Formula

Arithmetic:

• Dividend = (Divisor X Quotient) + Remainder

• Average =
$$\frac{\sum of \ values}{no \ of \ value}$$

Algebra:

Series

• nth term of the A.P is given by $T_n = a + (n-1)d$

• Sum of n terms of A.P is given by $S_n = \frac{n}{2}(2a + (n-1)d)$

• nth term of the GP is given by $T_n = a r^{(n-1)}$

• Sum of the n term of G.P is given by $S_n = \frac{a(r^n - 1)}{r - 1}$

Important Result:

• $(1+2+3+4+...+n) = \frac{n(n+1)}{2}$

• $(1^2+2^2+3^2+....+n^2) = \frac{n(n+1)(2n+1)}{6}$

• $(1^3+2^3+3^3+\ldots+n^3)=(\frac{n(n+1)}{2})^2$

Equation and Factorization:

1.
$$(x+y)^2 = x^2 + 2xy + y^2$$

2.
$$(x-y)^2 = x^2 - 2xy + y^2$$

3.
$$(x+y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

4.
$$(x-y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$

5.
$$x^2 - y^2 = (x + y)(x - y)$$

6.
$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

7.
$$x^3 + y^3 = (x+y)(x^2 - xy + y^2)$$

8. If a quadratic equation is given in the question, say a x^2 +bx+c=0 and the option given is (px-r1)(qx-r2)

9. For the General equation a $x^2 + bx + c = 0$, the quadratic formula will be

$$\mathbf{x} = \frac{\left[-b \pm \sqrt{(b^2 - 4ac)}\right]}{2a}$$

Indices:

$$\bullet \qquad a^m X a^n = a^{(m+n)}$$

$$\bullet \qquad \frac{a^m}{a^n} = a^{(m-n)}$$

•
$$(a^m)^n = a^{(mXn)}$$

• $(ab)^n = a^n b^n$

•
$$(ab)^n = a^n b^n$$

$$\bullet \qquad \left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

•
$$a^0 = 1$$

$$\bullet \qquad a^{(-n)} = \frac{1}{a^n}$$

•
$$\sqrt[n]{a} = a^{\wedge}(1/n)$$
•
$$(\sqrt[n]{a})^n = a$$
•
$$\sqrt[m]{\sqrt[n]{a}} = \sqrt[m]{a}$$
•
$$(\sqrt[n]{a})^m = \sqrt[n]{a}^m$$

•
$$(\sqrt[n]{a})^n = a$$

•
$$\sqrt[m]{\sqrt[n]{a}} = \sqrt[mn]{a}$$

•
$$(\sqrt[n]{a})^m = \sqrt[n]{a^m}$$

Probability:

- $P(A) = \frac{\text{Number of outcomes favorable to A}}{\text{Number of all possible outcomes of the experiment}}$
- P(A) + P(A') = 1
- If A and B are independent events then, $P(A \cap B) = P(A) \times P(B)$
- If A and B are mutually exclusive events then, $P(A \cap B) = 0$
- Hence if A' denotes the complement event of A then, $P(A \cap A') = 0$
- Conditional Probability: P(A|B) denotes the probability that event A will occur given that event B has occurred already. Hence P(A|B) is given by,

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

where:

P(A|B) = the (conditional) probability that event A will occur given that event B has occurred

 $P(A \cap B)$ = the (unconditional) probability that event A and event B both occur.

P(B) = the (unconditional) probability that event B occurs

Permutation and combination:

•
$$1 \times 2 \times 3 \times 4 \dots \times (n-1) \times n = n!$$

•
$${}^{\mathrm{n}}\mathbf{P}_{\mathrm{r}} = \frac{n!}{(n-r)!}$$

• The number of permutations of n different objects taken r at a time, where $0 \le r \le n$ and the objects do not repeat is n (n-1) (n-2). . (n-r+1), which is denoted by ${}^{n}P_{n}$.

- **Principal of addition :** If two events E_1 and E_2 can occur independently in m and n ways respectively, then either of the two events can occur in (m+n)ways.
- **Principal of multiplication:** If an event can occur in m different ways, following which another event can occur in n different ways, then the total number of occurrence of the events in the order given is m x n.
- the number of combinations of n different objects taken r at a time, denoted by nCr.
- ${}^{n}C_{r} = n!/(n-r)!*r!$

Statistics:

• Mean = $\frac{\sum of \ all \ members \ value}{No. \ of \ member}$

Applied Math:

Profit and Loss =>

- Profit = S.P C.P
- Loss = C.P S.P
- Profit % = $\frac{(S.P-C.P)}{C.P}X$ 100
- Loss % = $\frac{(C.P S.P)}{C.P} X 100$

Work men Effort =>

- If A can do a piece of work in n days then A's one day's work = $\frac{1}{n}$
- If A can finish a work in X days and B can finish the same work in Y days then together they can finish the work in $\frac{XY}{X+Y}$ days

Speed =>

- Speed = Distance over time
- Average speed = $\frac{Total \ distance}{Total \ time}$

Conversions:

Currency:

- 1 Dollar = 100 cents
- Quarter = 25 cents

Length:

- 1 m(metre) = 100 cm(centimetres)
- 1 km(kilometre)=1000 m
- 1 in(inch) = 2.54 cm
- 1 ft(foot) = 12 in
- 1 mile = 1.6 km
- 1 mile = 5280 ft
- 1 yard = 3 ft

• 1 mile = 1760 yd

Weight:

• 1 Kg(Kilogram) = 1000 gm(gram)

• 1 t(tonne) = 1000 Kg

• 1 Pound = 0.45 Kg

• 1 ounce = 28.3495 grams

• 1 Pound = 16 ounces

Volume:

• 1 L(Litre) = 1000 ml(millilitre)

• $1 L = 1 dm^3$ (decimetre)

• $1 L = 0.001 \text{ m}^3 \text{U}$

• 1 gallon = 3.78 L

Quantity:

• 1 Dozen = 12

• 1 gross = 12 Dozen

• 1 great gross =12 gross

• 1 million = $1000000 = 10^6$

• 1 billion = $10000000000 = 10^9$

• x km/hr = x X 5 over 18 m/sec

• x m/sec = x X 18 over 5 km/hr

Clock:

• Angle between the minutes hand and hour hand is given by

$$\theta = \frac{11}{2} \quad M - 30 \text{ H}$$

Inequality:

• If n is positive integer than

$$n^{(n+1)} > (n+1)^n$$
 for $n > 3$

Geometry:

• Sum of the Interior or internal angle of an n-gon = $(n - 2) \times 180$

• Measure of each interior or internal angle of a regular polygon

$$= (n-2)X\frac{180}{n}$$

• Sum of the exterior angles of n-gon is = 360 degree

• The measure of each exterior angle of a regular polygon is = $\frac{360}{n}$

• Sum of the external angles of the polygon = (n + 2) X 180

• Pythagorean Theorem

$$z^2 = x^2 + y^2$$

• By Pythagorean theorem, for a right angle triangle,

$$z^2 = x^2 + y^2$$

If $z^2 > x^2 + y^2$, the angle formed is an **obtuse angle.**

If $z^2 < x^2 + y^2$, the angle formed is an **acute angle**.

- The ratio of the sides of 45-45-90 right angled triangle is 1:1: $\sqrt{2}$.
- The ratio of the sides of 30-60-90 right angled triangle is 1: $\sqrt{3}$: 2.

Area/Perimeter:

- Area of Rectangle = length X breadth
- Perimeter of rectangle = 2 (length + breadth)
- Area of square = $(side)^2$
- Perimeter of square = $4 \times \text{side}$
- Area of triangle = $\frac{1}{2}$ X base X height
- Area of equilateral triangle = $\frac{\sqrt{3}}{4}X(side)^2$
- Area of parallelogram = base X height
- Area of trapezium = $\frac{1}{2}X(a+b)Xh$

where a and b are length of the parallel sides, h is distance between them.

- Circumference of circle = $2 \pi r$
- Area of circle = πr^2
- length of Arc = $\frac{\theta}{360} X 2\pi r$
- area of circle = $\frac{\theta}{360} X \pi r^2$

Volume:

- Volume of cuboid = lbh
- Surface area cuboid = 2 (1b + bh + h1)
- Body Diagonal = $\sqrt{(l^2 + b^2 + h^2)}$
- Volume of cube = a^3
- Surface area = $6 a^2$
- Body diagonal = $\sqrt{3} a$
- volume of Sphere = $\frac{4}{3}\pi r^3$
- Surface area of Sphere = $4 \pi r^2$
- Volume of Cylinder = $\pi r^2 h$
- Curved surface area of cylinder = $2\pi rh$
- Total surface area of cylinder = $2\pi r (h + r)$
- Slant height of cone = $\sqrt{(h^2 + r^2)}$
- Volume of cone = $\frac{1}{3}\pi r^2 h$
- Curved surface area of cone = π rl
- Total surface area of cone = $\pi r (r + 1)$