

# Model-based Adjustments for Non-concurrent Comparisons in Platform Trials

Pavla Krotka

Supervisors: Martin Posch, Marta Bofill Roig

Master's Seminar, 28.11.2022

# Platform trials

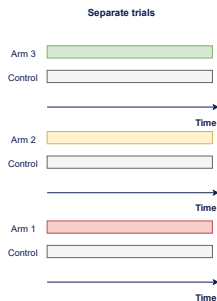
Multi-arm multi-stage trials that allow new experimental treatment arms to enter and leave the trial at different times.

- Treatments to be studied not defined upfront
- Control arm can be shared

# Platform trials

Multi-arm multi-stage trials that allow new experimental treatment arms to enter and leave the trial at different times.

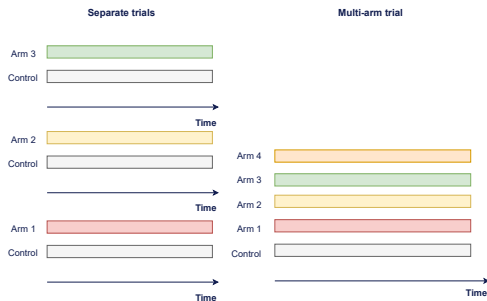
- Treatments to be studied not defined upfront
- Control arm can be shared



# Platform trials

Multi-arm multi-stage trials that allow new experimental treatment arms to enter and leave the trial at different times.

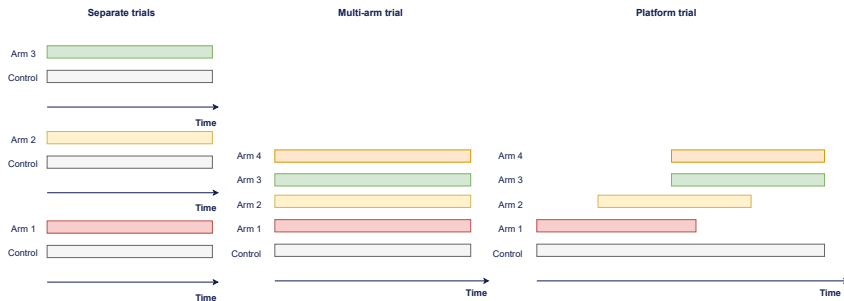
- Treatments to be studied not defined upfront
- Control arm can be shared



# Platform trials

Multi-arm multi-stage trials that allow new experimental treatment arms to enter and leave the trial at different times.

- Treatments to be studied not defined upfront
- Control arm can be shared



## Benefits

- Treatments are evaluated **faster** as compared to separate trials since drugs are tested **in parallel**
- Trials are **more efficient** due to the joint trial infrastructure
- **Less patients** are required in the control group as it is shared across all treatment arms
- Experimental treatments can enter the trial and be investigated as soon as they became available, which provides **more flexibility** than multi-arm trials

## Benefits

- Treatments are evaluated **faster** as compared to separate trials since drugs are tested **in parallel**
- Trials are **more efficient** due to the joint trial infrastructure
- **Less patients** are required in the control group as it is shared across all treatment arms
- Experimental treatments can enter the trial and be investigated as soon as they became available, which provides **more flexibility** than multi-arm trials

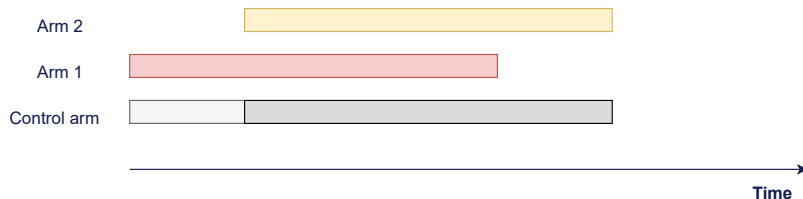
## Challenges

- Multiple operational and statistical challenges due to **higher complexity**
- The entering and leaving times, as well as the total number of experimental treatments are **unknown in advance**
- Use of the **shared control arm** in trial analysis

# Control groups in platform trials

## Concurrent and non-concurrent controls

- **Concurrent controls (CC):** patients recruited to the control when the experimental treatment is part of the platform
- **Non-concurrent controls (NCC):** patients recruited before the experimental treatment entered the platform

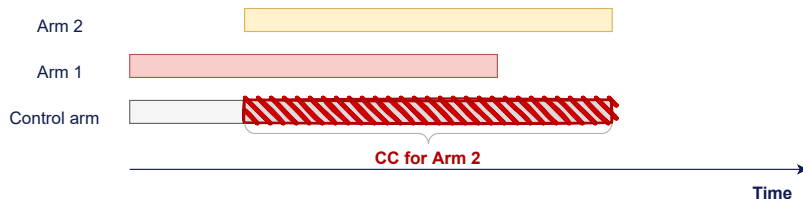




# Control groups in platform trials

## Concurrent and non-concurrent controls

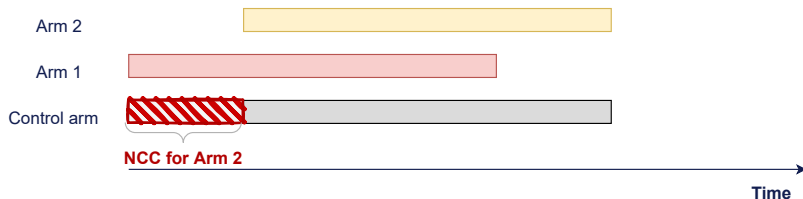
- **Concurrent controls (CC):** patients recruited to the control when the experimental treatment is part of the platform
- **Non-concurrent controls (NCC):** patients recruited before the experimental treatment entered the platform



# Control groups in platform trials

## Concurrent and non-concurrent controls

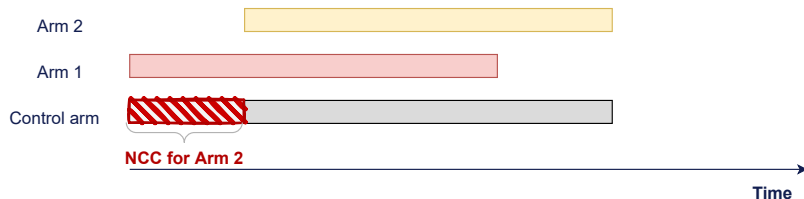
- **Concurrent controls (CC):** patients recruited to the control when the experimental treatment is part of the platform
- **Non-concurrent controls (NCC):** patients recruited before the experimental treatment entered the platform



# Control groups in platform trials

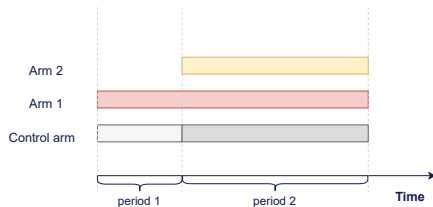
## Concurrent and non-concurrent controls

- **Concurrent controls (CC):** patients recruited to the control when the experimental treatment is part of the platform
- **Non-concurrent controls (NCC):** patients recruited before the experimental treatment entered the platform



Incorporating non-concurrent controls can substantially improve the **efficiency** (increased statistical power due to **larger sample sizes**) but may introduce **bias** due to **time trends**.

# State-of-the-art analysis methods

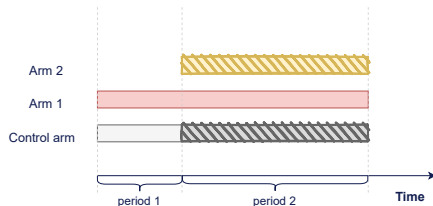


**Hypothesis testing problem:**

$$H_0 : \theta_2 = 0$$

$$H_1 : \theta_2 > 0$$

# State-of-the-art analysis methods



**Hypothesis testing problem:**

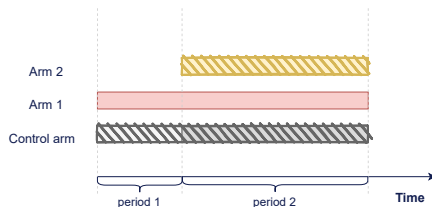
$$H_0 : \theta_2 = 0$$

$$H_1 : \theta_2 > 0$$

## Naive analysis methods

- **Separate approach:** analysis using only concurrent controls

# State-of-the-art analysis methods



**Hypothesis testing problem:**

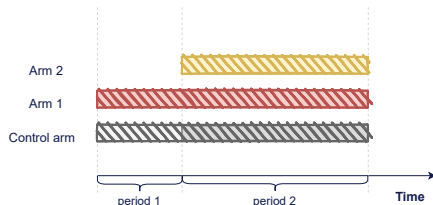
$$H_0 : \theta_2 = 0$$

$$H_1 : \theta_2 > 0$$

## Naive analysis methods

- **Separate approach:** analysis using only concurrent controls
- **Pooled approach:** pooling concurrent and non-concurrent controls

# State-of-the-art analysis methods



**Hypothesis testing problem:**

$$H_0 : \theta_2 = 0$$

$$H_1 : \theta_2 > 0$$

## Naive analysis methods

- **Separate approach:** analysis using only concurrent controls
- **Pooled approach:** pooling concurrent and non-concurrent controls

## Novel methods

- **Frequentist regression models:** adjust for time trends by including time as a covariate (Lee & Wason, 2020; Bofill Roig, Krotka, et al., 2022)
- **Bayesian Time Machine:** adjusts for time trends by smoothing over time bins using a second-order Bayesian normal dynamic linear model (Saville, et al., 2022)
- **Network meta-analysis:** uses meta-analysis techniques to combine information from different periods (Marschner & Schou, 2022)

# Frequentist regression model

Adjust for time trends by a stepwise function in a regression model

$$E(X) = \eta_0 + \sum_{k=1,2} \theta_k \cdot I(T = k) + \tau \cdot I(S = 2)$$

where  $X$  is the continuous outcome,  $T = 0, 1, 2$  denotes the treatment and  $S = 1, 2$  the period.

- All data available in the platform is used to estimate the time trend
- Time trend is assumed constant in every period
- Time is assumed to have equal effect for all arms



RESEARCH

Open Access

## On model-based time trend adjustments in platform trials with non-concurrent controls



Marta Bofill Roig<sup>1</sup>, Pavla Krotka<sup>1</sup>, Carl-Fredrik Burman<sup>2</sup>, Ekkehard Glimm<sup>3,4</sup>, Stefan M. Gold<sup>5,6,7</sup>, Katharina Hees<sup>8</sup>, Peter Jacko<sup>9,10</sup>, Franz Koenig<sup>1</sup>, Dominic Magirr<sup>3</sup>, Peter Mesenbrink<sup>11</sup>, Kert Viele<sup>12</sup> and Martin Posch<sup>1\*</sup>

### Key messages

- Increase in power as compared to the separate approach
- Type I error control, if:
  - Equal time trends across arms
  - Time trend additive on model scale
  - Block randomization

### Open questions

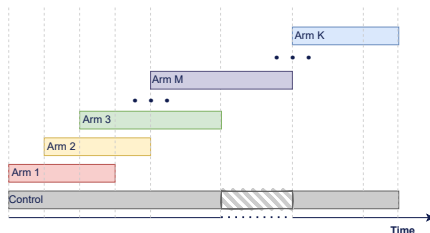
- How would the models perform in more general platform trials with more than two experimental treatment arms?
- Would more advanced modeling approaches improve the power while maintaining the type I error?

# Goals and contributions of this thesis

1. **Generalize** the **model-based approaches** to trials with more than two experimental treatment arms
2. Propose **alternative models** for incorporating NCC
  - Consider alternative definitions of the time variable
  - Consider more flexible methods to estimate the time trend
3. Investigate the **operating characteristics** of the proposed approaches in a simulation study
4. **Software** implementation in R

# Considered design

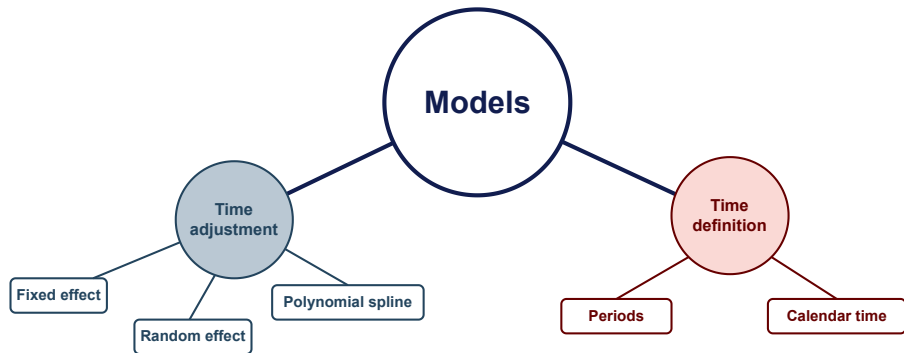
- Consider platform trials with  $K$  experimental treatment arms ( $K > 2$ )
- Statistical inference for arm  $M \in \{1, \dots, K\}$
- Use all data until arm  $M$  leaves the trial for the analysis



**Hypothesis testing problem:**

$$H_0 : \theta_M = 0$$

$$H_1 : \theta_M > 0$$



# Regression model for trials with multiple arms

Adjust for time as fixed effect:

$$y_j = \underbrace{\eta_0}_{\substack{\text{Control response} \\ \text{in period 1}}} + \underbrace{\sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k)}_{\text{Treatment effects}} + \underbrace{\sum_{s=2}^{S_M} \tau_s \cdot I(s_j = s)}_{\text{Period time effects}} + \varepsilon_j$$

$S_M$  ... period in which arm  $M$  finishes

$\mathcal{K}_M$  ... set of active treatments in periods prior or up to  $S_M$

$j$  ... patient index in the order of enrollment time

$\varepsilon_j \sim \mathcal{N}(0, \sigma^2)$

- Extension of the model considered in Bofill Roig, Krotka, et al. (2022)
- The model uses all data available in the trial until arm  $M$  leaves, including data from unfinished arms

# Mixed models

Adjust for time as random effect:

$$y_j = \underbrace{\eta_0}_{\substack{\text{Average control} \\ \text{response across the trial}}} + \underbrace{\sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k)}_{\text{Treatment effects}} + \underbrace{\sum_{s=2}^{S_M} u_s \cdot I(s_j = s)}_{\text{Period time effects}} + \varepsilon_j$$

$S_M \dots$  period in which arm  $M$  finishes

$\mathcal{K}_M \dots$  set of active treatments in periods prior or up to  $S_M$

$j \dots$  patient index in the order of enrollment time

$u_s \sim \mathcal{N}(0, \sigma_{\text{period}}^2)$

$\varepsilon_j \sim \mathcal{N}(0, \sigma^2)$

## Investigated variants:

- Uncorrelated random effects
- Autocorrelated (AR1) random effects

# Spline regression

Adjust for time with a spline function:

$$y_j = \underbrace{\eta_0}_{\text{Average control response across the trial}} + \underbrace{\sum_{k \in \mathcal{K}_M} \theta_k \cdot I(k_j = k)}_{\text{Treatment effects}} + \underbrace{f(j)}_{\text{Spline function of enrollment time}} + \varepsilon_j$$

$S_M$  ... period in which arm  $M$  finishes

$\mathcal{K}_M$  ... set of active treatments in periods prior or up to  $S_M$

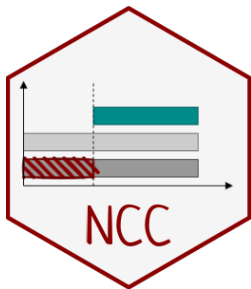
$j$  ... patient index in the order of enrollment time

$f(j)$  ... polynomial spline function of degree  $d$

$\varepsilon_j \sim \mathcal{N}(0, \sigma^2)$

## Investigated variants:

- Define the knots according to periods or calendar times
- Consider linear, quadratic and cubic splines



## Models:

- Regression models with fixed effects: `fixmodel_cont()`
- Mixed models: `mixmodel_cont()`
- Spline regressions: `splines_cont()`
- Pooled and separate analysis: `poolmodel_cont()`, `sepmode_cont()`

## Data generation:

- Functions to simulate platform trials with continuous and binary outcomes: `datasim_cont()`, `datasim_bin()`

## Simulation functions:

- Flexible wrapper functions to run multiple replications of desired scenarios in parallel: `sim_study_par()`, `all_models()`



## Goals

- Inference for an added treatment arm  $M$  using NCC
- Evaluate the operating characteristics of the considered approaches:
  - Type 1 error
  - Statistical power
  - Bias of the treatment effect estimates
- State conditions under which the investigated methods lead to valid statistical inference

## Setting

- Continuous endpoints
- Equal sample size  $n$  in each treatment arm
- Trials with  $K > 2$  arms entering sequentially after every  $d$  patients recruited to the trial
- Time trends for each arm of different strength and following patterns:
  - Linear
  - Stepwise
  - Inverted-U

# Selected references

- **Krotka, P.**, Bofill Roig, M., Hees, K., Jacko, P., Magirr, D. (2022). “*NCC: Simulation and analysis of platform trials with non-concurrent controls.*” R package: <https://github.com/pavlakrotka/NCC>, Web-page: <https://pavlakrotka.github.io/NCC/>.
- Bofill Roig, M., **Krotka, P.**, et al. “*On model-based time trend adjustments in platform trials with non-concurrent controls.*” BMC medical research methodology 22.1 (2022): 1-16
- Lee, K. M., and Wason, J. “*Including non-concurrent control patients in the analysis of platform trials: is it worth it?*” BMC medical research methodology 20.1 (2020): 1-12.
- Saville, B. R., Berry, D. A., et al. “*The Bayesian Time Machine: Accounting for Temporal Drift in Multi-arm Platform Trials.*” Clinical Trials 19.5 (2022): 490-501
- Marschner, I. C. and Schou, I. M. “*Analysis of adaptive platform trials using a network approach.*” Clinical Trials 19.5 (2022): 479-489
- Woodcock, J., and LaVange, L. M. *Master Protocols to Study Multiple Therapies, Multiple Diseases, or Both.* New England Journal of Medicine 377.1 (2017): 62–70

Thank you for your attention!