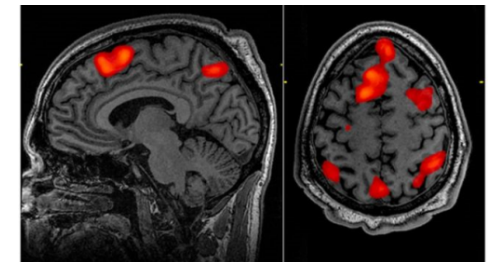


Inclass 26.1. A nuclear (proton) magnetic resonance machine is operated with a magnetic field of 21 Tesla. What is the electromagnetic wave frequency used in the machine to perform the imaging?  $g = 5.6$  and mass of proton  $= 1.67 \times 10^{-27} \text{ kg}$ .

RPI Professor William Edelstein: (from GE)  
Magnetic Resonance Imaging (MRI): APS  
Industrial Applications of Physics Award  
(2006)



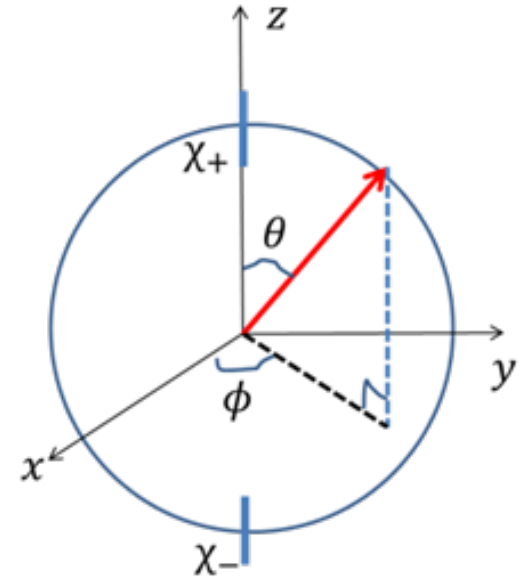
Inclass 26.2. The wavevector of a qubit from a spin  $\frac{1}{2}$  system can be described by  $\psi = A(\cos\frac{\theta}{2} \chi_+ + e^{i\phi} \sin\frac{\theta}{2} \chi_-)$  where  $A$  is the normalization factor,  $\theta$  and  $\phi$  are polar angles shown in the figure, and  $\chi_+$  and  $\chi_-$  are the up and down spin states.

(a) What are the values of  $\theta$  and  $\phi$  in order to achieve a state of the form

$$\psi = A (\chi_+ + \chi_-).$$

(b) Determine the normalization constant  $A$  and show that it is an eigenvector

of the spin operator  $\hat{S}_x = \frac{\hbar}{2} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ . What is the eigenvalue?



Inclass 26.3. Given a spin state of a spin  $\frac{1}{2}$  system:  $\chi = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ ,  
determine  $\Delta S_z$ , the uncertainty in  $S_z$ .

Inclass 26.4. Assume that at  $t = 0$ , a hydrogen atom is in its first excited state  $\Psi(r, \theta, \phi, t = 0) = \psi_{2,1,0}(r, \theta, \phi)$  with energy  $E = E_2$ . What is the probability of finding the atom in its ground state  $\psi_{1,0,0}(r, \theta, \phi)$  with energy  $E_1$  at time  $t$  later?

