

1. given context grammar is

$$S \rightarrow aB/bA$$

$$A \rightarrow a/as/bAA$$

$$B \rightarrow b/bs/aBB$$

we need to generate string aaabbabbbba

a) left most derivation;

consider; $S \rightarrow aB$

$$\rightarrow aaBB$$

$$\rightarrow aaaBBB$$

$$\rightarrow aaabBB$$

$$\rightarrow aaabbbB$$

$$\rightarrow aaabbbaBB$$

$$\rightarrow aaabbbaBBB$$

$$\rightarrow aaabbbaabbB$$

$$\rightarrow aaabbbaabbs$$

$$\rightarrow aaabbbaabbbA$$

$$\rightarrow aaabbbaabbbba$$

b) right most derivation:

consider; $S \rightarrow aB$

$$S \rightarrow aaBB$$

$$S \rightarrow aaBaBB$$

$$S \rightarrow aaBaBbs$$

$$S \rightarrow aaBaBbbA$$

$$S \rightarrow aaBaBbbba$$

$$S \rightarrow aaBaabbbba$$

$$S \rightarrow aaabBBabbbba$$

$$S \rightarrow aaabBbabbbba$$

$$S \rightarrow aaabbbaabbbba$$

2. The context free grammar for

$$L = \{a^n b^m c d^m e^n \mid n, m > 0\}$$

$$L = \{abcde, abcdeee, \dots\}$$

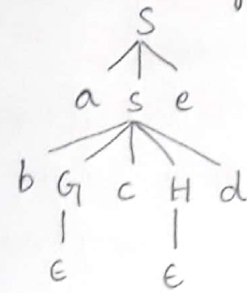
The grammar is

$$S \rightarrow ase / b G c H d$$

$$G \rightarrow b / \epsilon / G$$

$$H \rightarrow d / \epsilon / H$$

For string abcde



3. 4) $L = \{a^m b^{2m}\}$

$$L = \{abb, aabbbb, aaabbbbb, \dots\}$$

Consider string aabbbbe

$$\delta(q_0, a, z_0) = q_0, az_0$$

$$\delta(q_0, a, a) \rightarrow q_0, aa$$

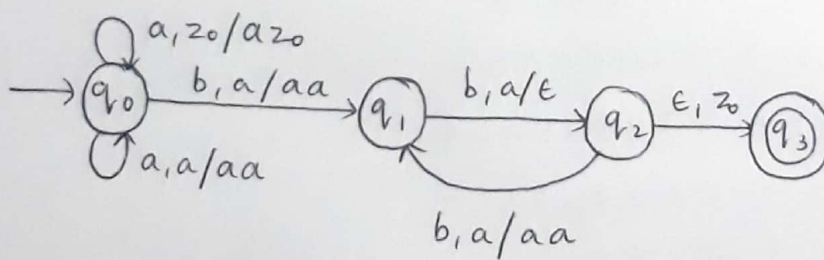
$$\delta(q_0, b, a) \rightarrow q_1, aa$$

$$\delta(q_1, b, a) \rightarrow q_2, \epsilon$$

$$\delta(q_2, b, a) \rightarrow q_1, aa$$

$$\delta(q_1, b, a) \rightarrow q_2, \epsilon$$

$$\delta(q_2, \epsilon, z_0) \rightarrow q_3, \text{accept}$$



3. 2) $L = \{ ww^R \mid w = \{a, b\}^* \}$

$L = \{ aa, bb, abba, baab, \dots \}$

Consider;

$\delta(q_0, a, z_0) \rightarrow q_1, az_0$

$\delta(q_0, b, z_0) \rightarrow q_1, bz_0$

$\delta(q_1, a, a) \rightarrow q_2, aa$

$\delta(q_1, b, b) \rightarrow q_2, bb$

$\delta(q_1, a, b) \rightarrow q_2, ab$

$\delta(q_1, b, a) \rightarrow q_2, ba$

$\delta(q_2, a, a) \rightarrow q_2, \epsilon$

$\delta(q_2, b, b) \rightarrow q_2, \epsilon$

$\delta(q_2, \epsilon, z_0) \rightarrow q_3, \text{accept}$

