CSM: EECS 16A

(Designing Information Devices and Systems I)

Worksheet #13

Term: Fall 2019 Name:

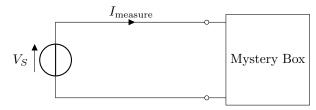
Problem 1: And You Thought You Could Ignore Circuits Until Dead Week

Learning Goal: Understand when Least Squares is helpful for estimating values, and how to translate a word problem with given data points into a Least Squares set up.

1	Write	Ohm's	we.I	for s	a resistor
Ι.	write	Onn s	Law	101 6	i resistor

2. You're given the following test setup and told to find R_{Th} between the two terminals of the mystery box. What is R_{Th} of the mystery box between the two terminals in terms of V_S and I_{measure} ?





3. You think you've figured out how to find R_{Th} ! You've taken the following measurements:

Measurement #	$I_{ m measure}$	V_S
1	1A	1.25kV
2	2A	1kV
3	3A	4kV
4	4A	3.5kV

Using the information above, formulate a least squares problem whose answer provides an estimate of R_{Th} .

- Worksheet #13

2

- Worksheet #13

Problem 3: Revisitng the Acoustic Positioning System

Learning Goal: Understand how to apply properties of inner products, cross correlations, trilateration, least squares, and OMP to build an acoustic positioning system. Learn how to identify the pros/cons when applying different techniques in building the system.

In this question, we will revisit the **Acoustic Positioning System** (APS) and learn how to build it from the ground up using what we know about cross correlation, trilateration, least squares, and Orthogonal Matching Pursuit (OMP).

Recall that in an APS, we have a number of satellites (let's say there are m) transmitting gold codes, and you are a person standing at a location with the coordinate \vec{x} , with your phone as the receiver of the signals.

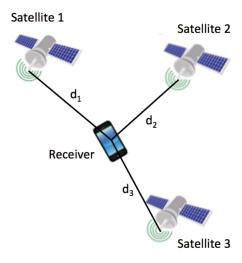
You receive a linear combination of these transmitted signals:

$$\vec{r} = \alpha_1 \vec{s}_1^{(\tau_1)} + \alpha_2 \vec{s}_2^{(\tau_2)} + \ldots + \alpha_m \vec{s}_m^{(\tau_m)}$$

As shown in the expression above, each signal is scaled by a constant which is a "message" the satellite encodes into its signal while transmitting.

To solve for our current position, we can set up a system of equations based on our current position \vec{x} , the position of each satellite $\vec{p_1}, \vec{p_2}, \dots, \vec{p_m}$, and the distance from our current position to each satellite d_i .

Here's an illustration of the APS (given 3 satellites):



- 1. Based on the provided information above, which of the following variables are known? Which are unknown (the ones we are trying to solve for)?
 - The position of each satellite $\vec{p_i}$
 - Our current position \vec{x}
 - The transmitted signals $\vec{s}_i^{(\tau_i)}$
 - The distances from our current position to each satellite d_i

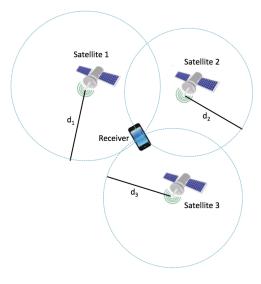
How can we	e express d_i in	terms of $\vec{p_i}$ ar	and \vec{x} ? How m	nany such equa	tions can we se	t up in total?	
	an APS can hent location?	elp us determ	ine where w	e are. Which v	variable given i	n the question of	correspo
	, c	uations we se	t up in part	2, how can we	solve for our cu	irrent position?	
Based on the	ne system of eq						
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4

- Worksheet #13

6. As shown below geometrically, we can represent the area of coverage by each satellite as a circle with a radius of d_i . Explain why the radius of each circle is d_i , and how finding our current position is equivalent to finding the point of intersection among the circumferences of the circles.





7. Now that we have figured out where we are, it is time for us to decode the message! Recall that what our phone receives is a linear combination of these transmitted signals:

$$\vec{r} = \alpha_1 \vec{s}_1^{(\tau_1)} + \alpha_2 \vec{s}_2^{(\tau_2)} + \ldots + \alpha_m \vec{s}_m^{(\tau_m)}$$

From the expression above, which of the following variables are we trying to solve for?

- The scaling (attenuating) constant α_i
- The original signal sent by the satellite $\vec{s_i}$
- The delay in the transmission of the signal τ_i

8. To solve for the unknown variables from the previous part, we can use the **least squares** method. How can we reformulate the given expression and information above as a **least squares** problem? In other words, if we are to rewrite the problem in the form:

$$A\vec{v} \approx \vec{b}$$
,

what would A, \vec{v} , and \vec{b} be equal to respectively?

- W	m forksheet~#13	6
9.	What is the solution using the least squares method?	_
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10.	Does there exist a case where least squares would not work? Write down a sufficient condition where we have to resort to some other techniques to recover the original message.	ıve
11.	If we are to solve this problem using Orthogonal Matching Pursuit (OMP) instead of least squares, what one assumption made by this technique?	is
		7
12.	Describe what the stopping conditions for OMP are. In other words, how do we know when to stop running the OMP algorithm?	ng