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„Model-based Adjustments for Non-concurrent Comparisons  
in Platform Trials“

verfasst von / submitted by

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Thank you!



# Abstract

This L<sup>A</sup>T<sub>E</sub>X template provides example on how to format and display text, mathematical formulas, and insert tables or images. There is a lot more you can do with L<sup>A</sup>T<sub>E</sub>X, for more information check out <https://en.wikibooks.org/wiki/LaTeX>.



# Kurzfassung

Das ist eine deutsche Kurzfassung meiner in Englisch verfassten Masterarbeit.





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## List of Algorithms





## Listings



# 1. Introduction

## 1.1. Clinical Trials

## 1.2. Platform Trials

## 1.3. State of the Art

## 1.4. Estimands in Platform Trials (?)

## 1.5. Thesis Contribution



## 2. Methods

In Section 2.1, we review current methods for incorporating non-concurrent controls into the analysis of platform trials <sup>and discuss the differences and similarities, as well as their limitations.</sup> These methods include model-based frequentist approaches, the "Time Machine" Bayesian approach and the network meta-analysis approach.

In Section 2.2, we extend the frequentist model approaches for treatment-control comparisons to more complex platform trials than those considered so far. Furthermore, we explore different variants of the models by considering different definitions of the time covariate and ~~the adjustment for this covariate in the model.~~

In Section 2.3 we expand the application of the methods to treatment-treatment comparisons between treatments that do not overlap in the trial, but have common concurrent arms.

*and propose new methods that permit further flexibility in the adj.*

### 2.1. Current Methods for Incorporating Non-concurrent Controls

Consider a platform trial design with  $K$  experimental treatment arms and a shared control group, where the experimental arms enter and leave the trial at different time points. The duration of the trial can then be split into periods, defined as time intervals bounded by any treatment arm either entering or leaving the platform. Moreover, the time can be divided into equidistant discrete units of calendar time.

We denote the experimental treatment arms by  $k$  ( $k = 1, \dots, K$ , ordered by entry time) and the control group by  $k = 0$ . Furthermore, we denote the periods the trial consists of by  $s$  ( $s = 1, \dots, S$ ) and the calendar time units by  $c$  ( $c = 1, \dots, C$ ). The total number of patients in the trial is given by  $N$ . The response for patient  $j$  ( $j = 1, \dots, N$ ) is indicated by  $y_j$ , the arm they were allocated to by  $k_j$  and the period and calendar time corresponding to their entry time by  $s_j$  and  $c_j$ , respectively. The observed time of recruitment of patient  $j$  is given by  $t_j$ .

The focus of this thesis is on continuous endpoints, hence the frequentist model-based approaches will only be discussed in this context. The Bayesian Time Machine, however, has only been proposed for binary endpoints so far and therefore it will be described for this type of endpoints.

#### 2.1.1. Frequentist Model-based Approaches

Focusing on a simple platform trial with  $K = 2$  experimental treatment arms, Lee and Wason [1] investigated linear regression models that allow to include non-concurrent

## 2. Methods

control data to the analysis. In particular, they assumed a trial, which starts with only one treatment arm and the control group. The second treatment arm is added to the trial later on and both treatment arms finish at the same time, so that The resulting trial consists of 2 periods, as illustrated in Fig. 2.1. Moreover, time trends of various strengths and shapes may be present in the trial.

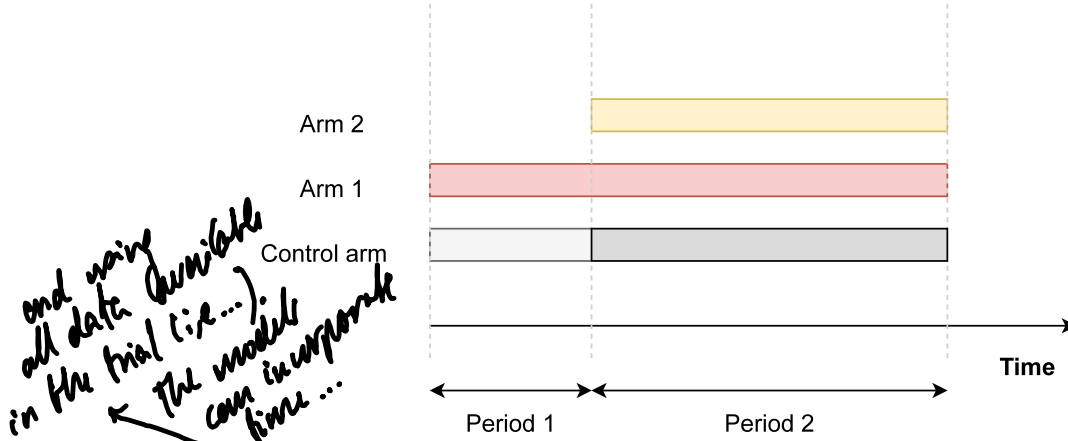


Figure 2.1.: Scheme of the platform trial considered in [1] and [2].

Lee and Wason [1] proposed two linear regression models for evaluating the efficacy of the second treatment arm, which adjust for potential time trends by including the time as a covariate to the model, either in terms of the patient recruitment (given by (2.1)) or the period indicator (given by (2.2)), as follows: *time*

$\epsilon_j \sim N(0, \sigma^2)$

$$y_j = \eta_0 + \sum_{k=1,2} \theta_k \cdot I(k_j = k) + \gamma \cdot j + \epsilon_j \quad (2.1)$$

$$y_j = \eta_0 + \sum_{k=1,2} \theta_k \cdot I(k_j = k) + \tau \cdot I(t_j \in s_2) + \epsilon_j \quad (2.2)$$

where the model intercept  $\eta_0$  is given in terms of the response in the control group in the first period and  $\theta_k$  is the treatment effect for treatment  $k$ . The time effect is estimated by the parameters  $\gamma$  and  $\tau$ . In (2.1),  $\gamma$  represents the effect of continuous recruitment, while in (2.2)  $\tau$  denotes the time effect between period 1 and 2. Note that both models implicitly assume that the time trend is equal across all arms. However, the first model (2.1) assumes that the time trend increases linearly with time, while the second one (2.2) models the time trend as constant in all periods.

Using these models to test the hypothesis  $H_{0,2} : \theta_2 = 0$  against the one-sided alternative  $H_{1,2} : \theta_2 > 0$ , it is shown that both regression models improve the statistical power as compared to the separate analysis and control the type I error, if the functional form of the time trend is correctly specified. Moreover, the model with stepwise adjustment (2.2)

+ eq time trend, + additivity

## 2.1. Current Methods for Incorporating Non-concurrent Controls

maintains the type I error even under misspecification of the functional form of the time trend (e.g., if this is linear instead of stepwise).

Again in the context of trials with 2 treatment arms, these models were further investigated by Bofill Roig et al. [2], demonstrating that the type I error control is only guaranteed if the time trend is equal across all arms and additive in the model scale. If the time trend differs in treatment arm 1, the type I error control for evaluating treatment arm 2 is lost.

I think it would be clearer if you merge this together with the prev. paragraph.

### 2.1.2. Bayesian Time Machine

of equal length

A Bayesian method that adjusts for potential time trend in the platform trial, the Bayesian Time Machine, has been introduced by Saville et al. [3]. The Time Machine uses the division of the trial into **equidistant calendar time intervals** ("buckets"), which are indexed backwards in time, so that the most recent time interval is denoted by  $c = 1$  and the time interval corresponding to the beginning of the trial by  $c = C$ .

The method can be described in terms of a generalized linear model as follows:

$$g(E(y_j)) = \eta_0 + \theta_{k_j} + \alpha_{c_j} \quad (2.3)$$

binary

logit

where  $y_j$  is the response for patient  $j$  and  $g(\cdot)$  is the link function, which maps the expected value of the patient response to the linear predictors in the model. Specifically, as the **Time Machine has been discussed in the context of binary endpoints in [3]**, the ~~logit link function was considered here~~. The model intercept  $\eta_0$  denotes the response of the control group at time of the analysis,  $\theta_{k_j}$  is the response of the treatment arm  $k$  that patient  $j$  was enrolled in, relative to control, and  $\alpha_{c_j}$  represents the change in the patient response for the time bucket  $c$  that corresponds to the enrollment of patient  $j$ , relative to  $c = 1$ . For the parameters  $\eta_0$  and  $\theta_{k_j}$ , normal prior distributions are assumed, with mean 0 and variances  $\sigma_{\eta_0}^2$  and  $\sigma_{\theta}^2$ , respectively:

$$\eta_0 \sim \mathcal{N}(0, \sigma_{\eta_0}^2)$$

$$\theta_{k_j} \sim \mathcal{N}(0, \sigma_{\theta}^2)$$

effect

maybe later

repetition?

The time trend **is described by the parameter  $\alpha_c$** , which is modelled using a Bayesian second-order normal dynamic linear model (NLDM) that creates a smoothing over the control response, **such that closer time buckets are modelled with closer response rates:**

$$\alpha_1 = 0$$

$$\alpha_2 \sim \mathcal{N}(0, 1/\tau)$$

$$\alpha_c \sim \mathcal{N}(2\alpha_{c-1} - \alpha_{c-2}, 1/\tau), \quad 3 \leq c \leq C$$

where  $\tau$  denotes the drift parameter that controls the degree of smoothing over the time buckets and is assumed to have a Gamma hyperprior distribution:

also later

## 2. Methods

$$\tau \sim \text{Gamma}(a, b)$$

Saville et al. [3] examined the operating characteristics of the Time Machine in a simulation study considering a scenario with  $K = 5$  treatment arms, focusing only on evaluating the efficacy of the last treatment arm ( $k = 5$ ) against the shared control arm (testing  $H_{0,5} : \theta_5 = 1$  vs.  $H_{1,5} : \theta_5 > 1$ ). They demonstrated that the Time Machine can lead to superior performance as compared to the frequentist model with categorical adjustment for time in scenarios with linear time trend. However, in situations with sudden changes in the time trend, the frequentist model-based approach is preferable, as the time effect is modelled independently for each time interval in this case.

Similarly to the frequentist model that adjusts for time by including it as a categorical variable, the Bayesian Time Machine relies on the assumption that the time trend affects all arms in the trial equally and is additive on the model scale. Hence there should be no interaction between treatment and time. The Time Machine may also lead to poor results in settings with little to no overlap between the treatment arms, as there is not enough data to provide a link between concurrent and non-concurrent controls. Moreover, the performance of the method is dependent on the choice of the time buckets and the prior parameters, which need to be chosen individually for a given endpoint, disease and population.

### 2.1.3. Network Meta-analysis

Marschner and Schou [4] propose to analyse platform trials using meta-analysis techniques, which allows to conduct both, treatment-control as well as treatment-treatment comparisons for non-concurrent arms. They argue that even though the design of a platform trial is usually adapted over time, the periods between adaptations may still be viewed as separate trials with fixed design. In particular, the randomization is preserved in each period, hence unbiased direct comparisons can be made between concurrent arms. Moreover, indirect comparisons between two arms across multiple stages can be performed by combining two direct comparisons to a common reference arm, that is concurrent to both arms of interest at some point (i.e. there is an overlap of the reference arm and the arms being compared). From this perspective, the platform trial can be viewed as a network of direct (concurrent) and indirect (non-concurrent) comparisons.

The proposed method linearly combines all direct contrast estimates  $\hat{\theta}$  from all periods, creating a synthesis of direct and indirect evidence to obtain the network estimates  $\hat{\theta}^{network}$  of the treatment-control comparisons.

$$\hat{\theta}^{network} = (\mathbf{X}^T \mathbf{W} \mathbf{X})^{-1} \mathbf{X}^T \mathbf{W} \hat{\theta} \quad (2.4)$$

where  $\mathbf{X}$  is a design matrix specifying the possible treatment contrasts in all periods the trial and  $\mathbf{W}$  is a weight matrix, chosen based on the treatment effect standard errors in each period. This weight matrix also quantifies the contribution of the direct evidence to the overall evidence.



## 2.2. Extensions to the Frequentist Models for Treatment-Control Comparisons

As all previously described approaches for incorporating non-concurrent controls, the validity of the network meta-analysis relies on the assumption that the underlying difference between the compared arms does not change over time, i.e. remains the same for all direct and indirect comparisons. This assumption can be assessed using formal tests of inconsistency, which were developed in the context of meta-analysis.

### 2.1.4. Open Questions

Commentary -> [5]

② Also, we propose the methods adjusting for time by using time periods at XX and XX', as well as using calendar time intervals at XX.

## 2.2. Extensions to the Frequentist Models for Treatment-Control Comparisons

We extend the frequentist models from [1] and [2] to platform trials with  $K$  experimental treatment arms, where  $K > 1$ , and a shared control group ③

The timing of adding of the treatment arms is given by  $d = (d_1, \dots, d_K)$ , where  $d_i$  indicates how many patients had already been enrolled to the trial by the time treatment  $i$  entered the platform.  $d_1$  is always set to 0 to ensure that the platform trial starts with at least one treatment (for illustration see Fig. 2.2).

do we need this here?

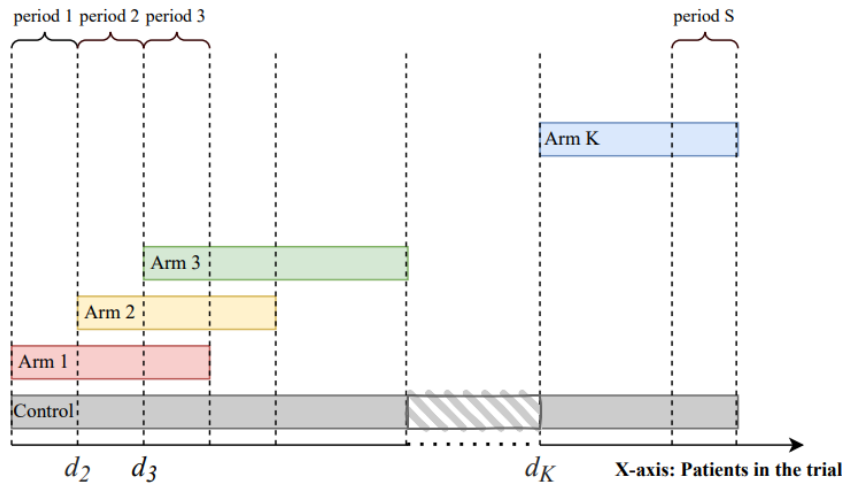


Figure 2.2.: Scheme of the considered general platform trial.

The division of the trial into periods in terms of recruitment times  $t_j$  can be described by the set  $\mathbf{T}_S$  that is given by  $\mathbf{T}_S = \{T_{S_1}, T_{S_2}, \dots, T_{S_S}\}$ , where  $T_{S_1} = (0, \min\{\max_{k_j=1}\{t_j\}, \min_{k_j=2}\{t_j\}\})$  and  $T_{S_l} = (\min\{\max_{k_j=l'}\{t_j\}, \min_{k_j=l}\{t_j\}\}, \min\{\max_{k_j=l'}\{t_j\}, \min_{k_j=l+1}\{t_j\}\})$  for  $l \in \{1, \dots, S\}$  and  $l, l' \in \{1, \dots, K\}$ ,  $l \neq l'$ .

2(1#)

Dividing the trial into equidistant discrete units of calendar time  $\mathbf{T}$  (e.g. months, where  $\mathbf{T} = 1$  would correspond to the first month of the trial) is given by the set of intervals

(#)

First, we divided the trial duration into periods, defined as... formally, let  $T$  be the set of all the periods in the trial

$T = \{ \dots \}$ , where the  $s$ -th period is defined by

$T_s = \dots$  for  $s = 1, \dots, S$  and  $l, l' \in \dots$   $l \neq l'$

Add summary table models

Name	Description	Time def		Time cov		Section (and ref)
		Per.	Cal	Ex	ran	
		x		F.		( - )
			↓	AL		

(##) As we assume that the effect of time is eq. across arms and uniform over the period as in  $XX$  and  $XX$ , the model relies on the same assumption, that is, ....

## 2. Methods

### notation

Symbol	Definition
$K$	number of experimental treatment arms
$k = 0, \dots, K$	arm indicator
$N$	total number of patients in the trial
$S$	total number of periods
$s = 1, \dots, S$	period indicator
$C$	total number of calendar time units
$c = 1, \dots, C$	calendar time unit indicator
$j = 1, \dots, N$	patient index
$y$	patient response
$t$	patient recruitment time
$\theta$	treatment effect
$\lambda$	strength of the time trend
$d$	timing of adding treatment arms in terms of patients recruited to the trial so far
$M$	currently evaluated treatment arm
$S_M$	period, in which arm $M$ left the trial
$C_M$	calendar time unit, in which arm $M$ left the trial
$\mathcal{K}_M$	set of treatment arms active in the trial prior or up to $S_M$ or $C_M$

Table 2.1.: Summary of the used notation.

$\mathbf{T}_C = \{T_{C_1}, T_{C_2}, \dots, T_{C_C}\}$ , where  $T_{C_i} = (i-1, i)$ , for  $i \in \{1, \dots, C\}$ . We summarize

The notation used in the following section is summarized in Table 2.1.

We focus on evaluating treatment arms  $k = 2, 3, \dots, K$  that enter when the trial is already ongoing and therefore NCC data is available for these arms. We aim at comparing the efficacy of each treatment against the control as soon as the treatment arm is completed. Consider the test of the one-sided null hypothesis  $H_{0,M} : \theta_M \leq 0$  for arm  $M$  under study, where  $\theta_M$  denotes the treatment effect size for treatment  $M$ .

→ To test the null hypothesis  $H_{0,M}$ , we propose model-based approaches adjusting for time as fixed or random factor, where time stratified either period or by calendar time.

### 2.2.1. Fixed-effects Models

Firstly, we consider two regression models fitted using all data from the trial until treatment  $M$  leaves the platform (i.e., all data in the set  $\mathcal{D}_M = \{(y_j, k_j, t_j), j = 1, \dots, N; t_j \leq \mathbf{T}_M\}$ , where  $\mathbf{T}_M$  denotes the calendar time unit in which arm  $M$  finishes). Note that also data from unfinished arms is included to the model. Both models estimate the effect of treatments, which were active in the trial prior or up to the time unit  $\mathbf{T}_M$ , and adjust for potential time trends by including time as a categorical covariate. The two approaches differ in the way time intervals are defined in the model: one using periods and the other the calendar time.

(before)

aren't the other models fitted with diff. data?

that

## 2.2. Extensions to the Frequentist Models for Treatment-Control Comparisons

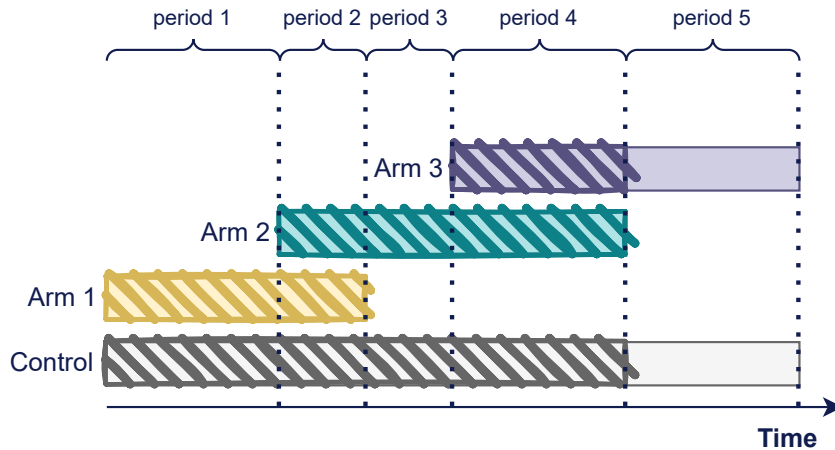


Figure 2.3.: Illustration of the data set  $\mathcal{D}_2$ . Data taken into account for the evaluation of the 2nd treatment arm are highlighted.

### Period Adjustment

In the first model, we adjust for the factor period, defined as the time interval bounded by any treatment arm entering or leaving, using a step-function:

$$y_j = \eta_0 + \sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k) + \sum_{s=2}^{S_M} \tau_s \cdot I(t_j \in T_{S_s}) + \varepsilon_j \quad (2.5)$$

where  $\eta_0$  is the response in the control arm in the first period; and  $\theta_k$  represents the effect of treatment  $k$  compared to control, for  $k \in \mathcal{K}_M$ , where  $\mathcal{K}_M$  is the set of treatments that were active in the trial during periods prior or up to  $T_M$ .  $S_M$  denotes the period, in which arm  $M$  left the trial (i.e. the period in which  $T_M$  is included) and  $\tau_s$  indicates a stepwise period effect between periods 1 and  $s$ , where  $s$  goes from 2 to  $S_M$ ...

This approach is a direct extension of the model (2.2), investigated in [1] and [2], to more flexible platform trials. Hence, the assumptions of equal time trend in all arms, and constant trend in each period are also made by this model.

### Calendar Time Adjustment

In the second approach, we consider a regression model adjusting for the time effect by using calendar time intervals, and thus estimating the calendar time effect rather than period effect:

$$y_j = \eta_0 + \sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k) + \sum_{c=2}^{C_M} \tau_c \cdot I(t_j \in T_{C_c}) + \varepsilon_j \quad (2.6)$$

## 2. Methods

Here  $\eta_0$  represents the control response in the first calendar time unit. As in (2.2.1),  $\theta_k$  denotes the treatment effect of treatment  $k$  compared to control and  $\mathcal{K}_M$  is the set of treatments that were active up until the arm  $M$  left the trial. The calendar time unit, in which arm  $M$  left the trial is indicated by  $C_M$  and  $\tau_c$  is the effect between calendar time units 1 and  $c$ .

The division of the trial into calendar times is depicted in Fig. 2.3. The length of these units is given in terms of the number of enrolled patients and can be specified arbitrarily.

PENDING - Add calendar times to Fig. 2.3!

Note that this model, similarly to the Bayesian Time Machine, divides time into bins of equal length. These bins are, unlike the period adjustment considered in [1] and [2], and in the extended model (2.5), independent of alternations to the trial design, i.e. adding and dropping arms is not taken into account.

### 2.2.2. Mixed Models

In models (2.5) and (2.6), time is treated as a fixed factor. Alternatively, patients within different periods or calendar time units could be considered as different clusters, having a period- or calendar time-specific random intercepts. In the next section, we include the time variable to the models as a random factor. In this way, possible correlation between the random effects associated with different periods or calendar times can also be taken into account.

#### Mixed Models with Uncorrelated Random Effects

First, we consider simple mixed-effect models, where the time effects are modeled as uncorrelated. The mixed-effect model with period adjustment specified by:

$$y_j = \eta_0 + \sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k) + \sum_{s=2}^{S_M} u_s \cdot I(t_j \in T_{S_s}) + \varepsilon_j \quad (2.7)$$

whereas the model adjusting for calendar time units is given by:

$$y_j = \eta_0 + \sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k) + \sum_{c=2}^{C_M} u_c \cdot I(t_j \in T_{C_c}) + \varepsilon_j \quad (2.8)$$

In (2.7) and (2.8),  $y_j$  denotes the response for patient  $j$  and the model intercept  $\eta_0$  is in this case given in terms of the control response across the whole trial up until  $S_M$  or  $C_M$ , respectively. This interpretation of the intercept corresponds to the Time Machine approach. The parameter  $\theta_k$  represents the fixed effect of treatment  $k$  compared to the control group.  $u_s$  and  $u_c$  denote the random effect associated with the intercept for period  $s$  or calendar time unit  $c$ .

The period-specific random effects in (2.7) are assumed to be normally distributed with mean 0 and constant variance  $\sigma_{period}^2$ :

## 2.2. Extensions to the Frequentist Models for Treatment-Control Comparisons

$$\mathbf{u} \sim \mathcal{N}(0, \sigma_{period}^2 \cdot I_{S_M \times S_M})$$

The random effects in (2.8) associated with calendar time units are distributed analogously:

$$\mathbf{u} \sim \mathcal{N}(0, \sigma_{calendar}^2 \cdot I_{C_M \times C_M})$$

Note that in this case the correlation between any two period or calendar time effects is 0.

In both models, the distribution of the residuals  $\varepsilon_j$ , associated with the response of individual patient  $j$  is assumed to be the same for all treatments:

$$\varepsilon \sim \mathcal{N}(0, \sigma^2 \cdot I_{N \times N})$$



The random effects,  $u_s$  or  $u_c$ , and the residuals,  $\varepsilon_j$ , are assumed to be independent.

### Mixed Models with Autocorrelated Random Effects

← follow prev. section for next version.

To account for possible correlation of the random effects, we also consider random effects with first-order autoregressive structure (AR(1)), again with period or calendar time adjustments. The model equations are identical to (2.7) and (2.8):

$$y_j = \eta_0 + \sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k) + \sum_{s=2}^{S_M} u_s \cdot I(t_j \in T_{S_s}) + \varepsilon_j \quad (2.9)$$

$$y_j = \eta_0 + \sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k) + \sum_{c=2}^{C_M} u_c \cdot I(t_j \in T_{C_c}) + \varepsilon_j \quad (2.10)$$

The model (2.9) considers period adjustments, while (2.10) adjusts for calendar times and the model parameters have the same interpretation as above.

There is a difference, however, with respect to the distribution of the random effects, which are now modelled as autocorrelated. The random effects for individual periods are assumed to be normally distributed with mean 0, constant variance  $\sigma_{period}^2$  and an AR(1) correlation structure:

$$\mathbf{u} \sim \mathcal{N}(0, \sigma_{period}^2 \cdot \Sigma_{S_M \times S_M})$$

$$\Sigma_{S_M \times S_M} = \begin{bmatrix} 1 & \phi & \dots & \phi^{S_M-1} \\ \phi & 1 & \dots & \phi^{S_M-2} \\ \vdots & \vdots & \ddots & \vdots \\ \phi^{S_M-1} & \phi^{S_M-2} & \dots & 1 \end{bmatrix}$$

## 2. Methods

Analogous distribution is assumed for the random effects associated with different calendar times:

$$\mathbf{u} \sim \mathcal{N}(0, \sigma_{calendar}^2 \cdot \Sigma_{C_M \times C_M})$$

$$\Sigma_{C_M \times C_M} = \begin{bmatrix} 1 & \phi & \dots & \phi^{C_M-1} \\ \phi & 1 & \dots & \phi^{C_M-2} \\ \vdots & \vdots & \ddots & \vdots \\ \phi^{C_M-1} & \phi^{C_M-2} & \dots & 1 \end{bmatrix}$$

The parameter  $\phi$  denotes the correlation between two adjacent periods or calendar time units. Note that  $\phi$  can range from -1 to 1 and the correlation of periods that are  $w$  units apart is equal to  $\phi^w$ , such that the correlation is weaker for periods that are further apart.

The residuals are again assumed to be normally distributed (i.i.d.) with mean 0 and constant variance:

$$\boldsymbol{\varepsilon} \sim \mathcal{N}(0, \sigma^2 \cdot I_{N \times N}) \quad (2.11)$$

### 2.2.3. Toy Example

Add a simple example trial and compare all methods + code.

## 2.3. Treatment-Treatment Comparisons

Great work!  
keep going! ⚡

## 3. Simulations and Results

### 3.1. Extension to More Than 2 Arms

### 3.2. Mixed Models

### 3.3. Period vs. Calendar Time Adjustments

### 3.4. Examples





## 4. Software

### 4.1. Software Description

### 4.2. Examples



## 5. Conclusions

### 5.1. Future Research



# Bibliography

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## A. Appendix

here you can put further things you want to add like transcripts, questionnaires, raw data...