

ZESTAW ZADAŃ IX

Zadanie 1 Oblicz granice stosując reguły de l'Hospitala:

$$\begin{aligned} & \text{(a)} \lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x^2 - 4}, \text{(b)} \lim_{x \rightarrow 0} \frac{\operatorname{tg}(3x)}{e^{-2x} - 1}, \text{(c)} \lim_{x \rightarrow 1} \frac{\sqrt{2x - x^4} - \sqrt[3]{x}}{1 - \sqrt[4]{x^3}}, \text{(d)} \lim_{x \rightarrow 0} \frac{x \sin(5x)}{\cos(3x) - 1}, \text{(e)} \lim_{x \rightarrow 1} \frac{x^3 - x^2 - x + 1}{2x^3 - 3x^2 + 1}, \text{(f)} \lim_{x \rightarrow 0} \frac{e^x - e^{-x} - 2x}{x - \sin x}, \\ & \text{(g)} \lim_{x \rightarrow +\infty} \frac{\ln x}{x^5}, \text{(h)} \lim_{x \rightarrow +\infty} \frac{x^2}{e^x}, \text{(i)} \lim_{x \rightarrow 0^+} x^{10} \ln x, \text{(j)} \lim_{x \rightarrow 0} \left(\operatorname{ctg}^2 x - \frac{1}{x^2} \right), \text{(k)} \lim_{x \rightarrow +\infty} \left(\frac{x+1}{x+3} \right)^{2x+3}, \text{(l)} \lim_{x \rightarrow 0} \left(\frac{\sin x}{x} \right)^{\frac{1}{1 - \cos x}}. \end{aligned}$$