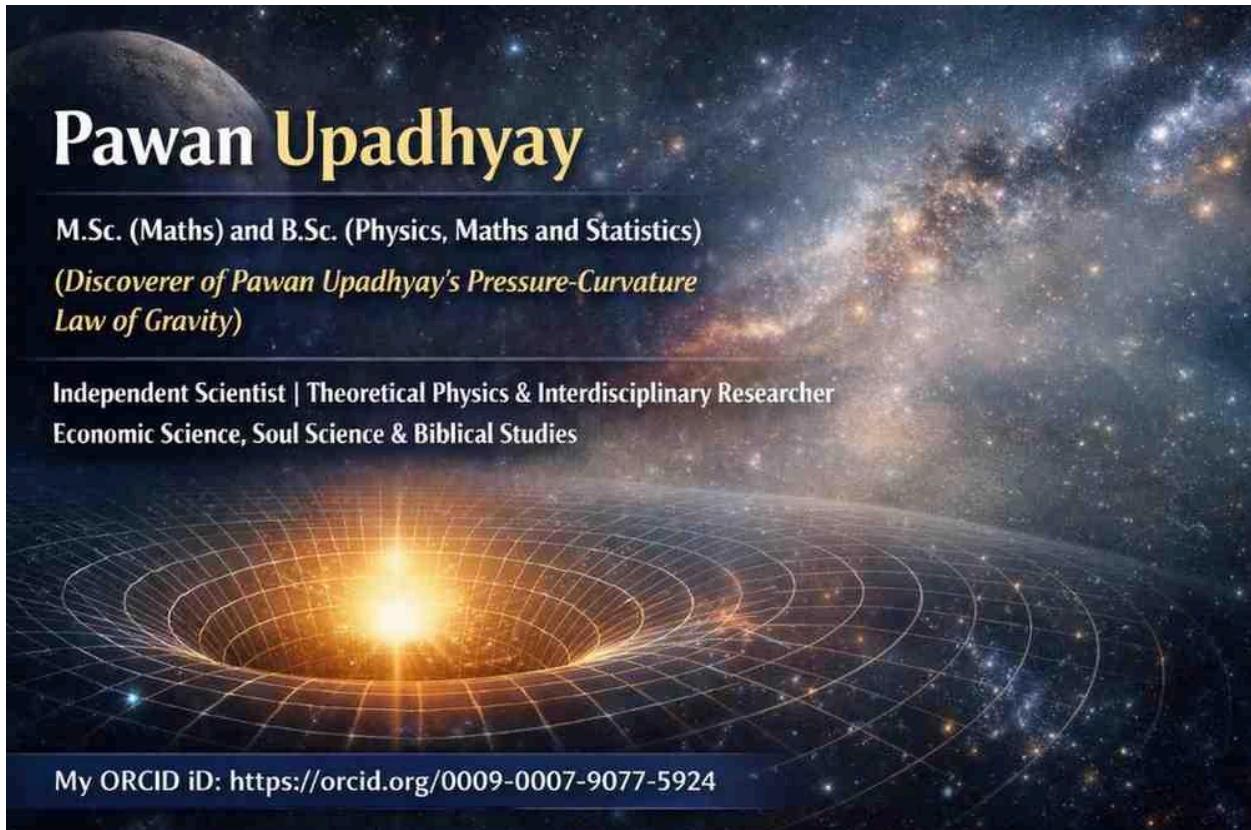


# Gravitational Pressure as the Central Mediator of Volume and Surface Forces

Author: Pawan Upadhyay

Affiliation: Independent Researcher

Email: [pawanupadhyay28@hotmail.com](mailto:pawanupadhyay28@hotmail.com)



## Abstract

In this work, gravitational pressure is identified as the central physical quantity linking local field dynamics to observable macroscopic forces. Within Pawan Upadhyay's Pressure–Curvature (PPC) framework, gravity is described using a hierarchy of force representations: local field force density, total volume force, local surface force, and total surface force. By clearly distinguishing these levels, the paper demonstrates how gravitational pressure mediates between spacetime geometry and measurable forces without introducing new fundamental

interactions. This formulation is fully consistent with continuum mechanics and General Relativity and provides a transparent physical interpretation of gravitational phenomena.

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## 1. Introduction

General Relativity describes gravity through spacetime geometry, while observable gravitational effects are often discussed in terms of forces and acceleration. To bridge this conceptual gap, the PPC framework emphasizes the role of gravitational pressure as the key scalar quantity underlying curvature and motion. Modern physics already recognizes pressure as a source of gravity through the stress–energy tensor. The purpose of this paper is to present a clean and self-contained explanation of how gravitational pressure generates forces at local and global levels.

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## 2. Gravitational Pressure in the PPC Framework

Gravitational pressure, denoted by  $P_g$ , represents the accumulated effect of energy density and stress in spacetime. It is not introduced as a new field but emerges naturally from the stress–energy content of matter and radiation. Within the PPC interpretation, pressure provides a physically intuitive way to understand how spacetime curvature influences motion.

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## 3. Local Field Force Density

At the most fundamental level, gravity is described by a local field force density acting throughout spacetime. This quantity represents force per unit volume and is generated by spatial variations of gravitational pressure.

The local field force density is defined as:

$$F = -\nabla P_g$$

This expression shows that local acceleration and motion arise from pressure gradients rather than from pressure itself. The field force density is equivalent to the inertial response of matter and governs local dynamics.

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## 4. Total Volume Force

For an extended system, the cumulative effect of the local field force density is obtained by integrating it over the volume of the system. This yields the total volume force acting on the system.

The total volume force is given by:

$$F_{\text{total}} = \int F \, dV$$

This quantity represents the net force resulting from pressure gradients distributed throughout the volume. It provides a macroscopic description of gravitational influence consistent with continuum mechanics.

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## 5. Local Surface Force

Gravitational pressure also produces forces directly on surfaces. When pressure acts on a surface element of area A, it generates a local surface force.

The local surface force is defined as:

$$F_p = P_g A$$

This force represents the direct mechanical action of gravitational pressure on boundaries or interfaces within a system.

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## 6. Total Surface Force

To obtain the complete surface force acting on an extended body, the local surface force must be integrated over the entire bounding surface. This yields the total surface force.

The total surface force is expressed as:

$$F_{p\text{total}} = \oint P_g \, dA$$

This formulation highlights how pressure acting on the boundary provides an alternative but equivalent description of gravitational force.

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## 7. Relationship Between Volume and Surface Forces

The total force obtained from pressure gradients within a volume and the total force obtained from pressure acting on the boundary surface represent two complementary descriptions of the same physical effect. In continuum mechanics, these descriptions are related through standard integral relations, ensuring consistency between local field dynamics and macroscopic force behavior.

Within the PPC framework, this equivalence reinforces the interpretation of gravitational pressure as the mediator between spacetime geometry and observable forces.

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## 8. Relation to Einstein's Equations

The formulation presented in this work does not modify or replace Einstein's field equations. In General Relativity, spacetime geometry is determined by the stress–energy tensor, whose components include energy density and pressure. Gravitational pressure, as used in the PPC framework, corresponds to the pressure components already present in the stress–energy description.

Einstein's field equations determine the spacetime metric from energy density and pressure, while the geodesic equation governs motion within that geometry. Within the PPC interpretation, local gravitational dynamics are expressed in force–pressure language by identifying the local field force density with the gradient of gravitational pressure.

Accordingly, the local field force density is given by:

$$F = -\nabla P_g$$

The total gravitational force acting on an extended system is obtained by integrating this local field force density over the system volume:

$$F_{\text{total}} = \int (-\nabla P_g) dV$$

This expression provides the macroscopic force corresponding to the same spacetime dynamics encoded geometrically in Einstein's equations. Thus, the PPC formulation offers an equivalent physical interpretation of gravitational motion while preserving the exact geometric structure of General Relativity.

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## 8. Central Role of Gravitational Pressure

The hierarchy of forces presented in this work demonstrates that gravitational pressure occupies a central position in gravitational physics. Local field dynamics originate from pressure

gradients, macroscopic volume forces arise from integrating these gradients, and observable surface forces result from pressure acting on boundaries.

Thus, gravitational pressure links:

- local spacetime dynamics,
- global force behavior,
- and measurable physical effects.

This unified view provides a coherent physical interpretation without modifying the geometric foundations of General Relativity.

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## 9. Conclusion

By systematically defining local field force density, total volume force, local surface force, and total surface force, this paper establishes gravitational pressure as the key quantity connecting microscopic dynamics to macroscopic observations. The PPC framework demonstrates that gravity can be understood as a pressure-mediated phenomenon fully compatible with General Relativity, offering enhanced conceptual clarity without introducing new fundamental laws.

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## Acknowledgments

The author acknowledges the foundational role of General Relativity and continuum mechanics in shaping the concepts presented in this work.