

# Probabilistic Modelling for Detecting Outliers in Medical Images

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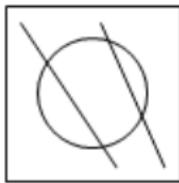
February 27, 2020

# Motivation

**A**



**B**



**C**



**D**

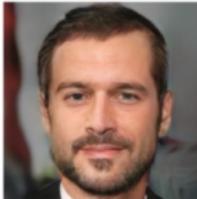
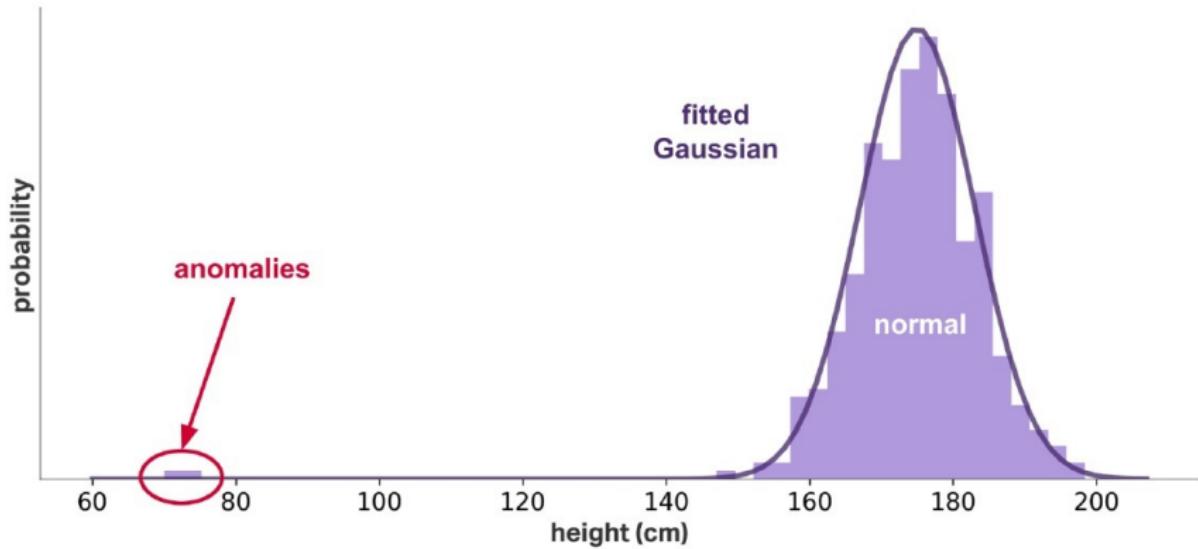


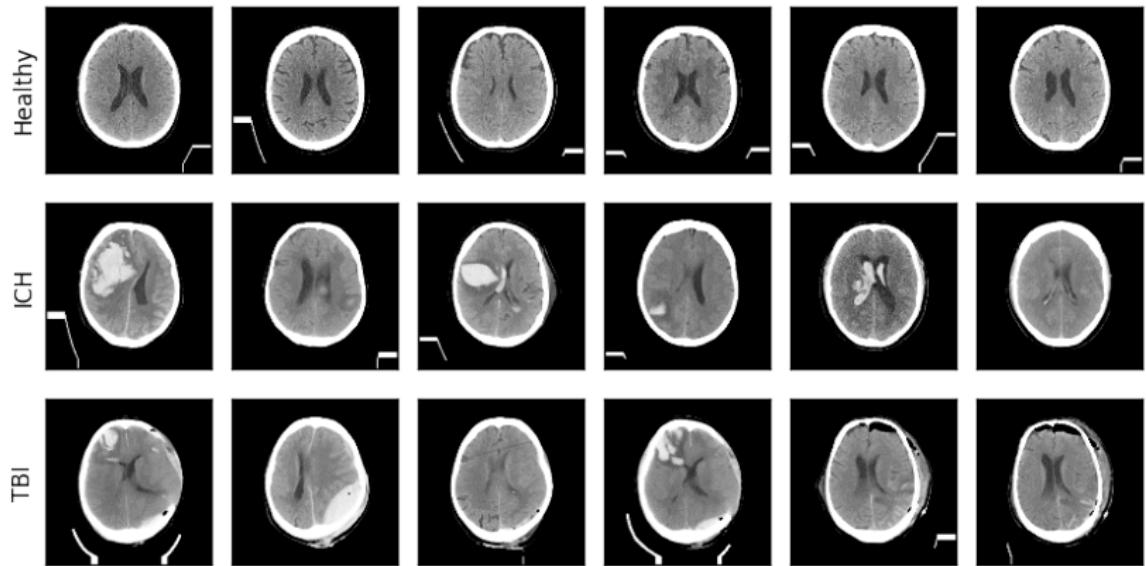
Image credit: <http://www.graduatewings.co.uk> & <https://www.elementai.com>

# Quantifying Normality - Toy Example

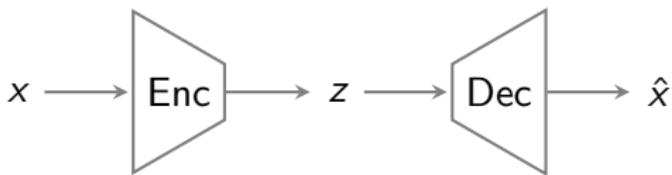
Let's model the distribution of the height of people:



# Treating Lesion Detection as Outlier Detection

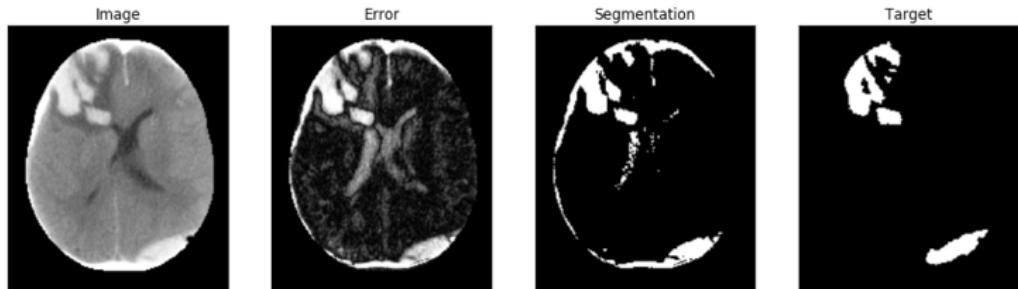
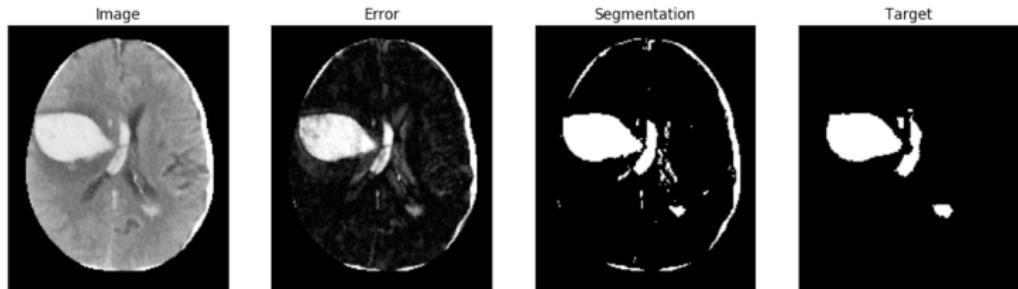


# Pixel-wise Outlier Detection



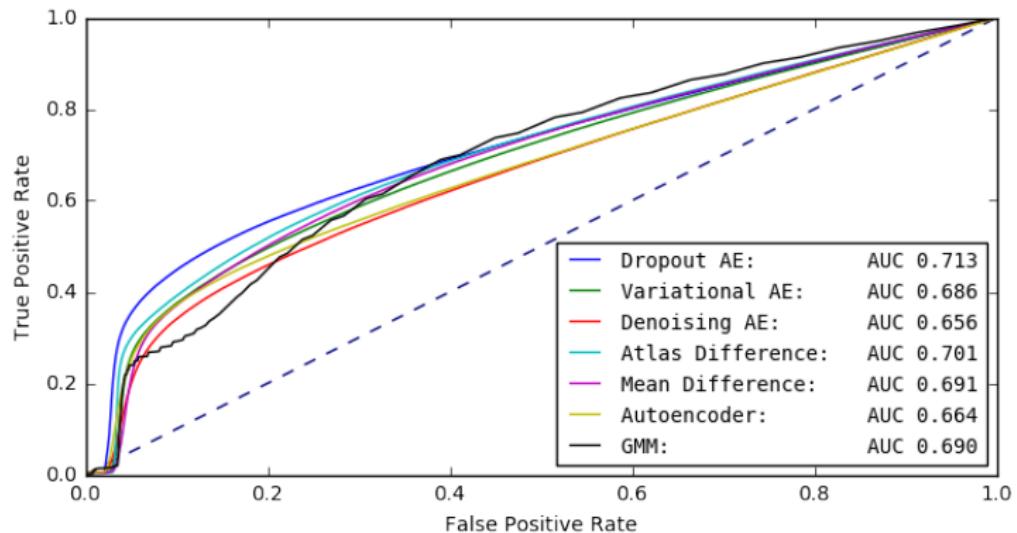
- Autoencoder learns about data distribution
  - Latent code  $z$  of VAEs informs about probability of single instance
- ⇒ Pixelwise reconstruction error informs about probability of image region:  $p(\text{outlier}) \propto |x - \hat{x}|$

# Segmenting Lesions

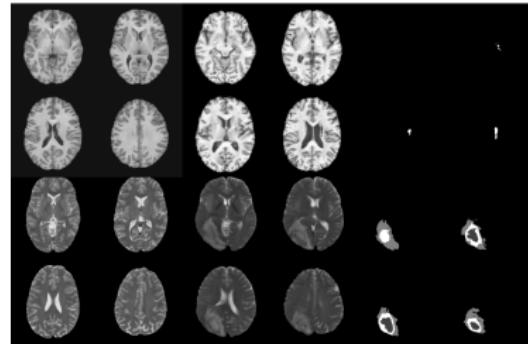


Possible segmentations by thresholding output of Dropout AE. Top: ICH, bottom: TBI

# Results - Intracranial Hemorrhages



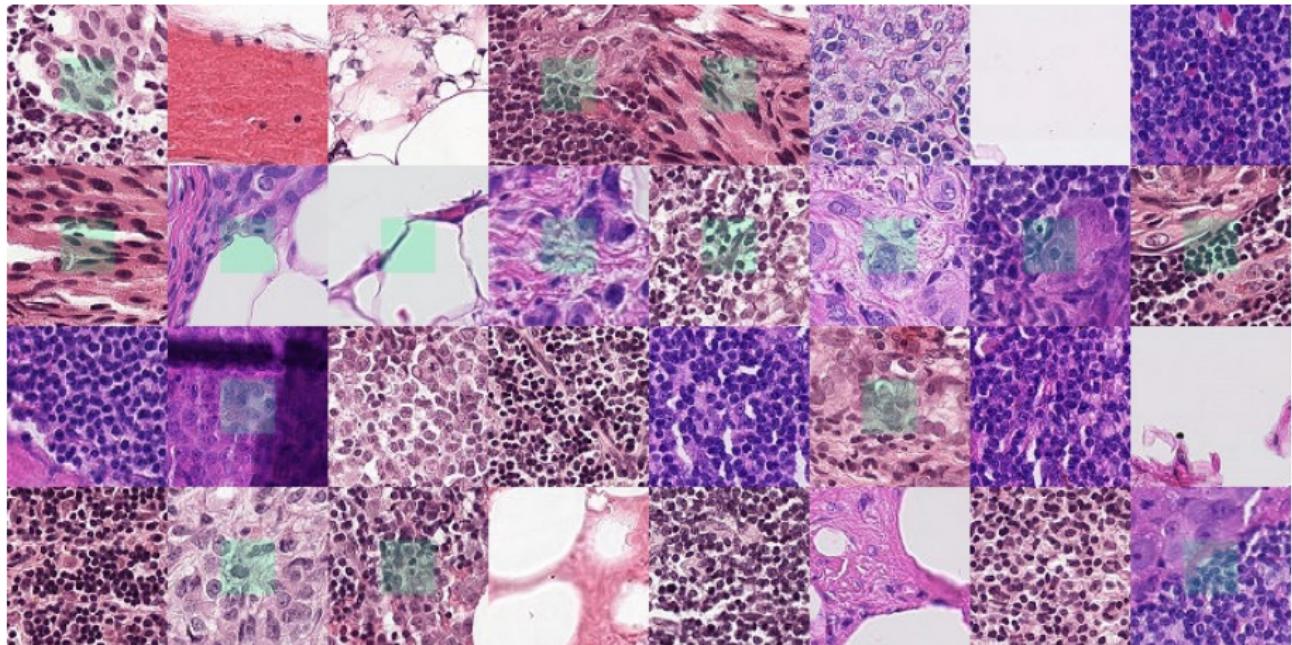
# Application to MRI



Example images: Healthy (CamCAN), Unhealthy (BraTS & ATLAS), Segmentations

Models	Latent variables	BraTS-T2w (whole tumor)		ATLAS-T1w	
		z	AUC	mDSC	AUC
mean	-		0.65	0.20	0.46
AE	256		0.63	0.41	0.49
DAE ( $\sigma=0.5$ )	256		0.59	0.29	0.41
VAE-128	(2,2,64)		0.69	0.42	0.64
VAE-BBB-128	(2,2,64)		0.69	0.40	0.67
VAE-256	(4,4,64)		0.67	0.40	0.66
AAE-128	(2,2,64)		0.70	0.41	0.63
AAE-256	(4,4,64)		0.67	0.38	0.60
$\alpha$ -GAN-128	128		0.66	0.35	0.60
$\alpha$ -GAN-256	256		0.67	0.37	0.60
GMM ( $\lambda_{out}=0.01$ )	-		0.80	0.22	0.78
GMM ( $\lambda_{out}=0.001$ )	-		0.79	0.21	0.77
U-net (supervised)	-		-	0.80	-
					0.50

# Detecting Cancerous Tissue on Histopathology

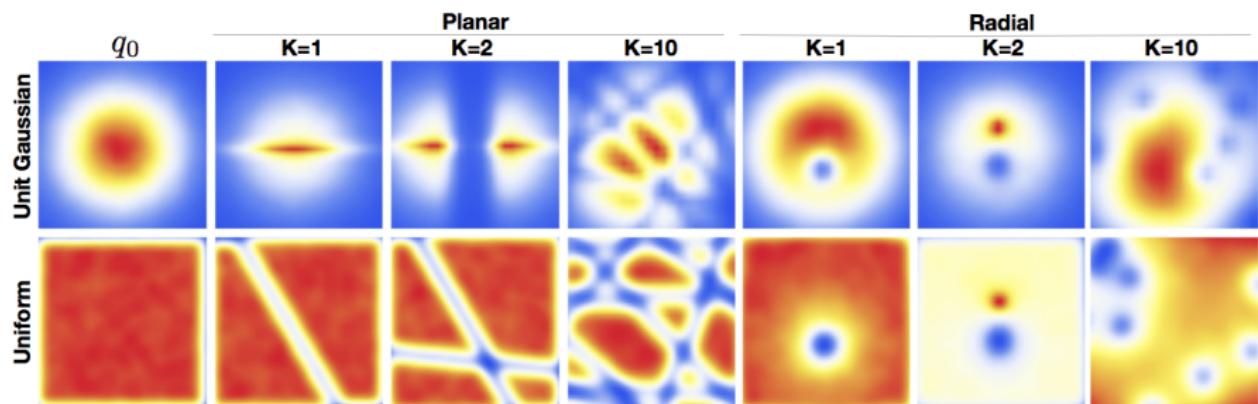


Examples of histopathology patches; green patches indicate cancerous patches.

# Normalising Flows

We model  $p(x)$  using invertible transformations  $f(x)$  on some base distribution  $\pi(u)$ :  $p(x) = \pi(f^{-1}(x)) \left| \det \frac{\partial f^{-1}}{\partial x} \right|$

We can approximate complex distributions by stacking simple transformations:



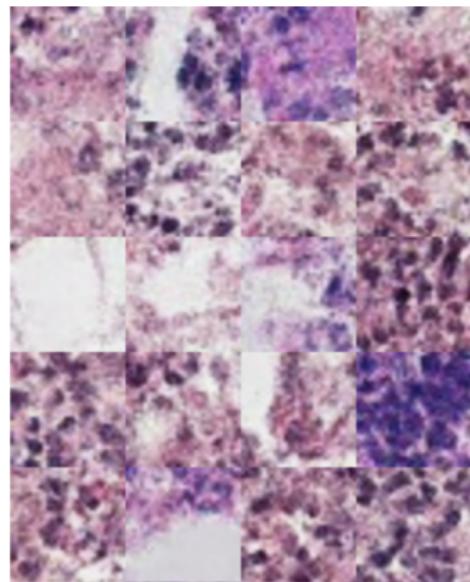
# Results

Method	Gaussian	RealNVP	VAE	ResNet@572	ResNet
AUROC	0.32	0.68	0.52	0.67	0.86

We compare the AUROC for:

- RealNVP (Dinh, et al. ICLR 2017) on  $32 \times 32$  px centre patches
- A Gaussian baseline fitted to each colour channel
- A supervised ResNet-50 with varying unhealthy examples
- VAE as described before

Synthethic patches:



# Conclusion

- Outlier detection can find medically relevant abnormalities
- VAEs seem to rely on intensity rather than including contextual information
- Normalising Flows offer more principled way to find outliers



Image credit: XKCD

# Thanks!



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