



# IDA-ML I: Project Presentation

**Project:** Binary Stroke Classification

**Examinee:** Paul Utsch

**Date:** August 7, 2024

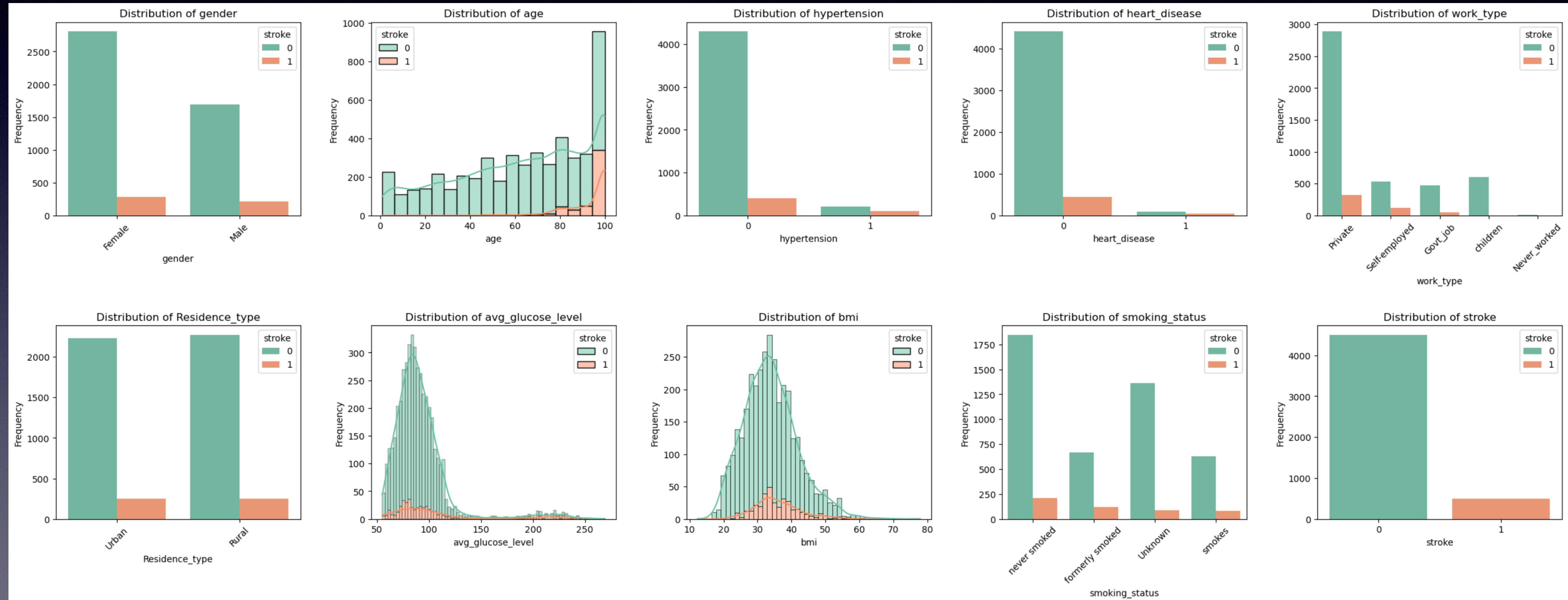
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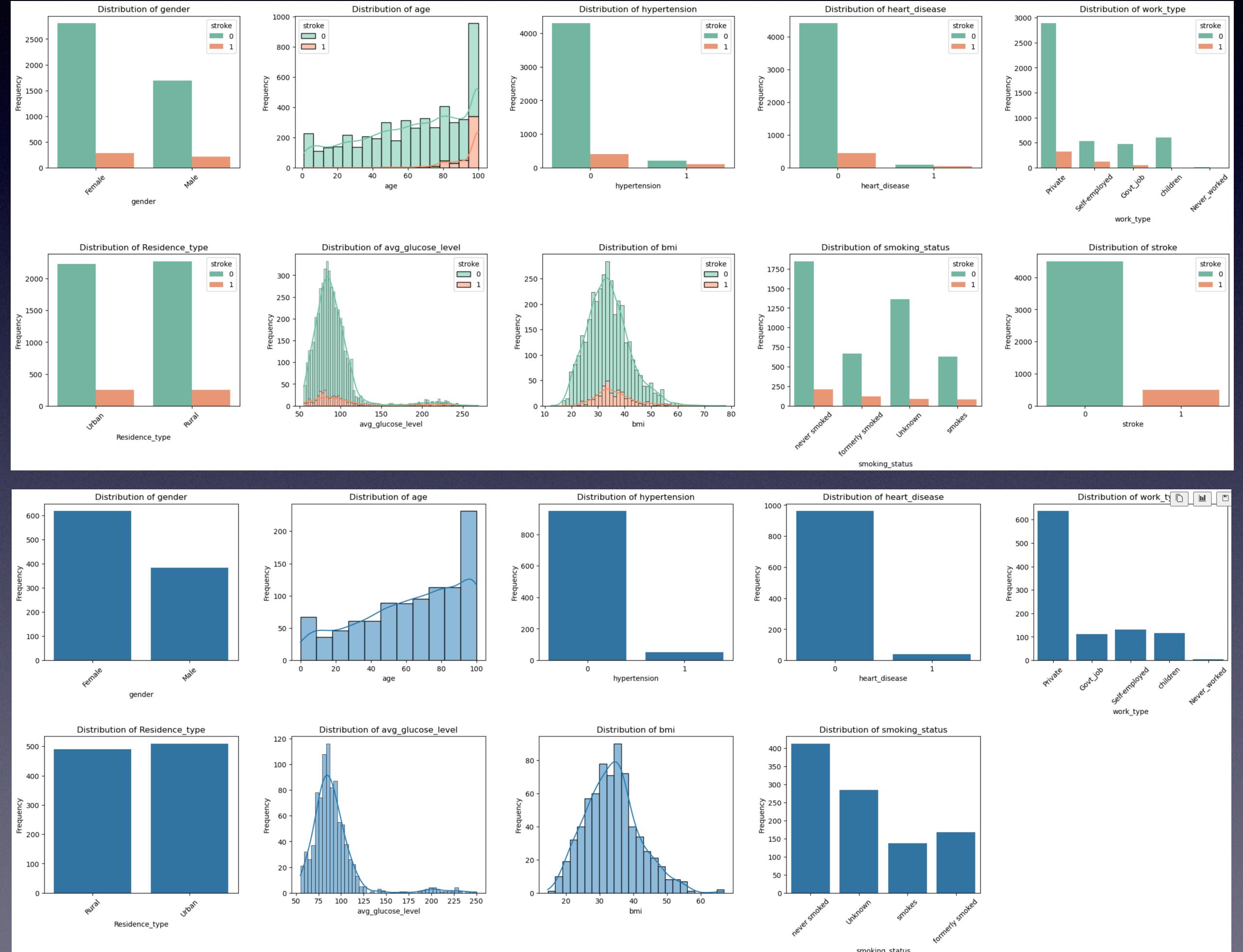
# 1. Problem Statement

- **Supervised Binary Classification Problem**
  - Input Space:  $X = \{x_i \in \mathbb{R}^d \mid i = 1, \dots, n\}$
  - Output Space:  $Y = \{y_i \in \{0,1\}\}$
  - Hypothesis space:  $H = \{h \mid h : X \rightarrow Y\}$
  - Objective:  $h^* = \arg \min_{h \in H} \mathbb{E}_{(x,y) \sim D}[L(h(x), y)]$
- **Predict stroke patients** based on medical and personal data
- **Data Set:**
  - **5000 samples** in train set, **1000 samples** in test set
  - **fictional data**
  - **source:** <https://www.kaggle.com/competitions/ida-ml-1-challenge-summer23/overview>

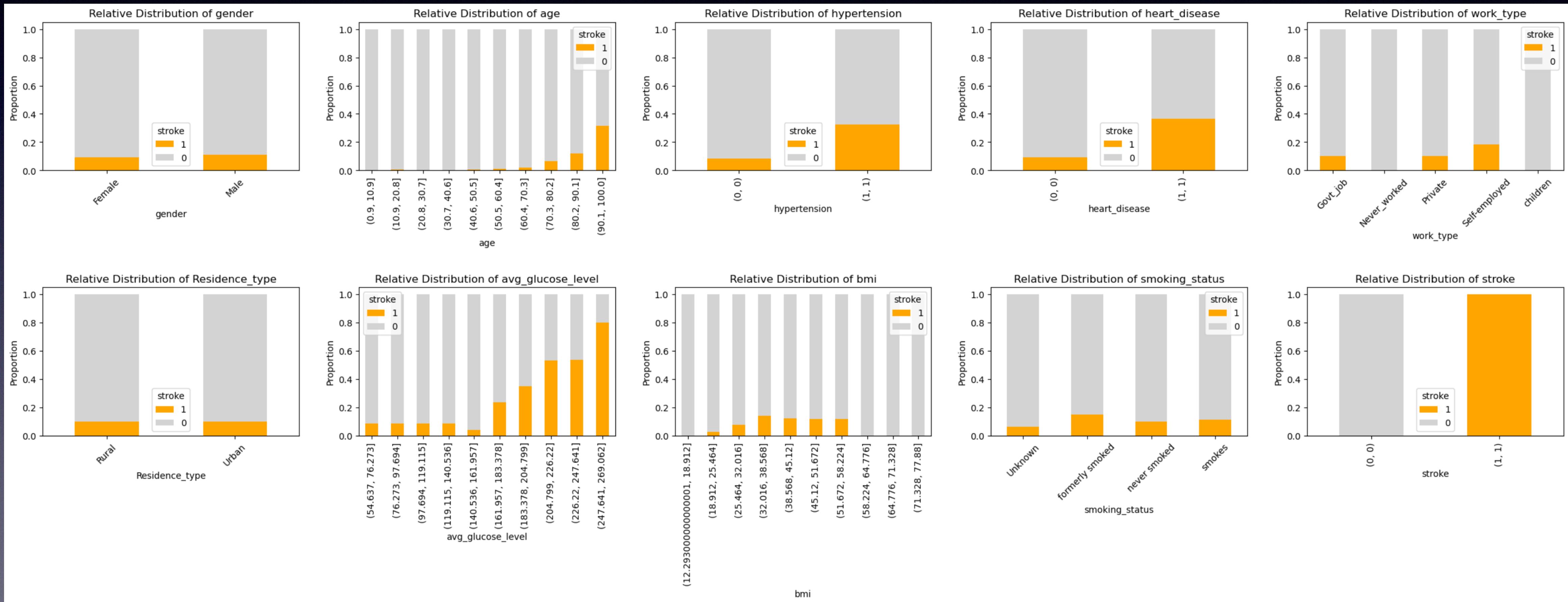
# 2. Data Analysis & Preprocessing



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```
2024-08-04 16:14:33.772 | INFO  | src.data_understanding.data_exploration:print_na:133 - Number of NaN values in column gender: 0 / 5000
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2024-08-04 16:14:33.776 | INFO  | src.data_understanding.data_exploration:print_na:133 - Number of NaN values in column avg_glucose_level: 393 / 5000
2024-08-04 16:14:33.776 | INFO  | src.data_understanding.data_exploration:print_na:133 - Number of NaN values in column bmi: 1552 / 5000
2024-08-04 16:14:33.777 | INFO  | src.data_understanding.data_exploration:print_na:133 - Number of NaN values in column smoking_status: 1451 / 5000
2024-08-04 16:14:33.778 | INFO  | src.data_understanding.data_exploration:print_na:133 - Number of NaN values in column stroke: 0 / 5000
2024-08-04 16:14:33.779 | INFO  | src.data_understanding.data_exploration:print_na:138 - Number of data points with NaN values: 2756 / 5000
```

# 2. Data Analysis & Preprocessing

- **Handling imbalanced data:**
  - Use **weighted cross-entropy loss** as loss function
- **Data preprocessing:**
  - Missing values: **Replace missing values with median**
  - Numerical representation: **Transform discrete features** into binary / one-hot-encoded features
  - **min-max-normalize continuous features**, range [0, 1]

# 3. Machine Learning Methods

- **Naive Implementation** as baseline model
    - random predictions based on target distribution in training set  
(should result in AUC of ~0.5)
  - **Logistic Regression** as linear model
    - train on polynomial features ( $d=2$ ) and principal components, effectively enabling some degree of non-linear separation with regards to the original data
  - **Neural Network** as non-linear model
    - allow model to derive relevant non-linear relations on its own
- ⇒ non-linear separation: polynomials / PCs vs. Neural Network architecture

```
7  class NaiveBaseline:-
8      def __init__(self):
9          super().__init__()
10         self.model = None
11         self.p_true = 0.0
12
13     def fit(
14         self,
15         X_train: npt.ArrayLike,
16         y_train: npt.ArrayLike,
17         X_val: npt.ArrayLike,
18         y_val: npt.ArrayLike,
19     ):-:
20         self.p_true = y_train.mean()
21
22         val_preds = self.predict(X_val)
23         val_accuracy = (val_preds == y_val).mean()
24         print(f"Validation accuracy: {val_accuracy}")
25
26     def predict(self, X: ArrayLike) -> ndarray:
27         """returns a random prediction based on the base probability of the true class, without any training"""
28         return np.random.choice([0, 1], size=len(X), p=[1 - self.p_true, self.p_true])
29
30     def predict_proba(self, X: ArrayLike) -> ndarray:
31         return np.full(len(X), self.p_true)
```

```
7  class NaiveBaseline:-
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13     def fit(
14         self,
15         X_train: npt.ArrayLike,
16         y_train: npt.ArrayLike,
17         X_val: npt.ArrayLike,
18         y_val: npt.ArrayLike,
19     ):-:
20         self.p_true = y_train.mean()
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22         val_preds = self.predict(X_val)
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29
30     def predict_proba(self, X: ArrayLike) -> ndarray:
31         return np.full(len(X), self.p_true)
```

```

12 class BinaryLogisticRegression(object):
13     name = "Binary Logistic Regression"
14
15     def __init__(self, n_features: int = 20, epochs: int = 20, learning_rate: float = 0.1, batch_size: int = 8, lambda_reg: float = 0.1, regularization: str = "L2"):
16         self.n_features = n_features
17         self.epochs = epochs
18         self.learning_rate = learning_rate
19         self.batch_size = batch_size
20         self.lambda_reg = lambda_reg
21         self.regularization = regularization
22
23     X: (n_samples, n_features)
24     Y: (n_samples,)
25
26     self.W: (n_features, 1)
27     self.B: (1,)
28
29     self.class_weights = np.zeros(2)
30
31     # initialize weights and bias to zeros
32     self.W = np.zeros(n_features)
33     self.B = 0.0
34
35     def forward(self, X: npt.ArrayLike) -> npt.ArrayLike:
36         Compute forward pass of the logistic regression model.
37
38         Y_hat: (n_samples,)
39
40         z = np.dot(X, self.W) + self.B
41         Y_hat = sigmoid(z)
42         return Y_hat
43
44     def predict(self, X: npt.ArrayLike) -> npt.ArrayLike:
45         Create a prediction matrix with `self.forward()`
46
47         pred: (n_samples,)
48
49         y_hat = self.forward(X)
50         pred = np.where(y_hat >= 0.5, 1, 0)
51
52         return pred
53
54     def predict_proba(self, X: npt.ArrayLike) -> npt.ArrayLike:
55         Predict probabilities for the input data.
56
57         Y_hat: (n_samples,)
58
59         Y_hat = self.forward(X)
60         return Y_hat
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    def __init__(self, n_features: int = 20, epochs: int = 20, learning_rate: float = 0.1, batch_size: int = 8, lambda_reg: float = 0.1, regularization: str = "L2"):
        """
        X: (n_samples, n_features)
        Y: (n_samples,)

        self.W: (n_features, 1)
        self.B: (1,)
        """
        self.n_features = n_features
        self.epochs = epochs
        self.learning_rate = learning_rate
        self.batch_size = batch_size
        self.lambda_reg = lambda_reg
        self.regularization = regularization

        self.class_weights = np.zeros(2)

        # initialize weights and bias to zeros
        self.W = np.zeros(n_features)
        self.B = 0.0

    def forward(self, X: npt.ArrayLike) -> npt.ArrayLike:
        """
        Compute forward pass of the logistic regression model.

        Y_hat: (n_samples,)
        """
        z = np.dot(X, self.W) + self.B
        Y_hat = sigmoid(z)
        return Y_hat

    def predict(self, X: npt.ArrayLike) -> npt.ArrayLike:
        """
        Create a prediction matrix with `self.forward()`

        pred: (n_samples,)
        """
        y_hat = self.forward(X)
        pred = np.where(y_hat >= 0.5, 1, 0)

        return pred

    def predict_proba(self, X: npt.ArrayLike) -> npt.ArrayLike:
        """
        Predict probabilities for the input data.

        Y_hat: (n_samples,)
        """
        Y_hat = self.forward(X)
        return Y_hat

    def _backward(self, X: npt.ArrayLike, Y: npt.ArrayLike, Y_hat: npt.ArrayLike) -> Tuple[npt.ArrayLike, npt.ArrayLike]:
        """
        Compute back propagation for logistic regression.

        batch_size = X.shape[0]

        # derivative of the loss with respect to the pre-activation of the output layer
        # equivalent to d L d z = Y_hat - Y in non-weighted binary cross-entropy
        d_L_d_z = delta_weighted_bce(Y_hat, Y, self.class_weights)

        d_L_d_W = np.dot(X.T, d_L_d_z) / batch_size
        d_L_d_B = np.sum(d_L_d_z, axis=0) / batch_size

        if self.regularization == "L1":
            # add L1 regularization derivative
            d_L_d_W += self.lambda_reg * np.sign(self.W)
        else:
            # add L2 regularization derivative
            d_L_d_W += self.lambda_reg * self.W
        """
        return d_L_d_W, d_L_d_B

    def fit(self, X: npt.ArrayLike, Y: npt.ArrayLike, X_val: npt.ArrayLike, Y_val: npt.ArrayLike, plot: bool = False):
        """
        Fit the logistic regression model to the training data.

        n = X.shape[0]

        self.class_weights = compute_class_weight(class_weight="balanced", classes=np.array([0, 1]), y=Y)
        """

        losses_train = []
        losses_val = []

        for epoch in range(self.epochs):
            epoch_loss_train = 0.0
            for i in range(0, n, self.batch_size):
                X_batch = X[i : i + self.batch_size]
                Y_batch = Y[i : i + self.batch_size]

                Y_hat = self.forward(X_batch)
                d_L_d_W, d_L_d_B = self._backward(X_batch, Y_batch, Y_hat)

                self.W -= self.learning_rate * d_L_d_W
                self.B -= self.learning_rate * d_L_d_B

                batch_loss = weighted_binary_cross_entropy_loss(Y_hat, Y_batch, self.class_weights)
                epoch_loss_train += batch_loss * len(Y_batch)

            loss_train = epoch_loss_train / n

            Y_hat_val = self.forward(X_val)
            loss_val = weighted_binary_cross_entropy_loss(Y_hat_val, Y_val, self.class_weights)

            losses_train.append(loss_train)
            losses_val.append(loss_val)

            if plot:
                print(f"Epoch {epoch}: Train Loss: {loss_train}, Val Loss: {loss_val}")

        if plot:
            plt.plot(losses_train, label="Training Loss")
            plt.plot(losses_val, label="Validation Loss")
            plt.xlabel("Number of epochs")
            plt.ylabel("Loss")
            plt.title("Training and Validation Loss")
            plt.legend()
            plt.show()
            print("Training complete.")

```

```

1 You, 1 hour ago | 1 author (You)
2 class BinaryNeuralNetwork(object):
3     name = "Binary Neural Network"
4
5     def __init__(self,
6         n_features: int,
7         n_hidden_units: int,
8         n_hidden_layers: int,
9         epochs: int = 10,
10        learning_rate: float = 0.05,
11        batch_size: int = 32,
12        lambda_reg: float = 0.01,
13    ):
14        """
15            X: n_input x d_input
16            Y: n_input
17
18            self.W[0]: n_features x n_hidden_units
19            self.B[0]: n_hidden_units
20
21            self.W[i: 0 < i < (n_hidden-1)]: n_hidden_units x n_hidden_units
22            self.B[i: 0 < i < (n_hidden-1)]: n_hidden_units
23
24            self.W[-1]: n_hidden_units
25            self.B[-1]: 1
26
27            self.n_features = n_features
28            self.n_hidden_units = n_hidden_units
29            self.n_hidden_layers = n_hidden_layers
30            self.epochs = epochs
31            self.learning_rate = learning_rate
32            self.batch_size = batch_size
33            self.lambda_reg = lambda_reg
34
35            self.class_weights = np.zeros(2)
36
37            self.W = []
38            self.B = []
39
40            self.initialize_params()
41
42        def initialize_params(self):
43            """
44                Initialize weights and biases (He initialization)
45            for i in range(self.n_hidden_layers + 1):
46                if i == 0: # input -> h_1
47                    limit = np.sqrt(2 / (self.n_features))
48                    w = np.random.normal(0, limit, (self.n_features, self.n_hidden_units))
49                    b = np.zeros((self.n_hidden_units,))
50
51                elif i < self.n_hidden_layers: # h_i -> h_{i+1}
52                    limit = np.sqrt(2 / (self.n_hidden_units))
53                    w = np.random.normal(
54                        0, limit, (self.n_hidden_units, self.n_hidden_units)
55                    )
56                    b = np.zeros((self.n_hidden_units,))
57
58                else: # h_{n} -> output
59                    limit = np.sqrt(2 / (self.n_hidden_units))
60                    w = np.random.normal(0, limit, (self.n_hidden_units, 1))
61                    b = np.zeros((1,))
62
63                    self.W.append(w)
64                    self.B.append(b)
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```

You, last week • feat: own models

```

12 class BinaryNeuralNetwork(object):
13
14     def forward(self, X: npt.ArrayLike, return_intermediates=False) -> npt.ArrayLike:
15         """
16             Compute forward pass of the neural network.
17
18             Y_hat: n_samples
19
20             A = [X]
21             Z = []
22
23             # forward propagation
24             a_i = X
25             for i in range(self.n_hidden_layers + 1):
26                 z_i = np.dot(a_i, self.W[i]) + self.B[i] # add bias row-wise
27
28                 if i < self.n_hidden_layers:
29                     a_i = relu(z_i)
30                 else: # output layer
31                     z_i = z_i.squeeze() # transform (n_samples, 1) to (n_samples,)
32                     a_i = sigmoid(z_i) # (n_samples,)
33
34                     Z.append(z_i)
35                     A.append(a_i)
36
37             Y_hat = A[-1].squeeze()
38
39             if return_intermediates:
40                 return Y_hat, A, Z
41
42             return Y_hat
43
44     def predict(self, X: npt.ArrayLike) -> npt.ArrayLike:
45         """
46             Create a prediction matrix with `self.forward()`
47
48             pred: (n_samples,)
49
50             y_hat = self.forward(X)
51             pred = np.where(y_hat >= 0.5, 1, 0)
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53             return pred
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55     def predict_proba(self, X: npt.ArrayLike) -> npt.ArrayLike:
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57             Create a prediction matrix with `self.forward()`
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59             y_hat: (n_samples,)
60
61             y_hat = self.forward(X)
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63             return y_hat
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```

```

1 You, 1 hour ago | 1 author (You)
2 class BinaryNeuralNetwork(object):
3     name = "Binary Neural Network"
4
5     def __init__(self,
6         n_features: int,
7         n_hidden_units: int,
8         n_hidden_layers: int,
9         epochs: int = 10,
10        learning_rate: float = 0.05,
11        batch_size: int = 32,
12        lambda_reg: float = 0.01,
13    ):
14        """
15            X: n_input x d_input
16            Y: n_input
17
18            self.W[0]: n_features x n_hidden_units
19            self.B[0]: n_hidden_units
20
21            self.W[i: 0 < i < (n_hidden-1)]: n_hidden_units x n_hidden_units
22            self.B[i: 0 < i < (n_hidden-1)]: n_hidden_units
23
24            self.W[-1]: n_hidden_units
25            self.B[-1]: 1
26
27            self.n_features = n_features
28            self.n_hidden_units = n_hidden_units
29            self.n_hidden_layers = n_hidden_layers
30            self.epochs = epochs
31            self.learning_rate = learning_rate
32            self.batch_size = batch_size
33            self.lambda_reg = lambda_reg
34
35            self.class_weights = np.zeros(2)
36
37            self.W = []
38            self.B = []
39
40            self.initialize_params()
41
42        def initialize_params(self):
43            """
44                Initialize weights and biases (He initialization)
45            for i in range(self.n_hidden_layers + 1):
46                if i == 0: # input -> h_1
47                    limit = np.sqrt(2 / (self.n_features))
48                    w = np.random.normal(0, limit, (self.n_features, self.n_hidden_units))
49                    b = np.zeros((self.n_hidden_units,))
50
51                elif i < self.n_hidden_layers: # h_i -> h_{i+1}
52                    limit = np.sqrt(2 / (self.n_hidden_units))
53                    w = np.random.normal(
54                        0, limit, (self.n_hidden_units, self.n_hidden_units)
55                    )
56                    b = np.zeros((self.n_hidden_units,))
57
58                else: # h_{n} -> output
59                    limit = np.sqrt(2 / (self.n_hidden_units))
60                    w = np.random.normal(0, limit, (self.n_hidden_units, 1))
61                    b = np.zeros((1,))
62
63                    self.W.append(w)
64                    self.B.append(b)
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```

```

12 class BinaryNeuralNetwork(object):
13
14     def forward(self, X: npt.ArrayLike, return_intermediates=False) -> npt.ArrayLike:
15         """
16             Compute forward pass of the neural network.
17
18             Y_hat: n_samples
19
20             A = [X]
21             Z = []
22
23             # forward propagation
24             a_i = X
25             for i in range(self.n_hidden_layers + 1):
26                 z_i = np.dot(a_i, self.W[i]) + self.B[i] # add bias row-wise
27
28                 if i < self.n_hidden_layers:
29                     a_i = relu(z_i)
30                 else: # output layer
31                     z_i = z_i.squeeze() # transform (n_samples, 1) to (n_samples,)
32                     a_i = sigmoid(z_i) # (n_samples,)
33
34             Z.append(z_i)
35             A.append(a_i)
36
37             Y_hat = A[-1].squeeze()
38
39             if return_intermediates:
40                 return Y_hat, A, Z
41
42             return Y_hat
43
44     def predict(self, X: npt.ArrayLike) -> npt.ArrayLike:
45         """
46             Create a prediction matrix with `self.forward()`
47
48             pred: (n_samples,)
49
50             y_hat = self.forward(X)
51             pred = np.where(y_hat >= 0.5, 1, 0)
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53             return pred
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56         """
57             Create a prediction matrix with `self.forward()`
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59             y_hat: (n_samples,)
60
61             y_hat = self.forward(X)
62
63             return y_hat
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```

```

12 class BinaryNeuralNetwork(object):-
13
14     def _backward(-
15         self,-
16         Y: npt.ArrayLike,-
17         Y_hat: npt.ArrayLike,-
18         A: npt.ArrayLike,-
19         Z: npt.ArrayLike,-
20     ) -> Tuple[npt.ArrayLike, npt.ArrayLike]:-
21         """
22             Compute back propagation of the neural network.
23         """
24         batch_size = Y.shape[0]
25
26         d_L_d_W = [np.zeros_like(w) for w in self.W]
27         d_L_d_B = [np.zeros_like(b) for b in self.B]
28
29         # derivative of the loss with respect to the pre-activation of the output layer
30         d_L_d_z = delta_weighted_bce(Y_hat, Y, self.class_weights)
31         d_L_d_z = d_L_d_z.reshape(-1, 1) # reshape from (n_samples,) to (n_samples, 1)
32
33         # derivatives of the loss with respect to the weights and biases of the last layer
34         d_L_d_W[-1] = np.dot(A[-2].T, d_L_d_z) / batch_size
35         d_L_d_B[-1] = np.sum(d_L_d_z, axis=0) / batch_size
36
37         # back propagation using chain rule
38         for l in range(self.n_hidden_layers - 1, -1, -1):
39             d_L_d_z = np.dot(d_L_d_z, self.W[l + 1].T) * relu_prime(
40                 Z[l]
41             ) #  $d^l = (d^{l+1})^T \times W^{l+1} \times (dA^l / dz^l)$ 
42
43             d_L_d_W[l] = (
44                 np.dot(A[l].T, d_L_d_z) / batch_size
45             ) # note: A[l] is actually correct here - A[0] is X!
46             d_L_d_B[l] = np.sum(d_L_d_z, axis=0) / batch_size
47
48             # add L2 regularization derivative
49             d_L_d_W[l] += self.lambda_reg * self.W[l]
50
51         return d_L_d_W, d_L_d_B
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```

```

12 class BinaryNeuralNetwork(object):-
13
14     def _backward(-
15         self,-
16         Y: npt.ArrayLike,-
17         Y_hat: npt.ArrayLike,-
18         A: npt.ArrayLike,-
19         Z: npt.ArrayLike,-
20     ) -> Tuple[npt.ArrayLike, npt.ArrayLike]:-
21         """
22             Compute back propagation of the neural network.
23         """
24         batch_size = Y.shape[0]
25
26         d_L_d_W = [np.zeros_like(w) for w in self.W]
27         d_L_d_B = [np.zeros_like(b) for b in self.B]
28
29         # derivative of the loss with respect to the pre-activation of the output layer
30         d_L_d_z = delta_weighted_bce(Y_hat, Y, self.class_weights)
31         d_L_d_z = d_L_d_z.reshape(-1, 1) # reshape from (n_samples,) to (n_samples, 1)
32
33         # derivatives of the loss with respect to the weights and biases of the last layer
34         d_L_d_W[-1] = np.dot(A[-2].T, d_L_d_z) / batch_size
35         d_L_d_B[-1] = np.sum(d_L_d_z, axis=0) / batch_size
36
37
38         # back propagation using chain rule
39         for l in range(self.n_hidden_layers - 1, -1, -1):
40             d_L_d_z = np.dot(d_L_d_z, self.W[l + 1].T) * relu_prime(
41                 Z[l]
42             ) #  $d^l = (d^{l+1})^T \times W^{l+1} \times (dA^l / dz^l)$ 
43
44             d_L_d_W[l] = (
45                 np.dot(A[l].T, d_L_d_z) / batch_size
46             ) # note: A[l] is actually correct here - A[0] is X!
47             d_L_d_B[l] = np.sum(d_L_d_z, axis=0) / batch_size
48
49             # add L2 regularization derivative
50             d_L_d_W[l] += self.lambda_reg * self.W[l]
51
52
53         return d_L_d_W, d_L_d_B
54
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```

```
5  def weighted_binary_cross_entropy_loss(←
6  |     output, target, class_weights=None, epsilon=0.001←
7  ):←
8  """←
9      Compute the weighted binary cross-entropy loss.←
10     """←
11     if class_weights is None:←
12         class_weights = compute_class_weights(target)←
13     ←
14     # avoiding numerical instability←
15     output = np.clip(output, epsilon, 1 - epsilon)←
16     ←
17     loss = class_weights[1] * (target * np.log(output)) + class_weights[0] * (←
18     |     (1 - target) * np.log(1 - output)←
19     )←
20     ←
21     return -np.mean(loss)←
22     ←
23     ←
24     def compute_class_weights(y: npt.ArrayLike) -> npt.ArrayLike:←
25     """←
26         Compute class weights for imbalanced datasets.←
27     """←
28     y = np.array(y, dtype=np.int64)←
29     classes = np.unique(y)←
30     class_counts = np.bincount(y)←
31     total_samples = len(y)←
32     ←
33     class_weights = {←
34         cls: total_samples / (len(classes) * count)←
35         for cls, count in zip(classes, class_counts)←
36     }←
37     ←
38     weights_array = np.array([class_weights[cls] for cls in classes], dtype=np.float64)←
39     ←
40     return weights_array
```

```
5  def weighted_binary_cross_entropy_loss(←
6  |     output, target, class_weights=None, epsilon=0.001←
7  ):←
8  """←
9      Compute the weighted binary cross-entropy loss.←
10     """←
11     if class_weights is None:←
12         class_weights = compute_class_weights(target)←
13     ←
14     # avoiding numerical instability←
15     output = np.clip(output, epsilon, 1 - epsilon)←
16     ←
17     loss = class_weights[1] * (target * np.log(output)) + class_weights[0] * (←
18     |     (1 - target) * np.log(1 - output)←
19     )←
20     ←
21     return -np.mean(loss)←
22     ←
23     ←
24     def compute_class_weights(y: npt.ArrayLike) -> npt.ArrayLike:←
25     """←
26         Compute class weights for imbalanced datasets.←
27     """←
28     y = np.array(y, dtype=np.int64)←
29     classes = np.unique(y)←
30     class_counts = np.bincount(y)←
31     total_samples = len(y)←
32     ←
33     class_weights = {←
34         cls: total_samples / (len(classes) * count)←
35         for cls, count in zip(classes, class_counts)←
36     }←
37     ←
38     weights_array = np.array([class_weights[cls] for cls in classes], dtype=np.float64)←
39     ←
40     return weights_array
```

# 4. Feature Selection for Logistic Regression

- Polynomial Features, Primal Decision Function
- Principal Components through Principal Component Analysis
- Feature Selection using custom backward selection protocol

# 4. Feature Selection for Logistic Regression

- Feature Selection Protocol: Backward Selection
  - delete one feature per iteration
  - train LogisticRegression model, calculate risk estimate on validation set at each step
  - as soon as all but one features are deleted: return the features that the model with the lowest risk estimate was trained on

```
42 def feature_selection(-
43     X,
44     y,
45     n_features_per_iteration: int = 1,
46     plot: bool = False,
47 ):-:
48     n_features = X.shape[1]
49     deleted_features = []
50     optimal_number_of_features_to_delete = 0
51
52     risk_estimates = [np.inf]
53     lowest_risk_estimate = np.inf
54
55     X_tmp = X.copy()
56     y_tmp = y.copy()
57
58     original_indices = np.arange(n_features)
59
60     for i in range(0, n_features - 1):
61         X_train, X_val, y_train, y_val = train_test_split(
62             X_tmp, y_tmp, test_size=0.2, random_state=42
63         )
64         model = LogisticRegression(
65             penalty="l1",
66             solver="liblinear",
67             max_iter=1000,
68             class_weight="balanced",
69         )
69         log_reg_tmp = model.fit(X_train, y_train)
70         y_pred = log_reg_tmp.predict_proba(X_val)[:, 1]
71         risk_estimate = weighted_binary_cross_entropy_loss(y_pred, y_val)
72         log_message = f"i = {i} / {n_features-1} - Empirical Risk Estimate: {risk_estimate}, Previous Estimate: {risk_estimates[-1]}"
73
74         features_to_delete = np.argsort(np.abs(log_reg_tmp.coef_))[0][
75             :n_features_per_iteration
76         ]
77         deleted_features.extend(original_indices[features_to_delete].tolist())
78
79         X_tmp = np.delete(X_tmp, features_to_delete, axis=1)
80         original_indices = np.delete(original_indices, features_to_delete)
81
82         risk_estimates.append(risk_estimate)
83
84         if risk_estimate < lowest_risk_estimate:
85             lowest_risk_estimate = risk_estimate
86             optimal_number_of_features_to_delete = i
87             log_message += " - new lowest risk estimate"
88
89         print(log_message)
90
91     features_to_delete = deleted_features[:optimal_number_of_features_to_delete]
92
93     if plot:
94         print(
95             f"Number of features to delete: {optimal_number_of_features_to_delete} / {n_features}"
96         )
97
98         plt.plot(
99             range(
100                 0, n_features - 1 + n_features_per_iteration, n_features_per_iteration
101             ),
102             risk_estimates,
103             label="Training Loss",
104         )
105         plt.xlabel("Number of deleted features")
106         plt.ylabel("Weighted Binary Cross Entropy Loss")
107         plt.title("Risk estimate as a function of deleted features")
108         plt.legend()
109         plt.show()
110
111
112     return features_to_delete, risk_estimates
```

# 5. Model Selection & Evaluation Protocol

- Nested Cross-Validation protocol for hyper parameter tuning and evaluation
  - 5-fold outer loop, 5-fold inner loop
    - inner loop: iterate over all given hyper parameter sets, calculate empirical risk estimate per iteration using 5-fold cross-validation
    - outer loop: 5-fold split of the data
  - after outer loop: average empirical risk estimates per hyper parameter set, pick set with lowest empirical risk estimate, evaluate model using 5-fold cross-validation, fit final model on whole training set

```
1 param_grid_lr = {  
2     "n_features": [X_selected.shape[1]],  
3     "epochs": [10, 20, 30],  
4     "learning_rate": [0.1, 0.05, 0.01],  
5     "lambda_reg": [0.1, 0.01, 0.001],  
6 }
```

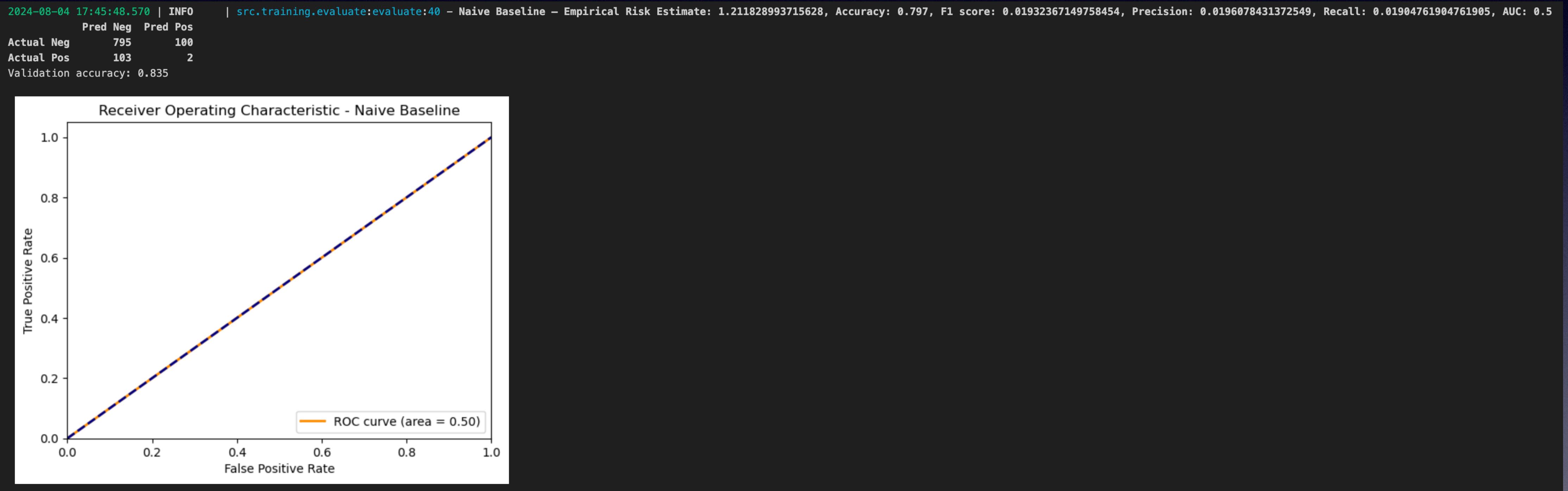
```
1 param_grid_nn = {  
2     "n_features": [X_original.shape[1]],  
3     "epochs": [10, 20, 30],  
4     "learning_rate": [0.1, 0.05, 0.01],  
5     "lambda_reg": [0.1, 0.01, 0.001],  
6     "n_hidden_units": [16, 32, 64],  
7     "n_hidden_layers": [1, 2],  
8 }
```

```

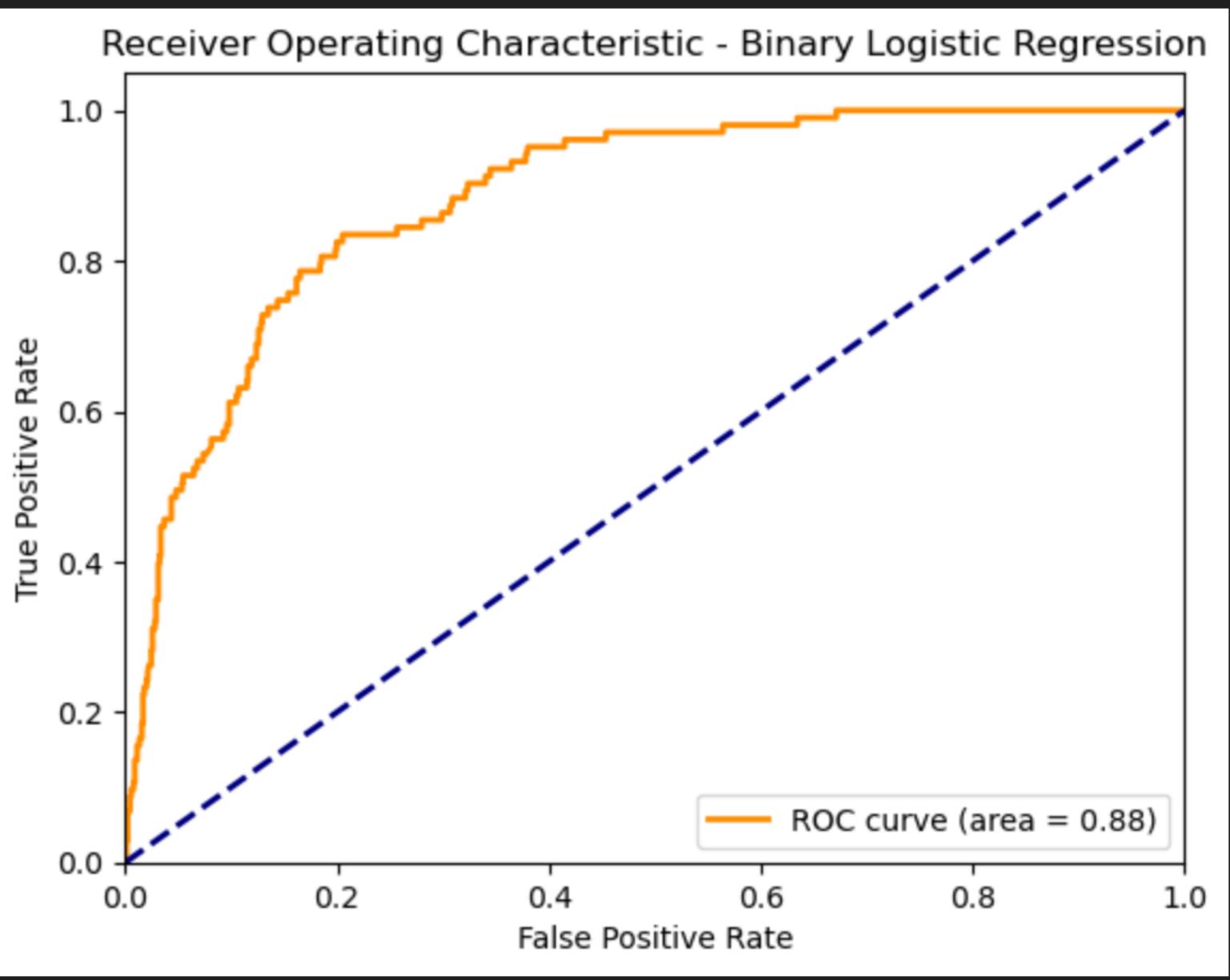
146 def nested_cross_validation(X, y, Model, param_grid, k=5):
147     print(
148         f"Performing nested cross-validation for model {Model.name} with {X.shape[0]} samples"
149     )
150     # list of one dict per parameter combination
151     param_combinations = [
152         dict(zip(param_grid.keys(), values)) for values in product(*param_grid.values())
153     ]
154     n_combinations = len(param_combinations)
155
156     R_est = np.zeros((k, len(param_combinations)))
157
158     kf_outer = KFold(n_splits=k, shuffle=True)
159
160     for i, (outer_train_idx, outer_test_idx) in enumerate(kf_outer.split(X)):
161         X_train_outer, X_val_outer = X[outer_train_idx], X[outer_test_idx]
162         y_train_outer, y_val_outer = y[outer_train_idx], y[outer_test_idx]
163
164         for j, params in enumerate(param_combinations):
165             model = Model(**params)
166
167             R_est[i, j] = k_fold_cross_validation(
168                 model, X_train_outer, y_train_outer, k=k, fit_final_model=False
169             )
170             print(
171                 f"Empirical risk estimate for fold {i+1} / {k}, parameter set {j+1} / {n_combinations}: {R_est[i, j]}",
172                 end="\r",
173             )
174
175     R_est_params = np.mean(R_est, axis=0)
176
177     params = param_combinations[np.argmin(R_est_params)]
178     print(
179         f"Risk estimate for argmin(R_est_params): {R_est_params[np.argmin(R_est_params)]}"
180     )
181     print(f"Selected best parameters: {params}")
182
183     model_final = Model(**params)
184     model_final_trained, R_est, acc, f1, auc, prec, rec, cm_df, fpr, tpr = (
185         k_fold_cross_validation(model_final, X, y, k=k, fit_final_model=True)
186     )
187     print(
188         f"{Model.name} - Empirical Risk Estimate: {R_est}, Accuracy: {acc}, F1 score: {f1}, Precision: {prec}, Recall: {rec}, AUC: {auc}\n{cm_df}"
189     )
190
191     # Plot ROC curve
192     plt.figure()
193     plt.plot(fpr, tpr, color="darkorange", lw=2, label=f"ROC curve (area = {auc:0.2f})")
194     plt.plot([0, 1], [0, 1], color="navy", lw=2, linestyle="--")
195     plt.xlim([0.0, 1.0])
196     plt.ylim([0.0, 1.05])
197     plt.xlabel("False Positive Rate")
198     plt.ylabel("True Positive Rate")
199     plt.title(f"Receiver Operating Characteristic - {Model.name}")
200     plt.legend(loc="lower right")
201     plt.show()
202
203     return model_final_trained, params, R_est, acc, f1, auc

```

# 6. Results – Naive Baseline



# 6. Results – Logistic Regression

```
[49] ✓ 2m 5.4s
...
... Performing nested cross-validation for model Binary Logistic Regression with 5000 samples
Risk estimate for argmin(R_ests_params): 0.431203867143375447: 0.44956165679782895
Selected best parameters: {'n_features': 3, 'epochs': 20, 'learning_rate': 0.1, 'lambda_reg': 0.001}
Binary Logistic Regression - Empirical Risk Estimate: 0.4326625244737709, Accuracy: 0.7598, F1 score: 0.4106326848282034, Precision: 0.27178922773035485, Recall: 0.8410820460604125, AUC: 0.8783259164403588
      Pred Neg  Pred Pos
Actual Neg      678      219
Actual Pos       17       86
...
...
Receiver Operating Characteristic - Binary Logistic Regression


The figure is a Receiver Operating Characteristic (ROC) plot titled "Receiver Operating Characteristic - Binary Logistic Regression". It features two axes: the x-axis is labeled "False Positive Rate" and ranges from 0.0 to 1.0, and the y-axis is labeled "True Positive Rate" and also ranges from 0.0 to 1.0. A solid orange line represents the "ROC curve (area = 0.88)". This curve starts at (0,0), rises steeply to approximately (0.05, 0.5), and then continues to rise more gradually, reaching (1.0, 1.0). A dashed blue diagonal line from (0,0) to (1,1) represents a random classifier.


```

# 6. Results – Neural Network

```
[50] ✓ 20m 28.7s
...
... Performing nested cross-validation for model Binary Neural Network with 5000 samples
Risk estimate for argmin(R_est_params): 0.43757705619196885162: 0.45009287877300624
Selected best parameters: {'n_features': 16, 'epochs': 30, 'learning_rate': 0.05, 'lambda_reg': 0.01, 'n_hidden_units': 32, 'n_hidden_layers': 1}
Binary Neural Network - Empirical Risk Estimate: 0.43897262965985584, Accuracy: 0.7506, F1 score: 0.4066613515367429, Precision: 0.2672795367251504, Recall: 0.85771651065744, AUC: 0.8732469714613273
    Pred Neg  Pred Pos
Actual Neg      655      255
Actual Pos       13       77
...
...
Receiver Operating Characteristic - Binary Neural Network



The figure is a Receiver Operating Characteristic (ROC) plot titled "Receiver Operating Characteristic - Binary Neural Network". The x-axis is labeled "False Positive Rate" and ranges from 0.0 to 1.0. The y-axis is labeled "True Positive Rate" and ranges from 0.0 to 1.0. A solid orange line represents the "ROC curve (area = 0.87)". A dashed blue diagonal line represents a random classifier. The ROC curve starts at (0,0), rises steeply, and then levels off towards the top-left corner of the plot.


```

# 6. Results – Comparison

- Logistic Regression model slightly outperforms Neural Network model regarding AUC and F1
  - Logistic Regression model is better at separating classes across decision thresholds and at threshold of 0.5
- Neural Network model slightly outperforms Logistic Regression model in recall, but lacks behind in precision
  - It is more liberal: less false negatives, but more false positives

## 7. Conclusion

- The Logistic Regression model slightly outperforms the Neural Network
  - AUC metric is especially important in medical context
  - Minimizing false negatives may be more important than maximizing F1
- The competitive edge of the Logistic Regression model is not large
- Neural Network's ability to derive non-linear relations on its own does not grant performance edge, given the data set at hand

# 7. Conclusion

- Future work could focus on:
  - Leveraging more comprehensive data set and more complex Neural Network architecture: Might boost Neural Network performance
  - Creating higher-order polynomials and use dual decision functions: Might boost Logistic Regression performance and computational efficiency – but might as well lead to overfitting
  - Implementing adaptive learning in Neural Network: potentially allow convergence in better minima