

MASARYKOVA UNIVERZITA  
FAKULTA INFORMATIKY



# **Alert Prediction in Metric Data Based on Time Series Analysis**

MASTER THESIS

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## **Declaration**

Hereby I declare, that this paper is my original authorial work, which I have worked out by my own. All sources, references and literature used or excerpted during elaboration of this work are properly cited and listed in complete reference to the due source.

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**Advisor:** RNDr. Adam Rambousek, Ph.D.

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Last but not least, I would like to thank to company Red Hat that provided me the great opportunity to work on this project.

## **Abstract**

The aim of the master's thesis is to develop a module for an open source monitoring and management platform Hawkular. This module is responsible for predicting alerts based on time series and providing data for predictive charts in Hawkular user interface.

## **Keywords**

Time Series, Hawkular, Alert Prediction, Exponential Smoothing

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# 1 Introduction

In driving successful business on the internet it is important to assure an application health and reliability. One can achieve that by monitoring subjected resources and setting up clever alerting system.

These features are offered in many monitoring systems, however being predictive in this area can even prevent undesirable states and most importantly gives administrators more time for reacting to such events. For instance it can decrease downtime of an application or ability to load balance workload in advance by horizontal scaling of targeted services.

Alerting system are sophisticated and can be composed by many conditions. This work focuses on predicting future metric values which are then sent as input for evaluation to alerting system.

The work starts with time series theory by describing various approaches for time series modelling and forecasting. The chapter describes models which are used within the work, could be used or explains why the decision was made to use other models.

Following chapter demonstrates models from previous chapter on real time series. It visually shows predictive capabilities of targeted models and compares produced statistical quantities.

The third chapter briefly describes existing monitoring and management solutions which are to some extent Hawkular competitors. There are also mentioned Java libraries for time series forecasting.

The fourth chapter describes implementation part of the thesis. It starts with core artifacts for time series forecasting and continues to building web application and integration into Hawkular.

The last chapter is dedicated to the evaluation of the forecasting accuracy of the implemented solution. As a default implementation were chosen models from forecast package from language R.

## 1.1 Hawkular

The implementation part of the master's thesis is developed as a part of an open source project Hawkular<sup>1</sup>. Therefore the application archi-

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1. Available at <http://www.hawkular.org>



itecture and used technologies had to fit into the overall project design.

Hawkular is middleware monitoring and management platform developed by company Red Hat and independent community of contributors. It is a successor to very successful RHQ<sup>2</sup> project, also known as JBoss Operations Network (JON). By monitoring is meant that there are agents for diverse applications which push data to the server. These agents can also execute application specific actions.

The monolithic architecture of the RHQ project was due its size hard to maintain and lacking robust REST API lead to fresh development of new application. In contrast Hawkular consist of several loosely coupled or even independent applications. These independent components are much easier to maintain and more importantly they communicate over REST API.

This architecture of microservices and chosen protocol allow simple development of agents which can be written in any programming language. In RHQ only Java agent were available.

Hawkular as a product is customized Wildfly<sup>3</sup> application server with all components deployed in it.

List of Hawkular main components:

- Console – user web interface.
- Accounts – authorization subsystem based on Keycloak<sup>4</sup>.
- Inventory – graph based registry of all entities in Hawkular.
- Metrics – time series metrics engine based on Cassandra<sup>5</sup>.
- Alerts – alerting subsystem based on JBoss Drools.

Some of the modules also uses Java messaging topics (JMS) for inter-component one to many communication.

Modules are packaged as standard Java web archives (WAR), or enterprise archives (EAR) and deployed into customized Wildfly. Build

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2. Available at <https://rhq-project.github.io/rhq/>.

3. An open source project of JBoss Enterprise Application Platform.

4. An open source single sign-on and identity management for RESTful web services.

5. An open source distributed database management system. Hybrid between key-value and column-oriented database.

and package management is performed by Maven and Gulp for user interface modules.

## 1.2 Data Mining Goals

The goal of this thesis is to develop a module for Hawkular which will provide forecasts for any time series metrics collected by agent.

On new metric data available the module learns from data and predicts new values. Based on this predicted values an alert can be triggered. Forecast should be also available for user interface in predictive charts.

One Wildfly agent on average collects hundreds to thousands metrics, therefore module should be capable of processing high volume of data. Some of the customers monitor hundreds of server each with multiple agents. Therefore performance of chosen learning algorithm has to be taken in the account.

## 1.3 Metrics in Hawkular

In Hawkular there are three types of metrics: gauge, counter and availability. All of them are univariate metrics of structure  $\{timestamp, value\}$ . Each of these types is used for collecting dedicated types of metric data. For example gauge can increase or decrease over the time, counter is monotonically decreasing or increasing and availability represents up or down state of a resource.

## 2 Time Series Models

This chapter focuses on time series theory and various approaches for time series modelling. Models are ordered from simpler to more complex ones. Only some of the discussed models are selected for the implementation. Chapter also adds some theory necessary for time series analysis, for example stationarity tests 2.9, seasonal decomposition 2.8 and period identification 2.10.

From the goals 1.2 results that selected time series models should be robust enough to work on arbitrary monitored time series and at the same time be computationally in expensive. In learning and forecasting process.

Firstly, it is important to define time series; it is a sequence of observations  $s_t \in \mathbb{R}$  ordered in time. This thesis focuses only on univariate equidistant discrete time series.

Time series analysis contains many segments, this work aims only on forecasting. It is defined as a process of making prediction of the future based on the past. In other words, forecasting is possible because future depends on the past or analogously because there is a relationship between the future and the past. However, this relation is not deterministic and can be hardly written in an analytical form [10].

Generally there are two forecasting types: qualitative and quantitative. Qualitative methods are mainly based on the opinion of the subject and are used when past data are not available, hence not suitable for this project. If there are past data available, quantitative forecasting methods are more suitable.

### 2.1 Simple quantitative methods

Following methods are the simplest forecasting quantitative models. They can be used on any time series without any prerequisites or further analysis.

- Average method – forecasts are equal to the value of the mean of historical data.

$$\hat{y}_{T+h|T} = \bar{y} = (y_1 + \dots + y_T)/T \quad (2.1)$$

- Naïve method – forecasts are equal to the last observed value.

$$\hat{y}_{T+h|T} = y_T \quad (2.2)$$

- Drift method – variation of naïve method which allow the forecasts to increase or decrease over time.

$$\hat{y}_{T+h|T} = y_T + \frac{h}{T-1} \sum_{t=2}^T y_t - y_{t-1} = y_T + h\left(\frac{y_T - y_1}{T-1}\right) \quad (2.3)$$

There are also a seasonal variants of these models which holds one model for each season. These methods in general produces high forecasting error but are very easy to implement.

## 2.2 Linear Regression

Linear regression is a classical statistical analysis technique. It is mostly used to determine whether there is linear relationship between dependent and eventually more independent variables [14]. It is also used for predictions mainly in econometric field.

Simple linear regression is defined as:

$$y = \beta_0 + \beta_1 x + \epsilon \quad (2.4)$$

Parameters  $\beta_0$  and  $\beta_1$  are calculated by minimizing the sum of squared errors:

$$SSE = \sum_{i=1}^N \epsilon_i^2 = \sum_{i=1}^N (y_i - \beta_0 - \beta_1 x_i)^2 \quad (2.5)$$

Once the parameters are estimated predictions for any time in the future can be calculated. If modelled time series is not stationary and trend changes over time parameters should be periodically reestimated to achieve better forecasting accuracy. So the regression model does not adapt if the underlying time series changes.

### 2.3 Simple Exponential Smoothing

The concept behind simple exponential smoothing is to attach larger weights to the most recent observations than to the observations from distant past. Forecasts are calculated using weighted averages where the weights decrease exponentially as observations come from further in the past [12]. In other words smaller weights are associated to older observations. Equation for simple exponential smoothing is listed in 2.6.

$$\begin{aligned}\hat{y}_{T+1|T} &= l_t \\ l_t &= \alpha y_t + (1 - \alpha)l_{t-1}\end{aligned}\tag{2.6}$$

For smoothing parameter  $\alpha$  holds  $0 \leq \alpha \leq 1$ . Note, if  $\alpha = 1$  then  $\hat{y}_{T+1|T} = y_T$  so forecasts are equal to the naïve method. If the parameter  $\alpha$  is smaller more weight is given to the observations from distance in the past.

Simple exponential smoothing has flat forecast function, that means all forecasts all the same. Smoothing can be generally used as technique to separate signal and noise. This method is useful if a series does not contain any trend or one is interested only in one step ahead prediction. Multi step ahead predictions for time series with trend usually produce high error.

### 2.4 Holt's Liner Trend Method

Simple exponential smoothing can be extended to allow forecasting of data with a trend. This was done by Charles C. Holt in 1957. This method is slightly more complicated than original one without trend. In order to add trend component another equation has to be added 2.7.

$$\begin{aligned}\hat{y}_{t+h|t} &= l_t + hb_t \\ l_t &= \alpha y_t + (1 - \alpha)(l_{t-1} + b_{t-1}) \\ b_t &= \beta(l_t - l_{t-1}) + (1 - \beta)b_{t-1}\end{aligned}\tag{2.7}$$

Where a parameter  $b_t$  denotes a slope of the series and the parameter  $l_t$  level. There is also a new smoothing parameter for the slope  $\beta$ . Its range is equal to  $\alpha$ , so  $\alpha, \beta \in [0,1]$ .

## 2.5 Holt-Winters Seasonal Method

This method is an extension of Holt's linear trend method with added seasonality. It is also called triple exponential smoothing. In this model there are three equations 2.8. One for level, second for trend and third for seasonality. Each pattern uses smoothing constant  $\alpha, \beta, \gamma \in [0,1]$ .

$$\begin{aligned}\hat{y}_{t+h|t} &= l_t + hb_t + s_{t+h_m-m} \\ l_t &= \alpha(y_t - s_{t-m}) + (1 - \alpha)(l_{t-1} + b_{t-1}) \\ b_t &= \beta(l_t - l_{t-1}) + (1 - \beta)b_{t-1} \\ s_t &= \gamma(y_t - l_{t-1} - b_{t-1}) + (1 - \gamma)s_{t-m}\end{aligned}\tag{2.8}$$

Where  $h_m = [(h - 1) \bmod m] + 1$ , which ensures that the estimates of the seasonal indices came from the correct season. This model can be used only if the period of time series is known beforehand. In Hawkular the period of the time series is unknown, therefore period identification should be also implemented.

Each exponential smoothing model contains parameters which should be precisely estimated ( $\alpha, \beta, \gamma$ ). But it is possible to use default values from literature. However, with default values models produce higher forecasting error than with estimated parameters. Estimation process defines objective function which value can be mean squared error, mean absolute error or likelihood. Then this objective function is passed to non-linear optimization algorithm.

Time complexity of exponential smoothing models for learning  $n$  observations is  $O(n)$ . With enabled optimization the complexity depends on used optimization algorithm.

Exponential smoothings have advantage over other more complicated models that if a system needs to achieve high performance than default parameters can be used. This would not be possible with ARIMA models.

## 2.6 Box – Jenkins Methodology (ARIMA)

Models from Box – Jenkins methodology are the most widely used in time series analysis for econometric data. This methodology is based on analysis of autocorrelation (ACF) and partial autocorrelation (PACF) functions.

The most generic model is ARIMA( $p, d, q$ ). It combines together autoregressive, integrated and moving average parts. An autoregressive model (AR) consist of sum of weighed lagged observations 2.9. The order of this model is defined by  $p$  and can be determined from PACF function [14].

$$y_t = \phi_1 y_{t-1} + \phi_2 y_{t-2} + \cdots + \phi_p y_{t-p} + \epsilon_t \quad (2.9)$$

$$\epsilon_t \stackrel{iid}{\sim} N(0, \sigma^2)$$

A moving average model (MA) is sum of weighted errors of order  $q$ . The order of this part can be determined from ACF function [14]. Moving averages model should not be confused with simple moving average from 2.3 which is used for trend estimation. In moving average model MA( $q$ ) the current value is a regression against white noise of prior values of the series [15]. A random noise from each point is assumed to come from the same distribution which typically is a normal distribution. Model of the order  $q$  is listed in 2.10.

$$y_t = \theta_1 \epsilon_{t-1} + \theta_2 \epsilon_{t-2} + \cdots + \theta_q \epsilon_{t-q} + \epsilon_t \quad (2.10)$$

$$\epsilon_t \stackrel{iid}{\sim} N(0, \sigma^2)$$

The last part of the model is used when a time series is non stationary. There are several ways how to make a particular time series stationary. Box – Jenkins methodology uses differencing – integration part I( $d$ ). The order of differentiated original series is denoted by  $d$  letter. Usually first order differences are enough to make a time series stationary.

It is important to mention that models AR( $p$ ) and MA( $q$ ) are invertible. Therefore any stationary AR( $p$ ) model can be written as MA( $\infty$ ) and with some assumptions vice versa [7]. ARIMA model is often

written with backshift operator  $By_t = y_{t-1}$ . With this operator ARIMA(p, d, q) is listed in 2.11. On the left side of the equation is AR(P) process and on the right MA(q).

$$(1 - \phi_1 B - \dots - \phi_p B^p)(1 - B)^d y_t = c + (1 + \theta_1 B + \dots + \theta_q B^q) \epsilon_t \quad (2.11)$$

The parameters of the model, including AR and MA part can be estimated by non-linear optimization algorithm with likelihood as objective function [7]. However this function is much more complicated than for exponential smoothings. For successful estimation a certain number of historical points needs to be available. In [14] minimal training size is set to at least fifty observations.

After this theoretical part it is clear that ARIMA models are more complicated than family of moving averages. To this also refers [11] and adds that ARIMA less robust than exponential smoothings.

## 2.7 Artificial Neural Networks

Recently a large number of successful applications using neural networks for time series modeling show that they can produce valuable results [16]. There are several non trivial issues with determining the appropriate architecture of the network. This has to be taken into account because it can dramatically effect learning performance and forecasting accuracy [6]. Besides the problems with selecting right architecture learning process of artificial neural network is much more computationally expensive than selecting appropriate ARIMA or exponential smoothing model [8].

Because Hawkular forecasting engine should be capable of predicting thousands of metrics at the same time, models based on neural networks would have too high computational requirements. Therefore they are not suitable for our environment.

## 2.8 Time series decomposition

In modelling time series it is sometimes necessary to decompose series to trend, seasonal and random component [10]. It is also used for



initialization seasonal indices in triple exponential smoothing.

- **Trend**  $T_t$  – exists if there is long term increase or decrease over time. Can be linear or nonlinear (e.g. exponential growth).
- **Seasonal**  $S_t$  – exists when a series is influenced by seasonal factors. Seasonality is always of fixed and known period.
- **Cyclic**  $C_t$  – exists if there are long term wave-like patterns. Waves are not of a fixed period.
- **Irregular**  $E_t$  – unpredictable random value referred as white noise.

Decomposition can be written in many forms. Two of them are additive 2.12 and multiplicative 2.13. Which one to use depends on the underlying time series model.

$$y_t = T_t + S_t + C_t + E_t \quad (2.12)$$

$$y_t = T_t \times S_t \times C_t \times E_t \quad (2.13)$$

An algorithm for additive decomposition consist of following steps:

- Compute a trend component  $\hat{T}_t$  using moving average model. If a period is even use  $2xMA(period)$ . If period is an odd use  $MA(period)$ .  $2xMA$  for even period is used because it has to be symmetric.
- Calculate detrended series  $y_t - \hat{T}_t$ .
- Estimate seasonal indices  $\hat{S}_t$  for each period by averaging values of given period. For example, the seasonal index for Monday is the average for all detrended Monday values in the data. Then the mean of seasonal indices is subtracted from each period.
- Random component is calculated by subtracting trend and seasonal component from original time series  $\hat{E}_t = y_t - \hat{T}_t - \hat{S}_t$ .

## 2.9 Augmented Dickey – Fuller Test

Time series statistical tests are often used for testing if there is particular characteristics present in time series. Unit root test are used whether a time series is non stationary. In this work Augmented Dickey – Fuller (ADF) test was chosen for unit root testing.

Its null hypothesis is  $H_0$ : time series contains a unit root – it is not stationary. Outcome of this test is a negative ADF statistics. The more negative it is the stronger the rejection of the hypothesis. The full form of ADF test is listen in 2.14.

$$\Delta y_t = \alpha + \beta t + \gamma \Delta y_{t-1} + \dots + \delta p - 1 \Delta y_{t-p+1} + \epsilon_t \quad (2.14)$$

$$ADF = \frac{\hat{\gamma}}{SE(\hat{\gamma})} \quad (2.15)$$

There are multiple variants of ADF test. Some of them leave out parts of equation 2.14. The most important ones and widely used are:

- $nc$  – for regression with no constant nor time trend ( $\beta t$ )
- $c$  – for regression with an intercept but no time trend ( $\beta t$ )
- $ct$  – for regression with an intercept and time trend

Each of them is good for testing particular type of stationarity. For example for testing if there is time trend present in the time series  $c$  version is the best choice.

The implementation of this test fits multiple linear regression model from equation 2.14. Then calculate ADF statistics with 2.15. SE denotes standard error of estimated  $\hat{\gamma}$ .

## 2.10 Seasonality detection

Forecasting engine in Hawkular system does not have any inside information about period of a time series being modelled. Therefore automatic period identification has to be implemented. In practice it is a difficult task and result often differs from correct period, specially if there is significant noise present in the series [13].

There are several approaches how to implement automatic period identification. The most used ones are based on autocorrelation function (ACF) or spectral density [2]. This work applies ACF method. In the following chart 2.1 ACF function of sine function is shown. The period of this function is seven. There are patterns repeated every seven observations and it is decreasing to zero.

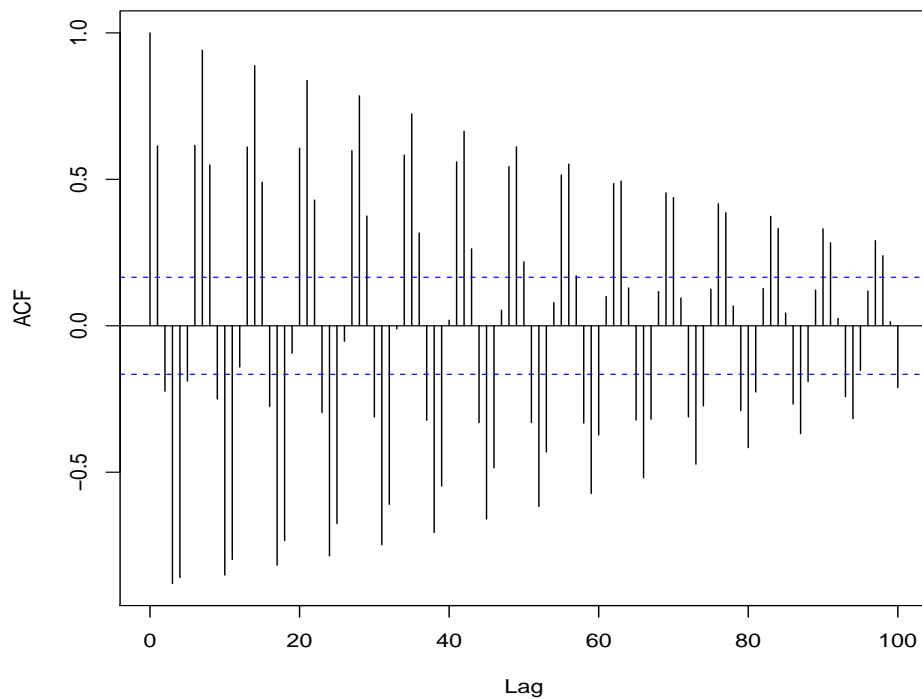


Figure 2.1: Autocorrelation function of sine function.

The algorithm for automatic period identification is demonstrated in 1. It is looking for periodically repeated significant values of ACF function. At some rate these values have to be decreasing to zero. In the infinity ACF function converges to zero.

The algorithm as input takes only time series. If there is a unit

root present differencing is applied. Follows calculation of autocorrelation function of input time series and finding the index of its highest value. Then it checks if there are significant values of ACF present at following  $n * period$  indices. There have to be present at least two consecutive values of ACF, so  $n$  takes values from 1, 2, 3...

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**Algorithm 1** Find period of time series

---

```

1: function FINDFREQUENCY(int[] ts)
2:   if unitRootPresent(ts) then                                     ▷ e.g. ADF test
3:     ts ← diff(ts)                                               ▷ first order differences
4:   end if
5:   acf ← acf(ts)
6:                                     ▷ returns index of the highest value
7:   period ← findHighest(ts, period)
8:   while period * 2 < ts.length do
9:     if checkPeriodExists(x, ts) then
10:      return period
11:    end if
12:    period ← findHighest(ts, period)
13:  end while
14:  return 1
15: end function

```

---

### 3 Analytical Forecasting Process

In the previous chapter several time series models were described. However, in Hawkular only a few of them were selected and implemented.

This chapter demonstrates targeted models on real time series. There is also conducted a statistical comparison of the models. So this chapter also contains theory how different models should be compared. At the end there is a discussion which models were selected for usage in Hawkular.

#### 3.1 Evaluating Forecasting Accuracy

In order to evaluate a forecasts produces by a particular model it is important to calculate the errors of the forecasts. There are several statistics for evaluating forecasting errors. The most used ones are mean squared error (MSE) 3.1 and mean absolute error (MAE) 3.2 [9]. The difference between them is that MSE emphasizes the extremes while MAE is more robust to outliers [11].

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad (3.1)$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i| \quad (3.2)$$

#### 3.2 Measuring Model Quality

When comparing multiple models, statistics like MSE or MAE are not the best objective functions. Comparison based on this statistics can select complicated model with lots of parameters, which may overfits training data and most importantly it selects less robust model [14]. Therefore for comparing multiple models another factors has to be added to the objective function. These factors are number of parameters of the model. The most used criteria for model sections are: Akaike information criterion (AIC) and Bayesian information criterion (BIC). Model with lower information criterion is preferred.

$$\begin{aligned} AIC &= 2k - \ln(L) \\ BIC &= k \ln(n) - 2 \ln(L) \end{aligned} \quad (3.3)$$

Equations for AIC and BIC are listed in 3.3. Number of parameters of the model represents  $k$ ,  $n$  is number of observations and  $L$  is maximized value of the likelihood function of the model. In case for exponential smoothing it is minimized sum of squared error of one step ahead prediction of training data set.

From the equations it can be seen that BIC penalizes models with more parameters. There is also AIC criterion with correction form 3.4. Corrected version of AIC more penalizes longer models.

$$AICc = AIC + \frac{2k(k+1)}{n-k-1} \quad (3.4)$$

### 3.3 Models Demonstration

An analytical process of modelling time series starts with plotting the data and fitting various models chosen by forecaster's previous experience. In second step forecaster compares statistics of those models and choose one the best describes data.

In this section a real time series is modelled using time series discussed in chapter 2. Chosen time series is *austourists* from R package *fpp*. This series is a measurement of quarterly visitor nights spent by international tourists in Australia. It was chosen on purpose because it contains trend and seasonality.

In the first chart 3.1 there is depicted naïve, average and drift model. Average model is just an overall average of the whole time series. It does not change over time. However there could be online version of this algorithm for which an average would be calculated for each new value.

Naïve and drift model copy values of time series with lag of one observation. These two models differs in forecasts where drift model is capable of forecasting trends.

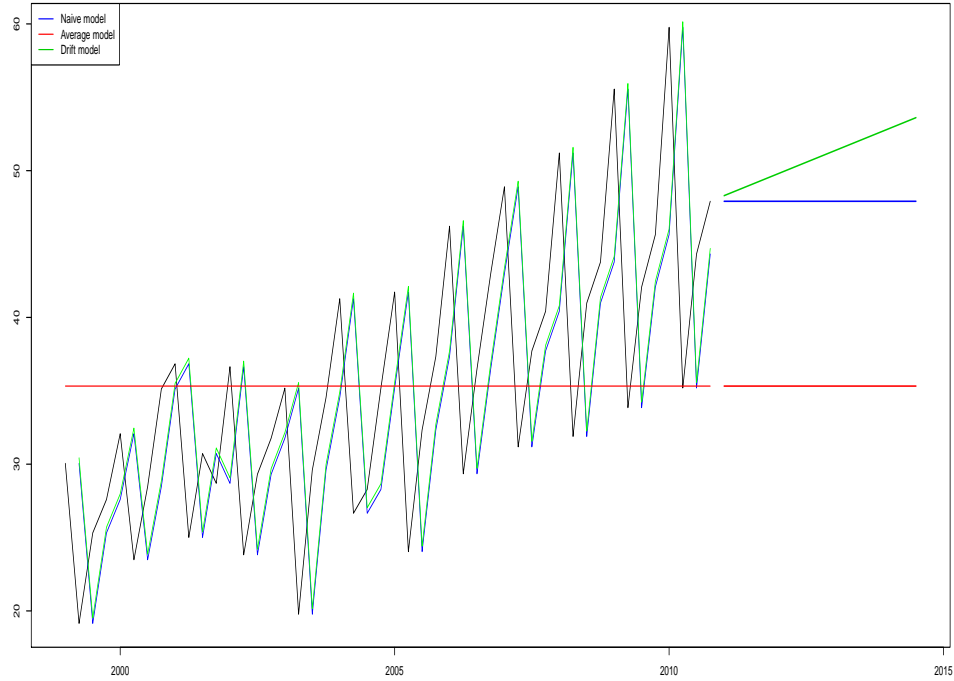


Figure 3.1: Simple models on *austourists*.

Exponential smoothings are depicted in 3.2. For this particular series it is obvious that seasonal model is the best describing modelled time series.

In the beginning it can be seen how is the seasonal model changing and learning the seasonal pattern from data. Learning and adaptivity to new trends depends on smoothing parameters of the models. Higher values of parameters allows the model quicker adapt to changes. Models with lower smoothing parameters are more robust to the changes.

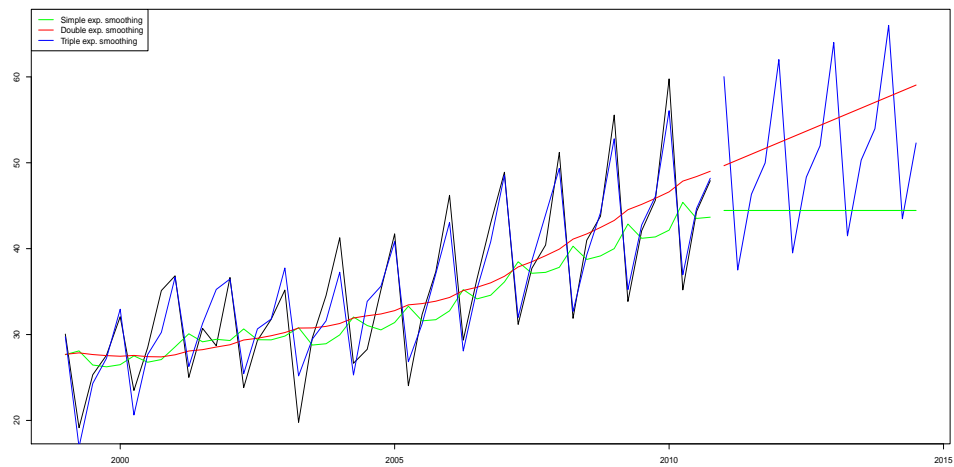


Figure 3.2: Exponential smoothings on *austourists*.

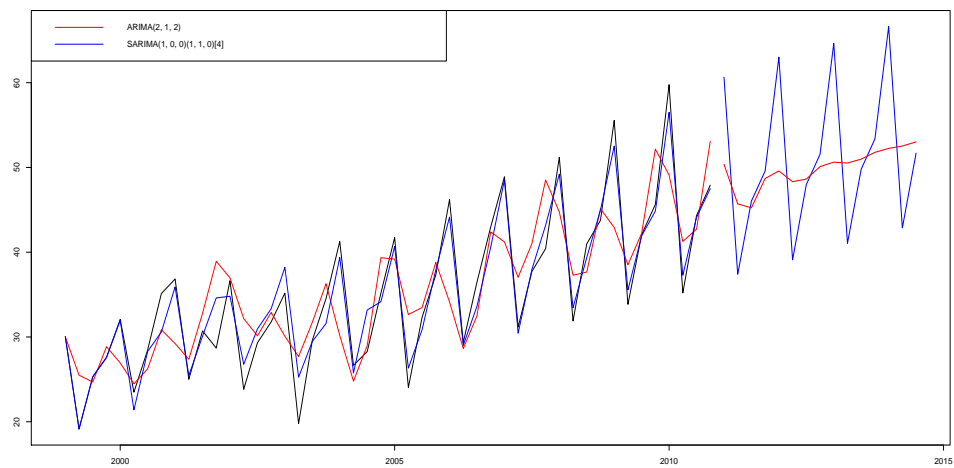


Figure 3.3: Arima models on *austourists*.



ARIMA models are showed in 3.3. Non seasonal model is already capable of capturing some seasonal patterns but it is more random whereas seasonal patterns should be of fixed period. Therefore seasonal ARIMA with dedicated model for each period is more appropriate.

Model	MSE	MAE	AIC
Naïve	104.74	8.64	
Drift	104.60	8.47	
Average	79.91	7.14	
Simple exp. smoothing	53.54	5.91	380.88
Double exp. smoothing	44.41	5.28	375.90
Triple exp. smoothing	5.34	1.71	282.73
Linear regression	41.85	5.10	321.46
ARIMA(2, 1, 2)	30.88	4.35	310.6
SARIMA(1, 0, 0)(1, 1, 0)[4]	4.79	1.63	206.95

Table 3.1: Statistics of models.

In 3.1 are listed statistics produces by each model. Models with the lowest one step ahead prediction error are seasonal ARIMA and triple exponential smoothing which is correct for this highly seasonal time series.

As it was discussed in 3.2 for models comparison should be used AIC criterion. From the table 3.1 it can be seen that AIC and MSE are related, however MSE of double exponential smoothing is 8.3 times higher than MSE of triple exponential smoothing. Whereas AIC of double exponential smoothing is only 1.3 times higher. From this example it is obvious how AIC discriminates models with more parameters.

## 4 Existing Solutions

Before going directly to the design and implementation let's briefly look at existing monitoring solutions and libraries for time series modelling.

In the next section are described not only direct competitors of Hawkular but also generally available software of this kind. Because Hawkular is still only an upstream project and not deliverable product for the customers thereby as its alternative is considered Jboss Operations Network (JON). This work does not focus on precise comparison of monitoring applications. It is only mentioned for more wider overview of this domain.

### 4.1 Monitoring and Management Platforms

Out there are many monitoring solutions available. Some of them are offered as service (SaaS) and other need to be deployed in customer's environment. For each application are highlighted the most important features and how it differs from its rivals. It is also mentioned if the application offers predictive engine for metric data.

#### 4.1.1 New Relic

New Relic was the first monitoring solution offered as SaaS [4]. It focuses on application performance rather than infrastructure view. Monitoring of Java applications is done by an agent. Because agent manipulates with bytecode it is able to identify business transactions and monitor for instance utilization of REST endpoints. Agent also automatically identifies databases connected to the application being monitored. From alert prediction perspective New Relic does not offer any alert prediction or predictive charts.

#### 4.1.2 Dynatrace Ruxit

Ruxit is another popular SaaS solution for monitoring middleware applications. Monitoring is also done by agents which instruments bytecode so the application is also able to monitor business trans-

actions. Ruxit differs from others that it offers root cause analysis rather than firing multiple alerts [5]. It directly shows causing problems with visual representation. Ruxit does not offer any predictive alerting or charts.

#### 4.1.3 Open Source Projects

As Hawkular is an open source project it is important to mention its direct competitors from this area. There are two major open source projects. The first one is Nagios and second Zabbix. Nagios was started in 1991 and Zabbix in 2001 therefore both are more than fifteen years old. In comparison to Hawkular, Ruxit or New Relic the user interface of these two projects feels much older. By the time of writing this thesis last contribution to Nagios was from 17th September 2015 and Nagios project was active until the last moment. Both these projects does not offer alert prediction.

#### 4.1.4 HP OpenView and IBM Tivoli

The biggest monitoring solutions offered by these two software giants are HP OpenView and IBM Tivoli. Both are composed of many independent products. Solution from HP does not offer any predictive capabilities.

Operations Analytics, one of IBM Tivoli products can automatically detect correlations between metrics which can lead to detection of application issues, for example an anomaly detection [1].

Another part of Tivoli solution – Netcool Network Management is capable of predicting events. There is also another predictive analysis in Tivoli Monitoring module<sup>1</sup> In the online document there is mentioned that predictive engine does not work on real time streams of data. Tivoli is definitely big solution and in order to get real predictive capabilities it would require to contact IBM support.

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1. Available at <https://www.ibm.com/developerworks/community/wikis/home?lang=en#/wiki/Tivoli+Monitoring/page/Details+for+ITPA+Predictive+Analytics+and+Non+Linear+Trending>.

## 4.2 Libraries For Time Series Forecasting

In Java there is only one publicly available library for time series modelling. The library is called OpenForecast<sup>2</sup>. It contains models like naïve, linear regression and exponential smoothings. Whereas the library is open source, code was reviewed and tested. Some assumptions about the implementation were made. The parameters of some models are not estimated correctly. For example in linear regression slope and intercept are not estimated by minimizing sum of squared errors.

The library provides nice feature called automatic forecaster which selects the best model for given time series, however the code produces null pointer exception. The bug was identified but the library is no any more maintained.

Performance of the library was also tested. Table 4.1 contains execution times of optimizers for simple, double and triple exponential smoothing models. The tested time series is generated sine function of length 200 observations. The result is compared against execution times of R's function ets from forecast package.

Model	OpenForecast	R forecast
Simple ex.	4.91 sec.	0.003 sec.
Double ex.	9.31 sec.	0.006 sec.
Triple ex.	6.45 sec.	0.209 sec.

Table 4.1: Execution time of parameters estimation for exponential smoothing models.

From the table it is obvious that R's implementation is much faster. For example optimization of thousand double exponential smoothing models would take about two and half hour. This results are not acceptable for Hawkular in real time environment.

Another possibility is to directly use R implementation. There are various libraries<sup>3</sup> which allow executing R code from Java, however it

2. Available at <http://www.stevengould.org/software/openforecast/index.shtml>.

3. The most widely used: RCaller and JRI.

requires installed R system in the target environment. Other possible solution is to use Rengin<sup>4</sup> – JVM interpreter for R. However forecast package depends on other package which allows invocation of native C++ code for optimized computations. Therefore package forecast can not be used with Rengin.

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4. Available at <http://www.renjin.org/>

## 5 Design and Implementation

The module for an alert prediction is named Hawkular Data Mining. Source code is versioned in Git and hosted on Github<sup>1</sup> under license Apache version 2.0.

The project is split into several Maven artifacts. This approach decomposes problem into smaller parts which have dedicated functionality and can be easy reused in other projects. It also ensures that third party dependencies are loaded only for certain artifacts where are needed.

A figure A.1 shows dependency tree of datamining-dist, which is the top level artifact. The most important modules are listed in 5.1. All ids of the listed artifacts have prefix hawkular-datamining.

Artifact Id	Description
parent	Manages shared dependencies and versions.
forecast	Core library for time series modeling and forecasting.
api	API used within Data Mining.
cdi	Support for context dependency injection.
rest	Web archive for standalone usage without Hawkular.
dist	Web archive with Hawkular integration code.
itest	Artifact for integration tests.

Table 5.1: Hawkular Data Mining modules.

In the following sections the most important parts of the implementation are described. This text work focuse on design of data structures, interaction between modules and algorithms.

### 5.1 Forecast Package

The forecast package is time series modelling and forecasting library. It contains several time series models and utility classes for time series modelling. It is designed to be easy used in any Java project. The

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1. Available at <https://github.com/hawkular/hawkular-datamining>.

footprint of the artifact is small. It depends only on Apache Math, Commons, Guava and Jboss logging.

The core data structures from datamining-forecast package are interfaces of time series models 5.1 and forecasters. This two interfaces are related but not the same. Each time series model should be capable of predicting and learning. Models also collect initialization and running statistics so it is possible to make assumptions of the forecasting accuracy.

The main difference between forecaster and time series model is that forecaster is designed for online learning and it autonomously selects the most appropriate time series model. Time series models by default are not designed for online learning, however it can be accomplished with a wrapper class.

Metric in the Data Mining is represented as structure `MetricContext` which contains metadata like collection interval, metric id and tenant id. Collection interval is necessary for calculating timestamps of predicted points.

Listing 5.1: Interface for time series models.

```
interface TimeSeriesModel {  
    void learn(List<DataPoint> ts);  
    List<DataPoint> forecast(int steps);  
    int numberOfParameters();  
    MetricContext context();  
    AccuracyStatistics initStatistics();  
    AccuracyStatistics runStatistics();  
    ...  
}
```

List of implemented models, statistical and utility classes for time series manipulation:

- |                           |                                  |
|---------------------------|----------------------------------|
| • Simple ex. smoothing    | • Automatic forecaster           |
| • Double ex. smoothing    | • Augmented Dickey – Fuller test |
| • Triple ex. smoothing    | • Time series decomposition      |
| • Weighted moving average | • Autocorrelation function       |

- Time series lagging
- Time series differencing
- Automatic period identification

#### 5.1.1 Automatic Forecaster

One of the most important forecasting classes in Data Mining is `AutomaticForecaster`. This class autonomously decides which time series model should be used for modelled time series. Currently it decides from three implemented models: simple, double and triple exponential smoothing. Other models which implement interface `TimeSeriesModel` can be easily added.

The most importantly this class is capable of dealing with concept drift. It holds circular buffer of historical metrics and if statistical properties of the underlying time series changes content of the buffer is used for selecting new model.

The strategy when a new model should be selected is configurable. System currently supports two strategies. The first strategy periodically each  $n$  observations selects new model. The second one is more sophisticated and it selects a new model only when the error produced on learning data exceeds by  $x\%$  error calculated on learning points when model was initialized.

Model selection is based on information criterion from section 3.2. Automatic forecaster in successive steps calls optimizers of given models and then selects the best with the lowest information criterion. Used criterion is configurable for each forecaster.

#### 5.1.2 Model Optimizers

Model optimizers are the most important part of the models implementation. If the model parameters are not estimated correctly model would produce high forecasting error.

The idea behind optimization is to find such parameters best describes training data [12]. Optimization criterion can be: mean squared error, mean absolute error and likelihood. These criterion basically computes errors produced by ahead predictions. The number of prediction steps depends on the forecaster's objective. The most common is to use only one step ahead. Data Mining currently supports only MSE criterion but others can be easily added.



The criterion is returned from model's objective function. This objective function is then passed to non-linear optimization algorithm from Apache Math Commons. This library implements several optimization algorithms: Nelder-Mead simplex, multi-directional simplex and bound optimization by quadratic approximation (BOBYQA). These algorithms does not need computed derivatives of the cost function.

In terms of the lowest execution time and quality of the estimated parameters the best results were produced by Nelder-Mead simplex algorithm. The quality of estimated parameters were compared to R's estimations.

Table 4.1 contains comparison of optimizers execution times from OpenForecast and R implementation. This section adds execution time of Data Mining implementation. Complete execution times are listed in 5.2. Execution times of Data Mining's optimizers are in some cases faster than R. Quality of the produced forecasts is discussed in the chapter 6.

Model	OpenForecast	R forecast	Data Mining
Simple ex.	4.91 sec.	0.003 sec.	0.033 sec.
Double ex.	9.31 sec.	0.006 sec.	0.002 sec.
Triple ex.	6.45 sec.	0.209 sec.	0.023 sec.

Table 5.2: Execution time of parameters estimation for exponential smoothing models.

## 5.2 API Package

The next package is api. It depends on forecast and it eventually could depend on another library for data analysis, for instance a library for an outlier detection. In this package there is a code necessary for using Data Mining as a web application, for example classes for accessing data analysis objects for given metric.

The interface SubscriptionManager was designed for accessing time series analysis objects. Some of its methods are listed in 5.2. Implementation of this interface could store entities in database. How-

ever, Data Mining directly does not use any database. Therefore SubscriptionManager holds all objects in memory. Internally it stores objects in a map where the key is tenant and value another map where the key is metric id and value the object for data analysis – Subscription.

Listing 5.2: Interface SubscriptionManager.

```
interface SubscriptionManager {  
    void subscribe(Subscription , Owner);  
    void unsubscribe(tenant , metric , Owner);  
    Subscription model(tenant , metric );  
    ...  
}
```

For subscribing it is necessary to specify the owner of the prediction configuration. It was specially added for integration with Ineventory. It is more described in section 5.4.

Object Subscription holds instance of AutomaticForecaster and it could also hold another data analysis objects. Its role is to delegates calls to the business logic objects.

Class diagram of the most important classes from forecast and api is in A.2.

Some of the service classes like SubscriptionManager are used in several other classes and also multiple implementation could exists (in memory or database implementation). Therefore dependency injection design pattern was introduced. Used technology is Java context dependency injection (CDI). In order to keep API classes clean module cdi with CDI configuration was introduced. It directly depends on api, but does not add any other functionality.

### 5.3 REST Package

Package rest contains implementation of REST services provided by Data Mining. Implementation is compatible with standard JAX-RS.

Data Mining REST API is designed to operate on the forecasting engine. When the module is deployed into Hawkular main interaction with Data Mining goes through Inventory REST API and metric data are collected from JMS topic. However, this is not limited and Data Mining offers alternative REST endpoints which can be used

for example in standalone deployment.

REST API provides following capabilities:

- Operate on subscriptions – enable and disable prediction.
- Push learning data to the engine.
- Get predictions for any number of steps ahead.
- Configure automatic forecaster.
- Get information about model being used and statistics of the predictions.

Accurate and more comprehensive REST API documentation is available on Hawkular web page<sup>2</sup>. This documentation is automatically generated using Swagger framework.

### 5.4 Distribution Package – Integration into Hawkular

As it was mentioned before the build produces two web archives, one for standalone usage and another for deployment into Hawkular. The second web archive adds extra functionality for interacting with other Hawkular components. Hawkular is packaged as a modified Wildfly server with several Hawkular components deployed.

In Hawkular all entities are stored in Inventory, therefore Data Mining uses this module for querying metric definitions and it adds some extra attributes necessary for predictions. Another module which is used by Data Mining is Hawkular Metrics. Diagram 5.1 shows Data Mining integration into Hawkular.

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2. Available at <http://www.hawkular.org/>.

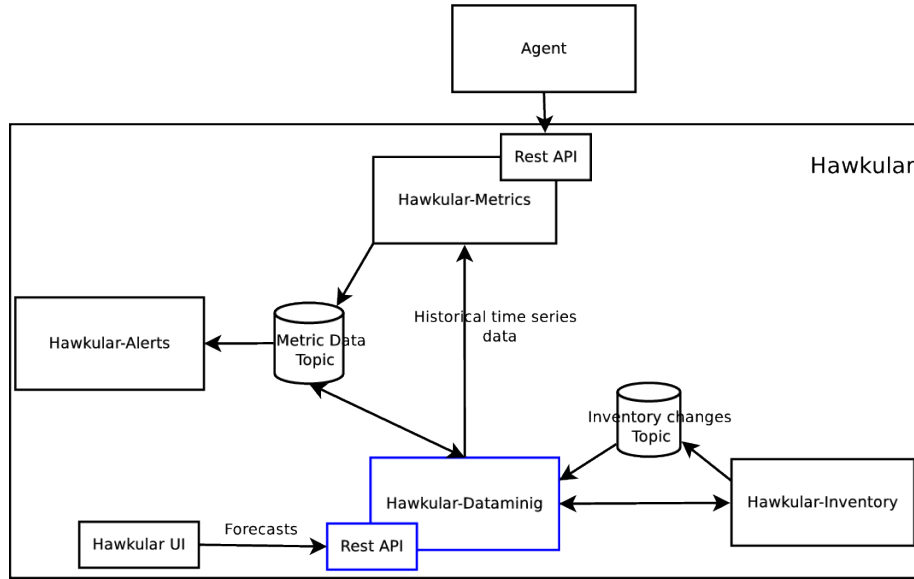


Figure 5.1: The integration into Hawkular.

When Data Mining is deployed into Hawkular users can enable predictions by creating Relationship<sup>3</sup> from tenant to the target entity. Target entity can be metric, metric type or tenant. When relationship is created from tenant to tenant predictions are enabled for all metrics under given tenant. Similarly, when a target entity is a metric type, predictions are enabled for all metrics of that type. In the figure 5.2 is depicted part of the structure of inventory with enabled predictions.

Relationships also store properties needed for predictions. One of them is forecasting horizon which tells how many prediction steps are performed for each incoming metric data point. With this approach of storing relationships in Inventory, Data Mining doesn't have to use any database for entities related to predictions. This approach was achieved without any changes to Inventory data model, this shows that Inventory's generic data model build on top of graph database<sup>4</sup> is good approach for storing data model in this domain.

3. Entity from Inventory which can be created between arbitrary two entities.

4. Compatible with Apache Tinkerpop.

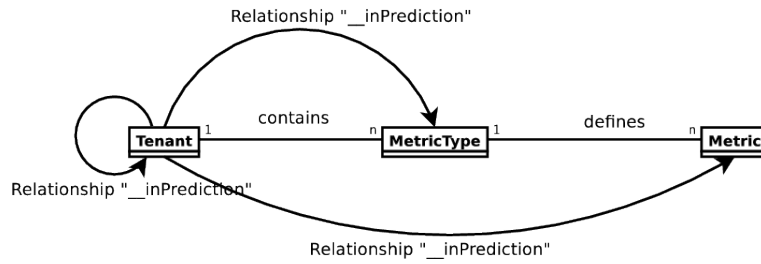


Figure 5.2: Relationship between entities of Inventory.

Any changes in Inventory are propagated to Data Mining by subscribing to specific events. This propagation is done through JMS topic where Inventory sends these events. However on application start Data Mining also needs to query all predictive relationships from inventory. For this purpose JMS request-response communication was implemented in Inventory. Any component which has access to internal messaging subsystem can construct a query and send it for execution to Inventory. REST API approach was also proposed but it could expose vulnerability – client could access any data objects of any tenant. Diagram 5.3 depicts sequence of calls when prediction gets enabled.

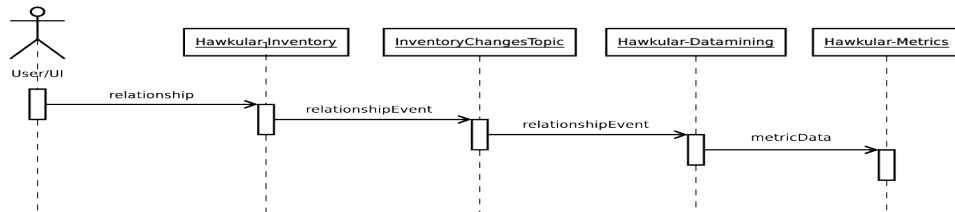


Figure 5.3: Sequence diagram of enabling predictions.

From the diagram 5.3 it is clear that when a prediction gets enabled historical metrics are queried from Metrics module. This means that Data Mining needs to access metrics of all tenants. It is similar scenario to getting all predictive relationships from Inventory. It could not be implemented via REST API because of potential vulnerability and JMS based query was rejected by Metrics owners.

Another two solutions were proposed. The first was to bypass Metrics and query data directly from Cassandra. The second was to inject Metrics as CDI bean and directly use its Java API. The first solution was refused because the schema is maintained by Metrics and it can eventually change and also the backed database (Cassandra) can change. The final and implemented solution injects Metrics as CDI bean. This approach assumes that Metrics are deployed in the same application server as Data Mining. From the performance perspective it is faster than JMS or REST calls.

Diagram 5.4 shows complete data flow from agent to alerts evaluation engine. First metric data is sent by agent to Metrics where it is stored to database. Then it is sent to JMS topic and consumed by Alerts and Data Mining. In parallel Alerts evaluates alerts criteria and Data Mining computes predictions. After computation the predicted data are sent back to the same JMS topic and consumed by Alerts. At this point an alert of predicted metrics can be triggered.

Data Mining changes id of predicted points in order to be able to distinguish original time series from predicted. For predicted metrics Alerts can evaluate the same conditions as for original time series or use different ones, more in 5.4.1.

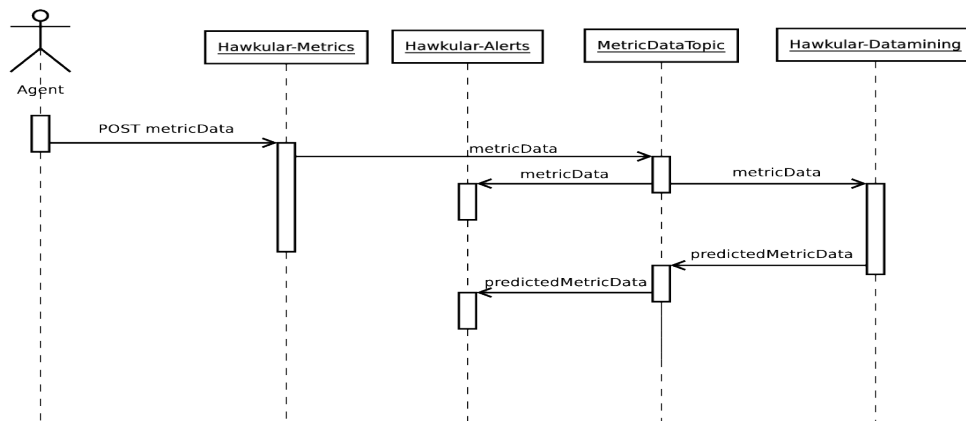


Figure 5.4: Sequence diagram of incoming data from agent.

### 5.4.1 Alerts and Conditions

In this section is briefly described how the alerting system works. Alerts is a separate module which is responsible for firing alerts based on defined conditions. As it is depicted in diagram 5.4 Alerts listens on the JMS topic and if conditions for given metric are positively evaluated an alert is fired.

Though Alerts data model is little bit more complicated. For each unique metric id can be defined multiple conditions. These conditions are evaluated for every received metric data point on the bus. Conditions are grouped under a trigger. If the result of evaluation is positive than the trigger triggers an action. This action can be for instance send an email, sms or perform a webhook...

Triggers can be grouped which facilitates creation of the similar triggers. Particularly this can be used for creating trigger for predictive metrics. If there is a trigger defined for the original metric it can be duplicated and used on predicted values of that metric. If necessary the conditions can be changed in order to not trigger an alert if the predictions are not very accurate. For this can be used trigger dampening. So for the trigger which operates on predicted metrics dampening can be set as follows: *"fire an alert if X consecutive evaluations of conditions are positive"*.

### 5.4.2 Hawkular UI

Predictive charts in Hawkular are located in Metric explorer tab. In the figure 5.5 is showed predictive chart for metric accumulated garbage collection duration. In this case automatic forecaster decided to use seasonal model of some automatically identified period. Note that for displaying original time series in the chart buckets were used, so the periods would be more easily seen on raw data points.

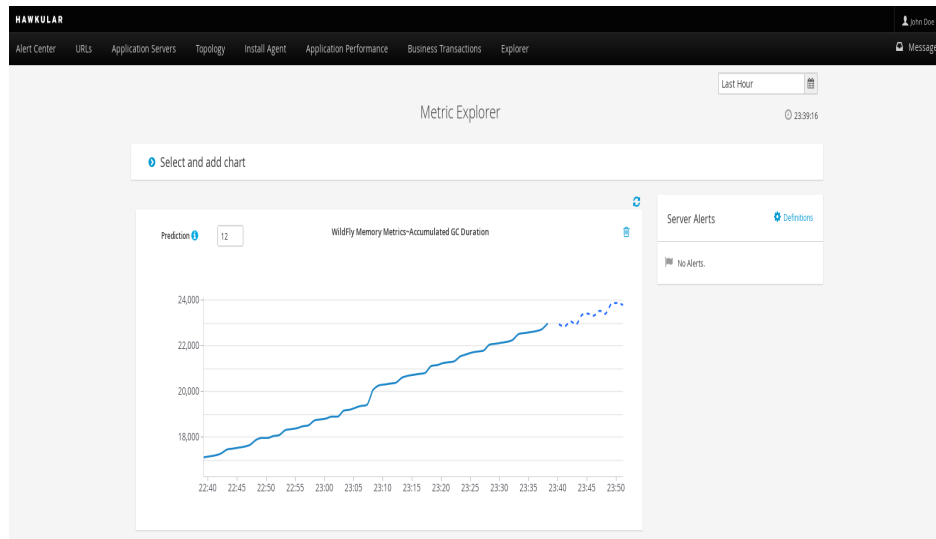


Figure 5.5: Metric explorer tab in Hawkular user interface.

After adding concrete chart predictions can be enabled by increasing prediction horizon input. So there is no need to enable predictions manually by creating relationship in Inventory.

Predictive charts were used from repository hawkular-charts. These charts are built on top of D3<sup>5</sup> library and encapsulated as Angular directives.

## 5.5 Test Automation and Documentation

Core functionality of the application is covered by unit tests. Junit framework is used for this type of tests. Because Data Mining interacts with other applications and modules integration tests are also implemented. These tests are run from Maven profile which starts web server with necessary modules deployed.

The last type of implemented tests are end-to-end tests which calls REST endpoint of one module and expect result in call from another module. This type of tests are also executed in Maven profile with

5. Available at <https://d3js.org/>.



running web server. End-to-end tests for Data Mining project live in the main Hawkular integration repository<sup>6</sup>.

All tests are automatically executed every time developer creates a pull request or pushes code to the master branch. For this Travis continuous integration platform was used which is for free for open source projects on Github.

Documentation is directly written in Java code as javadoc. REST API documentation is also directly written in source code using Swagger framework and automatically generated at build time<sup>7</sup>.

## 5.6 Releases

By the time writing of this thesis there was only one release with version 0.1.Final. It is also available in the Maven central repository. Complete group id is `org.hawkular.datamining`. The most important artifact ids are listed in 5.1. Release notes are available on Github<sup>8</sup>.

## 5.7 Retrospective

In this section is mentioned how the project was changing during the implementation, what did not worked well and what could have be done better.

At the beginning of the project Apache Spark<sup>9</sup> was used for building regression models. Its machine learning library (MLIB) offers several learning algorithms. In Data Mining linear regression with stochastic gradient descent was used. Because the gradient is stochastic produced predictions are not very robust and quickly change by significant value.

Spark was mainly used because of its streaming extension that can handle high-throughput stream data [3]. There is also time series

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6. Available at <https://github.com/hawkular/hawkular>.

7. Available at <http://www.hawkular.org/docs/rest/rest-datamining.html>.

8. Available at <https://github.com/hawkular/hawkular-datamining/releases>.

9. Open source cluster computing framework available at <https://spark.apache.org/>.

library `spark-ts`<sup>10</sup> which contains some time series models but does not offer functionality of automatic model selection.

Due to problems discussed in 2.2 and lack of automatic forecaster decision was made to drop Spark and directly implement exponential smoothing models.

During the implementation a lot of time was spent on integration with other modules, in particular with Inventory. The problem was that Inventory is developed by another party and any concrete document describing the integration was not proposed. The design of the integration was understood differently by both parties, what lead to reimplementing of some parts. Therefore it is better to precisely define the integration interface with other modules or projects.

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10. Available at <https://github.com/sryza/spark-timeseries>.

## **6 Evaluation of Implemented Models**

TODO Do an example how to generate an alert.

### **6.1 Prediction capabilities**

Show prediction capabilities of implemented models. TODO Can I compare it against R implementation?

### **6.2 The Most Important Metrics**

TODO select subset of the most important metrics and show on them predictions.

## 7 Conclusion

TODO

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## A Diagrams

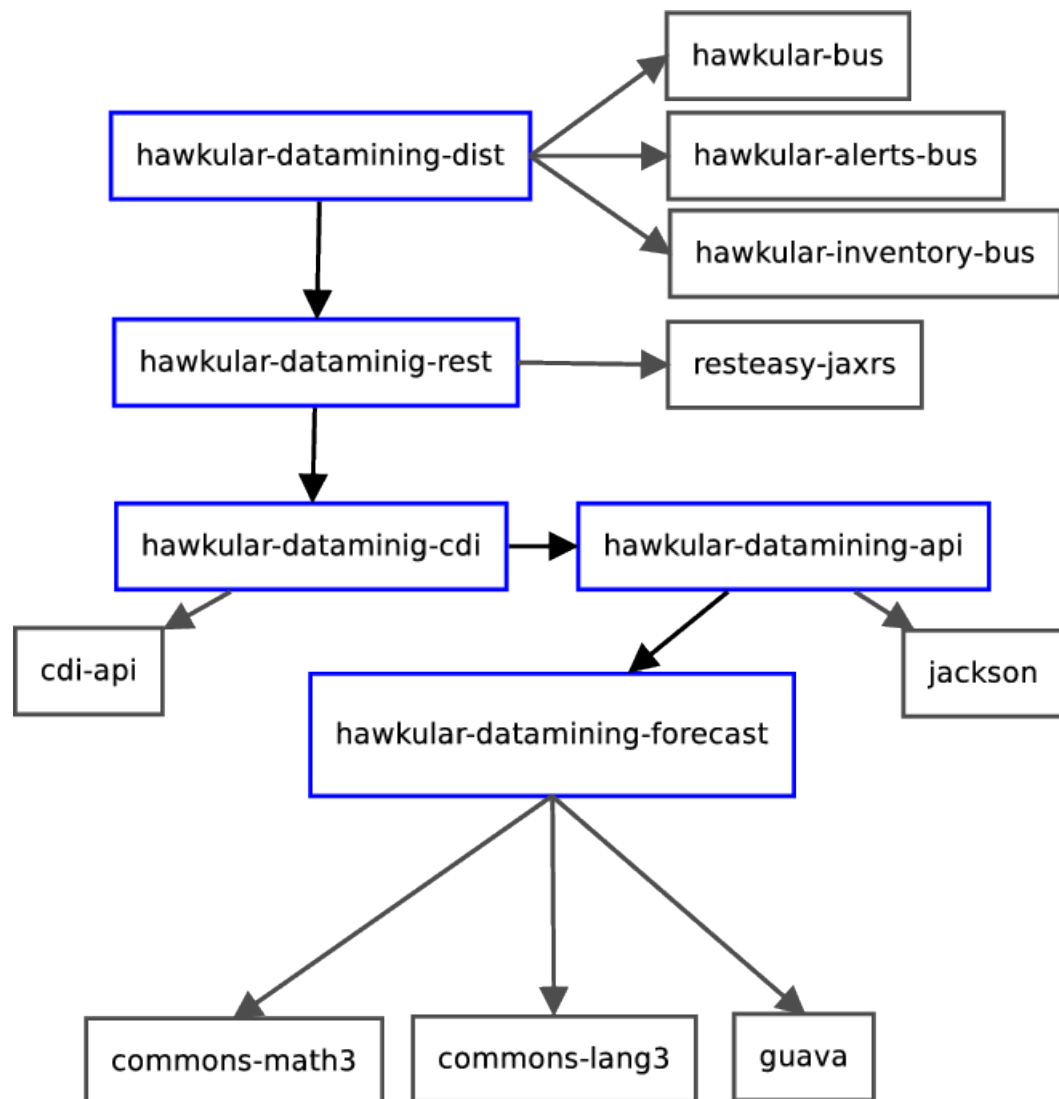
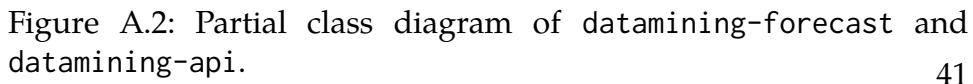


Figure A.1: Dependency tree of maven artifacts.





## B Predictive Charts

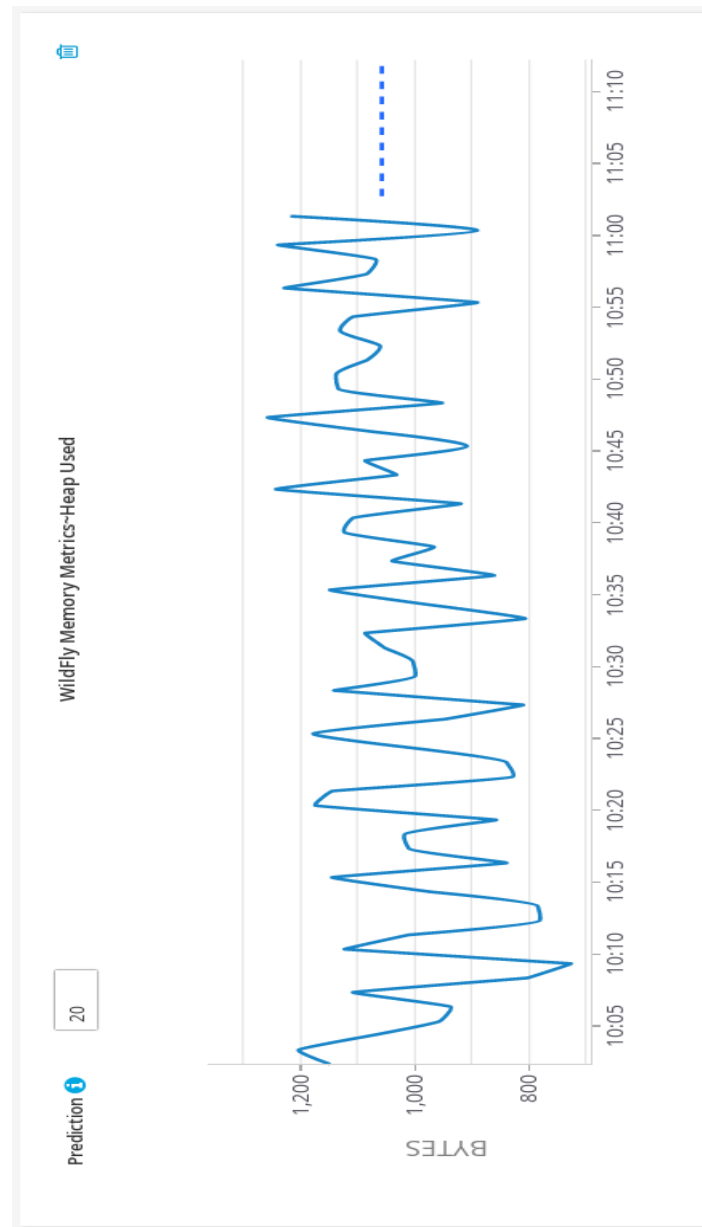


Figure B.1: Predictive chart for simple exponential smotohing.

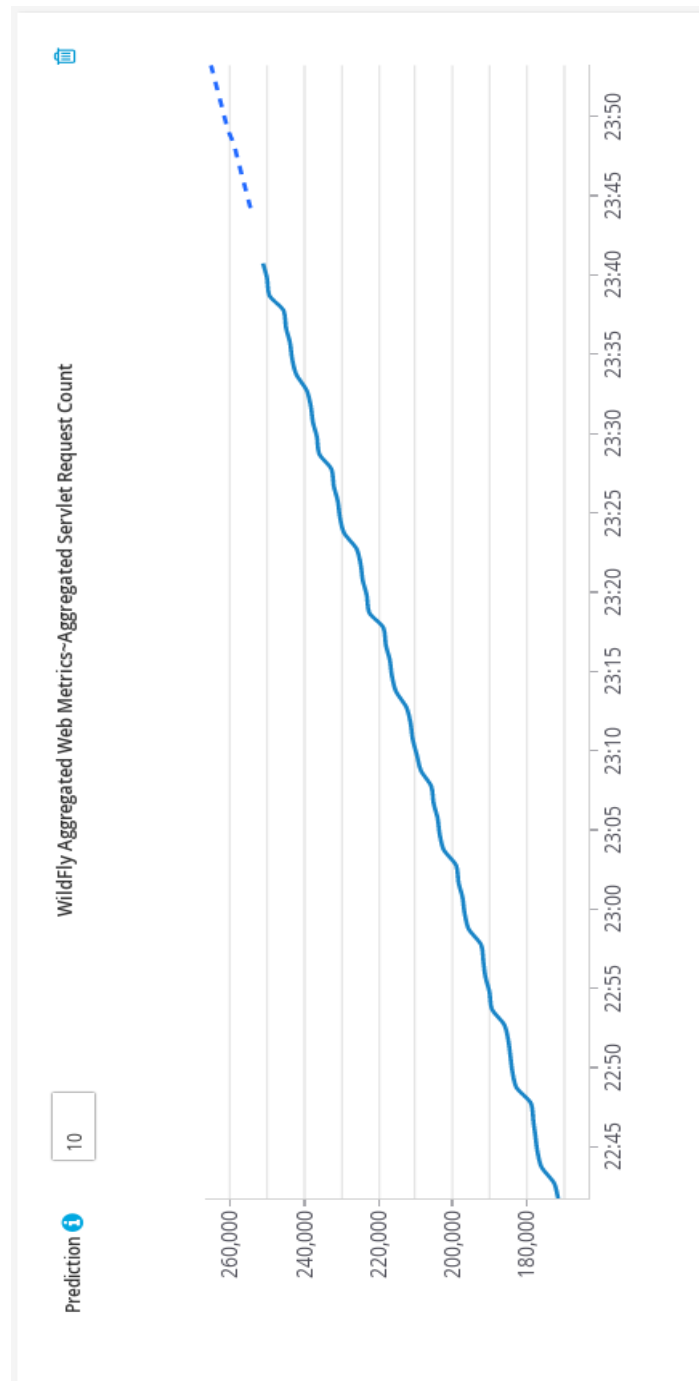


Figure B.2: Predictive chart for double exponential smooting.

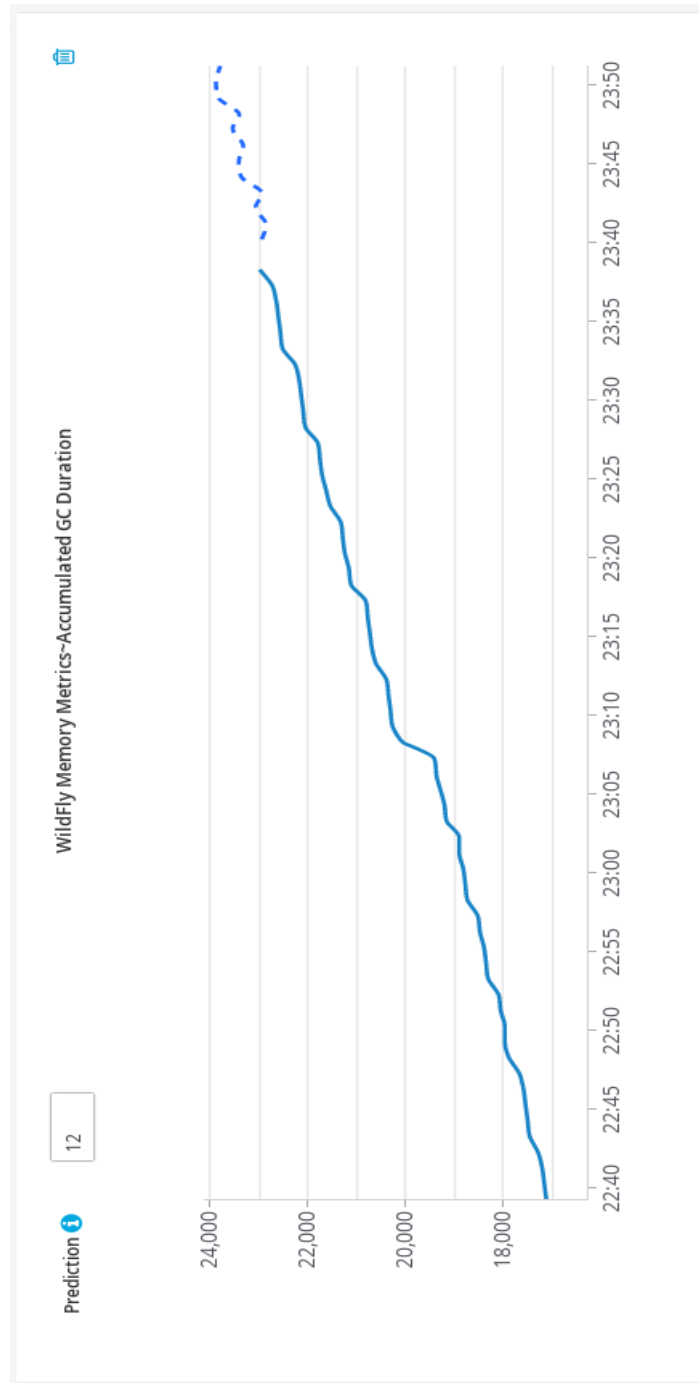


Figure B.3: Predictive chart for triple exponential smotohing.

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