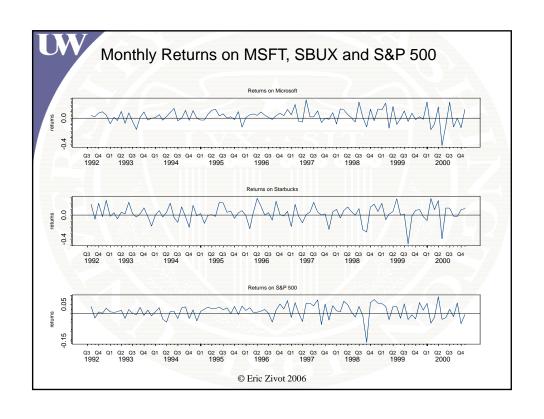


Eric Zivot
Summer 2012
Updated: July 17, 2012

© Eric Zivot 2006



```
Estimated Standard Errors
 > se.muhat = sigmahat.vals/sqrt(nobs)
 > rbind(muhat.vals,se.muhat)
                 sbux
                          msft
                                    sp500
 muhat.vals
                 0.0277
                          0.0275
                                    0.01253
   se.muhat
                 0.0135
                           0.0106
                                    0.00378
> se.sigma2hat = sigma2hat.vals/sqrt(nobs/2)
> rbind(sigma2hat.vals,se.sigma2hat)
                     sbux
                               msft
                                          sp500
                     0.01845
                               0.01141
sigma2hat.vals
                                          0.00143
  se.sigma2hat
                     0.00261
                               0.00161
                                          0.00020
> se.sigmahat = sigmahat.vals/sqrt(2*nobs)
> rbind(sigmahat.vals,se.sigmahat)
                   sbux
                             msft
                                       sp500
sigmahat.vals
                   0.1358
                             0.1068
                                       0.0378
                   0.0096
                             0.0075
                                       0.0026
  se.sigmahat
                      © Eric Zivot 2006
```

random permutations of the index vector 1:5 > sample(5) [1] 1 3 2 5 4 > sample(5) [1] 4 2 3 5 1 # random sample of size 5 from MSFT return with replacement > sample(MSFT, 5, replace=TRUE) [1] -0.02904 0.12130 -0.01890 -0.15332 -0.14627

UW

Brute Force Bootstrap

Same idea as Monte Carlo Simulation but instead of generating random data from an assumed distribution, you generate random data by sampling with replacement from the observed data

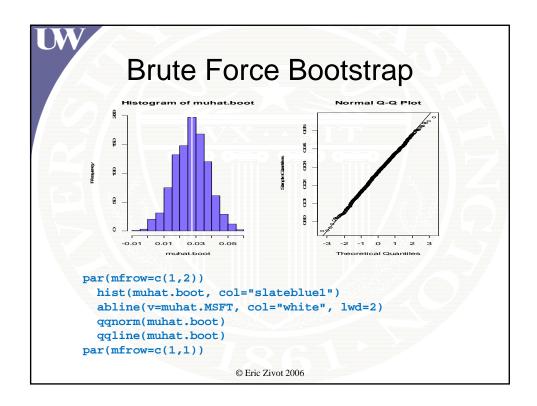
```
> B = 999 # why use 999?
> muhat.boot = rep(0, B)
> nobs = length(MSFT)
> for (i in 1:B) {
+ boot.data = sample(MSFT, nobs, replace=TRUE)
+ muhat.boot[i] = mean(boot.data)
}
```

© Eric Zivot 2006

UW

Brute Force Bootstrap

© Eric Zivot 2006

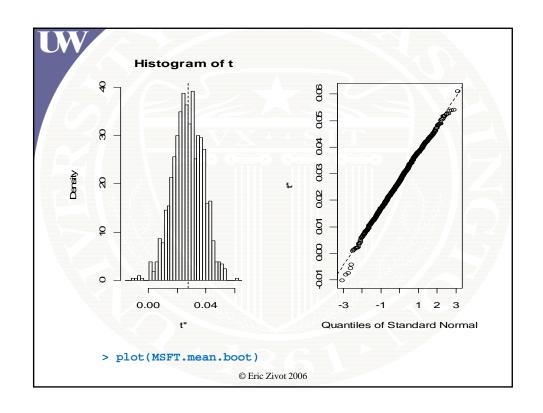


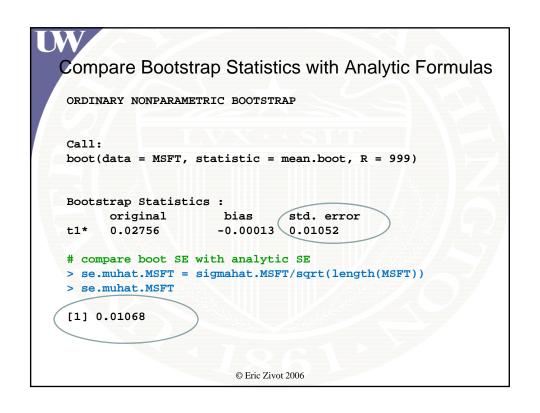
R Package boot

- Implements a variety of bootstrapping functions
- Background material is book by Davidson and Hinkley, Bootstrap Methods and Their Application, Cambridge University Press, 1997.
- · Main functions are:
 - boot ()bootstrap user supplied function
 - boot.ci() compute bootstrap confidence
 interval

© Eric Zivot 2006

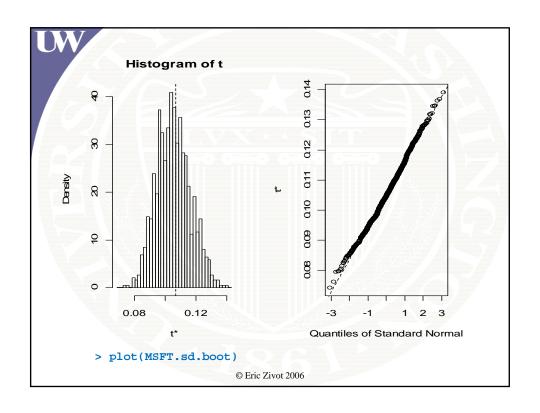
```
Example: Bootstrapping sample mean
 > MSFT.mean.boot = boot(MSFT, statistic = mean.boot, R=999)
 > class(MSFT.mean.boot)
 [1] "boot"
                                     Number of bootstrap samples
 > MSFT.mean.boot
 ORDINARY NONPARAMETRIC BOOTSTRAP
boot(data = MSFT, statistic = mean.boot, R = 999)
Bootstrap Statistics:
      original bias
                                std. error
                      -0.00013 0.01052
 t1*
       0.02756
                                         Bootstrap estimate of SE
Sample mean
                 Bootstrap estimate of
                          © Eric Zivot 2006
```





© Fric Zivot 2006


```
Example: Bootstrapping Sample SD
> MSFT.sd.boot = boot(MSFT, statistic = sd.boot, R=999)
> MSFT.sd.boot
ORDINARY NONPARAMETRIC BOOTSTRAP
Call:
boot(data = MSFT, statistic = sd.boot, R = 999)
Bootstrap Statistics :
     original
                bias
                          std. error
                -0.00145 0.01078
t1* 0.1068
# compare boot SE with analytic SE based on CLT
> se.sigmahat.MSFT = sigmahat.MSFT/sqrt(2*length(MSFT))
> se.sigmahat.MSFT
[1] 0.00755
                       © Eric Zivot 2006
```



Example: Boostrapping Normal VaR ValueAtRisk.boot = function(x, idx, p=0.05, w=100000) { # x.mat data to be resampled vector of scrambled indices created by # idx boot() function probability value for VaR calculation value of initial investment # value: # ans Value-at-Risk computed using resampled data q = mean(x[idx]) + sd(x[idx])*qnorm(p)VaR = (exp(q) - 1)*wVaR } © Eric Zivot 2006

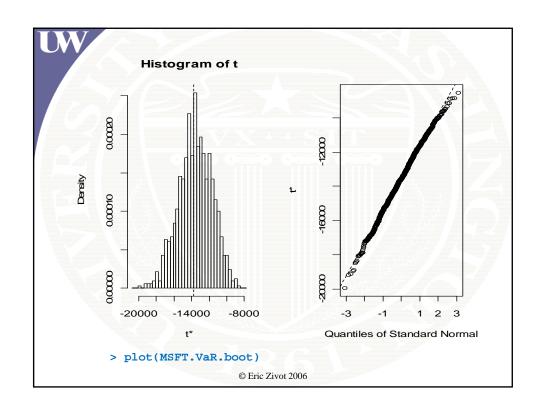
```
Example: Boostrapping Normal VaR

> MSFT.VaR.boot

ORDINARY NONPARAMETRIC BOOTSTRAP

Call:
boot(data = MSFT, statistic = ValueAtRisk.boot, R = 999)

Bootstrap Statistics:
    original bias std. error
t1* -13769.40 210.2801 1886.953
```



Example: Boostrapping Normal VaR > boot.ci(MSFT.VaR.boot, conf=0.95, type=c("norm", "perc")) BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS Based on 999 bootstrap replicates CALL: boot.ci(boot.out = MSFT.VaR.boot, conf = 0.95, type = c("norm", "perc")) Intervals: Level Normal Percentile 95% (-17678, -10281) (-17212, -10009) $\hat{\theta} \pm 2 \times SE_{boot}(\hat{\theta})$ [$q_{.025}^*$, $q_{.975}^*$]