

Heuristics Analysis

Problems:

This analysis report details out the set of problems in PDDL (Planning Domain Definition Language) for Air Cargo domains and provides experimentation metrics and analysis for various search algorithms.

- Air Cargo Action Schema:

```
Action(Load(c, p, a),
      PRECOND: At(c, a) ∧ At(p, a) ∧ Cargo(c) ∧ Plane(p) ∧ Airport(a)
      EFFECT: ¬ At(c, a) ∧ In(c, p))
Action(Unload(c, p, a),
      PRECOND: In(c, p) ∧ At(p, a) ∧ Cargo(c) ∧ Plane(p) ∧ Airport(a)
      EFFECT: At(c, a) ∧ ¬ In(c, p))
Action(Fly(p, from, to),
      PRECOND: At(p, from) ∧ Plane(p) ∧ Airport(from) ∧ Airport(to)
      EFFECT: ¬ At(p, from) ∧ At(p, to))
```

- Problem 1 initial state and goal:

```
Init(At(C1, SFO) ∧ At(C2, JFK)
     ∧ At(P1, SFO) ∧ At(P2, JFK)
     ∧ Cargo(C1) ∧ Cargo(C2)
     ∧ Plane(P1) ∧ Plane(P2)
     ∧ Airport(JFK) ∧ Airport(SFO))
Goal(At(C1, JFK) ∧ At(C2, SFO))
```

- Problem 2 initial state and goal:

```
Init(At(C1, SFO) ∧ At(C2, JFK) ∧ At(C3, ATL)
     ∧ At(P1, SFO) ∧ At(P2, JFK) ∧ At(P3, ATL)
     ∧ Cargo(C1) ∧ Cargo(C2) ∧ Cargo(C3)
     ∧ Plane(P1) ∧ Plane(P2) ∧ Plane(P3)
     ∧ Airport(JFK) ∧ Airport(SFO) ∧ Airport(ATL))
Goal(At(C1, JFK) ∧ At(C2, SFO) ∧ At(C3, SFO))
```

- Problem 3 initial state and goal:

```
Init(At(C1, SFO) ∧ At(C2, JFK) ∧ At(C3, ATL) ∧ At(C4, ORD)
     ∧ At(P1, SFO) ∧ At(P2, JFK)
     ∧ Cargo(C1) ∧ Cargo(C2) ∧ Cargo(C3) ∧ Cargo(C4)
     ∧ Plane(P1) ∧ Plane(P2)
     ∧ Airport(JFK) ∧ Airport(SFO) ∧ Airport(ATL) ∧ Airport(ORD))
Goal(At(C1, JFK) ∧ At(C3, JFK) ∧ At(C2, SFO) ∧ At(C4, SFO))
```

Part 1: Planning Problems

The non-heuristics planning was done with below search algorithms and the respective results were shown in the table.

- Bread-First Search
- Depth-First Search
- Uniform-Cost-Search

Experiment Metrics:

Problem	Search Type	Plan Length	Expansion	Goal Tests	Time elapsed (s)	Optimality
P1	breadth_first_search	6	43	56	0.0432	Y
P1	depth_first_graph_search	12	12	13	0.0133	N
P1	uniform_cost_search	6	55	57	0.0541	Y
P2	breadth_first_search	9	3343	4609	19.3146	Y
P2	depth_first_graph_search	575	582	583	4.1984	N
P2	uniform_cost_search	9	4834	4836	17.7042	Y
P3	breadth_first_search	9	3461	6072	27.1578	Y
P3	depth_first_graph_search	4071	7857	7858	120.8559	N
P3	uniform_cost_search	9	7356	7358	31.4102	Y

Comparison Insights:

1. **Time:** The time taken to get to the goal state by Depth-First Search was considerably less in Problem 1 and Problem 2 but it took more time in Problem 3 than other two. So time taken is not consistent.
2. **Nodes Expanded:** The nodes expanded to get to the goal state by Depth-First Search was considerably less in Problem 1 and Problem 2 but it took more nodes in Problem 3 than other two.
3. **Plan Length:** The plan length to get to the goal state by Depth-First Search was considerably more in all problems than other two.
4. **Optimality:** Looking at the nodes expanded, it is obvious that Depth-First Search is not optimal compared to other two search algorithms.
5. **Goal Tests:** Looking at the goal test, both Breadth-First Search and Uniform Cost Search take about the same range steps but Depth-First Search varies based on plan length to the goal state.

Part 2: Domain-Independent Heuristics

The heuristics planning was done with below heuristics functions and the respective results were shown in the table.

- h_1
- h_ignore_preconditions
- h_pg_levelsum

Experiment Metrics:

Problem	Search Type	Plan Length	Expansion	Goal Tests	Time elapsed (s)	Optimality
P1	astar_search-h_1	6	55	57	0.054	Y
P1	astar_search-h_ignore_preconditions	6	41	43	0.0401	Y
P1	astar_search-h_pg_levelsum	6	55	57	1.8947	Y
P2	astar_search-h_1	9	4834	4836	17.0342	Y
P2	astar_search-h_ignore_preconditions	9	1450	1452	5.1977	Y
P2	astar_search-h_pg_levelsum	9	4834	4836	1041.1107	Y
P3	astar_search-h_1	9	7356	7358	30.4781	Y
P3	astar_search-h_ignore_preconditions	9	858	860	3.9313	Y
P3	astar_search-h_pg_levelsum	9	7356	7358	3974.9554	Y

Comparison Insights:

1. **Time:** The time taken to get to the goal state by h_ignore_preconditions heuristic was greatly less than other two heuristics.
$$h_ignore_preconditions < h_1 < h_pg_levelsum$$
2. **Nodes Expanded:** The nodes expanded to get to the goal state by h_ignore_preconditions heuristic was considerably less than other two.
$$h_ignore_preconditions < h_1 = h_pg_levelsum$$
3. **Plan Length:** The plan length to get to the goal state by all three heuristics was exactly the same in three problems.
$$h_ignore_preconditions = h_1 = h_pg_levelsum$$
4. **Optimality:** Looking at the nodes expanded, it is obvious that all three heuristics are optimal and better than non-heuristics searches.
$$h_ignore_preconditions = h_1 = h_pg_levelsum$$
5. **Goal Tests:** Looking at the goal test, h_ignore_preconditions heuristic was greatly less than other two heuristics.
$$h_ignore_preconditions < h_1 = h_pg_levelsum$$

Part 3: Written Analysis

Below sections explains the best heuristics and the optimal plan obtained from it.

Best Heuristics:

Looking at the time taken to get the goal state and the nodes expanded, we can conclude that the heuristic `h_ignore_preconditions` is the best heuristics among all heuristics and non-heuristics searches. The reasons this heuristic function is better than other two are,

- Time to get to goal is less
- Number of nodes expanded is less

In the non-heuristics searches, Depth-First search shows better results in terms of less time taken to achieve goal but it is not consistent in all three problems.

Optimal plan:

Below is the optimal plan described using `h_ignore_preconditions` heuristics approach for all three problems.

Problem 1 using `h_ignore_preconditions`:

Solving Air Cargo Problem 1 using `astar_search` with `h_ignore_preconditions`...

Expansions	Goal Tests	New Nodes
41	43	170

Plan length: 6 Time elapsed in seconds: 0.04016264993697405

```
Load(C1, P1, SFO)
Fly(P1, SFO, JFK)
Unload(C1, P1, JFK)
Load(C2, P2, JFK)
Fly(P2, JFK, SFO)
Unload(C2, P2, SFO)
```

Problem 2 using `h_ignore_preconditions`:

Solving Air Cargo Problem 2 using `astar_search` with `h_ignore_preconditions`...

Expansions	Goal Tests	New Nodes
1450	1452	13303

Plan length: 9 Time elapsed in seconds: 5.197764916811138

```
Load(C3, P3, ATL)
Fly(P3, ATL, SFO)
Unload(C3, P3, SFO)
Load(C2, P2, JFK)
Fly(P2, JFK, SFO)
Unload(C2, P2, SFO)
Load(C1, P1, SFO)
Fly(P1, SFO, JFK)
Unload(C1, P1, JFK)
```

Problem 3 using h_ignore_preconditions:

Solving Air Cargo Problem 3 using astar_search with h_ignore_preconditions...

Expansions	Goal Tests	New Nodes
858	860	7468

Plan length: 9 Time elapsed in seconds: 3.931323932018131

Load(C1, P1, SFO)
Fly(P1, SFO, ATL)
Load(C3, P1, ATL)
Fly(P1, ATL, JFK)
Unload(C3, P1, JFK)
Load(C2, P2, JFK)
Fly(P2, JFK, SFO)
Unload(C2, P2, SFO)
Unload(C1, P1, JFK)