

Exercise 1.18: Recall $\frac{m\langle v^2 \rangle}{2} = \frac{3}{2}k_bT$. If we fill in we get $\frac{(2 \cdot 2.3258671 \times 10^{-26} \text{ kg})\langle v^2 \rangle}{2} = \frac{3}{2}(1.38064852 \times 10^{-23} \text{ m}^2 \text{ kg s}^{-2} \text{ K}^{-1})(295 \text{ K})$ we then see $\langle v^2 \rangle = 1.3134 \times 10^5 \text{ m}^2/\text{s}^2$ or $\text{rms} = 362 \text{ m/s}$.

Exercise 1.21: After a quick bit of research (watching YouTube videos) I have concluded that hailstones colliding with a object is a inelastic process, they bounce back with trivial velocity if they don't stick. The force exerted by the hailstones would be $F_1 = .002 \text{ kg} * \sqrt{2}/2 * 15 \text{ m/s} * 30/\text{s} = 0.63640 \text{ N}$ thus the pressure would be 1.2728 Pa , whereas the atmospheric pressure is $101,000 \text{ Pa}$. However before one concludes that a glass window can easily support a hailstorm note that the pressure exerted by the atmosphere is exerted on both sides of the glass and thus does not actually put stress on the glass.

Exercise 1.34: (a) For A and C there is no change in volume and thus no work is done.

Define $\Delta P = P_2 - P_1$ and $\Delta V = V_2 - V_1$. The work done on the system for D is $w_D = P_1 \Delta V$ and for B it would be $w_B = -P_2 \Delta V$. For each step $\Delta U = U_f - U_i = 5/2 N k_b (T_f - T_i)$. Note that we are dealing with a ideal gas thus $PV = N k_b T$, and so $\Delta U = 5/2 (P_f V_f - P_i V_i)$. Now computing the changes in internal energy we get $\Delta U_A = 5/2 V_1 \Delta P$, $\Delta U_B = 5/2 P_2 \Delta V$, $\Delta U_C = -5/2 V_2 \Delta P$, $\Delta U_D = -5/2 P_1 \Delta V$. Noting that $Q = \delta U - w$ we see $Q_A = 5/2 V_1 \Delta P$, $Q_B = 5/2 P_2 \Delta V + P_2 \Delta V = 7/2 P_2 \Delta V$, $Q_C = -5/2 V_2 \Delta P$, $Q_D = -7/2 P_1 \Delta V$.

(b) In B a fixed force is applied to the piston while the gas is heated, allowing the gas to expand under constant pressure. In C the piston is locked and the gas is cooled. In D the gas is heated while a constant force is applied to the piston.

(c) The net work would be $w_B + w_D = P_1 \Delta V - P_2 \Delta V = -\Delta P \Delta V$. The net change in internal energy would be zero since this is a cycle and internal energy is a state function, to confirm $\Delta U_{total} = 5/2 (V_1 \Delta P + P_2 \Delta V - V_2 \Delta P - P_1 \Delta V) = 5/2 (-\Delta V \Delta P + \Delta P \Delta V) = 0$. The heat added to the system should be exactly the negation of the work done on the system thus $Q_{total} = \Delta P \Delta V$. In conclusion this is a cycle where net heat is added and work is extracted.