

```

j12 = {{0, -1, 0, 0}, {1, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}
k13 = {{0, 0, 1, 0}, {0, 0, 0, 0}, {1, 0, 0, 0}, {0, 0, 0, 0}}
k14 = {{0, 0, 0, 1}, {0, 0, 0, 0}, {0, 0, 0, 0}, {1, 0, 0, 0}}
k24 = {{0, 0, 0, 0}, {0, 0, 0, 1}, {0, 0, 0, 0}, {0, 1, 0, 0}}
j34 = {{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 1}, {0, 0, -1, 0}}
k23 = {{0, 0, 0, 0}, {0, 0, 1, 0}, {0, 1, 0, 0}, {0, 0, 0, 0}}

```

```

Out[28]=
{{0, -1, 0, 0}, {1, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}

```

```

Out[29]=
{{0, 0, 1, 0}, {0, 0, 0, 0}, {1, 0, 0, 0}, {0, 0, 0, 0}}

```

```

Out[30]=
{{0, 0, 0, 1}, {0, 0, 0, 0}, {0, 0, 0, 0}, {1, 0, 0, 0}}

```

```

Out[31]=
{{0, 0, 0, 0}, {0, 0, 0, 1}, {0, 0, 0, 0}, {0, 1, 0, 0}}

```

```

Out[32]=
{{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 1}, {0, 0, -1, 0}}

```

```

Out[33]=
{{0, 0, 0, 0}, {0, 0, 1, 0}, {0, 1, 0, 0}, {0, 0, 0, 0}}

```

```

Out[35]=
{{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}

```

**Commutator[A\_, B\_] := A.B - B.A**

```

In[74]:= ans = Commutator[j12, k13]
MatrixForm[ans]

```

```

Out[74]=
{{0, 0, 0, 0}, {0, 0, 1, 0}, {0, 1, 0, 0}, {0, 0, 0, 0}}

```

```

Out[75]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$


```

```

In[76]:= ans = Commutator[j12, k14]
MatrixForm[ans]

```

```

Out[76]=
{{0, 0, 0, 0}, {0, 0, 0, 1}, {0, 0, 0, 0}, {0, 1, 0, 0}}

```

```

Out[77]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$


```

```
In[78]:= ans = Commutator[j12, k24]
MatrixForm[ans]
```

```
Out[78]= {{0, 0, 0, -1}, {0, 0, 0, 0}, {0, 0, 0, 0}, {-1, 0, 0, 0}}
```

```
Out[79]//MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix}$$

```
In[80]:= ans = Commutator[j12, j34]
MatrixForm[ans]
```

```
Out[80]= {{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}
```

```
Out[81]//MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

```
In[82]:= ans = Commutator[j12, k23]
MatrixForm[ans]
```

```
Out[82]= {{0, 0, -1, 0}, {0, 0, 0, 0}, {-1, 0, 0, 0}, {0, 0, 0, 0}}
```

```
Out[83]//MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

```
In[90]:= ans = Commutator[k13, k14]
MatrixForm[ans]
```

```
Out[90]= {{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 1}, {0, 0, -1, 0}}
```

```
Out[91]//MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

```
In[93]:= ans = Commutator[k13, k24]
MatrixForm[ans]
```

```
Out[93]= {{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}
```

```
Out[94]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

```

```
In[95]:= ans = Commutator[k13, j34]
MatrixForm[ans]
```

```
Out[95]= {{0, 0, 0, 1}, {0, 0, 0, 0}, {0, 0, 0, 0}, {1, 0, 0, 0}}
```

```
Out[96]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}$$

```

```
In[97]:= ans = Commutator[k13, k23]
MatrixForm[ans]
```

```
Out[97]= {{0, 1, 0, 0}, {-1, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}
```

```
Out[98]//MatrixForm=

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

```

```
In[99]:= ans = Commutator[k14, k24]
MatrixForm[ans]
```

```
Out[99]= {{0, 1, 0, 0}, {-1, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}
```

```
Out[100]//MatrixForm=

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

```

In[101]:=

```
ans = Commutator[k14, j34]
MatrixForm[ans]
```

Out[101]=

```
{{0, 0, -1, 0}, {0, 0, 0, 0}, {-1, 0, 0, 0}, {0, 0, 0, 0}}
```

Out[102]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

In[103]:=

```
ans = Commutator[k14, k23]
MatrixForm[ans]
```

Out[103]=

```
{{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}
```

Out[104]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

In[105]:=

```
ans = Commutator[k24, j34]
MatrixForm[ans]
```

Out[105]=

```
{{0, 0, 0, 0}, {0, 0, -1, 0}, {0, -1, 0, 0}, {0, 0, 0, 0}}
```

Out[106]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

In[107]:=

```
ans = Commutator[k24, k23]
MatrixForm[ans]
```

Out[107]=

```
{{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, -1}, {0, 0, 1, 0}}
```

Out[108]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

In[109]:=

```
ans = Commutator[j34, k23]  
MatrixForm[ans]
```

Out[109]=

```
{{0, 0, 0, 0}, {0, 0, 0, -1}, {0, 0, 0, 0}, {0, -1, 0, 0}}
```

Out[110]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}$$