

Solutions: Conditional Probability and Independence Checkpoint 1

The first three questions refer to the following information:

Suppose a basketball team had a season of games with the following characteristics:

- 60% of all the games were **at-home** games. Denote this by **H** (the remaining were **away** games).
- 25% of all games were **wins**. Denote this by **W** (the remaining were **losses**).
- 20% of all games were at-home wins.

Question 1

Of the at-home games, we are interested in finding what proportion were wins. In order to figure this out, we need to find:

Select one answer.
10 points

- ☐ (a) $P(H)$
- ☐ (b) $P(W)$
- ☐ (c) $P(H \text{ and } W)$
- ☐ (d) $P(H \mid W)$
- ☐ (e) $P(W \mid H)$

Correct answer: (e)

Question 2

Of the at-home games, what proportion of games were wins? (Note: Some answers are rounded to two decimal places.)

Select one answer.
10 points

- ☐ (a) .12
- ☐ (b) .15
- ☐ (c) .20
- ☐ (d) .33
- ☐ (e) .42

Correct answer: (d)

Question 3

If the team won a game, how likely is it that this was a home game? (Note: Some answers are rounded to 2 decimal places.)

Select one answer.
10 points

- ☐ (a) .05
- ☐ (b) .12
- ☐ (c) .15
- ☐ (d) .42
- ☐ (e) .80

Correct answer: (e)

Question 4

Let A and B be two independent events. If $P(A) = .5$, what can you say about $P(A \mid B)$?

Select one answer.
10 points

- ☐ (a) Cannot find it since $P(B)$ is not known.
- ☐ (b) Cannot find it since $P(A \text{ and } B)$ is not known.
- ☐ (c) Cannot find it since both $P(B)$ and $P(A \text{ and } B)$ are not known.
- ☐ (d) It is equal to .5.
- ☐ (e) It is equal to .25.

Correct answer: (d)

Question 5

Dogs are inbred for such desirable characteristics as blue eye color; but an unfortunate by-product of such inbreeding can be the emergence of characteristics such as deafness. A 1992 study of Dalmatians (by Strain and others, as reported in *The Dalmatians Dilemma*) found the following:

Select one answer.
10 points

(i)	31% of all Dalmatians have blue eyes.
(ii)	38% of all Dalmatians are deaf.
(iii)	42% of blue-eyed Dalmatians are deaf.

Based on the results of this study is "having blue eyes" independent of "being deaf"?

- ☐ (a) No, since $.31 * .38$ is not equal to .42.
- ☐ (b) No, since .38 is not equal to .42.
- ☐ (c) No, since .31 is not equal to .42.
- ☐ (d) Yes, since $.31 * .38$ is not equal to .42.
- ☐ (e) Yes, since .38 is not equal to .42.

Correct answer: (b)