

## **Foundations of the Pawan Upadhyay's Pressure–Curvature Law of Gravity (PPC Law of Gravity)**

### **Definitions, Regimes, and Consistency Conditions**

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**Year:** 2025

### **Introduction :**

The Pawan Upadhyay's Pressure–Curvature Law of Gravity (PPC Law) provides a physically intuitive foundation for gravitational interaction by identifying pressure generated by mass–energy as the causal agent behind spacetime curvature and motion. While Newtonian gravity successfully describes gravitational forces and General Relativity accurately formulates gravity as spacetime geometry, neither framework explicitly emphasizes the physical role of pressure as the intermediary between energy and curvature.

The PPC Law bridges this conceptual gap by establishing a causal sequence in which mass–energy generates pressure, pressure produces forces, and these forces give rise to spacetime curvature through the stress–energy tensor. Motion and gravitational waves then emerge as natural consequences of this pressure-induced curvature. The PPC framework does not modify the equations of General Relativity; rather, it provides a physical interpretation of their content.

Two equivalent causal chains are presented below to express this foundation—one in terms of mass–energy, and the other in terms of energy density.

### **Causal Chain I: Mass–Energy–Based Formulation**

Mass-Energy → Pressure → Forces of Pressure → Curvature Via Stress-Energy Tensor →  
Spacetime Curvature → Geodesic Motion → Pressure Waves

### **Explanation :**

#### **Mass–Energy**

All gravitational phenomena originate from mass–energy. The presence of mass–energy establishes the fundamental source responsible for gravitational interaction.

#### **Pressure**

Mass–energy generates gravitational pressure, representing the physical intensity exerted on spacetime. Pressure acts as the intermediary between energy content and geometric response.

## Forces of Pressure

Pressure gives rise to forces that act both through space and on physical bodies. These forces mediate gravitational interaction and initiate motion.

### Curvature via the Stress–Energy Tensor

Pressure and energy density enter spacetime geometry through the stress–energy tensor, which mathematically encodes how matter and energy deform spacetime.

### Spacetime Curvature

Spacetime curvature is the geometric manifestation of gravitational pressure. It defines the structure of spacetime in which physical processes occur.

### Geodesic Motion

Objects move in response to curved spacetime. Motion is therefore not caused by a mysterious attraction but is the dynamical response to pressure-induced curvature.

### Pressure Waves

Time-dependent changes in pressure and curvature propagate through spacetime as pressure–curvature waves, corresponding physically to gravitational waves.

### Causal Chain II: Energy-Density–Based Formulation

E\_d → Pressure → Field Force, Surface Force → Curvature Via Stress-Energy Tensor → Spacetime Curvature → Geodesic Motion → Pressure Waves

### Explanation

#### Energy Density (E\_d)

Energy density, defined as  $E_d = \rho (c^2)$ , provides a quantitative measure of mass–energy concentration and serves as the fundamental gravitational source.

### Pressure

Energy density generates gravitational pressure, which characterizes the physical influence of energy on spacetime.

### Field Force and Surface Force

Gravitational pressure produces two complementary effects:  
The field force, arising from pressure gradients, governs acceleration and orbital motion through space.  
The surface force, arising when pressure acts on finite areas, governs binding, tidal effects, and internal stress in extended bodies.

### **Curvature via the Stress–Energy Tensor**

Both energy density and pressure contribute to spacetime curvature through the stress–energy tensor, ensuring consistency with General Relativity.

Spacetime Curvature

Curvature represents the structured deformation of spacetime produced by pressure.

### **Geodesic Motion**

Physical bodies follow trajectories determined by the curved spacetime geometry, resulting in gravitational motion.

### **Pressure Waves**

Dynamic variations in pressure and curvature propagate as pressure waves, representing the wave-like transmission of gravitational effects.

### **Unified Interpretation**

Both causal chains describe the same physical process from different perspectives. The first emphasizes mass–energy, while the second emphasizes energy density and force mechanisms. Together, they establish that:

- **Pressure is the physical cause of gravity,**
- **Curvature is the geometric effect,**
- **Motion is the dynamical response, and**
- **Pressure waves are the propagating manifestation of gravity.**

The PPC Law thus provides a coherent and physically intuitive foundation for gravitational phenomena while remaining fully consistent with Newtonian gravity in the weak-field limit and with General Relativity in all regimes.

### **Note :-**

The surface force ( $F_p = P_g A$ ),

exists only if:

- there is a field pressure, and
- there is an extended body with area A.

It is therefore:

- not independent
- not fundamental
- caused by the field pressure generated by the field force

👉 Surface force is a consequence, not a primary cause.

### **Important Points :**

#### **Two levels of chains**

##### **Level 1 — Fundamental PPC Chain :**

###### **1. Energy Density Chain**

( For Foundations / GR context)

Energy density → Pressure → Field force → Curvature via stress-energy Tensor → Spacetime curvature → Geodesic motion → Pressure waves

Or

###### **2. Mass-Energy Chain**

(For Interpretive sections)

Mass-Energy → Pressure → Field force → Curvature via stress-energy Tensor → Spacetime curvature → Geodesic motion → Pressure waves

Or

###### **3. Mass Chain**

[For Applications (orbits, planets)]

Mass → Pressure → Field force → Curvature via stress-energy Tensor → Spacetime curvature → Geodesic motion → Pressure waves

Or

#### **4. Mass density Chain**

**[For Applications (orbits, planets)]**

Mass density → Pressure → Field force → Curvature via stress-energy Tensor → Spacetime curvature → Geodesic motion → Pressure waves

**All Four PPC causal chains → mass-based, mass density based, mass–energy-based, and energy-density-based—are equivalent descriptions of the same gravitational process, differing only in the level of physical representation.**

“The fundamental PPC causal chain may be expressed either in terms of energy density, or mass–energy, or mass, or mass density, depending on the level of description.”

#### **Level 2 — Derived Physical Effects**

(Used when discussing planets, moons, structures)

Field force → Surface force → Binding, tides, internal stress, stability

# 1. Fundamental Definitions

## 1.1 Energy Density

In relativistic physics, mass density  $\rho$  corresponds to energy density:

$$E_d = \rho c^2$$

This is a **definition**, not an assumption.

## 1.2 Gravitational Pressure

In PPC gravity, gravitational interaction is interpreted through a **gravitational pressure field**  $P_g$ , defined generally as:

$$P_g = w E_d = w \rho c^2$$

where

- $w$  is a **dimensionless pressure-scaling parameter**,
- $0 \leq w \leq 1$ .

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## 2. Meaning of the Parameter $w$

The parameter  $w$  characterizes the **physical regime of matter-energy**:

Regime	Physical system
Non-relativistic	planets, moons, stars
Relativistic	radiation-dominated
Extreme / stiff	near black holes

<b>Physical system</b>	<b>Value of <math>w</math></b>
planets, moons, stars	$w \ll 1$
radiation-dominated	$w = \frac{1}{3}$
near black holes	$w = 1$

Thus,  $(\omega)$  controls how much of energy density manifests as gravitational pressure.

### 3. Maximum-Pressure Limit

The relation

$$P_g = E_d = \rho c^2$$

It is valid **if and only if**:

$$w = 1$$

This corresponds to the **maximum gravitational pressure state**, applicable to:

- black holes,
- near-event-horizon regions,
- extreme relativistic collapse.

## 4. Ordinary Astrophysical Systems

For systems such as:

- Moon–Earth,
- Earth–Sun,
- planetary and stellar dynamics,

matter is **non-relativistic**, therefore:

$$w \ll 1 \quad \Rightarrow \quad P_g \ll \rho c^2$$

In these systems:

- gravitational pressure exists,
- but it is **far below the maximum-pressure limit**,
- orbital motion arises from **pressure gradients**, not from extreme pressure.

## 5. Pressure-Gradient Force (Field Force)

The physical force associated with gravitational pressure is given by:

$$\mathbf{F} = -\nabla P_g$$

Substituting the general PPC definition:

$$\mathbf{F} = -\nabla(w\rho c^2)$$

This expression:

- reproduces standard gravitational acceleration in weak fields,
- introduces **no new force law**,
- provides a **causal physical interpretation** of gravity.

## 6. Relation to General Relativity

General Relativity already incorporates pressure through the stress-energy tensor:

$$T_{\mu\nu} = \left(\rho + \frac{p}{c^2}\right) u_\mu u_\nu + p g_{\mu\nu}.$$

In the weak-field limit:

$$\nabla^2 \Phi = 4\pi G \left(\rho + \frac{3p}{c^2}\right) = 4\pi G\rho(1 + 3w)$$

Thus:

- pressure is a genuine source of curvature,
- PPC gravity **does not modify GR equations**,
- it clarifies the **physical meaning** of pressure in curvature generation.

## 7. Summary of PPC Relations

$$E_d = \rho c^2$$

$$P_g = w E_d = w \rho c^2$$

$$\mathbf{F} = -\nabla P_g$$

$w \ll 1 \Rightarrow$  planets, moons, stars

$w = 1 \Rightarrow$  maximum-pressure (black holes)

## 8. Scientific Scope

- PPC gravity is an **interpretive framework**, not a new gravitational theory.
  - It preserves all predictions of Newtonian gravity and General Relativity.
  - It introduces **pressure as the causal agent** behind curvature.
  - Experimental and observational tests remain those of standard gravity.
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