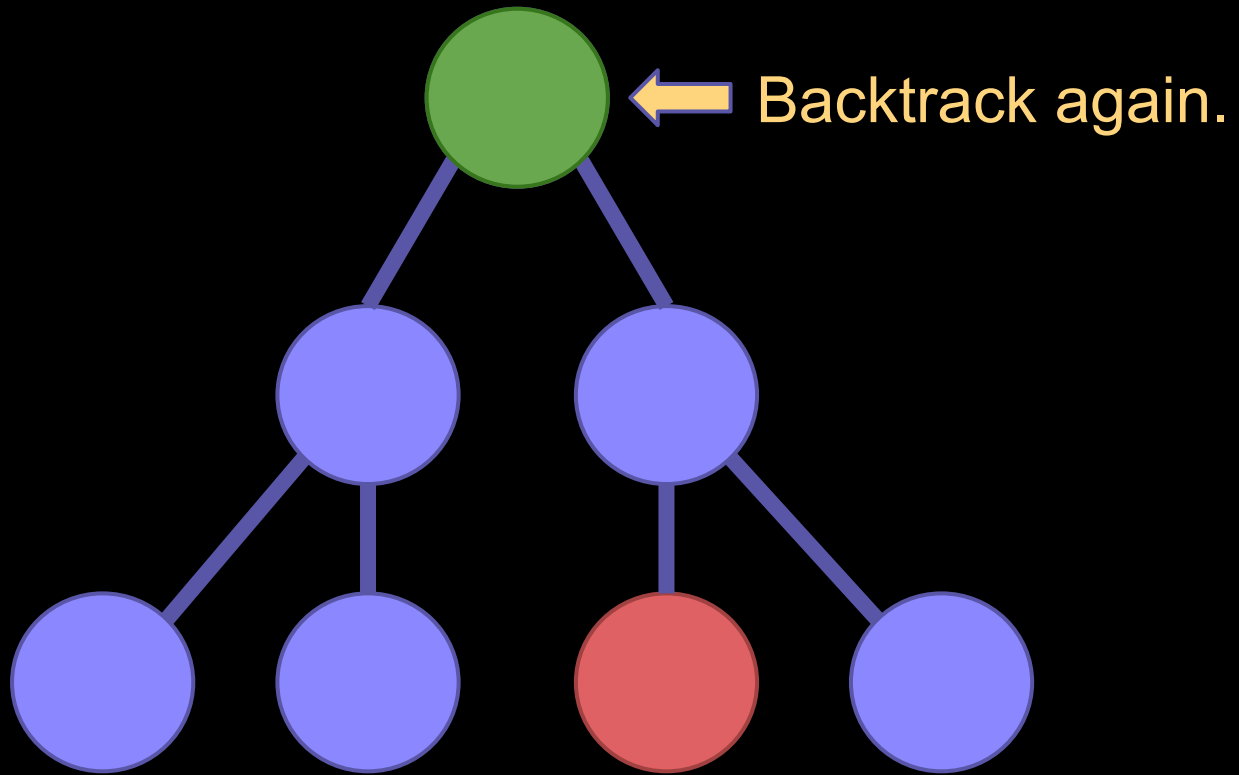
... and visit
the next child.

Solve something easy with DFS

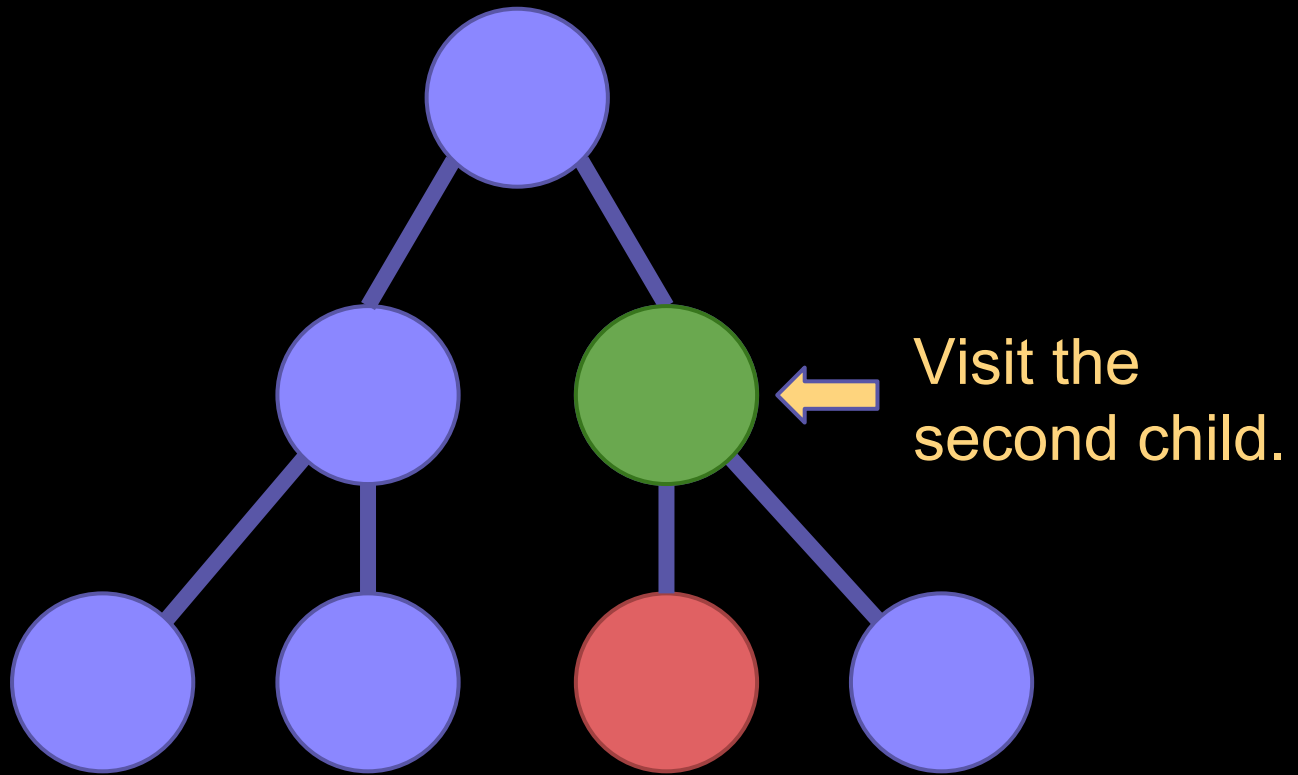
We're back to
the parent.



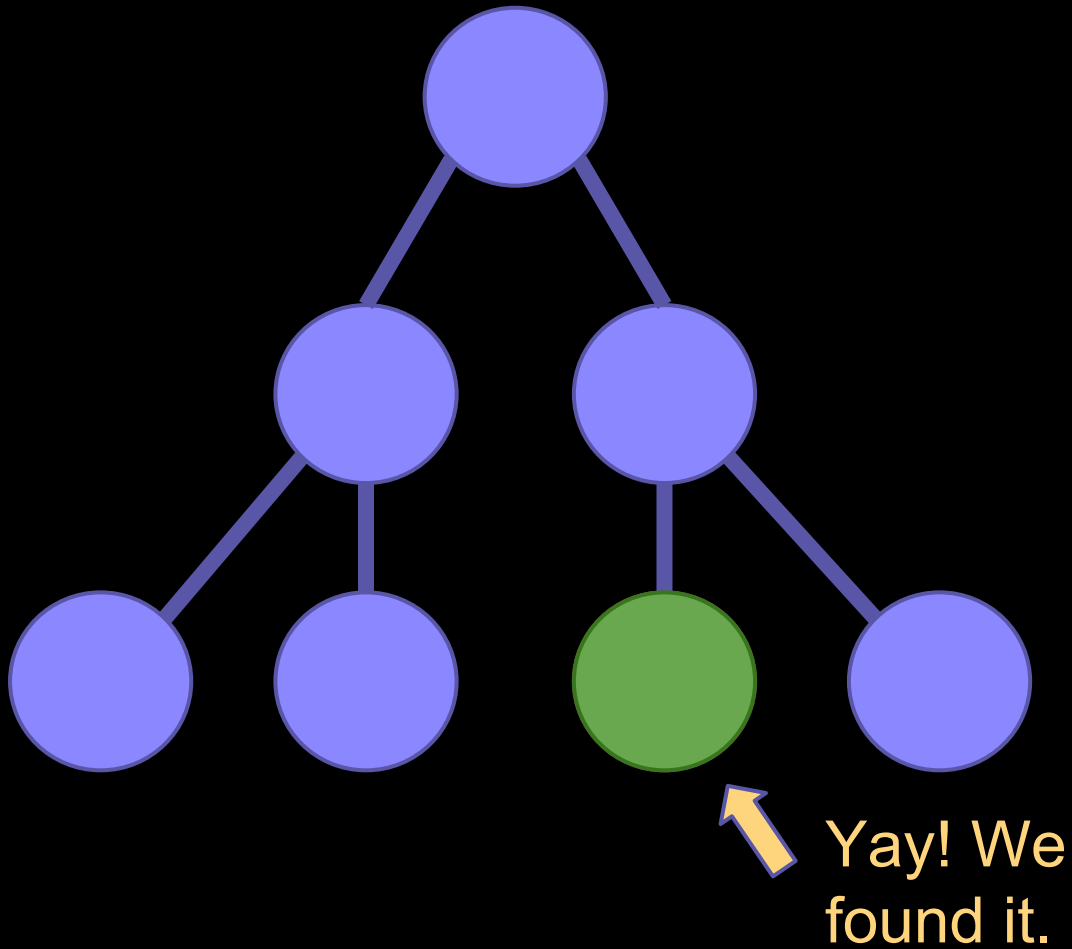
Solve something easy with DFS



Solve something easy with DFS



Solve something easy with DFS



What does DFS have to do with data structures?

Some DFS pseudocode with a stack...

```
Push the root node
```

```
while stack is not empty:
```

```
    Mark the current  
    node as visited
```

```
    if current node is end:
```

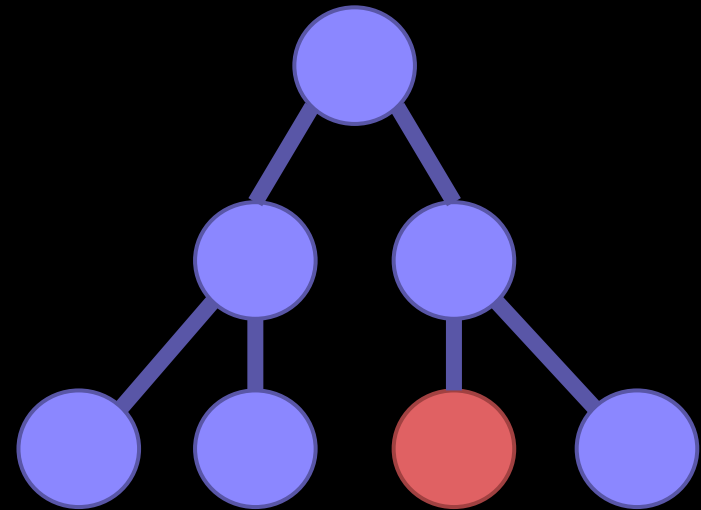
```
        Stop the search
```

```
    else:
```

```
        Push the next unvisited  
        child node onto the
```

```
stack
```

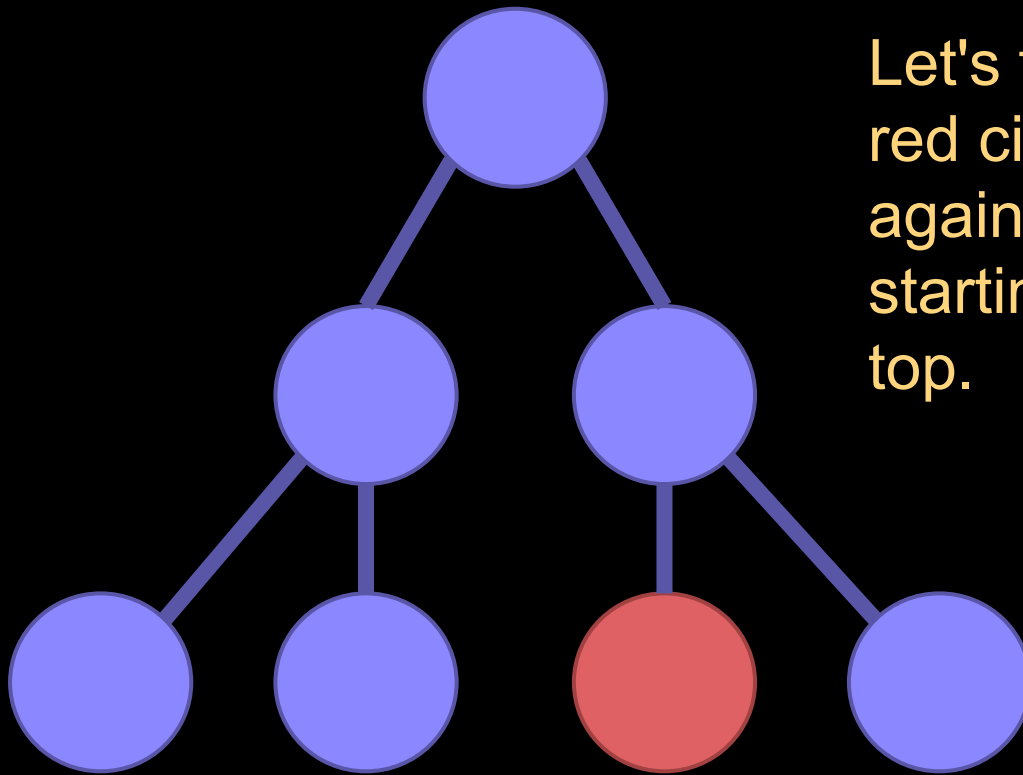
Backtracking is as simple as popping items from the stack.



Introducing the breadth-first search (BFS)

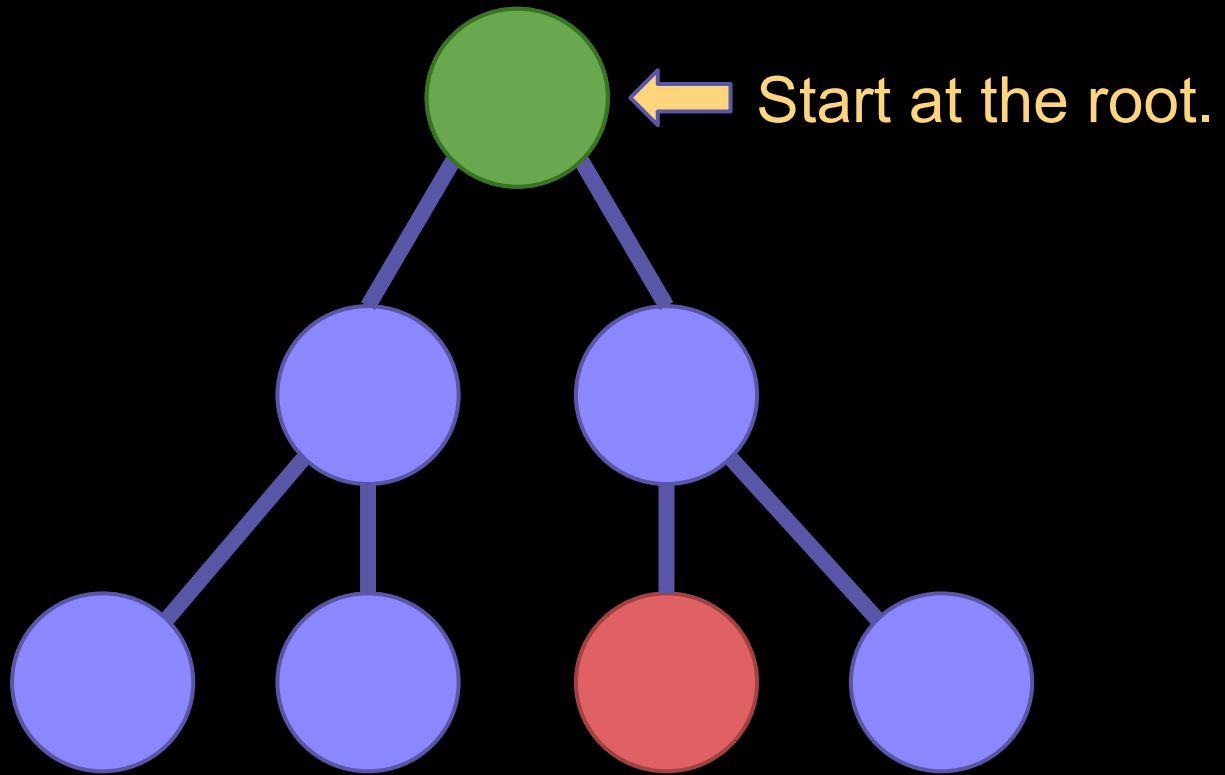
- BFS searches each level of nodes in turn (root, root's children, root's children's children...).
- Though it can certainly reach the end of a branch, it never backtracks.

Solve something easy with BFS



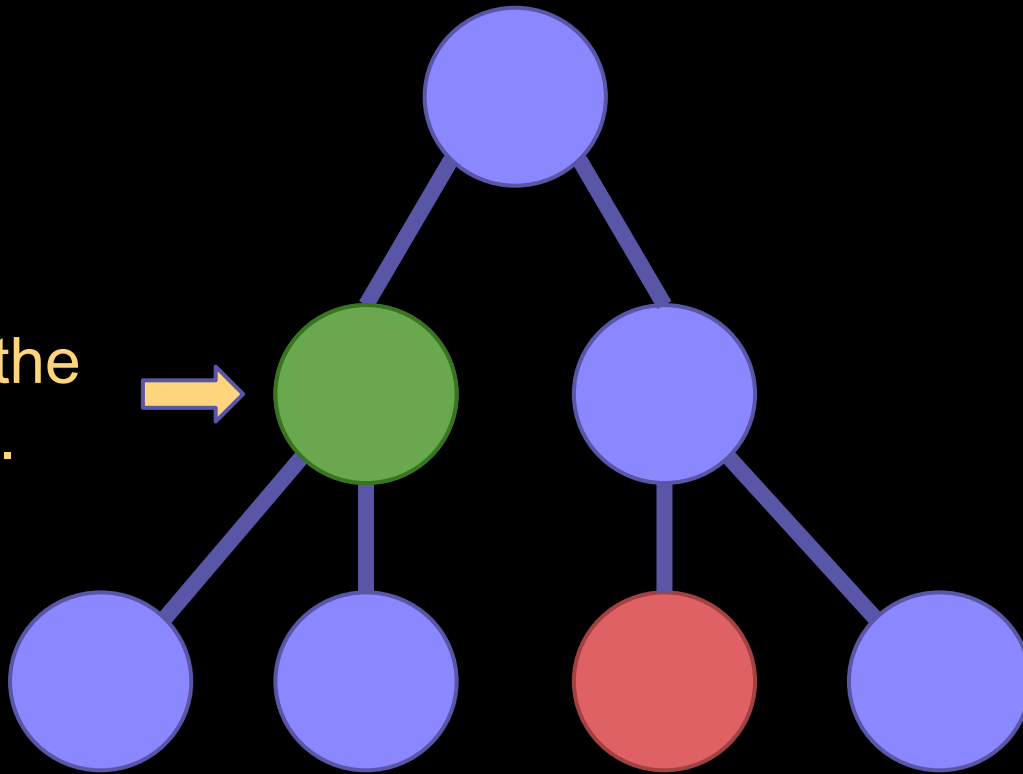
Let's find the red circle again, still starting at the top.

Solve something easy with BFS

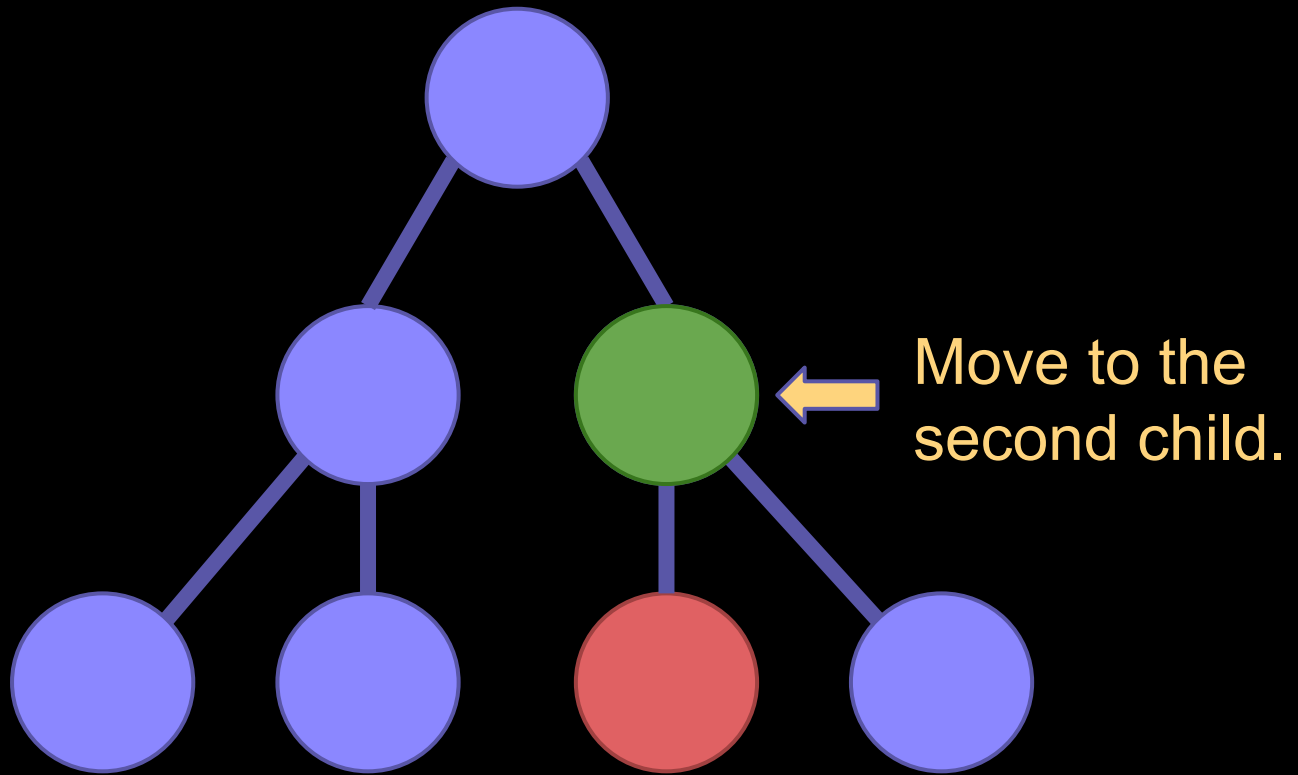


Solve something easy with BFS

Move to the
first child.

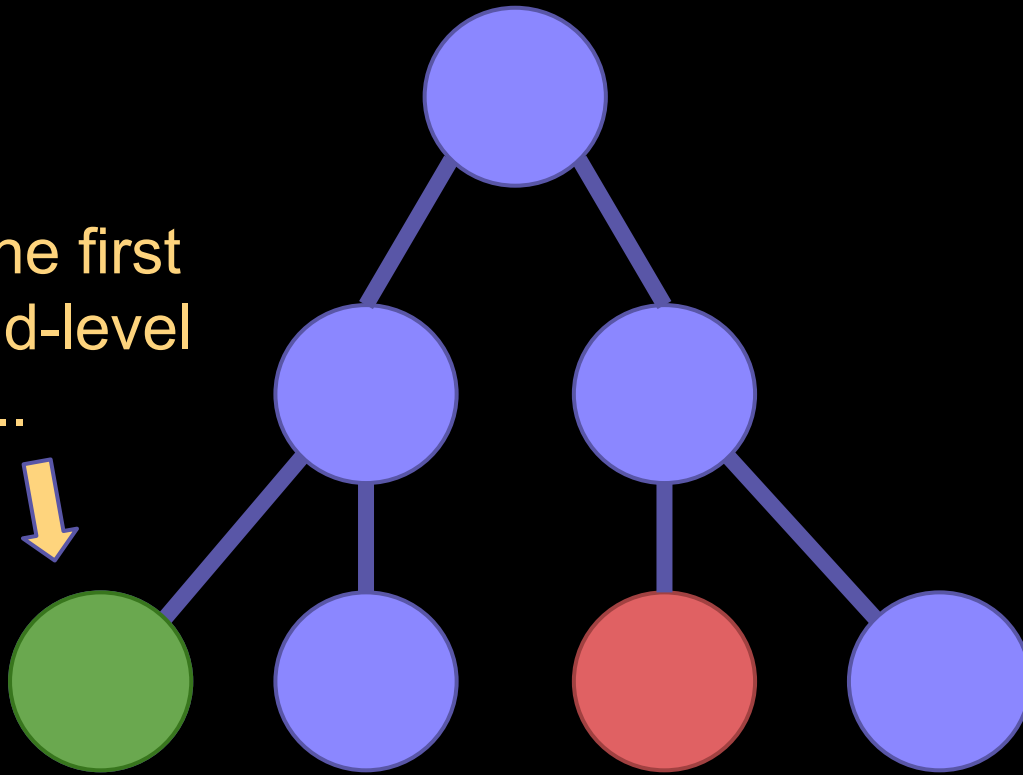


Solve something easy with BFS

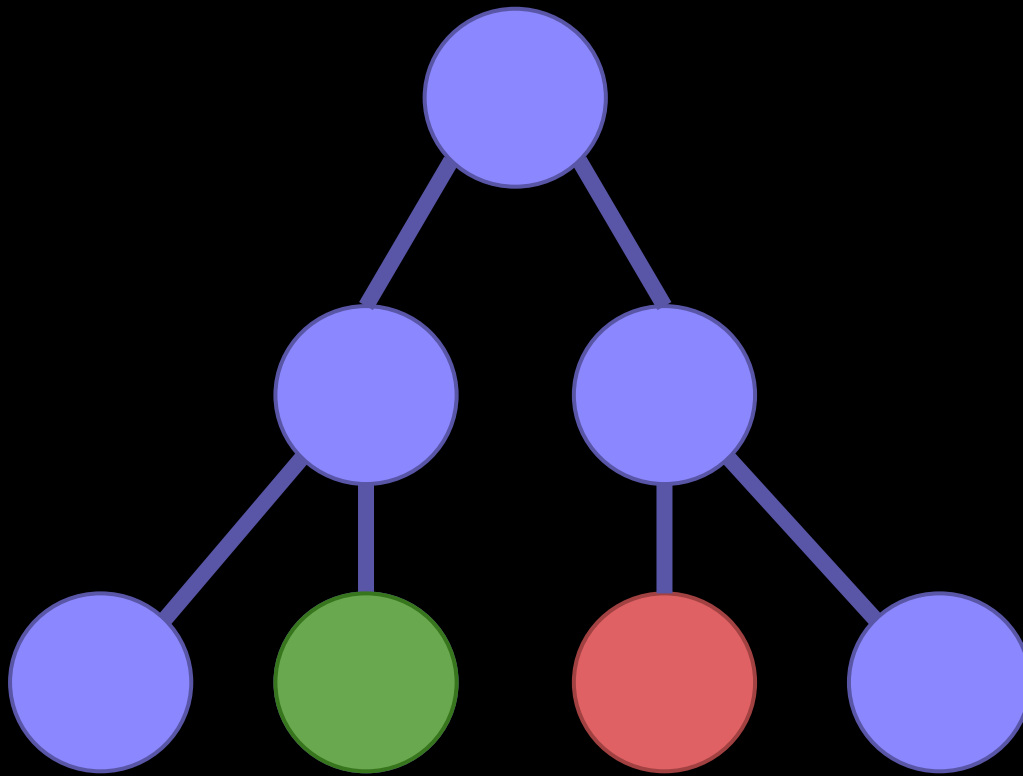



Solve something easy with BFS

Visit the first
second-level
node...

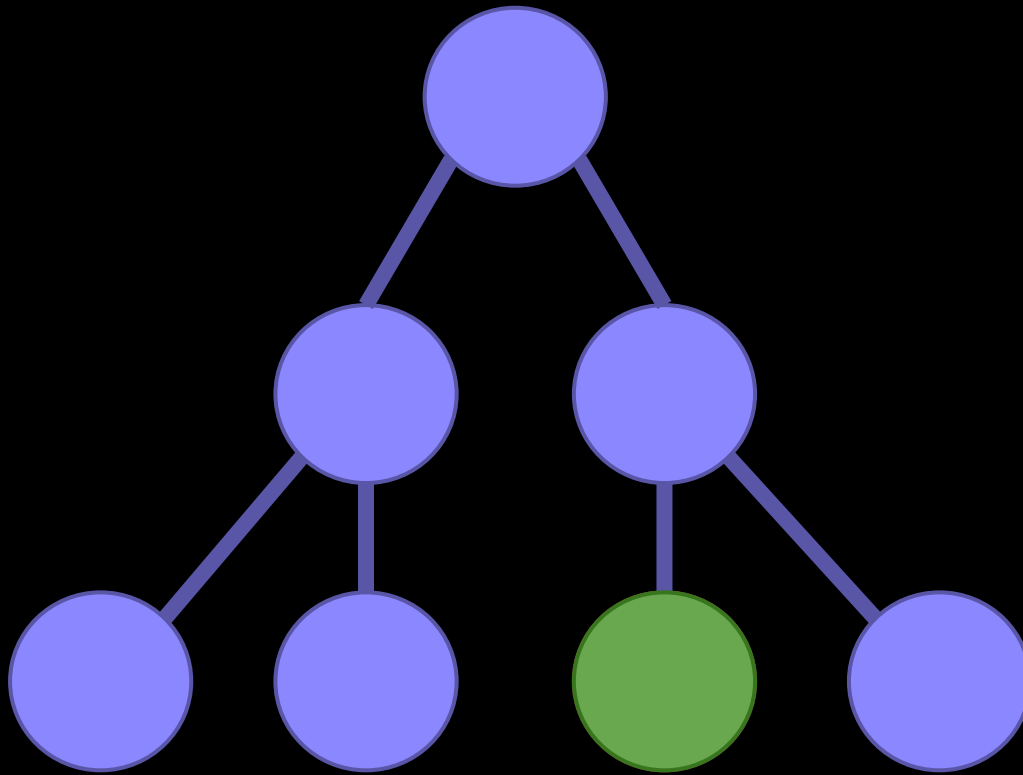


Solve something easy with BFS



... then the
second... 

Solve something easy with BFS



... then the
third. Found it!

What does BFS have to do with data structures?

Some BFS pseudocode with a queue...

```
Enqueue the first node
```

```
while queue is not empty:
```

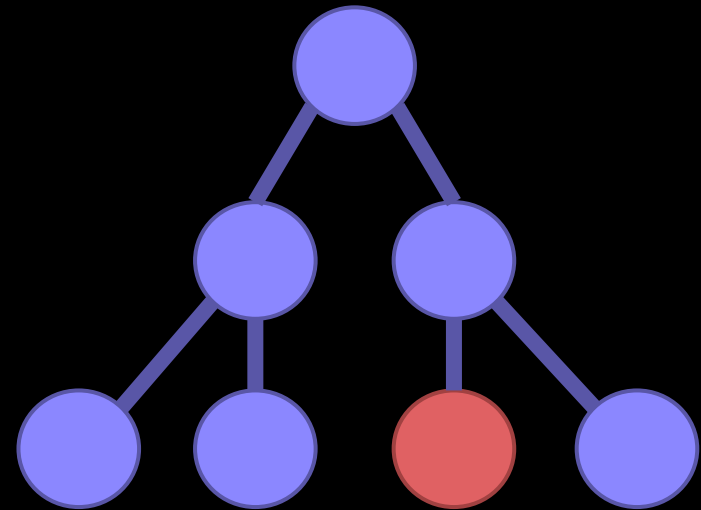
```
    Mark the current node as  
    visited
```

```
    if current node is end:
```

```
        Stop the search
```


```
    else:
```

```
        Enqueue all unvisited  
        child nodes
```




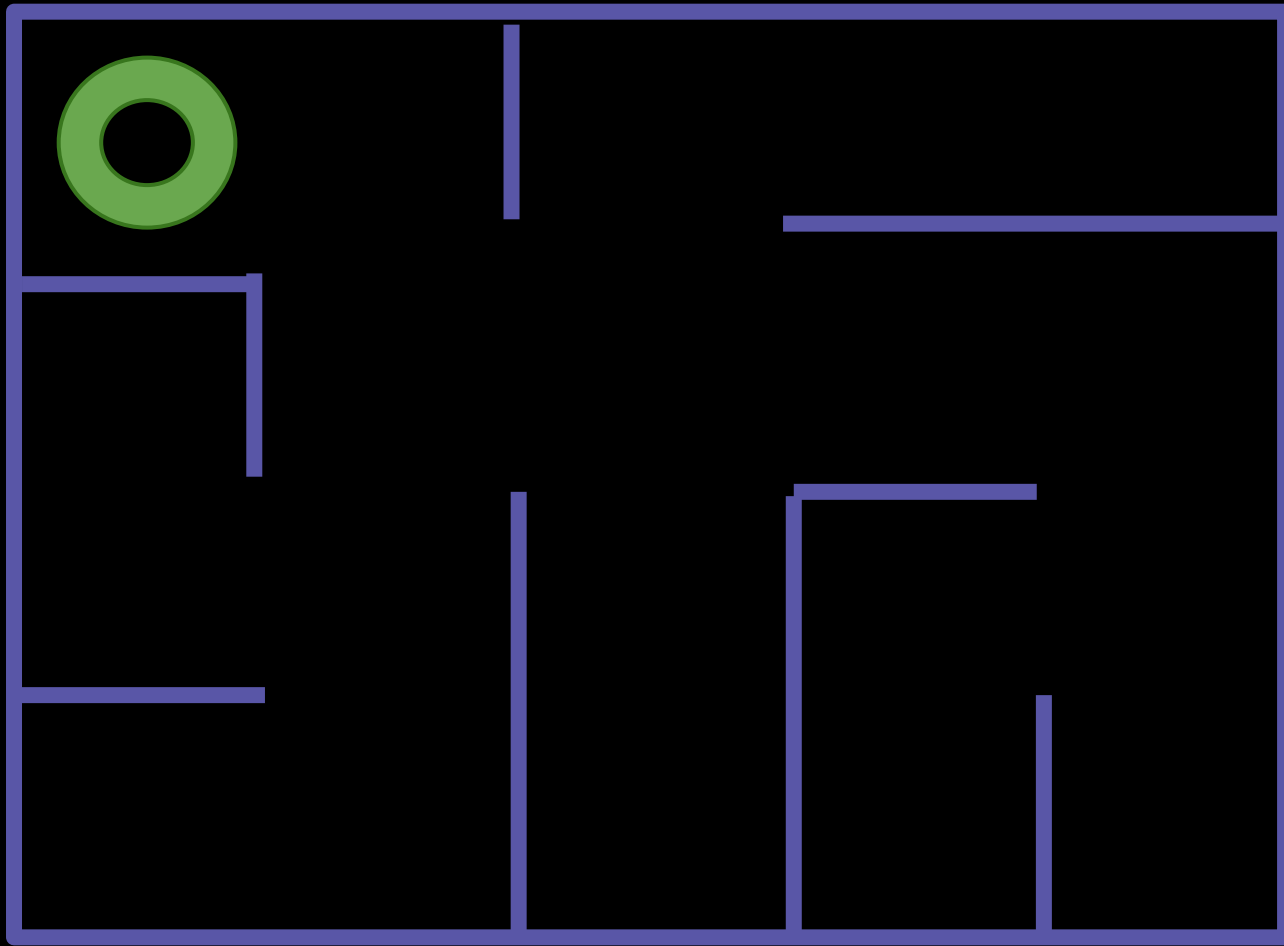
From trees to mazes

- Trees aren't much different than mazes.
- A node of the tree corresponds to a square of the maze.
- The children of a node correspond to the squares you can move to from the current square.
- You have to keep track of where you've been!

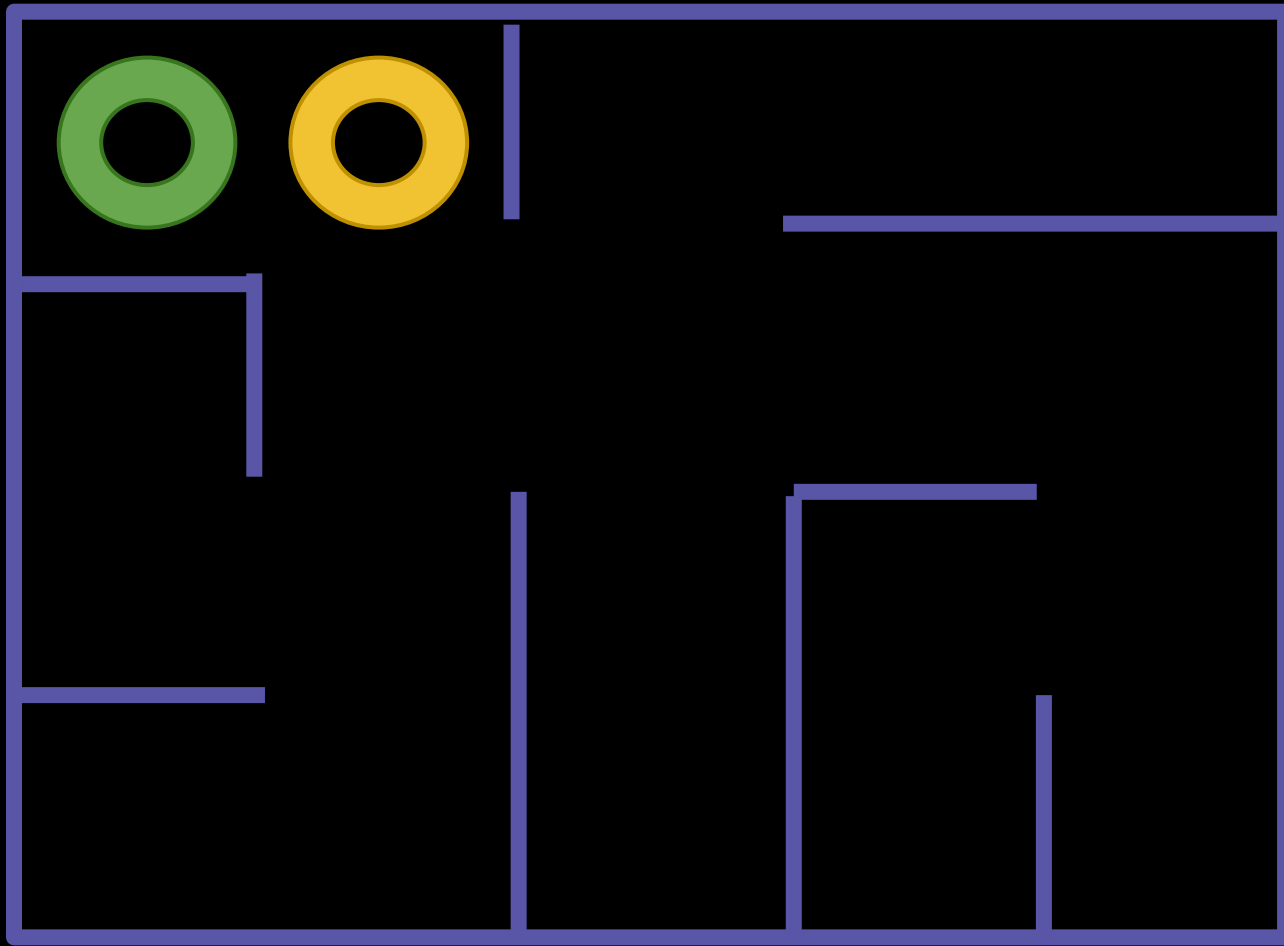


**But what does this
have to do with
mazes???**

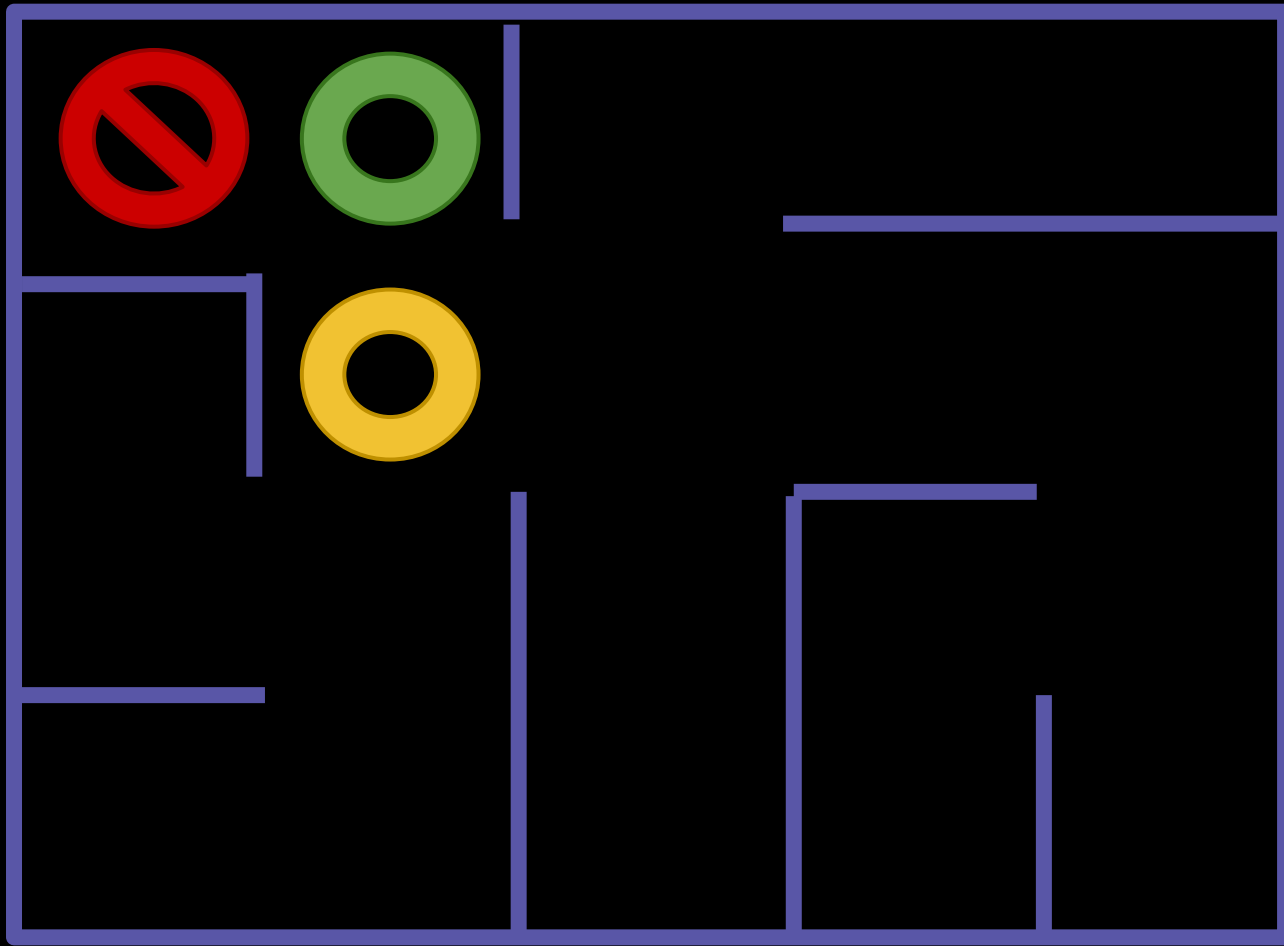




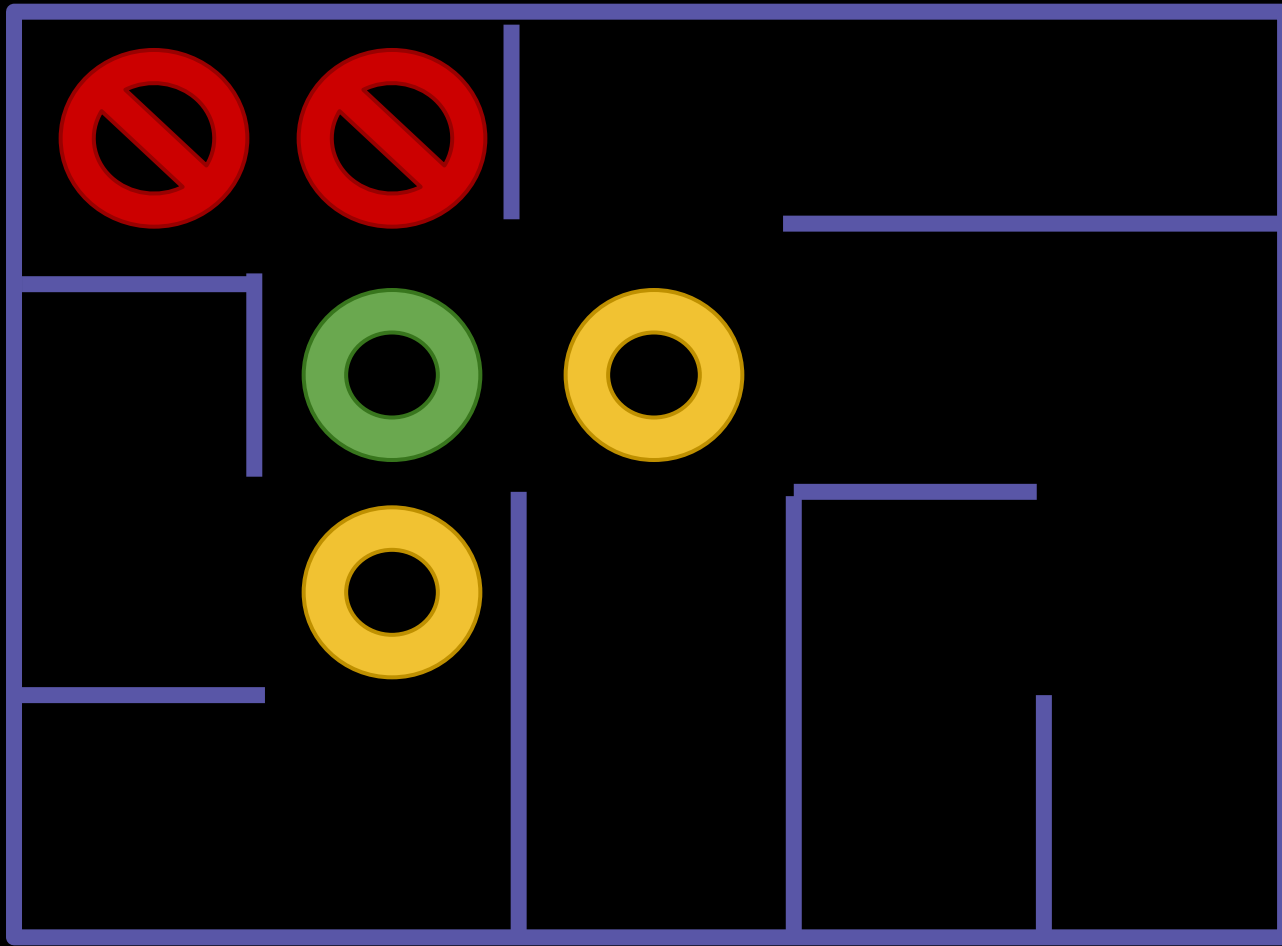
A maze can be viewed as a tree whose node is your starting point in the maze and every possible adjacent move from a node is a child.



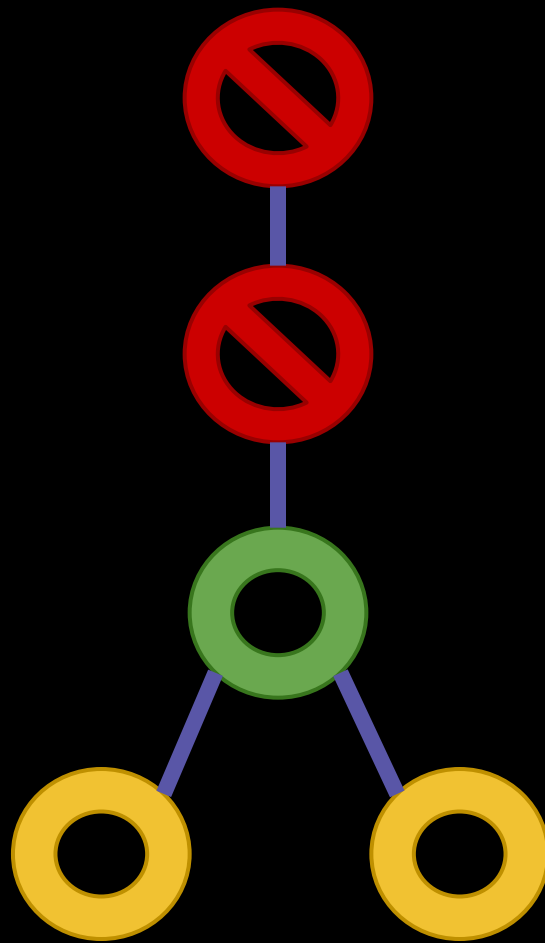
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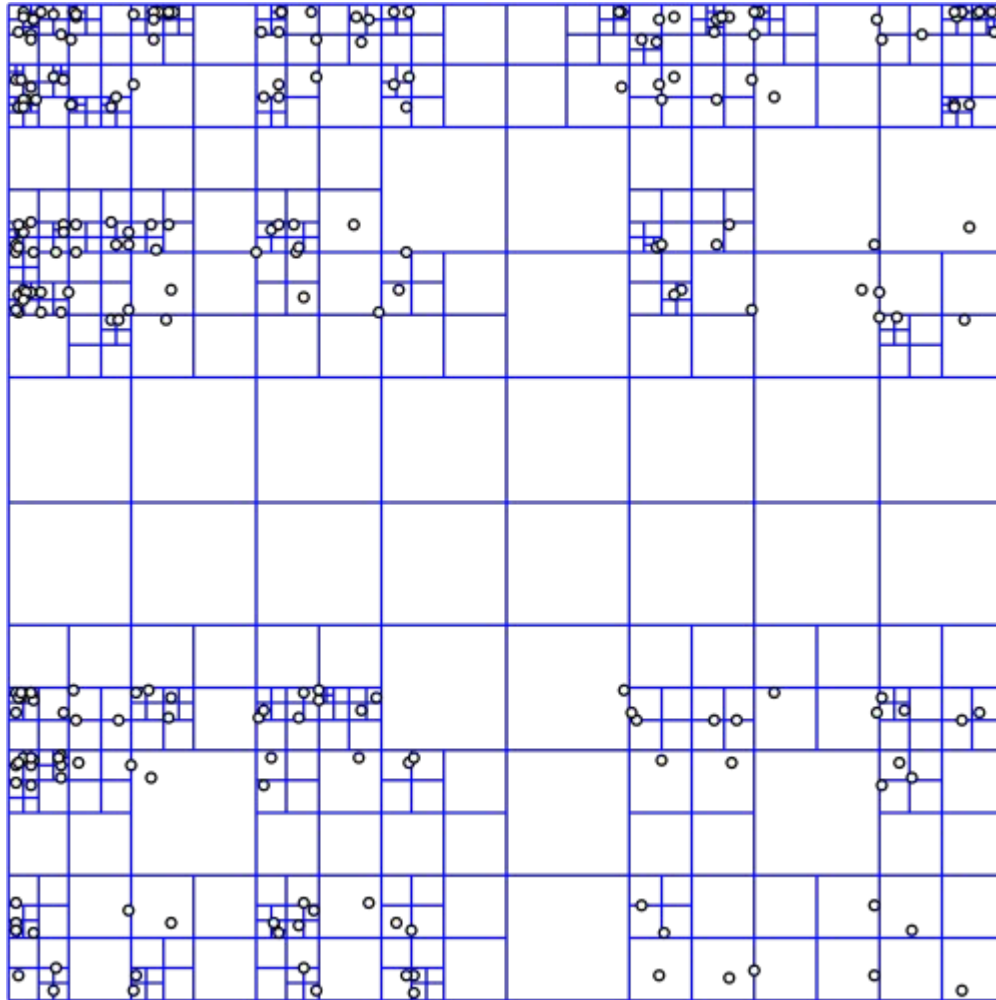
The tree equivalent to the maze might look something like this; hopefully, you can see that mazes and trees are basically the same thing, so you can search a maze with BFS and DFS.

Notes

- Read the supplied code before starting
- In `DepthFirstSolver::get_path()`, do not use `push()`
- The stack and queue themselves should be linked lists, not `std::vector`'s
- Comment your code
- Don't delete files that running "make clean" wouldn't delete

Advanced topic: Quadtrees (or how to organize spatial points)

Quadrees



No rectangle
(region)
contains more
than one point!

Image credit: Wikipedia

Good Luck

