Numerical modelling of physical systems

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Abstract. We present a new Python library enabling scientist to write accurate and effective numerical simulations. We investigate it's accuracy in a range of physical models, as Lorentz attractor and quantum harmonic oscillator.

Keywords: numerical modelling, Runge-Kutta, Numerov, chaos

- 1 Introduction
- 2 Numerical methods
- 2.1 Runge-Kutta method
- 2.2 Numerov's method
- 3 Models of physical systems
- 3.1 Classical harmonic oscillator
- 3.2 Lorentz attractor
- 3.3 Quantum harmonic oscillator
- 4 Conclusions



Fig. 1: Mock - just a template how to insert images.

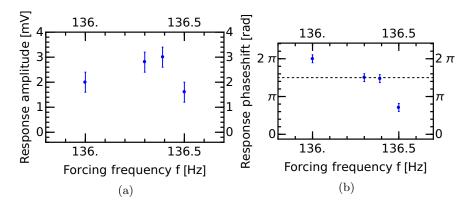


Fig. 2: Figure 2a presents response amplitude as a function of frequency. Figure 2b presents the phase-shift, dashed line denotes value $3\pi/4$ (value when the phase-shift is a quater of the whole period). Both figures show that the resonance frequency can be estimated as 136.4(1) Hz.

References

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