

Solutions: Conditional Probability and Independence Checkpoint 2

Question 1

Dogs are inbred for such desirable characteristics as blue eye color; but an unfortunate by-product of such inbreeding can be the emergence of characteristics such as deafness. A 1992 study of Dalmatians (by Strain and others, as reported in *The Dalmatians Dilemma*) found the following:

(i)	31% of all Dalmatians have blue eyes.
(ii)	38% of all Dalmatians are deaf.
(iii)	42% of blue-eyed Dalmatians are deaf.

What is the probability that a randomly chosen Dalmatian is blue-eyed *and* deaf?

(a)

$.31 \cdot .38 = .1178$

(b)

$.31 \cdot .42 = .1302$

(c)

$.38 \cdot .42 = .1596$

(d)

$.31 / .38 = .8158$

(e)

$.31 / .42 = .7381$

(f)

$.38 / .42 = .9048$

Correct answer: (b)

Select one answer.
10 points

The next four questions refer to the following information:

Two methods, A and B, are available for teaching a certain industrial skill. There is an 80% chance of successfully learning the skill if method A is used, and a 95% chance of success if method B is used. However, method B is substantially more expensive and is therefore used only 25% of the time (method A is used the other 75% of the time). The following notations are suggested:

- **A**—method **A** is used
- **B**—method **B** is used
- **L**—the skill was **L**earned successfully

Question 2

Which of the following is the correct representation of the information that is provided to us?

(a)

$P(A) = .75, P(B) = .25, P(L | A) = .80, P(L | B) = .95$

(b)

$P(A) = .75, P(B) = .25, P(A | L) = .80, P(B | L) = .95$

(c)

$P(A) = .75, P(B) = .25, P(A \text{ and } L) = .80, P(B \text{ and } L) = .95$

(d)

$P(A | L) = .75, P(B | L) = .25, P(L | A) = .80, P(L | B) = .95$

(e)

$P(A \text{ and } L) = .75, P(B \text{ and } L) = .25, P(L | A) = .80, P(L | B) = .95$

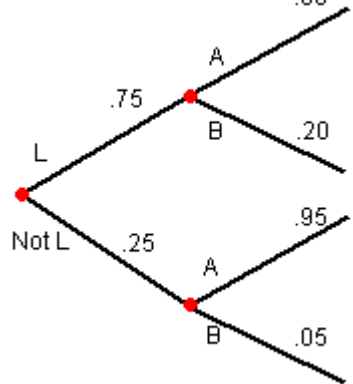
Correct answer: (a)

Select one answer.
10 points

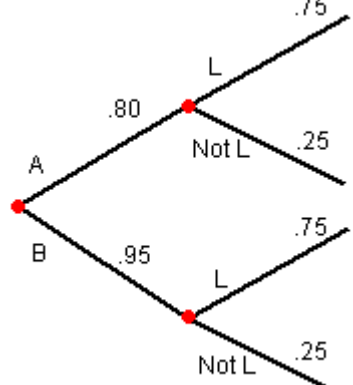
Question 3

Which of the following is the correct probability tree for this problem?

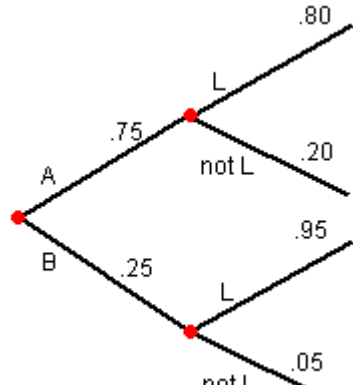
(a)



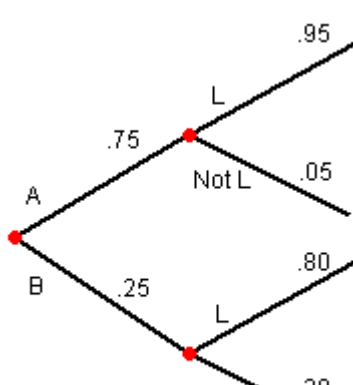
(b)



(c)



(d)



Correct answer: (c)

Select one answer.
10 points

Question 4

What is the probability that a worker will learn the skill successfully?

(a)

$P(L) = .75 \cdot .80 = .60$

(b)

$P(L) = .25 \cdot .95 = .2375$

(c)

$P(L) = .75 \cdot .25 + .80 \cdot .95 = .9475$

(d)

$P(L) = .75 \cdot .95 + .25 \cdot .80 = .9125$

(e)

$P(L) = .75 \cdot .80 + .25 \cdot .95 = .8375$

Correct answer: (e)

Select one answer.
10 points

Question 5

A worker learned the skill successfully. What is the probability that he was taught by method A?

(a)

$.75 \cdot .80 = .60$

(b)

$.80$

(c)

$$\frac{.25 \cdot .95}{.75 \cdot .80 + .25 \cdot .95} = .2836$$

(d)

$$\frac{.75 \cdot .80}{.75 \cdot .80 + .25 \cdot .95} = .7164$$

(e)

$$\frac{.75 \cdot .80}{.8 + .95} = .3429$$

Correct answer: (d)

Select one answer.
10 points