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# Assignment 14

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Download the latex-tikz codes from

https://github.com/pavanmanesh/EE5609/tree/master/Assignment14

### 1 Problem

Let T be the linear operator on a n- dimensional vector space V and suppose that T has an n distinct characteristic values. Prove that T is diagonalizable.

### 2 RESULTS USED

Diagonalizable	A linear operator <b>T</b> on a finite-dimensional vector space <b>V</b> is diagonalizable if and only if there exists an basis of <b>V</b> , consisting of eigen vectors of <b>T</b>
Eigen vectors	Eigen vectors that are associated to distinct eigen values are linearly independent.

### 3 Solution

Given	$\mathbf{T}$ has an n distinct characteristic values and $dim(\mathbf{V}) = n$
T is diagonalizable	Let $\lambda_1, \lambda_2, \dots, \lambda_n$ be distinct eigen values of <b>T</b> and let $\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_n$ be the eigen vectors of <b>T</b> From above results we can state that $\{\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_n\}$ is linearly independent. And also given that $\dim(\mathbf{V}) = \mathbf{n}$ .So, this set forms a basis of <b>V</b> . $\{\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_n\}$ is a basis for <b>V</b> consisting of eigen vectors of <b>T</b> . So, <b>T</b> is diagonalizable.