



Processamento
e Recuperação
de Informação

Search Engine
Ranking

Ranking
Signals

The Ranking
Function

Unsupervised
Rank Fusion

Learning to
Rank

Some Context

Learning to
Rank (cont.)

Processamento e Recuperação de Informação

Learning to Rank

Departamento de Engenharia Informática
Instituto Superior Técnico

1º Semestre
2018/2019



Outline

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- Ricardo Baeza-Yates, Berthier Ribeiro-Neto, Modern Information Retrieval, 2nd edition. Chapter 11.
- T.-Y. Liu, "Learning to rank for information retrieval," Foundations and Trends in Databases, vol. 3, no. 3, pp. 225-331, 2009.



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Search Engine Ranking

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Ranking is the hardest and most important function of a search engine

Main challenges:

- Evaluation
- Managing Web spam
- Identification of relevant content
- Defining the ranking function



Evaluating the Ranking

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- Devise an adequate process of **evaluating the ranking**, in terms of **relevance** of results to the user
- Without such evaluation, it is close to impossible to fine tune the ranking function
- Without fine tuning the ranking, there is no state-of-the-art engine—this is an empirical field of science



Dealing with Web Spam

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- Avoiding, preventing, managing Web spam
- Spammers are malicious users who try to trick search engines by artificially inflating signals used for ranking
- A consequence of the economic incentives of the current advertising model adopted by search engines



Defining Relevant Content

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Evidence of quality can be indicated by several signals such as:

- Domain names
- Text content
- Links (e.g. PageRank)
- Web page access patterns

Additional useful signals are provided by the layout of the Web page, its title, metadata, font sizes, etc.



The Ranking Function

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Following: from simple ranking functions to complex combinations of signals



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Evidences for Relevance

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Three main types of signals:

- 1 Content
- 2 Structure
- 3 Usage

In total we can have hundreds of distinct signals

- Bing claims to use > 1000 (see [here](#))
- Google claims to use > 200 many with > 50 variations



Content Signals

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- Related to the **text** itself
- Can vary from **simple word counts** to a **full IR score**, such as TF-IDF or BM25
- Can be provided by the layout, that is, the HTML source
 - Simple **format** indicators (more weight given to titles/headings)
 - Sophisticated indicators as the **proximity** of certain tags in the page



Structure Signals

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- Intrinsic to the **linked structure** of the Web
- Some of them are textual in nature, such as **anchor text**
- Others pertain to the links themselves, such as **in-links** and **out-links** from a page
- Link-based signals find broad usage beyond classic search engine ranking



Web Usage Signals

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- Main one is the implicit feedback provided by the user clicks (**click-through**)
- Other usage signals include:
 - information on the user's **geographical context** (IP address, language)
 - **technological context** (operating system, browser)
 - **temporal context** (query history by the use of cookies)
 - even **site speed**



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Simple Ranking Scheme

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- Use only **text-based ranking**
 - E.g. BM25 or cosine similarity
- Applied in early search engines

Or...

- Use a global ranking function such as **PageRank**
- Quality of a Web page in the result set is independent of the query
- The query only selects pages to be ranked



Simple Combination of Signals

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Learning to
Rank (cont.)

- Use a linear combination of different ranking signals

Example

- Consider the pages p that satisfy query Q
- Rank score $R(p, Q)$ of page p with regard to query Q can be computed as

$$R(p, Q) = \alpha BM25(p, Q) + (1 - \alpha) PR(p)$$

- $\alpha = 1$: text-based ranking
- $\alpha = 0$: link-based ranking, independent of the query



A More Complex Combination

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- Current engines combine a text-based ranking with a link-based ranking, most of them a lot more complex than BM25 and PageRank
- Value of α is tuned experimentally using
 - Labeled data as ground truth, or
 - Clickthrough data
- α might even be query dependent
 - for *navigational* queries α could be made smaller than for *informational* queries



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Principle

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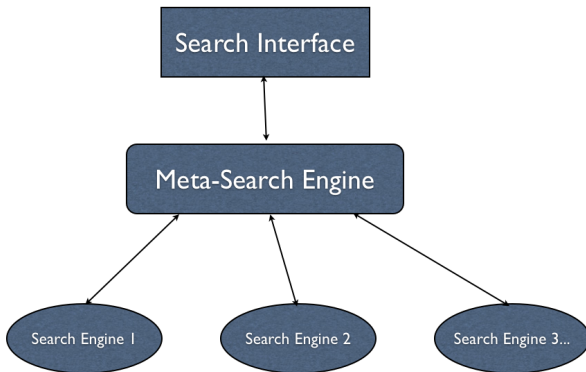
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Combining Similarity Scores

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Learning to
Rank (cont.)

- ① eliminate **duplicates**
- ② apply a fusion algorithm
 - using similarity scores provided by underlying SE

these techniques can be used also to combine ranking functions within a search engine



Combination Using Similarities

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Learning to
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- $CombMIN(d_j) = \min(s_{1j}, s_{2j}, \dots, s_{kj})$
(use the minimum ranking)
- $CombMAX(d_j) = \max(s_{1j}, s_{2j}, \dots, s_{kj})$
- $CombSUM(d_j) = \sum s_{ij}$
(add the similarity scores)
- $CombMNZ(d_j) = CombSUM(d_j) \times r_j$, where r_j is the number of systems that retrieved d_j

CombSUM and *CombMNZ* perform better. *CombMNZ* slightly outperforms *CombSUM* in most cases.



Combination using ranking positions

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Borda(1770) Ranking: each voter assigns a linear preference order of candidates, n to the first, $n - 1$ to the second, etc. Unranked candidates divide the votes. Winner gets the most points.

Condorcet (1787) Ranking: do pairwise comparisons to count how many times a doc “wins”, “loses” or “ties” against other documents (as in a soccer tournament). Doc with most wins gets highest score. Ties broken on number of losses.

Reciprocal ranking: assign a score $1/pos$ to each doc. Rank based on sum of scores.



Borda Ranking

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5 underlying search engines,
which have ranked four candidate pages a, b, c, d .

System 1: a, b, c, d

System 2: b, a, d, c

System 3: c, b, a, d

System 4: c, b, d

System 5: c, b

Scores:

$$\text{Score}(a) = 4 + 3 + 2 + 1 + 1.5 = 11.5$$

$$\text{Score}(b) = 3 + 4 + 3 + 3 + 3 = 16$$

$$\text{Score}(c) = 2 + 1 + 4 + 4 + 4 = 15$$

$$\text{Score}(d) = 1 + 2 + 1 + 2 + 1.5 = 7.5$$

The final ranking is: b, c, a, d



Condorcet Ranking

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Learning to
Rank (cont.)

System 1: a,b,c,d

System 2: b,a,d,c

System 3: c,b,a,d

System 4: c,b,d

System 5: c,b

comparisons (win:lose:tie):

pair	a	b	c	d
a	-	1:4:0	2:3:0	3:1:1
b	4:1:0	-	2:3:0	5:0:0
c	3:2:0	3:2:0	-	4:1:0
d	1:3:1	0:5:0	1:4:0	-

The final ranking is: *b, c, a, d*



Reciprocal Ranking

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5 underlying search engines,
which have ranked four candidate pages a, b, c, d .

System 1: a, b, c, d

System 2: b, a, d, c

System 3: c, b, a, d

System 4: c, b, d

System 5: c, b

Scores:

$$\text{Score}(a) = 1 + 1/2 + 1/3 + 0 + 0 = 1.83$$

$$\text{Score}(b) = 1/2 + 1 + 1/2 + 1/2 + 1/2 = 3$$

$$\text{Score}(c) = 1/3 + 1/4 + 1 + 1 + 1 = 3.55$$

$$\text{Score}(d) = 1/4 + 1/3 + 1/4 + 1/3 + 0 = 1.17$$

The final ranking is: c, b, a, d



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Why Learning to Rank?

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Learning to
Rank (cont.)

- Manual parameter tuning is usually difficult
 - Especially when there are many parameters and the evaluation measures are non-smooth
- Manual parameter tuning sometimes leads to **overfitting**
- It is non-trivial to combine the large number of models proposed in the literature (e.g. BM25, etc.) to obtain an even more effective model



What is Learning to Rank?

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L2R: apply machine learning techniques to learn the ranking of the results

- Use a **learning algorithm** fed with **training data** that contains ranking information
- **loss function to minimize:** number of mistakes done by the learned model



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Supervised Learning

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Rank (cont.)

Input: $\{(x_i, y_i)\}_{i=1}^N, x_i \in \mathcal{R}^M, y_i \in \mathcal{R}$

Hypothesis space: $h^* \in H$

Loss function: $L(h(x), y)$

Learning Algorithm: $\hat{h} = A(\{(x_i, y_i)\}_{i=1}^N)$, such that
$$\hat{h} = \operatorname{argmin}_h \sum_{i=1}^N L(h(x_i), y_i)$$

I.e. given a set of **training data** as input, use **learning algorithm** A to discover the function \hat{h} that minimizes the **loss** (e.g. the error)



An Example: Linear Regression

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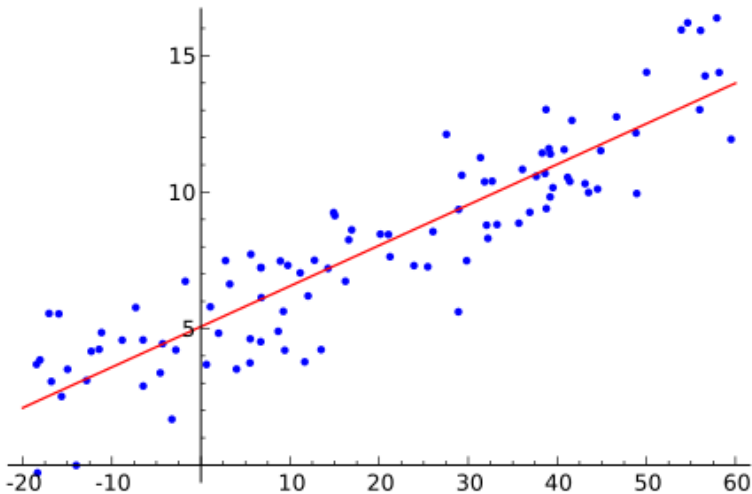
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(source: [wikipedia](#))



Linear Regression (cont.)

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Learning to
Rank (cont.)

- The hypothesis space:

$$h_{\vec{w}}(x) = w_0 + w_1 x$$

where $\vec{w} = [w_0, w_1]$

- The loss function:

$$L(h_{\vec{w}}, y) = \sum_{i=1}^N (y_i - h_{\vec{w}}(x_i))^2$$

i.e. the sum of the squared error

- We want to find

$$w^* = \underset{w}{\operatorname{argmin}} L(h_{\vec{w}}, y)$$



Minimizing the Loss

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Learning to
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- In the most simple case, we can easily find one (or more) solution(s)
 - Just take the derivatives and equal to 0
- In many cases this is not possible (or we may want to enforce some constraints on the parameters)
- In practice, there are many ways to estimate w^*



An Example: Gradient Descent

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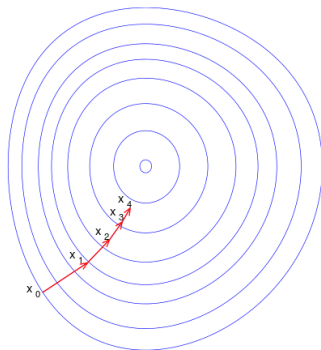
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Learning to
Rank (cont.)

$w \leftarrow$ any point in the
parameter space
loop until convergence **do**
 for each w_i **in** \vec{w} **do**
 $w_i \leftarrow w_i - \alpha \frac{\partial}{\partial w_i} L(h_{\vec{w}}, y)$

$\alpha =$ learning rate



(source: [wikipedia](#))



Other Types of Supervised Learning

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Learning to
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(besides regression and ranking)

- Classification
 - Classify email as spam vs. ham
 - Loss: accuracy
- Structured prediction
 - Find faces in an image
 - Loss: Precision/Recall of faces



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The L2R Framework

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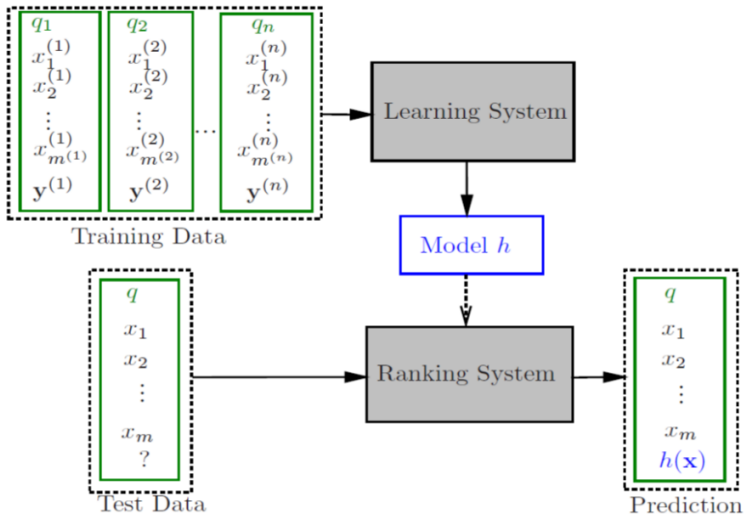
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L2R Techniques

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Three main approaches:

Pointwise: focuses on individual pages

Pairwise: focuses on comparing pairs of pages

Listwise: focuses on the ranked list of pages



The Pointwise Approach

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	The Pointwise Approach		
	Regression	Classification	Ordinal Regression
Input Space	Single documents y_j		
Output Space	Real values	Non-ordered Categories	Ordinal categories
Hypothesis Space	Scoring function $f(x)$		
Loss Function	Regression loss	Classification loss	Ordinal regression loss
	$L(f; x_j, y_j)$		



An Example: Ranking Perceptron

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Koby Crammer and Yoram Singer, "Pranking with ranking," In Proceedings of the 14th International Conference on Neural Information Processing Systems (NIPS'01), 2001.

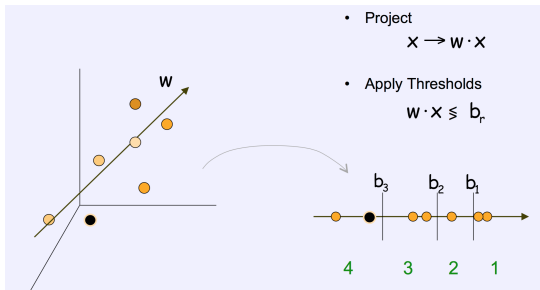
Adaptation of the *Perceptron algorithm*:

Input space: $\mathbf{x} = \{x_j\}_{j=1}^m$

Output space: $y_j \in \{1, 2, 3, \dots\}$

Hypothesis Space: $f(\mathbf{x}) = \mathbf{w} \cdot \mathbf{x}$

Loss function: $L(f, x_j, y_j) = \sum_{j=1}^T |y_j - f(x_j)|$





The Ranking Perceptron Algorithm

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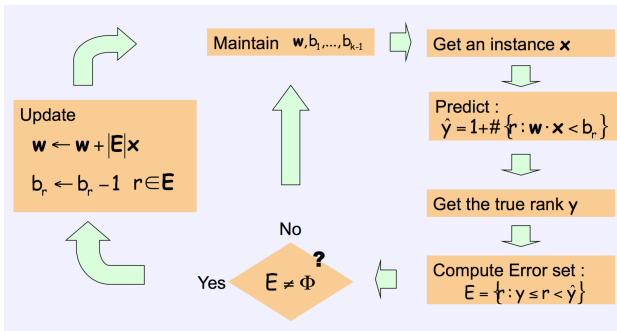
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Adaptation of the *Perceptron algorithm*:





Problem with the Pointwise Approach

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- The position of documents in the ranked list is invisible to the loss functions
- The overall loss function will be dominated by queries with a large number of documents



The Pairwise Approach

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	The Pairwise Approach
Input Space	Document pairs (x_u, x_v)
Output Space	Preference $y_{u,v} \in \{+1, -1\}$
Hypothesis Space	Preference function $h(x_u, x_v) = 2 \cdot I_{\{f(x_u) > f(x_v)\}} - 1$
Loss Function	Pairwise classification loss $L(h; x_u, x_v, y_{u,v})$



An Example: RankBoost

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Y. Freund, R. Iyer, R. E. Schapire, and Y. Singer, "An efficient boosting algorithm for combining preferences," Journal of Machine Learning Research, vol. 4, pp. 933–969, 2003.

Input space: Document pairs (x_u, x_v)

Output space: Relative order $y_{u,v} \in \{-1, +1\}$

Hypothesis Space: $f(x) = \sum_t \alpha_t f_t(x)$

Loss function: $L(f; x_u; x_v; y_{u,v}) = e^{-y_{u,v}(f(x_u) - f(x_v))}$

Algorithm 1 Learning Algorithm for RankBoost

Input: document pairs

Given: initial distribution \mathcal{D}_1 on input document pairs.

For $t = 1, \dots, T$

 Train weak ranker f_t based on distribution \mathcal{D}_t .

 Choose α_t

 Update $\mathcal{D}_{t+1}(x_u^{(i)}, x_v^{(i)}) = \frac{1}{Z_t} \mathcal{D}_t(x_u^{(i)}, x_v^{(i)}) \exp(\alpha_t(f_t(x_u^{(i)}) - f_t(x_v^{(i)})))$

 where $Z_t = \sum_{i=1}^n \sum_{u,v: y_{u,v}=1} \mathcal{D}_t(x_u^{(i)}, x_v^{(i)}) \exp(\alpha_t(f_t(x_u^{(i)}) - f_t(x_v^{(i)})))$.

Output: $f(x) = \sum_t \alpha_t f_t(x)$.



The RankBoost Algorithm

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- Initial distribution: $D_1 = 1/\#pairs$
- Weak learners: $f_t(x) = \begin{cases} 1 & \text{if } h_i > \theta \\ 0 & \text{if } h_i \leq \theta \end{cases}$
 - h_i is the value of a single feature
 - θ is found by maximizing
$$r = \sum_{h(x) > \theta} f_t(x) \pi(x) + \sum_{h(x) \leq \theta} f_t(x) \pi(x)$$
where $\pi(x) = \sum_{x'} (D(x', x) - D(x, x'))$
- Updating D_t for a pair (x_u, x_v) (where $y_{v,u} = 1$):
 - if f_t yields the correct ranking, $D_t(x_u, x_v)$ is decreased, otherwise it is increased
- Finding α_t : minimize Z_t as a function of α_t
 - Can be done by binary search
 - Other methods can be applied (see paper)



Improvement of Pairwise Approach

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Search Engine
Ranking

Ranking
Signals

The Ranking
Function

Unsupervised
Rank Fusion

Learning to
Rank

Some Context

Learning to
Rank (cont.)

Advantage

Predicting relative order is closer to the nature of ranking than predicting class label or relevance score

Problems

- Relative order of two documents still does not predict their final position
- The distribution of document pair number is more skewed than the distribution of document rank, with respect to different queries



Document Pair Distribution

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Ranking

Ranking
Signals

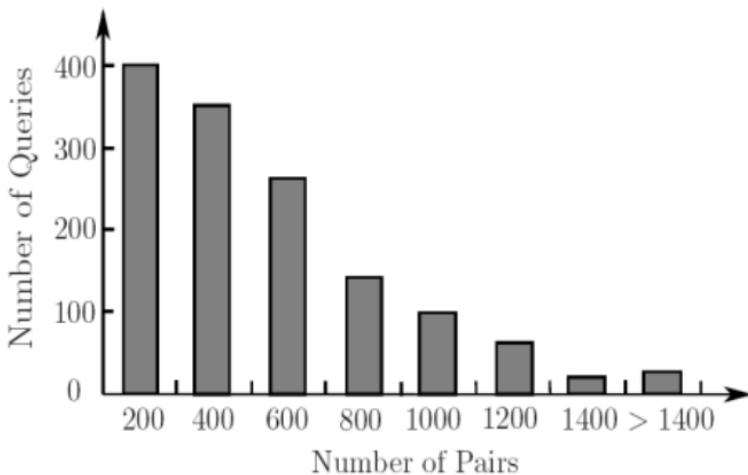
The Ranking
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Learning to
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Some Context

Learning to
Rank (cont.)





The Listwise Approach

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Learning to
Rank (cont.)

	The Listwise Approach	
	Listwise Loss Minimization	Direct Optimization of IR Measure
Input Space	Document set $\mathbf{x} = \{x_j\}_{j=1}^m$	
Output Space	Permutation π_y	Ordered categories $\mathbf{y} = \{y_j\}_{j=1}^m$
Hypothesis Space	$h(\mathbf{x}) = \text{sort}_\circ f(\mathbf{x})$	$h(\mathbf{x}) = f(\mathbf{x})$
Loss Function	Listwise loss $L(h; \mathbf{x}, \pi_y)$	1-surrogate measure $L(h; \mathbf{x}, \mathbf{y})$



Direct Optimization of IR Measures

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Learning to
Rank (cont.)

- It is natural to directly optimize what is used to evaluate the ranking results
- However, it is non-trivial
- Evaluation measures such as NDCG are **non-continuous** and **non-differentiable** since they depend on the rank positions
- It is challenging to optimize such objective functions, since most optimization techniques in the literature were developed to handle continuous and differentiable cases



Solutions

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Learning to
Rank (cont.)

- Approximate the objective
 - Soften (approximate) the evaluation measure so as to make it smooth and differentiable
- Bound the objective
 - Optimize a smooth and differentiable upper bound of the evaluation measure
- Optimize the non-smooth objective directly
 - Use IR measure to update the distribution in Boosting
 - Use genetic programming



An Example: RankGP

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Learning to
Rank (cont.)

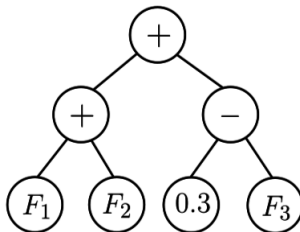
J.-Y. Yeh et al, "Learning to rank for information retrieval using genetic programming," in SIGIR 2007 Workshop in Learning to Rank for Information Retrieval, 2007.

Input space: $\mathbf{x} = \{x_j\}_{j=1}^m$

Output space: Relative order $\mathbf{y} = \{y_j\}_{j=1}^m$

Hypothesis Space: $f(x)$

Loss function: IR evaluation measure





RankGP Algorithm

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Learning to
Rank (cont.)

A standard Genetic Programming approach

- **Individual:** ranking function
- **Evolution mechanism:**
 - Crossover, Mutation, Reproduction
 - Tournament selection
- **Fitness:**
 - Mean Average Precision



Improvement of Listwise Approach

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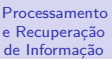
Learning to
Rank (cont.)

Advantages

- Take all the documents associated with the same query as the learning instance
- Rank position is visible to the loss function

Problems

- Complexity



Ranking Signals

The Ranking Function

Unsupervised Rank Fusion

Learning to Rank

Some Context

Learning to Rank (cont.)

Questions?