

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Other Issues

# Processamento e Recuperação de Informação Classification

Departamento de Engenharia Informática Instituto Superior Técnico

1<sup>o</sup> Semestre 2018/2019



#### Outline

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

- Introduction
- 2 Supervised Learning
- Text Classifiers
  - Nearest Neighbor Classifiers
  - Generative Bayesian Classifiers
  - Linear Discriminative Classifiers
- Other Issues



# Bibliography

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

- Bing Liu, Web Data Mining Exploring Hyperlinks, Contents, and Usage Data. Chapter 3.
- Ricardo Baeza-Yates and Berthier Ribeiro-Neto, Modern Information Retrieval. Chapter 8.
- Christopher D. Manning, Prabhakar Raghavan and Hinrich Schütze, Introduction to Information Retrieval. Chapters 13, 14 and 15.
- Jure Leskovec, Anand Rajaraman, and Jeff Ullman, Mining of Massive Datasets, Chapter 12



#### Outline

Processamento e Recuperação de Informação

#### Introduction

Supervised Learning

Text Classifiers

- Introduction
- 2 Supervised Learning
- 3 Text Classifiers
- 4 Other Issues



#### Organizing Knowledge

Processamento e Recuperação de Informação

#### Introductio

Supervised Learning

Text Classifiers

- Organize into systematic knowledge structures
- Ontologies
  - Dewey decimal system
  - ACM Computing Classification System
  - Patent subject classification
- Web catalogs
  - Yahoo Directory (RIP 2002–2014)
  - Dmoz Directory



### Organizing Knowledge

Processamento e Recuperação de Informação

#### Introduction

Supervised Learning

Text Classifiers

Other Issues

- Organize into systematic knowledge structures
- Ontologies
  - Dewey decimal system
  - ACM Computing Classification System
  - Patent subject classification
- Web catalogs
  - Yahoo Directory (RIP 2002–2014)
  - Dmoz Directory

Problem: Manual maintenance



#### Outline

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

- Introduction
- 2 Supervised Learning
- 3 Text Classifiers
- 4 Other Issues



# Supervised Learning

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Other Issues

Given a set of training data as input, use learning algorithm A to discover the function  $\hat{h}$  that minimizes the loss (e.g. the error)

Input: 
$$\{(x_i, y_i)\}_{i=1}^N$$
,  $x_i \in \mathcal{R}^M$ ,  $y_i \in \mathcal{R}$ 

Hypothesis space:  $h^* \in H$ 

Loss function: L(h(x), y)

Learning Algorithm:  $\hat{h} = A(\{(x_i, y_i)\}_{i=1}^N)$ , such that

$$\hat{h} = \operatorname{argmin}_{h} \sum_{i=1}^{N} L(h(x_i), y_i)$$



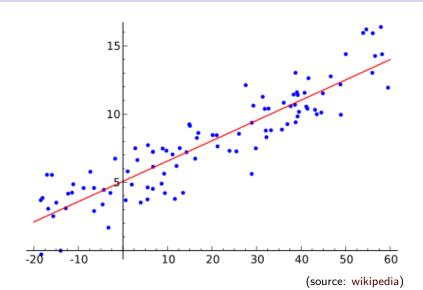
### An Example: Linear Regression

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers





# Linear Regression (cont.)

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Other Issues

• The hypothesis space:

$$h_{\vec{w}}(x) = w_0 + w_1 x$$

where  $\vec{w} = [w_0, w_1]$ 

• The loss function:

$$L(h_{\vec{w}}, y) = \frac{1}{N} \sum_{i=1}^{N} (y_i - h_{\vec{w}}(x_i))^2$$

i.e. the sum of the squared error

We want to find

$$w^* = \underset{w}{\operatorname{argmin}} L(h_{\vec{w}}, y)$$



### Minimizing the Loss

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

- In the most simple case, we can easily find one (or more) solution(s)
  - Just take the derivatives and equal to 0
- In many cases this is not possible (or we may want to enforce some constraints on the parameters)
- In practice, there are many ways to estimate  $w^*$



#### An Example: Gradient Descent

Processamento e Recuperação de Informação

Introduction

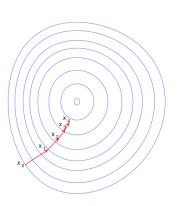
Supervised Learning

Text Classifiers

Other Issues

 $w \leftarrow$  any point in the parameter space **loop** until convergence **do for each**  $w_i$  **in**  $\vec{w}$  **do**  $w_i \leftarrow w_i - \alpha \frac{\partial}{\partial w_i} L(h_{\vec{w}}, y)$ 

 $\alpha = \text{learning rate}$ 



(source: wikipedia)



#### Classification

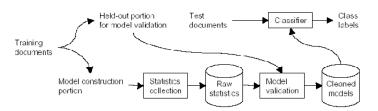
Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

- Learning to assign objects to classes given examples
- Learn a classifier





### An Example: Logistic Regression

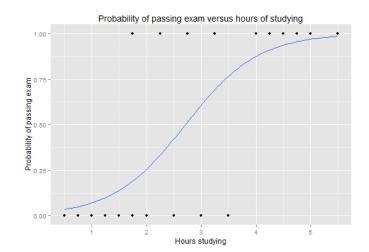
Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Other Issues



(source: wikipedia)





# Logistic Regression (cont.)

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Other Issues

The hypothesis space:

$$h_{\vec{w}}(x) = \frac{1}{1 + e^{-(w_0 + w_1 x)}}$$

where  $\vec{w} = [w_0, w_1]$ 

• The loss function:

$$L(h_{\vec{w}}, y) = \frac{1}{N} \sum_{i=1}^{N} C(h_{\vec{w}}(x_i), y)$$

where

$$C(h_{\vec{w}}(x), y) = \begin{cases} -\log(h_{\vec{w}}(x)) & \text{if } y = 1\\ -\log(1 - h_{\vec{w}}(x)) & \text{if } y = 0 \end{cases}$$

We want to find

$$w^* = \underset{w}{\operatorname{argmin}} L(h_{\vec{w}}, y)$$



#### Outline

Processamento e Recuperação de Informação

Introduction

Supervised Learning

#### Text Classifiers

Classifiers
Nearest Neighbor

Classifiers Generative Bayesian Classifiers

Linear Discriminative Classifiers

- Introduction
- 2 Supervised Learning
- Text Classifiers
  - Nearest Neighbor Classifiers
  - Generative Bayesian Classifiers
  - Linear Discriminative Classifiers
- 4 Other Issues



### Text Classification vs. Data Mining

Processamento e Recuperação de Informação

#### Introduction

Supervised Learning

#### Text Classifiers

Nearest Neighbor

Classifiers
Generative Bayesian

Linear Discriminative Classifiers

- Lots of features and a lot of noise
- No fixed number of columns
- No categorical attribute values
- Data scarcity
- Larger number of class labels
- Hierarchical relationships between classes less systematic



#### Text Classifiers

Processamento e Recuperação de Informação

Introduction

Supervised Learning

#### Text

Classifiers
Nearest Neighbor

Classifiers
Generative Bayesian
Classifiers
Linear Discriminative

Classifiers

- Nearest Neighbor Classifiers
  - Classify documents according to the class distribution of their neighbors
- Generative Bayesian classifiers (e.g., naïve Bayes)
  - Discover the class distribution most likely to have generated a test document
- Linear discriminative classifiers (e.g., the perceptron, or support vector machines):
  - Discover an hyperplane that separates classes



# Nearest Neighbor Classifiers

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

- Similar documents are expected to be assigned the same class label
  - Similarity: vector space model + cosine similarity
- Training:
  - Index each document and remember class label
- Testing:
  - Fetch k most similar documents to the given document
  - Majority class wins
  - Alternatives:
    - Weighted counts: counts of classes weighted by the corresponding similarity measure
    - Per-class offset: tuned by testing the classifier on a portion of training data held out for this purpose



#### kNN Classifier

Processamento e Recuperação de Informação

Introduction

Supervised Learning

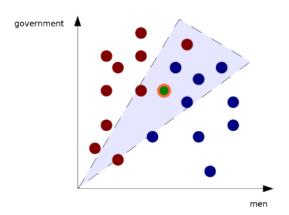
Text Classifiers

Nearest Neighbor

Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers



$$score(c, d_q) = b_c + \sum_{d \in kNN(d_q)} sim(d_q, d)$$



# Properties of kNN

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Generative Bayesian

Linear Discriminative Classifiers

Other Issues

#### Advantages:

- Reuse of standard vector space model and availability of associated technology (e.g., inverted indexes)
- Collection updates trivial
- Accuracy comparable to best known classifiers

#### Problems:

- Classification efficiency
  - many lookups over the document collection/index
  - sorting by overall similarity
  - picking the best k documents
- Space overhead and redundancy
  - Data stored at level of individual documents
  - Poor generalization
- Choosing a value for k



#### Improvements for kNN

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Classifiers
Nearest Neighbor

Classifiers Generative Bayesian

Linear Discriminative Classifiers

- To reduce space requirements and speed up classification
  - Find clusters in the data (clustering will be covered in the next lecture)
  - Store only a few statistical parameters per cluster
  - Compare with documents in only the most promising clusters
- However...
  - Ad-hoc choices for number and size of clusters and parameters
  - Number of clusters depends on the data



#### Bayesian Classifiers

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Generative Bayesian Classifiers

Linear Discriminative Classifiers

Other Issues

- Probabilistic document classifier
- Assumptions:
  - A document can belong to exactly one class
  - **2** Each class c has an associated prior probability P(c)
  - **3** There is a class-conditional document distribution P(d|c) for each class (i.e., the likelihood)
- Given a document *d*, the probability of it being generated by class *c* is:

$$P(c|d) = \frac{P(d|c)P(c)}{\sum_{\gamma} P(d|\gamma)P(\gamma)}$$

• The class with the highest probability is assigned to  $d_q$  (i.e., we use a maximum a-posteriory rule)



### Learning the Document Distribution

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Classifiers Generative Bayesian

Classifiers
Linear Discriminative

Classifiers

- P(d|c) is estimated based on parameters  $\Theta$
- ullet  $\Theta$  is estimated based on two factors:
  - Prior knowledge before seeing any documents
  - 2 Terms in the training documents
- Bayes Optimal Classifier

$$P(c|d) = \int_{\Theta} \frac{P(d|c,\Theta)P(c|\Theta)}{\sum_{\gamma} P(d|\gamma,\Theta)P(\gamma|\Theta)} P(\Theta|D)$$

- This can be hard to compute
- Maximum Likelihood Estimate:  $P(d|c, \hat{\Theta})$

$$\hat{\Theta} = argmax_{\Theta} P(d|c,\Theta)$$



#### Naïve Bayes Classifier

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Classifiers Generative Bayesian

Classifiers

Linear Discriminative Classifiers

Other Issues

Naïve assumption

- assumption of independence between terms
- joint term distribution is the product of the marginals
- Widely used owing to
  - simplicity and speed of training, applying, and updating
- Two kinds of widely used marginals for text
  - Binary model
  - Multinomial model



# Naïve Bayes Models

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text

Classifiers
Nearest Neighbor

Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

Other Issues

Binary Model: Each parameter  $\theta_{c,t}$  indicates the probability that a document in class c will mention term t at least once

$$P(d|c,\Theta) = \prod_{t \in d} \theta_{c,t} \prod_{t \notin d} (1 - \theta_{c,t})$$
$$\theta_{c,t} = \frac{N_{c,t}}{N_c}$$

 $N_{c,t} = n$ . of docs in class c containing term t  $N_c = n$ . of docs in class c



# Naïve Bayes Models (cont.)

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Classifiers Generative Bayesian

Classifiers
Linear Discriminative

Classifiers

Other Issues

#### Multinomial Model:

- ullet each class has an associated die with |W| faces
- each parameter  $\theta_{c,t}$  denotes probability of the face turning up on tossing the die, i.e.  $\sum_{d \in c} n(d,t) / \sum_{d \in c} \ell_d$
- term t occurs n(d, t) times in document d
- document length is a random variable denoted L

$$P(d|c,\Theta) = P(L = \ell_d|c)P(d|\ell_d,c)$$

$$= P(L = \ell_d|c)\frac{\ell_d!}{\prod_{t \in d} n(d,t)!} \prod_{t \in d} \theta_{c,t}^{n(d,t)}$$

$$\sim P(L = \ell_d|c)\prod_{t \in d} \theta_{c,t}^{n(d,t)}$$



#### Parameter Smoothing

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text

Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

Other Issues

• What if a test document  $d_q$  contains a term t that never occurred in any training document in class c?



# Parameter Smoothing

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Classifiers Generative Bayesian

Classifiers

Linear Discriminative Classifiers

Other Issues

• What if a test document  $d_q$  contains a term t that never occurred in any training document in class c?

- $P(c|d_q) = 0$
- Even if many other terms clearly hint at a high likelihood of class c generating the document
- Thus, MLE cannot be used directly
- We can use Laplace smoothing
  - Simply adds 1 to each count

$$\theta_{c,t} = \frac{\sum_{d \in c} n(d,t) + 1}{\sum_{d \in c} \ell_d + |W|}$$



#### Performance Analysis

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Classifiers
Generative Bayesian

Classifiers

Linear Discriminative Classifiers

- Multinomial naïve Bayes classifier generally outperforms the binary variant
- kNN may outperform Naïve Bayes
- Naïve Bayes is faster and more compact
- Determines decision boundaries
  - Regions of the term-space where different classes have similar probabilities
  - Documents in these regions are hard to classify
  - Strongly biased



#### Discriminative Classification

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Classifiers

- Naïve Bayes classifiers are generative
- Differently, discriminative classifiers:
  - Directly map the feature space to class labels
  - Class labels are encoded as numbers
    - $\bullet\,$  e.g: +1 and -1 for two a class problem
- For instance, we can try to find a vector  $\alpha$  such that the sign of  $\alpha \cdot d + b$  directly predicts the class of a document d
- Possible solutions:
  - Linear least-square regression
  - The Perceptron
  - Support Vector Machines



#### What is a Linear Discriminative Classifier?

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor

Generative Bayesian

Linear Discriminative Classifiers

Other Issues

#### Essentially:

- Classification decision is based on the value of a linear combination of the features
- Can be seen as the splitting of a high-dimensional input space with a hyperplane

$$y(d_1,\ldots,d_n)=f(\alpha_1d_1+\alpha_2d_2+\ldots+\alpha_nd_n)$$

- $\alpha_i$  are parameters (i.e., the weight of each feature  $d_i$ )
- f is the activation function (e.g.,  $f(d) = 1_{x \ge 0}(d)$ )
- The result of  $y(d_1, \ldots, d_n)$  corresponds to the estimated class



#### The Bias Term

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

- Notice that the decision hyperplane must go through the origin
- Could be achieved by preprocessing the input, but this is not always desirable or possible
- Solution : Add a bias input:

$$y(d_1,\ldots,d_n)=f(b+\alpha_1d_1+\ldots+\alpha_nd_n)$$

- Same as an input connected to the constant 1
- We consider this ghost input implicit henceforth



### Training: The Perceptron Algorithm

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers Generative Bayesian

Linear Discriminative Classifiers

Other Issues

Switching to vector notation:

$$y(\mathbf{d}) = f(\alpha \mathbf{d}) = f_{\alpha}(d) \tag{1}$$

 Assume we need to separate sets of points A (i.e., the positive examples) and B (i.e., the negative examples)

$$E(\alpha) = \sum_{\mathbf{d} \in A} (1 - f_{\alpha}(\mathbf{d})) + \sum_{\mathbf{d} \in B} f_{\alpha}(\mathbf{d})$$
 (2)

- Goal:  $E(\alpha) = 0$
- ullet Start from a random lpha and improve it iteratively



# Algorithm Pseudo-Code

Processamento e Recuperação de Informação

#### Introduction

Supervised Learning

#### Text

Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

Other Issues

**1** Start with random  $\alpha$ , set t = 0

2 Select a vector  $\mathbf{d} \in A \cup B$ 

**3** If  $\mathbf{d} \in A$  and  $\alpha \mathbf{d} \leq 0$ , then  $\alpha_{t+1} = \alpha_t + \mathbf{d}$ 

**1** Else if  $\mathbf{d} \in B$  and  $\alpha \mathbf{d} \geq 0$ , then  $\alpha_{t+1} = \alpha_t - \mathbf{d}$ 

Conditionally go to step 2

ullet Guaranteed to converge iff A and B are linearly separable!



#### Summary of Simple Perceptrons

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers Nearest Neighbor

Classifiers
Generative Bayesian

Linear Discriminative Classifiers

- Simple and reasonably efficient online training
- Easy to extend in order to consider multi-class classification
- Works well for document classification, and more generally for problems with many features
- Limited capabilities (e.g., does not try to optimize the separation "distance" between classes)
  - Just looks for a hyperplane that separates the two sets
  - Methods such as Support Vector Machines, on the other hand, try to maximize the distance between two closest opposite sample points (i.e., the margin of the separating hyperplane)



#### Linear Discriminative Classifiers and SVMs

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers Generative Bayesian

Linear Discriminative Classifiers

Other Issues

Hypothesis:

- The classes can be separated by an hyperplane
- The hyperplane that is close to many training data points has a greater chance of misclassifying test instances
- An hyperplane that passes through a "no-man's land", has lower chances of misclassifications
- Make a decision by thresholding
  - Seek an hyperplane that maximizes the distance to any training point
  - Choose the class on the same side of the hyperplane as the test document (i.e., same as in the Perceptron)



### Discovering the Hyperplane

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

- Assume the training documents are separable by an hyperplane perpendicular to a vector  $\alpha$
- ullet Seek a vector  $\alpha$  which maximizes the distance of any training point to the hyperplane
- This corresponds to solving the following quadratic programming problem:

Minimize 
$$\frac{1}{2}\alpha \cdot \alpha$$
  
subject to  $c_i(\alpha \cdot d_i + b) \ge 1, \forall i = 1, \dots, n$ 



#### **SVM** Classifier

Processamento e Recuperação de Informação

Introduction

Supervised Learning

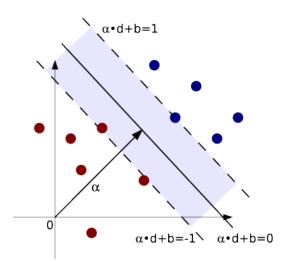
Text

Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers





# Non Separable Classes

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

Other Issues

Classes in the training data not always separable

We introduce slack variables

Minimize 
$$\frac{1}{2}\alpha \cdot \alpha + C \sum_i \xi_i$$
  
subject to  $c_i(\alpha \cdot d_i + b) \ge 1 - \xi_i, \forall i = 1, \dots, n$   
and  $\xi_i \ge 0, \forall i = 1, \dots, n$ 

Implementations often solve the equivalent dual problem

Maximize 
$$\sum_{i} \lambda_{i} - \frac{1}{2} \sum_{i,j} \lambda_{i} \lambda_{j} c_{i} c_{j} (d_{i} \cdot d_{j})$$
 subject to  $\sum_{i} c_{i} \lambda_{i} = 0$  and  $0 < \lambda_{i} < C, \forall i = 1, \dots, n$ 



### Analysis of SVMs

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Nearest Neighbor Classifiers

Generative Bayesian Classifiers

Linear Discriminative Classifiers

Other Issues

#### Complexity:

- Quadratic optimization problem
- Requires on-demand computation of inner-products
- Recent SVM packages work in linear time

#### Performance:

- Amongst most accurate classifier for text
- Better accuracy than Naïve Bayes and most classifiers
- Linear SVMs suffice
  - Standard text classification tasks have classes almost separable using a hyperplane in feature space
- Non-linear SVMs can be achieved through kernel functions



#### Outline

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

- Introduction
- 2 Supervised Learning
- 3 Text Classifiers
- 4 Other Issues



# Other Issues (1)

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

- Tokenization and feature extraction
  - E.g.: replacing monetary amounts by a special token, part-of-speech tagging, representations based on *n*-grams, etc.
- Handling scenarios with multiple classes, or with multiple labels per test document, with binary classifyers like SVMs
  - E.g., one-vs.-rest heuristic
    - e.g. "sports" vs. "not-sports", "science" vs. "not-science", etc.
    - Create a classifier for each case
    - Assign class(es) with the highest confidence



# Other Issues (2)

Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Other Issues

Evaluating text classifiers

- Accuracy
- Training speed and scalability
- Simplicity, speed, and scalability for document modifications
- Ease of diagnosis, interpretation of results, and adding human judgment and feedback
- Many other practical issues...



Processamento e Recuperação de Informação

Introduction

Supervised Learning

Text Classifiers

Other Issues

Questions?