Computer Organization and Architecture

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Question -1:

a) Recursion

```
Code:
```

```
#include <iostream>
#include <ctime>
using namespace std;
long long fibonacci recursion(int n) {
  if (n \le 1) return n;
  return fibonacci_recursion(n - 1) + fibonacci_recursion(n - 2);
}
int main() {
  struct timespec start, end;
  clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &start);
  for (int i = 0; i < 50; ++i) {
     cout << fibonacci recursion(i) << " ";</pre>
  clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &end);
  double time_taken = (end.tv_sec - start.tv_sec) + (end.tv_nsec - start.tv_nsec)
/ 1e9;
  cout << "\nRecursion Time: " << time taken << " seconds\n";
  return 0;
}
```

pavandeekshith@Pavans-MacBook-Air-8 Question-1 % cd "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-1/" && g++ recursion.cpp -o recursion && "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-1/"recursion
0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 987 1597 2584 4181 6765 10946 17711 28657 46368 75025 121393 196418 317811 514229 832040 13
46269 2178309 3524578 5702887 9227465 14930352 24157817 39088169 63245986 102334155 165580141 267914296 433494437 701408733 1134903170 1
836311903 2971215073 4807526976 7778742049
Recursion Time: 179.22 seconds

```
b) Loop
```

```
Code:
#include <iostream>
#include <ctime>
using namespace std;
void fibonacci loop(int n) {
  long long a = 0, b = 1, next;
  for (int i = 0; i < n; ++i) {
     cout << a << " ";
     next = a + b;
     a = b;
     b = next;
  }
}
int main() {
  struct timespec start, end;
  clock gettime(CLOCK PROCESS CPUTIME ID, &start);
  fibonacci loop(50);
  clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &end);
double time_taken = (end.tv_sec - start.tv_sec) + (end.tv_nsec - start.tv_nsec)/ 1e9;
  cout << "\nLoop Time: " << time_taken << " seconds\n";
  return 0;
}
```

pavandeekshith@Pavans-MacBook-Air-8 Question-1 % cd "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Ques tion-1/" && g++ loop.cpp -o loop && "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-1/"loop 0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 987 1597 2584 4181 6765 10946 17711 28657 46368 75025 121393 196418 317811 514229 832040 13 46269 2178309 3524578 5702887 9227465 14930352 24157817 39088169 63245986 102334155 165580141 267914296 433494437 701408733 1134903170 1 836311903 2971215073 4807526976 7778742049 Loop Time: 2.2e-05 seconds

Speed up = 81.36 * 10^5 times faster than baseline

c) Recursion and memoization

```
Code:
#include <iostream>
#include <vector>
#include <ctime>
using namespace std;
vector<long long> memo(51, -1);
long long fibonacci_recursion_memo(int n) {
  if (n \le 1) return n;
  if (memo[n] != -1) return memo[n];
  return memo[n] = fibonacci recursion memo(n - 1) + fibonacci recursion memo(n - 2);
}
int main() {
  struct timespec start, end;
  clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &start);
  for (int i = 0; i < 50; ++i) {
     cout << fibonacci recursion memo(i) << " ";
  }
  clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &end);
  double time taken = (end.tv sec - start.tv sec) + (end.tv nsec - start.tv nsec) / 1e9;
  cout << "\nRecursion with Memoization Time: " << time_taken << " seconds\n";</pre>
  return 0;
```

pavandeekshith@Pavans-MacBook-Air-8 Question-1 % cd "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-1/" && g++ recursion_and_memo.cpp -o recursion_and_memo && "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-1/"recursion_and_memo
0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 987 1597 2584 4181 6765 10946 17711 28657 46368 75025 121393 196418 317811 514229 832040 13
46269 2178309 3524578 5702887 9227465 14930352 24157817 39088169 63245986 102334155 165580141 267914296 433494437 701408733 1134903170 1
336311903 2971215073 4807526976 7778742049
Recursion with Memoization Time: 2.3e-05 seconds

Speed up = 77.8 * 10^5 times faster than baseline

d) Loop and memoization

```
Code:
#include <iostream>
#include <vector>
#include <ctime>
using namespace std;
void fibonacci loop memo(int n) {
  vector<long long> fib(n, 0);
  fib[1] = 1;
  for (int i = 2; i < n; ++i) {
     fib[i] = fib[i - 1] + fib[i - 2];
  for (int i = 0; i < n; ++i) {
     cout << fib[i] << " ";
  }
}
int main() {
  struct timespec start, end;
  clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &start);
  fibonacci loop memo(50);
  clock gettime(CLOCK PROCESS CPUTIME ID, &end);
  double time_taken = (end.tv_sec - start.tv_sec) + (end.tv_nsec - start.tv_nsec) / 1e9;
  cout << "\nLoop with Memoization Time: " << time taken << " seconds\n";
  return 0;
```

pavandeekshith@Pavans-MacBook-Air-8 Question-1 % cd "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-1/" && g++ loop_memo.cpp -o loop_memo && "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-1/"loop_memo 0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 987 1597 2584 4181 6765 10946 17711 28657 46368 75025 121393 196418 317811 514229 832040 13 46269 2178309 3524578 5702887 9227465 14930352 24157817 39088169 63245986 102334155 165580141 267914296 433494437 701408733 1134903170 1 836311903 2971215073 4807526976 7778742049 Loop with Memoization Time: 3.1e-05 seconds

Question-2:

```
a) C++
   Code:
   #include <iostream>
   #include <vector>
   #include <ctime>
   #include <iomanip>
   using namespace std;
   void multiplyIntegerMatrices(const vector<vector<int> >& matrix1, const
   vector<vector<int> >& matrix2, vector<vector<int> >& result, int dimension) {
      for (int i = 0; i < dimension; i++) {
        for (int j = 0; j < dimension; j++) {
           result[i][i] = 0;
           for (int k = 0; k < dimension; k++) {
              result[i][j] += matrix1[i][k] * matrix2[k][j];
           }
        }
      }
   }
   void multiplyFloatingPointMatrices(const vector<vector<double> > & matrix1, const
   vector<vector<double> >& matrix2, vector<vector<double> >& result, int dimension) {
      for (int i = 0; i < dimension; i++) {
        for (int j = 0; j < dimension; j++) {
           result[i][j] = 0.0;
           for (int k = 0; k < dimension; k++) {
              result[i][j] += matrix1[i][k] * matrix2[k][j];
        }
      }
   }
   void displayTime(const struct timespec& startTime, const struct timespec& endTime,
   const string& message) {
      double elapsedTime = (endTime.tv sec - startTime.tv sec) * 1e9;
      elapsedTime = (elapsedTime + (endTime.tv_nsec - startTime.tv_nsec)) * 1e-9;
      cout << message << fixed << elapsedTime << setprecision(9) << " seconds" << endl;</pre>
   }
   int main() {
      int dimensions[] = \{64, 128, 256, 512, 1024\};
```

```
for (int dim : dimensions) {
    struct timespec systemStartTime, systemEndTime, cpuStartTime, cpuEndTime;
    clock_gettime(CLOCK_MONOTONIC, &systemStartTime);
    clock gettime(CLOCK PROCESS CPUTIME ID, &cpuStartTime);
    vector<vector<int> > matrixInt1(dim, vector<int>(dim, 1));
    vector<vector<int> > matrixInt2(dim, vector<int>(dim, 1));
    vector<vector<int> > matrixIntResult(dim, vector<int>(dim, 0));
    struct timespec multiplyStartTime, multiplyEndTime;
    clock gettime(CLOCK MONOTONIC, &multiplyStartTime);
    multiplyIntegerMatrices(matrixInt1, matrixInt2, matrixIntResult, dim);
    clock_gettime(CLOCK_MONOTONIC, &multiplyEndTime);
    clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &cpuEndTime);
    clock gettime(CLOCK MONOTONIC, &systemEndTime);
    double totalSystemTime = (systemEndTime.tv_sec - systemStartTime.tv_sec) +
(systemEndTime.tv nsec - systemStartTime.tv nsec) * 1e-9;
    double totalCPUTime = (cpuEndTime.tv sec - cpuStartTime.tv sec) +
(cpuEndTime.tv_nsec - cpuStartTime.tv_nsec) * 1e-9;
    double multiplyTime = (multiplyEndTime.tv sec - multiplyStartTime.tv sec) +
(multiplyEndTime.tv_nsec - multiplyStartTime.tv_nsec) * 1e-9;
    double meatProportion = (multiplyTime / totalCPUTime) * 100;
    cout << "Dimension=" << dim << ", Integer Matrix Multiplication: " << endl;</pre>
    displayTime(systemStartTime, systemEndTime, "System Time: ");
    displayTime(cpuStartTime, cpuEndTime, "CPU Time: ");
    displayTime(multiplyStartTime, multiplyEndTime, "Integer Multiplication Time: ");
    cout << "Integer MEAT Proportion: " << fixed << meatProportion << setprecision(2)
<< "%" << endl:
    clock gettime(CLOCK MONOTONIC, &systemStartTime);
    clock_gettime(CLOCK_PROCESS_CPUTIME_ID, &cpuStartTime);
    vector<vector<double> > matrixFloat1(dim, vector<double>(dim, 1.0));
    vector<vector<double> > matrixFloat2(dim, vector<double>(dim, 1.0));
    vector<vector<double> > matrixFloatResult(dim, vector<double>(dim, 0.0));
```

```
clock_gettime(CLOCK_MONOTONIC, &multiplyStartTime);
     multiplyFloatingPointMatrices(matrixFloat1, matrixFloat2, matrixFloatResult, dim);
     clock_gettime(CLOCK_MONOTONIC, &multiplyEndTime);
     clock gettime(CLOCK PROCESS CPUTIME ID, &cpuEndTime);
     clock_gettime(CLOCK_MONOTONIC, &systemEndTime);
    totalSystemTime = (systemEndTime.tv sec - systemStartTime.tv sec) +
(systemEndTime.tv nsec - systemStartTime.tv nsec) * 1e-9;
     totalCPUTime = (cpuEndTime.tv_sec - cpuStartTime.tv_sec) +
(cpuEndTime.tv nsec - cpuStartTime.tv nsec) * 1e-9;
     multiplyTime = (multiplyEndTime.tv_sec - multiplyStartTime.tv_sec) +
(multiplyEndTime.tv nsec - multiplyStartTime.tv nsec) * 1e-9;
     meatProportion = (multiplyTime / totalCPUTime) * 100;
     cout << "Dimension=" << dim << ", Floating-Point Matrix Multiplication: " << endl;</pre>
     displayTime(systemStartTime, systemEndTime, "System Time: ");
     displayTime(cpuStartTime, cpuEndTime, "CPU Time: ");
     displayTime(multiplyStartTime, multiplyEndTime, "Floating-Point Multiplication
Time: ");
    cout << "Floating-Point MEAT Proportion: " << fixed << meatProportion <<
setprecision(2) << "%" << endl;
  }
  return 0;
}
```

```
tion-2/" && g++ matrix_multiplication.cpp -o matrix_multiplication && "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture
/Assignment-1/Question-2/"matrix_multiplication
matrix_multiplication.cpp:137:18: warning: range-based for loop is a C++11 extension [-Wc++11-extensions]
for (int dim _ dimensions) {
matrix_multiplication.cpp:137:18: warning: range-based for (int dim : dimensions) {

l warning generated.

limension=64, Integer Matrix Multiplication:
system Time: 0.002802 seconds

Loteger Multiplication Time: 0.002669000 seconds

Integer MEAT Proportion: 97:566837294%

limension=64, Floating-Point Matrix Multiplication:
system Time: 0.00 seconds

Loting-Point Multiplication Time: 0.002530000 seconds

Floating-Point Multiplication Time: 0.002530000 seconds

Floating-Point Meat Proportion: 95.041322314%

limension=128, Integer Matrix Multiplication:
system Time: 0.02 seconds

Loteger Multiplication Time: 0.020820000 seconds

Integer MEAT Proportion: 99.621991483%

limension=128, Floating-Point Matrix Multiplication:
system Time: 0.02 seconds

Loteger Meat Proportion: 99.020820000 seconds

Integer Meat Proportion: 98.720152818%

Dimension=128, Floating-Point Matrix Multiplication:
system Time: 0.12 seconds

PU Time: 0.020940000 seconds

Floating-Point Multiplication Time: 0.020672000 seconds

Floating-Point Multiplication Time: 0.175682000 seconds

Integer Multiplication Time: 0.175682000 seconds

Integer Meat Proportion: 99.925489014%

Dimension=256, Floating-Point Matrix Multiplication:
system Time: 0.17 seconds

PU Time: 0.165504000 seconds

Floating-Point Multiplication Time: 0.165037000 seconds

Floating-Point Multiplication Time: 0.165037000 seconds

Floating-Point Multiplication Time: 0.165037000 seconds

Floating-Point Multiplication Time: 1.37314000 seconds

Floating-Point Multiplication Time: 1.37314000 seconds

Floating-Point Multiplication Time: 1.37314000 seconds

Floating-Point Meat Proportion: 100.147032654%

Dimension=512, Floating-Point Matrix Multiplication:
system Time: 1.32 seconds

FU Time: 1.31657000 seconds

Floating-Point Multiplication Time: 1.31815000 seconds

Floating-Point Meat Proportion: 100.1470326554%

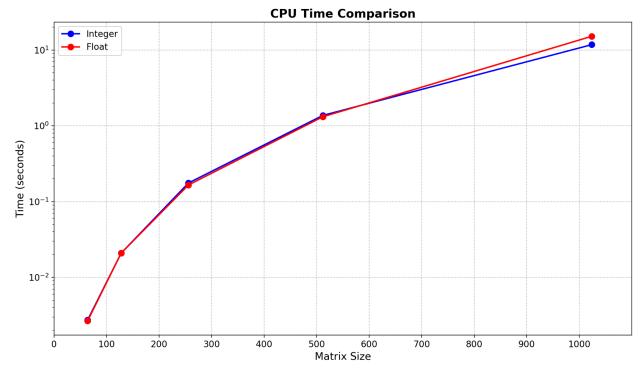
Dimension=1024, Floating-Point Matrix Multiplication:
system Time: 1.193 seconds

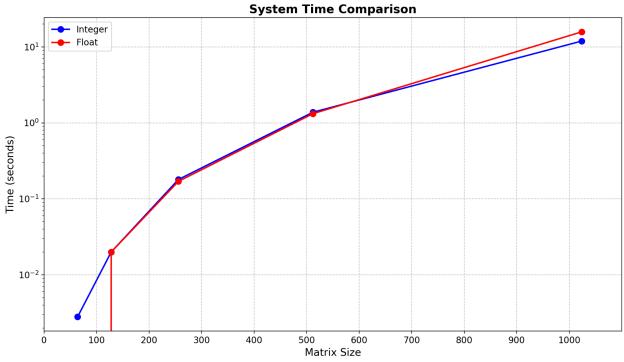
FU Time: 1.3165020000 seconds

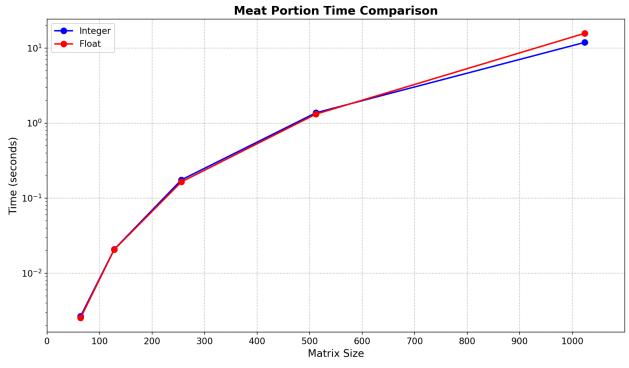
Floating-Point Meat Proportion: 100.1470326554%

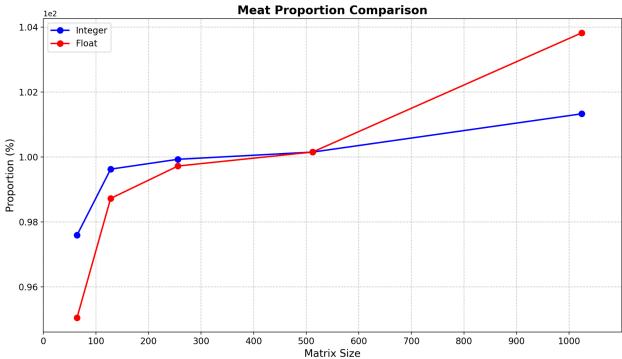
Dimension=1024, Fl
```

| Matrix Size | Operation Type | CPU Time (s) | System Time (s) | Meat Portion Time (s) | Meat Proportion (%) |
|-------------|----------------|--------------|-----------------|-----------------------|---------------------|
| 64x64 | Integer | 0.002802 | 0.002735 | 0.002669 | 97.58683729 |
| 64x64 | Float | 0 | 0.002662 | 0.00253 | 95.04132231 |
| 128x128 | Integer | 0.02 | 0.020899 | 0.02082 | 99.62199148 |
| 128x128 | Float | 0.02 | 0.02094 | 0.020672 | 98.72015282 |
| 256x256 | Integer | 0.18 | 0.175813 | 0.175682 | 99.92548901 |
| 256x256 | Float | 0.17 | 0.165504 | 0.165037 | 99.71783159 |
| 512x512 | Integer | 1.38 | 1.371124 | 1.37314 | 100.1470327 |
| 512x512 | Float | 1.32 | 1.316157 | 1.318115 | 100.1487664 |
| 1024x1024 | Integer | 11.93 | 11.757134 | 11.913057 | 101.3261991 |
| 1024x1024 | Float | 15.77 | 15.16502 | 15.744324 | 103.8200016 |
| | | | | | |









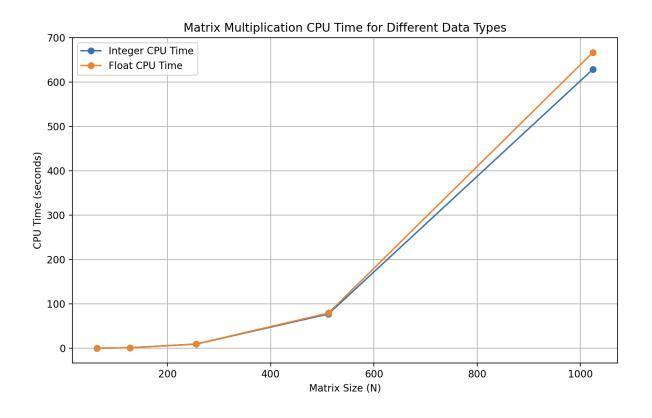
b) Python

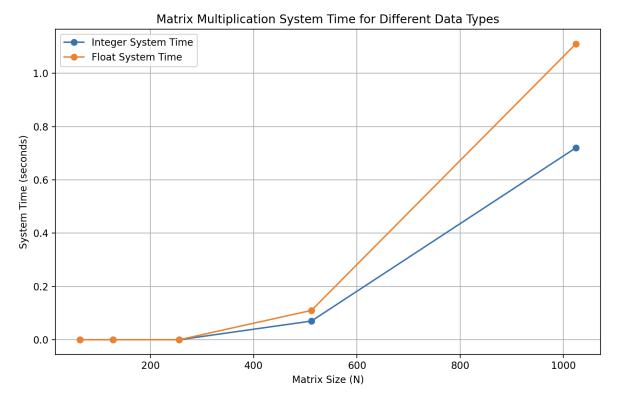
```
Code:
import numpy as np
import time
import os
import matplotlib.pyplot as plt
N_values = [64, 128, 256, 512, 1024]
int cpu times = []
int_system_times = []
float_cpu_times = []
float system times = []
int meat times = []
float_meat_times = []
int meat percentages = []
float_meat_percentages = []
def matrix multiplication(N, dtype):
  np.random.seed(0)
  matrix = np.random.randint(0, 11, size=(N, N)).astype(dtype)
  result = np.zeros((N, N), dtype=dtype)
  start process time total = time.process time()
  start_os_times_total = os.times()
  start_meat_time = time.process_time()
  for i in range(N):
    for j in range(N):
       for k in range(N):
          result[i][j] += matrix[i][k] * matrix[k][j]
  end_meat_time = time.process_time()
  end process time total = time.process time()
  end_os_times_total = os.times()
  cpu time used total = end process time total - start process time total
  user_time_used_total = end_os_times_total.user - start_os_times_total.user
  system_time_used_total = end_os_times_total.system - start_os_times_total.system
```

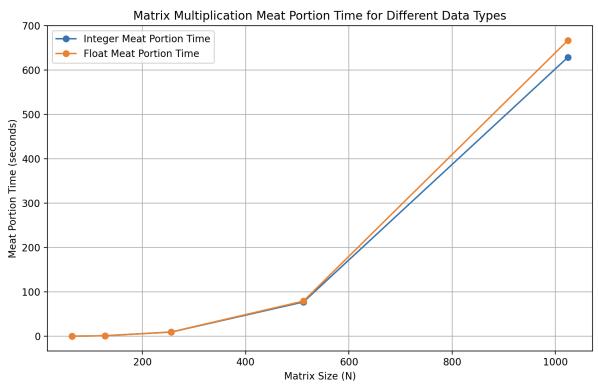
```
meat time used = end meat time - start meat time
  meat percentage = (meat time used / cpu time used total * 100) if
cpu time used total > 0 else 0
  return cpu time used total, system time used total, meat time used,
meat percentage
for N in N values:
  print(f"Performing matrix multiplication for size {N}x{N}")
  int cpu time, int system time, int meat time, int meat percentage =
matrix multiplication(N, dtype=int)
  int_cpu_times.append(int_cpu_time)
  int system times.append(int system time)
  int_meat_times.append(int_meat_time)
  int meat percentages.append(int meat percentage)
  print(f"Integer matrix multiplication CPU time for {N}x{N}: {int_cpu_time:.6f} seconds")
  print(f"Integer matrix multiplication System time for {N}x{N}: {int_system_time:.6f}
seconds")
  print(f"Integer matrix multiplication Meat portion time for {N}x{N}: {int_meat_time:.6f}
seconds")
  print(f"Integer matrix multiplication Meat proportion for {N}x{N}:
{int meat percentage:.2f}%")
  float cpu time, float system time, float meat time, float meat percentage =
matrix_multiplication(N, dtype=float)
  float cpu times.append(float cpu time)
  float system times.append(float system time)
  float_meat_times.append(float_meat_time)
  float meat percentages.append(float meat percentage)
  print(f"Float matrix multiplication CPU time for {N}x{N}: {float cpu time:.6f} seconds")
  print(f"Float matrix multiplication System time for {N}x{N}: {float_system_time:.6f}
seconds")
  print(f"Float matrix multiplication Meat portion time for {N}x{N}: {float meat time:.6f}
seconds")
  print(f"Float matrix multiplication Meat proportion for {N}x{N}:
(float meat percentage:.2f)%")
plt.figure(figsize=(10, 6))
plt.plot(N values, int cpu times, label="Integer CPU Time", marker='o')
plt.plot(N values, float cpu times, label="Float CPU Time", marker='o')
plt.xlabel('Matrix Size (N)')
```

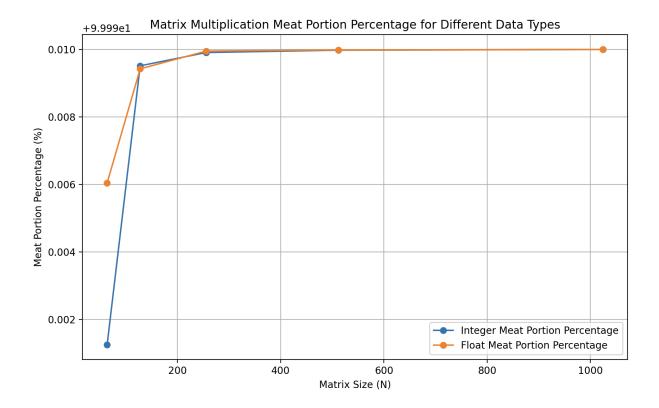
```
plt.ylabel('CPU Time (seconds)')
plt.title('Matrix Multiplication CPU Time for Different Data Types')
plt.legend()
plt.grid(True)
plt.show()
plt.figure(figsize=(10, 6))
plt.plot(N values, int system times, label="Integer System Time", marker='o')
plt.plot(N values, float system times, label="Float System Time", marker='o')
plt.xlabel('Matrix Size (N)')
plt.ylabel('System Time (seconds)')
plt.title('Matrix Multiplication System Time for Different Data Types')
plt.legend()
plt.grid(True)
plt.show()
plt.figure(figsize=(10, 6))
plt.plot(N values, int meat times, label="Integer Meat Portion Time", marker='o')
plt.plot(N_values, float_meat_times, label="Float Meat Portion Time", marker='o')
plt.xlabel('Matrix Size (N)')
plt.ylabel('Meat Portion Time (seconds)')
plt.title('Matrix Multiplication Meat Portion Time for Different Data Types')
plt.legend()
plt.grid(True)
plt.show()
plt.figure(figsize=(10, 6))
plt.plot(N values, int meat percentages, label="Integer Meat Portion Percentage",
marker='o')
plt.plot(N_values, float_meat_percentages, label="Float Meat Portion Percentage",
marker='o')
plt.xlabel('Matrix Size (N)')
plt.ylabel('Meat Portion Percentage (%)')
plt.title('Matrix Multiplication Meat Portion Percentage for Different Data Types')
plt.legend()
plt.grid(True)
plt.show()
```

```
Savandeekshith@Pavans-MacBook-Air-8 Computer Architecture % /usr/local/bin/python3 "/Users/pavandeekshith/B-Tech/Btech 3rd Year/Computer Architecture/Assignment-1/Question-Z/matrix_multiplication.py" Performing matrix multiplication for izee 646446 4. 0.000000 seconds for the property matrix multiplication CPU time for 646461 0.000000 seconds for the property multiplication Meat portion time for 646461 0.18552 seconds for partial multiplication Meat portion time for 646461 0.18552 seconds for partial multiplication Meat proportion for 646461 0.18503 seconds float matrix multiplication System time for 646461 0.18503 seconds float matrix multiplication Meat portion time for 64661 0.18503 seconds float matrix multiplication float time for 64661 0.18503 seconds float matrix multiplication float time float flo
```









| Matrix Size | Operation Type | CPU Time (s) | System Time (s) | Meat Portion Time (s) | Meat Proportion (%) |
|-------------|----------------|--------------|-----------------|-----------------------|---------------------|
| 64x64 | Integer | 0.148525 | 0 | 0.148512 | 99.99 |
| 64x64 | Float | 0.151631 | 0 | 0.151625 | 100 |
| 128x128 | Integer | 1.228439 | 0 | 1.228433 | 100 |
| 128x128 | Float | 1.208985 | 0 | 1.208978 | 100 |
| 256x256 | Integer | 9.48732 | 0 | 9.487311 | 100 |
| 256x256 | Float | 9.732542 | 0 | 9.732537 | 100 |
| 512x512 | Integer | 77.290959 | 0.07 | 77.290939 | 100 |
| 512x512 | Float | 79.293617 | 0.11 | 79.2936 | 100 |
| 1024x1024 | Integer | 628.674765 | 0.72 | 628.674743 | 100 |
| 1024x1024 | Float | 666.760044 | 1.11 | 666.760025 | 100 |
| | | | | | |