

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Processamento e Recuperação de Informação Information Retrieval Models

Departamento de Engenharia Informática Instituto Superior Técnico

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Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- The Vector Space Model
- Probabilistic Models
- **5** Comparison of the Different Models



Bibliography

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different

Models

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Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- 3 The Vector Space Model
- Probabilistic Models
- 6 Comparison of the Different Models



Retrieval Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean

The Vector Space Model

Probabilistic Models





Index Terms

Processamento e Recuperação de Informação

Document Model

Model

Models

The Vector

Space Model
Probabilistic

Comparison of the Different Models In the classic IR models, documents are represented by index terms

- full text/selected keywords
- structure/no structure

Not all terms are equally useful

• index terms can be weighted

We assume that terms are mutually independent

• this is, of course, a simplification



Definition of a Document Model

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Definition

Let t be the number of index terms in the collection of documents, and let k_i be a generic index term.

- $K = \{k_1, \dots, k_t\}$ is the set of all index terms.
- A weight $w_{i,j} \ge 0$ is associated with each index term k_i of a document d_j .
- For an index term which does not appear in the document text, $w_{i,j} = 0$.
- Each document d_j is associated a term vector $\vec{d_j}$, represented by $\vec{d_j} = (w_{1,j}, w_{2,j}, \dots, w_{t,j})$.
- Function $g_i(\vec{d_j})$ returns the weight of index term k_i in vector $\vec{d_i}$.



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- 3 The Vector Space Model
- Probabilistic Models
- 6 Comparison of the Different Models



Boolean Model Queries

Processamento e Recuperação de Informação

Document Model

Generic

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models Follows Boolean algebra syntax and semantics

Term weights are binary

•
$$w_{i,j} \in \{0,1\}$$

•
$$w_{i,j} = 1$$
 — term present,

•
$$w_{i,j} = 0$$
 — term not present

Queries are Boolean expressions

• E.g.,
$$q = k_a \wedge (k_b \vee \neg k_c)$$

 Documents are considered relevant if the query evaluates to 1 (true)



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

d_1

That government is best which governs least

d_2

That government is best which governs not at all

d_3

When men are prepared for it, that will be the kind of government which they will have



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic
Models

Comparison of the Different

Models

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When men are prepared for it, that will be the kind of government which they will have $q = \mathsf{government} \land \mathsf{best}$

answer: d_1, d_2



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic

Models

Models

Comparison of the Different

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answer: d_1, d_2

 $q = \mathsf{government} \land \mathsf{best} \land \neg \mathsf{all}$

answer: d_1



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

d_1

That government is best which governs least

d_2

That government is best which governs not at all

d_3

When men are prepared for it, that will be the kind of government which they will have $q = \mathsf{government} \land \mathsf{best}$

answer: d_1, d_2

 $q = \mathsf{government} \land \mathsf{best} \land \neg \mathsf{all}$

answer: d_1

 $q = \mathsf{government} \lor \mathsf{best} \land \neg \mathsf{all}$

answer: d_1, d_2, d_3



Document-Query Similarity

Processamento e Recuperação de Informação

Document Model

Generic

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models Queries can be translated to a disjunction of conjunctive vectors

$$\vec{q} = k_a \wedge (k_b \vee \neg k_c) \Leftrightarrow (1, 1, 1) \vee (1, 1, 0) \vee (1, 0, 0)$$

each tuple corresponds to a vector (k_a, k_b, k_c)

Similarity of a document to a query is defined as:

$$\mathit{sim}(d_j,q) = \left\{ egin{array}{ll} 1 & ext{if } \exists \vec{q_c} \in \vec{q} | \forall_i, g_i(\vec{d_j}) = g_i(\vec{q_c}) \\ 0 & ext{otherwise} \end{array} \right.$$



The Boolean Model

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Why is it good?

- Simple model based on Boolean algebra
- Intuitive concept
- Precise semantics
- Clear formal basis
- Widely adopted by early information systems



Boolean Model

Processamento e Recuperação de Informação

Document Model

Generic

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Limitations:

- Retrieval based only on binary decisions
 - More similar to data retrieval than information retrieval
 - Can retrieve too many, or too little documents
 - Some documents may be more relevant than others
- How do you translate a query to a Boolean expression?
 - Non-expert users may not be able to represent their information needs using Boolean expressions
- Terms are all equally important
 - Index term weighting can bring great improvements in performance



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- 1 Generic Document Mode
 - 2 The Boolean Model
 - The Vector Space Model
 - Probabilistic Models
- 6 Comparison of the Different Models



Documents as Vectors

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models Documents are represented as vectors

•
$$\vec{d}_j = (w_{1,j}, w_{2,j}, \dots, w_{t,j})$$

- $w_{i,j}$ is the weight of term i in document j
- Queries are also vectors

•
$$\vec{q} = (w_{1,q}, w_{2,q}, \dots, w_{t,q})$$

 Vector operations can be used to compare queries×documents (or documents×documents)



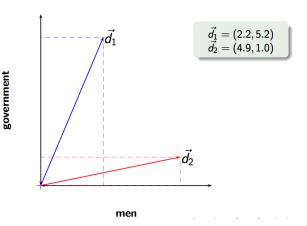
Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models





Defining Document Vectors

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Two questions are still unanswered:

- How do we define term weights?
- 4 How do we compare documents to queries?



Defining Term Weights — TF

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Term frequency

Term frequency is a measure of term importance within a document

Definition

Let N be the total number of documents in the system and n_i be the number of documents in which term k_i appears. The normalized frequency of a term k_i in document d_i is given by:

$$f_{i,j} = \frac{freq_{i,j}}{\max_{l} freq_{l,j}}$$

where $freq_{i,j}$ is the number of occurrences of term k_i in document d_i .



Defining Term Weights — IDF

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

(Inverse) Document frequency

Document frequency is a measure of term importance within a collection

Definition

The inverse document frequency of a term k_i is given by:

$$idf_i = \log\left(\frac{N}{n_i}\right)$$



Defining Term Weights — TF-IDF

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Definition

The weight of a term k_i in document d_j for the vector space model is given by the tf-idf formula:

$$w_{i,j} = f_{i,j} \times \log\left(\frac{N}{n_i}\right)$$



Components of TF-IDF

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Generic Document Model

The Boolean Model

The Vector

Probabilistic Models

Comparison of the Different Models Different TF-IDF formulations consider alternative approaches for the TF and IDF components, and also for normalizing the resulting vectors.

Term frequency		Document frequency		Normalization	
n (natural)	$tf_{t,d}$	n (no)	1	n (none)	1
l (logarithm)	$1 + \log(tf_{t,d})$	t (idf)	$\log \frac{N}{df_z}$	c (cosine)	$\frac{1}{\sqrt{w_1^2 + w_2^2 + + w_M^2}}$
a (augmented)	$0.5 + rac{0.5 imes ext{t} ext{f}_{t,d}}{ ext{max}_t (ext{t} ext{f}_{t,d})}$	p (prob idf)	$\text{max}\{0, \text{log} \frac{\textit{N}-\text{d}f_t}{\text{d}f_t}\}$	u (pivoted unique)	1/u
b (boolean)	$\begin{cases} 1 & \text{if } \operatorname{tf}_{t,d} > 0 \\ 0 & \text{otherwise} \end{cases}$			b (byte size)	$1/\mathit{CharLength}^{lpha}$, $lpha < 1$
L (log ave)	$\frac{1 + \log(tf_{t,d})}{1 + \log(ave_{t \in d}(tf_{t,d}))}$				



Document Similarity

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Similarity between documents and queries is a measure of the correlation between their vectors
- Documents/queries that share the same terms, with similar weights, should be more similar
- Thus, as similarity measure, we use the cosine of the angle between the vectors

$$sim(d_j, q) = \frac{\vec{d_j} \cdot \vec{q}}{|\vec{d_j}| \times |\vec{q}|} = \frac{\sum_{i=1}^t w_{i,j} \times w_{i,q}}{\sqrt{\sum_{i=1}^t w_{i,j}^2} \times \sqrt{\sum_{i=1}^t w_{i,q}^2}}$$



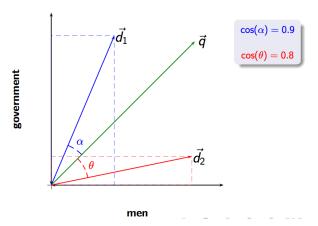
Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models





The Vector Space Model

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

Space Model
Probabilistic
Models

Comparison of the Different

Models

Why is it so good?

- Simple model, based on linear algebra
- Term weights are not binary
- Allows computing a continuous degree of similarity between queries and documents
- Thus, allows ranking documents according to their possible relevance



Improving the VSM (1)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

The BM25 Model

Consider not only the term frequency and inverse document frequency heuristics, but also the document length as a normalization factor for the term frequency

$$TF_{i,j} = rac{f_{i,j} imes (k_1+1)}{f_{i,j} + k_1 imes \left(1 - b + b rac{|d_j|}{avgdl}
ight)}$$
 $IDF_i = \log rac{N - n_i + 0.5}{n_i + 0.5}$
 $sim(d_j, q) = \sum_{i \in q} IDF_i imes TF_{i,j}$

To be detailed in the next lecture



Improving the VSM (2)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Latent Semantic Indexing

- Find a low-rank approximation of the matrix which describes the occurrences of terms in documents
 - Singular Value Decomposition
 - Compare the documents in the low-dimensional space
- The consequence of the rank lowering is that some dimensions are combined (e.g., mitigates the problem of identifying synonymy)
- To be detailed latter in the course



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- The Vector Space Model
- Probabilistic Models
- **6** Comparison of the Different Models



Probabilistic Models for IR

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models TF-IDF and VSM produces sufficiently good results in practice, but often criticized for being too ad-hoc or not principled

- Typically outperformed by probabilistic retrieval models and statistical language models in IR benchmarks
- Probabilistic retrieval models
 - use generative models of documents as bags-of-words
 - ullet explicitly model probability of relevance $P(R|d_j,q)$
 - probabilistic justification for TF-IDF-like approaches
- Statistical language models
 - use generative models of documents and queries as sequences-of-words
 - consider likelihood of generating query from document model or divergence of document model and query model



Probabilistic Retrieval Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector

Probabilistic Models

Comparison of the Different Models

Bayes optimal decision rule for set retrieval

$$d_j$$
 is relevant iff $P(R|d_j,q)>P(\overline{R}|d_j,q)$

- Model the IR problem in a probabilistic framework
- Estimate the probability of document d_j being relevant to the user that that submited the query q
- When considering ranked retrieval, present documents in decreasing order of their estimated probability of relevance



Binary Independence Model (BIM)

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Simplifying assumptions for $P(R|d_i, q)$

- A simple probabilistic model can assume that:
 - probability depends only on query and document
 - there is a subset R of relevant documents
 - index terms are independent
 - 4 non-query terms are equally likely to appear in relevant and non-relevant documents
- Use binary term weights
 - documents and queries as binary term incidence vectors
 - terms not appearing in the query do not affect the ranking



Document Query Similarity

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Generic Document Model

The Boolean Model

Space Model

Probabilistic Models

Comparison of the Different Models As a similarity measure, we can use the ratio between the probability of finding the relevant documents and the probability of finding the non-relevant documents

$$sim(d_j, q) = rac{P(R|\vec{d_j}, \vec{q})}{P(\overline{R}|\vec{d_i}, \vec{q})}$$

• Often refered to as the Retrieval Status Value (RSV)



Similarity Probabilities (1)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Initial Equation

We can simplify the expression leveraging Bayes' theorem and rank equivalence (i.e., remove query-independent constants)

$$\mathit{sim}(\textit{d}_{j},\textit{q}) = \frac{\textit{P}(\textit{R}|\vec{\textit{d}}_{j},\vec{\textit{q}})}{\textit{P}(\overline{\textit{R}}|\vec{\textit{d}}_{j},\vec{\textit{q}})} = \frac{\textit{P}(\vec{\textit{d}}_{j},\vec{\textit{q}}|\textit{R}) \times \textit{P}(\textit{R})}{\textit{P}(\vec{\textit{d}}_{j},\vec{\textit{q}}|\overline{\textit{R}}) \times \textit{P}(\overline{\textit{R}})} \sim \frac{\textit{P}(\vec{\textit{d}}_{j},\vec{\textit{q}}|\textit{R})}{\textit{P}(\vec{\textit{d}}_{j},\vec{\textit{q}}|\overline{\textit{R}})}$$

Assuming term independence...

$$\textit{sim}(\textit{d}_{j},\textit{q}) \sim \frac{(\Pi_{\textit{g}_{i}(\vec{d}_{j}) = \textit{g}_{i}(\vec{q}) = 1}P(k_{i}|R)) \times (\Pi_{\textit{g}_{i}(\vec{d}_{j}) = 0 \land \textit{g}_{i}(\vec{q}) = 1}P(\overline{k_{i}}|R))}{(\Pi_{\textit{g}_{i}(\vec{d}_{i}) = \textit{g}_{i}(\vec{q}) = 1}P(k_{i}|\overline{R})) \times (\Pi_{\textit{g}_{i}(\vec{d}_{i}) = 0 \land \textit{g}_{i}(\vec{q}) = 1}P(\overline{k_{i}}|\overline{R}))}$$



Similarity Probabilities (2)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Taking logs and removing constant factors...

$$\textit{sim}(d_j,q) = \sum_{i=1}^t w_{i,q} \times w_{i,j} \times \left(\log \frac{P(k_i|R)}{1 - P(k_i|R)} + \log \frac{1 - P(k_i|\overline{R})}{P(k_i|\overline{R})}\right)$$

Blind assumptions

$$P(k_i|R) = 0.5$$

$$P(k_i|\overline{R}) = \frac{n_i}{N}$$

- $P(k_i|R)$ reflects that we have no information about relevant documents (i.e., each query term is equally likely to occur in a relevant document)
- $P(k_i|\overline{R})$ reflects a much smaller number of relevant documents than the collection size



Similarity Probabilities (3)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector

Probabilistic Models

Comparison of the Different Models

After document retrieval or leveraging training data...

- Let V be the number of returned documents (i.e., number of documents estimated to be relevant)
- Let V_i be the number of returned docs with term k_i

$$P(k_i|R) = \frac{V_i}{V} P(k_i|\overline{R}) = \frac{n_i - V_i}{N - V}$$



Similarity Probabilities (4)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Avoiding small values when using blind assumptions...

- With zero counts probability is not well-defined
- Maximum likelihood estimates do not work for rare events
- To avoid zeros add 0.5 to each count (expected likelihood estimation) or use a different type of smoothing

$$P(k_i|R) = 0.5$$

$$P(k_i|\overline{R}) = \frac{n_i + 0.5}{N+1}$$

Avoiding small values with estimates after retrieval...

$$P(k_i|R) = \frac{V_i + \frac{n_i}{N}}{V+1}$$

$$P(k_i|\overline{R}) = \frac{n_i - V_i + \frac{n_i}{N}}{N-V+1}$$



Problems of this Simple Probabilistic Model

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

- There is no accurate estimate for the first run probabilities
- Index terms are not weighted
- Terms are assumed mutually independent

In fact, many different probabilistic retrieval models have been proposed, some addressing the aforementioned limitations!



Another Look at the BIM (1)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

Recall the log odds ratio for computing RSV

$$\mathit{sim}(d_j,q) = \sum_{i=1}^t w_{i,q} \times w_{i,j} \times \left(\log \frac{P(k_i|R)}{1 - P(k_i|R)} + \log \frac{1 - P(k_i|\overline{R})}{P(k_i|\overline{R})}\right)$$

Denoting $p_i = P(k_i|R)$ and $u_i = P(k_i|\overline{R})$

$$sim(d_j, q) = \sum_{i=1}^t w_{i,q} \times w_{i,j} \times \left(\log \frac{p_i}{1 - p_i} + \log \frac{1 - u_i}{u_i}\right)$$



Another Look at the BIM (2)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

With the blind estimates, does the equation look familiar?

$$P(k_i|R)=p_i=0.5$$

$$P(k_i|\overline{R})=u_i=\frac{n_i}{N}$$

Replacing p_i and u_i in the previous equation...

$$\log \frac{p_i}{1 - p_i} = 0$$

$$\log \frac{1 - u_i}{u_i} = \log \frac{N - n_i}{n_i} \approx \log \left(\frac{\mathbf{N}}{\mathbf{n}_i}\right)$$



Another Look at the BIM (3)

Processamento e Recuperação de Informação

Generic Document Model

Model

The Boolean The Vector Space Model

Probabilistic Models

Comparison of the Different Models

- The BIM can be seen as TF-IDF with binary term frequencies and logarithmically dampened inverse document frequencies
- The score for document d_i is just IDF weighting of the guery terms present in the document

$$sim(d_j, q) = \sum_{i=1}^{t} w_{i,q} \times w_{i,j} \times \log\left(\frac{N}{n_i}\right)$$

Alternative formulation using smoothing

$$sim(d_j, q) = \sum_{i=1}^{t} w_{i,q} \times w_{i,j} \times \log\left(\frac{N - n_i + 0.5}{n_i + 0.5}\right)$$



The Okapi BM25 Model (1)

Processamento e Recuperação de Informação

Generic Document Model The Boolean

Model

The Vector Space Model

Probabilistic Models

- Inspired by the BIM probabilistic formulation
- Considering an alternative for term weighting
- Captures various aspects in a simple formula, tuning each component
 - Inverse Document Frequency (IDF)
 - Term Frequncy (TF)
 - Document length
 - Query term fequency (in some formulations)
- BM25 (BestMatch25) is an effective and widely used model for full-text retrieval over large collections



The Okapi BM25 Model (2)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

The BM25 Model

$$TF_{i,j} = \frac{f_{i,j} \times (k_1 + 1)}{f_{i,j} + k_1 \times \left(1 - b + b \frac{|d_j|}{avgdl}\right)}$$

$$IDF_i = \log \frac{N - n_i + 0.5}{n_i + 0.5}$$

$$sim(d_j, q) = \sum IDF_i \times TF_{i,j}$$

- Postulates Poisson (or 2-Poisson-mixture) distributions for terms, instead of Binomial distributions as in BIM
- Parameters k_1 and b need to be tuned
 - ullet k_1 controls impact of term frequency
 - b controls impact of document length
 - Setting $k_1 = 1.5$ and b = 0.75 are common defaults



Extending BM25 to Consider Document Fields

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models

- Textual data often found in some sort of structural form
- Retrieval effectiveness can be improved by taking the structure into account
- Simple solution: calculate score for each field and combine the different fields linearly

$$sim(d_j, q) = \sum_{z \in F} \alpha^z \times sim(d_j^z, q)$$

Problems of linear combination

- With similarities per field, IDF can vary highly in different fields (e.g. stopwords scoring highly in the title)
- TF usually non-linear and information gained by observing a term for the first time is greater than observing subsequent occurrences



BM25F and Combining Term Frequencies

Processamento e Recuperação de Informação

Generic Document Model

The Boolean

The Vector

Probabilistic Models

$$\begin{aligned} TF_{i,j} &= \sum_{z \in F} \alpha^z \times \frac{f_{i,j}^z \times (k_1 + 1)}{f_{i,j}^z + k_1 \times \left(1 - b^z + b^z \frac{|d_j^z|}{avgdl^z}\right)} \\ IDF_i &= \log \frac{N - n_i + 0.5}{n_i + 0.5} \\ sim(d_j, q) &= \sum_{i \in q} IDF_i \times TF_{i,j} \end{aligned}$$



Probabilistic Language Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Another simple probabilistic retrieval formulation
- Each document d is treated as (the basis for) a probabilistic language model
- Given a query q rank documents based on P(d|q)

$$P(d|q) = \frac{P(d) \times P(q|d)}{P(q)}$$

- The evidence P(q) is the same for all documents, so ignore
- *P*(*d*) is the prior
 - ullet often treated as the same for all d
 - we can give a higher prior to "high-quality" documents (e.g., those with high PageRank – to be seen latter)
- P(q|d) is likelihood, i.e. the probability of q given d



How to compute P(q|d)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

Space Model

Probabilistic Models

Comparison of the Different Models Conditional independence assumption

$$P(q|d) = P(\lbrace t_1, \dots, t_{|q|} \rbrace | d) = \prod_{1 < i < |q|} P(t_i|d)$$

- |q| is length of q
- t_i is the token occurring at position i in q
- The above multinomial model is equivalent to:

$$P(q|d) = \prod_{ ext{distinct term } t \in q} P(t|d)^{TF_{t,q}}$$

- Component $TF_{t,q}$ is the term frequency of t in q
- lacktriangle Parameters P(t|d) computed through maximum likelihood estimates

$$P(t|d) = \frac{TF_{t,d}}{|d|}$$



Types of Language Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Different Models The unigram language model (show before)

$$P(d) = P(t_1t_2t_3...) = P(t_1)P(t_2)P(t_3)...$$

n-gram language models (e.g. bigram language models)

$$P(d) = P(t_1t_2t_3...) = P(t_1)P(t_2|t_1)P(t_3|t_2)...$$

- More complex langue models, e.g. using probabilistic context-free grammars
 - Used for tasks like speech recognition, spelling correction, and machine translation



LM Retrieval and Naïve Bayes

Processamento e Recuperação de Informação

Generic Document Model

Model

The Boolean The Vector

Space Model Probabilistic

Models

Comparison of the Different Models

The next class will introduce a simple probabilistic document classifyer, known as the Naïve Bayes approach

- We want to classify document d. We want to classify a query q
- Human-defined classes: e.g., politics, economics, sports. Each document in the collection is a different class
- Assume that d was produced by the generative model. Assume that a was generated by a generative model
- Which of the classes (= class models) is most likely to have generated the document d? Which document (=class) is most likely to have generated the query q?
- For which class do we have the most evidence? For which document (as source for query) do we have the most evidence?



More on computing P(q|d)

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Comparison of

Comparison of the Different Models

Problems with the aforementioned unigram model

$$P(q|d) = P(\{t_1, \ldots, t_{|q|}\}|d) = \prod_{1 < i < |q|} P(t_i|d)$$

- A document with a single missing query-term will receive a score of zero (similar to Boolean AND)
- Where is the equivalent of the IDF?

Linear interpolation smoothing

$$P(q|d) = \prod_{1 < =i < =|q|} (\alpha \times P(t_i|d)) \times ((1 - \alpha) \times P(t_i|c))$$



Query Likelihood Retrieval with Linear Interpolation Smoothing

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- Helps us avoid zero-probabilities
- Another added benefit...
 - Without smoothing, the query-likelihood model ignores how frequently the term occurs in general
 - Linear interpolation smoothing also introduces an IDF-like scoring of documents



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- 3 The Vector Space Model
- Probabilistic Models
- **5** Comparison of the Different Models



What makes these Models Work?

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Comparison of the Different Models

Three main term weighting normalization driving features:

- TF Term Frequency
- IDF Inverse Document Frequency
- DL Document Length



Comparison of the Different Models

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Probabilistic Models

- Boolean model is considered the weakest
- There is some controversy over which shows better performance: vector space or probabilistic
 - Simple BIM is just IDF weighting of the terms
 - BIM originally designed for short catalog records of fairly consistent length, working reasonably in these contexts
 - BM25 or language models offer a better performance (e.g., paying attention to term frequency and document length)
- Nowadays, BM25 is perhaps the most widely used



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Comparison of the Different Models Questions?