

$$\log_{\sqrt[3]{100}} \sqrt[6]{0,1} = z \rightarrow \left(\sqrt[3]{100}\right)^z = \sqrt[6]{0,1} \rightarrow$$

$$100^{\frac{z}{3}} = (0,1)^{\frac{1}{6}} \rightarrow (10^2)^{\frac{z}{3}} = (10^{-1})^{\frac{1}{6}} \rightarrow 10^{\frac{2z}{3}} = 10^{-\frac{1}{6}} \rightarrow$$

$$\frac{2z}{3} = -\frac{1}{6} \rightarrow 12z = -3 \rightarrow z = -\frac{3}{12} \rightarrow z = -\frac{1}{4}$$

$$\therefore S = X + Y + Z =$$

$$S = -\frac{9}{4} - \frac{9}{2} - \frac{1}{4} \rightarrow \frac{-9-18-1}{4} \rightarrow \frac{-28}{4} \rightarrow \frac{-14}{2}$$

$$\therefore S = -7 //$$

B115. Resolução: ☒

$$\begin{aligned} d) 8^{\log_4 5} &\rightarrow (2^3)^{\log_4 5} \rightarrow 2^{3 \cdot \log_4 5} \rightarrow 2^{3 \cdot \log_2 2^{\frac{1}{2}} 5} \rightarrow \\ &\rightarrow 2^{\frac{1}{2} \cdot 3 \log_2 5} \rightarrow 2^{\frac{3}{2} \cdot \log_2 5} \rightarrow \cancel{2^{\log_2 5^{\frac{3}{2}}}} \rightarrow \\ &\rightarrow 5^{\frac{3}{2}} \rightarrow \sqrt[2]{5^3} \rightarrow \sqrt[2]{5^2 \cdot 5} \rightarrow 5\sqrt{5} /// \end{aligned}$$

$$\begin{aligned} &8^{\log_4 5} \rightarrow (2^3)^{\log_4 5} \rightarrow \left(2^{\log_4 5}\right)^3 \rightarrow \left(2^{\log_2 2^{\frac{1}{2}} 5}\right)^3 \rightarrow \\ &\left(2^{\frac{1}{2} \cdot \log_2 5}\right)^3 \rightarrow \left(2^{\log_2 5^{\frac{1}{2}}}\right)^3 \rightarrow \left(5^{\frac{1}{2}}\right)^3 \rightarrow 5^{\frac{3}{2}} \\ &\sqrt[2]{5^3} \rightarrow 5\sqrt{5} /// \end{aligned}$$