

①

$$y' - 2xy = e^{x^2}$$

homogenni řešení:

$$y' - 2xy = 0$$

$$y' = 2xy$$

→ $y \neq 0$

$$\int \frac{y'}{y} = \int 2x dx$$

$$\ln|y| = x^2 + C$$



$$y_h = e^{x^2} \cdot e^C$$

$$y_h = e^{x^2} D, x \in \mathbb{R}, D \in \mathbb{R}$$

variance:

$$y_p = D(x) \cdot e^{x^2}$$

$$y_p' = D'(x) \cdot e^{x^2} + D(x) \cdot e^{x^2} \cdot 2x$$

$$y_p' - 2xy_p = e^{x^2}$$

$$D'(x) \cdot e^{x^2} + \cancel{D(x) \cdot e^{x^2} \cdot 2x} - \cancel{2x \cdot D(x) \cdot e^{x^2}} = e^{x^2}$$

$$D'(x) \cdot e^{x^2} = e^{x^2}$$

$$D(x) = \int \frac{e^{x^2}}{e^{x^2}} dx = x$$

$$y_p = D(x) \cdot e^{x^2}$$

$$y_p = x \cdot e^{x^2}$$

$$z(x) = z_p + z_h = x \cdot e^{x^2} + e^{x^2} D, D \in \mathbb{R}, x \in \mathbb{R}$$

(2)

$$a) z' = z^4 - z^3$$

$$z' = z^3(z-1)$$

$$\downarrow \quad \downarrow$$

$$z=0 \quad z=1$$



$$(0,1) \rightarrow z' = 1+1=2 \text{ (+)}$$

$$(0, \frac{1}{2}) \rightarrow z' = \frac{1}{32} - \frac{1}{16} \rightarrow \ominus$$

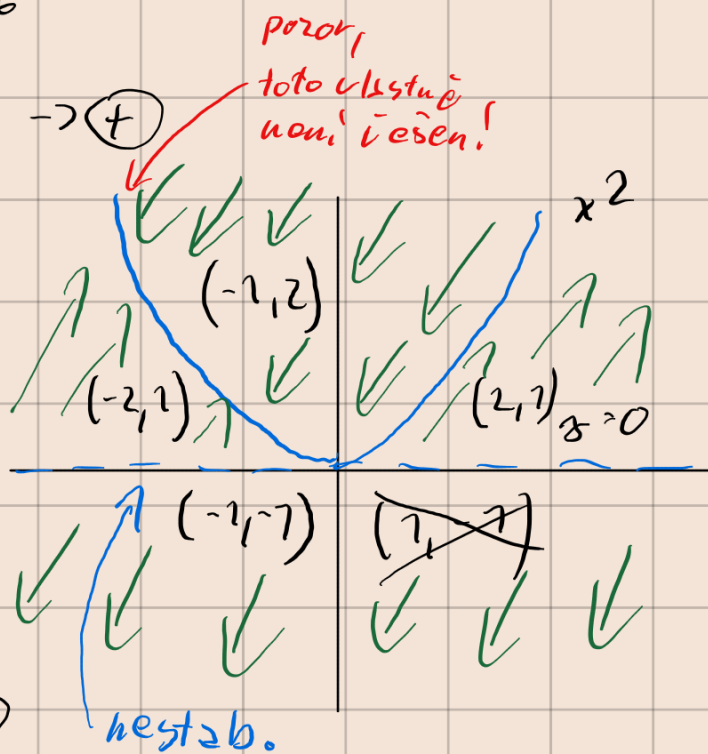
$$(0,2) \rightarrow z' = 32 - 16 \rightarrow \text{(+)}$$

$$b) z' = z(x^2 - z)$$

$$\downarrow \quad \downarrow$$

$$z=0 \quad x^2+z$$

$$z \neq x^2$$



$$(-1,-1) z' = -1(1+1) \rightarrow \ominus$$

$$\text{crossed out } (1,1) z' = -(1+1) \rightarrow \ominus$$

$$(-2,1) z' = 1(4-1) \rightarrow \text{(+)}$$

$$(2,1) z' = 1(4-1) \rightarrow \text{(+)}$$

$$(-1,2) z' = 2(1-2) \rightarrow \ominus$$

