

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Processamento e Recuperação de Informação Information Retrieval Models

Departamento de Engenharia Informática Instituto Superior Técnico

1^o Semestre 2018/2019



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- 3 The Vector Space Model
- Probabilistic Models
- **6** Comparison of the Classic Models



Bibliography

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic

Models

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Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

Space Model
Probabilistic
Models

Comparison of the Classic

Models

- Generic Document Model
 - 2 The Boolean Model
 - 3 The Vector Space Model
 - 4 Probabilistic Models
- **6** Comparison of the Classic Models



Retrieval Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean

The Vector Space Model

Probabilistic Models





Index Terms

Processamento e Recuperação de Informação

Generic
Document
Model
The Boolean

Model

Models

Models

The Vector

Space Model
Probabilistic

Comparison of the Classic

In the classic IR models, documents are represented by index terms

- full text/selected keywords
- structure/no structure

Not all terms are equally useful

• index terms can be weighted

We assume that terms are mutually independent

• this is, of course, a simplification



Definition of a Document Model

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Definition

Let t be the number of index terms in the collection of documents, and let k_i be a generic index term.

- $K = \{k_1, \dots, k_t\}$ is the set of all index terms.
- A weight $w_{i,j} \ge 0$ is associated with each index term k_i of a document d_j .
- For an index term which does not appear in the document text, $w_{i,j} = 0$.
- Each document d_j is associated a term vector $\vec{d_j}$, represented by $\vec{d_i} = (w_{1,j}, w_{2,j}, \dots, w_{t,j})$.
- Function $g_i(\vec{d_j})$ returns the weight of index term k_i in vector $\vec{d_i}$.



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- The Vector Space Mode
- Probabilistic Models
- **(5)** Comparison of the Classic Models



Boolean Model Queries

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models Follows Boolean algebra syntax and semantics

Term weights are binary

•
$$w_{i,j} \in \{0,1\}$$

•
$$w_{i,j} = 1$$
 — term present,

•
$$w_{i,j} = 0$$
 — term not present

Queries are Boolean expressions

• E.g.,
$$q = k_a \wedge (k_b \vee \neg k_c)$$

 Documents are considered relevant if the query evaluates to 1 (true)



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

d_1

That government is best which governs least

d_2

That government is best which governs not at all

d_3

When men are prepared for it, that will be the kind of government which they will have



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models d_1

That government is best which governs least

 d_2

That government is best which governs not at all

 d_3

When men are prepared for it, that will be the kind of government which they will have $q = \mathsf{government} \land \mathsf{best}$

answer: d_1, d_2



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models d_1

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answer: d_1, d_2

 $q = \mathsf{government} \land \mathsf{best} \land \neg \mathsf{all}$

answer: d_1



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

d_1

That government is best which governs least

d_2

That government is best which governs not at all

d_3

When men are prepared for it, that will be the kind of government which they will have $q = \mathsf{government} \land \mathsf{best}$

answer: d_1, d_2

 $q = \mathsf{government} \land \mathsf{best} \land \neg \mathsf{all}$

answer: d_1

 $q = \mathsf{government} \lor \mathsf{best} \land \neg \mathsf{all}$

answer: d_1, d_2, d_3



Document-Query Similarity

Processamento e Recuperação de Informação

Document Model

Generic

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models Queries can be translated to a disjunction of conjunctive vectors

$$\vec{q} = k_a \wedge (k_b \vee \neg k_c) \Leftrightarrow (1, 1, 1) \vee (1, 1, 0) \vee (1, 0, 0)$$

each tuple corresponds to a vector (k_a, k_b, k_c)

Similarity of a document to a query is defined as:

$$\mathit{sim}(d_j,q) = \left\{ egin{array}{ll} 1 & ext{if } \exists \vec{q_c} \in \vec{q} | \forall_i, g_i(\vec{d_j}) = g_i(\vec{q_c}) \\ 0 & ext{otherwise} \end{array} \right.$$



The Boolean Model

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Why is it good?

- Simple model based on Boolean algebra
- Intuitive concept
- Precise semantics
- Clear formal basis
- Widely adopted by early information systems



Boolean Model

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Limitations:

- Retrieval based only on binary decisions
 - More similar to data retrieval than information retrieval
 - Can retrieve too many, or too little documents
 - Some documents may be more relevant than others
- How do you translate a query to a Boolean expression?
 - Non-expert users may not be able to represent their information needs using Boolean expressions
- Terms are all equally important
 - Index term weighting can bring great improvements in performance



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- The Vector Space Model
- Probabilistic Models
- 6 Comparison of the Classic Models



Documents as Vectors

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models Documents are represented as vectors

•
$$\vec{d}_j = (w_{1,j}, w_{2,j}, \dots, w_{t,j})$$

- $w_{i,j}$ is the weight of term i in document j
- Queries are also vectors

•
$$\vec{q} = (w_{1,q}, w_{2,q}, \dots, w_{t,q})$$

 Vector operations can be used to compare queries×documents (or documents×documents)



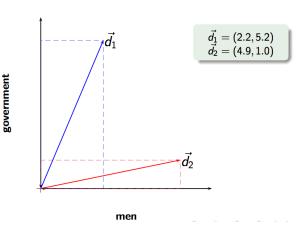
Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models





Defining Document Vectors

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Two questions are still unanswered:

- How do we define term weights?
- We have do we compare documents to queries?



Defining Term Weights — TF

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Term frequency

Term frequency is a measure of term importance within a document

Definition

Let N be the total number of documents in the system and n_i be the number of documents in which term k_i appears. The normalized frequency of a term k_i in document d_i is given by:

$$f_{i,j} = \frac{freq_{i,j}}{\max_{l} freq_{l,j}}$$

where $freq_{i,j}$ is the number of occurrences of term k_i in document d_i .



Defining Term Weights — IDF

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

(Inverse) Document frequency

Document frequency is a measure of term importance within a collection

Definition

The inverse document frequency of a term k_i is given by:

$$idf_i = \log\left(\frac{N}{n_i}\right)$$



Defining Term Weights — TF-IDF

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Definition

The weight of a term k_i in document d_j for the vector space model is given by the tf-idf formula:

$$w_{i,j} = f_{i,j} \times \log\left(\frac{N}{n_i}\right)$$



Components of TF-IDF

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models Different TF-IDF formulations consider alternative approaches for attenuating the TF and IDF components, and also for normalizing the resulting vectors.

Term frequency		Document frequency		Normalization	
n (natural)	$tf_{t,d}$	n (no)	1	n (none)	1
I (logarithm)	$1 + \log(tf_{t,d})$	t (idf)	$\log \frac{N}{\mathrm{df}_z}$	c (cosine)	$\frac{1}{\sqrt{w_1^2+w_2^2++w_M^2}}$
a (augmented)	$0.5 + \frac{0.5 \times tf_{t,d}}{max_t(tf_{t,d})}$	p (prob idf)	$max\{0, log \tfrac{\mathit{N}-\mathrm{df}_t}{\mathrm{df}_t}\}$	u (pivoted unique)	1/u
b (boolean)	$\begin{cases} 1 & \text{if } \operatorname{tf}_{t,d} > 0 \\ 0 & \text{otherwise} \end{cases}$			b (byte size)	$1/\mathit{CharLength}^{lpha}, \ lpha < 1$
L (log ave)	$\frac{1 + \log(tf_{t,d})}{1 + \log(ave_{t \in d}(tf_{t,d}))}$				



Document Similarity

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Similarity between documents and queries is a measure of the correlation between their vectors
- Documents/queries that share the same terms, with similar weights, should be more similar
- Thus, as similarity measure, we use the cosine of the angle between the vectors

$$\mathit{sim}(d_j,q) = \frac{\vec{d_j} \cdot \vec{q}}{|\vec{d_j}| \times |\vec{q}|} = \frac{\sum_{i=1}^t w_{i,j} \times w_{i,q}}{\sqrt{\sum_{i=1}^t w_{i,j}^2} \times \sqrt{\sum_{i=1}^t w_{i,q}^2}}$$



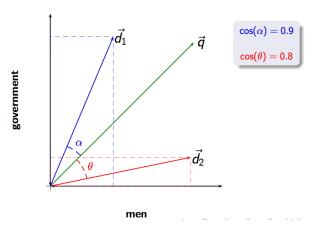
Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models





The Vector Space Model

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

Space Model

Probabilistic Models

Comparison of the Classic Models

Why is it so good?

- Simple model, based on linear algebra
- Term weights are not binary
- Allows computing a continuous degree of similarity between queries and documents
- Thus, allows ranking documents according to their possible relevance



Improving the VSM (1)

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

The BM25 Model

Consider not only the term frequency and inverse document frequency heuristics, but also the document length as a normalization factor for the term frequency.

$$TF_{i,j} = rac{f_{i,j} imes (k_1+1)}{f_{i,j} + k_1 imes \left(1 - b + b rac{|d_j|}{avgdl}
ight)}$$
 $IDF_i = \log rac{N - n_i + 0.5}{n_i + 0.5}$
 $sim(d_j, q) = \sum_{i \in q} IDF_i imes TF_{i,j}$

To be detailed in the next lecture



Improving the VSM (2)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Latent Semantic Indexing

- Find a low-rank approximation of the matrix which describes the occurrences of terms in documents
 - Singular Value Decomposition
 - Compare the documents in the low-dimensional space
- The consequence of the rank lowering is that some dimensions are combined (e.g., mitigates the problem of identifying synonymy)
- To be detailed latter in the course



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Generic Document Model
 - 2 The Boolean Model
- 3 The Vector Space Model
- Probabilistic Models
- **6** Comparison of the Classic Models



Probabilistic Models for IR

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

Space Model

Probabilistic Models

Comparison of the Classic Models TF-IDF and VSM produce sufficiently good results in practice but often criticized for being too ad-hoc or not principled.

- Typically outperformed by probabilistic retrieval models and statistical language models in IR benchmarks (e.g., TREC)
- Probabilistic retrieval models
 - use generative models of documents as bags-of-words
 - ullet explicitly model probability of relevance P[R |d, q]
 - provide a probabilistic justification for TF-IDF-like approaches
- Statistical language models
 - use generative models of documents and queries as sequences-of-words
 - consider likelihood of generating query from document model or divergence of document model and query model (e.g., Kullback-Leibler)



Probabilistic Retrieval Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

- Model the IR problem in a probabilistic framework
- Estimate the probability of document d_j being relevant to the user
- Bayes optimal decision rule for set retrieval

$$d_j$$
is relevant iff $P(R|ec{d_j},ec{q}) > P(\overline{R}|ec{d_j},ec{q})$

 When considering ranked retrieval, present documents in decreasing order of their estimated probability of relevance



Binary Independence Model (BIM)

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Simplifying assumptions to make modeling $P(R|\vec{d}_j, \vec{q})$ feasible
- A simple probabilistic model can assume that:
 - the probability depends only on the query and the document
 - there is a subset R of relevant documents
 - index terms are independent
 - non-query terms are equally likely to appear in relevant and non-relevant documents
- A simple probabilistic model can use binary term weights
 - documents and queries as binary term incidence vectors
 - terms not appearing in the query do not affect the ranking



Document Query Similarity

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector

Probabilistic Models

Comparison of the Classic Models As a similarity measure, we use the ratio between the probability of finding the relevant documents and the probability of finding the non-relevant documents

$$sim(d_j,q) = rac{P(R|ec{d_j},ec{q})}{P(\overline{R}|ec{d_i},ec{q})}$$



Similarity Probabilities (1)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

Space Model

Probabilistic Models

Comparison of the Classic Models

Initial Equation

$$sim(d_j,q) = \frac{P(R|\vec{d_j})}{P(\overline{R}|\vec{d_j})} = \frac{P(\vec{d_j}|R) \times P(R)}{P(\vec{d_j}|\overline{R}) \times P(\overline{R})} \sim \frac{P(\vec{d_j}|R)}{P(\vec{d_j}|\overline{R})}$$

Assuming term independence...

$$\mathit{sim}(d_j,q) \sim rac{(\prod_{g_i(ec{d_j})=1} P(k_i|R)) imes (\prod_{g_i(ec{d_j})=0} P(\overline{k_i}|R))}{(\prod_{g_i(ec{d_i})=1} P(k_i|\overline{R})) imes (\prod_{g_i(ec{d_i})=0} P(\overline{k_i}|\overline{R}))}$$

Tanking logs and removing constant factors...

$$sim(d_j,q) = \sum_{i=1}^t w_{i,q} imes w_{i,j} imes \left(\log rac{P(k_i|R)}{1 - P(k_i|R)} + \log rac{1 - P(k_i|\overline{R})}{P(k_i|\overline{R})}
ight)$$



Similarity Probabilities (2)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Blind assumptions

$$P(k_i|R) = 0.5$$

$$P(k_i|\overline{R}) = \frac{n_i}{N}$$

After document retrieval...

Let V be the number of returned documents; let V_i be the number of returned documents containing term k_i .

$$P(k_i|R) = \frac{V_i}{V}$$

$$P(k_i|\overline{R}) = \frac{n_i - V_i}{N - V}$$



Similarity Probabilities (3)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models Avoiding small values...

$$P(k_i|R) = \frac{V_i + \frac{n_i}{N}}{V+1}$$

$$P(k_i|\overline{R}) = \frac{n_i - V_i + \frac{n_i}{N}}{N-V+1}$$



Problems of this Simple Probabilistic Model

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- There is no accurate estimate for the first run probabilities
- Index terms are not weighted
- Terms are assumed mutually independent
- In fact, many different probabilistic retrieval models have been proposed!



The Okapi BM25 Model (1)

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Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Inspired by the BIM probabilistic formulation
- Considering an alternative for term weighting
- Captures various aspects in a simple formula, tuning each component
 - Inverse Document Frequency (IDF)
 - Term Frequncy (TF)
 - Document length
 - Query term fequency
- Effective and widely used model



The Okapi BM25 Model (2)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

The BM25 Model

$$TF_{i,j} = \frac{f_{i,j} \times (k_1 + 1)}{f_{i,j} + k_1 \times \left(1 - b + b \frac{|d_j|}{avgdl}\right)}$$

$$IDF_i = \log \frac{N - n_i + 0.5}{n_i + 0.5}$$

$$sim(d_j, q) = \sum_{i \in q} IDF_i \times TF_{i,j}$$



Probabilistic Language Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Another simple probabilistic retrieval model
- Each document d is treated as (the basis for) a probabilistic language model
- Given a query q rank documents based on P(d|q)

$$P(d|q) = \frac{P(d) \times P(q|d)}{P(q)}$$

- The evidence P(q) is the same for all documents, so ignore
- *P*(*d*) is the prior
 - often treated as the same for all d
 - we can give a higher prior to "high-quality" documents (e.g., those with high PageRank – to be seen latter)
- P(q|d) is likelihood, i.e. the probability of q given d



How to compute P(q|d)

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models Conditional independence assumption

$$P(q|d) = P(\lbrace t_1, \ldots, t_{|q|} \rbrace | d) = \prod_{1 < i < |q|} P(t_k|d)$$

- |q| is length of q
- ullet t_k is the token occurring at position k in q
- The above multinomial model is equivalent to:

$$P(q|d) = \prod_{\substack{ ext{distinct term } t \in q}} P(t_k|d)^{TF_{t,q}}$$

- Component $TF_{t,q}$ is the term frequency of t in q
- ullet Parameters $P(t_k|d)$ computed through maximum likelihood estimates

$$P(t_k|d) = \frac{TF_{t_k,d}}{|d|}$$



LM Retrieval and Naïve Bayes

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Generic Document Model

Model

The Boolean The Vector

Space Model Probabilistic

Models

Comparison of the Classic Models

The next class will introduce a simple probabilistic document classifyer, known as the Naïve Bayes approach

- We want to classify document d. We want to classify a query q
- Human-defined classes: e.g., politics, economics, sports. Each document in the collection is a different class
- Assume that d was produced by the generative model. Assume that a was generated by a generative model
- Which of the classes (= class models) is most likely to have generated the document d? Which document (=class) is most likely to have generated the query q?
- For which class do we have the most evidence? For which document (as source for query) do we have the most evidence?



Outline

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models Generic Document Model

2 The Boolean Model

The Vector Space Mode

Probabilistic Models



What makes these Models Work?

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic

Models

Models

Comparison of the Classic

Three main term weighting normalization driving features:

- TF Term Frequency
- IDF Inverse Document Frequency
- DL Document Length



Comparison of the Classic Models

Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

- Boolean model is considered the weakest
- There is some controversy over which shows better performance: vector space or probabilistic
- However, nowadays, the vector space model is the most widely used



Processamento e Recuperação de Informação

Generic Document Model

The Boolean Model

The Vector Space Model

Probabilistic Models

Comparison of the Classic Models

Questions?