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For each of the following  $T(n)$ , write the corresponding Big O time complexity. Some series may require research.

1. (2 points)  $T(n) = n^2 + 3n + 2$
2. (2 points)  $T(n) = (n^2 + n)(n^2 + \frac{n}{2})$
3. (2 points)  $T(n) = 1 + 2 + 3 + \dots + n - 1 + n$
4. (3 points)  $T(n) = 1^2 + 2^2 + 3^2 + \dots + (n-1)^2 + n^2$
5. (2 points)  $T(n) = 10$
6. (2 points)  $T(n) = 10^{100}$
7. (2 points)  $T(n) = n + \log n$
8. (2 points)  $T(n) = 12 \log(n) + \frac{n}{2} - 400$
9. (4 points)  $T(n) = (n+1) \cdot \log(n) - n$
10. (4 points)  $T(n) = \frac{n^4 + 3n^2 + 2n}{n}$

1.  $O(n)^2$

2.  $O(n^4)$

3.  $O(n)$

4.  $O(n^2)$

5.  $O(n)$

6.  $O(n)$

7.  $O(n)$

8.  $O(n)$

9.  $O(\log n)$

10.  $O(n^3)$

11. (5 points) What is the time complexity to insert or remove an item in the middle of an ArrayList?

Inserting or deleting in middle  
 $O(n)$

12. (5 points) Why?

Inserting an item in the middle of an ArrayList will need to work  $O(n)$  times to relocate the size of the array. Same with deleting anything from middle of the ArrayList the list has to shift one block which make it work  $O(n)$  time.

13. (5 points) What is the average time complexity to add an item to the end of an ArrayList?

$O(1)$  add and remove at end.

14. (5 points) What is the worst case time complexity to add an item to the end of an ArrayList?

$O(n)$  add remove in the interior.

$O(n)$  Find by target value.

15. (5 points) Taking this all into account, what situations would an ArrayList be the appropriate data structure for storing your data?

Appropriate data structure for storing is inserting at the end of the ArrayList.

```

public static int[] allEvensUnder(int limit){
    if (limit <= 0){
        return new int[0];
    }
    if (limit < 2){
        return new int[1];
    }
    int[] vals = new int[(limit+1)/2];
    for(int i = 0; i < (limit+1)/2 ; i++){
        vals[i] = i*2;
    }
    return vals;
}

```

16. (10 points) What is the time complexity of the above algorithm?

$O(n)$

17. (5 points) What is the space complexity of the above algorithm? In other words, how much space is used up based on the input size?

$O(n)$

```

/*
 * https://rosettacode.org/wiki/Sorting\_algorithms/Insertion\_sort#Java
 */
public static void insertSort(int[] A){
    for(int i = 1; i < A.length; i++){
        int value = A[i];
        int j = i - 1;
        while(j >= 0 && A[j] > value){
            A[j + 1] = A[j];
            j = j - 1;
        }
        A[j + 1] = value;
    }
}

```

18. (10 points) What is the time complexity of the above algorithm?

$O(n^2)$

`bogosort` attempts to sort a list by shuffling the items in the list. If the list is unsorted after shuffling, we continue shuffling the list and checking until it is finally sorted.

19. (5 points) What is the worst case run time for `bogosort`?

$$O(\infty)$$

20. (5 points) Why?

The worst case is infinite since there is no guarantee that a random shuffling will ever produce a sorted sequence.

21. (5 points) What is the average case run time for `bogosort` (Hint: think about a deck of cards)?

$$O(n)!$$

22. (10 points) Why?

Because the chance that any given shuffle of a set will end up in sorted order is about  $1/n!$ .