Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Processamento e Recuperação de Informação

Information Retrieval Models

Departamento de Engenharia Informática
Instituto Superior Técnico

1º Semestre
2018/2019

Outline

1. Generic Document Model
2. The Boolean Model
3. The Vector Space Model
4. Probabilistic Models
5. Comparison of the Classic Models

Bibliography

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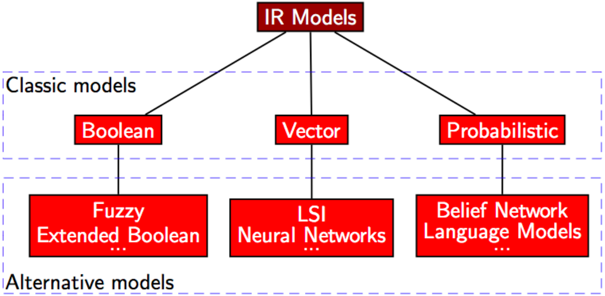
Retrieval Models



Index Terms

In the classic IR models, documents are represented by index terms

- full text/selected keywords
- structure/no structure

Not all terms are equally useful

- index terms can be weighted

We assume that terms are mutually independent

- this is, of course, a simplification

Definition of a Document Model

Definition

Let t be the number of index terms in the collection of documents, and let k_i be a generic index term.

- $K = \{k_1, \ldots, k_t\}$ is the set of all index terms.
- A weight $w_{i,j} \geq 0$ is associated with each index term k_i of a document d_j.
- For an index term which does not appear in the document text, $w_{i,j} = 0$.
- Each document d_j is associated a term vector $\vec{d_j}$, represented by $\vec{d_j} = (w_{1,j}, w_{2,j}, \ldots, w_{t,j})$.
- Function $g_i(\vec{d_j})$ returns the weight of index term k_i in vector $\vec{d_j}$.

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Boolean Model Queries

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- Follows Boolean algebra syntax and semantics
- Term weights are binary
  - $w_{i,j} \in \{0, 1\}$
  - $w_{i,j} = 1$ — term present,
  - $w_{i,j} = 0$ — term not present
- Queries are Boolean expressions
  - E.g., $q = k_a \wedge (k_b \vee \neg k_c)$
- Documents are considered relevant if the query evaluates to *1* (true)

An Example

d_1

That government is best which governs least

d_2

That government is best which governs not at all

d_3

When men are prepared for it, that will be the kind of government which they will have

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$q = \text{government} \wedge \text{best}$

answer: d_1, d_2

An Example

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answer: d_1

An Example

d_1

That government is best which governs least

d_2

That government is best which governs not at all

d_3

When men are prepared for it, that will be the kind of government which they will have

$q =$ government $\wedge$ best

answer: d_1, d_2

$q =$ government $\wedge$ best $\wedge \neg$ all

answer: d_1

$q =$ government $\vee$ best $\wedge \neg$ all

answer: d_1, d_2, d_3

Document-Query Similarity

- Queries can be translated to a disjunction of conjunctive vectors

$$\vec{q} = k_a \wedge (k_b \vee \neg k_c) \Leftrightarrow (1,1,1) \vee (1,1,0) \vee (1,0,0)$$

each tuple corresponds to a vector (k_a, k_b, k_c)

- Similarity of a document to a query is defined as:

$$sim(d_j, q) = \begin{cases} 1 & \text{if } \exists \vec{q_c} \in \vec{q} | \forall_i, g_i(\vec{d_j}) = g_i(\vec{q_c}) \\ 0 & \text{otherwise} \end{cases}$$

The Boolean Model

Why is it good?

- Simple model based on Boolean algebra
- Intuitive concept
- Precise semantics
- Clear formal basis
- Widely adopted by early information systems

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Limitations:

- Retrieval based only on binary decisions
  - More similar to *data retrieval* than *information retrieval*
  - Can retrieve too many, or too little documents
  - Some documents may be more relevant than others
- How do you translate a query to a Boolean expression?
  - Non-expert users may not be able to represent their information needs using Boolean expressions
- Terms are all equally important
  - Index term weighting can bring great improvements in performance

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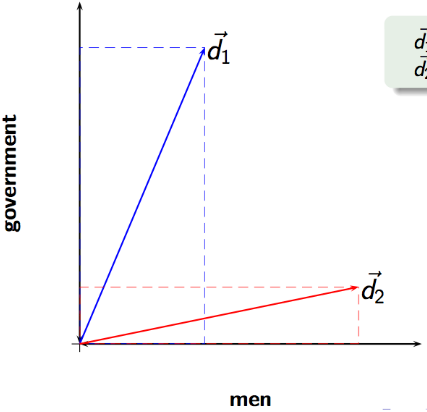
Documents as Vectors

- Documents are represented as vectors
  - $\vec{d}_j = (w_{1,j}, w_{2,j}, \ldots, w_{t,j})$
  - $w_{i,j}$ is the weight of term i in document j
- Queries are also vectors
  - $\vec{q} = (w_{1,q}, w_{2,q}, \ldots, w_{t,q})$
- Vector operations can be used to compare queries$\times$documents (or documents$\times$documents)

An Example



$$\vec{d}_1 = (2.2, 5.2)$$
$$\vec{d}_2 = (4.9, 1.0)$$

Defining Document Vectors

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Two questions are still unanswered:

1. How do we define term weights?
2. How do we compare documents to queries?

Defining Term Weights — TF

Term frequency

Term frequency is a measure of term importance within a document

Definition

Let N be the total number of documents in the system and n_i be the number of documents in which term k_i appears. The normalized frequency of a term k_i in document d_j is given by:

$$f_{i,j} = \frac{freq_{i,j}}{\max_l freq_{l,j}}$$

where $freq_{i,j}$ is the number of occurrences of term k_i in document d_j.

Defining Term Weights — IDF

(Inverse) Document frequency

Document frequency is a measure of term importance within a collection

Definition

The inverse document frequency of a term k_i is given by:

$$idf_i = \log\left(\frac{N}{n_i}\right)$$

Defining Term Weights — TF-IDF

Definition

The weight of a term k_i in document d_j for the vector space model is given by the tf-idf formula:

$$w_{i,j} = f_{i,j} \times \log\left(\frac{N}{n_i}\right)$$

Components of TF-IDF

Different TF-IDF formulations consider alternative approaches for attenuating the TF and IDF components, and also for normalizing the resulting vectors.

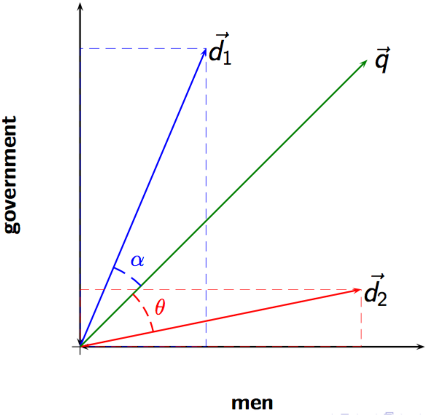
Term frequency		Document frequency		Normalization	
n (natural)	$\mathrm{tf}_{t,d}$	n (no)	1	n (none)	1
l (logarithm)	$1 + \log(\mathrm{tf}_{t,d})$	t (idf)	$\log \frac{N}{\mathrm{df}_t}$	c (cosine)	$\frac{1}{\sqrt{w_1^2 + w_2^2 + \ldots + w_M^2}}$
a (augmented)	$0.5 + \frac{0.5 \times \mathrm{tf}_{t,d}}{\max_t(\mathrm{tf}_{t,d})}$	p (prob idf)	$\max\{0, \log \frac{N - \mathrm{df}_t}{\mathrm{df}_t}\}$	u (pivoted unique)	$1/u$
b (boolean)	$\begin{cases} 1 & \text{if } \mathrm{tf}_{t,d} > 0 \\ 0 & \text{otherwise} \end{cases}$			b (byte size)	$1/\mathit{CharLength}^{\alpha}$, $\alpha < 1$
L (log ave)	$\frac{1 + \log(\mathrm{tf}_{t,d})}{1 + \log(\mathrm{ave}_{t \in d}(\mathrm{tf}_{t,d}))}$				

Document Similarity

- Similarity between documents and queries is a measure of the correlation between their vectors
- Documents/queries that share the same terms, with similar weights, should be more similar
- Thus, as similarity measure, we use the cosine of the angle between the vectors

$$sim(d_j, q) = \frac{\vec{d_j} \cdot \vec{q}}{|\vec{d_j}| \times |\vec{q}|} = \frac{\sum_{i=1}^{t} w_{i,j} \times w_{i,q}}{\sqrt{\sum_{i=1}^{t} w_{i,j}^2} \times \sqrt{\sum_{i=1}^{t} w_{i,q}^2}}$$

An Example



$\cos(\alpha) = 0.9$

$\cos(\theta) = 0.8$

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Why is it so good?

- Simple model, based on linear algebra
- Term weights are not binary
- Allows computing a continuous degree of similarity between queries and documents
- Thus, allows ranking documents according to their possible relevance

Improving the VSM (1)

The BM25 Model

Consider not only the term frequency and inverse document frequency heuristics, but also the document length as a normalization factor for the term frequency.

$$TF_{i,j} = \frac{f_{i,j} \times (k_1 + 1)}{f_{i,j} + k_1 \times \left(1 - b + b\frac{|d_j|}{avgdl}\right)}$$

$$IDF_i = \log \frac{N - n_i + 0.5}{n_i + 0.5}$$

$$sim(d_j, q) = \sum_{i \in q} IDF_i \times TF_{i,j}$$

To be detailed in the next lecture

Improving the VSM (2)

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Latent Semantic Indexing

- Find a low-rank approximation of the matrix which describes the occurrences of terms in documents
  - Singular Value Decomposition
  - Compare the documents in the low-dimensional space
- The consequence of the rank lowering is that some dimensions are combined (e.g., mitigates the problem of identifying synonymy)
- To be detailed latter in the course

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Probabilistic Models

- Model the IR problem in a probabilistic framework
- Estimate the probability of document d_j being relevant to the user
- A simple probabilistic model can assume that:
  1. the probability depends only on the query and the document
  2. there is a subset R of relevant documents
  3. index terms are independent
- A simple probabilistic model can use binary term weights

Document Query Similarity

- As a similarity measure, we use the ratio between the probability of finding the relevant documents and the probability of finding the non-relevant documents

$$sim(d_j, q) = \frac{P(R|\vec{d_j})}{P(\overline{R}|\vec{d_j})}$$

Similarity Probabilities (1)

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Initial Equation

$$sim(d_j, q) = \frac{P(R|\vec{d_j})}{P(\overline{R}|\vec{d_j})} = \frac{P(\vec{d_j}|R) \times P(R)}{P(\vec{d_j}|\overline{R}) \times P(\overline{R})} \sim \frac{P(\vec{d_j}|R)}{P(\vec{d_j}|\overline{R})}$$

Assuming term independence...

$$sim(d_j, q) \sim \frac{(\prod_{g_i(\vec{d_j})=1} P(k_i|R)) \times (\prod_{g_i(\vec{d_j})=0} P(\overline{k_i}|R))}{(\prod_{g_i(\vec{d_j})=1} P(k_i|\overline{R})) \times (\prod_{g_i(\vec{d_j})=0} P(\overline{k_i}|\overline{R}))}$$

Tanking logs and removing constant factors...

$$sim(d_j, q) = \sum_{i=1}^{t} w_{i,q} \times w_{i,j} \times \left(\log \frac{P(k_i|R)}{1 - P(k_i|R)} + \log \frac{1 - P(k_i|\overline{R})}{P(k_i|\overline{R})} \right)$$

Similarity Probabilities (2)

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Blind assumptions

$$\begin{aligned} P(k_i|R) &= 0.5 \\ P(k_i|\overline{R}) &= \frac{n_i}{N} \end{aligned}$$

After document retrieval...

Let V be the number of returned documents; let V_i be the number of returned documents containing term k_i.

$$\begin{aligned} P(k_i|R) &= \frac{V_i}{V} \\ P(k_i|\overline{R}) &= \frac{n_i - V_i}{N - V} \end{aligned}$$

Similarity Probabilities (3)

Avoiding small values...

$$
\begin{aligned}
P(k_i|R) &= \frac{V_i + \frac{n_i}{N}}{V+1} \\
P(k_i|\overline{R}) &= \frac{n_i - V_i + \frac{n_i}{N}}{N - V + 1}
\end{aligned}
$$

Problems of this Simple Probabilistic Model

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- There is no accurate estimate for the first run probabilities
- Index terms are not weighted
- Terms are assumed mutually independent

- In fact, many different probabilistic retrieval models have been proposed!

Probabilistic Language Models

- Another simple probabilistic retrieval model
- Each document d is treated as (the basis for) a probabilistic language model
- Given a query q rank documents based on $P(d|q)$

$$P(d|q) = \frac{P(d) \times P(q|d)}{P(q)}$$

- The evidence $P(q)$ is the same for all documents, so ignore
- $P(d)$ is the prior
  - often treated as the same for all d
  - we can give a higher prior to "high-quality" documents (e.g., those with high PageRank – to be seen latter)
- $P(q|d)$ is likelihood, i.e. the probability of q given d

How to compute $P(q|d)$

- Conditional independence assumption

$$P(q|d) = P(\{t_1, \ldots, t_{|q|}\}|d) = \prod_{1<=i<=|q|} P(t_k|d)$$

- $|q|$ is length of q
- t_k is the token occurring at position k in q

- The above multinomial model is equivalent to:

$$P(q|d) = \prod_{\text{distinct term } t \in q} P(t_k|d)^{TF_{t,q}}$$

- Component $TF_{t,q}$ is the term frequency of t in q
- Parameters $P(t_k|d)$ computed through maximum likelihood estimates

$$P(t_k|d) = \frac{TF_{t_k,d}}{|d|}$$

LM Retrieval and Naïve Bayes

The next class will introduce a simple probabilistic document classifyer, known as the Naïve Bayes approach

- We want to classify document d.
  We want to classify a query q
- Human-defined classes: e.g., politics, economics, sports.
  Each document in the collection is a different class
- Assume that d was produced by the generative model.
  Assume that q was generated by a generative model
- Which of the classes (= class models) is most likely to have generated the document d?
  Which document (=class) is most likely to have generated the query q?
- For which class do we have the most evidence?
  For which document (as source for query) do we have the most evidence?

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What makes these Models Work?

Three main term weighting normalization driving features:

- TF - Term Frequency
- IDF - Inverse Document Frequency
- DL - Document Length

Comparison of the Classic Models

- Boolean model is considered the weakest
- There is some controversy over which shows better performance: vector space or probabilistic
- However, nowadays, the vector space model is the most widely used

Questions?