

CSC 148: Introduction to Computer Science

Week 9

Tree traversals

Binary Search Trees (BSTs)



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Today: Tree Traversals

- Formalize strategies for traversing any **general** Tree
 - BSTs are just a special type of Tree ...
 - Hence, traversals are similar



Functions as Arguments

```
def list_if(self, p: Callable[[Any], bool]) -> list[Any]:  
    """Return a list of values in this Tree that satisfy predicate <p>.
```

Parameter <p> is a function which takes a single value argument and checks some predicate on that value, returning True or False.

```
    """
```

```
    pass
```

Idea: if self._root is empty => return []

if it's a leaf => [self._root] if p(self._root) else []

otherwise => call recursively for each subtree in self._subtrees
and construct the list of values that satisfy p



Traversal

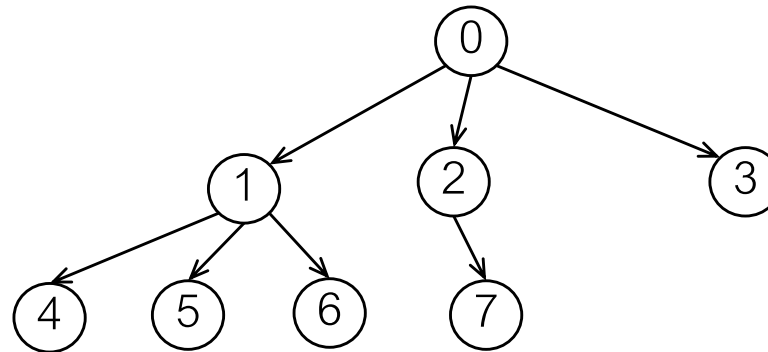
- The functions and methods we have seen get information from every node of the tree -- in some sense they **traverse** the tree
- Sometimes the **order** of processing tree nodes is important:
 - Do we process the root of the tree (and the root of each subtree...) before or after its children?
 - Or, perhaps, we process along levels that are the same distance from the root?



Preorder Traversal

- Visit each node of Tree t as follows:
 - do something with the node / value, e.g., print it
 - visit its first subtree **in preorder**
 - visit its second subtree **in preorder**
 - ...

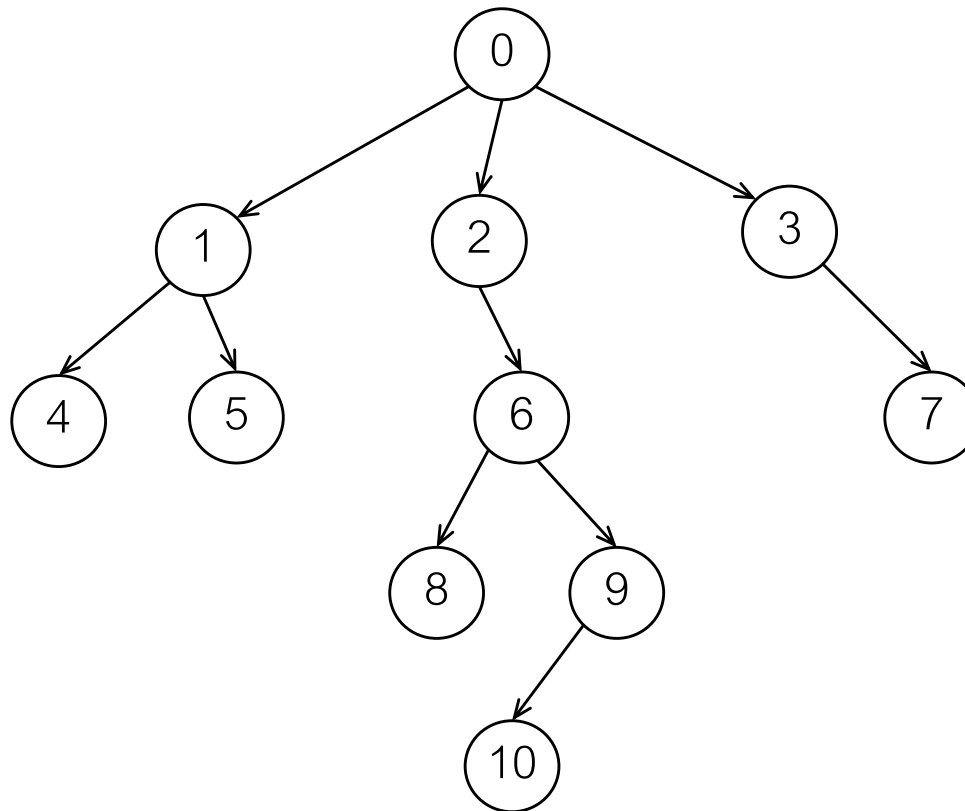
What is the sequence of nodes being visited in preorder?





Preorder – More Examples

- Visit each node of Tree t as follows:
 - do something with the node / value, e.g., print it
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 - ...

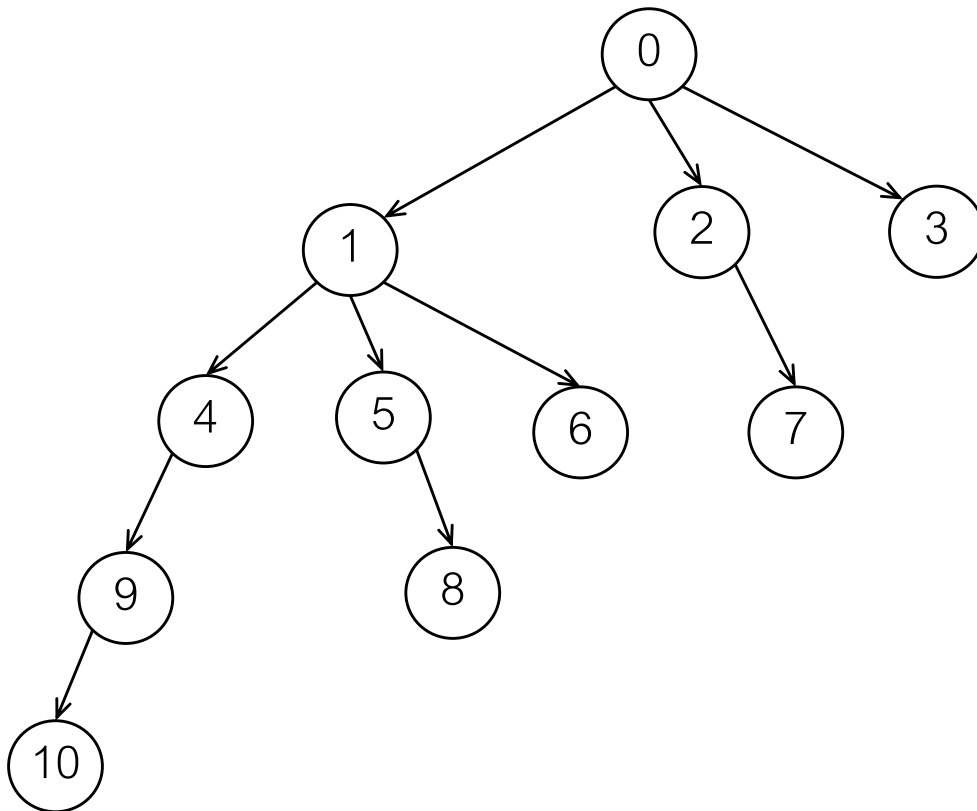


What is the sequence of nodes being visited in preorder?



Preorder - More Examples

- Visit each node of Tree t as follows:
 - do something with the node / value, e.g., print it
 - visit its first subtree **in preorder**
 - visit its second subtree **in preorder**
 - ...



What is the sequence of nodes being visited in preorder?

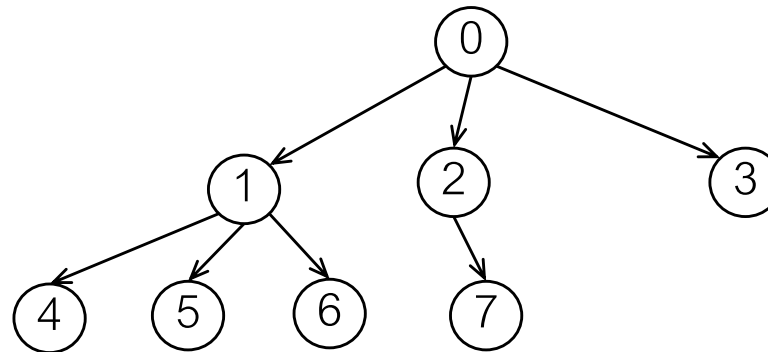
Any thoughts on how to implement this visit order?



Postorder Traversal

- Visit each node of Tree t as follows:
 - visit its first subtree **in postorder**
 - visit its second subtree **in postorder**
 - ...
 - do something with the node / value, e.g., print it

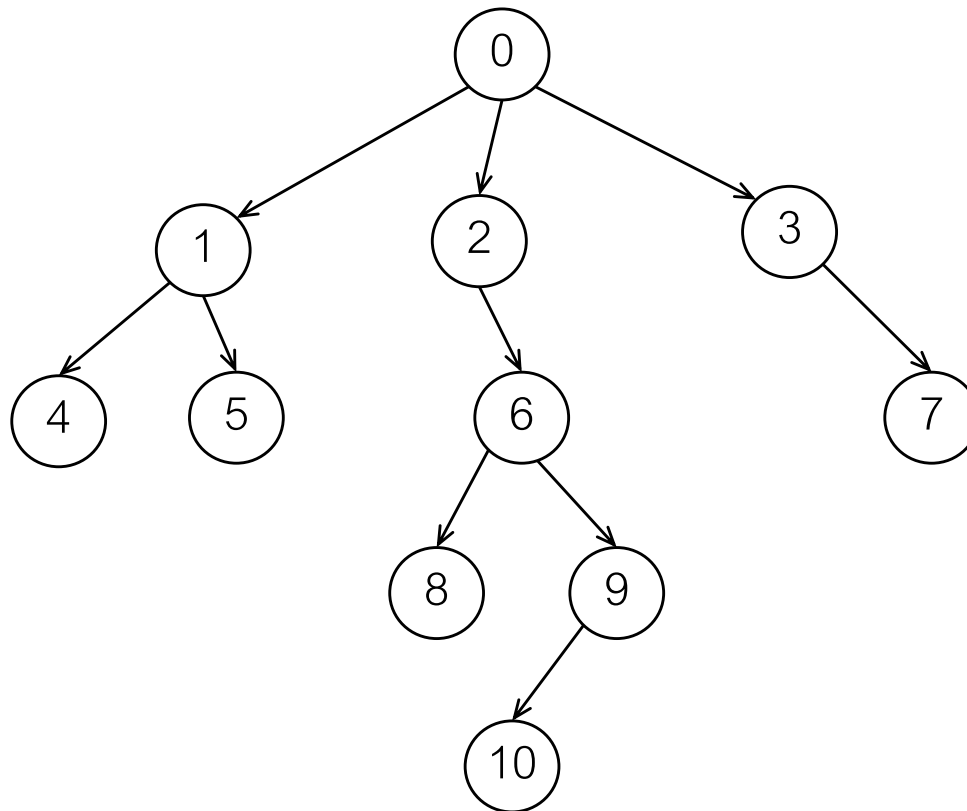
What is the sequence of nodes being visited in postorder?





Postorder – More Examples

- Visit each node of Tree t as follows:
 - visit its first subtree **in postorder**
 - visit its second subtree **in postorder**
 - ...
 - do something with the node / value, e.g., print it

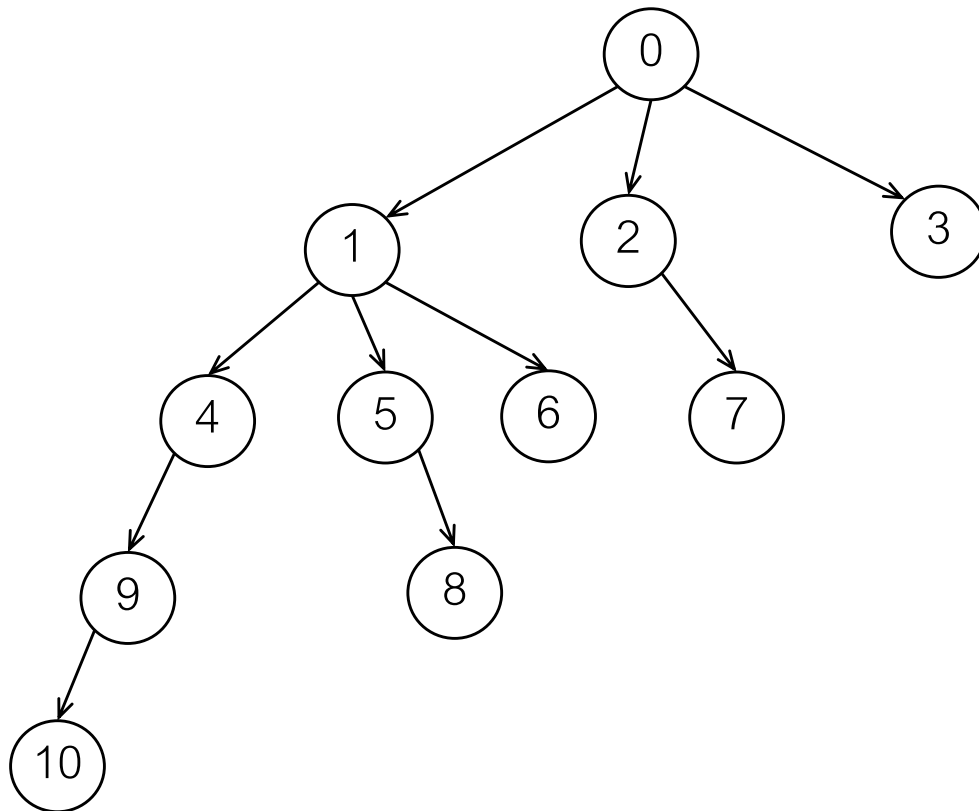


What is the sequence of nodes being visited in postorder?



Postorder – More Examples

- Visit each node of Tree t as follows:
 - visit its first subtree **in postorder**
 - visit its second subtree **in postorder**
 - ...
 - do something with the node / value, e.g., print it



What is the sequence of nodes being visited in postorder?

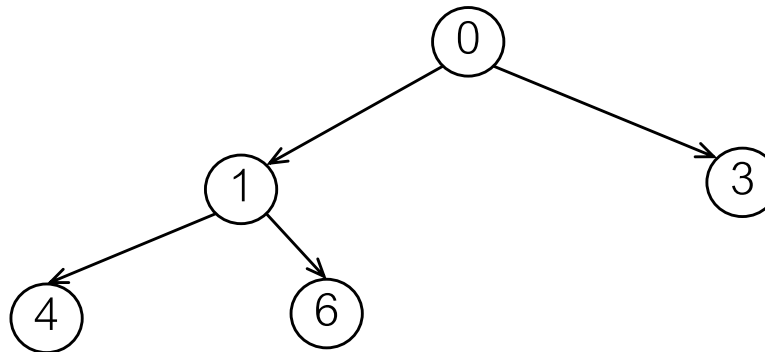
Any thoughts on how to implement this visit order?



Inorder Traversal (BST only)

- Visit each node of Tree t as follows:
 - visit its first subtree **in inorder**
 - do something with the node / value, e.g., print it
 - visit its second subtree **in inorder**

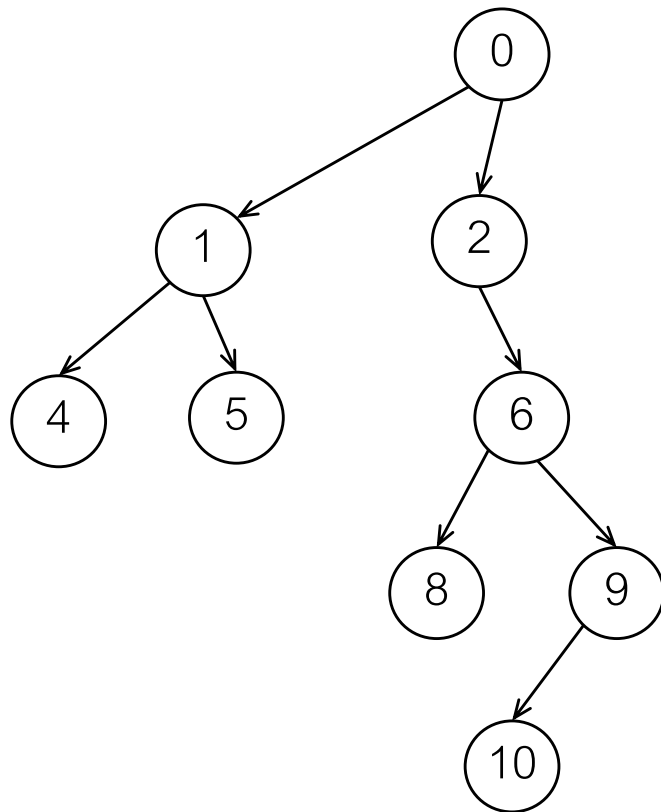
What is the sequence of nodes being visited in inorder?





Inorder – More Examples

- Visit each node of Tree t as follows:
 - visit its first subtree **in inorder**
 - do something with the node / value, e.g., print it
 - visit its second subtree **in inorder**

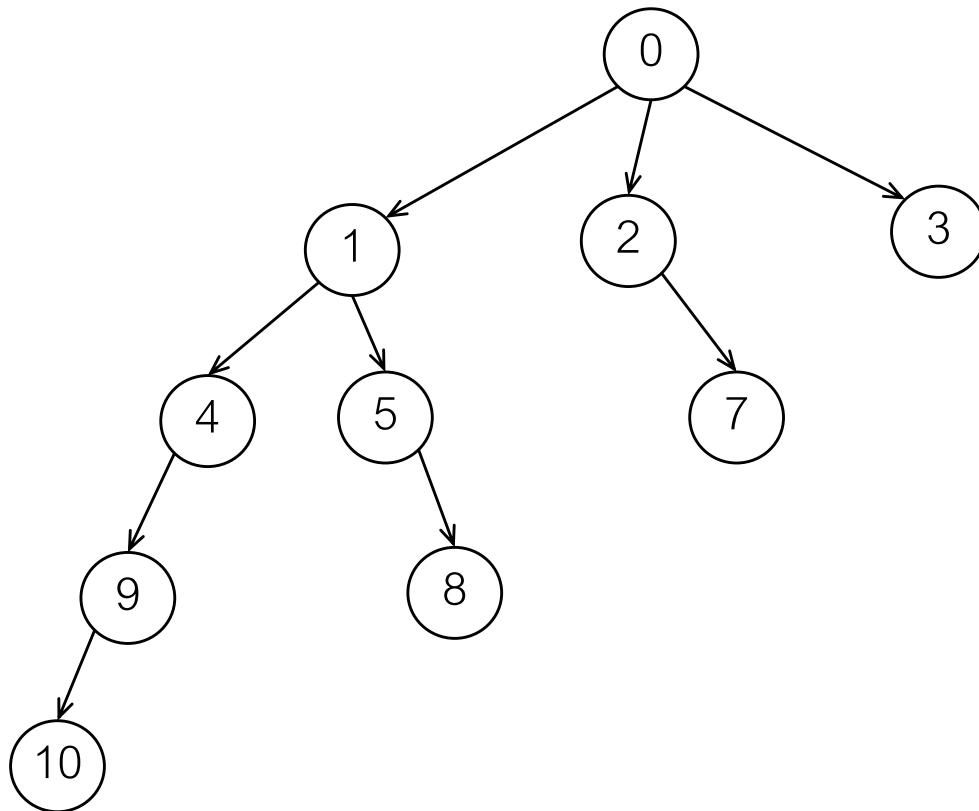


What is the sequence of nodes being visited in inorder?



Inorder – More Examples

- Visit each node of Tree t as follows:
 - visit its first subtree **in inorder**
 - do something with the node / value, e.g., print it
 - visit its second subtree **in inorder**



What is the sequence of nodes being visited in inorder?

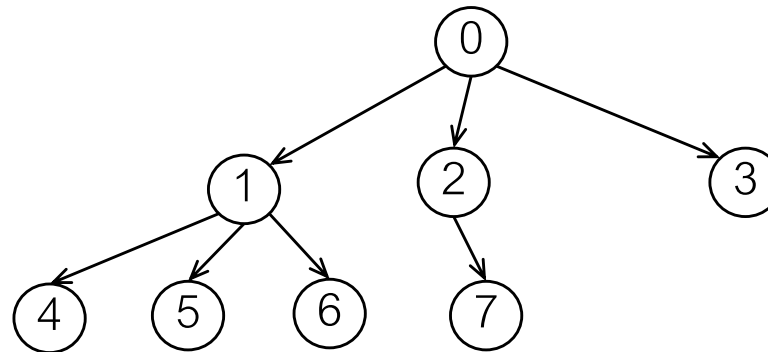
Any thoughts on how to implement this visit order?



Level-order Traversal

- Visit each node of Tree t as follows:
 - do something with the node / value, e.g., print it
 - visit all its children (**first level** in the tree) and act on the nodes
 - visit all the children's children (**second level** in the tree) and act on the nodes
 - visit **third level** in the tree, etc..

What is the sequence of nodes being visited in level order?

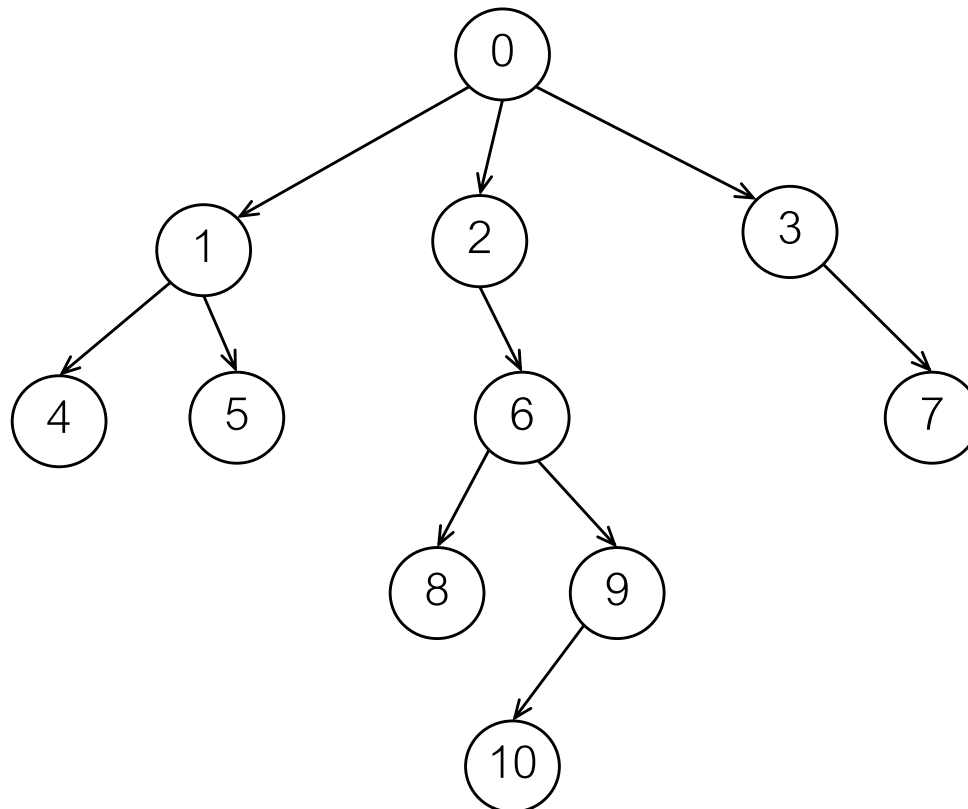




Level-order

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What is the sequence of nodes being visited in level order?



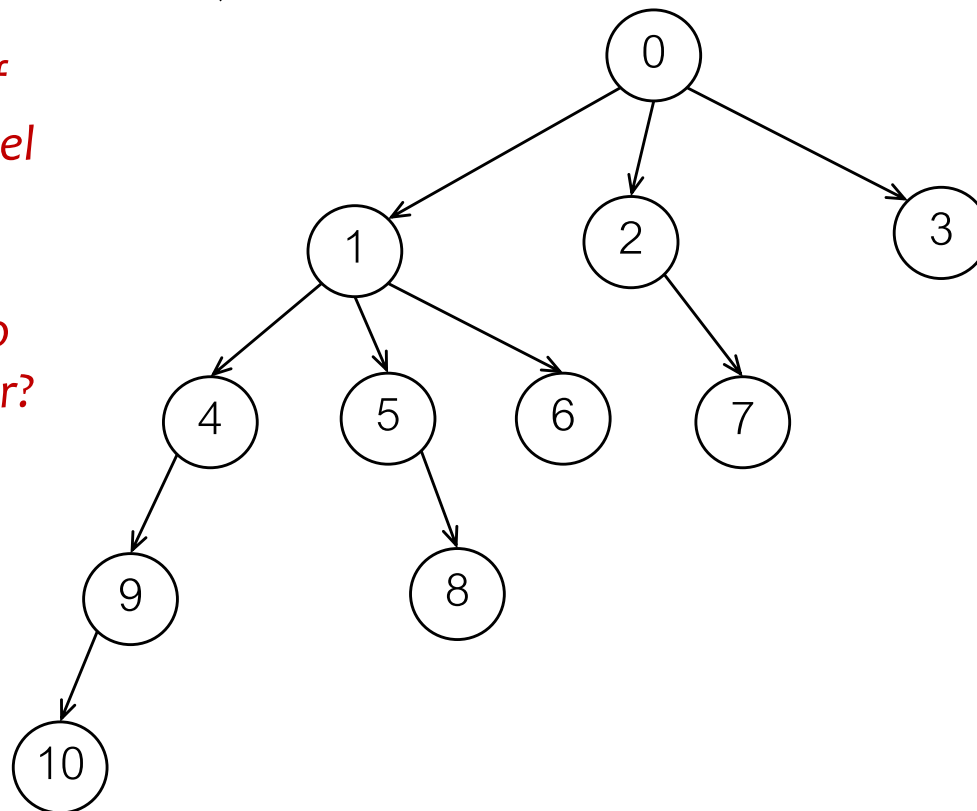


Level-order

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 - visit all its children (**first level** in the tree) and act on the nodes
 - visit all the children's children (**second level** in the tree) and act on the nodes
 - visit **third level** in the tree, etc..

What is the sequence of nodes being visited in level order?

Any thoughts on how to implement this visit order?





Worksheet

- Tree traversals...



Queues, Stacks, Recursion

- You may have noticed in the code for level order visit that there were no recursive calls, and a queue was used to process a recursive structure in level order
- Careful use of a stack allows you to process a tree in preorder, postorder, or inorder (no recursion needed)
- Remember recursive vs. iterative discussion from last week