# Personalized cancer diagnosis

## 1. Business Problem

# 1.1. Description

Source: https://www.kaggle.com/c/msk-redefining-cancer-treatment/

Data: Memorial Sloan Kettering Cancer Center (MSKCC)

Download training\_variants.zip and training\_text.zip from Kaggle.

#### Context:

Source: https://www.kaggle.com/c/msk-redefining-cancer-treatment/discussion/35336#198462

#### Problem statement:

Classify the given genetic variations/mutations based on evidence from text-based clinical literature.

## 1.2. Source/Useful Links

Some articles and reference blogs about the problem statement

- https://www.forbes.com/sites/matthewherper/2017/06/03/a-new-cancer-drug-helped-almost-everyone-who-took-it-almost-heres-what-it-teaches-us/#2a44ee2f6b25
- 2. <a href="https://www.youtube.com/watch?v=UwbuW7oK8rk">https://www.youtube.com/watch?v=UwbuW7oK8rk</a>
- 3. https://www.youtube.com/watch?v=qxXRKVompI8

## 1.3. Real-world/Business objectives and constraints.

- No low-latency requirement.
- · Interpretability is important.
- Errors can be very costly.
- Probability of a data-point belonging to each class is needed.

# 2. Machine Learning Problem Formulation

## 2.1. Data

#### 2.1.1. Data Overview

- Source: <a href="https://www.kaggle.com/c/msk-redefining-cancer-treatment/data">https://www.kaggle.com/c/msk-redefining-cancer-treatment/data</a>
- We have two data files: one conatins the information about the genetic mutations and the other contains the clinical evidence (text) that human experts/pathologists use to classify the genetic mutations.
- Both these data files are have a common column called ID
- · Data file's information:
  - training\_variants (ID , Gene, Variations, Class)
  - training text (ID, Text)

## 2.1.2. Example Data Point

#### training\_variants

ID,Gene,Variation,Class 0,FAM58A,Truncating Mutations,1 1,CBL,W802\*,2 2,CBL,Q249E,2

...

### training\_text

#### ID.Text

0||Cyclin-dependent kinases (CDKs) regulate a variety of fundamental cellular processes. CDK10 stands out as one of the last orphan CDKs for which no activating cyclin has been identified and no kinase activity revealed. Previous work has shown that CDK10 silencing increases ETS2 (v-ets erythroblastosis virus E26 oncogene homolog 2)-driven activation of the MAPK pathway, which confers tamoxifen resistance to breast cancer cells. The precise mechanisms by which CDK10 modulates ETS2 activity, and more generally the functions of CDK10, remain elusive. Here we demonstrate that CDK10 is a cyclin-dependent kinase by identifying cyclin M as an activating cyclin. Cyclin M, an orphan cyclin, is the product of FAM58A, whose mutations cause STAR syndrome, a human developmental anomaly whose features include toe syndactyly, telecanthus, and anogenital and renal malformations. We show that STAR syndrome-associated cyclin M mutants are unable to interact with CDK10. Cyclin M silencing phenocopies CDK10 silencing in increasing c-Raf and in conferring tamoxifen resistance to breast cancer cells. CDK10/cyclin M phosphorylates ETS2 in vitro, and in cells it positively controls ETS2 degradation by the proteasome. ETS2 protein levels are increased in cells derived from a STAR patient, and this increase is attributable to decreased cyclin M levels. Altogether, our results reveal an additional regulatory mechanism for ETS2, which plays key roles in cancer and development. They also shed light on the molecular mechanisms underlying STAR syndrome. Cyclin-dependent kinases (CDKs) play a pivotal role in the control of a number of fundamental cellular processes (1). The human genome contains 21 genes encoding proteins that can be considered as members of the CDK family owing to their sequence similarity with bona fide CDKs, those known to be activated by cyclins (2). Although discovered almost 20 y ago (3, 4), CDK10 remains one of the two CDKs without an identified cyclin partner. This knowledge gap has largely impeded the exploration of its biological functions. CDK10 can act as a positive cell cycle regulator in some cells (5, 6) or as a tumor suppressor in others (7, 8). CDK10 interacts with the ETS2 (v-ets erythroblastosis virus E26 oncogene homolog 2) transcription factor and inhibits its transcriptional activity through an unknown mechanism (9). CDK10 knockdown derepresses ETS2, which increases the expression of the c-Raf protein kinase, activates the MAPK pathway, and induces resistance of MCF7 cells to tamoxifen (6). ...

# 2.2. Mapping the real-world problem to an ML problem

## 2.2.1. Type of Machine Learning Problem

There are nine different classes a genetic mutation can be classified into => Multi class classification problem

### 2.2.2. Performance Metric

Source: https://www.kaggle.com/c/msk-redefining-cancer-treatment#evaluation

Metric(s):

- · Multi class log-loss
- Confusion matrix

## 2.2.3. Machine Learing Objectives and Constraints

Objective: Predict the probability of each data-point belonging to each of the nine classes.

Constraints:

- Interpretability
- Class probabilities are needed.
- Penalize the errors in class probabilites => Metric is Log-loss.
- No Latency constraints.

## 2.3. Train, CV and Test Datasets

Split the dataset randomly into three parts train, cross validation and test with 64%,16%, 20% of data respectively

# 3. Exploratory Data Analysis

In [1]:

```
import pandas as pd
import matplotlib.pyplot as plt
import re
import time
import warnings
import numpy as np
from nltk.corpus import stopwords
from sklearn.decomposition import TruncatedSVD
from sklearn.preprocessing import normalize
from sklearn.feature_extraction.text import CountVectorizer
from sklearn.manifold import TSNE
import seaborn as sns
from sklearn.neighbors import KNeighborsClassifier
from sklearn.metrics import confusion matrix
from sklearn.metrics.classification import accuracy score, log loss
from sklearn.feature extraction.text import TfidfVectorizer
from sklearn.linear model import SGDClassifier
from imblearn.over sampling import SMOTE
from collections import Counter
from scipy.sparse import hstack
from sklearn.multiclass import OneVsRestClassifier
#from sklearn import OneVsRestClassifier
from sklearn.svm import SVC
from sklearn.model selection import StratifiedKFold
from collections import Counter, defaultdict
from sklearn.calibration import CalibratedClassifierCV
from sklearn.naive bayes import MultinomialNB
from sklearn.naive bayes import GaussianNB
from sklearn.model selection import train test split
from sklearn.model selection import GridSearchCV
import math
from sklearn.metrics import normalized mutual info score
from sklearn.ensemble import RandomForestClassifier
warnings.filterwarnings("ignore")
from mlxtend.classifier import StackingClassifier
from sklearn import model selection
from sklearn.linear model import LogisticRegression
```

# 3.1. Reading Data

In [2]:

Out[2]:

## 3.1.1. Reading Gene and Variation Data

```
data = pd.read_csv('training_variants')
print('Number of data points : ', data.shape[0])
print('Number of features : ', data.shape[1])
print('Features : ', data.columns.values)
data.head()

Number of data points : 3321
Number of features : 4
Features : ['ID' 'Gene' 'Variation' 'Class']
```

ID	Gene	Variation	Class

0	Ю	FA <b>66</b>	Truncating Mutations	class
1	1	CBL	W802*	2
2	2	CBL	Q249E	2
3	3	CBL	N454D	3
4	4	CBL	L399V	4

training/training\_variants is a comma separated file containing the description of the genetic mutations used for training. Fields are

- ID: the id of the row used to link the mutation to the clinical evidence
- Gene: the gene where this genetic mutation is located
- Variation: the aminoacid change for this mutations
- Class: 1-9 the class this genetic mutation has been classified on

## 3.1.2. Reading Text Data

#### In [3]:

```
# note the separator in this file
data_text =pd.read_csv("training_text",sep="\|\\|",engine="python",names=["ID","TEXT"],skiprows=1)
print('Number of data points : ', data_text.shape[0])
print('Number of features : ', data_text.shape[1])
print('Features : ', data_text.columns.values)
data_text.head()
```

```
Number of data points: 3321
Number of features: 2
Features: ['ID' 'TEXT']
```

#### Out[3]:

	ID	ТЕХТ
0	0	Cyclin-dependent kinases (CDKs) regulate a var
1	1	Abstract Background Non-small cell lung canc
2	2	Abstract Background Non-small cell lung canc
3	3	Recent evidence has demonstrated that acquired
4	4	Oncogenic mutations in the monomeric Casitas B

## 3.1.3. Preprocessing of text

## In [4]:

```
string += word + " "

data_text[column][index] = string

In [5]:
```

```
#text processing stage.
start_time = time.clock()
for index, row in data_text.iterrows():
    if type(row['TEXT']) is str:
        nlp_preprocessing(row['TEXT'], index, 'TEXT')
    else:
        print("there is no text description for id:",index)
print('Time took for preprocessing the text :',time.clock() - start_time, "seconds")
```

```
there is no text description for id: 1109
there is no text description for id: 1277
there is no text description for id: 1407
there is no text description for id: 1639
there is no text description for id: 2755
Time took for preprocessing the text : 379.25390385832304 seconds
```

### In [6]:

```
#merging both gene_variations and text data based on ID
result = pd.merge(data, data_text,on='ID', how='left')
result.head()
```

#### Out[6]:

	ID	Gene	Variation	Class	ТЕХТ
0	0	FAM58A	Truncating Mutations	1	cyclin dependent kinases cdks regulate variety
1	1	CBL	W802*	2	abstract background non small cell lung cancer
2	2	CBL	Q249E	2	abstract background non small cell lung cancer
3	3	CBL	N454D	3	recent evidence demonstrated acquired uniparen
4	4	CBL	L399V	4	oncogenic mutations monomeric casitas b lineag

## In [7]:

```
result[result.isnull().any(axis=1)]
```

## Out[7]:

	ID	Gene	Variation	Class	TEXT
1109	1109	FANCA	S1088F	1	NaN
1277	1277	ARID5B	Truncating Mutations	1	NaN
1407	1407	FGFR3	K508M	6	NaN
1639	1639	FLT1	Amplification	6	NaN
2755	2755	BRAF	G596C	7	NaN

#### In [8]:

```
result.loc[result['TEXT'].isnull(),'TEXT'] = result['Gene'] +' '+result['Variation']
```

## In [9]:

```
result[result['ID']==1109]
```

```
Out[9]:
```

	ID	Gene	Variation	Class	TEXT
1109	1109	FANCA	S1088F	1	FANCA S1088F

## 3.1.4. Test, Train and Cross Validation Split

#### 3.1.4.1. Splitting data into train, test and cross validation (64:20:16)

#### In [10]:

```
y_true = result['Class'].values
result.Gene = result.Gene.str.replace('\s+', '_')
result.Variation = result.Variation.str.replace('\s+', '_')

# split the data into test and train by maintaining same distribution of output varaible 'y_true'
[stratify=y_true]
X_train, test_df, y_train, y_test = train_test_split(result, y_true, stratify=y_true, test_size=0.2)
# split the train data into train and cross validation by maintaining same distribution of output
varaible 'y_train' [stratify=y_train]
train_df, cv_df, y_train, y_cv = train_test_split(X_train, y_train, stratify=y_train, test_size=0.2)
```

We split the data into train, test and cross validation data sets, preserving the ratio of class distribution in the original data set

#### In [11]:

```
print('Number of data points in train data:', train_df.shape[0])
print('Number of data points in test data:', test_df.shape[0])
print('Number of data points in cross validation data:', cv_df.shape[0])

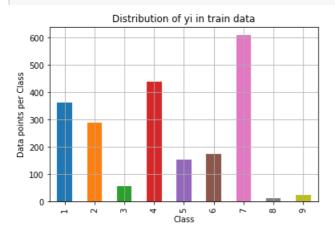
Number of data points in train data: 2124
Number of data points in test data: 665
Number of data points in cross validation data: 532
```

## 3.1.4.2. Distribution of y\_i's in Train, Test and Cross Validation datasets

## In [12]:

```
# it returns a dict, keys as class labels and values as the number of data points in that class
train class distribution = train df['Class'].value counts().sortlevel()
test class distribution = test df['Class'].value counts().sortlevel()
cv_class_distribution = cv_df['Class'].value_counts().sortlevel()
my colors = 'rgbkymc'
train class distribution.plot(kind='bar')
plt.xlabel('Class')
plt.ylabel('Data points per Class')
plt.title('Distribution of yi in train data')
plt.grid()
plt.show()
# ref: argsort https://docs.scipy.org/doc/numpy/reference/generated/numpy.argsort.html
# -(train_class_distribution.values): the minus sign will give us in decreasing order
sorted yi = np.argsort(-train class distribution.values)
for i in sorted yi:
   print('Number of data points in class', i+1, ':',train class distribution.values[i], '(', np.ro
und((train class distribution.values[i]/train df.shape[0]*100), 3), '%)')
print('-'*80)
my colors = 'rgbkymc'
test class distribution.plot(kind='bar')
plt.xlabel('Class')
plt.ylabel('Data points per Class')
plt.title('Distribution of yi in test data')
plt.grid()
plt.show()
```

```
# ref: argsort https://docs.scipy.org/doc/numpy/reference/generated/numpy.argsort.html
# -(train_class_distribution.values): the minus sign will give us in decreasing order
sorted yi = np.argsort(-test class distribution.values)
for i in sorted yi:
   print('Number of data points in class', i+1, ':',test_class_distribution.values[i], '(', np.rou
nd((test class distribution.values[i]/test df.shape[0]*100), 3), '%)')
print('-'*80)
my colors = 'rgbkymc'
cv class distribution.plot(kind='bar')
plt.xlabel('Class')
plt.ylabel('Data points per Class')
plt.title('Distribution of yi in cross validation data')
plt.grid()
plt.show()
# ref: argsort https://docs.scipy.org/doc/numpy/reference/generated/numpy.argsort.html
# -(train class distribution.values): the minus sign will give us in decreasing order
sorted yi = np.argsort(-train class distribution.values)
for i in sorted yi:
   print('Number of data points in class', i+1, ':',cv_class_distribution.values[i], '(', np.round
((cv class distribution.values[i]/cv df.shape[0]*100), 3), '%)')
```



```
Number of data points in class 7 : 609 ( 28.672 %)

Number of data points in class 4 : 439 ( 20.669 %)

Number of data points in class 1 : 363 ( 17.09 %)

Number of data points in class 2 : 289 ( 13.606 %)

Number of data points in class 6 : 176 ( 8.286 %)

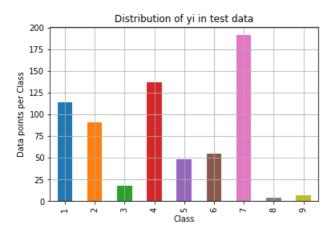
Number of data points in class 5 : 155 ( 7.298 %)

Number of data points in class 3 : 57 ( 2.684 %)

Number of data points in class 9 : 24 ( 1.13 %)

Number of data points in class 8 : 12 ( 0.565 %)
```

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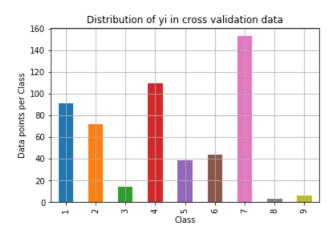


```
Number of data points in class 7 : 191 ( 28.722 %) Number of data points in class 4 : 137 ( 20.602 %) Number of data points in class 1 : 114 ( 17.143 %) Number of data points in class 2 : 91 ( 13.684 %) Number of data points in class 6 : 55 ( 8.271 %) Number of data points in class 5 : 48 ( 7.218 %)
```

```
Number of data points in class 3 : 18 ( 2.707 %)

Number of data points in class 9 : 7 ( 1.053 %)

Number of data points in class 8 : 4 ( 0.602 %)
```



```
Number of data points in class 7 : 153 ( 28.759 %)

Number of data points in class 4 : 110 ( 20.677 %)

Number of data points in class 1 : 91 ( 17.105 %)

Number of data points in class 2 : 72 ( 13.534 %)

Number of data points in class 6 : 44 ( 8.271 %)

Number of data points in class 5 : 39 ( 7.331 %)

Number of data points in class 3 : 14 ( 2.632 %)

Number of data points in class 9 : 6 ( 1.128 %)

Number of data points in class 8 : 3 ( 0.564 %)
```

# 3.2 Prediction using a 'Random' Model

In a 'Random' Model, we generate the NINE class probabilites randomly such that they sum to 1.

#### In [13]:

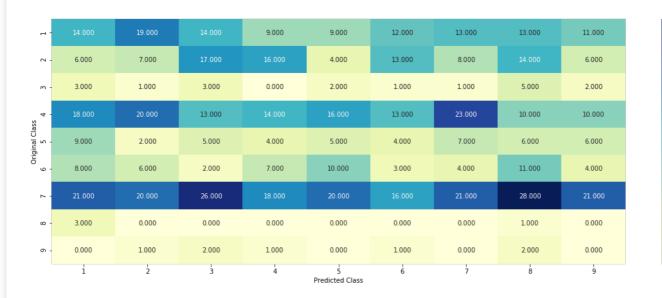
```
# This function plots the confusion matrices given y_i, y_i_hat.
def plot_confusion_matrix(test_y, predict_y):
   C = confusion_matrix(test_y, predict_y)
    \# C = 9,9 matrix, each cell (i,j) represents number of points of class i are predicted class j
    A = (((C.T)/(C.sum(axis=1))).T)
    #divid each element of the confusion matrix with the sum of elements in that column
    \# C = [[1, 2],
         [3, 4]]
    # C.T = [[1, 3],
    # C.sum(axis = 1) axis=0 corresonds to columns and axis=1 corresponds to rows in two
diamensional array
   \# C.sum(axix = 1) = [[3, 7]]
    \# ((C.T)/(C.sum(axis=1))) = [[1/3, 3/7]
    # ((C.T)/(C.sum(axis=1))).T = [[1/3, 2/3]
                                [3/7, 4/7]]
    # sum of row elements = 1
    B = (C/C.sum(axis=0))
    #divid each element of the confusion matrix with the sum of elements in that row
    \# C = [[1, 2],
         [3, 4]]
    # C.sum(axis = 0) axis=0 corresonds to columns and axis=1 corresponds to rows in two
diamensional array
   \# C.sum(axix = 0) = [[4, 6]]
    \# (C/C.sum(axis=0)) = [[1/4, 2/6],
                           [3/4, 4/6]]
    labels = [1,2,3,4,5,6,7,8,9]
    # representing A in heatmap format
    print ("-"*20. "Confusion matrix". "-"*20)
```

```
CONTROLON MACLEN,
plt.figure(figsize=(20,7))
sns.heatmap(C, annot=True, cmap="YlGnBu", fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.show()
print("-"*20, "Precision matrix (Column Sum=1)", "-"*20)
plt.figure(figsize=(20,7))
sns.heatmap(B, annot=True, cmap="YlGnBu", fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.show()
# representing B in heatmap format
print("-"*20, "Recall matrix (Row sum=1)", "-"*20)
plt.figure(figsize=(20,7))
sns.heatmap(A, annot=True, cmap="YlGnBu", fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.show()
```

## In [14]:

```
\# we need to generate 9 numbers and the sum of numbers should be 1
# one solution is to genarate 9 numbers and divide each of the numbers by their sum
# ref: https://stackoverflow.com/a/18662466/4084039
test_data_len = test df.shape[0]
cv_data_len = cv_df.shape[0]
# we create a output array that has exactly same size as the CV data
cv predicted y = np.zeros((cv data len,9))
for i in range(cv_data_len):
    rand probs = np.random.rand(1,9)
    cv predicted y[i] = ((rand probs/sum(sum(rand probs)))[0])
print("Log loss on Cross Validation Data using Random Model",log loss(y cv,cv predicted y, eps=1e-
15))
# Test-Set error.
#we create a output array that has exactly same as the test data
test_predicted_y = np.zeros((test_data_len,9))
for i in range(test data len):
    rand probs = np.random.rand(1,9)
    test_predicted_y[i] = ((rand_probs/sum(sum(rand_probs)))[0])
print("Log loss on Test Data using Random Model", log loss(y test, test predicted y, eps=1e-15))
predicted_y =np.argmax(test_predicted_y, axis=1)
plot confusion matrix(y test, predicted y+1)
```

Log loss on Cross Validation Data using Random Model 2.456814966189978 Log loss on Test Data using Random Model 2.479952691325209 ------ Confusion matrix ------

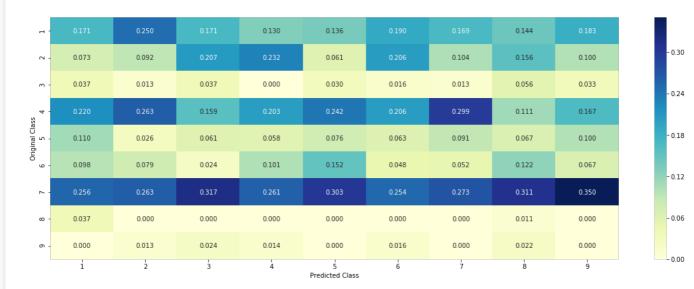


- 20

- 15

- 10

- 5



----- Recall matrix (Row sum=1) -----



# 3.3 Univariate Analysis

#### In [15]:

```
# code for response coding with Laplace smoothing.
# alpha : used for laplace smoothing
# feature: ['gene', 'variation']
# df: ['train_df', 'test_df', 'cv_df']
# algorithm
# Consider all unique values and the number of occurances of given feature in train data dataframe
\# build a vector (1*9) , the first element = (number of times it occured in class1 + 10*alpha / nu
mber of time it occurred in total data+90*alpha)
\# gv_dict is like a look up table, for every gene it store a (1*9) representation of it
# for a value of feature in df:
# if it is in train data:
# we add the vector that was stored in 'gv_dict' look up table to 'gv_fea'
# if it is not there is train:
# return 'gv_fea'
# get gv fea dict: Get Gene varaition Feature Dict
def get gv fea dict(alpha, feature, df):
    # value_count: it contains a dict like
    # print(train df['Gene'].value counts())
```

```
{BRCA1
                      174
            TP5.3
                      106
            EGFR
            BRCA2
                      75
                      69
            PTEN
            KIT
                       61
            BRAF
                       60
            ERBB2
                      47
            PDGFRA
                      46
   # print(train df['Variation'].value counts())
   # output:
   # {
                                          63
   # Truncating Mutations
   # Deletion
                                          4.3
   # Amplification
                                          43
   # Fusions
                                           22
                                           3
   # Overexpression
   # E17K
                                           3
                                           .3
   # 061L
   # S222D
   # P130S
   # }
   value count = train df[feature].value counts()
   # gv dict : Gene Variation Dict, which contains the probability array for each gene/variation
   gv dict = dict()
   # denominator will contain the number of time that particular feature occured in whole data
   for i, denominator in value count.items():
       \# vec will contain (p(yi==1/Gi) probability of gene/variation belongs to perticular class
       # vec is 9 diamensional vector
       vec = []
       for k in range(1,10):
           # print(train_df.loc[(train_df['Class']==1) & (train_df['Gene']=='BRCA1')])
                   ID Gene Variation Class
          # 2470 2470 BRCA1
# 2486 2486 BRCA1
                                         S1715C
                                                   1
                                          S1841R
           # 2614 2614 BRCA1
                                            M1R
           # 2432 2432 BRCA1
                                         I.1657P
           # 2567 2567 BRCA1
                                          T1685A
                                         E1660G
           # 2583 2583 BRCA1
           # 2634 2634 BRCA1
                                          W1718L
           # cls cnt.shape[0] will return the number of rows
          cls cnt = train df.loc[(train df['Class']==k) & (train df[feature]==i)]
          # cls cnt.shape[0](numerator) will contain the number of time that particular feature (
ccured in whole data
          vec.append((cls cnt.shape[0] + alpha*10)/ (denominator + 90*alpha))
       # we are adding the gene/variation to the dict as key and vec as value
       gv dict[i]=vec
   return gv dict
# Get Gene variation feature
def get gv feature(alpha, feature, df):
   # print(gv dict)
      {'BRCA1': [0.2007575757575757575, 0.037878787878788, 0.06818181818181817,
0.13636363636363635,\ 0.25,\ 0.1931818181818181818,\ 0.0378787878787888,\ 0.037878787878787888,
0.0378787878787878788],
         'TP53': [0.32142857142857145, 0.061224489795918366, 0.061224489795918366,
163265307, 0.056122448979591837],
         'EGFR': [0.05681818181818181816, 0.215909090909091, 0.0625, 0.068181818181818177,
0.0681818181818177, 0.0625, 0.346590909090912, 0.0625, 0.056818181818181816],
  # 'BRCA2': [0.1333333333333333333, 0.0606060606060608, 0.0606060606060608,
0.07878787878787878782,\ 0.1393939393939394,\ 0.34545454545454546,\ 0.060606060606060608,
0.06060606060606060608, 0.060606060606060608],
  # 'PTEN': [0.069182389937106917, 0.062893081761006289, 0.069182389937106917,
761006289, 0.062893081761006289],
       'KIT': [0.066225165562913912, 0.25165562913907286, 0.072847682119205295,
0.072847682119205295,\ 0.066225165562913912,\ 0.066225165562913912,\ 0.27152317880794702,
0.066225165562913912, 0.066225165562913912],
```

# vulpul.

```
BKAF: [U.U00000000000000000, U.I/377777777777, U.U/333333333333334,
0.07333333333333334,\ 0.09333333333333333338,\ 0.0800000000000002,\ 0.2999999999999999,
}
   gv_dict = get_gv_fea_dict(alpha, feature, df)
   # value_count is similar in get_gv_fea_dict
   value count = train df[feature].value counts()
   # gv fea: Gene variation feature, it will contain the feature for each feature value in the da
ta
   gv_fea = []
   # for every feature values in the given data frame we will check if it is there in the train
data then we will add the feature to gv fea
    # if not we will add [1/9,1/9,1/9,1/9,1/9,1/9,1/9,1/9,1/9] to gv fea
   for index, row in df.iterrows():
       if row[feature] in dict(value count).keys():
          gv_fea.append(gv_dict[row[feature]])
       else:
          gv_fea.append([1/9,1/9,1/9,1/9,1/9,1/9,1/9,1/9])
            gv fea.append([-1,-1,-1,-1,-1,-1,-1,-1])
   return gv fea
                                                                                          . ▶
4
```

when we caculate the probability of a feature belongs to any particular class, we apply laplace smoothing

• (numerator + 10\\*alpha) / (denominator + 90\\*alpha)

## 3.2.1 Univariate Analysis on Gene Feature

Q1. Gene, What type of feature it is?

Ans. Gene is a categorical variable

h = unique\_genes.values/s;

plt.legend()

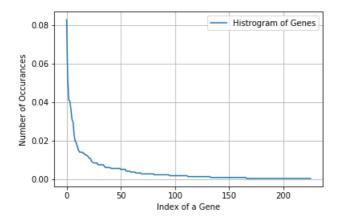
plt.xlabel('Index of a Gene')
plt.ylabel('Number of Occurances')

plt.plot(h, label="Histrogram of Genes")

Q2. How many categories are there and How they are distributed?

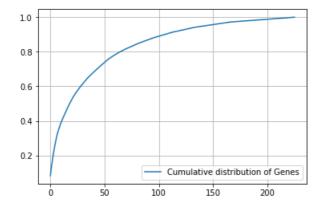
```
In [16]:
unique genes = train df['Gene'].value counts()
print('Number of Unique Genes :', unique_genes.shape[0])
# the top 10 genes that occured most
print(unique_genes.head(10))
Number of Unique Genes: 226
BRCA1
         176
TP53
          112
EGFR
           88
PTEN
           86
           77
BRCA2
BRAF
          66
KTT
          63
           48
ALK
PIK3CA
          42
ERBB2
          40
Name: Gene, dtype: int64
In [17]:
print("Ans: There are", unique genes.shape[0], "different categories of genes in the train data, an
d they are distibuted as follows",)
4
Ans: There are 226 different categories of genes in the train data, and they are distibuted as fol
lows
In [18]:
s = sum(unique_genes.values);
```

```
plt.grid()
plt.show()
```



## In [19]:

```
c = np.cumsum(h)
plt.plot(c,label='Cumulative distribution of Genes')
plt.grid()
plt.legend()
plt.show()
```



### Q3. How to featurize this Gene feature?

Ans.there are two ways we can featurize this variable check out this video: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/handling-categorical-and-numerical-features/

- 1. One hot Encoding
- 2. Response coding

We will choose the appropriate featurization based on the ML model we use. For this problem of multi-class classification with categorical features, one-hot encoding is better for Logistic regression while response coding is better for Random Forests.

## In [20]:

```
#response-coding of the Gene feature
# alpha is used for laplace smoothing
alpha = 1
# train gene feature
train_gene_feature_responseCoding = np.array(get_gv_feature(alpha, "Gene", train_df))
# test gene feature
test_gene_feature_responseCoding = np.array(get_gv_feature(alpha, "Gene", test_df))
# cross validation gene feature
cv_gene_feature_responseCoding = np.array(get_gv_feature(alpha, "Gene", cv_df))
```

### In [21]:

```
print("train_gene_feature_responseCoding is converted feature using respone coding method. The sha
pe of gene feature:", train_gene_feature_responseCoding.shape)
```

```
train gene feature responseCoding is converted feature using respone coding method. The shape of g
ene feature: (2124, 9)
In [22]:
# one-hot encoding of Gene feature.
gene_vectorizer = TfidfVectorizer(max_features=2000, ngram_range=(1,4))
train gene feature onehotCoding = gene vectorizer.fit transform(train df['Gene'])
test_gene_feature_onehotCoding = gene_vectorizer.transform(test_df['Gene'])
cv_gene_feature_onehotCoding = gene_vectorizer.transform(cv_df['Gene'])
In [23]:
train_df['Gene'].head()
Out[23]:
       FGFR3
1402
1330
       MLH1
761
      ERBB2
       TP53
389
2330
        JAK2
Name: Gene, dtype: object
In [24]:
gene vectorizer.get feature names()
Out[24]:
['abl1',
 'acvr1',
 'ago2',
 'akt1',
 'akt2',
 'akt3',
 'alk',
 'apc',
 'ar',
 'araf',
 'aridla',
 'arid1b',
 'arid2',
 'arid5b',
 'asxl1',
 'atm',
 'aurka',
 'aurkb',
 'axin1',
 'axl',
 'b2m',
 'bap1',
 'bcl10',
 'bcl2111',
 'bcor',
 'braf',
 'brcal',
 'brca2',
 'brd4',
 'brip1',
 'btk',
 'card11',
 'carm1',
 'casp8',
 'cbl',
 'ccnd1',
 'ccnd2',
 'ccnd3',
 'ccne1',
 'cdh1',
 'cdk12',
 'cdk4',
```

```
'cdk6',
'cdk8',
'cdknla',
'cdkn1b',
'cdkn2a',
'cdkn2b',
'cdkn2c',
'cebpa',
'chek2',
'cic',
'crebbp',
'ctcf',
'ctnnb1',
'ddr2',
'dicer1',
'dnmt3a',
'dusp4',
'egfr',
'eiflax',
'elf3',
'ep300',
'epas1',
'epcam',
'erbb2',
'erbb3',
'erbb4',
'ercc2',
'ercc3',
'ercc4',
'erg',
'errfi1',
'esr1',
'etv6',
'ewsr1',
'ezh2',
'fam58a',
'fanca',
'fancc',
'fat1',
'fbxw7',
'fgf19',
'fgf3',
'fgfr1',
'fgfr2',
'fgfr3',
'fgfr4',
'flt3',
'foxa1',
'fox12',
'foxp1',
'gata3',
'gli1',
'gnas',
'h3f3a',
'hla',
'hnfla',
'hras',
'idh1',
'idh2',
'igf1r',
'ikbke',
'jak1',
'jak2',
'kdm5a',
'kdm5c',
'kdm6a',
'kdr',
'keap1',
'kit',
'kmt2a',
'kmt2c',
'kmt2d',
'knstrn',
'kras',
'lats1',
'lats2',
'map2k1',
```

```
'map2k2',
'map2k4',
'map3k1',
'mapk1',
'med12',
'mef2b',
'met',
'mga',
'mlh1',
'mpl',
'msh2',
'msh6',
'mtor',
'myc',
'myd88',
'myod1',
'ncor1',
'nf1',
'nf2',
'nfe212',
'nfkbia',
'nkx2',
'notch1',
'nras',
'nsd1',
'ntrk1',
'ntrk2',
'ntrk3',
'nup93',
'pax8',
'pbrm1',
'pdgfra',
'pdgfrb',
'pik3ca',
'pik3cb',
'pik3cd',
'pik3r1',
'pik3r2',
'pim1',
'pms2',
'pole',
'ppmld',
'ppp2r1a',
'ppp6c',
'prdm1',
'ptch1',
'pten',
'ptpn11',
'ptprd',
'ptprt',
'rac1',
'rad21',
'rad50',
'rad51b',
'rad51c',
'rad541',
'raf1',
'rasa1',
'rb1',
'rbm10',
'ret',
'rheb',
'rhoa',
'rictor',
'rit1',
'ros1',
'rras2',
'runx1',
'rxra',
'rybp',
'sdhb',
'setd2',
'sf3b1',
'shoc2',
'shq1',
'smad2',
'smad3',
```

```
'smad4',
 'smarca4',
 'smo',
 'sos1',
 'sox9',
 'spop',
 'src',
 'srsf2',
 'stag2',
 'stat3',
 'stk11',
 'tcf3',
 'tcf712',
 'tert',
 'tet1',
 'tet2',
 'tqfbr1',
 'tgfbr2',
 'tmprss2',
 'tp53',
 'tp53bp1',
 'tsc1',
 'tsc2',
 'u2af1',
 'vegfa',
 'vhl',
 'whsc1',
 'xpo1',
 'xrcc2',
 'yap1']
In [25]:
print ("train gene feature onehotCoding is converted feature using one-hot encoding method. The sha
pe of gene feature:", train gene feature onehotCoding.shape)
train gene feature onehotCoding is converted feature using one-hot encoding method. The shape of g
```

## **Q4.** How good is this gene feature in predicting y\_i?

There are many ways to estimate how good a feature is, in predicting y\_i. One of the good methods is to build a proper ML model using just this feature. In this case, we will build a logistic regression model using only Gene feature (one hot encoded) to predict y\_i.

```
In [26]:
```

ene feature: (2124, 226)

```
alpha = [10 ** x for x in range(-5, 1)] # hyperparam for SGD classifier.
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n jobs=1, random state=None, learning rate='optimal', eta0
=0.0, power t=0.5,
# class weight=None, warm start=False, average=False, n iter=None)
# some of methods
# fit(X, y[, coef init, intercept init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link:
cv_log_error_array=[]
for i in alpha:
    clf = SGDClassifier(alpha=i, penalty='12', loss='log', random state=42)
    clf.fit(train_gene_feature_onehotCoding, y_train)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
   sig clf.fit(train gene feature onehotCoding, y train)
```

```
predict y = sig clf.predict proba(cv gene feature onehotCoding)
    cv_log_error_array.append(log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
   print('For values of alpha = ', i, "The log loss is:",log loss(y cv, predict y, labels=clf.clas
ses , eps=1e-15))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
    ax.annotate((alpha[i],np.round(txt,3)), (alpha[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best alpha = np.argmin(cv log error array)
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='log', random_state=42)
clf.fit(train_gene_feature_onehotCoding, y_train)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_gene_feature_onehotCoding, y_train)
predict_y = sig_clf.predict_proba(train_gene_feature_onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The train log loss is:",log loss(y train,
predict y, labels=clf.classes , eps=1e-15))
predict_y = sig_clf.predict_proba(cv_gene_feature_onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The cross validation log loss is:",log lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_gene_feature_onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The test log loss is:",log loss(y test, p
redict_y, labels=clf.classes_, eps=1e-15))
For values of alpha = 1e-05 The log loss is: 1.3368009935888565
For values of alpha = 0.0001 The log loss is: 1.1545038781790566
```

For values of alpha = 1e-05 The log loss is: 1.3368009935888565

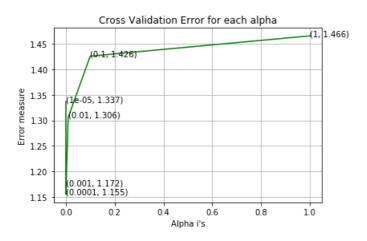
For values of alpha = 0.0001 The log loss is: 1.1545038781790566

For values of alpha = 0.001 The log loss is: 1.1722262981090035

For values of alpha = 0.01 The log loss is: 1.306082679098516

For values of alpha = 0.1 The log loss is: 1.426237301488987

For values of alpha = 1 The log loss is: 1.4660850197925832



```
For values of best alpha = 0.0001 The train log loss is: 1.0387201537414488
For values of best alpha = 0.0001 The cross validation log loss is: 1.1545038781790566
For values of best alpha = 0.0001 The test log loss is: 1.2268569304490295
```

## Q5. Is the Gene feature stable across all the data sets (Test, Train, Cross validation)?

Ans. Yes, it is. Otherwise, the CV and Test errors would be significantly more than train error.

```
In [27]:
```

```
print("Q6. How many data points in Test and CV datasets are covered by the ", unique_genes.shape[0]
], " genes in train dataset?")

test_coverage=test_df[test_df['Gene'].isin(list(set(train_df['Gene'])))].shape[0]
cv_coverage=cv_df[cv_df['Gene'].isin(list(set(train_df['Gene'])))].shape[0]

print('Ans\n1. In test data',test_coverage, 'out of',test_df.shape[0], ":",(test_coverage/test_df.
```

```
shape[0])*100)
print('2. In cross validation data',cv coverage, 'out of ',cv df.shape[0],":", (cv coverage/cv df.s
hape[0])*100)
Q6. How many data points in Test and CV datasets are covered by the 226 genes in train dataset?
1. In test data 635 out of 665 : 95.48872180451127
2. In cross validation data 515 out of 532 : 96.80451127819549
```

## 3.2.2 Univariate Analysis on Variation Feature

**Q7.** Variation, What type of feature is it?

Ans. Variation is a categorical variable

**Q8.** How many categories are there?

```
In [28]:
unique_variations = train_df['Variation'].value_counts()
print('Number of Unique Variations :', unique variations.shape[0])
# the top 10 variations that occured most
print(unique_variations.head(10))
Number of Unique Variations : 1938
Truncating_Mutations
                       60
Deletion
Amplification
                        42
                        21
Fusions
G12V
                         4
061H
                         3
E17K
G12D
                         2
Overexpression
Q22K
Name: Variation, dtype: int64
```

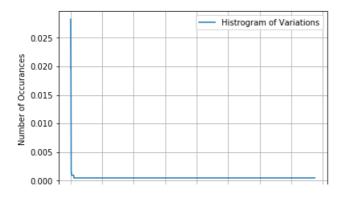
#### In [29]:

```
print("Ans: There are", unique_variations.shape[0] , "different categories of variations in the
train data, and they are distibuted as follows",)
```

Ans: There are 1938 different categories of variations in the train data, and they are distibuted as follows

## In [30]:

```
s = sum(unique_variations.values);
h = unique variations.values/s;
plt.plot(h, label="Histrogram of Variations")
plt.xlabel('Index of a Variation')
plt.ylabel('Number of Occurances')
plt.legend()
plt.grid()
plt.show()
```

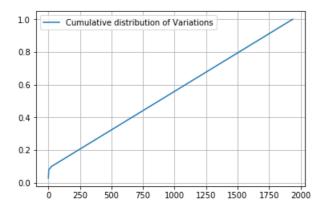


```
0 250 500 750 1000 1250 1500 1750 2000
```

#### In [31]:

```
c = np.cumsum(h)
print(c)
plt.plot(c,label='Cumulative distribution of Variations')
plt.grid()
plt.legend()
plt.show()
```

```
[0.02824859 0.0480226 0.06779661 ... 0.99905838 0.99952919 1.
```



## Q9. How to featurize this Variation feature?

**Ans.**There are two ways we can featurize this variable check out this video: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/handling-categorical-and-numerical-features/

- 1. One hot Encoding
- 2. Response coding

We will be using both these methods to featurize the Variation Feature

## In [32]:

```
# alpha is used for laplace smoothing
alpha = 1
# train gene feature
train_variation_feature_responseCoding = np.array(get_gv_feature(alpha, "Variation", train_df))
# test gene feature
test_variation_feature_responseCoding = np.array(get_gv_feature(alpha, "Variation", test_df))
# cross validation gene feature
cv_variation_feature_responseCoding = np.array(get_gv_feature(alpha, "Variation", cv_df))
```

### In [33]:

```
print("train_variation_feature_responseCoding is a converted feature using the response coding met
hod. The shape of Variation feature:", train_variation_feature_responseCoding.shape)
```

train\_variation\_feature\_responseCoding is a converted feature using the response coding method. The shape of Variation feature: (2124, 9)

#### In [34]:

```
# one-hot encoding of variation feature.
variation_vectorizer = TfidfVectorizer(max_features=2000, ngram_range=(1,4))
train_variation_feature_onehotCoding = variation_vectorizer.fit_transform(train_df['Variation'])
test_variation_feature_onehotCoding = variation_vectorizer.transform(test_df['Variation'])
cv_variation_feature_onehotCoding = variation_vectorizer.transform(cv_df['Variation'])
```

III [JJ].

```
print("train_variation_feature_onehotEncoded is converted feature using the onne-hot encoding meth
od. The shape of Variation feature:", train_variation_feature_onehotCoding.shape)
```

train\_variation\_feature\_onehotEncoded is converted feature using the onne-hot encoding method. The shape of Variation feature: (2124, 2000)

## Q10. How good is this Variation feature in predicting y\_i?

Let's build a model just like the earlier!

```
In [36]:
```

```
alpha = [10 ** x for x in range(-5, 1)]
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n_jobs=1, random_state=None, learning_rate='optimal', eta0
=0.0, power t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef_init, intercept_init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link:
cv log error array=[]
for i in alpha:
    clf = SGDClassifier(alpha=i, penalty='12', loss='log', random_state=42)
    clf.fit(train_variation_feature_onehotCoding, y_train)
   sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_variation_feature_onehotCoding, y_train)
   predict_y = sig_clf.predict_proba(cv_variation_feature_onehotCoding)
   cv_log_error_array.append(log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
   print('For values of alpha = ', i, "The log loss is:",log loss(y cv, predict y, labels=clf.clas
ses , eps=1e-15))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
   ax.annotate((alpha[i],np.round(txt,3)), (alpha[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best alpha = np.argmin(cv log error array)
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='log', random state=42)
clf.fit(train variation feature onehotCoding, y train)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_variation_feature_onehotCoding, y_train)
predict y = sig clf.predict proba(train variation feature onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict y, labels=clf.classes , eps=1e-15))
predict_y = sig_clf.predict_proba(cv_variation_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_variation_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=1e-15))
```

```
For values of alpha = 1e-05 The log loss is: 1.721544302989071

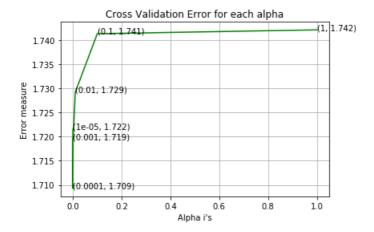
For values of alpha = 0.0001 The log loss is: 1.7092817793612023

For values of alpha = 0.001 The log loss is: 1.7193691732666683

For values of alpha = 0.01 The log loss is: 1.729206230678092

For values of alpha = 0.1 The log loss is: 1.741290479737912

For values of alpha = 1 The log loss is: 1.74208701536609
```



```
For values of best alpha = 0.0001 The train log loss is: 0.7627882666186675 For values of best alpha = 0.0001 The cross validation log loss is: 1.7092817793612023 For values of best alpha = 0.0001 The test log loss is: 1.684736874106243
```

## Q11. Is the Variation feature stable across all the data sets (Test, Train, Cross validation)?

Ans. Not sure! But lets be very sure using the below analysis.

#### In [37]:

```
print("Q12. How many data points are covered by total ", unique_variations.shape[0], " genes in te
st and cross validation data sets?")
test_coverage=test_df[test_df['Variation'].isin(list(set(train_df['Variation'])))].shape[0]
cv_coverage=cv_df[cv_df['Variation'].isin(list(set(train_df['Variation'])))].shape[0]
print('Ans\n1. In test data',test_coverage, 'out of',test_df.shape[0], ":",(test_coverage/test_df.shape[0])*100)
print('2. In cross validation data',cv_coverage, 'out of ',cv_df.shape[0],":",(cv_coverage/cv_df.shape[0])*100)
```

Q12. How many data points are covered by total 1938 genes in test and cross validation data sets?

Ans

- 1. In test data 78 out of 665 : 11.729323308270677
- 2. In cross validation data 55 out of 532 : 10.338345864661653

## 3.2.3 Univariate Analysis on Text Feature

- 1. How many unique words are present in train data?
- 2. How are word frequencies distributed?
- 3. How to featurize text field?
- 4. Is the text feature useful in predicitng y\_i?
- 5. Is the text feature stable across train, test and CV datasets?

#### In [38]:

```
# cls_text is a data frame
# for every row in data fram consider the 'TEXT'
# split the words by space
# make a dict with those words
# increment its count whenever we see that word

def extract_dictionary_paddle(cls_text):
    dictionary = defaultdict(int)
    for index, row in cls_text.iterrows():
        for word in row['TEXT'].split():
```

```
dictionary[word] +=1
return dictionary
```

#### In [39]:

#### In [40]:

```
# building a TfidfVectorizer with all the words that occured minimum 3 times in train data
#text_vectorizer = CountVectorizer(min_df=3)
text_vectorizer = TfidfVectorizer(min_df=3, max_features=2000, ngram_range=(1,4))
train_text_feature_onehotCoding = text_vectorizer.fit_transform(train_df['TEXT'])
# getting all the feature names (words)
train_text_features= text_vectorizer.get_feature_names()

# train_text_feature_onehotCoding.sum(axis=0).Al will sum every row and returns (1*number of features) vector
train_text_fea_counts = train_text_feature_onehotCoding.sum(axis=0).Al

# zip(list(text_features),text_fea_counts) will zip a word with its number of times it occured
text_fea_dict = dict(zip(list(train_text_features),train_text_fea_counts))

print("Total number of unique words in train data :", len(train_text_features))
```

Total number of unique words in train data: 2000

#### In [41]:

```
dict list = []
# dict list =[] contains 9 dictoinaries each corresponds to a class
for i in range (1,10):
    cls text = train df[train df['Class']==i]
    # build a word dict based on the words in that class
    dict_list.append(extract_dictionary_paddle(cls_text))
    # append it to dict list
# dict list[i] is build on i'th class text data
# total dict is buid on whole training text data
total dict = extract dictionary paddle(train df)
confuse array = []
for i in train text features:
   ratios = []
   \max val = -1
    for j in range (0,9):
        ratios.append((dict list[j][i]+10 )/(total dict[i]+90))
   confuse_array.append(ratios)
confuse array = np.array(confuse array)
```

## In [42]:

```
#response coding of text features
train_text_feature_responseCoding = get_text_responsecoding(train_df)
test_text_feature_responseCoding = get_text_responsecoding(test_df)
cv_text_feature_responseCoding = get_text_responsecoding(cv_df)
```

#### In [43]:

```
# https://stackoverflow.com/a/16202486
# we convert each row values such that they sum to 1
train_text_feature_responseCoding =
(train_text_feature_responseCoding.T/train_text_feature_responseCoding.sum(axis=1)).T
test_text_feature_responseCoding =
(test_text_feature_responseCoding.T/test_text_feature_responseCoding.sum(axis=1)).T
cv_text_feature_responseCoding = (cv_text_feature_responseCoding.T/cv_text_feature_responseCoding.sum(axis=1)).T
```

### In [44]:

```
# don't forget to normalize every feature
train_text_feature_onehotCoding = normalize(train_text_feature_onehotCoding, axis=0)

# we use the same vectorizer that was trained on train data
test_text_feature_onehotCoding = text_vectorizer.transform(test_df['TEXT'])
# don't forget to normalize every feature
test_text_feature_onehotCoding = normalize(test_text_feature_onehotCoding, axis=0)

# we use the same vectorizer that was trained on train data
cv_text_feature_onehotCoding = text_vectorizer.transform(cv_df['TEXT'])
# don't forget to normalize every feature
cv_text_feature_onehotCoding = normalize(cv_text_feature_onehotCoding, axis=0)
```

### In [45]:

```
#https://stackoverflow.com/a/2258273/4084039
sorted_text_fea_dict = dict(sorted(text_fea_dict.items(), key=lambda x: x[1] , reverse=True))
sorted_text_occur = np.array(list(sorted_text_fea_dict.values()))
```

### In [46]:

```
# Number of words for a given frequency.
print(Counter(sorted_text_occur))
```

```
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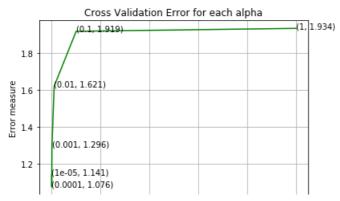
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3.999234462076511: 1, 3.9787652351069664: 1, 3.978282093463443: 1, 3.9641905041084953: 1,
3.9615310912263157: 1, 3.954999366794561: 1, 3.9494876396556804: 1, 3.930910543091535: 1,
3.9265581952217588: 1, 3.9170056086488567: 1, 3.9159189329310498: 1, 3.913811001911172: 1,
3.9016536056097277: 1, 3.901602663344786: 1, 3.892639367424239: 1, 3.888479163995114: 1, 3.88677746
98041235: 1, 3.8859530995501492: 1, 3.8833757298830807: 1, 3.8643280036820573: 1,
3.862595799614239: 1, 3.856991673338055: 1, 3.8553534291677627: 1, 3.8304218564217702: 1,
3.8140695508338895: 1, 3.784368559937053: 1, 3.7818876841223217: 1, 3.766212863554476: 1,
3.76008440675485: 1, 3.7579953737410645: 1, 3.7554984336773614: 1, 3.737079753367513: 1,
3.731023062501971\colon 1,\ 3.714630209528808\colon 1,\ 3.7113095345991995\colon 1,\ 3.703335940592092\colon 1,
3.6991104191987314: 1, 3.692806724228393: 1, 3.685041005469602: 1, 3.6800714948941584: 1,
3.6670021103478807: 1, 3.638773654221167: 1, 3.6302718490605943: 1, 3.5995065962705493: 1,
3.58925970646872: 1, 3.561762066825263: 1, 3.5527486298816426: 1, 3.5315851225603274: 1,
3.5300195765981393: 1, 3.4315456701777634: 1, 3.348318957722383: 1, 3.1693411128895326: 1})
                                                                                                                               •
```

#### In [47]:

```
| # default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n jobs=1, random state=None, learning rate='optimal', eta0
=0.0, power_t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef_init, intercept_init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link:
cv log error array=[]
for i in alpha:
    clf = SGDClassifier(alpha=i, penalty='12', loss='log', random state=42)
    clf.fit(train_text_feature_onehotCoding, y_train)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train text feature onehotCoding, y train)
    predict_y = sig_clf.predict_proba(cv_text_feature_onehotCoding)
    cv_log_error_array.append(log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
    print('For values of alpha = ', i, "The log loss is:",log loss(y cv, predict y, labels=clf.clas
ses_, eps=1e-15))
fig, ax = plt.subplots()
ax.plot(alpha, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
    ax.annotate((alpha[i],np.round(txt,3)), (alpha[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='log', random_state=42)
clf.fit(train text feature onehotCoding, y train)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_text_feature_onehotCoding, y_train)
predict_y = sig_clf.predict_proba(train_text_feature_onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The train log loss is:",log loss(y train,
predict y, labels=clf.classes , eps=1e-15))
        y = sig clf.predict proba(cv text feature onehotCoding)
predict
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_text_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict y, labels=clf.classes , eps=1e-15))
For values of alpha = 1e-05 The log loss is: 1.140779489415932
For values of alpha = 0.0001 The log loss is: 1.0758027258362972
For values of alpha = 0.001 The log loss is: 1.29578788031302
For values of alpha = 0.01 The log loss is: 1.6207186003778338
For values of alpha = 0.1 The log loss is: 1.9185358313165983
For values of alpha = 1 The log loss is: 1.934455072880182
```



```
Alphai's

For values of best alpha = 0.0001 The train log loss is: 0.7360639947052967

For values of best alpha = 0.0001 The cross validation log loss is: 1.0758027258362972

For values of best alpha = 0.0001 The test log loss is: 1.2094711851133668
```

1.0

## Q. Is the Text feature stable across all the data sets (Test, Train, Cross validation)?

Ans. Yes, it seems like!

0.0

0.2

```
In [48]:
```

```
def get_intersec_text(df):
    df_text_vec = CountVectorizer(min_df=3)
    df_text_fea = df_text_vec.fit_transform(df['TEXT'])
    df_text_features = df_text_vec.get_feature_names()

df_text_fea_counts = df_text_fea.sum(axis=0).A1
    df_text_fea_dict = dict(zip(list(df_text_features), df_text_fea_counts))
    len1 = len(set(df_text_features))
    len2 = len(set(train_text_features) & set(df_text_features))
    return len1,len2
```

#### In [49]:

```
len1,len2 = get_intersec_text(test_df)
print(np.round((len2/len1)*100, 3), "% of word of test data appeared in train data")
len1,len2 = get_intersec_text(cv_df)
print(np.round((len2/len1)*100, 3), "% of word of Cross Validation appeared in train data")
```

```
5.806\ \% of word of test data appeared in train data 6.618\ \% of word of Cross Validation appeared in train data
```

# 4. Machine Learning Models

```
In [50]:
```

```
#Data preparation for ML models.

#Misc. functionns for ML models

def predict_and_plot_confusion_matrix(train_x, train_y,test_x, test_y, clf):
    clf.fit(train_x, train_y)
    sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_x, train_y)
    pred_y = sig_clf.predict(test_x)

# for calculating log_loss we will provide the array of probabilities belongs to each class
    print("Log_loss:",log_loss(test_y, sig_clf.predict_proba(test_x)))
    # calculating the number of data points that are misclassified
    print("Number of mis-classified points:", np.count_nonzero((pred_y- test_y))/test_y.shape[0])
    plot_confusion_matrix(test_y, pred_y)
```

## In [51]:

```
def report_log_loss(train_x, train_y, test_x, test_y, clf):
    clf.fit(train_x, train_y)
    sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_x, train_y)
    sig_clf_probs = sig_clf.predict_proba(test_x)
    return log_loss(test_y, sig_clf_probs, eps=1e-15)
```

## In [52]:

```
# this function will be used just for naive bayes
# for the given indices, we will print the name of the features
```

```
# and we will check whether the feature present in the test point text or not
def get_impfeature_names(indices, text, gene, var, no_features):
   gene count vec = CountVectorizer()
    var count vec = CountVectorizer()
   text_count_vec = CountVectorizer(min_df=3)
    gene vec = gene count vec.fit(train df['Gene'])
    var_vec = var_count_vec.fit(train_df['Variation'])
    text vec = text count vec.fit(train df['TEXT'])
    fea1_len = len(gene_vec.get_feature_names())
    fea2 len = len(var count vec.get feature names())
    word present = 0
    for i,v in enumerate(indices):
        if (v < feal_len):</pre>
            word = gene vec.get feature names()[v]
            yes no = True if word == gene else False
            if ves no:
                word_present += 1
               print(i, "Gene feature [{}] present in test data point [{}]".format(word, yes no))
        elif (v < fea1_len+fea2_len):</pre>
            word = var_vec.get_feature_names()[v-(fea1_len)]
            yes no = True if word == var else False
            if yes no:
                word present += 1
                print(i, "variation feature [{}] present in test data point [{}]".format(word,yes_r
0))
        else:
            word = text_vec.get_feature names()[v-(fea1 len+fea2 len)]
            yes no = True if word in text.split() else False
            if yes no:
                word present += 1
                print(i, "Text feature [{}] present in test data point [{}]".format(word,yes no))
    print ("Out of the top ", no features," features ", word present, "are present in query point")
```

# Stacking the three types of features

```
In [53]:
```

```
# merging gene, variance and text features
# building train, test and cross validation data sets
# a = [[1, 2],
       [3, 4]]
#b = [[4, 5],
      [6, 7]]
\# hstack(a, b) = [[1, 2, 4, 5],
                 [ 3, 4, 6, 7]]
train_gene_var_onehotCoding =
hstack((train_gene_feature_onehotCoding,train_variation_feature_onehotCoding))
test gene var onehotCoding =
hstack((test_gene_feature_onehotCoding,test_variation_feature_onehotCoding))
cv gene var onehotCoding = hstack((cv gene feature onehotCoding,cv variation feature onehotCoding)
train x onehotCoding = hstack((train gene var onehotCoding, train text feature onehotCoding)).tocs
train y = np.array(list(train df['Class']))
test x onehotCoding = hstack((test gene var onehotCoding, test text feature onehotCoding)).tocsr()
test_y = np.array(list(test_df['Class']))
cv_x_onehotCoding = hstack((cv_gene_var_onehotCoding, cv_text_feature_onehotCoding)).tocsr()
cv_y = np.array(list(cv_df['Class']))
train gene var responseCoding =
np.hstack((train_gene_feature_responseCoding,train_variation_feature_responseCoding))
test_gene_var_responseCoding =
np.hstack((test gene feature responseCoding, test variation feature responseCoding))
```

```
cv gene var responseCoding =
np.hstack((cv_gene_feature_responseCoding,cv_variation_feature_responseCoding))
train x responseCoding = np.hstack((train gene var responseCoding,
train text feature responseCoding))
test x responseCoding = np.hstack((test gene var responseCoding, test text feature responseCoding)
cv_x_responseCoding = np.hstack((cv_gene_var_responseCoding, cv_text_feature_responseCoding))
In [54]:
print("One hot encoding features :")
print("(number of data points * number of features) in train data = ", train_x_onehotCoding.shape)
print("(number of data points * number of features) in test data = ", test_x_onehotCoding.shape)
print("(number of data points * number of features) in cross validation data = ", cv x onehotCoding
.shape)
One hot encoding features :
(number of data points * number of features) in train data = (2124, 4226)
(number of data points * number of features) in test data = (665, 4226)
(number of data points * number of features) in cross validation data = (532, 4226)
In [55]:
print(" Response encoding features :")
print("(number of data points * number of features) in train data = ", train x responseCoding.shap
print("(number of data points * number of features) in test data = ", test_x_responseCoding.shape)
print("(number of data points * number of features) in cross validation data =",
cv_x_responseCoding.shape)
Response encoding features :
(number of data points * number of features) in train data = (2124, 27)
```

(number of data points \* number of features) in test data = (665, 27)

(number of data points \* number of features) in cross validation data = (532, 27)

## 4.1. Base Line Model

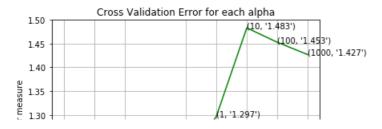
## 4.1.1. Naive Bayes

## 4.1.1.1. Hyper parameter tuning

In [56]:

```
# find more about Multinomial Naive base function here http://scikit-
learn.org/stable/modules/generated/sklearn.naive bayes.MultinomialNB.html
# default paramters
# sklearn.naive bayes.MultinomialNB(alpha=1.0, fit prior=True, class prior=None)
# some of methods of MultinomialNB()
# fit(X, y[, sample weight]) Fit Naive Bayes classifier according to X, y
# predict(X) Perform classification on an array of test vectors X.
# predict_log_proba(X) Return log-probability estimates for the test vector X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/naive-bayes-
algorithm-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
```

```
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/naive-bayes-
algorithm-1/
cv_log_error_array = []
for i in alpha:
    print("for alpha =", i)
    clf = MultinomialNB(alpha=i)
    clf.fit(train x onehotCoding, train y)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train x onehotCoding, train y)
    sig clf probs = sig clf.predict proba(cv x onehotCoding)
    cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    \# to avoid rounding error while multiplying probabilites we use log-probability estimates
    print("Log Loss :",log loss(cv y, sig clf probs))
fig, ax = plt.subplots()
ax.plot(np.log10(alpha), cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
    ax.annotate((alpha[i],str(txt)), (np.log10(alpha[i]),cv log error array[i]))
plt.grid()
plt.xticks(np.log10(alpha))
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = MultinomialNB(alpha=alpha[best alpha])
clf.fit(train_x_onehotCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x onehotCoding, train y)
predict y = sig clf.predict proba(train x onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict y = sig clf.predict proba(test x onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The test log loss is:",log loss(y test, p
redict_y, labels=clf.classes_, eps=1e-15))
for alpha = 1e-05
Log Loss: 1.153105050504226
for alpha = 0.0001
Log Loss: 1.152707984150967
for alpha = 0.001
Log Loss: 1.1504317324504902
for alpha = 0.1
Log Loss: 1.199030089131308
for alpha = 1
Log Loss: 1.2969612308356298
for alpha = 10
Log Loss: 1.4827173823549864
for alpha = 100
Log Loss: 1.4525345412018227
for alpha = 1000
Log Loss: 1.4266255568324775
```



```
125

120

115 (1e-05, (0.0881)(0)0053'1.15')

-5 -4 -3 -1 0 1 2 3

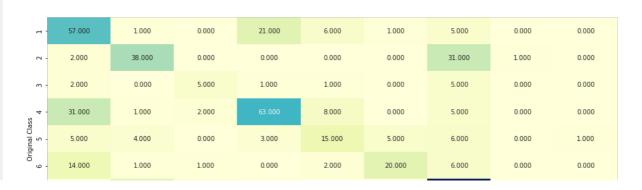
Alpha i's
```

```
For values of best alpha = 0.001 The train log loss is: 0.5812146150905396
For values of best alpha = 0.001 The cross validation log loss is: 1.1504317324504902
For values of best alpha = 0.001 The test log loss is: 1.2333635964950285
```

### 4.1.1.2. Testing the model with best hyper paramters

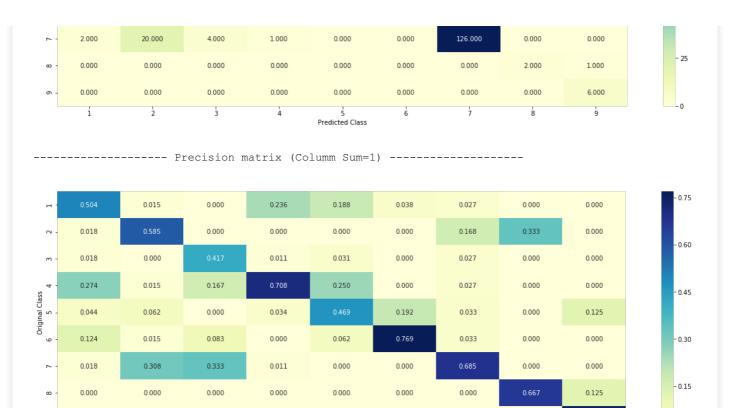
#### In [57]:

```
# find more about Multinomial Naive base function here http://scikit-
learn.org/stable/modules/generated/sklearn.naive bayes.MultinomialNB.html
# default paramters
# sklearn.naive bayes.MultinomialNB(alpha=1.0, fit prior=True, class prior=None)
# some of methods of MultinomialNB()
# fit(X, y[, sample weight]) Fit Naive Bayes classifier according to X, y
# predict(X) Perform classification on an array of test vectors X.
# predict log proba(X) Return log-probability estimates for the test vector X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/naive-bayes-
algorithm-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
\# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
clf = MultinomialNB(alpha=alpha[best alpha])
clf.fit(train_x_onehotCoding, train_y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)
sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
# to avoid rounding error while multiplying probabilites we use log-probability estimates
print("Log Loss :",log_loss(cv_y, sig_clf_probs))
print("Number of missclassified point:", np.count nonzero((sig clf.predict(cv x onehotCoding) - cv
y))/cv y.shape[0])
plot_confusion_matrix(cv_y, sig_clf.predict(cv_x_onehotCoding.toarray()))
```



- 100

75



----- Recall matrix (Row sum=1) ------

0.000

0.000

Predicted Class

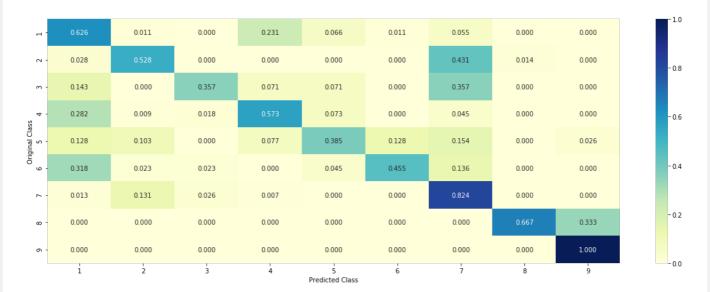
0.000

0.000

0.000

8

0.000



#### 4.1.1.3. Feature Importance, Correctly classified point

0.000

5

0.000

i

```
In [58]:
```

```
test point index = 1
no feature = 100
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef_)[predicted_cls-1][:,:no_feature]
print("-"*50)
get_impfeature_names(indices[0],
test df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test point index], no feature)
  1' ' 1 07
```

#### 4.1.1.4. Feature Importance, Incorrectly classified point

```
In [59]:
```

```
test point index = 100
no feature = 100
predicted cls = sig clf.predict(test x onehotCoding[test point index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
\verb"np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]), 4)")" \\
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.coef_) [predicted_cls-1][:,:no_feature]
print("-"*50)
get impfeature names (indices [0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test point index], no feature)
Predicted Class : 1
Predicted Class Probabilities: [[0.5557 0.0517 0.0128 0.197 0.0416 0.0416 0.0928 0.0045 0.0023]]
Actual Class : 4
_____
48 Text feature [15] present in test data point [True]
Out of the top 100 features 1 are present in query point
```

# 4.2. K Nearest Neighbour Classification

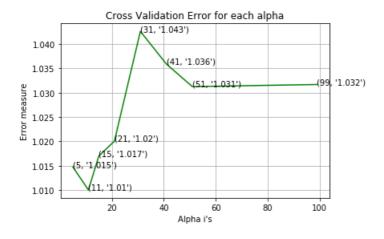
### 4.2.1. Hyper parameter tuning

In [60]:

```
# find more about KNeighborsClassifier() here http://scikit-
learn.org/stable/modules/generated/sklearn.neighbors. KNeighborsClassifier.html \\
# default parameter
# KNeighborsClassifier(n_neighbors=5, weights='uniform', algorithm='auto', leaf size=30, p=2,
# metric='minkowski', metric params=None, n jobs=1, **kwargs)
# methods of
\# fit(X, y) : Fit the model using X as training data and y as target values
# predict(X):Predict the class labels for the provided data
# predict_proba(X): Return probability estimates for the test data X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/k-nearest-ne
ighbors-geometric-intuition-with-a-toy-example-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link:
```

```
alpha = [5, 11, 15, 21, 31, 41, 51, 99]
cv_log_error_array = []
for i in alpha:
    print("for alpha =", i)
    clf = KNeighborsClassifier(n_neighbors=i)
    clf.fit(train x responseCoding, train y)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_x_responseCoding, train_y)
    sig_clf_probs = sig_clf.predict_proba(cv_x_responseCoding)
    cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    # to avoid rounding error while multiplying probabilites we use log-probability estimates
    print("Log Loss :",log loss(cv y, sig clf probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
   ax.annotate((alpha[i],str(txt)), (alpha[i],cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = KNeighborsClassifier(n neighbors=alpha[best alpha])
clf.fit(train x responseCoding, train y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x responseCoding, train y)
predict_y = sig_clf.predict_proba(train_x_responseCoding)
print('For values of best alpha = ', alpha[best alpha], "The train log loss is:",log loss(y train,
predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_responseCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_responseCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y test, p
redict_y, labels=clf.classes_, eps=1e-15))
for alpha = 5
Log Loss : 1.0147585241733181
for alpha = 11
Log Loss : 1.0100418537371045
for alpha = 15
```

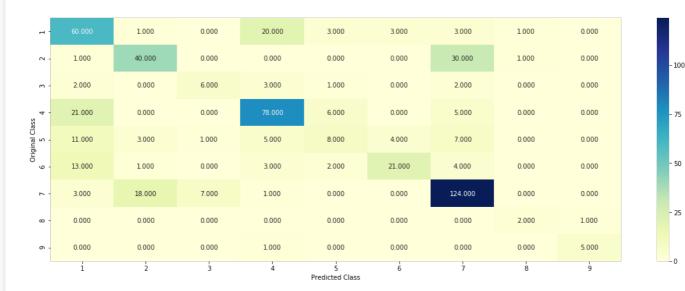
```
Log Loss: 1.0147585241733181
for alpha = 11
Log Loss: 1.0100418537371045
for alpha = 15
Log Loss: 1.017000427290506
for alpha = 21
Log Loss: 1.020051465209906
for alpha = 31
Log Loss: 1.0425869526802527
for alpha = 41
Log Loss: 1.0358922726241941
for alpha = 51
Log Loss: 1.0312499090574307
for alpha = 99
Log Loss: 1.0316815087635784
```

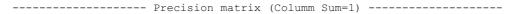


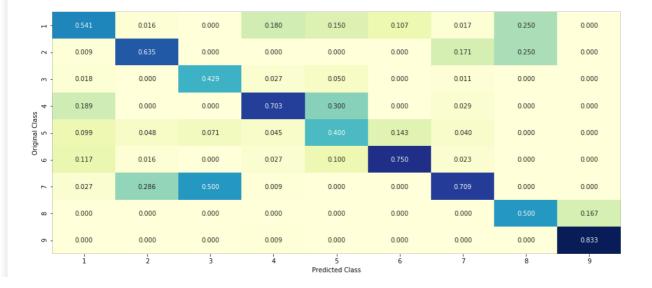
```
For values of best alpha = 11 The cross validation log loss is: 1.0100418537371045
For values of best alpha = 11 The test log loss is: 1.0813518997758362
```

# 4.2.2. Testing the model with best hyper paramters

#### In [61]:







- 0.75

- 0.60

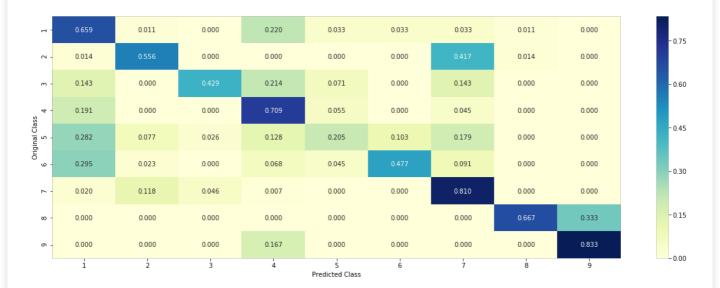
- 0.45

- 0.30

0.15

- 0.00

----- Recall matrix (Row sum=1) -----



# 4.2.3. Sample Query point -1

```
In [62]:
```

```
clf = KNeighborsClassifier(n neighbors=alpha[best alpha])
clf.fit(train_x_responseCoding, train_y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x responseCoding, train y)
test point index = 1
predicted cls = sig clf.predict(test x responseCoding[0].reshape(1,-1))
print("Predicted Class :", predicted_cls[0])
print("Actual Class :", test y[test point index])
neighbors = clf.kneighbors(test x responseCoding[test point index].reshape(1, -1), alpha[best alpha
])
print("The ",alpha[best alpha]," nearest neighbours of the test points belongs to classes",train y
[neighbors[1][0]])
print("Fequency of nearest points :",Counter(train_y[neighbors[1][0]]))
Predicted Class: 7
Actual Class: 3
The 11 nearest neighbours of the test points belongs to classes [1 4 4 1 4 1 1 4 4 4 1]
```

#### 4.2.4. Sample Query Point-2

Fequency of nearest points : Counter({4: 6, 1: 5})

#### In [63]:

Actual Class: 4

```
clf = KNeighborsClassifier(n_neighbors=alpha[best_alpha])
clf.fit(train_x_responseCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_responseCoding, train_y)

test_point_index = 100

predicted_cls = sig_clf.predict(test_x_responseCoding[test_point_index].reshape(1,-1))
print("Predicted Class :", predicted_cls[0])
print("Actual Class :", test_y[test_point_index])
neighbors = clf.kneighbors(test_x_responseCoding[test_point_index].reshape(1, -1), alpha[best_alpha])
print("the k value for knn is",alpha[best_alpha],"and the nearest neighbours of the test points be longs to classes",train_y[neighbors[1][0]])
print("Fequency of nearest points :",Counter(train_y[neighbors[1][0]]))
```

```
the k value for knn is 11 and the nearest neighbours of the test points belongs to classes [4\ 1\ 1\ 5\ 1\ 4\ 4\ 4\ 4\ 1] Fequency of nearest points : Counter(\{4:\ 6,\ 1:\ 4,\ 5:\ 1\})
```

# 4.3. Logistic Regression

# 4.3.1. With Class balancing

#### 4.3.1.1. Hyper paramter tuning

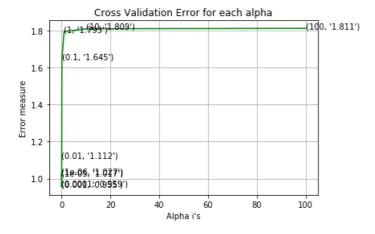
```
In [64]:
```

```
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
# shuffle=True, verbose=0, epsilon=0.1, n_jobs=1, random_state=None, learning_rate='optimal', eta0
=0.0, power t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef init, intercept init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/geometric-in
tuition-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get_params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link:
alpha = [10 ** x for x in range(-6, 3)]
cv_log_error_array = []
for i in alpha:
   print("for alpha =", i)
   clf = SGDClassifier(class_weight='balanced', alpha=i, penalty='12', loss='log', random state=42
    clf.fit(train x onehotCoding, train y)
    sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train x onehotCoding, train y)
    sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
    cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    # to avoid rounding error while multiplying probabilites we use log-probability estimates
    print("Log Loss :",log loss(cv y, sig clf probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
   ax.annotate((alpha[i], str(txt)), (alpha[i], cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
```

```
best_alpha = np.argmin(cv_log_error_array)
clf = SGDClassifier(class_weight='balanced', alpha=alpha[best_alpha], penalty='12', loss='log', ran
dom_state=42)
clf.fit(train_x_onehotCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)

predict_y = sig_clf.predict_proba(train_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict_y, labels=clf.classes_, eps=le-15))
predict_y = sig_clf.predict_proba(cv_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=le-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=le-15))
```

for alpha = 1e-06Log Loss : 1.0270228120402658 for alpha = 1e-05Log Loss: 1.0172016464993268 for alpha = 0.0001Log Loss: 0.9592513281465967 for alpha = 0.001Log Loss: 0.9554926080094617 for alpha = 0.01Log Loss: 1.1118829662812784 for alpha = 0.1Log Loss: 1.6447457229985016 for alpha = 1Log Loss: 1.793442602408434 for alpha = 10Log Loss: 1.8090578411240252 for alpha = 100Log Loss: 1.8108508261835534



For values of best alpha = 0.001 The train log loss is: 0.6779496215824264For values of best alpha = 0.001 The cross validation log loss is: 0.9554926080094617For values of best alpha = 0.001 The test log loss is: 1.087019650771065

#### 4.3.1.2. Testing the model with best hyper paramters

#### In [65]:

```
# predict(X) Predict class labels for samples in X.
#-----
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/geometric-in
tuition-1/
#-------
clf = SGDClassifier(class_weight='balanced', alpha=alpha[best_alpha], penalty='12', loss='log', ran
dom_state=42)
predict_and_plot_confusion_matrix(train_x_onehotCoding, train_y, cv_x_onehotCoding, cv_y, clf)
```

125

- 100

- 75

- 50

- 25

1.0

- 0.8

- 0.6

- 0.4

- 0.2

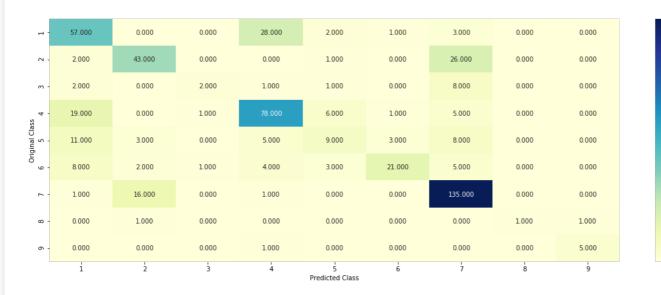
-00

- 0.75

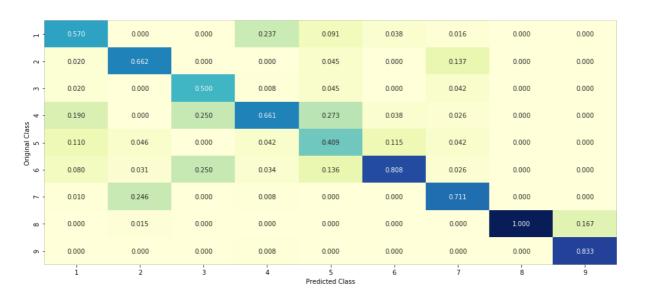
- 0.60

0.45

0.30

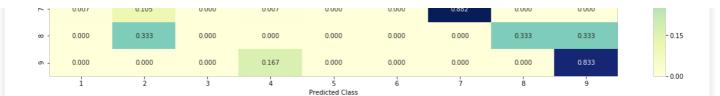






----- Recall matrix (Row sum=1) ------





#### 4.3.1.3. Feature Importance

```
In [66]:
```

```
def get_imp_feature_names(text, indices, removed_ind = []):
    word present = 0
    tabulte list = []
    incresingorder ind = 0
    for i in indices:
        if i < train_gene_feature_onehotCoding.shape[1]:</pre>
            tabulte list.append([incresingorder ind, "Gene", "Yes"])
        elif i< 18:
            tabulte_list.append([incresingorder_ind,"Variation", "Yes"])
        if ((i > 17) \& (i not in removed ind)):
            word = train_text_features[i]
            yes_no = True if word in text.split() else False
            if yes no:
                word present += 1
            tabulte list.append([incresingorder_ind,train_text_features[i], yes_no])
        incresingorder\_ind += 1
    print(word_present, "most importent features are present in our query point")
    print("-"*50)
    print("The features that are most importent of the ",predicted cls[0]," class:")
    print (tabulate(tabulte_list, headers=["Index",'Feature name', 'Present or Not']))
```

#### 4.3.1.3.1. Correctly Classified point

```
In [67]:
```

```
# from tabulate import tabulate
clf = SGDClassifier(class_weight='balanced', alpha=alpha[best_alpha], penalty='l2', loss='log', ran
dom state=42)
clf.fit(train x onehotCoding,train y)
test_point_index = 1
no feature = 500
predicted cls = sig clf.predict(test x onehotCoding[test point index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
np.round(sig clf.predict proba(test x onehotCoding[test point index]),4))
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.coef )[predicted cls-1][:,:no feature]
print("-"*50)
get_impfeature_names(indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test_point_index], no_feature)
Predicted Class: 4
Predicted Class Probabilities: [[3.766e-01 5.990e-02 5.900e-03 4.614e-01 2.100e-02 4.120e-02 3.120
e - 02
  2.400e-03 4.000e-04]]
Actual Class : 3
184 Text feature [1673] present in test data point [True]
481 Text feature [11] present in test data point [True]
Out of the top 500 features 2 are present in query point
```

#### 4.3.1.3.2. Incorrectly Classified point

```
In [68]:
```

```
test_point_index = 100
no_feature = 500
```

```
predicted cls = sig clf.predict(test x onehotCoding[test point index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
np.round(sig clf.predict proba(test x onehotCoding[test point index]),4))
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.coef)[predicted cls-1][:,:no feature]
print("-"*50)
get impfeature names(indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test point index], no feature)
Predicted Class : 1
Predicted Class Probabilities: [[5.295e-01 5.900e-03 8.000e-04 4.429e-01 7.800e-03 8.700e-03 2.500
 1.600e-03 3.000e-04]]
Actual Class : 4
 _____
221 Text feature [11] present in test data point [True]
234 Text feature [13] present in test data point [True]
328 Text feature [125] present in test data point [True]
432 Text feature [163] present in test data point [True]
Out of the top 500 features 4 are present in query point
```

### 4.3.2. Without Class balancing

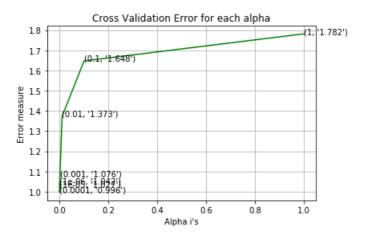
#### 4.3.2.1. Hyper paramter tuning

In [69]:

```
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n jobs=1, random state=None, learning rate='optimal', eta0
=0.0, power t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef_init, intercept_init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/geometric-in
tuition-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict_proba(X) Posterior probabilities of classification
# video link:
alpha = [10 ** x for x in range(-6, 1)]
cv log error array = []
for i in alpha:
   print("for alpha =", i)
   clf = SGDClassifier(alpha=i, penalty='12', loss='log', random state=42)
   clf.fit(train_x_onehotCoding, train_y)
   sig clf = CalibratedClassifierCV(clf, method="sigmoid")
   sig_clf.fit(train_x_onehotCoding, train_y)
```

```
sig clf probs = sig clf.predict proba(cv x onehotCoding)
    cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    print("Log Loss :",log loss(cv y, sig clf probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array, c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
    ax.annotate((alpha[i], str(txt)), (alpha[i], cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best alpha = np.argmin(cv log error array)
clf = SGDClassifier(alpha=alpha[best alpha], penalty='12', loss='log', random state=42)
clf.fit(train x onehotCoding, train y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x onehotCoding, train y)
predict y = sig clf.predict proba(train x onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y train,
predict_y, labels=clf.classes_, eps=1e-15))
predict y = sig clf.predict proba(cv x onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=1e-15))
```

```
for alpha = 1e-06
Log Loss: 1.0416137856317276
for alpha = 1e-05
Log Loss: 1.0266312464450722
for alpha = 0.0001
Log Loss: 0.9961974290273851
for alpha = 0.001
Log Loss: 1.0756890922790818
for alpha = 0.01
Log Loss: 1.3733161040645743
for alpha = 0.1
Log Loss: 1.6475765253978356
for alpha = 1
Log Loss: 1.7816740956313173
```



```
For values of best alpha = 0.0001 The train log loss is: 0.4145289103332108
For values of best alpha = 0.0001 The cross validation log loss is: 0.9961974290273851
For values of best alpha = 0.0001 The test log loss is: 1.089069587425559
```

### 4.3.2.2. Testing model with best hyper parameters

In [70]:

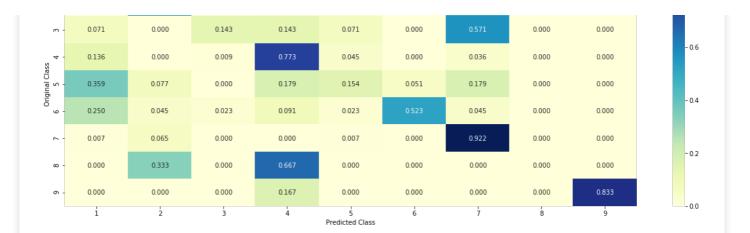


----- Precision matrix (Columm Sum=1) ------



----- Recall matrix (Row sum=1) -----

1 -	0.703	0.000	0.000	0.242	0.022	0.000	0.033	0.000	0.000
2 -	0.000		0.000	0.014	0.014	0.000		0.000	0.000



#### 4.3.2.3. Feature Importance, Correctly Classified point

```
Tn [711:
```

```
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='log', random_state=42)
clf.fit(train x onehotCoding,train y)
test_point_index = 1
no feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef )[predicted cls-1][:,:no feature]
print("-"*50)
get impfeature names (indices [0],
test df['TEXT'].iloc[test point index],test df['Gene'].iloc[test point index],test df['Variation']
.iloc[test point index], no feature)
Predicted Class: 1
Predicted Class Probabilities: [[5.061e-01 2.340e-02 4.200e-03 3.611e-01 1.200e-02 2.990e-02 6.010
e-02
  3.000e-03 2.000e-04]]
Actual Class : 3
216 Text feature [13] present in test data point [True]
290 Text feature [06] present in test data point [True]
443 Text feature [1008] present in test data point [True]
Out of the top 500 features 3 are present in query point
```

#### 4.3.2.4. Feature Importance, Inorrectly Classified point

# In [72]:

```
test point index = 100
no_feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
\verb"np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]), 4))" \\
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.coef_)[predicted_cls-1][:,:no_feature]
print("-"*50)
get impfeature names(indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test point index], no feature)
Predicted Class: 4
Predicted Class Probabilities: [[4.256e-01 1.590e-02 2.000e-04 5.396e-01 7.900e-03 5.800e-03 2.900
e - 03
  2.000e-03 1.000e-04]]
Actual Class: 4
357 Text feature [125] present in test data point [True]
359 Text feature [1met] present in test data point [True]
```

```
387 Text feature [11] present in test data point [True]
425 Text feature [04] present in test data point [True]
Out of the top 500 features 4 are present in query point
```

# 4.4. Linear Support Vector Machines

### 4.4.1. Hyper paramter tuning

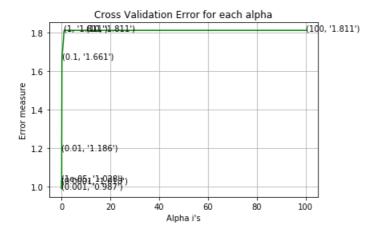
```
In [73]:
```

```
# read more about support vector machines with linear kernals here http://scikit-
learn.org/stable/modules/generated/sklearn.svm.SVC.html
# default parameters
# SVC(C=1.0, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, t
# cache size=200, class weight=None, verbose=False, max iter=-1, decision function shape='ovr', ra
ndom state=None)
# Some of methods of SVM()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-
online/lessons/mathematical-derivation-copy-8/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample_weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict_proba(X) Posterior probabilities of classification
# video link:
alpha = [10 ** x for x in range(-5, 3)]
cv log error array = []
for i in alpha:
   print("for C =", i)
     clf = SVC(C=i,kernel='linear',probability=True, class weight='balanced')
   clf = SGDClassifier( class weight='balanced', alpha=i, penalty='12', loss='hinge', random state
=42.
    clf.fit(train x onehotCoding, train y)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train x onehotCoding, train y)
    sig clf probs = sig clf.predict proba(cv x onehotCoding)
    cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    print("Log Loss :",log_loss(cv_y, sig_clf_probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
   ax.annotate((alpha[i],str(txt)), (alpha[i],cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
# clf = SVC(C=i,kernel='linear',probability=True, class weight='balanced')
clf = SGDClassifier(class weight='balanced', alpha=alpha[best alpha], penalty='l2', loss='hinge', r
```

```
andom_state=42)
clf.fit(train_x_onehotCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)

predict_y = sig_clf.predict_proba(train_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p_redict_y, labels=clf.classes_, eps=1e-15))
```

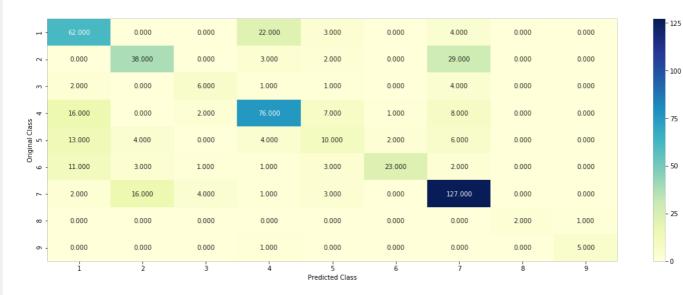
```
for C = 1e-05
Log Loss: 1.0277883889967174
for C = 0.0001
Log Loss: 1.017711976873179
for C = 0.001
Log Loss : 0.98672780417483
for C = 0.01
Log Loss: 1.1863350195666134
for C = 0.1
Log Loss: 1.6614809870077587
for C = 1
Log Loss: 1.81129299984073
for C = 10
Log Loss: 1.8112857229231774
for C = 100
Log Loss: 1.8112887384029561
```



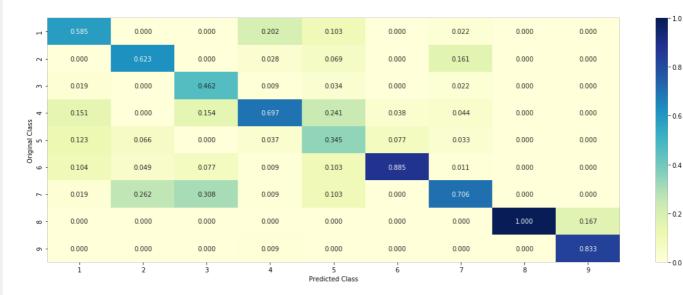
```
For values of best alpha = 0.001 The train log loss is: 0.5486032324500404
For values of best alpha = 0.001 The cross validation log loss is: 0.98672780417483
For values of best alpha = 0.001 The test log loss is: 1.1185141557394398
```

#### 4.4.2. Testing model with best hyper parameters

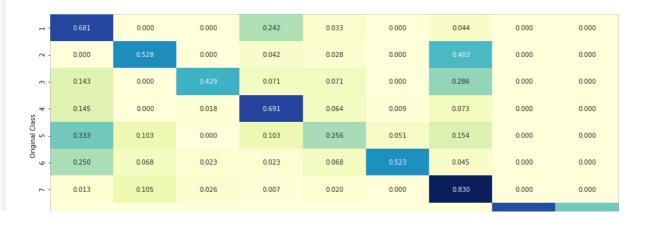
#### In [74]:



----- Precision matrix (Columm Sum=1) -----



----- Recall matrix (Row sum=1) -----

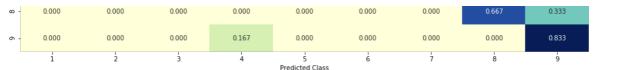


0.75

- 0.60

0.45

- 0.30



# -0.15

### 4.3.3. Feature Importance

#### 4.3.3.1. For Correctly classified point

```
In [75]:
```

```
clf = SGDClassifier(alpha=alpha[best alpha], penalty='12', loss='hinge', random state=42)
clf.fit(train x onehotCoding,train y)
test_point_index = 1
# test_point_index = 100
no_feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.coef )[predicted cls-1][:,:no feature]
print("-"*50)
get_impfeature_names(indices[0],
test df['TEXT'].iloc[test point index],test df['Gene'].iloc[test point index],test df['Variation']
.iloc[test_point_index], no_feature)
Predicted Class: 1
Predicted Class Probabilities: [[0.4849 0.0321 0.0094 0.3564 0.012 0.0293 0.0739 0.001 0.001 ]]
Actual Class : 3
300 Text feature [06] present in test data point [True]
391 Text feature [18] present in test data point [True]
465 Text feature [13] present in test data point [True]
468 Text feature [1008] present in test data point [True]
Out of the top 500 features 4 are present in query point
```

# 4.3.3.2. For Incorrectly classified point

```
In [76]:
```

```
test_point_index = 100
no feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef )[predicted cls-1][:,:no feature]
print("-"*50)
get_impfeature_names(indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test_point_index], no_feature)
Predicted Class: 1
Predicted Class Probabilities: [[0.4911 0.0529 0.0022 0.3522 0.0442 0.0148 0.0378 0.0024 0.0023]]
Actual Class : 4
391 Text feature [18] present in test data point [True]
419 Text feature [158] present in test data point [True]
465 Text feature [13] present in test data point [True]
Out of the top 500 features 3 are present in query point
```

#### 4.5 Random Forest Classifier

#### 4.5.1. Hyper paramter tuning (With One not Encoding)

In [77]:

```
# default parameters
# sklearn.ensemble.RandomForestClassifier(n estimators=10, criterion='gini', max depth=None, min s
amples split=2,
# min_samples_leaf=1, min_weight_fraction leaf=0.0, max features='auto', max leaf nodes=None, min
impurity decrease=0.0,
# min impurity split=None, bootstrap=True, oob score=False, n jobs=1, random state=None,
verbose=0, warm start=False,
# class weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
\# predict(X) Perform classification on samples in X.
# predict proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
 feature importances : array of shape = [n features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link:
alpha = [100, 200, 500, 1000, 2000]
max depth = [5, 10]
cv_log_error_array = []
for i in alpha:
    for j in max depth:
       print("for n estimators =", i,"and max depth = ", j)
       clf = RandomForestClassifier(n estimators=i, criterion='gini', max depth=j, random state=42
, n jobs=-1)
       clf.fit(train_x_onehotCoding, train_y)
        sig clf = CalibratedClassifierCV(clf, method="sigmoid")
        sig clf.fit(train_x_onehotCoding, train_y)
       sig clf probs = sig clf.predict proba(cv x onehotCoding)
        cv log error array.append(log loss(cv y, sig clf probs, labels=clf.classes , eps=1e-15))
        print("Log Loss :",log_loss(cv_y, sig_clf_probs))
'''fig, ax = plt.subplots()
features = np.dot(np.array(alpha)[:,None],np.array(max depth)[None]).ravel()
ax.plot(features, cv log error array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
   ax.annotate((alpha[int(i/2)], max\_depth[int(i\%2)], str(txt)),\\
(features[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best alpha = np.argmin(cv log error array)
clf = RandomForestClassifier(n estimators=alpha[int(best alpha/2)], criterion='gini', max depth=max
_depth[int(best_alpha%2)], random_state=42, n_jobs=-1)
clf.fit(train x onehotCoding, train y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
```

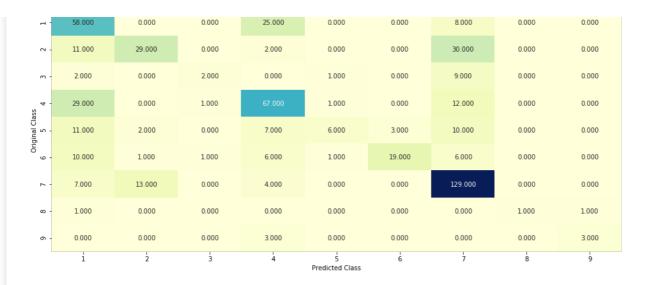
```
sig_clf.fit(train_x_onehotCoding, train_y)
predict y = sig clf.predict proba(train x onehotCoding)
print('For values of best estimator = ', alpha[int(best_alpha/2)], "The train log loss
is:",log loss(y train, predict y, labels=clf.classes , eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_onehotCoding)
print('For values of best estimator = ', alpha[int(best alpha/2)], "The cross validation log loss
is:",log loss(y cv, predict y, labels=clf.classes , eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best estimator = ', alpha[int(best alpha/2)], "The test log loss
is:",log_loss(y_test, predict_y, labels=clf.classes_, eps=1e-15))
for n estimators = 100 and max depth = 5
Log Loss : 1.1871913034149577
for n_{estimators} = 100 and max depth = 10
Log Loss: 1.2008652546844876
for n estimators = 200 and max depth = 5
Log Loss : 1.177984271330672
for n estimators = 200 and max depth = 10
Log Loss: 1.1857118498130315
for n estimators = 500 and max depth = 5
Log Loss: 1.1603839257641497
for n_{estimators} = 500 and max depth = 10
Log Loss: 1.1797182123190368
for n estimators = 1000 and max depth = 5
Log Loss : 1.1573728839303261
for n estimators = 1000 and max depth = 10
Log Loss : 1.1715823371359846
for n estimators = 2000 and max depth = 5
Log Loss : 1.1548718022616935
for n estimators = 2000 and max depth = 10
Log Loss : 1.1730732218915103
For values of best estimator = 2000 The train log loss is: 0.8545244378444445
For values of best estimator = 2000 The cross validation log loss is: 1.1548718014820822
For values of best estimator = 2000 The test log loss is: 1.205521549726899
```

#### 4.5.2. Testing model with best hyper parameters (One Hot Encoding)

```
In [78]:
# default parameters
# sklearn.ensemble.RandomForestClassifier(n estimators=10, criterion='gini', max depth=None, min s
amples split=2.
# min samples leaf=1, min weight fraction leaf=0.0, max features='auto', max leaf nodes=None, min
impurity decrease=0.0,
# min impurity split=None, bootstrap=True, oob score=False, n jobs=1, random state=None,
verbose=0, warm_start=False,
# class_weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature importances : array of shape = [n features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
clf = RandomForestClassifier(n_estimators=alpha[int(best_alpha/2)], criterion='gini', max_depth=max
depth[int(best alpha%2)], random state=42, n jobs=-1)
predict and plot confusion matrix(train x onehotCoding, train y,cv x onehotCoding,cv y, clf)
```

Number of mis-classified points: 0.40977443609022557 ------ Confusion matrix -----

Log loss: 1.1548718022616937



- 25

- 0.8

- 0.6

- 0.4

- 0.60

- 0.45

- 0.30

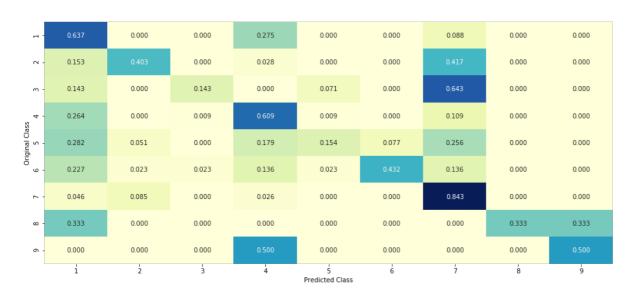
-0.15

- 0.00

----- Precision matrix (Columm Sum=1) -----



----- Recall matrix (Row sum=1) -----



# 4.5.3. Feature Importance

#### 4.5.3.1. Correctly Classified point

```
# test point index = 10
clf = RandomForestClassifier(n estimators=alpha[int(best alpha/2)], criterion='gini', max depth=max
_depth[int(best_alpha%2)], random state=42, n jobs=-1)
clf.fit(train x onehotCoding, train y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x onehotCoding, train y)
test_point_index = 1
no feature = 100
predicted cls = sig clf.predict(test x onehotCoding[test point index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
\verb"np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]), 4))" \\
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.feature importances )
print("-"*50)
get impfeature names(indices[:no feature], test df['TEXT'].iloc[test point index], test df['Gene'].
iloc[test point index], test df['Variation'].iloc[test point index], no feature)
Predicted Class: 1
Predicted Class Probabilities: [[0.4156 0.061 0.0179 0.2158 0.092 0.0905 0.099 0.0065 0.0018]]
Actual Class : 3
_____
4 Text feature [1g] present in test data point [True]
26 Text feature [141] present in test data point [True]
35 Text feature [117] present in test data point [True]
71 Text feature [17] present in test data point [True]
92 Text feature [12] present in test data point [True]
96 Text feature [1673] present in test data point [True]
Out of the top 100 features 6 are present in query point
```

#### 4.5.3.2. Inorrectly Classified point

```
In [80]:
```

```
test point index = 100
no_feature = 100
predicted cls = sig clf.predict(test x onehotCoding[test point index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
np.round(sig clf.predict proba(test x onehotCoding[test point index]),4))
print("Actuall Class :", test y[test point index])
indices = np.argsort(-clf.feature_importances_)
print("-"*50)
get_impfeature_names(indices[:no_feature], test_df['TEXT'].iloc[test_point_index],test_df['Gene'].
iloc[test_point_index], test_df['Variation'].iloc[test_point_index], no_feature)
Predicted Class: 1
Predicted Class Probabilities: [[0.3892 0.0565 0.0106 0.3033 0.0595 0.0529 0.1149 0.0069 0.0062]]
Actuall Class : 4
16 Text feature [1c] present in test data point [True]
26 Text feature [141] present in test data point [True]
71 Text feature [17] present in test data point [True]
76 Text feature [125] present in test data point [True]
92 Text feature [12] present in test data point [True]
Out of the top \ 100 features \ 5 are present in query point
```

### 4.5.3. Hyper paramter tuning (With Response Coding)

```
In [81]:
```

```
# ------
# default parameters
# sklearn.ensemble.RandomForestClassifier(n_estimators=10, criterion='gini', max_depth=None, min_s
amples_split=2,
# min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_
impurity_decrease=0.0,
# min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None,
verbose=0, warm_start=False,
# class_weight=None)
```

```
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample_weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature importances : array of shape = [n features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict_proba(X) Posterior probabilities of classification
# video link:
alpha = [10, 50, 100, 200, 500, 1000]
\max depth = [2,3,5,10]
cv_log_error_array = []
for i in alpha:
    for j in max depth:
       print("for n_estimators =", i,"and max depth = ", j)
        clf = RandomForestClassifier(n estimators=i, criterion='gini', max depth=j, random state=42
, n jobs=-1)
       clf.fit(train x responseCoding, train y)
        sig clf = CalibratedClassifierCV(clf, method="sigmoid")
        sig clf.fit(train x responseCoding, train y)
        sig_clf_probs = sig_clf.predict_proba(cv_x_responseCoding)
        cv log error array.append(log loss(cv y, sig clf probs, labels=clf.classes , eps=1e-15))
        print("Log Loss :",log_loss(cv_y, sig_clf_probs))
. . .
fig, ax = plt.subplots()
features = np.dot(np.array(alpha)[:,None],np.array(max_depth)[None]).ravel()
ax.plot(features, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
    ax.annotate((alpha[int(i/4)],max_depth[int(i%4)],str(txt)),
(features[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = RandomForestClassifier(n estimators=alpha[int(best alpha/4)], criterion='gini', max depth=max
 _depth[int(best_alpha%4)], random_state=42, n_jobs=-1)
clf.fit(train x responseCoding, train y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_responseCoding, train_y)
predict_y = sig_clf.predict_proba(train_x_responseCoding)
print('For values of best alpha = ', alpha[int(best_alpha/4)], "The train log loss is:",log loss(y
train, predict y, labels=clf.classes , eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_responseCoding)
print('For values of best alpha = ', alpha[int(best alpha/4)], "The cross validation log loss is:"
,log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_responseCoding)
print('For values of best alpha = ', alpha[int(best alpha/4)], "The test log loss is:",log loss(y
test, predict_y, labels=clf.classes_, eps=1e-15))
```

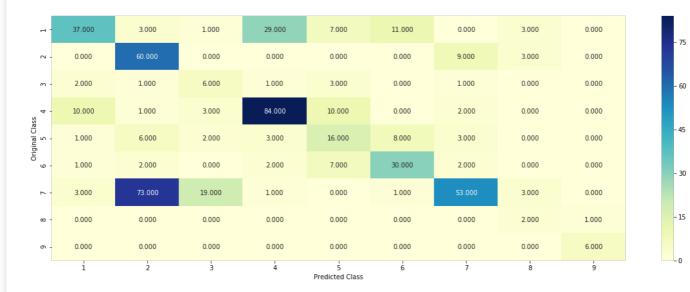
```
for n estimators = 10 and max depth = 2
Log Loss : 2.139267104191326
for n estimators = 10 and max depth = 3
Log Loss: 1.6299104374172773
for n estimators = 10 and max depth = 5
Log Loss : 1.41424870577866
for n estimators = 10 and max depth = 10
Log Loss: 1.6270134996125234
for n estimators = 50 and max depth = 2
Log Loss: 1.7310221225998332
for n estimators = 50 and max depth = 3
Log Loss : 1.4041832606738556
for n estimators = 50 and max depth = 5
Log Loss : 1.3244255868561363
for n estimators = 50 and max depth = 10
Log Loss: 1.7757140475003752
for n estimators = 100 and max depth = 2
Log Loss: 1.5972056754778616
for n estimators = 100 and max depth = 3
Log Loss: 1.4323699055270096
for n estimators = 100 and max depth = 5
Log Loss : 1.2507739261153945
for n estimators = 100 and max depth = 10
Log Loss: 1.726293381836022
for n_{estimators} = 200 and max depth = 2
Log Loss: 1.6403073593465964
for n estimators = 200 and max depth = 3
Log Loss: 1.4598520984779337
for n estimators = 200 and max depth = 5
Log Loss: 1.2971390642835883
for n estimators = 200 and max depth = 10
Log Loss : 1.6868808157429092
for n estimators = 500 and max depth = 2
Log Loss : 1.6665956169330705
for n estimators = 500 and max depth = 3
Log Loss : 1.510857860851123
for n estimators = 500 and max depth = 5
Log Loss : 1.3145229485201817
for n estimators = 500 and max depth = 10
Log Loss: 1.713294369727822
for n estimators = 1000 and max depth = 2
Log Loss: 1.6686845838021007
for n estimators = 1000 and max depth = 3
Log Loss : 1.5198573589099125
for n estimators = 1000 and max depth = 5
Log Loss : 1.304623884700354
for n_{estimators} = 1000 and max depth = 10
Log Loss: 1.709877150168174
For values of best alpha = 100 The train log loss is: 0.05480299322089486
For values of best alpha = 100 The cross validation log loss is: 1.250773926115395
For values of best alpha = 100 The test log loss is: 1.3004141198588886
```

### 4.5.4. Testing model with best hyper parameters (Response Coding)

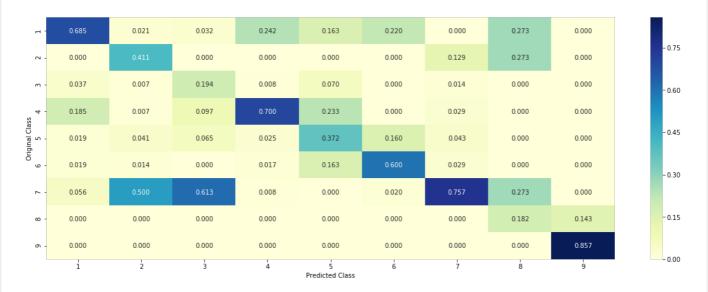
# In [82]:

```
# -------
# default parameters
# sklearn.ensemble.RandomForestClassifier(n_estimators=10, criterion='gini', max_depth=None, min_s
amples_split=2,
# min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_
impurity_decrease=0.0,
# min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None,
verbose=0, warm_start=False,
# class_weight=None)

# Some of methods of RandomForestClassifier()
# fit(X, y, [sample_weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict_proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature_importances_: array of shape = [n_features]
# The feature importances (the higher, the more important the feature).
```



----- Precision matrix (Columm Sum=1) -----



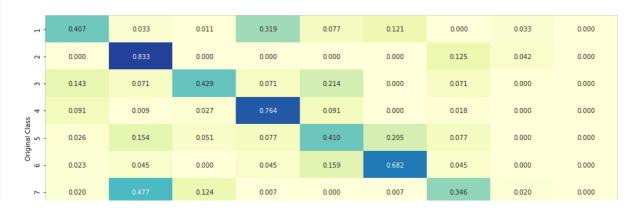
1.0

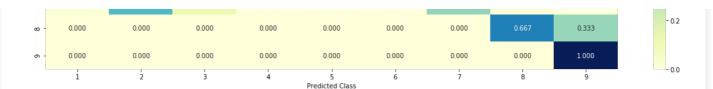
- 0.8

- 0.6

- 0.4

----- Recall matrix (Row sum=1) -----





### 4.5.5. Feature Importance

#### 4.5.5.1. Correctly Classified point

```
In [83]:
```

```
clf = RandomForestClassifier(n_estimators=alpha[int(best_alpha/4)], criterion='gini', max_depth=max
_depth[int(best_alpha%4)], random_state=42, n_jobs=-1)
clf.fit(train_x_responseCoding, train_y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x responseCoding, train y)
test point index = 1
no_feature = 27
predicted cls = sig clf.predict(test x responseCoding[test point index].reshape(1,-1))
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_responseCoding[test point index].reshape(1,-1)),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.feature importances )
print("-"*50)
for i in indices:
    if i<9:
        print("Gene is important feature")
    elif i<18:
       print("Variation is important feature")
    else:
       print("Text is important feature")
Predicted Class: 4
Predicted Class Probabilities: [[0.2071 0.0236 0.1277 0.4264 0.065 0.0763 0.0118 0.0275 0.0346]]
Actual Class : 3
Variation is important feature
Variation is important feature
Variation is important feature
Variation is important feature
Gene is important feature
Variation is important feature
Variation is important feature
Text is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Text is important feature
Text is important feature
Gene is important feature
Variation is important feature
Text is important feature
Gene is important feature
Variation is important feature
Variation is important feature
Text is important feature
Gene is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Gene is important feature
```

```
In [84]:
test point index = 100
predicted cls = sig clf.predict(test x responseCoding[test point index].reshape(1,-1))
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
np.round(sig clf.predict proba(test x responseCoding[test point index].reshape(1,-1)),4))
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.feature_importances_)
print("-"*50)
for i in indices:
    if i<9:
       print("Gene is important feature")
    elif i<18:
       print("Variation is important feature")
       print("Text is important feature")
Predicted Class: 4
Predicted Class Probabilities: [[0.2788 0.021 0.1708 0.3726 0.0351 0.0661 0.0096 0.0172 0.0289]]
Actual Class : 4
Variation is important feature
Variation is important feature
Variation is important feature
Variation is important feature
Gene is important feature
Variation is important feature
Variation is important feature
Text is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Text is important feature
Text is important feature
Gene is important feature
Variation is important feature
Text is important feature
Gene is important feature
Variation is important feature
Variation is important feature
Text is important feature
Gene is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Gene is important feature
```

#### 4.7 Stack the models

#### 4.7.1 testing with hyper parameter tuning

In [85]:

```
tuition-1/
# read more about support vector machines with linear kernals here http://scikit-
learn.org/stable/modules/generated/sklearn.svm.SVC.html
# default parameters
# SVC(C=1.0, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, t
01=0.001,
# cache size=200, class weight=None, verbose=False, max iter=-1, decision function shape='ovr', ra
ndom state=None)
# Some of methods of SVM()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
\# predict(X) Perform classification on samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-
online/lessons/mathematical-derivation-copy-8/
# read more about support vector machines with linear kernals here http://scikit-
learn.org/stable/modules/generated/sklearn.ensemble.RandomForestClassifier.html \\
# default parameters
# sklearn.ensemble.RandomForestClassifier(n estimators=10, criterion='gini', max depth=None, min s
# min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_
impurity decrease=0.0,
# min impurity split=None, bootstrap=True, oob score=False, n jobs=1, random state=None,
verbose=0, warm start=False,
# class weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature importances : array of shape = [n features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
clf1 = SGDClassifier(alpha=0.001, penalty='12', loss='log', class_weight='balanced', random_state=0
clf1.fit(train x onehotCoding, train y)
sig clf1 = CalibratedClassifierCV(clf1, method="sigmoid")
clf2 = SGDClassifier(alpha=1, penalty='12', loss='hinge', class weight='balanced', random state=0)
clf2.fit(train_x_onehotCoding, train_y)
sig clf2 = CalibratedClassifierCV(clf2, method="sigmoid")
clf3 = MultinomialNB(alpha=0.001)
clf3.fit(train x onehotCoding, train y)
sig clf3 = CalibratedClassifierCV(clf3, method="sigmoid")
sig clf1.fit(train x onehotCoding, train y)
print("Logistic Regression: Log Loss: %0.2f" % (log loss(cv y, sig clf1.predict proba(cv x onehot
Coding))))
sig clf2.fit(train x onehotCoding, train y)
print("Support vector machines : Log Loss: %0.2f" % (log loss(cv y,
sig_clf2.predict_proba(cv_x_onehotCoding))))
sig_clf3.fit(train_x_onehotCoding, train_y)
print("Naive Bayes : Log Loss: %0.2f" % (log_loss(cv_y, sig_clf3.predict_proba(cv_x_onehotCoding)))
print("-"*50)
alpha = [0.0001, 0.001, 0.01, 0.1, 1, 10]
best alpha = 999
for i in alpha:
lr = LogisticRegression(C=i)
```

```
sclf = StackingClassifier(classifiers=[sig clf1, sig clf2, sig clf3], meta classifier=lr, use p
robas=True)
   sclf.fit(train x onehotCoding, train y)
   print("Stacking Classifer : for the value of alpha: %f Log Loss: %0.3f" % (i, log loss(cv y, sc
lf.predict_proba(cv_x_onehotCoding))))
    log\_error = log\_loss(cv\_y, sclf.predict\_proba(cv\_x\_onehotCoding))
    if best alpha > log error:
        best alpha = log error
4
Logistic Regression: Log Loss: 0.95
Support vector machines : Log Loss: 1.81
Naive Bayes : Log Loss: 1.15
Stacking Classifer: for the value of alpha: 0.000100 Log Loss: 2.177
Stacking Classifer: for the value of alpha: 0.001000 Log Loss: 2.027
Stacking Classifer: for the value of alpha: 0.010000 Log Loss: 1.474
Stacking Classifer: for the value of alpha: 0.100000 Log Loss: 1.104
Stacking Classifer : for the value of alpha: 1.000000 Log Loss: 1.268
Stacking Classifer : for the value of alpha: 10.000000 Log Loss: 1.664
```

# 4.7.2 testing the model with the best hyper parameters

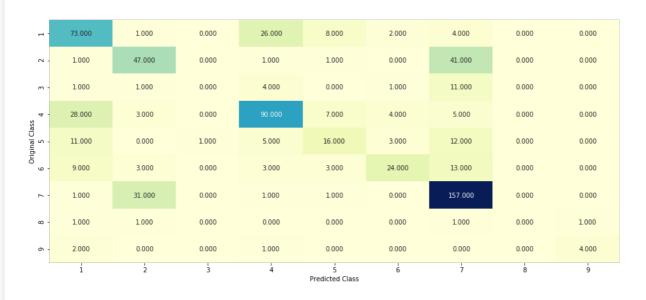
```
In [86]:
```

```
lr = LogisticRegression(C=0.1)
sclf = StackingClassifier(classifiers=[sig_clf1, sig_clf2, sig_clf3], meta_classifier=lr, use_proba
s=True)
sclf.fit(train_x_onehotCoding, train_y)
log_error = log_loss(train_y, sclf.predict_proba(train_x_onehotCoding))
print("Log loss (train) on the stacking classifier :",log_error)
log_error = log_loss(cv_y, sclf.predict_proba(cv_x_onehotCoding))
print("Log loss (CV) on the stacking classifier :",log_error)
log_error = log_loss(test_y, sclf.predict_proba(test_x_onehotCoding))
print("Log loss (test) on the stacking classifier :",log_error)

print("Number of missclassified point :", np.count_nonzero((sclf.predict(test_x_onehotCoding)-test_y))/test_y.shape[0])
plot_confusion_matrix(test_y=test_y, predict_y=sclf.predict(test_x_onehotCoding))

Log loss (train) on the stacking classifier : 0.5919636909006337
Log loss ((V) on the stacking classifier : 0.5919636909006337
```

Log loss (train) on the stacking classifier: 0.5919636909006337 Log loss (CV) on the stacking classifier: 1.103928043162243 Log loss (test) on the stacking classifier: 1.1820319422217422 Number of missclassified point: 0.3819548872180451 ------ Confusion matrix -------



----- Precision matrix (Columm Sum=1) ------

- 120

- 90

- 30



------ Recall matrix (Row sum=1)

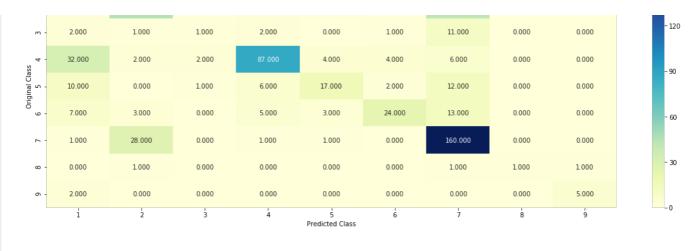


# 4.7.3 Maximum Voting classifier

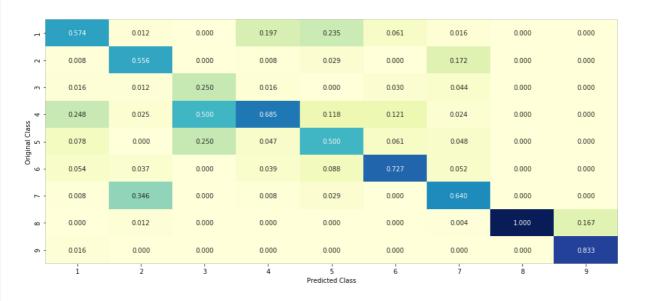
```
In [87]:
#Refer:http://scikit-learn.org/stable/modules/generated/sklearn.ensemble.VotingClassifier.html
from sklearn.ensemble import VotingClassifier
vclf = VotingClassifier(estimators=[('lr', sig_clf1), ('svc', sig_clf2), ('rf', sig_clf3)], voting=
'soft')
vclf.fit(train_x_onehotCoding, train_y)
print("Log loss (train) on the VotingClassifier:", log loss(train y,
vclf.predict proba(train x onehotCoding)))
print("Log loss (CV) on the VotingClassifier:", log_loss(cv_y,
vclf.predict proba(cv x onehotCoding)))
print("Log loss (test) on the VotingClassifier:", log loss(test y,
vclf.predict_proba(test_x_onehotCoding)))
print("Number of missclassified point :", np.count nonzero((vclf.predict(test x onehotCoding)-
test_y))/test_y.shape[0])
plot_confusion_matrix(test_y=test_y, predict_y=vclf.predict(test_x_onehotCoding))
Log loss (train) on the VotingClassifier: 0.8469761018953182
Log loss (CV) on the VotingClassifier: 1.1281406017858757
Log loss (test) on the VotingClassifier: 1.2041189385686248
```

Number of missclassified point : 0.3774436090225564 ----- Confusion matrix -----

п -	74.000	1.000	0.000	25.000	8.000	2.000	4.000	0.000	0.000
2 -	1.000	45.000	0.000	1.000	1.000	0.000	43.000	0.000	0.000



----- Precision matrix (Columm Sum=1)



- 0.8

- 0.6

- 0.4

- 0.2

0.75

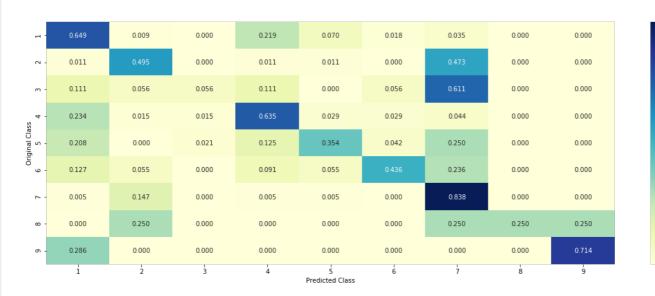
0.45

- 0.30

- 0.15

-0.00

----- Recall matrix (Row sum=1) -----



# 5. Conclusion

1. Applied TfidfVectorizer on all three features; Gene, Variation and text and taken top 2000 words with ngram\_range=(1,4)

```
x = PrettyTable()
x.field names = ["Vectorization", "Model", "Train Loss", "CV Loss", "Test Loss", "Percentage Miscla
ssified"]
x.add row(["OneHotEnCoding","NaiveBayes", 0.58,1.15,1.23,37.59])
x.add_row(["ResponseCoding","KNN",0.66,1.01,1.08,35.33])
x.add row(["OneHotEnCoding ClassBalancing", "LogisticRegression", 0.67, 0.95, 1.08, 34.02])
x.add_row(["OneHotEnCoding_Without_ClassBalancing","LogisticRegression",0.41,0.99,1.08,31.95])
x.add row(["OneHotEnCoding", "LinearSVM", 0.57, 0.98, 1.11, 34.39])
x.add row(["OneHotEnCoding", "RandomForest", 0.85, 1.15, 1.20, 40.97])
x.add_row(["ResponseCoding","RandomForest",0.05,1.25,1.30,44.73])
x.add_row(["OneHotEnCoding","Stacking",0.59,1.10,1.18,38.19])
x.add_row(["OneHotEnCoding","Voting",0.84,1.12,1.20,37.74])
print(x)
Vectorization
                               Model
                                                | Train Loss | CV Loss | Test Loss | F
rcentage Misclassified |
                     ------
          OneHotEnCoding
                           | NaiveBayes | 0.58 | 1.15 | 1.23 |
ResponseCoding | KNN
                                            0.66
                                                           | 1.01 | 1.08 |
          OneHotEnCoding ClassBalancing | LogisticRegression | 0.67 | 0.95 | 1.08 |
34.02
           | OneHotEnCoding Without ClassBalancing | LogisticRegression | 0.41
                                                          | 0.99 |
                                                                       1.08
                                                                             31.95
          OneHotEnCoding
                              - 1
                                    LinearSVM
                                                | 0.57 | 0.98 | 1.11 |
34.39
            | RandomForest | 0.85 | 1.15 | 1.2 |
          OneHotEnCoding
40.97
           | RandomForest | 0.05
          ResponseCoding
                                                              1.25 |
                                                                       1.3
44.73
```

1. After Applying TfidfVectorizer with top 2000 words, CV Log Loss for LogisticRegression with Class Balancing = 0.9

2. After Applying TfidfVectorizer with top 2000 words, CV Log Loss for LogisticRegression without Class Balancing = 0.99

Voting

| Stacking | 0.59 | 1.1 |

0.84

1.18

1.2

1.12

3. After Applying TfidfVectorizer with top 2000 words, CV Log Loss for LinearSVM = 0.98

OneHotEnCoding

OneHotEnCoding

38.19

4