

CSC 148: Introduction to Computer Science

Week 7

Recursion (continued)

List comprehensions, recursion efficiency



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New Lists from Old

- Suppose L is a list of the first hundred natural numbers
 $L = \text{list}(\text{range}(100))$
- If I want a new list with the squares of all the elements of L,

I could:

```
new_list = []  
for x in L:  
    new_list.append(x * x)
```

- Or I could use the equivalent list comprehension

```
new_list = [x * x for x in L]
```



Filtering with [...]

- I can make sure my new list only uses specific elements of the old list ...

```
L = ["one", "two", "three", "four", "five", "six"]
```

by adding a condition ...

```
New_list = [s * 3  
             for s in L  
             if s <= "one"]
```

- Notice that a comprehension can span several lines, if that makes it easier to understand



General comprehension pattern

`[expression for name in iterable if condition]`

- *expression* evaluates to a value
- *name* refers to each element in the iterable (list, tuple, dict, ...)
- *condition* (optional) evaluates to either True or False



Practice ... worksheet



Recall: Sum of Elements in Nested List

- $L = [1, [5, 3], 8, [4, [9, 7]]]$

```
def sum_list(L):  
    if isinstance(L, list):  
        s = 0  
        for elem in L:  
            # calculate the sum of the sublist "elem" recursively  
            s += sum_list(elem)  
        return s  
    else:  
        return L
```

recursive step

base case

⇒ We could rewrite the recursive step using list comprehensions:

```
if isinstance(L, list):  
    return sum([sum_list(elem) for elem in L])
```



Sum of list elements – nested lists

- $L = [1, [5, 3], 8, [4, [9, 7]]]$

```
def sum_list(L):
```

```
recursive step { if isinstance(L, list):  
                  return sum([sum_list(elem) for elem in L])  
base case { else:  
             return L
```



- Can we make this even more compact?



Sum of list elements – nested lists

- $L = [1, [5, 3], 8, [4, [9, 7]]]$

```
def sum_list(L):
```

```
    return sum([sum_list(elem) if isinstance(elem, list) else elem  
                for elem in L])
```




More Complex: `semi_homogeneous`

- A single integer and empty list are semi-homogeneous.
- In general, a list is semi-homogeneous if and only if:
 - (all of its sub-nested-lists are integers) OR (all of them are lists)
 - all of its sub-nested-lists are semi-homogeneous