

```

In[ ]:= deqn = Laplacian[V[x, y], {x, y}] == 0
rectangle = Rectangle[{0, 0}, {10, 10}]
boundary = DirichletCondition[
  V[x, y] == Piecewise[{{0, x == 10 && 0 < y < 10}, {0, x == 0 && 0 < y < 10}}, 10], True]
solution = DSolveValue[{deqn, boundary}, V, {x, y} ∈ rectangle]

```

```
Out[ ]:= V(0,2)[x, y] + V(2,0)[x, y] == 0
```

```
Out[ ]:= Rectangle[{0, 0}, {10, 10}]
```

```
Out[ ]:= DirichletCondition[V[x, y] == ( { 0 (x == 10 && 0 < y < 10) || (x == 0 && 0 < y < 10) }, True]
```

```
Out[ ]:= Function[{x, y}, Sum[ - ( 20 (-1 + (-1)K[1]) Csch[π K[1]] Sin[ $\frac{1}{10}$  π x K[1]] Sinh[ $\frac{1}{10}$  π (10 - y) K[1]] ] / (π K[1]) , {K[1] = 1, ∞} ] - Sum[ 20 (-1 + (-1)K[1]) Csch[π K[1]] Sin[ $\frac{1}{10}$  π x K[1]] Sinh[ $\frac{1}{10}$  π y K[1]] ] / (π K[1]) , {K[1] = 1, ∞} ] ]
```

```

In[ ]:= first200 = solution /. ∞ → 200 // Activate

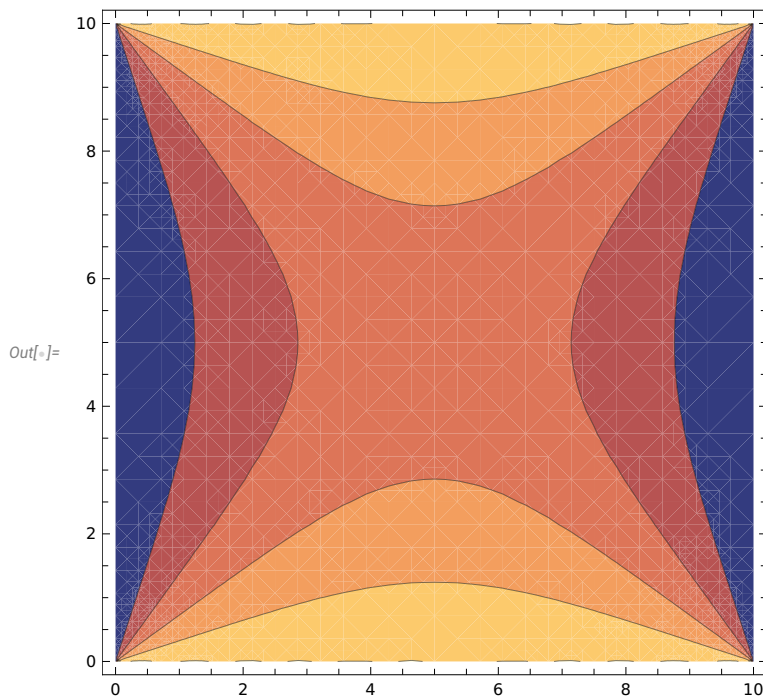
```

```
Out[ ]:= Function[{x, y}, Sum[ - ( 20 (-1 + (-1)K[1]) Csch[π K[1]] Sin[ $\frac{1}{10}$  π x K[1]] Sinh[ $\frac{1}{10}$  π (10 - y) K[1]] ] / (π K[1]) , {K[1] = 1, 200} ] - Sum[ 20 (-1 + (-1)K[1]) Csch[π K[1]] Sin[ $\frac{1}{10}$  π x K[1]] Sinh[ $\frac{1}{10}$  π y K[1]] ] / (π K[1]) , {K[1] = 1, 200} ] ]
```

```

In[ ]:= ContourPlot[first200[x, y], {x, y} ∈ rectangle]

```



In[ ]:=

**deqn2 = Laplacian[V[x, y], {x, y}] == -4  $\pi$  x**

Out[ ]:=  $V^{(0,2)}[x, y] + V^{(2,0)}[x, y] == -4 \pi x$

In[ ]:= **solution2 = NDSolveValue[{deqn2, boundary}, V, {x, y}  $\in$  rectangle]**

Out[ ]:= InterpolatingFunction[ Domain: {{0., 10.}, {0., 10.}}  
Output: scalar ]

In[ ]:= **ContourPlot[solution2[x, y], {x, y}  $\in$  rectangle]**

