

Options



Options - Definitions

- ✚ A call is an option to buy an asset at a given price
- ✚ A put is an option to sell an asset at a given price
- ✚ A European option can be exercised only at the end of its life
- ✚ An American option can be exercised at any time



Outline

- ✚ The mechanics of options and their trading.
Types of options by:
 - ✚ Exercise optionality
 - ✚ Underlying asset (equity, index, futures)
- ✚ Option properties:
 - ✚ Risks
 - ✚ Put-call parity
 - ✚ Dividends

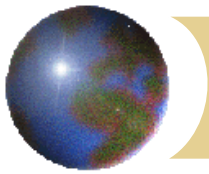


Option Positions

There are two sides to each option: the option writer and the option holder (buyer)

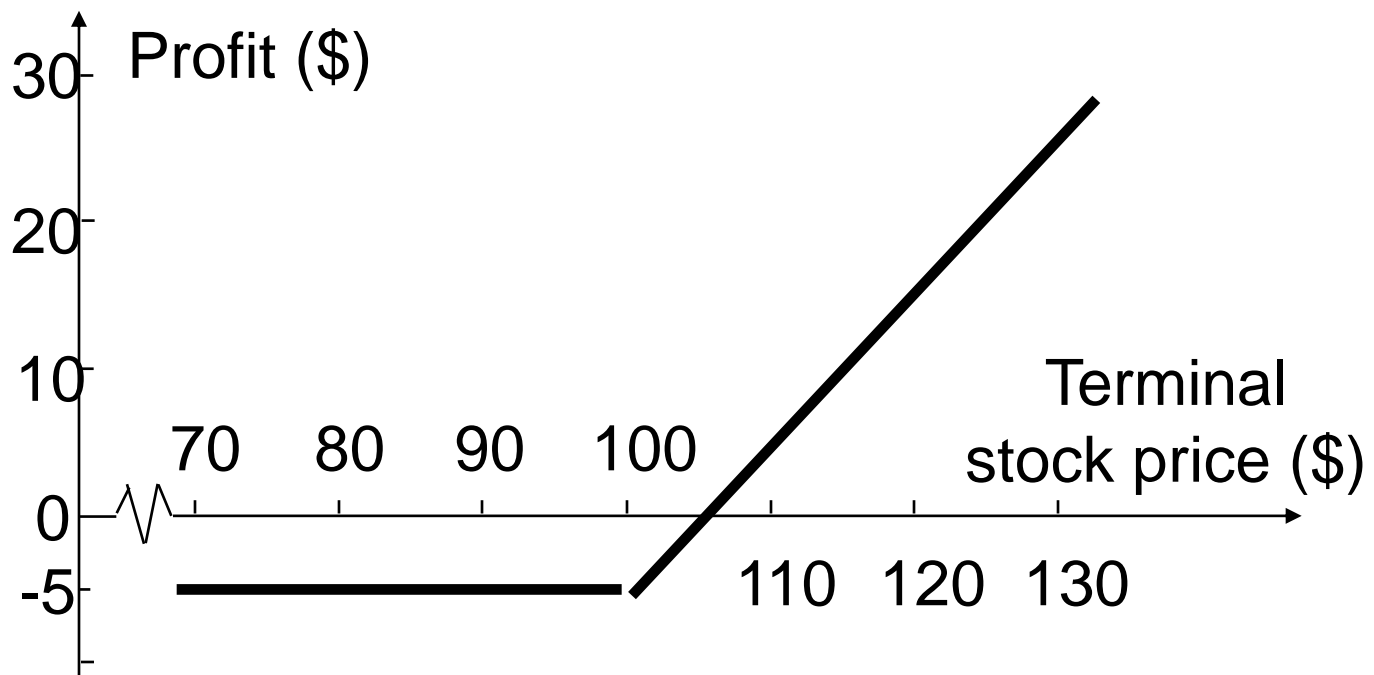


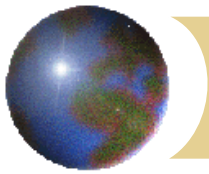
- ⊕ Long call – bought a call option
- ⊕ Long put – bought a put option
- ⊕ Short call – wrote a call option
- ⊕ Short put – wrote a put option



Long Call (Figure 10.1, Page 210)

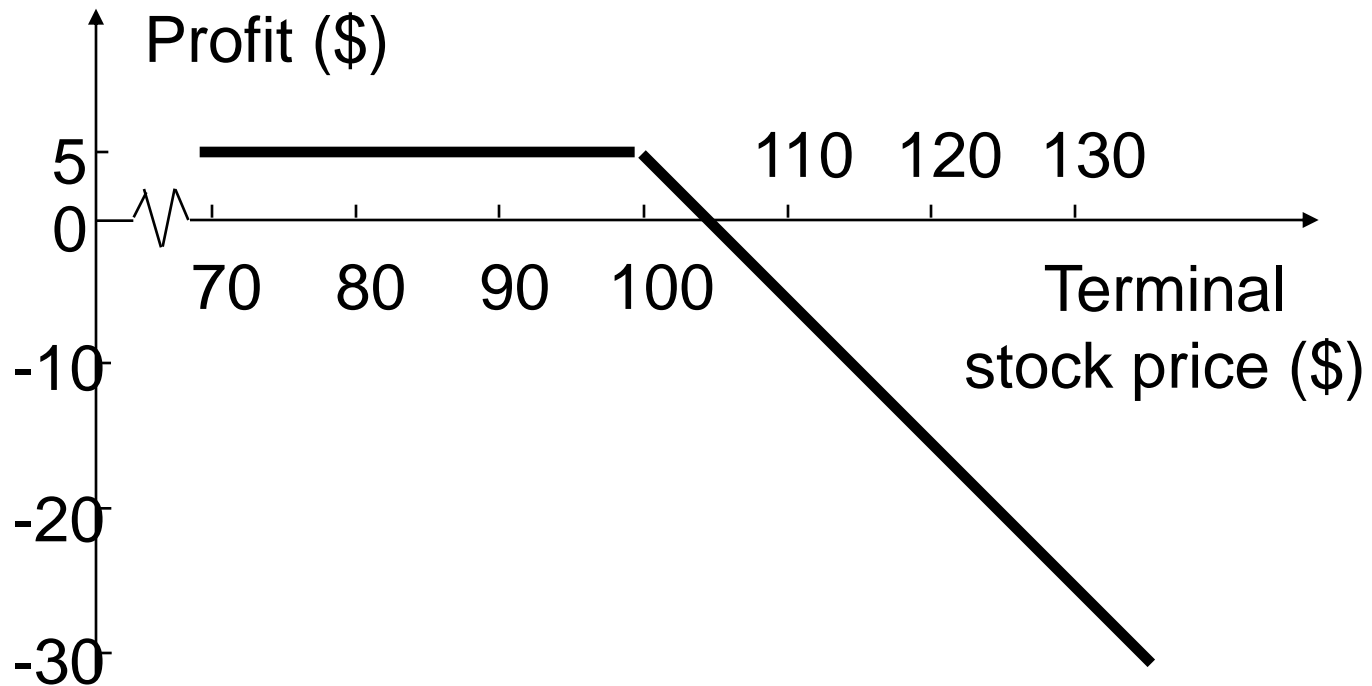
Profit from buying one European call option: option price = \$5, strike price = \$100, option life = 2 months

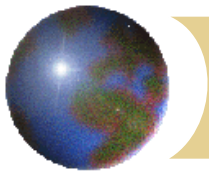




Short Call (Figure 10.3, page 212)

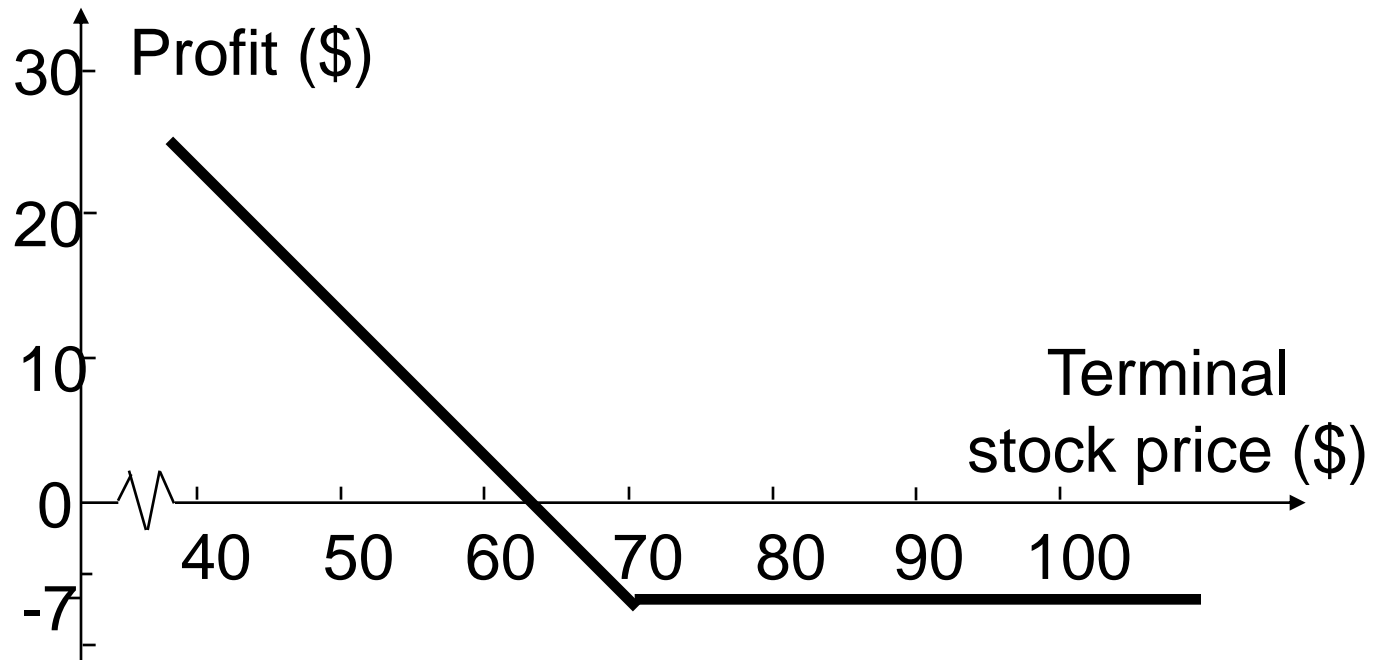
Profit from writing one European call option: option price = \$5, strike price = \$100

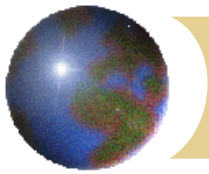




Long Put (Figure 10.2, page 211)

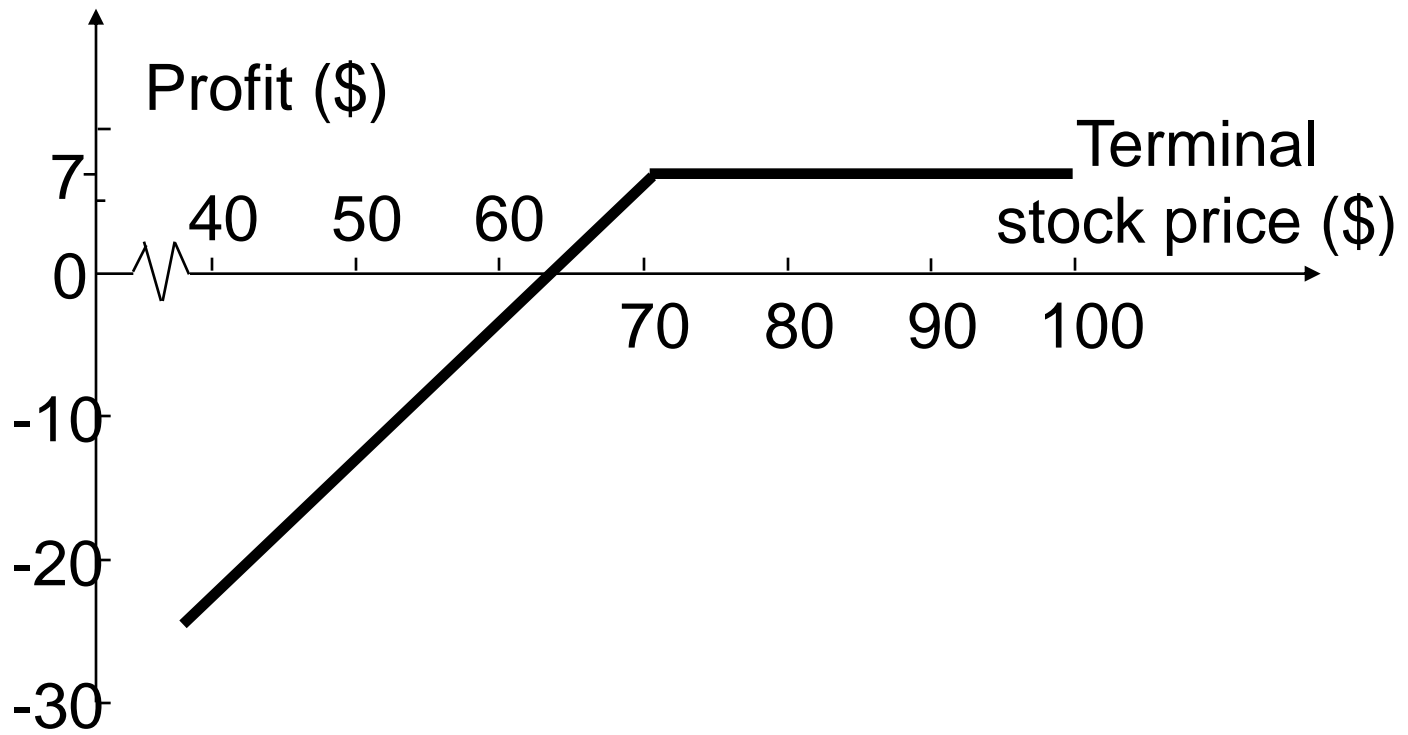
Profit from buying a European put option: option price = \$7, strike price = \$70

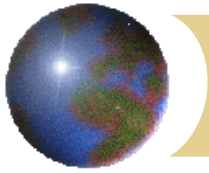




Short Put (Figure 10.4, page 212)

Profit from writing a European put option: option price = \$7, strike price = \$70



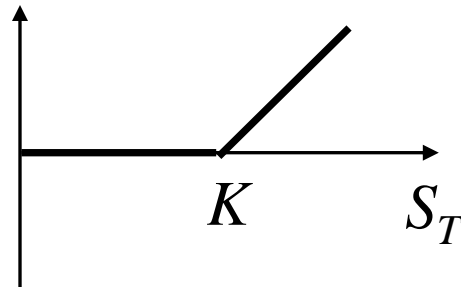


Payoffs from Options

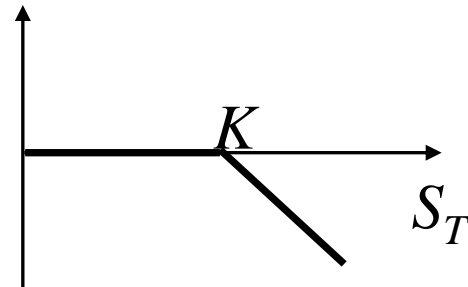
What is the Option Position in Each Case?

K = Strike price, S_T = Price of asset at maturity

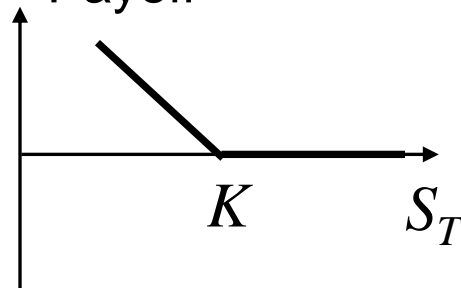
Payoff



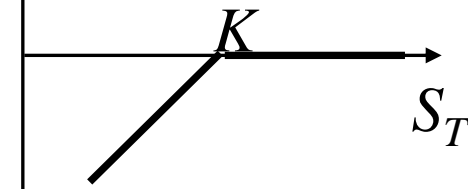
Payoff



Payoff



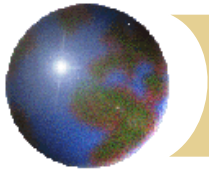
Payoff





Assets Underlying Options

- ✚ Stocks
- ✚ Exchange Traded Funds (ETFs), e.g. SPY
- ✚ Foreign Currency
- ✚ Stock Indices
- ✚ Futures



Option parameters

- ✚ Expiration date
- ✚ Strike price
- ✚ European or American
- ✚ Call or Put (option class)



Terminology

Moneyiness :

- ❏ At-the-money option
- ❏ In-the-money option
- ❏ Out-of-the-money option

Q: What are the strikes of ITM call options?



More Terminology

- ✚ Option class (call or put)
- ✚ Option series
- ✚ Intrinsic value
- ✚ Time value
- ✚ Naked vs covered options

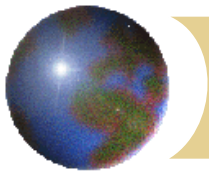


How to get stock price and options data

- ✚ Yahoo finance has freely available data but no historical option prices

<https://finance.yahoo.com>

- ✚ Options on futures are listed on the CME Group website
- ✚ Bloomberg has historical option price data



Example: options on SPY

NYSEArca - Nasdaq Real Time Price • USD

SPDR S&P 500 ETF Trust (SPY) [☆ Follow](#)

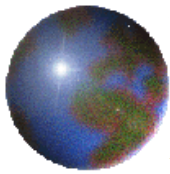
577.14 **+3.97 (+0.69%)** **576.77** **-0.37 (-0.06%)**

At close: 4:00 PM EDT

After hours: 4:56 PM EDT



Previous Close	573.17	Day's Range	572.55 - 577.71	Net Assets	591.49B	YTD Daily Total Return	21.73%
Open	573.16	52 Week Range	409.21 - 577.71	NAV	573.09	Beta (5Y Monthly)	1.00
Bid	576.71 x 1000	Volume	34,648,991	PE Ratio (TTM)	29.07	Expense Ratio (net)	0.09%
Ask	576.51 x 1200	Avg. Volume	52,177,696	Yield	1.22%		



NYSEArca - Nasdaq Real Time Price • USD

SPDR S&P 500 ETF Trust (SPY) ☆ Follow

577.14 **+3.97 (+0.69%)** **576.79** **-0.35 (-0.06%)**

At close: 4:00 PM EDT

After hours: 4:59 PM EDT



Oct 11, 2024 ▾ All Strike Prices ▾ Straddle ▾

Calls

Last Price	Change	% Change	Volume	Open Interest
4.64	+1.53	+49.20%	9,900	4,941
3.96	+1.32	+50.00%	15,535	7,439
3.29	+1.12	+51.61%	17,775	3,621
2.74	+1.01	+58.38%	17,843	6,505
2.20	+0.86	+64.18%	12,265	4,890
1.73	+0.68	+64.76%	10,984	3,502
1.31	+0.52	+65.82%	30,072	9,228
0.98	+0.42	+75.00%	8,617	5,067

Puts

Last Price	Change	% Change	Volume	Open Interest
1.72	-1.99	-53.64%	19,811	1,828
2.03	-2.12	-51.08%	33,236	2,282
2.41	-2.34	-49.26%	17,352	760
2.84	-2.58	-47.60%	13,775	1,027
3.29	-2.89	-46.76%	4,212	323
3.88	-2.96	-43.27%	2,472	493
4.47	-3.02	-40.32%	1,884	913
5.09	-4.23	-45.39%	506	245



Dividends & Stock Splits

(Page 217-218)

Suppose you own N options with strike price K :

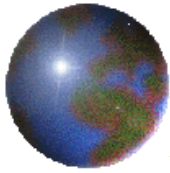
- ✚ No adjustments are made to the option terms for cash dividends
- ✚ When there is an n -for- m stock split,
 - the strike price is reduced to mK/n
 - the no. of options is increased to nN/m
- ✚ Stock dividends are handled similarly to stock splits



Dividends & Stock Splits

(continued)

- ✚ Consider a call option to buy 100 shares for \$20/share
- ✚ How should terms be adjusted:
 - ✚ for a 2-for-1 stock split?
 - ✚ for a 5% stock dividend?



Option Properties

(Chapter 11)



Notation

c : European call option price

p : European put option price

S_0 : Stock price today

K : Strike price

T : Life of option

σ : Volatility of stock price

C : American call option price

P : American put option price

S_T : Stock price at option maturity

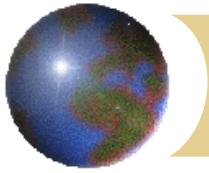
D : PV of dividends paid during life of option

r : Risk-free rate for maturity T with cont. comp.



Effect of Variables on Option Pricing (Table 11.1, page 232)

Variable	European		American	
	c	p	C	P
S_0	+	−	+	−
K	−	+	−	+
T	?	?	+	+
σ	+	+	+	+
r	+	−	+	−
D	−	+	−	+

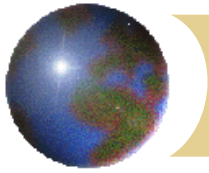


American vs European Options

An American option is worth at least as much as the corresponding European option

$$C \geq c$$

$$P \geq p$$



Calls: An Arbitrage Opportunity?

✚ Suppose that

$$c = 3$$

$$S_0 = 20$$

$$T = 1$$

$$r = 10\%$$

$$K = 18$$

$$D = 0$$

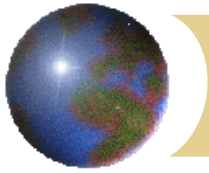
✚ Is there an arbitrage opportunity?



Lower Bound for European Call Option Prices; No Dividends

(Equation 11.4, page 237)

$$c \geq \max(S_0 - Ke^{-rT}, 0)$$



Puts: An Arbitrage Opportunity?

✚ Suppose that

$$p = 1$$

$$S_0 = 37$$

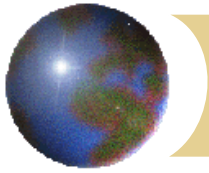
$$T = 0.5$$

$$r = 5\%$$

$$K = 40$$

$$D = 0$$

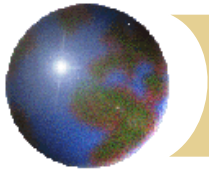
✚ Is there an arbitrage opportunity?



Lower Bound for European Put Prices; No Dividends

(Equation 11.5, page 238)

$$p \geq \max(Ke^{-rT} - S_0, 0)$$



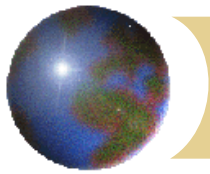
Put-Call Parity: No Dividends

- ✚ Consider the following 2 portfolios:
 - ✚ Portfolio A: European call on a stock + zero-coupon bond that pays K at time T
 - ✚ Portfolio C: European put on the stock + the stock



Values of Portfolios

		$S_T > K$	$S_T < K$
Portfolio A	Call option	$S_T - K$	0
	Zero-coupon bond	K	K
	Total	S_T	K
Portfolio C	Put Option	0	$K - S_T$
	Share	S_T	S_T
	Total	S_T	K



The Put-Call Parity Result (Equation 11.6, page 239)

- Both are worth $\max(S_T, K)$ at the maturity of the options
- They must therefore be worth the same today. This means that

$$c + Ke^{-rT} = p + S_0$$



Arbitrage Opportunities

- Suppose that

$$c = 3$$

$$T = 0.25$$

$$K = 30$$

$$S_0 = 31$$

$$r = 10\%$$

$$D = 0$$

- What are the arbitrage possibilities when

$$p = 2.25 ?$$

$$p = 1 ?$$



Check put-call parity

$$c + e^{-rT}K \text{ vs } p + S_0$$

Case 1:

$$32.26 \text{ vs } 33.25$$

Put is overpriced: buy calls, short puts

Case 2:

$$32.25 \text{ vs } 32.00$$

Put is underpriced: buy puts, short calls



American Options: Early Exercise

- ✚ Usually there is some chance that an American option will be exercised early
- ✚ An exception is an American call on a non-dividend paying stock
- ✚ This should never be exercised early



Reasons For Not Exercising an American Call Early (No Dividends)

- ✚ No income is sacrificed
- ✚ You delay paying the strike price
- ✚ Holding the call provides insurance against stock price falling below strike price

However American put options can be exercised early, if the stock price drops below a critical value (exercise boundary)



Extensions of Put-Call Parity

- ✚ American options; $D = 0$

$$S_0 - K < C - P < S_0 - Ke^{-rT}$$

Equation 11.7 p. 240

- ✚ European options; $D > 0$

$$c + D + Ke^{-rT} = p + S_0$$

Equation 11.10 p. 247

- ✚ American options; $D > 0$

$$S_0 - D - K < C - P < S_0 - Ke^{-rT}$$

Equation 11.11 p. 247



Exotic options

- ⊕ Non-standard American options
- ⊕ Barrier options
- ⊕ Asian options
- ⊕ Lookback options



Non-Standard American Options

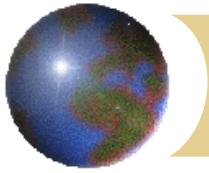
(page 598)

- ✚ Exercisable only on specific dates (Bermudans)
- ✚ Early exercise allowed during only part of life (initial “lock out” period)
- ✚ Strike price changes over the life (warrants, convertibles)



Barrier Options *(page 602-604)*

- ✚ Option comes into existence only if stock price hits barrier before option maturity
 - ✚ 'In' options
- ✚ Option dies if stock price hits barrier before option maturity
 - ✚ 'Out' options



Barrier Options (continued)

- ⊕ Stock price must hit barrier from below
 - ⊕ 'Up' options
- ⊕ Stock price must hit barrier from above
 - ⊕ 'Down' options
- ⊕ Option may be a put or a call
- ⊕ Eight possible combinations



Binary Options *(page 604-605)*

- ✚ Cash-or-nothing: pays Q if $S_T > K$, otherwise pays nothing.
- ✚ Asset-or-nothing: pays S_T if $S_T > K$, otherwise pays nothing.



Lookback Options (page 605-607)

- ✚ Floating lookback call pays $S_T - S_{\min}$ at time T (Allows buyer to buy stock at lowest observed price in some interval of time)
- ✚ Floating lookback put pays $S_{\max} - S_T$ at time T (Allows buyer to sell stock at highest observed price in some interval of time)
- ✚ Fixed lookback call pays $\max(S_{\max} - K, 0)$
- ✚ Fixed lookback put pays $\max(K - S_{\min}, 0)$
- ✚ Analytic valuation for all types



Asian Options (page 608-609)

- ✚ Payoff related to average stock price

- ✚ Average Price options pay:

 - ✚ Call: $\max(S_{\text{ave}} - K, 0)$

 - ✚ Put: $\max(K - S_{\text{ave}}, 0)$

- ✚ Average Strike options pay:

 - ✚ Call: $\max(S_T - S_{\text{ave}}, 0)$

 - ✚ Put: $\max(S_{\text{ave}} - S_T, 0)$



Asian Options

- ✚ No exact analytic valuation
- ✚ Can be approximately valued by assuming that the average stock price is lognormally distributed