

ECOM 2001 Term Project on NVDA, CMCSA and EA stocks

Aidan Daggett 19786975

```
# loading required libraries
library(tidyquant)
library(tidyverse)
library(broom)
library(knitr)
library(kableExtra)
library(ggplot2)
library(plotly)
library(gridExtra)
```

1. Importing stocks data

```
stocks <- c("NVDA", "CMCSA", "EA") %>%
  tq_get(get = "stock.prices", from = "2000-01-01") %>%
  select(symbol, date, adjusted)

head(stocks, n = 6) %>%
  kable(caption = "selected stocks data")
```

2. The Analysis

2.1. Plot prices over time.

```
# time series plot for the three stocks
NVDA = stocks[stocks$symbol=="NVDA",]
CMCSA = stocks[stocks$symbol=="CMCSA",]
EA = stocks[stocks$symbol=="EA",]
plot1 <- ggplot(NVDA, aes(x=date, y=adjusted)) +
  geom_line(color="darkblue") + labs(title="NVDA prices")
plot2 <- ggplot(CMCSA, aes(x=date, y=adjusted)) +
```

Table 1: selected stocks data

symbol	date	adjusted
NVDA	2000-01-03	0.895542
NVDA	2000-01-04	0.871630
NVDA	2000-01-05	0.842934
NVDA	2000-01-06	0.787934
NVDA	2000-01-07	0.801086
NVDA	2000-01-10	0.827391

```

    geom_line(color="orange")+labs(title="CMCSA prices ")
plot3 <- ggplot(EA,aes(x=date,y=adjusted))+
    geom_line(color="tomato")+labs(title="EA prices")
grid.arrange(plot1,plot2,plot3,ncol=3)

```

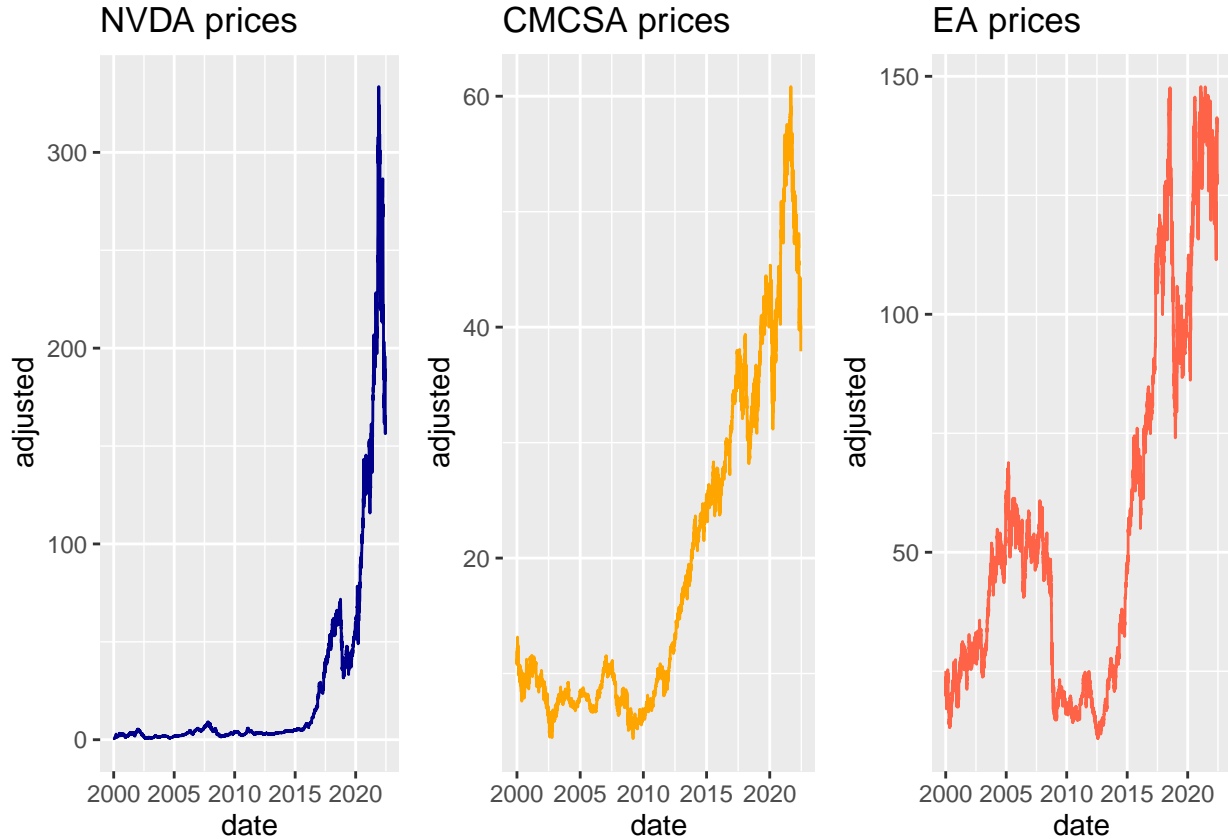


Figure 1: Time series of stocks prices

NVDA: The stock prices were very low and stationary from 2000 to around 2016 after when they increased rapidly with cyclic patterns. The prices were at their maximum in 2021, but could not maintain that price where its followed by a decreasing trend.

CMCSA: The stock prices were low from 2000 to 2010. Since 2010, the prices have been on sharp increasing trend with seasonal properties. This stock reaches its peak in 2021, falling immediately thereafter.

EA: EA stock prices started in 2000 with an upward trend where they rose for 5 yrs to 2005, then started to depreciate. At around 2008, EA stock prices fell sharply to where they were in 2000 and remained so with some seasonal rise and falls up to mid-2012. The prices then skyrocketed, reaching their peak in 2018 where they immediately falls again in 2019 and 2020, but rises in 2021.

2.2.

Given the formula:

$$r_t = 100 * \ln \left(\frac{P_t}{P_{t-1}} \right)$$

```

# percentage returns for each stock
stocks <- stocks %>%group_by(symbol) %>%
  mutate(per_returns=(100*(log(adjusted)-log(lag(adjusted))))
stocks <- na.omit(stocks)
# subset percentage returns for each stock
NVDA_RT=stocks[stocks$symbol=="NVDA",]
CMCSA_RT=stocks[stocks$symbol=="CMCSA",]
EA_RT=stocks[stocks$symbol=="EA",]
# rendering plots fro the percentage returns
plt1 <-ggplot(CMCSA_RT,aes(x=date,y=per_returns))+geom_line(color="darkblue")+labs(title="NVDA percentage returns")
plt2 <-ggplot(CMCSA_RT,aes(x=date,y=per_returns))+geom_line(color="orange")+labs(title="CMCSA percentage returns")
plt3 <-ggplot(EA_RT,aes(x=date,y=per_returns))+geom_line(color="tomato")+labs(title="EA percentage returns")
plts<-grid.arrange(plt1,plt2,plt3,ncol=2)

```

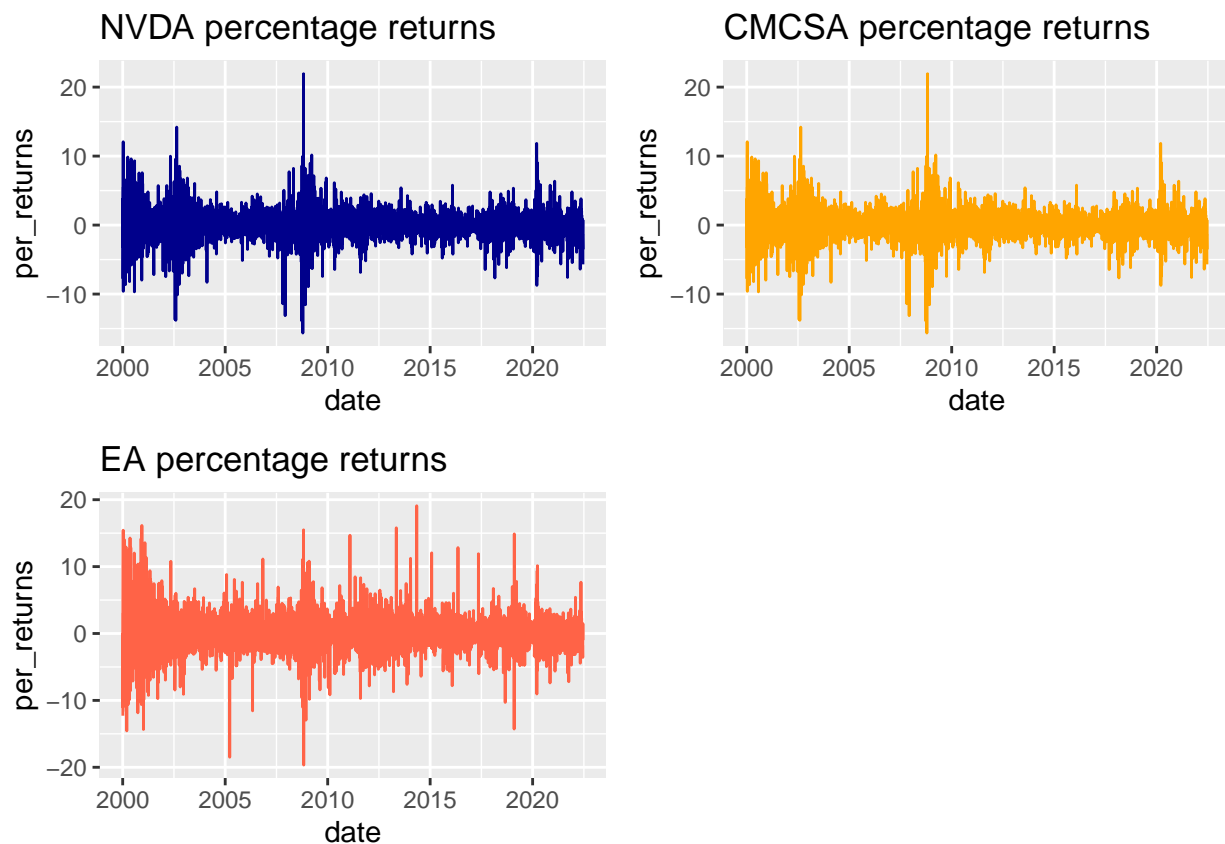


Figure 2: Time series of percentage returns

```

plts

## TableGrob (2 x 2) "arrange": 3 grobs
##   z      cells  name      grob
## 1 1 (1-1,1-1) arrange gtable[layout]
## 2 2 (1-1,2-2) arrange gtable[layout]
## 3 3 (2-2,1-1) arrange gtable[layout]

```

2.3

To find the number of bins, consider the following formula:

$$bins = (Max - Min)/h$$

where

$$h = 2 \times IQR \times n^{-1/3}$$

#histogram for each stock return series.

```
hist1 <-ggplot(NVDA_RT,aes(x=per_returns))+geom_histogram(bins = 151,fill = "darkblue")+labs(title="NVDA returns Histogram")
hist2 <-ggplot(CMCSA_RT,aes(x=per_returns))+geom_histogram(bins = 96,fill = "orange")+labs(title="CMCSA returns Histogram")
hist3 <-ggplot(EA_RT,aes(x=per_returns))+geom_histogram(bins = 91,fill = "tomato")+labs(title="EA returns Histogram")
hists<-grid.arrange(hist1,hist2,hist3,ncol=2)
```

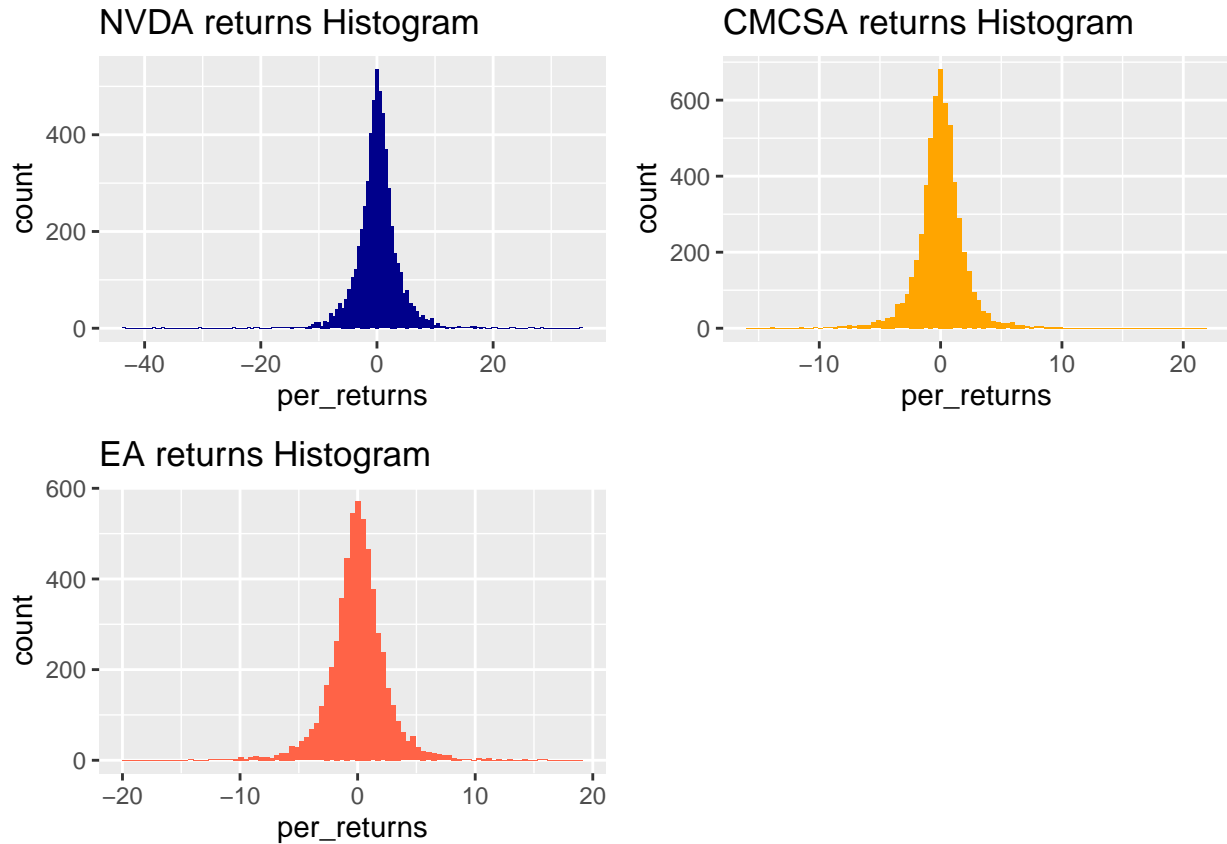


Figure 3: Histograms of percentage returns

`hists`

```
## TableGrob (2 x 2) "arrange": 3 grobs
##   z      cells  name      grob
## 1 1 (1-1,1-1) arrange gtable[layout]
## 2 2 (1-1,2-2) arrange gtable[layout]
## 3 3 (2-2,1-1) arrange gtable[layout]
```

The three histograms indicate that the returns of the three stocks (NVDA, CMCSA, and EA) are normally distributed with sharp apex indicating highly positive kurtosis, hence leptokurtic. In all three stocks, most of the stocks' returns cluster around zero, since more returns are above the normal distribution and less values are distributed in the tail.

Table 2: Summary table of returns

symbol	type	mean	median	variance	sd	skewness	kurtosis
CMCSA	adjusted	19.1994217	10.6285470	205.401670	14.331841	0.9761561	-0.2518994
EA	adjusted	56.1800242	47.7187500	1490.996295	38.613421	0.8668134	-0.4590129
NVDA	adjusted	26.7655564	3.9967255	2982.289711	54.610344	2.9974481	9.1639855
CMCSA	returns	0.0204231	0.0338371	4.192171	2.047479	-0.0112877	8.2719957
EA	returns	0.0288748	0.0353464	6.750653	2.598202	0.1248974	6.4033306
NVDA	returns	0.0913318	0.1037125	14.278268	3.778659	-0.2533467	13.3750051

2.4

```
# summary for NDVA, CMCSA, and EA stocks.
# summary for the adjusted prices
tab1 <- stocks %>%
  group_by(symbol)%>% summarize(mean=mean(adjusted),median=median(adjusted),variance=var(adjusted),sd=sd(adjusted))
# summary for percentage returns
tab2 <- stocks %>%
  group_by(symbol)%>% summarize(mean=mean(per_returns,na.rm=T),median=median(per_returns,na.rm=T),var=var(per_returns,na.rm=T))
summary <- rbind(tab1,tab2)
#adding labels
summary$type<- c("adjusted","adjusted","adjusted","returns","returns","returns")
summary <- summary[,c(1,8,2,3,4,5,6,7)] # formatting the columns
summar <- summary %>% group_by(symbol,type)
kable(summar, caption = "Summary table of returns")
```

The average stock returns do not appear to be significantly different from zero(0.0204, 0.0289, and 0.0913) since more returns are above the normal distribution and lies between 2 and 4 standard deviations. NVDA stock returns the biggest return of 0.0913, with an almost 10% return on investment, but experiences the most variations.

2.5

Significant test for all stocks (t-test)

- Null Hypothesis: Average returns equals zero
- Alternative Hypothesis: Average returns not equals zero

$$\begin{aligned}
 H_0 : \mu &= 0 \\
 H_1 : \mu &\neq 0 \\
 \alpha &= 0.01 \\
 t &= \left(\frac{\hat{\mu}\sqrt{N}}{\sigma} \right) t_{N-1}
 \end{aligned}$$

Significant test for NVDA (t-test)

```
#select returns for NVDA stock
nvda_ret <- subset(stocks,stocks$symbol=="NVDA")%>%select(per_returns)
#t-test for NVDA stock
nvda_test=t.test(nvda_ret$per_returns,mu=0,conf.level=0.99)
res <- data.frame(nvda_test$statistic,nvda_test$p.value)
names(res)<-c("t","p-value")
res
```

```
##           t    p-value
## t 1.816806 0.06929986
```

$$t = 1.837498$$

$$p - value = 0.0661 > 0.05$$

Significant test for CMCSA

```
# returns for CMCSA stock
cmcsa_ret <- subset(stocks,stocks$symbol=="CMCSA")%>%select(per_returns)
#t-test for CMCSA stock
cmcsa_test=t.test(cmcsa_ret$per_returns,mu=0,conf.level=0.99)
cmcsa_res <- data.frame(cmcsa_test$statistic,cmcsa_test$p.value)
names(cmcsa_res)<-c("t","p-value")
cmcsa_res
```

```
##           t    p-value
## t 0.7497668 0.4534264
```

$$t = 0.7872869$$

$$p - value = 0.4311469 > 0.05$$

Significant Test (t-test) for EA

```
ea_ret <- subset(stocks,stocks$symbol=="EA")%>%select(per_returns)#select returns for EA stock
#t-test for EA stock
ea_test=t.test(ea_ret$per_returns,mu=0,conf.level=0.99)
ea_res <- data.frame(ea_test$statistic,ea_test$p.value)
names(ea_res)<-c("t","p-value")
ea_res
```

```
##           t    p-value
## t 0.8353535 0.403554
```

$$t = 0.8405$$

$$p - value = 0.4007 > 0.05$$

```
# t critical value
qt(0.01, 5648, lower.tail = F)
```

```
## [1] 2.327008
```

$$t_{critical} = 2.327$$

- summary of the three tests

Table 3: Tests of significant differences from zero

Type	T_stat	T_crit	P_value
NVDA	1.8375	2.327	0.06612
CMCSA	0.7873	2.327	0.43110
EA	0.8405	2.327	0.40070

```
tests <- data.frame(
  Type = c("NVDA", "CMCSA", "EA"),
  T_stat = c(1.8375, 0.7873, 0.8405),
  T_crit = c(2.327, 2.327, 2.327),
  P_value = c(0.06612, 0.4311, 0.4007)
)
kable(tests, caption = "Tests of significant differences from zero")
```

The t-values obtained for all the three stocks are less than the critical value(2.327), therefore we fail to reject the null hypothesis and conclude that the stocks returns are not significantly different from 0 at 1% significance level. The p-values being higher than 0.01 suggest that we do not have sufficient evidence to say that the average returns are different from 0.

2.6. Significance differences of the average returns.

Testing for equality of variances

$$\text{Let Variance NVDA} = \sigma_N^2$$

$$\text{Let variance CMCSA} = \sigma_C^2$$

$$\text{Let variance EA} = \sigma_E^2$$

* 1. NVDA and CMCSA

$$H_0 : \sigma_N^2 = \sigma_C^2$$

$$H_1 : \sigma_N^2 \neq \sigma_C^2$$

$$\alpha = 0.01 \quad \frac{\alpha}{2} = 0.005$$

The test statistic

$$F = \left(\frac{\hat{\sigma}_N^2}{\hat{\sigma}_C^2} \right)$$

$$F = \frac{14.275}{4.187} = 3.409$$

$$F_c = F_{N_G-1, N_C-1} = F_{5649-1, 5649-1}$$

F critical can be obtained using r as follows:

```
qf(p=.005, df1=5649-1, df2=5649-1, lower.tail=FALSE)
```

```
## [1] 1.070963
```

$$F_c = 1.070963$$

$$F > F_c$$

Reject the null hypothesis. Therefore there the variances of NVDA and CMCSA stocks returns are significantly different from each other. T-test assuming unequal variances is appropriate in this case.

- **2. NVDA and EA**

$$H_0 : \sigma_N^2 = \sigma_E^2$$

$$H_1 : \sigma_N^2 \neq \sigma_E^2$$

$$\alpha = 0.01 \text{ then } \frac{\alpha}{2} = 0.005$$

$$F = \left(\frac{\hat{\sigma}_N^2}{\hat{\sigma}_E^2} \right)$$

$$F = \frac{14.275}{6.752} = 2.114$$

$$F_c = 1.071$$

$$F > F_c$$

Hence reject the null hypothesis. Therefore NVDA and EA stocks variances are significantly different. We shall assume unequal variance when calculating t-value.

- **3. CMCSA and EA**

$$H_0 : \sigma_C^2 = \sigma_E^2$$

$$H_1 : \sigma_C^2 \neq \sigma_E^2$$

$$\alpha = 0.01 \text{ then } \frac{\alpha}{2} = 0.005$$

$$F = \left(\frac{\hat{\sigma}_C^2}{\hat{\sigma}_E^2} \right)$$

$$F = \frac{4.187}{6.752} = 0.062$$

$$F_c = 1.072$$

$$F < F_c$$

Fail to reject the null hypotheses This suggests that the variances returns of the two stocks returns does not differs significantly, hence t-test will assume equal variances.

Let μ_N represent mean of NVDA stocks returns

let μ_C = CMCSA average returns

let μ_E = EA average returns

Perform t-test for the three pairs:

- i) NVDA and CMCSA

$$H_0 : \mu_N = \mu_C$$

$$H_1 : \mu_N \neq \mu_C$$

Consider that it's a two tailed t-test:

$$\alpha = 0.01 \text{ then } \frac{\alpha}{2} = 0.005$$

$$t = \frac{\hat{\mu}_N - \hat{\mu}_C}{\sqrt{\left(\frac{\hat{\sigma}_N^2}{N_N} + \frac{\hat{\sigma}_C^2}{N_C}\right)}}$$

computing using R:

```
NVDA_CMCS <- t.test(nvda_ret$per_returns,cmcsa_ret$per_returns,
                    alternative="two.sided",var.equal=F)
NVDA_CMCSA <- data.frame(NVDA_CMCS$statistic,NVDA_CMCS$p.value,NVDA_CMCS$parameter)
names(NVDA_CMCSA)<- c("t","p-value","df")
NVDA_CMCSA

##           t    p-value      df
## t 1.240181 0.2149418 8702.892
```

$$t = 1.2408$$

$$t_c = t_{df} = t_{8698.91}$$

Computing t critical using R:

```
qt(p=.005, df=8698.91, lower.tail=FALSE)

## [1] 2.576395
```

$$t_c = 2.5764$$

$$|t| < |t_c|$$

In this case, fail to reject the null hypotheses and conclude that the average returns for NVDA and CMCSA are not significantly different.

- ii) NVDA and EA

$$H_0 : \mu_N = \mu_E$$

$$H_1 : \mu_N \neq \mu_E$$

$$\alpha = 0.01 \text{ then } \frac{\alpha}{2} = 0.005$$

$$t = \frac{\hat{\mu}_N - \hat{\mu}_E}{\sqrt{\left(\frac{\hat{\sigma}_N^2}{N_N} + \frac{\hat{\sigma}_E^2}{N_E}\right)}}$$

```
NVDA_E <-t.test(nvda_ret$per_returns,ea_ret$per_returns,alternative="two.sided",var.equal=F)
NVDA_EA <- data.frame(NVDA_E$statistic,NVDA_E$p.value,NVDA_E$parameter)
names(NVDA_EA)<- c("t","p-value","df")
NVDA_EA
```

```
##           t    p-value      df
## t 1.023757 0.3059749 10014.72
```

$$t = 1.0378$$

$$t_c = t_{df} = t_{7455.11}$$

```
qt(p=.005, df=10014.05, lower.tail=FALSE)
```

```
## [1] 2.57632
```

$$t_c = 2.5763$$

$$|t| < |t_c|$$

Fail to reject the null hypothesis and conclude that there is no significant difference between the average returns of NVDA and EA stocks.

- iii) CMCSA and EA

$$H_0 : \mu_H = \mu_N$$

$$H_1; \mu_H \neq \mu_N$$

$$\alpha = 0.01 \text{ then } \frac{\alpha}{2} = 0.005$$

$$t = \frac{\hat{\mu}_C - \hat{\mu}_E}{\sqrt{\left(\frac{\hat{\sigma}_C^2}{N_C} + \frac{\hat{\sigma}_E^2}{N_E}\right)}}$$

Computing using R:

```
CMCSA_E <-t.test(cmcsa_ret$per_returns,ea_ret$per_returns,alternative="two.sided",var.equal=T,)
CMCSA_EA <- data.frame(CMCSA_E$statistic,CMCSA_E$p.value,CMCSA_E$parameter)
names(CMCSA_EA)<- c("t","p-value","df")
CMCSA_EA
```

```
##           t    p-value      df
## t -0.1920454 0.8477101 11298
```

$$t = -0.1732$$

$$t_c = t_{df} = t_{11296}$$

```
qt(p=.005, df=11296, lower.tail=T)
```

```
## [1] -2.576265
```

Table 4: Correlation matrix of the three returns

	NVDA	CMCSA	EA
NVDA	1.0000000	0.3255846	0.3754482
CMCSA	0.3255846	1.0000000	0.3030101
EA	0.3754482	0.3030101	1.0000000

$$t_c = -2.5763$$

$$t > t_c$$

Reject the null hypotheses and conclude that the average returns for CMCSA and EA stocks return are significantly different.

From the three tests of significance, the average stocks returns for CMCSA and EA are significantly different but both average returns for EA and CMSA are not significantly different from NVDA

2.7

```
corr <- data.frame(NVDA=nvda_ret$per_returns,CMCSA=cmcsa_ret$per_returns,EA=ea_ret$per_returns)
kable(corr,method="pearson", caption = "Correlation matrix of the three returns")
```

According to the correlation matrix, the three stocks returns are not strongly correlated with each other. The correlation coefficients between NVDA and CMCSA and EA are 0.3251 and 0.3754 respectively, while CMCSA and EA pair has a coefficient of 0.3030.

2.8. Testing the significance of correlations

Set up the null and alternative hypothesis:

$$H_0 : \rho = 0$$

$$H_1 : \rho \neq 0$$

Consider the the following test statistic:

$$t = \frac{r\sqrt{N-2}}{\sqrt{1-r^2}}$$

Decision rule: If $p - value > 0$ reject the H_0

```
cor1 <- cor.test(nvda_ret$per_returns,cmcsa_ret$per_returns,method="pearson")#test between NVDA and CMCSA
cor2 <- cor.test(nvda_ret$per_returns,ea_ret$per_returns,method="pearson")#test between NVDA and EA stocks
cor3 <- cor.test(cmcsa_ret$per_returns,ea_ret$per_returns,method="pearson")# test between CMCSA and EA stocks

#add the outputs into a table
cor1 <- data.frame(statistic=cor1$statistic,p_value=round(cor1$p.value,2))
row.names(cor1)<-c("NVDA_CMCSA")
cor2 <- data.frame(statistic=cor2$statistic,p_value=round(cor2$p.value,2))
row.names(cor2)<-c("NVDA_EA")
cor3<- data.frame(statistic=cor3$statistic,p_value=round(cor3$p.value,2))
row.names(cor3)<-c("CMCSA_EA")
```

Table 5: Test for correlations significance

	statistic	p_value
NVDA_CMCSA	25.87878	0
NVDA_EA	30.44325	0
CMCSA_EA	23.89556	0

Table 6: covariance matrix

	Nvda	Cmcsa	Ea
Nvda	14.278268	2.518959	3.686046
Cmcsa	2.518959	4.192171	1.611942
Ea	3.686046	1.611942	6.750653

```
cor <- rbind(cor1,cor2,cor3)
kable(cor,caption = "Test for correlations significance")
```

Decision: Therefore p-values obtained equals to 0 which is less than $\alpha = 0.05$ significance level therefore reject the null hypotheses.

This indicates that the correlation between the stocks are significant.

2.9 Advising an investor.

Suppose that an investor has asked you to assist them in choosing **two** of these three stocks to include in their portfolio. The portfolio is defined by

$$r = w_1 r_1 + w_2 r_2$$

Where r_1 and r_2 represent the returns from the first and second stock, respectively, and w_1 and w_2 represent the proportion of the investment placed in each stock. The entire investment is allocated between the two stocks, so $w_1 + w_2 = 1$.

The investor favors the combination of stocks that provides the highest return, but dislikes risk. Thus the investor's happiness is a function of the portfolio, r :

$$h(r) = \mathbb{E}(r) - \text{Var}(r)$$

Where $\mathbb{E}(r)$ is the expected return of the portfolio, and $\text{Var}(r)$ is the variance of the portfolio.¹

FIRST of all, find the covariance matrix of returns

```
Nvda <- NVDA_RT$per_returns
Cmcsa <- CMCSA_RT$per_returns
Ea <- EA_RT$per_returns
pfol <- data.frame(Nvda, Cmcsa, Ea)
kable(cov(pfol), caption = "covariance matrix")
```

Then calculate the optimum weights as follows:

$$h(r) = \mathbb{E}(r) - \text{Var}(r)$$

¹Note that $\mathbb{E}(r) = w_1 \mathbb{E}(r_1) + w_2 \mathbb{E}(r_2)$, and $\text{Var}(r) = w_1^2 \text{Var}(r_1) + w_2^2 \text{Var}(r_2) + 2w_1 w_2 \text{Cov}(r_1, r_2)$

$$E(r) = E(w_1r_1 + w_2r_2) = w_1E(r_1) + w_2E(r_2)$$

$$Var(r) = Var(w_1r_1 + w_2r_2) = w_1Var(r_1) + w_2Var(r_2) + 2w_1w_2COV(r_1, r_2)$$

Test For NVDA and CMCSA

$$E(r) = (0.0913)w_1 + (0.0204)w_2$$

$$Var(r) = 14.2747w_1 + 4.1922w_2 + 2(2.519)w_1w_2$$

$$w_1 + w_2 = 1$$

$$w_2 = 1 - w_1$$

$$E(r) = 0.0913w_1 + 0.0204(1 - w_1)$$

$$= 0.071w_1 + 0.0204$$

$$Var(r) = 14.2747w_1 + 4.1922(1 - w_1) + 2(2.519)w_1(1 - w_1)$$

$$= 14.2747w_1 + 4.1922 - 4.1922w_1 + 5.038w_1 - 5.038w_1^2$$

$$= 4.1922 + 5.1207w_1 - 5.038w_1^2$$

$$h(r) = 0.071w_1 + 0.0204 - (4.1922 + 5.1207w_1 - 5.038w_1^2)$$

$$= 0.01w_1 + 0.047 - 1.7 - 3.92w_1 + 1.82w_1^2$$

$$= 5.038w_1^2 - 15.0497w_1 - 4.1718$$

$$\text{first order derivative} = \frac{dh(r)}{dw_1} = 10.076w_1 - 15.0497$$

$$\text{for optimum weight, } 10.076w_1 - 15.0497 = 0$$

$$\text{therefore, } w_1 = 1.494, \text{ and } w_2 = 1 - w_1 = -0.494$$

$$\text{second order derivative} = \frac{dh(r)^2}{d^2w_1} = 10.054$$

$$\frac{dh(r)^2}{d^2w_1} > 0, \text{ opt weight is minimum.}$$

Hence the expected return for portfolio NVDA and CMCSA is

$$E(r) = (0.0913)(1.494) + (0.0204)(-0.494) = 0.1263$$

$$Var(r) = 14.2747(1.4044) + 4.1871(-0.4044) + 2(1.4044)(-0.4044)(2.5135) = 7.1795$$

$$h(r) = 0.1211 - 7.1795 = -7.0584$$

TEST FOR NVDA and EA

$$E(r) = (0.0924)w_1 + (0.0291)w_2$$

$$E(r) = (0.0924)w_1 + (0.0291) - 0.0291w_1$$

$$Var(r) = 14.2747w_1 + 6.7517w_2 + 2(3.6856)w_1w_2$$

$$w_1 + w_2 = 1$$

$$w_2 = 1 - w_1$$

$$E(r) = 0.0924w_1 + 0.0291(1 - w_1)$$

$$= 0.0924w_1 + 0.0291 - 0.0291w_1$$

$$= 0.0633w_1 + 0.0291$$

$$Var(r) = 14.2747w_1 + 6.7517(1 - w_1) + 2w_1(3.6856)(1 - w_1)$$

$$= 14.2747w_1 + 6.7517 - 6.7517w_1 + 7.3712w_1 - 7.3712w_1^2$$

$$= 7.3712w_1^2 + 14.8942w_1 - 6.7517$$

$$h(r) = 0.0633w_1 + 0.0291 - (7.3712w_1^2 + 14.8942w_1 - 6.7517)$$

$$= 6.7808 - 14.8309w_1 - 7.3712w_1^2$$

$$\text{first order derivative} = \frac{dh(r)}{dw_1} = -14.7424w_1 - 14.8309$$

$$\text{for optimum weight, } -14.7424w_1 - 14.8309 = 0$$

$$\text{therefore, } w_1 = -1.006, \text{ and } w_2 = 1 - w_1 = 2.006$$

$$\text{second order derivative} = \frac{dh(r)^2}{d^2w_1} = -14.7424$$

$$\frac{dh(r)^2}{d^2w_1} < 0, \text{ opt weight is maximum.}$$

Hence the expected return for portfolio NVDA and EA is

SUBSTITUTE w_1 and w_2 to $E(r)$, $Var(r)$, and $h(r)$

$$E(r) = (0.0924)(-1.006) + (0.0291)(2.006) = -0.0346$$

$$Var(r) = 14.2747(-1.006) + 6.7517(2.006) + 2(3.6856)(-1.006)(2.006) = -15.69$$

$$h(r) = -0.0346 + 15.69 = 15.66$$

TEST FOR CMCSA and EA

$$E(r) = (0.0214)w_1 + (0.0291)w_2$$

$$Var(r) = 4.1871w_1 + 6.7517w_2 + 2(1.6111)w_1w_2$$

$$w_1 + w_2 = 1$$

$$w_2 = 1 - w_1$$

$$E(r) = (0.0214)w_1 + (0.0291)(1 - w_1)$$

Table 7: Optimum portfolio table

	weight_1	weight_2	E(r)	Var(r)	h(r)
NVDA and CMCSA	1.494	-0.4940	0.1263	7.1796	-7.0584
NVDA and EA	-1.006	2.0060	-0.0346	-15.6900	15.6600
CMCSA and EA	1.047	-0.0466	0.0211	3.9120	-3.9120

$$= 0.0291 - 0.0077w_1$$

$$Var(r) = 4.1871w_1 + 6.7517(1 - w_1) + 2w_1(1.6111)(1 - w_1)$$

$$= 0.6576 + 6.7517w_1 - 3.222w_1^2$$

$$h(r) = 0.0291 - 0.0077w_1 - (0.6576 + 6.7517w_1 - 3.222w_1^2)$$

$$= 3.222w_1^2 - 6.744w_1 - 0.6285$$

$$first\ order\ derivative = \frac{dh(r)}{dw_1} = 6.444w_1 - 6.744$$

$$for\ optimum\ weight, 6.444w_1 - 6.744 = 0$$

$$therefore, w_1 = 1.047, and w_2 = 1 - w_1 = -0.0466$$

$$second\ order\ derivative = \frac{dh(r)^2}{d^2w_1} = 6.444$$

$$\frac{dh(r)^2}{d^2w_1} > 0, opt\ weight\ is\ minimum.$$

Therefore

$$E(r) = 0.0214(1.047) + (0.0291)(-0.0466) = 0.02105$$

$$Var(r) = 4.1871(1.047) + 6.7517(-0.0466) + 2(1.6111)(1.047)(-0.0466) = 3.912$$

$$h(r) = 0.02105 - 3.912 = -3.8909$$

You can use this section to create a table of your results.

```
optimal_pfolio <- matrix(c(1.494,-0.494,0.1263,7.1796,-7.0584,-1.006,2.006,-0.0346,-15.69,15.66,1.047,-3.8909),
  ncol = 5,
  byrow = TRUE)
colnames(optimal_pfolio) <- c("weight_1", "weight_2", "E(r)", "Var(r)", "h(r)")
rownames(optimal_pfolio) <- c("NVDA and CMCSA", "NVDA and EA", "CMCSA and EA")
optimal_pfolio <- as.table(optimal_pfolio)
kable(optimal_pfolio,caption = "Optimum portfolio table")
```

According the expected returns, A combination of NVDA and CMCSA generates the biggest returns with a 0.1263 coefficient. This implies that an investor has a higher probability(12.63%) of generating a profit. Since the investor is interested in a strategy with less uncertainty, CMCSA could provide a better option since it has the lowest variations in returns, hence more stable portfolio. However, the weights of the the two stocks (CMCSA and EA) suggests that the investor needs to consider investing 4.66% in EA and 95.34% in CMCSA.

2.10. The impact of financial events on returns (6 points)

```
extract <- function(stocks,smb){
  stoc <- subset(stocks,symbol==smb)
  lehman <- stoc[stoc$date=="2008-09-15",] # Lehman bankruptcy
  pandemic <- stoc[stoc$date=="2020-03-11",]# COVID pandemic
  bankrpyc1 <- stoc[stoc$date!="2008-09-15",]#omit the bankruptcy date
  bankrpyc2 <- stoc[stoc$date!="2020-03-11",]#omit the pandemic date
  BAU <- rbind(bankrpyc1,bankrpyc2) #joining the dataframes
  #create new column with three factors
  BAU$event <- "BAU"
  lehman$event="lehman"
  pandemic$event <- "pandemic"
  events <- rbind(lehman,pandemic,BAU) #merge the three dataframes
  events$event <- factor(events$event) #column to a factor
  events <- na.omit(events)#drop the na columns
  return (events)
}

#call the function to extract and create the factor column
NVDA_EVENTS <- extract(stocks,"NVDA")
CMCSA_EVENTS <- extract(stocks,"CMCSA")
EA_EVENTS <- extract(stocks,"EA")
#linear regression model for the three stocks
model_nvda <- lm(per_returns~event,data=NVDA_EVENTS)
model_cmcsa <- lm(per_returns~event,dat=CMCSA_EVENTS)
model_ea <- lm(per_returns~event,data=EA_EVENTS)

# NVDA events
summary(model_nvda)$coefficients

##              Estimate Std. Error   t value    Pr(>|t|)
## (Intercept)   0.09266659 0.03553819   2.607521 0.009132039
## eventlehman   -9.23187700 3.77759465  -2.443851 0.014546632
## eventpandemic -5.85131399 3.77759465  -1.548952 0.121421195

# CMCSA events
summary(model_cmcsa)$coefficients

##              Estimate Std. Error   t value    Pr(>|t|)
## (Intercept)   0.02105378 0.01925837   1.093227 0.27431727
## eventlehman   -4.01500563 2.04710272  -1.961311 0.04986725
## eventpandemic -3.11179797 2.04710272  -1.520099 0.12851418

# EA events
summary(model_ea)$coefficients

##              Estimate Std. Error   t value    Pr(>|t|)
## (Intercept)   0.02940919 0.02444192   1.203227 0.2289136
## eventlehman   -3.85816636 2.59809725  -1.4849969 0.1375725
## eventpandemic -2.18045253 2.59809725  -0.8392498 0.4013469
```

- (a) According to the regression models, all the three stocks never exhibited positive returns over time since R-squared from the three models are not significantly different from zero.
- (b) Both pandemic and bankruptcy events have negative impacts on the three stocks. In all cases, Lehman Brothers bankruptcy affected the stocks more negatively as the “eventlehman” coefficients are less

than “eventpandemic” coefficients. Lehman bankruptcy had significantly negative impacts on both NVDA($p - value = 0.0146$) and CMCSA($p - value = 0.0499$) at 5% significance level.