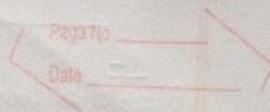


Some DBMS: SQL, MySQL, Oracle, DB2

Father of DBMS: EF Codd



- \* Data: known facts and statistics  
eg: text, image, audio, video etc
- \* Information: processed form of data, usable data
- \* Database: collection of related data stored together  
on purpose for further use
- \* Types of databases

### Structured Database (10%)

- data which can be organised in the form of rows and columns constitutes structured database
- eg: data of employees in a firm.
- stored and accessed using RDBMS etc.

### Unstructured Database (90%)

- data which can't be organised constitutes unstructured database  
nowadays it is utilised via AI
- eg: photos, videos, social media data
- cloud storage etc

### \* Database Management System (DBMS)

A system (software) which facilitates storage, maintenance & utilisation of database (structured)

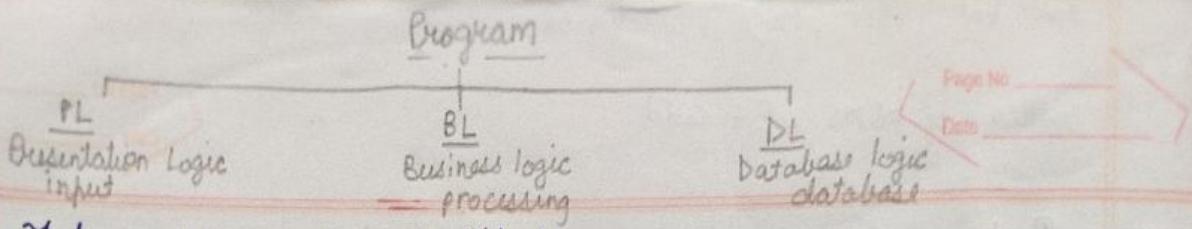
eg SQL (Microsoft)

Oracle 9i, 11, 12c (Oracle)

MySQL (Oracle)

DB2 (IBM)

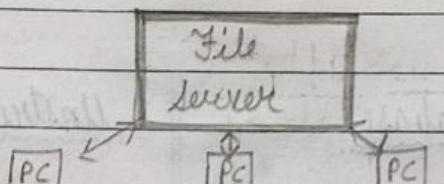
### \* Relational DBMS: DBMS which maintains data in the form of relations.



## Types of DBMS Architecture

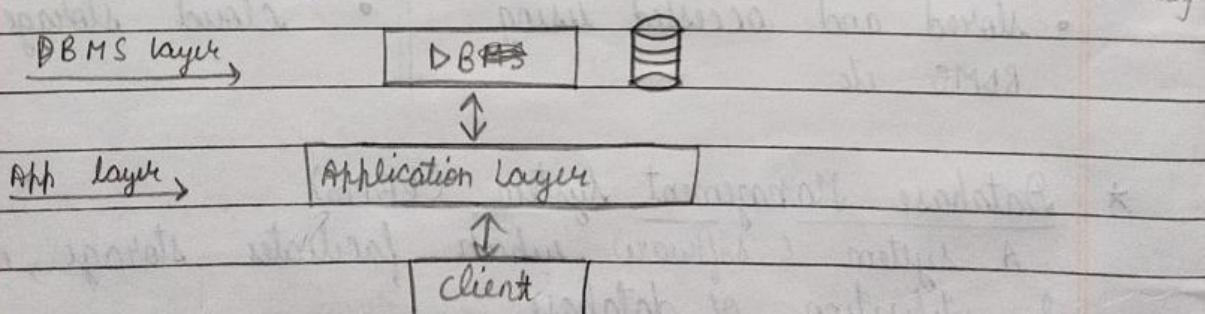
### 1) One-Tier Architecture

- client and server are at same place (usually in the same computer)
- (uses local servers)
- client directly access the file server
- includes window projects



### 2) Two-Tier Architecture

- usually client and server are at diff places & (at two diff machines connected via network)
- communicates through application layer (uses local servers)
- direct interaction with DBMS through application (ODBC)
- window projects



### Advantages

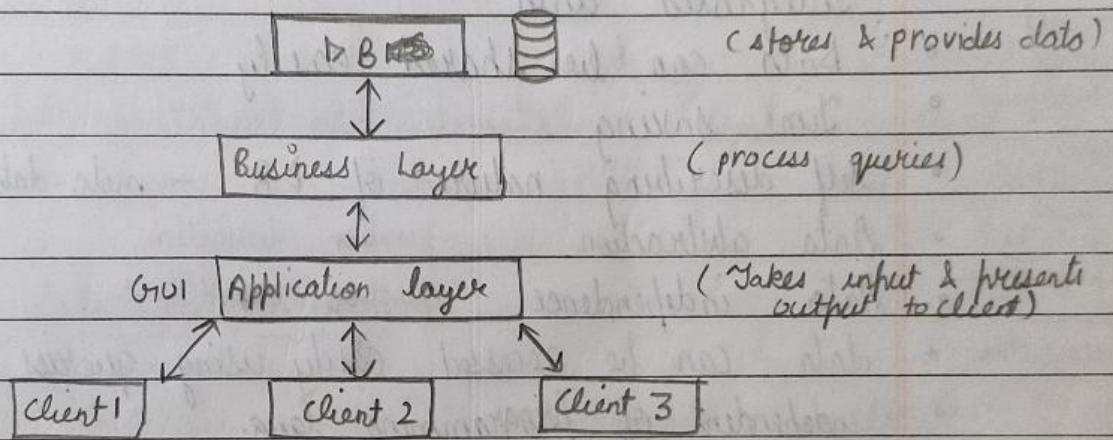
- easy to maintain & modify
- communication is faster
- 0

### Disadvantages

- limited clients
- security issues
- (queries are processed by database itself)

### 3) 3-Tier Architecture

- multiple clients are present at remote places & server too is located at a remote destination. (remote server is used)
- client doesn't interact directly with DBMS but through business layer.
- web projects



#### Advantages

- Security
- Scalability (large no. of remote clients can be handled)
- Performance is better (due to presence of business layer)

professional date

## Advantages of DBMS over file system

Disadv.

Requires  
technical  
person

- Reduce data redundancy
- Consistency of data
- ensures back up & recovery
- More privacy & security (role based access)
- Concurrency (Multiple access at same time) Multiple views
- Integrated data
- Data can be shared easily
- Time saving

It ensures  
correct  
transaction  
is performed

when  
multiple  
users  
tries to  
perform  
some  
transaction

- self describing nature of DB - meta-data (in catalog) In file pr. system
- Data abstraction operation abstraction
- Data independence operation independence
- data can be accessed easily using queries
- independent of programming lang.
- Atomicity either all or none
- Integrity (provides constraints)

### Terms related to RDBMS

- Entity set / relation - table
- entity / tuple / record / instance - row
- attributes / fields - columns
- degree - no. of attributes in a relation / no. of entity sets
- cardinality - no. of records

in case  
of relation  
ships

schemas: A logical representation of a database

\* Abstraction

Hiding the complexities of the system from the client & providing an abstract view of only relevant info.

\* Data Independence (Transparency)

Property of DBMS which helps to change the Database schema at one level of a database system without having to change the schema at <sup>next</sup> higher levels.

• logical data independence

*what is stored* Ability to change the logical schema without having to change external schema or application programs

eg: Addition or removal of new entities in conceptual schema won't effect existing application program.

- no effect on view level
- even if changes are made in <sup>concept</sup> schema by one user, views of other users won't change (bcz virtual schema of only required data is presented to them)
- user won't get any idea of change in concep. schema

• physical data independence

*how data is stored* Ability to change the physical schema without having to change logical schema

Types of models

Types of lang. DDL DML DCL  
File system v/s DBMS

Page No.

Date

e.g. Changes include:

- using new storage devices
- using different data structures
- Modifying indexes

e.g.

Name : Payal

Roll No : 23609

Page No \_\_\_\_\_

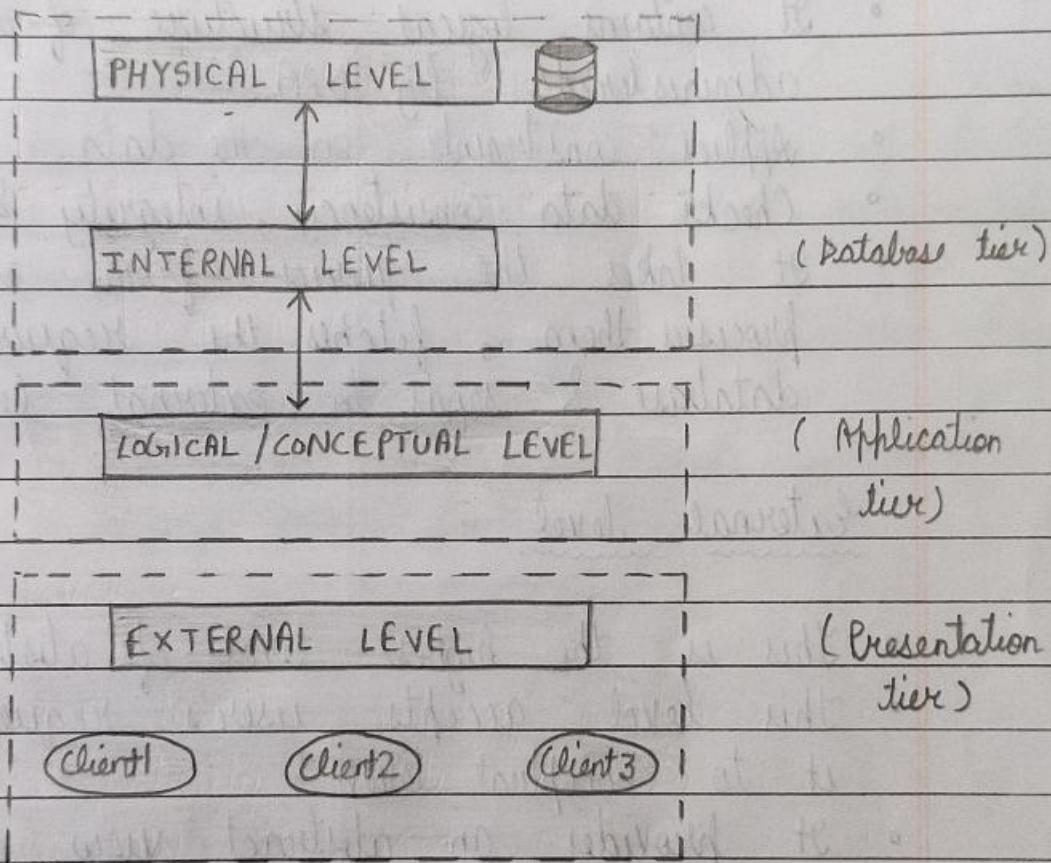
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This is a theoretical model

## THREE LEVEL OF ABSTRACTION (Three Tier Architecture)

It involves following three levels:

- 1> External level (client side)
- 2> Logical / Conceptual / Business level
- 3> Internal level



### Internal level

- This is the lowest level of abstraction and the one closest to the database.
- This level indicates HOW the data is stored in database (data structure, file structure)
- Describes address of data, memory utilised by the data, compression & encryption techniques.

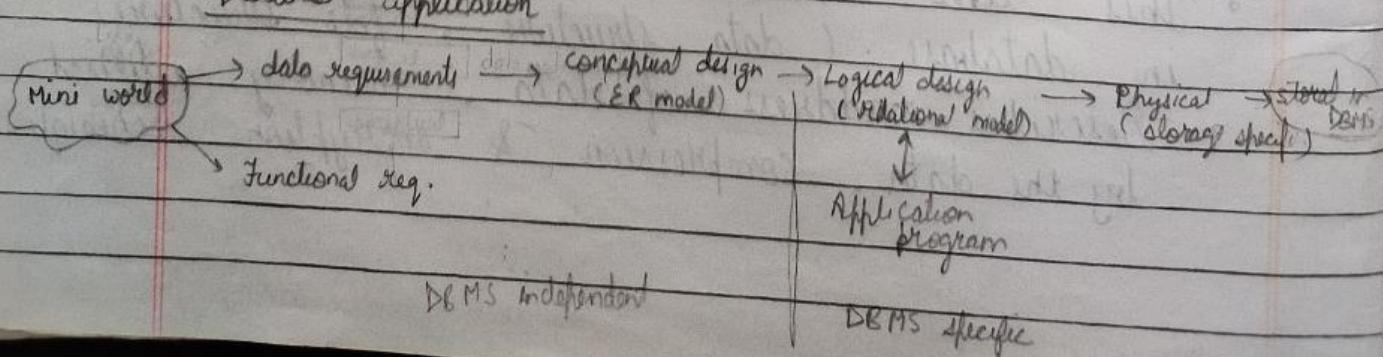
## Logical / Conceptual level

- This is intermediate level of abstraction which facilitates communication between the client & the database
- This level describes WHAT data is stored in the database & relationships among the data
- It contains logical structures of database administered by DBA
- Applies constraints on the data
- Checks data consistency, integrity & security
- It takes the queries from external level, processes them, fetches the required data from database & sends to external level.

## External level

- This is the highest level of abstraction.
- This level accepts user's request & sends it to conceptual level.
- It provides an abstract view of data to the user & gives only relevant information.
- Multiple user views may exist.
- This level is closest to the user concerned with the way data is viewed by individual users.

## Database application



## DATA MODELS

Data model is an abstract model that defines the logical structures of a database.  
It is independent of hardware or software constraints

## ▷ Hierarchical Data Model

oldest model (1950) (North American Rockwell/IBM)  
(one → many) cardinality



- (one → many) cardinality

  - H. Data Model represents data hierarchically (top down / bottom up) in the form of parent - child relationship (tree like structure)
  - A parent may have many children but children have only one parent. (one to many) & (one to one)
  - Data of entities (parent / child) is stored in records & connected through links (pointers)

**COLLEGE**

1	A	18	2	B	17	3	C	20	
S-ID	S-Name	S-Age							
CO1	Java	CO2	Ruby	CO3	Python	CO4	DBMS	CO1	Java
C-ID	C-Name								

## Disadvantages

- Data redundancy (in case of M to 1)  
  - Complex algs for retrieval
  - lack of structured independence . Rigid structures.  
poor flexibility.
  - if parent data is deleted , all child elements gets deleted .
  - difficult to design complex relationships
  - difficult to implement M : N
    - LML , DDL X
    - programming complexity

## Advantages

- Fast & easy retrieval
  - Referential integrity
    - changes in parent record  
& updated in child
  - efficient for 1:N
  - security enforced
    - level of retrieval  
can be defined

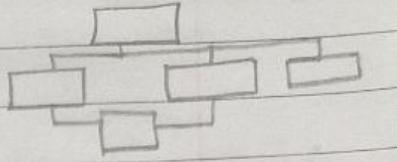
record-based

## Network Model (1969)

charles Bachman

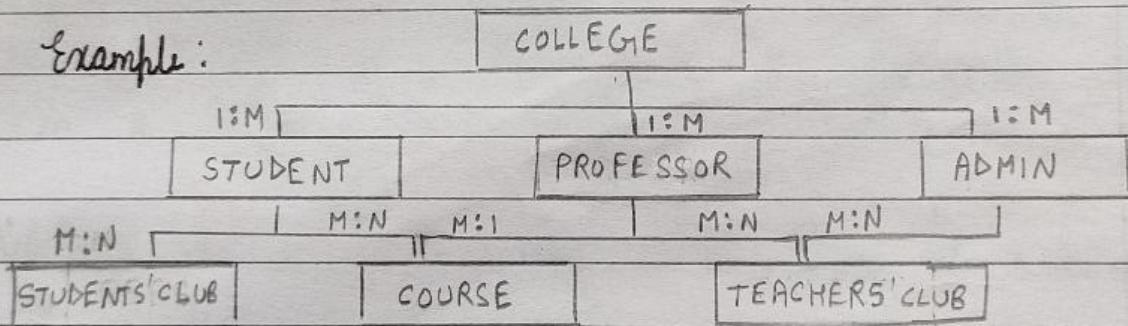
(graph structure)

set form



- This is an extension in hierarchical model.
- It represents data in owner-member relationship where each owner may have multiple members and each member may have multiple owners.
- It can describe one to one, M as well as 1, many to many rel.
- There can be more than one path from a previous node to successor nodes.
- connected through pointers.

Example:



### Advantages

- Ability to manage more relationship types (M:N, 1:1, 1:M, M:1)
- Easy access to data (multiple paths)
- Data integrity (owner-member rel.)
- Flexibility

### Disadvantages

- System complexity
- Lack of structural indep.
- Complex algs for retrieval

record-based

## Relational Model

Relational data model represent data by the collection of inter-related tables. Each table consists of rows and columns.

- Table / relation : It consists of rows & columns.
- Attribute / field / column : It defines the properties of the entity.
- Row / tuple / record : Data is stored in records.
- Domain : Set of values for a particular attribute in a relation.
- Relational schema : It contains the name of relation & all the attributes present in it.
- Relational key : It is an attribute / group of attributes which uniquely identifies a record in a relation.

### Properties :

- order of columns/mas is immaterial
- A relation must not contain identical rows.
- Each attribute must have a distinct name.
- A relation must have a unique name.
- Each record must have attributes must have a single value corresponding to a record.
- A relation should contain key attributes.

Example :

Student			Issue			Book			Attributes	
PK	FK ↓	↓ FK	PK	S-Id	B-Id	PK	B-Id	Subject		
Record (instance) →	S-Id	S-Name	S-Age	PK	S-Id	B-Id	PK	B-Id	Math	
	S1	A	20		S1	B4		B1	DBMS	
	S2	B	18		S2	B3		B2	DSA	
	S3	C	17		S3	B1		B3	Java	
	S4	D	19		S4	B2		B4		

### Constraints

- Domain constr. : Integer , character , Boolean , String etc.
- Key constr. :
  - Not null (\*) Candidate key
  - Unique Composite key
  - Primary key Alternate key
- Ref. integrity constr. : foreign key

Advantages :	Disadv.
most popular	
Simple & easy to use	Hardware overhead
hides physical storage details	Information Island phenomenon
scalable	(a lot of info-redundancy, inconsistency)
redundancy reduced	failed to manage complex info. systems
structural independence (no navigation)	(multiple databases)
easy retrieval (using SQL)	

Some RDBMS : MySql , Oracle , MS Access , Sql server  
 Language used : SQL

2015

Object-based

## Object-Oriented Model (set of objects)

- It represents data in the form of objects which contains some properties & behaviours.
- It supports OOPS concepts of classes & objects, inh, poly, encap.
- It allows storage of complex data such as image, audio & video etc.
- Data is not fragmented rather stored as a unit in objects. Each object is an independently functioning unit.
- As data is not fragmented, retrieval is easy.

instances  
of class

Objects are composed of:

- **Messages** : Messages act as a communication medium b/w an object & outside world.

- Read-only message : if invoked, doesn't change value of variables.
- Update message : if invoked, changes the value of variables.

- **Methods** : set of instructions which perform a particular task

behaviour  
of object

executes when message is passed.

- Read only method
- update method

- **Variables** : data of an object which distinguishes it from other objects is stored in variables.

defines state of  
object

Class blueprint of an object.

consists of declarations of methods & variables.  
inheritance, multiple inheritance, encapsulation etc.

# Class Definition

```
class employee {
```

// variables

```
    string name;
```

```
    string address;
```

```
    int salary;
```

## EMPLOYEE

```
string name
```

```
string address
```

```
int salary
```

```
annual-salary()
```

```
get-name()
```

```
get-address()
```

```
set-address(string newaddress)
```

## // Messages & methods

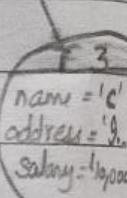
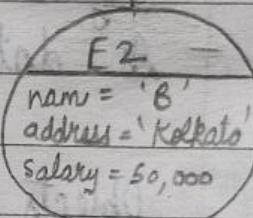
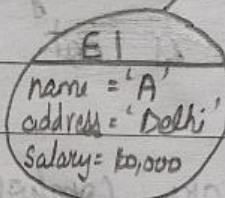
```
int annual-salary()
```

```
string get-name();
```

```
string get-address();
```

```
int set-address(string newaddress);
```

```
}
```

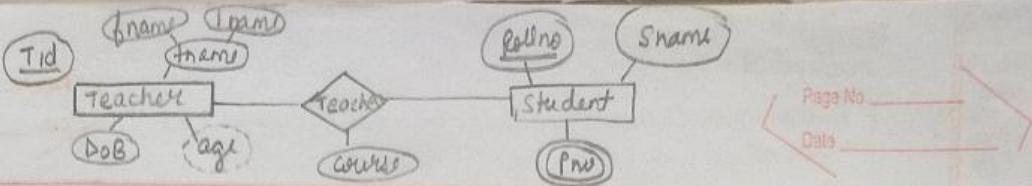


## Advantages :

- allows storage of multimedia
- query language is not required for retrieval
- no primary key
- complex relationships can be easily implemented.

## Disadv.

- language dependent
- lack of structural independence
- lack of experienced programmers (new concept)



## E-R MODEL (by Dr Peter Chen in 1976)

diagrammatic (Entity - Relationship Model)

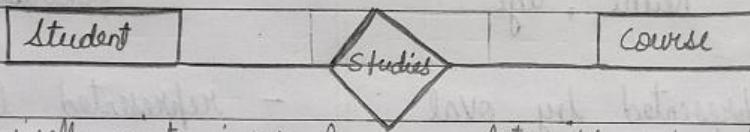
represents - non technical design

of database easy to understand even by non-technys  
E-R model is a conceptual data model diagram which represents real-world entities, and the relationships between them along with their attributes

- standard & logical way of visualising data

\* Entity : Entity is a real-world object having some properties (attributes) which distinguishes it from other objects.  
eg: students, teachers, courses etc.

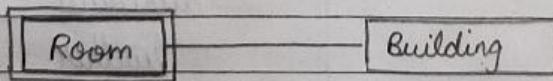
- It is represented by a rectangle



tangible : physically exists : car, pen      intangible : logically exists : Account

Weak entity : an entity which depends on another entity

- It doesn't contain any key attribute of its own
- represented by double rectangle



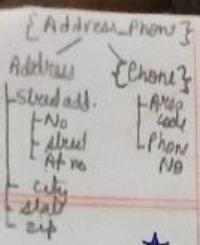
Symbol representations :

entity : rectangle      student

attribute : ellipse      name

relation : diamond      study

Entity type is like class which describes the properties of an entity



composite  $\rightarrow ()$   
multi-valued  $\rightarrow \{ \}$

eg: { Address-phone({ phone(Area-Code, Phone-No) }), Address(Street-Address(No, Street, apartment-no), city, state, zip)) }

Page No.

each attribute has its domain / value set (specified by datatype)  
(not specified in ER model)



## Attributes

SSN

Social Security No

In US, it is assigned to each individual

It is used to define property of an entity  
eg: attributes of entity 'Student': Name, Registration no. etc

- For each attribute there is a set of permitted values called domains

### Types of Attributes

multivalued  
attr can have  
constraints to  
restrict the no  
of values

#### Single

- It can have only one value for an instance
- eg: Registration No., Name, age
- represented by oval

age

Significance of comp attr

Composite attrs are composed of simple ones. These simple components are used in DBMS. They are useful in situations where to compose attrs at other levels as composite

#### Simple

- can't be further divided

eg: age

oval connected to entity (rect.)

In google maps

list

stored

current loc &  
final loc

#### Stored

- Attribute which is directly taken as input and stored
- eg: date of birth
- represented by oval (DOB)

#### Multivalued

a new table in RDBMS

- It can have multiple values for an instance
- eg: Name, age, Mobile no., address (permanent, corresponding)
- represented by double oval

address

relations

#### Composite

- Composed of many other attributes. Hence, can be further divided
- eg: name (first name, last name)

address (city, state, country)

oval connected to oval

#### Derived

for attributes which change cont.

- Attribute which ~~is~~ can be derived from other attributes
- eg: age (can be derived from DOB)
- represented by dotted oval (age)

Relationship set: a set of similar kind of relations

ER model represents entity set & relationship set.  
 ↳ not individual entities / relationships  
 ↳ in RDBMS

Page No. \_\_\_\_\_

Date \_\_\_\_\_

### Key

- Attribute which can't be repeated.
- Represents the main property of the entity
- eg: Registration no., ID etc
- Represented by oval with text underlined

ER model  
doesn't  
contain  
PK  
widely  
used  
during  
mapping

RollNo

Name

### Non - Key

- Attribute which may or may not be repeated.
- Name, age etc.
- represented by oval

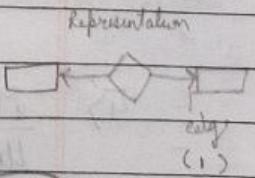
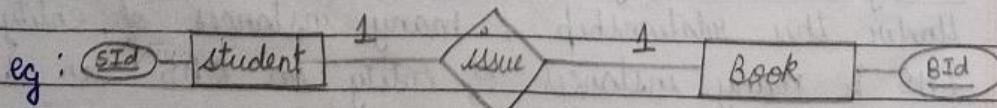
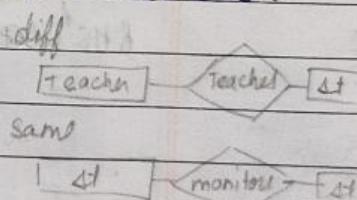
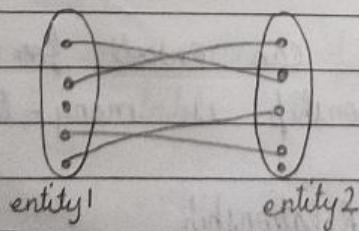
### \* Relationship May have descriptive attributes

- It describes the relation or link<sup>↑</sup> between entities of <sup>association</sup> same/diff. entity set
- It is represented by a diamond.
- Weak relationship is represented by double diamond.

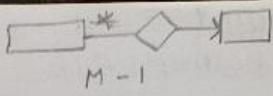
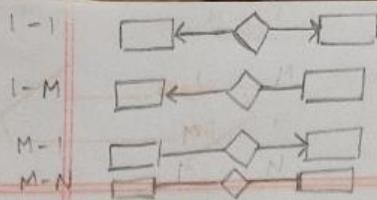
### Types of relationships

#### i) One-to-one Relationship :

- Under this relationship, only one instance of an entity can be linked with the relationship on both sides.



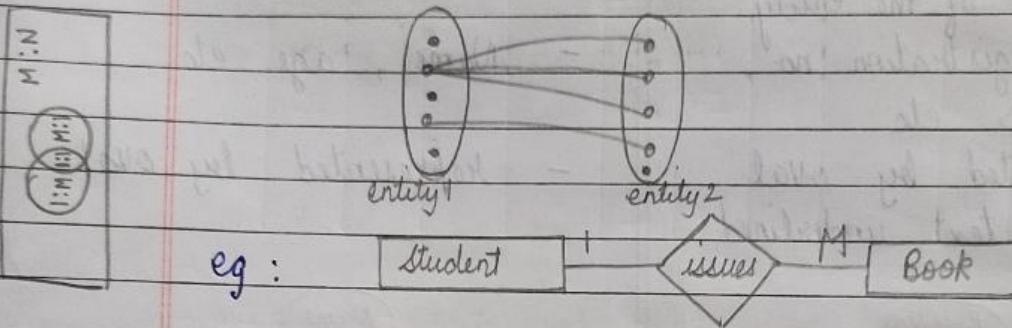
If a student can issue only 1 book, then this will be a one-to-one relationship.



edge - One  
 star/null - many  
 Page No. \_\_\_\_\_  
 Date \_\_\_\_\_

### 2) One - to - many Relationship

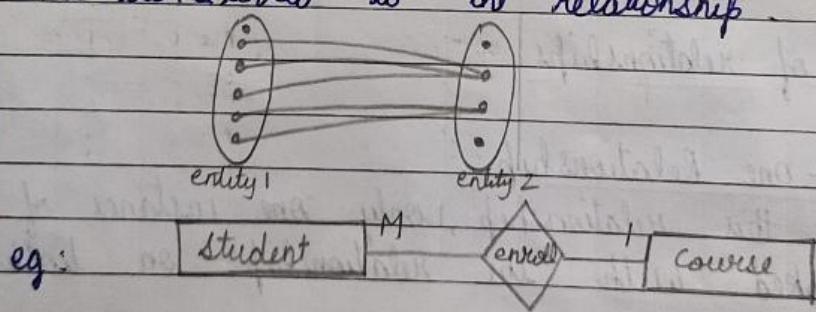
Under this relationship, only one instance of an entity on LHS & many instances of entity on RHS can be linked to the relationship.



If a student can issue multiple books at a time, then this relationship is one to many.

### 3) Many - to - one Relationship

Under this relationship, many instances of entity on LHS & only one instance of entity on RHS can be linked to the relationship.



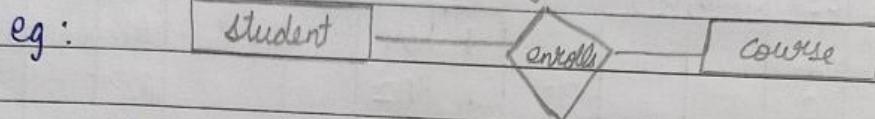
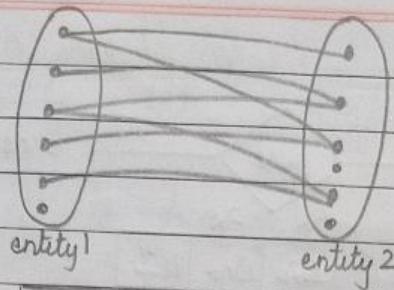
If a student can enroll for only 1 course, then this relationship is many - to - one.

### 4) Many - to - many Relationship

Under this relationship, many instances of entity on LHS & many instances of entity on RHS can be linked to the relationship.

Table - Entity set / schema  
or row - entity / instance

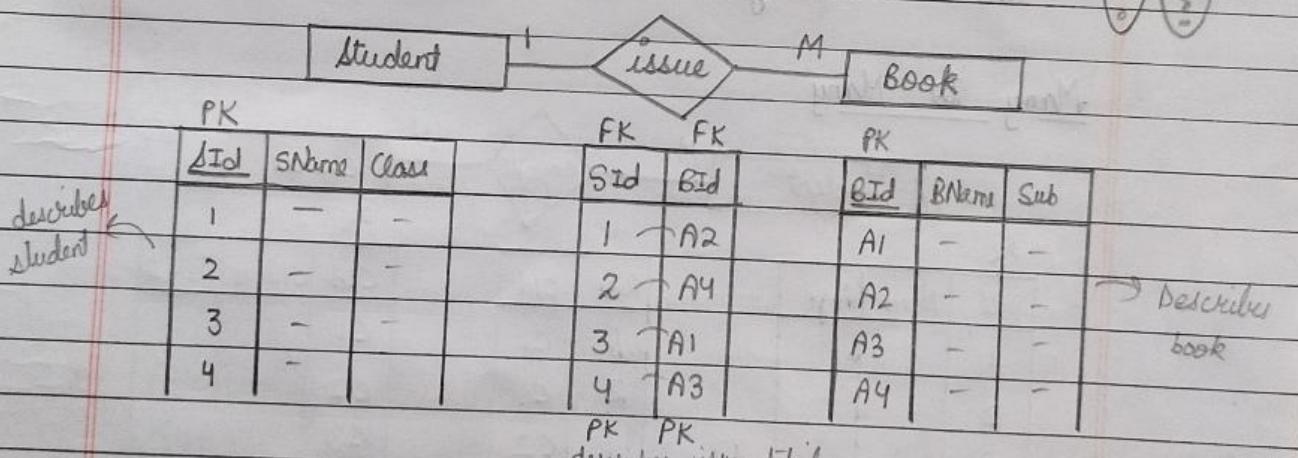
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If a student can enroll for multiple courses at a time, then this relationship is many-to-many

### Implementation of ER Models

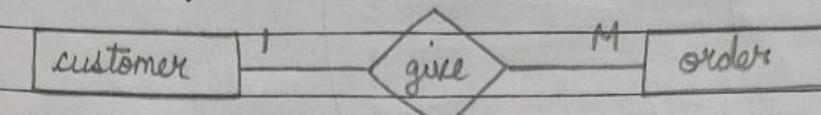
→ One-to-one



- In relationship table, SID as well as BID can be made Primary key
- We can merge any of the entity tables with relationship table to reduce them to 2 tables

SId	SName	Class	BId	BId	BName	Sub
1	-	-	A2	A1	-	-
2	-	-	A4	A2	-	-
3	-	-	A1	A3	-	-
4	-	-	A3	A4	-	-

## One - to - many

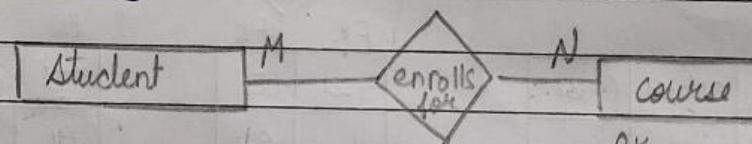


customer			give			order		
PK	FK	FK	PK	FK	FK	PK	FK	FK
CId	CName	City		CId	One	Dals		Ons
1	-	-		1	A1			A1
2	-	-		1	A2			A2
3	-	-		1	A3			A3
4	-	-		2	A4			A4

descriptive attributes

- entity Attributes of entity on 'many' side will serve as PK for relationship table
- Can be merged with table on 'many' side

## Many to Many



Student			enrolls			Course		
PK	PK	PK	PK	PK	PK	PK	PK	PK
Roll	Name	Age		Roll	Cid		CId	CName
1	-	-		1	C1		C1	-
2	-	-		2	C1		C2	-
3	-	-		1	C2		C3	-
4	-	-		3	C4		C4	-

composit key

- no merging

Null : no value

↓  
Not applicable      ↓  
unknown

↓  
Missing  
eg height

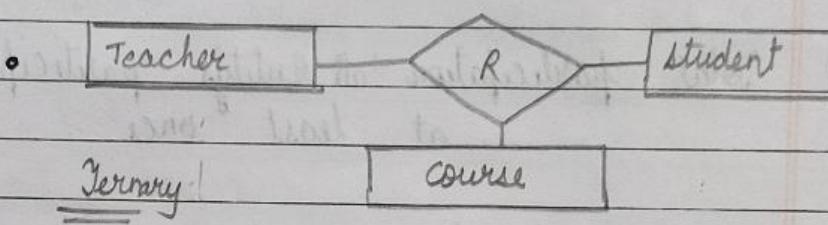
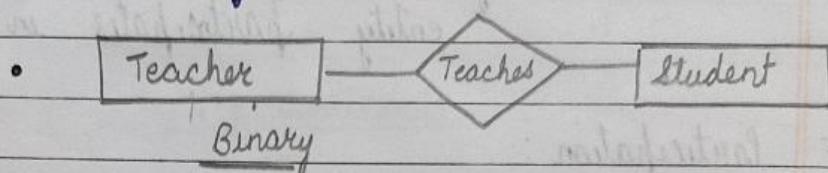
↓  
not known whether  
value exists

## Degree of a relationship

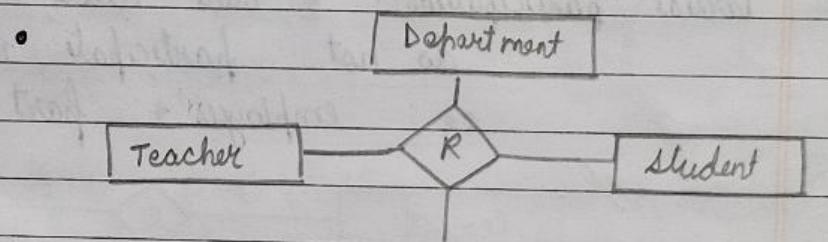
no. of entity set associated with the relationship set.

- usually it is binary 80 - 85 %.

Example:



unary



N-ary

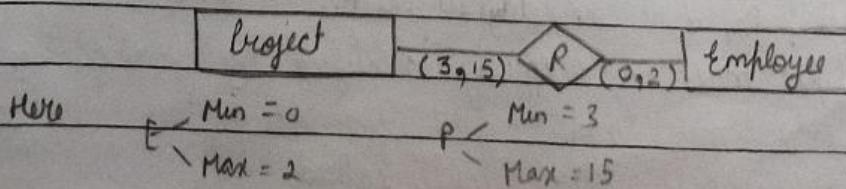
Quaternary

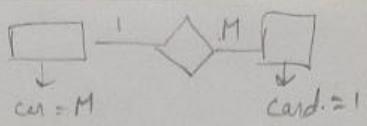
## \* Cardinality & Cardinality ratio

Express the no. of entities to which other entity can be related via a relationship.

\* Participation constraints: specifies whether the existence of an entity depends on its being related to another entity via a relationship type.

- These constraints specify the max. & min. no. of relationship instances that each entity can/must participate in





Page No. \_\_\_\_\_

Date \_\_\_\_\_

(MinC, MaxC)

Max cardinality: It defines the max. no. of times an entity ~~or~~ participates in a relationship.

Min cardinality: It defines the min. no. of times an entity participates in a relationship.

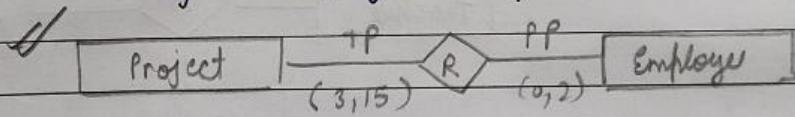
### \* Participation :

min C  $\geq 1$

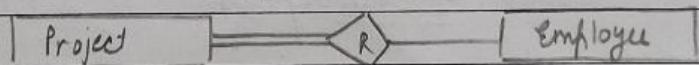
Total participation: all entities participate in relationship at least once eg part. of project

min C = 0

Partial participation:  $\diamond$  there exists some entities which do not participate in relationship  
eg: employees \* part.



or



- In a rel. set, PKs of all the entity set are not and serve as SK for rel. set
- Relationships must be uniquely identified by participating entities attr.
- Relationships must not repeat for descriptive attributes  
Rather make desc. attr. multi valued

## INTEGRITY CONSTRAINTS

Integrity constraints are the set of rules applied on attributes of an entity.

### Integrity Constraints

Domain constraints	Entity Integrity constraint	Referential Integrity constraints	Key constraints
--------------------	-----------------------------	-----------------------------------	-----------------

#### 1) Domain Constraints

set of rules that restricts the kind of data stored in the attributes (domains).

Example : Integer , float , string , character , time , date , timestamp , currency

	int	string	int
Roll	Name	Age	
1	A	21	
2	B	28	
not allowed	← (B)	C	(A) → not allowed

## 2) Entity Integrity Constraints

It ensures the uniqueness of each record in a table.

Not Null: null values are not allowed in it.

Unique Key: It doesn't allow duplicacy  
only 1 NULL value is allowed.

Primary key: uniquely identifies each record.

have distinct values + null values are not allowed.

PK	unique		
Id	Name	Age	
1	NULL	20	
2	B	21	
not allowed ← NULL	(B)	17	not allowed

## 3) Referential Integrity Constraints

ensures that the relationship between two tables is valid.

Foreign key.

entity  $\rightarrow$  table  
 entity instance  $\rightarrow$  row  
 column  $\rightarrow$  Attribute / field  
 Row  $\rightarrow$  tuple / record

keys must not change frequently

Page No.

Date

## 4) Constraints / Keys (basically, the rules applied on attributes)

every table should have a key

Key : Keys are used the <sup>set of</sup> attributes which uniquely identifies two each by tuple.  $(\text{key})^+ = R$

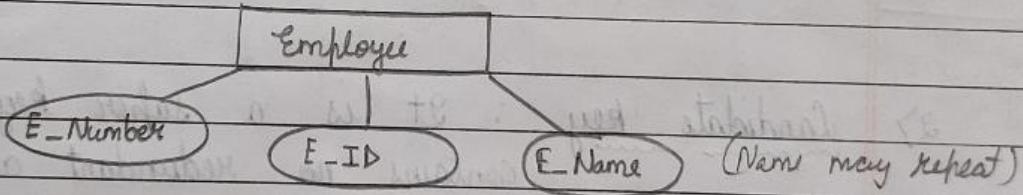
- Keys are also used to establish relationship among the tables in a schema.

### Types of keys

1) Super key : It is a single attribute or a set of attributes which uniquely identifies each tuple in a table.

(all the candidate keys and their combos)

eg :



Possible Super Keys are :

- E-ID
- E-Number
- E-ID, E-Name
- E-Number, E-Name
- E-ID, E-Number
- E-ID, E-Number, E-Name

$\rightarrow R(A_1, A_2, A_3, \dots, A_n)$

- Here  $A_1$  is candidate key

No. of Super Keys = ?

$$A_1 - \frac{(n-1)}{2} - A_n = 2^n$$

Imp  $\rightarrow$  Find SK from CKs

CKs from SKs

If a set of attr. is  
not a SK, none of  
its subsets is.

Max no. of super keys =  $2^n - 1$  (excluding  $\emptyset$ , all the subsets)  
Suppose 5 attr.:  $S_{C_1} + S_{C_2} + S_{C_3} + S_{C_4} + S_{C_5} = 31$

Page No.  
Date:

R(A B C D)

1	1	5	1
2	1	7	1
3	1	7	1
4	2	7	1
5	2	5	1
6	2	5	2

SK = A, AB, AC, ABC

AD, ABC, ABD

ACD, ABCD

CK = A

PK = A

- A<sub>1</sub>, A<sub>2</sub> are candidate keys

No. of super keys = ?

$$A_1 - \underset{n-1}{\dots} - A_n \quad 2^{n-1}$$

$$A_2 - \underset{n-1}{\dots} - A_n \quad 2^{n-1}$$

$$A_1 A_2 - \underset{n-2}{\dots} - A_n \quad 2^{n-2}$$

$$2^{n-1} + 2^{n-1} - 2^{n-2} = 3 \cdot 2^{n-2}$$

R(A B C)

1	1	1
2	1	2
3	2	1
4	2	2

SK = A, AB, AC,

ABC, BC

CK = A, BC

PK = any one of CK

- A<sub>1</sub>, A<sub>2</sub>, A<sub>3</sub>, A<sub>4</sub> are candidate keys

No. of super keys = ?

$$A_1 A_2 - \underset{n-2}{\dots} - A_n \quad 2^{n-2}$$

$$A_3 A_4 - \underset{n-2}{\dots} - A_n \quad 2^{n-2}$$

$$A_1 A_2 A_3 A_4 - \underset{n-4}{\dots} - A_n \quad 2^{n-4}$$

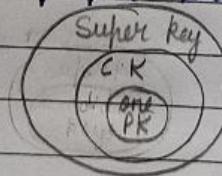
$$2^{n-2} + 2^{n-2} - 2^{n-4}$$

no. of  
super keys  
a proper  
subset is a  
subset of a  
super key

can have  
null values

2) Candidate key : It is a super key that contains no redundant attributes.

- also called minimal super key
- They are a proper subset of super keys



3)

Primary key : It is a column or set of columns (attribute) in a table that uniquely identifies each tuple.

- It is subset of candidate keys
- It must not contain null values

PK = unique + not null

A table can have only 1 PK.

- It is used to represent diff entity instances that is why it shouldn't contain null values.

- Not null (indicated by \*)
  - unique (only 1 null allowed)

4) Composite key: It consists of more than one attribute to uniquely identify rows of a table.

e.g.: [Customer-ID, Order-ID] forms a composite key.

57 Foreign key : It is an attribute or set of attributes which points to (refers to) the primary key of same or another table.

- The table which contains the FK - referencing table
  - \_\_\_\_\_ PK - referenced table
  - Multiple FK can be present in a table.
  - A PK in a particular referenced table can be referenced by multiple FK in referencing tables.

PK	SID	SName	SAge		CID	SID	FK
	1	A	-		C1	1	
	2	B	-		C2	1	
	3	C	-		C3	2	
	4	D	-	-	C4	3	

referenced / base table      referencing table

\* Foreign key maintains referential integrity (thus) checks for any ambiguity

Referenced (base) tables

- Insert
  - Delete
  - update PK

## Referencing table

- must be deleted from here if not updated

- ~~on delete cascade~~ <sup>preferred</sup>
  - on delete set Null (if FK happens to be PK → error)
  - on delete no action generates error (by default)

## Referencing table

- delete
- update
- insert

## referenced table

check first  
check first

Ques: Let  $R_1(a, b, c)$  and  $R_2(x, y, z)$  be two relations in which  $a$  is FK in  $R_1$  that refers to PK of  $R_2$ .

Consider 4 options:

- (a) insert into  $R_1$
- (b) insert into  $R_2$
- (c) Delete from  $R_1$
- (d) Delete from  $R_2$

which will cause violation.

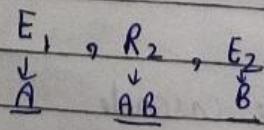
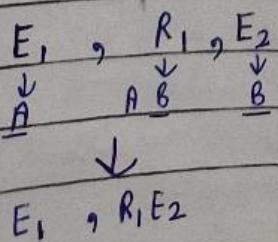
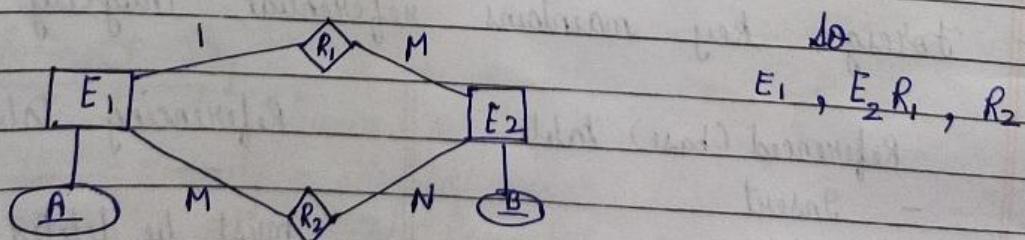
FK			PK		
a	b	c	x	y	z

$R_1$        $R_2$

Question:

→ What is the min. no. of tables req. to represent this ER model into relational model?

- a) 2
- b) 3
- c) 4
- d) 5



$f: \alpha \rightarrow \beta$   
means if  $\alpha$  is given, we can search  $\beta$   
 $\alpha$  can determine  $\beta$

- follow rules of fcn

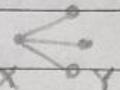
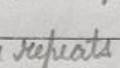
$\alpha^*$  can't repeat  
unique & not null  
PK  
if repeat then  $\beta$  also repeats

## FUNCTIONAL DEPENDENCIES

$X \rightarrow \beta$   
If  $X \subseteq R$ ,  $\beta \subseteq R$

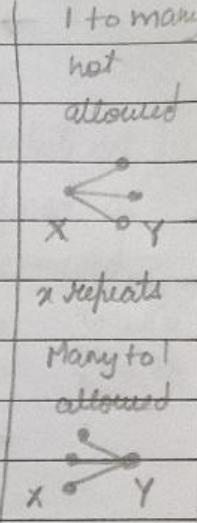
1 a  $X \rightarrow \beta$

2 a Then,  $t_1[\alpha] = t_2[\alpha]$   
valid  $\Rightarrow t_1[\beta] = t_2[\beta]$

	X	$\beta$	
$t_1$	a	b	
$t_2$	a	b	

whether both  
values of  $\beta$   
are same/no  
is determined  
by  $\alpha$

$X \rightarrow \beta$   
determinant dependent -  $X$  determines  $\beta$  or  
 $\beta$  is determined by  $X$



FD is a relationship between two attributes, typically between PK & other non key attributes within a table.

If  $X \rightarrow Y$  then  $X$  uniquely determines  $Y$ .

### Types :

$$X \rightarrow Y$$

we need to  
mention that

#### Trivial

- $Y$  is subset of  $X$  i.e.  $Y \subseteq X$   
eg:  $XY \rightarrow X$ ,  $X \rightarrow X$
- Trivial functional dependencies are always valid / true.
- $LHS \cap RHS \neq \emptyset$

$$\begin{array}{l} Sid \rightarrow Sid, \quad Sid \text{ Sname} \rightarrow Sid \\ (Sid \cap Sid = Sid) \quad (Sid \text{ Sname} \cap Sid = Sid) \end{array}$$

#### Non trivial

- $Y$  is not a subset of  $X$   
eg:  $XY \rightarrow XYZ$  non-trivial,  $X \rightarrow Y$  non-trivial
- May or may not be valid.
- $LHS \cap RHS \neq \emptyset$   $LHS \cap RHS = \emptyset$  non-trivial

$$Sid \rightarrow Sname$$

Page No. \_\_\_\_\_  
Date \_\_\_\_\_

data depends on FD & not vice versa  
for every X there must be only 1 Y

→ a)  $A \rightarrow BC$

b)  $DE \rightarrow C$

c)  $C \rightarrow DE$

d)  $BC \rightarrow A$

(check only repeated values of  $\alpha$ )

	A	B	C	D	E
a	2		3	4	5
2	a		3	4	5
a	2		3	6	5
a	2		3	6	6

- (If all  $\alpha$  are unique. It will be a FB certainly)

- (If all values of  $\beta$  are same, it will be a FB)

→  $X Y Z$

	X	Y	Z	a) $X \rightarrow Y \& \& Z \rightarrow Y$
1	4	2		b) $YZ \rightarrow X \& \& Y \rightarrow Z$
1	5	3		c) $YZ \rightarrow X \& \& X \rightarrow Z$
1	6	3		d) $XZ \rightarrow Y \& \& Y \rightarrow Z$
3	2	2		

→  $A B C$

	A	B	C	a) $A \rightarrow B \& \& BC \rightarrow A$
1	2	4		b) $C \rightarrow B \& \& CA \rightarrow B$
3	5	4		c) $B \rightarrow C \& \& AB \rightarrow C$
3	7	2		d) $A \rightarrow C \& \& BC \rightarrow A$
1	4	2		

## CLOSURE METHOD

(Attribute closure / closure on attribute set / closure of attribut set)

Attribute closure of an attribute set A can be defined as a set of attributes which can be functionally determined by it.

- denoted by  $F^+$

$$\rightarrow R(ABC)$$

$$A \rightarrow B, \quad B \rightarrow C$$

$$A^+ = ABC$$

$$\beta^+ = \beta C$$

$$\rightarrow R(AB\mid CDEF)$$

$$A \rightarrow B, C \rightarrow D E, A C \rightarrow F, D \rightarrow A F, F \rightarrow c f$$

$$D^+ = DAFB$$

$$\Delta E^+ = \Delta AFBCE$$

## Armstrong Axioms

- Axiom is a statement that is taken to be true & serve as a premise or starting point for further arguments
  - Armstrong axioms holds on every relational database & can be used to generate closure sets.

Primary rules: (RAT rules)

- **Reflexivity** : If  $Y \subseteq X$   
Then  $X \rightarrow Y$       eg :  $ABC \rightarrow AB$
  - **Augmented Augmentation** : If  $X \rightarrow Y$        $XZ \rightarrow Y \checkmark \quad XZ \rightarrow Z \checkmark$   
Then,  $XZ \rightarrow YZ$       so  $XZ \rightarrow YZ$
  - **Transitivity** : If  $X \rightarrow Y$  &  $Y \rightarrow Z$   
Then  $X \rightarrow Z$

## Secondary rules :

- Union : If  $x \rightarrow Y \wedge x \rightarrow z$  Then  $x \rightarrow Yz$ 

$$\begin{array}{c} AB \rightarrow CD \\ \downarrow \\ AB \rightarrow C \\ AB \rightarrow D \end{array}$$
- Decomposition : If  $x \rightarrow Yz$  Then  $x \rightarrow Y \wedge x \rightarrow z$ 

$$\begin{array}{c} AB \rightarrow CD \\ \downarrow \\ AB \rightarrow C \\ AB \rightarrow D \end{array}$$

but not  $\times A \rightarrow CB \wedge B \rightarrow CB \times$
- Pseudo trans : If  $x \rightarrow Y \wedge wY \rightarrow z$  Then  $wx \rightarrow z$ 

$$\begin{array}{c} AB \rightarrow CD \\ \downarrow \\ AB \rightarrow C \\ AB \rightarrow D \end{array}$$

but not required

$$\begin{array}{l} x \rightarrow Y \Rightarrow xw \rightarrow wY \Rightarrow wx \rightarrow z \\ x \rightarrow Y, Yw \rightarrow z \rightarrow xw \rightarrow z \end{array}$$
- Composition : If  $x \rightarrow Y \wedge z \rightarrow w$   $xz \rightarrow Yw$

$$\rightarrow R(ABCDEF_1)$$

$$A \rightarrow B, BC \rightarrow DE, AEG_1 \rightarrow G_1$$

$$(AC)^+ = ACBDE$$

$$\rightarrow R(ABCD_1)$$

$$A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A$$

$$B^+ = BD$$

$$\rightarrow R(ABCDEF)$$

$$AB \rightarrow C, BC \rightarrow AD, D \rightarrow E, CF \rightarrow B$$

$$(AB)^+ = ABCDE$$

$$\rightarrow R(ABCDEF_1H)$$

$$A \rightarrow BC, CD \rightarrow E, F \rightarrow C, D \rightarrow A, EH, ABH \rightarrow BD, DH \rightarrow BC$$

$$BCD \rightarrow H ?!$$

$$(BCD)^+ = BCDEF \bullet AH$$

F & G  
are not  
on RHS  
so can't be  
obtained

## Comparison of sets of FD

### \* Equivalence of functional Dependencies

$\rightarrow R(ACD \Delta EH)$

$$F: A \rightarrow C$$

$$AC \rightarrow D$$

$$E \rightarrow AD$$

$$E \rightarrow H$$

$$G_1: A \rightarrow CD$$

$$E \rightarrow AH$$

$$a) F \subseteq G_1$$

$$b) F \supseteq G_1$$

$$c) F = G_1$$

$$d) F \neq G_1$$

$$A^+ = ACD$$

$$(AC)^+ = ACD$$

$$E^+ = EAHC$$

$$\text{do } F \subseteq G_1$$

$$\text{do } F = G_1$$

$$A^+ = ACD$$

$$E^+ = EADHC$$

$$\text{do } G_1 \subseteq F$$

$$\text{do } F = G_1$$

$\rightarrow R(PQRS)$

~~Better~~  $X: P \rightarrow Q$   
 $Q \rightarrow R$   
 $R \rightarrow S$

$$P^+ = PQRS$$

$$R^+ = RS$$

$$Y \subseteq X$$

$$Y: P \rightarrow QR$$

$$R \rightarrow S$$

$$a) X \subseteq Y$$

$$b) Y \subseteq X$$

$$c) X = Y$$

$$d) X \neq Y$$

$$P^+ = PQRS$$

$$Q^+ = Q$$

$$R^+ = RS$$

$$X \subseteq Y$$

$\rightarrow R(ABC)$

$$F: A \rightarrow B$$

$$B \rightarrow C$$

$$C \rightarrow A$$

$$A^+ = ABC$$

$$B^+ = BCA$$

$$C^+ = ABC$$

$$G_1 \subseteq F$$

$$G_1: A \rightarrow BC$$

$$B \rightarrow A$$

$$C \rightarrow A$$

$$A^+ = ABC$$

$$B^+ = BAC$$

$$C^+ = CAB$$

$$F \subseteq G_1$$

$$G_1 = F$$

~~Better~~  $R(VWXY\bar{Z})$

$$F: W \rightarrow X$$

$$WX \rightarrow Y$$

$$Z \rightarrow WY$$

$$Z \rightarrow V$$

$$W^+ = WX\bar{Y}$$

$$Z^+ = ZWYVX$$

$$G_1 \subseteq F$$

$$G_1: W \rightarrow XY$$

$$Z \rightarrow WX$$

$$W^+ = WX\bar{Y}$$

$$(WX)^+ = WX\bar{Y}$$

$$Z^+ = ZWXY$$

$$F \not\subseteq G_1$$

✓ First remove Trivials  
 Then LHS red  
 RHS red  
 whole

Page No.

Date

## \* Minimal set / Canonical Cover / Irreducible set of FD

There can be redundancy on  $\alpha$  side /  $\beta$  side / both sides

First remove trivial

extra attr; extra FD

Remove & Red [ 1) Decompose all FD (to eliminate  $\beta$  side red.)

2) Find closure for each twice

1 - By including that FD

2 - By excluding that FD

3) If closures in each case comes out to be the same  
 $\rightarrow$  FD is redundant, eliminate it.

else

$\rightarrow$  FD is essential

Remove & Red [ 4) Now, compute closure of LHS of FD having more than 1 attribute & find closure

Example :  $R(WXYZ)$  by ignoring 1st & Remove acc.

$$X \rightarrow W$$

$$WZ \rightarrow XY$$

$$Y \rightarrow WXZ$$

① Decompose :

$$X \rightarrow W \checkmark$$

$$WZ \rightarrow X \checkmark$$

$$WZ \rightarrow Y \checkmark$$

$$Y \rightarrow W \times$$

$$Y \rightarrow X \checkmark$$

$$Y \rightarrow Z \checkmark$$

②

$$X^+ = XW \quad X^+ = X$$

$$(WZ)^+ = WZX \quad (WZ)^+ = WZY$$

$$(WZ)^+ = WZ$$

$$Y^+ = YWXZ$$

$$Y^+ = YXZW$$

$$Y^+ = YZ$$

$$Y^+ = YXW$$

③ So  $X \rightarrow W$

- There may be multiple

canonical forms for the same set of FD

$$WZ \rightarrow Y$$

- Depends on order

$$Y \rightarrow X \text{ (incorrect)}$$

If red. occurs due to 2 FD

we remove the first one & keep 2nd one

so if order is reversed 2nd one is kept

$$(WZ)^+ = WXYZ$$

$$W^+ = W$$

$$Z^+ = Z$$

Canonical form :  $X \rightarrow W$

$$WZ \rightarrow Y$$

$$Y \rightarrow XZ$$

$$\rightarrow R(ABC) \quad AB \rightarrow C, C \rightarrow AB, B \rightarrow C, ABC \rightarrow AC, A \rightarrow C, AC \rightarrow B$$

$$AB \rightarrow C, C \rightarrow A, C \rightarrow B, B \rightarrow C, ABC \not\rightarrow A, ABC \not\rightarrow C, A \rightarrow C, AC \rightarrow B$$

$$\begin{array}{ll} AB^+ = ABC & C^+ = CAB \\ AB^+ = ABC & C^+ = CB \\ C^+ = CAB & C^+ = CAB \\ B^+ = BC & B^+ = B \end{array}$$

Date: \_\_\_\_\_

$$A^+ = ACB \quad AC^+ = ABC$$

$$A^+ = A \quad AC^+ = AC$$

$$c \rightarrow A, B \rightarrow C, A \rightarrow C, AC \rightarrow B$$

$$AC^+ = ABC \quad A^+ = ACB \quad C^+ = CAB$$

$$\therefore A \rightarrow B \quad C \rightarrow A$$

$$B \rightarrow C \quad A \rightarrow C$$

$$A \rightarrow B \quad A \rightarrow B$$

$\rightarrow R(ABCD)$

$$A \rightarrow B \quad AC \rightarrow D$$

$$C \rightarrow B$$

$$D \rightarrow ABC$$

$$A \rightarrow B \checkmark$$

$$A^+ = AB$$

$$A^+ = A$$

$$C \rightarrow B \checkmark$$

$$C^+ = CB$$

$$C^+ = C$$

$$D \rightarrow A \checkmark$$

$$D^+ = DABC$$

$$D^+ = DBC$$

$$D \rightarrow B \times$$

"

$$D^+ = DCAB$$

$$D \rightarrow C \checkmark$$

"

$$D^+ = DAB$$

$$AC \rightarrow D \checkmark$$

$$(AD)^+ \neq ACBD$$

$$(AC)^+ = ACB$$

$$(AC)^+ = ABCD \checkmark$$

$$A^+ = AB \checkmark$$

$$C^+ = CB \checkmark$$

Canonical for cover :  $A \rightarrow B$   
 (minimal set)  
 $C \rightarrow B$   
 $D \rightarrow AC$   
 $AC \rightarrow D$

$\rightarrow R(VWXYZ)$

$$V \rightarrow W$$

$$VW \rightarrow X$$

$$Y \rightarrow VZX$$

$$V \rightarrow W \checkmark$$

$$V^+ = VWX$$

$$V^+ = V$$

$$VW \rightarrow X \checkmark$$

$$(VW)^+ = VWX$$

$$(VW)^+ = VW$$

$$Y \rightarrow V \checkmark$$

$$Y^+ = YVXZW$$

$$Y^+ = YXZ$$

$$Y \rightarrow X \times$$

"

$$Y^+ = YVZWX$$

$$Y \rightarrow Z \checkmark$$

"

$$Y^+ = YVXW$$

$$(VW)^+ = VWX$$

$$V^+ = VWX \checkmark$$

$$W^+ = W$$

$$V \rightarrow X$$

Minimal cover :  $V \rightarrow W \cancel{X}$   $Y \rightarrow VZ$

Superset of SK is always a SK  
subset of SK can be a SK

Superset of CK or subset of CK can never be a CK

Superset of CK is always a SK

Subset of CK can never be a SK

Page No.

Date

\* To find SK, CK

$\rightarrow R(\overline{A} \overline{B} \overline{C} \overline{D})$

AB

BDA

CD BA

$AB \rightarrow C, C \rightarrow BD, D \rightarrow A$

A, B, C, D

C

AB, AC, AD, BC, BD  $\times$  D

AB

, AC, BC, (BD), CD

ABC, ABD, ACD, BCD

ABC

, ABD, ACD, BCD

ABCD

ABCD

$\rightarrow$  attributes which are not tnf on RHS must be tnf in CK

$\rightarrow$  Once u get a CK, further combos must not contain it

Procedure : ① write all the attr which are not on RHS (if not prefer attribute)

② Start making combos by inc 1 at a time

(if u get  $\phi$  in step ① start with single attr)

③ check if its closure is entire set of attr for each combo

if yes  $\rightarrow$  it is a CK

no  $\rightarrow$  use it for further combos

④ In next level of combos first check whether it contains the obtained CK  
if yes  $\rightarrow$  have it  
no  $\rightarrow$  check -

$\rightarrow R(\overline{A} \overline{B} \overline{C} \overline{D})$

$A \rightarrow B, B \rightarrow C, C \rightarrow A$

D must be tnf

$D^+ = D \quad X$

$(AD)^+ = ADBC \quad \checkmark$

$(BD)^+ = BDCA \quad \checkmark$

$(CD)^+ = CDAB \quad \checkmark$

$\rightarrow R(\overline{A} \overline{B} \overline{C} \overline{D})$

$AB \rightarrow CD, D \rightarrow A$

B must be tnf

$B^+ = B \quad X$

$(AB)^+ = ABCD \quad \checkmark$

$(BC)^+ = BC \quad X$

$(BD)^+ = BDAC \quad \checkmark$

$\rightarrow R(ABCDEF)$

$AB \rightarrow C, C \rightarrow DE, E \rightarrow F, D \rightarrow A, C \rightarrow B$

$A^x$	$B^x$	$C^x$	$D^x$	$E^x$	$F^x$				
$(AB)$	$AD^x$	$AE^x$	$AF^x$	$(BD)$	$BE^x$	$BF^x$	$DE^x$	$DF^x$	$EF^x$
$ABE^x$	$ADF^x$	$ADB$	$AEF^x$	$ABE$	$ABF$	$BEF^x$	$BDE$	$BDF$	$DEF^x$
$ADEF^x$	$ADER$	$ADFB$	$AEFB$		$BDEF^x$				

Page No. \_\_\_\_\_  
Date \_\_\_\_\_  
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S Combed \_\_\_\_\_  
 $S_3$   
 $S_4$

$\rightarrow R(\overbrace{ABCDEF})$

$AB \rightarrow C, C \rightarrow D, B \rightarrow AE$

$B, F$  must be +nt

$$(BF)^+ = FB AEC D \quad \checkmark$$

All other  $\times$  combos are bad.

$\rightarrow R(ABCb)$

$AB \rightarrow cb, D \rightarrow b, C \rightarrow A$

$AB, AD, BC, CD$

$\rightarrow R(\overbrace{ABCD})$

$AB \rightarrow CD, C \rightarrow A, D \rightarrow B$

$$A^+ = A^x$$

$$B^+ = B^x$$

$$C^+ = CA^x$$

$$D^+ = DB^x$$

$$(AB)^+ = ABCD \quad \checkmark$$

$$(AC)^+ = AC^x$$

$$(AD)^+ \times$$

$$(BC)^+ = BCAD^x, BD^x$$

$$(CD)^+ = CDBA^x \quad \checkmark$$

$\rightarrow R(\overbrace{ABCDF})$

$AB \rightarrow CD, D \rightarrow A, BC \rightarrow DF$

$B$  must be +nt

single

$$B^+ = B^x$$

pair

$$(AB)^+ \checkmark \quad BC^x \quad BD^x \quad BE^x$$

$B$  must be there so  $AB^- \times \quad BC^- \times \quad BD^- \times \quad BE^-$  (cancel)

3

$$(BEA)^+ \times \quad (BEC)^+ \times$$

$$(BDE)^+ \times$$

$B$  must be makes combos of 4 leaving 1 nth 1 by 1 except  $B$

4

$$ABCD^x \quad ABCE^x \quad ABDE^x \quad BCDE^x$$

so  $AB, BC, BD$

$\rightarrow R(\overbrace{WXYZ})$

$Z \rightarrow w, Y \rightarrow XZ, Xw \rightarrow Y$

$$X^+ \times \quad Y^+ = YXzw \quad \checkmark \quad w^+ = x \quad z^+ = zw \quad \times$$

$$wx^x \quad wz^x \quad xz = xzwY^+ \quad \checkmark$$

$Y$  &  $XZ$

$\rightarrow R(\overbrace{ABCDEF})$

$AB \rightarrow C, DC \rightarrow AE, E \rightarrow F$

$B, D$

$$BD^+ = BD^x$$

$$ABD \quad \checkmark \quad BDC^x \quad \checkmark$$

$$BDE^x \quad BDF^x$$

$$BDEF^x \quad \times$$

Don't make other combos  
only for these

If essentials form CK no need to proceed further

Page No.

Date

$\rightarrow R(\underline{ABCDEF})$

$CE \rightarrow D, D \rightarrow B, C \rightarrow A$

$C, E$  must

$(CE)^+ = CEDBA \checkmark$

$\rightarrow R(ABCD\bar{E}FGH\bar{I}\bar{J})$

$AB \rightarrow C, AD \rightarrow GH, BD \rightarrow EF, A \rightarrow I, H \rightarrow J$

$A, B, D$  must

$(ABD)^+ = ABDCGH\bar{E}FI\bar{J} \checkmark$

$\rightarrow R(ABCDE)$

$A \rightarrow B, BC \rightarrow F, DE \rightarrow A$

$C, D$  must

$(CD)^+ = CD \times$

$(ACD)^+ = ACDBF \checkmark \quad (BCD)^+ = BCDEA \checkmark \quad (ECD)^+ = ECDA\bar{B} \checkmark$

$\rightarrow R(ABC\bar{D}E)$

$BC \rightarrow ADE$

$C$  must

$(BC)^+$

$CD$

$= CDBAE \checkmark$

$CE$

$D \rightarrow B$

$ABC$

$ACD$

$ACE$

$CDE$

$BCE$

$ABC\bar{E}$

$ACED$

$\rightarrow R(ABC\bar{D}EF)$

$AB \rightarrow C, C \rightarrow D, D \rightarrow BE, E \rightarrow F, F \rightarrow A$

$A^+ \quad B^+ \quad C^+ \quad CD\bar{BEFA} \checkmark \quad D^+ \quad DBE\bar{FAC} \checkmark \quad E^+ = EFA \times \quad F^+$

$AB^+$

$AE^+$

$AF^+$

$BE^+$

$BF^+$

$EF^+$

$\rightarrow R(ABCDEF\bar{G}\bar{H})$

$CH \rightarrow G, A \rightarrow BC, B \rightarrow CFH, E \rightarrow A, F \rightarrow EG$

$D^+ \quad (AD)^+ \quad ABCDFH\bar{EG} \checkmark \quad (BD)^+ \quad BCFH\bar{DEGA} \checkmark \quad (CD)^+ \times \quad DE^+ \checkmark$

$CDG$

$CDH$

$H\bar{D}G$

$CDG\bar{H} \times$

Alternat

Page No.  
Date

$R(ABCD)$

$AB \rightarrow CD, D \rightarrow B, C \rightarrow A$

$AB \leftarrow D$

↓ discard

Primi attr = A, B

CK

AB

sk  $\underline{AB^+ = ABCD}$

$A^+ = A^x$

$B^+ = B^x$

ABC CK

Check → if PA are on RHS

- A in  $C \rightarrow A$
- B in  $D \rightarrow B$

Replace in AB

BC

$B^+ x$

$C^+ = CA^x$

AD

$A^+ x$

$D^+ PB^x$

Primi attr = A, B, C, D

CK

AB

BC

AD

CD

BC CK

AD CK

Check →

- $AB \rightarrow C$        $AB \rightarrow D$

Replace in BC

CD      AB<sup>v</sup>

$C^+ x$

$D^+ x$

Replace in AD

CD , AB<sup>v</sup>

CD CK

$\rightarrow R(ABCDEF)$

$AB \rightarrow C, C \rightarrow DE, E \rightarrow F, D \rightarrow A, C \rightarrow B$

$AB \cancel{CDEF}$

$AB$

$A^+ \times$

$B^+ \times$

$|AB \text{ is } CK|$

$D \rightarrow A$

$C \rightarrow B$

$PA = A, B, C, D$

$CK$

$AB$

$BD$

$C$

~~$AB$~~   $XAC$

$B^+ \times \quad A^- \times$

$B^+ \times \quad C^+ \checkmark$

$|BD \text{ is } CK|$

$|C \text{ is } CK|$

$AB \rightarrow C$

$C \rightarrow D$

$XCD$

$AB \checkmark$

$C^+ \checkmark$

## Problem Redundancy

Idea: In the table `Student_Info` we tried to store entities data about student. (in 1 table)

Result: Entire branch data of a branch must be repeated for every student of the branch

Key

Sid	Name	Age	Br_Code	Branch	Hod_name
1	A	18	101	CS	ABC
2	B	19	101	CS	ABC
3	C	18	101	CS	ABC
4	D	21	102	EC	PQR
5	E	20	102	EC	PQR
6	F	19	103	ME	XYZ

unnecessary repetition

Redundancy: When some data is stored multiple times unnecessarily in a database.

### Disadvantages

suppose we change Hod of CS  
it due to some user  
it is not updated at all places

- Insertion, deletion & modification anomalies
- Inconsistency of data
- Inc in database size & access time (slow)

- Insertion anomalies: When certain data (attribute) cannot be inserted into database without the presence of other data

eg: Branch data can't be inserted without student data i.e. if a branch doesn't contain any student, it doesn't exist in the database.

- Deletion anomalies: If you want to delete some unwanted data & it causes deletion of necessary data

eg: If we delete data of Student with `Sid=6`, all data of ME branch vanishes from the table bcz F was the only st. in ME branch.

updation

- Modification anomalies: If we want to update a single piece of data but to do this we need to update all its copies.

OLTP require norm. OLAP - not req.

multiple entity data in 1 table

Adv. remove anomalies  
avg ↓ speed ↑  
Simple queries  
OLTP system  
reduce red/ines

Page No.  
Date

Process of removing redundant data from your tables to improve storage efficiency, data integrity & scalability. speed too. Page No. \_\_\_\_\_  
 usually involves decomposition of table.

Data \_\_\_\_\_

Page No. \_\_\_\_\_

~~Diff. entities must be stored in diff. tables~~

Decomposition

## NORMALISATION

Key

Sid	Name	Age	Br_code
1	A	18	101
2	B	19	101
3	C	18	101
4	D	21	102
5	E	20	102
6	F	19	103

Key

Br_code	Branch	HOD_Name
101	CS	ABC
102	EC	PQR
103	ME	XYZ

Branch\_Info

Student\_Inf

## FIRST NORMAL FORM

(When ERD is mapped into relational  $\rightarrow$  It is in 1NF)

PK

not in 1NF

Roll	Name	Course
101	Modi	CN/OS
102	Sonia	DBMS/CO

↓

Roll	Name	Course
101	Modi	CN
101	Modi	OS
102	Sonia	DBMS
102	Sonia	CO

PK = Roll, Course

Multival attr

- Values of all attributes must be atomic (single)

split row sometimes column

- Every column must have unique name. & rows  $\rightarrow$  unique

Composite attr

- Order of rows & columns is irrelevant

Each multival attr will have a separate table

- all values of a particular column must be from same domain.

Take multi columns for multival attr (not preferred)

- A relation must have a PK

## SECOND NORMAL FORM

For a table to be in 2NF

- It must be in 1NF
- It must not contain partial dependencies.

cg R(A B C D)

CK = AB

prime attributes - A, B  
 non prime - C, D

AB  $\rightarrow$  D But B  $\rightarrow$  C (partial)

To find whether a table is in 2NF

when it is given that table is in 1NF

- Find all CK
- Find prime & non prime attributes
- Non prime attributes must not be involved in partial dependencies

→ Major problem with partial dependencies

A B

AB combined can find A

1 -

But B alone can't find C as it contains null values

- 2

3 -

5 4

→ To solve → decompose:

$$R(ABC) \rightarrow R_1(AB) \& R_2(BC)$$

(This must contain CK)

→ R(ABC)

INF ✓

R		
A	B	C
a	1	x
b	2	y
a	3	z
c	3	z
d	3	z
e	3	z

Candidate keys:

$$(AB)^+ = ABC$$

so AB is CK

Prime attributes: A, B

Non prime — : C

$B \rightarrow C$  is partial dep.

not in 2NF

$$R(ABC) \rightarrow R_1(AB) \& R_2(BC)$$

2NF ✓ 2NF ✓

$B \rightarrow C$

R <sub>1</sub>		R <sub>2</sub>	
A	B	B	C
a	1	1	x
b	2	2	y
a	3	3	z
c	3		
d	3		
e	3		

→  $R(ABCDE)$

$$AB \rightarrow C, D \rightarrow E$$

- Candidate keys:

$$(ABD)^+ = ABDCFE$$

∴  $ABD$  is the CK

- Prime attributes:  $A, B, D$

- Non prime - :  $C, E$

part of CK  $AB \rightarrow C^{NP}$  is partial def.

Part of CK  $D \rightarrow E^{NP}$  is also

∴ It is not in 2NF

To convert in 2NF:

$$R(ABCDEF) \rightarrow R_1(ABC), R_2(DE), R_3(ABD)$$
$$AB \rightarrow C \quad D \rightarrow E$$

→  $R(ABCDE)$

$$A \rightarrow B, B \rightarrow E, C \rightarrow D$$

- Candidate keys:

$$(AC)^+ = ACBDE$$

∴  $AC$  is CK

To convert into 2NF

- while decomposition

- make a table of CR & attr dep on it

- Partial dep. of NP

attr determin some other

attr, u may include it in the table

- Prime attributes:  $A, C$

- Non prime - :  $B, D, E$

- Partial dependencies:

$$A \rightarrow B, C \rightarrow D$$

∴ It is not in 2NF

To convert into 2NF

$$R(ABCDEF) \rightarrow R_1(ABE), R_2(ED), R_3(AC)$$

→  $R(ABCDEFGHIJ)$

$$AB \rightarrow C, AD \rightarrow GH, BD \rightarrow EF, A \rightarrow I, H \rightarrow J$$

CK:  $(ABD)^+ = ABDCGHIJEF$   $\Rightarrow ABD$  is CK

PA =  $A, B, D$ , NPA =  $C, E, F, G, H, I, J$

PD =  $AB \rightarrow C, AD \rightarrow GH, BD \rightarrow EF, A \rightarrow I,$

Dec.:  $R_1(ABC), R_2(ADGH), R_3(BDEF), R_4(AI), R_5(ABD)$

Partial dep.  $\rightarrow$  proper subset of CK  $\rightarrow$  NP

Transitive dep.  $\rightarrow$  NP  $\rightarrow$  NP

So  $\alpha = \text{Super Key}$   $\beta \supseteq NP$

Page No.

Date

### THIRD NORMAL FORM

NP  $\rightarrow$  NP

Transitive Dependency:

A FD from  $\alpha - \beta$  is called  
transitive if  $\alpha, \beta \in$  Non prime

R(ABC)

$A \rightarrow B$ ,  $B \rightarrow C$

It is in 2NF

Conditions:

A relation R is in 3NF if

- It is in 2NF
- It has no transitive dependency

$R(ABC) \rightarrow R_1(BC), R_2(AB)$

R		
A	B	C
a	1	x
b	1	x
c	1	x
d	2	y
e	2	y
f	3	z
g	3	z

Alternative:

For every dep. from  $\alpha \rightarrow \beta$

- either  $\alpha$  is super Key or
- $\beta$  is a prime attribute

R<sub>1</sub>      R<sub>2</sub>

A	B	R <sub>1</sub>	R <sub>2</sub>
a	1	1	x
b	1	2	y
c	1	3	z
d	2		
e	2		
f	3		
g	3		

$\Rightarrow R(ABCDEFGH)$   
 $ABC \rightarrow E, E \rightarrow GH, H \rightarrow G, G \rightarrow H, ABCD \rightarrow EF$

BCNF ✓

is in 3NF

$\Rightarrow R(ABCD)$   $AB \rightarrow CD$   $AC \rightarrow BD$   $BC \rightarrow D$

CK = AB, AC

\* union of proper subsets of cliff  
CKs is treated as proper subset  
of CK

$\Rightarrow R(A, B, C, D, E, F)$

$AB \rightarrow CDEF$      $BD \rightarrow F$

CK: AB

PA = A, B

NPA = C, D, E, F

2NF:  $AB \rightarrow CDEF$ ,  $BD \rightarrow F$

not part of CK

3NF:  $AB \rightarrow CDEF$ ,  $BD \rightarrow F$

PA

NPA

But if it was

$ABD \rightarrow F$

it is in BCNF

so it is in 3NF

→  $R(ABCDF)$

$A \rightarrow B$ ,  $B \rightarrow F$ ,  $C \rightarrow D$

CK :  $(AC)^+ = ABCDE$   $\therefore AC$  is CK

PA = A, C

NPA = B, D, E

$R_1(ABE)$

$A \rightarrow B$ ,  $B \rightarrow E$

↓

$R_{11}(AB)$   $A \rightarrow B$

$R_{12}(BE)$   $B \rightarrow E$

$R_2(CD)$

$C \rightarrow D$

$R_3(AC)$

↓

→  $R(ABCDEFIGHIJ)$

$AB \rightarrow C$ ,  $A \rightarrow DF$ ,  $B \rightarrow F$ ,  $F \rightarrow GH$ ,  $D \rightarrow IJ$

CK :  $(AB)^+ = ABCDEFIGHIJ \Rightarrow AB$  is CK

PA = A, B

NPA = C, D, E, F, G, H, I, J

$R_1(ADEIJ)$

$A \rightarrow DE$ ,  $D \rightarrow IJ$

↓

$R_{11}(ADE)$

$A \rightarrow DE$

$R_{12}(DIJ)$

$D \rightarrow IJ$

$R_2(BFGH)$

$B \rightarrow F$ ,  $F \rightarrow GH$

↓

$R_{21}(BF)$

$B \rightarrow F$

$R_3(ABC)$

$AB \rightarrow C$

→  $R(ABCDEF)$

$AB \rightarrow C$ ,  $B \rightarrow D$ ,  $D \rightarrow E$

CK :  $(AB)^+ = ABCDEF$

$AB$  is CK

PK  
B

$R_1(BDE)$   $B \rightarrow D$ ,  $D \rightarrow E$

↓

$R_{11}(BD)$   $B \rightarrow D$

$R_{12}(DE)$   $D \rightarrow E$

$R_2(ABC)$

$AB \rightarrow C$

$\rightarrow R(ABCDEF GHIJ)$

$AB \rightarrow C, AD \rightarrow GH, BD \rightarrow EF, A \rightarrow I, H \rightarrow J$

CK:  $(ABD)^+ = ABCDEFGHIJ$   $ABD$  is CK

$R_1 (\underline{ABC}I)$

$AB \rightarrow C, A \rightarrow I$

$R_{11} (\underline{ABC})$

$AB \rightarrow C$

$R_{12} (\underline{AI})$

$A \rightarrow I$

$R_2 (ADGHJ)$

$AD \rightarrow GH, H \rightarrow J$

$R_{21} (\underline{ADGH})$

$AD \rightarrow GH$

$R_{22} (\underline{HJ})$

$H \rightarrow J$

$R_3 (BDEF) R_4 (\underline{ABD})$

$-BD \rightarrow EF$

Boyce  
Codd  
Normal  
Form

BCNF

(Advanced 3NF)

P/NP  $\rightarrow P$

P shouldn't be of RHS

Eg:  $R(ABC)$

$AB \rightarrow C, C \rightarrow B$

2NF ✓ 3NF ✓

X BCNF

$A^+ X (AB)^+ = ABC \checkmark$   $AC^+ = ABC \checkmark$

$PA = A, B, C$   $NPA = X$

Condition:  $\alpha$  should be super key.

$\rightarrow$  It says prime attributes shouldn't be determined by any non prime or part of CK.

Rules:

- It must be in 3NF

- Prime attributes shouldn't be determined by any non prime attributes or part of CK.

or  $\alpha \rightarrow SK$

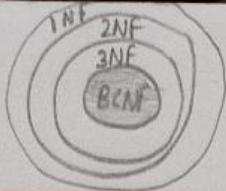
bcoz if  $\alpha = SK$  3NF ✓ &  $\alpha \neq NP$  or part of CK

If all CK are simple (single attr.) it will be in 2NF

If all attr. of a relation are prime attr., it will be in 3NF

$\times$  If relation is in 3NF & all CKs are simple, it will be in BCNF

$R(ABCD)$  Let A & B are CK & one of PB is  $C \rightarrow B$  3NF ✓ CK are simple but still not in BCNF - 1



Page No.  
Data

→  $R(ABC)$

$AB \rightarrow C$ ,  $C \rightarrow B$   
 $CK = AB, AC$   
 $3NF \checkmark$        $BCNF X$

$R_1(CB)$

$R_2(AC)$

A	B	C
a	1	z
b	2	y
c	2	z
c	3	w
d	3	w
e	3	w

One table should contain any  
one of the CKs

$R_2(AC)$        $R_3(AB)$

C is common      B is common  
C is PK      but B isn't PK

A	C	C	B
a	x	x	1
b	y	y	2
c	z	z	2
c	w	w	3
d	w		
e	w		

Problems :

A relational table is always in 1NF

Check for  $BCNF \rightarrow 3NF \rightarrow 2NF \rightarrow 1NF$

- $BCNF \rightarrow \alpha$  is SK
- $3NF \rightarrow \alpha \rightarrow SK$  or  $\beta$  is P
- $2NF \rightarrow$  check for partial dep
- $1NF \rightarrow$  always ✓

→  $R(ABCDEFGH)$

$\cancel{AB} \rightarrow C$ ,  $\cancel{A} \rightarrow DE$ ,  $\cancel{B} \rightarrow F$ ,  $\cancel{F} \rightarrow GH$

$CK : (AB)^+ = ABCDEFGH$       AB is CK

$BCNF X$        $3NF X$        $2NF X$        $1NF \checkmark$

→  $R(ABCDE)$

$\cancel{CF} \rightarrow D$ ,  $\cancel{D} \rightarrow B$ ,  $\cancel{C} \rightarrow A$

$CK : (CE)^+ = ABCDE$       CF is CK

$BCNF X$        $3NF X$        $2NF X$        $1NF \checkmark$

\*  $\rightarrow R(ABCDEF)$

$$\cancel{\exists AB \rightarrow C}, \cancel{\exists DC \rightarrow AE}, \cancel{\exists E \rightarrow F}$$

$$CK: (BD)^+ = BD$$

BCNF X

3NF X

2NF X

1NF ✓

$$(ABD)^+ = ABCDEF \checkmark$$

$$(BCD)^+ = BCDAEFF \checkmark$$

$$(BDE)^+ = BDEF \times$$

$$(BDF)^+ = BDF \times$$

$$(BDEF)^+ = BDEF \times$$

so ABD & BCD are CKs

$\rightarrow R(ABCDEFHI)$

$$\cancel{\exists AB \rightarrow C}, \cancel{\exists BD \rightarrow EF}, \cancel{\exists AD \rightarrow GH}, \cancel{\exists A \rightarrow I}$$

$$CK: (ABD)^+ = ABCDEFGHI \checkmark \quad ABD \text{ is CK}$$

BCNF X

3NF X

2NF X

1NF ✓

$\rightarrow R(ABCDE)$

$$\cancel{\exists AB \rightarrow CD}, \cancel{\exists D \rightarrow A}, \cancel{\exists BC \rightarrow DE}$$

$$CK: B \times \#$$

$$(AB)^+ = ABCDE \checkmark \quad (BC)^+ = ABCDE \checkmark \quad (BD)^+ = BDACE \checkmark \quad (BE)^+ = BE \times$$

AB, BC, BD are CK

BCNF X

3NF ✓

2NF ✓

1NF ✓

$\rightarrow R(ABCDE)$

$$\cancel{\exists BC \rightarrow ADE}, \cancel{\exists D \rightarrow B}$$

$$CK: C \times$$

BCNF X

3NF ✓

2NF ✓

1NF ✓

$$(AC)^+ = AC \times \quad (BC)^+ = ABCDE \checkmark \quad (CD)^+ = CDBAE \checkmark \quad CE \times$$

$$(ACE)^+ = ACE \times$$

BC & CD are CK

$\rightarrow R(VWXYZ)$

$$\cancel{\exists X \rightarrow YV}, \cancel{\exists Y \rightarrow Z}, \cancel{\exists Z \rightarrow Y}, \cancel{\exists VW \rightarrow X}$$

$$CK: W \times ,$$

BCNF X

3NF X

2NF X

1NF ✓

$$(XW)^+ = XYVZW \checkmark \quad (VW)^+ = VWXYZ \checkmark$$

$$(YW)^+ = YWZ \times$$

$$(ZW)^+ = ZWY \times$$

$$(YZW)^+ = YWZ \times$$

$$XW \& VW \text{ are CK}$$

attaining BCNF is too expensive

Theoretical concept  
3NF is far too good  
2NF too is OK

Page No.

Date

→  $R(ABCDEF)$

$\checkmark ABC \rightarrow D$ ,  $\checkmark ABD \rightarrow E$ ,  $\checkmark CD \rightarrow F$ ,  $\checkmark CDF \rightarrow B$ ,  $\checkmark BF \rightarrow D$   
 $CK : (Ac)^+ = AC \times$

$PA = A, B, CD$      $(ABC)^+ = ABCDEF \checkmark$      $(ACD)^+ = ACDFBF \checkmark$   
 $NPA = E, F$      $(ACE)^+ = ACE \times$      $(ACF)^+ = ACF \times$   
                     $(ACEF)^+ = ACEF \times$

ABC & ACB are CKs

BCNF X    3NF X    2NF X    INF ✓

→  $R(ABC)$

$A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow A$   
 $CK : A^+ = ABC \checkmark$      $B^+ = BCA \checkmark$      $C^+ = CAB \checkmark$

→  $R(ABCDEF)$

$A \rightarrow BCDEF$ ,  $BC \rightarrow ABDEF$ ,  $DEF \rightarrow ABC$   
 $CK : A^+ = ABCDEF \checkmark$      $B^+ = C \times$      $D \times$      $F \times$   
 $(BC)^+ = ABCDEF \checkmark$      $BD \times$      $BE \times$      $BF \times$      $CD \times$      $CF \times$      $CE \times$      $DE \times$      $EF \times$   
 $BDF \times$      $BDF$      $BCD$      $BEF \times$      $BCF \times$      $BFC \times$      $CDE \times$      $CDF \times$      $CFE \times$      $DEF \times$   
 $BDEF$      $BDEC$      $BDFC$      $BFFC$      $CDEF$   
 $\therefore A, BC \& DEF$  are CK

→  $R(ABC)$

$\checkmark AB \rightarrow C$ ,  $\checkmark C \rightarrow A$   
 $CK : B^+ = \times$      $AB \checkmark$      $BC \checkmark$

BCNF X

3NF ✓

2NF ✓

INF ✓

→  $R(ABCDEF)$

$\cancel{A} \rightarrow B$ ,  $\cancel{BC} \rightarrow E$ ,  $\cancel{DE} \rightarrow A$   
 $CK : CD \times$

BCNF X

3NF ✓

2NF ✓

INF ✓

$CDA \rightarrow ABCDEF \checkmark$      $BCD = BCDEF \checkmark$      $CDE = ACDFB \checkmark$

ACD, BCD & CDF are CK

$\rightarrow R(ABCDEF)$

$$\checkmark AB \rightarrow CD, \checkmark D \rightarrow A, \checkmark BC \rightarrow DE$$

BCNF X

3NF ✓

$$CK: \begin{matrix} A^x & B^x & C^x & D^x & E^x \\ AB & AC & AD & AE & BE \\ AC^x & AC^x & ABC & ADE & ADB \\ ACD & ACE & ABC & ADE & ADB \end{matrix}$$

$$\begin{matrix} BC^v & BD^v & BE^x & CD^x & CE^x & DE^x \\ BE^x & CD^x & CE^x & DE^x \\ ACFBEC & BDF & CDE & ACD \end{matrix}$$

$\rightarrow R(WXYZ)$

$$\checkmark z \rightarrow w, \checkmark Y \rightarrow XZ, \checkmark Xw \rightarrow Y, \checkmark$$

BCNF X

3NF ✓

$$CK: \begin{matrix} w^x & x^x & Y^v & z^x \\ WX^v & WZ^x & XZ^v \end{matrix}$$

$\rightarrow R(ABCDEF)$

$$\checkmark A \rightarrow B, \checkmark B \rightarrow E, \checkmark C \rightarrow D$$

BCNF X

3NF X

INF ✓

$$CK: AC = ACDBE \quad \checkmark$$

2NF X

$\rightarrow R(ABCDEF)$

$$\checkmark AB \rightarrow C, \checkmark DC \rightarrow AE, \checkmark E \rightarrow F$$

BCNF X

3NF X

2NF X

INF ✓

$$CK: \begin{matrix} BD^x & (ABD)^+ = ABDCF & (BCD)^+ = BCAE & BDF^x & BDF^x \\ ABD & ABDF & BDEF & BDEF & BDEF \end{matrix}$$

ABD & BCD

$\rightarrow R(VWYZ)$

$$\checkmark z \rightarrow Y, \checkmark Y \rightarrow Z, \checkmark X \rightarrow YV, \checkmark VW \rightarrow X$$

BCNF X

3NF X

INF ✓

$$CK: \begin{matrix} W^x & (VW)^+ = VWXYZ & (WX)^+ = WXYZ^v & (WY)^+ = WYZ^x \\ (WZ)^+ = WZY^x & \end{matrix}$$

$$WYZ = WYZ^x$$

$\rightarrow R(ABCDEF)$

$$\checkmark ABC \rightarrow D, \checkmark ABD \rightarrow E, \checkmark CD \rightarrow F, \checkmark CDF \rightarrow B, \checkmark BF \rightarrow D$$

BCNF X

3NF X

2NF X

$$CK: (AC)^+ = ^x$$

$$\begin{matrix} ABC^v & ACD^v & ACE^x \\ ACEF^x & \end{matrix}$$

$$ACE^x$$

$$ACF^x$$

INF ✓

$\rightarrow R(ABCDEF)$

$$\begin{array}{l} \cancel{C} \rightarrow F, \cancel{E} \rightarrow A, EC \rightarrow D, \cancel{A} \rightarrow B \\ CK: (CE)^+ = CEFAD \end{array}$$

BCNF X

3rd X

2NF X

INF ✓

$\rightarrow R(ABCDEFGH)$

$$\begin{array}{l} \checkmark A \rightarrow B, BC \rightarrow D, \cancel{E} \rightarrow C, \checkmark D \rightarrow A \end{array}$$

BCNF X

3rd X

$$CK: (EH)^+ = EHC$$

2NF X

INF ✓

$$\begin{array}{c} AEH \quad BEH \quad CEH \quad DEH \\ \cancel{BFHG} \end{array}$$

$\therefore EH, AEH, DEH, BEH$

$\rightarrow R(ABCDEPGI)$

$$\begin{array}{l} \checkmark AB \rightarrow CD, \checkmark DE \rightarrow P, \cancel{C} \rightarrow E, \cancel{P} \rightarrow C, \checkmark B \rightarrow G \\ CK: (AB)^+ = ABCDEPG \end{array}$$

BCNF X

3NF X

2NF X

INF ✓

$\rightarrow R(ABCDEFGH)$

$$\begin{array}{l} \cancel{CH} \rightarrow G, \cancel{A} \rightarrow BC, \checkmark B \rightarrow CFH, \cancel{E} \rightarrow A, \cancel{F} \rightarrow EG \\ CK: \cancel{D} \end{array}$$

BCNF X

3NF X

2NF X

$$\begin{array}{ccccccc} AD & \cancel{AB} & BD & \cancel{CD} & FD & \cancel{FG} & \cancel{HD} \\ ABCDFHEG & BDCFHGEA & & ABCDEF & ABCD & FHEG & \end{array}$$

$$\begin{array}{ccc} \cancel{CDG} & \cancel{CDH} & \cancel{GDH} \\ \cancel{CDGH} & \end{array}$$

$\therefore CK = AD, BD, FD, FG$

$\rightarrow R(ABCD)$

BCNF X

3NF X

CK is not  
compleat  
so 2NF

$$\begin{array}{l} \checkmark A \rightarrow B, \cancel{B} \rightarrow C, \cancel{C} \rightarrow BD \\ CK: (A)^+ = ABCD \end{array}$$

2NF V

INF V

$\rightarrow R(ABCDEF)$

BCNF X

3NF X

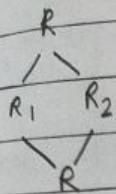
2NF V

INF V

$$\begin{array}{l} \cancel{AB} \rightarrow CD, \cancel{CD} \rightarrow EF, \cancel{BC} \rightarrow DEF, \cancel{BD} \rightarrow B, \cancel{CE} \rightarrow F \\ CK: (A)^+ = ABCD \end{array}$$

$$\begin{array}{ccc} AC & ACF & AEF \\ AC \cancel{EF} & & \end{array}$$

## DECOMPOSITION



Lossless join decomposition / non additive

This property guarantees that the extra or less tuple generation problem doesn't occur after decomposition.

- Decomposition must be lossless

If a relation  $R$  is decomposed into two relations  $R_1$  &  $R_2$ , then it will be loss-less iff

- $\text{attr}(R_1) \cup \text{attr}(R_2) = \text{attr}(R)$

$A$	$B$	$C$	$D$	$\xrightarrow{\text{decompo-}} \quad \quad \quad$	$A$	$B$	$D$	$\circled{Lossy}$
$\equiv$	$\equiv$	$\equiv$	$\equiv$		$\equiv$	$\equiv$	$\equiv$	
$R$					$R_1$		$R_2$	$c$ is missing

- $\text{attr}(R_1) \cap \text{attr}(R_2) \neq \emptyset$

$A$	$B$	$C$	$D$	$\xrightarrow{\text{decompo-}} \quad \quad \quad$	$A$	$B$	$C$	$D$	$\xrightarrow{\text{combine}} \quad \quad \quad$	$A$	$B$	$C$	$D$
1	a	p	x		1	a	p	x		1	a	p	x
2	b	q	y		2	b	q	y		2	b	q	y
$R$					$R_1$		$R_2$			$R$			

extra tuples added (loss)  $\circled{Lossy}$

- $\text{attr}(R_1) \cap \text{attr}(R_2) \rightarrow \text{attr}(R_1)$

or

- $\text{attr}(R_1) \cap \text{attr}(R_2) \rightarrow \text{attr}(R_2)$

common attr must be  
super key of atleast  
one of the subtables

common attr must be  
super key of atleast  
one of the subtables  
it must be  
values of  
the decom-  
position  
of the decom-  
position  
must be  
fixed

$A$	$B$	$C$	$\xrightarrow{\text{decompo-}} \quad \quad \quad$	$A$	$B$	$B$	$C$	$\xrightarrow{R_1 \Delta R_2} \quad \quad \quad$	$A$	$B$	$C$
1	a	p		1	a	a	p		1	a	p
2	b	q	$\xrightarrow{\text{-sition}}$	2	b	b	q		1	a	x
3	a	x		3	a	a	x		2	b	q
$R$				$R_1$		$R_2$			3	a	p

extra tuples added  $\circled{Lossy}$

## Examples

→

lossy X -  $R_1(AB)$   $R_2(CD)$   $\overset{1st}{\times}$

lossy X -  $R_1(ABC)$   $R_2(BE)$   $\overset{2nd}{\times}$

lossy -  $R_1(ABC)$   $R_2(CDE)$   $\overset{1st}{\checkmark}$   $\overset{2nd}{\checkmark}$   $\overset{3rd}{\times}$

lossless ✓ -  $R_1(ABCD)$   $R_2(ACDE)$

lossless ✓ -  $R_1(ABCD)$   $R_2(DE)$

lossless ✓ -  $R_1(ABC)$   $R_2(BCD)$   $R_3(DE)$

BC common & CK

$R(ABCD)$   $R_3(CDE)$

D common & CK

union = ABCDE

A	B	C	D	E
a	122	1	p	w
b	234	2	q	x
c	568	1	r	y
c	343	3	s	z

whether common key is distinct

→  $R(VWXYZ)$

✓ -  $Z \rightarrow Y$ ,  $Y \rightarrow Z$ ,  $X \rightarrow YV$ ,  $VW \rightarrow X$

-  $R_1(VWX)$   $R_2(XYZ)$

X -  $R_1(VW)$   $R_2(YZ)$   $\overset{1st}{\times}$

X -  $R_1(VWX)$   $R_2(YZ)$   $\overset{2nd}{\times}$

(may not be lossy) -  $R_1(VW)$   $R_2(WXYZ)$   $\overset{3rd}{\times}$

but not lossless

→ X  $R_1(ABC)$   $R_2(DE)$  X common x

✓  $R_1(ABC)$ ,  $R_2(ABDE)$

X  $R_1(ABC)$ ,  $R_2(CD)$  X E x

✓  $R_1(ABC)$   $R_2(CDE)$  ✓

X  $R_1(AB)$   $R_2(BCDE)$  x

X  $R_1(AB)$   $R_2(CD)$   $R_3(DE)$  ✓

combine any 2 first

$R_1(AB)$   $R_{23}(CDE)$  X

A	B	C	D	E
1	1	2	1	3
2	2	2	1	3
3	1	6	3	6
4	2	8	5	7
5	3	9	5	7

→  $R(ABCDEF)$  X lossy

F : {  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow A$  }

$R_1(ABC)$   $R_2(CD)$

$C \rightarrow ABC$

∴ C is CK of R.

→  $R(ABCDEF)$  X lossy

F - {  $AB \rightarrow C$ ,  $C \rightarrow D$ ,  $D \rightarrow EF$ ,

$F \rightarrow A$ ,  $D \rightarrow B$  }

3 E + F  
lossless

$D(ABC, CDE, EF)$

$C^+ = CD$   $EFAB$

$R_1(ABCDEF)$   $R_3(EF)$

$E^+ = E$

$R$   
 $FD \rightarrow F$

$R_1$        $R_2$   
 $FD \rightarrow F_1$      $FD \rightarrow F_2$   
 $FD \rightarrow F$

## Dependency Preserving Decomposition

If a table  $R$  having  $FD$  set  $F$  is decomposed into two tables  $R_1$  &  $R_2$  having  $FD$  sets  $F_1$  &  $F_2$  then,

$F_1 \subseteq F^+$   
 $F_2 \subseteq F^+$   
 $(F_1 \cup F_2)^+ = F^+$

$R_1, R_2, R_3, \dots, R_n = R$   
 $F_1 \cup F_2 \cup F_3 \cup \dots \cup F_n = F$

~~CF X~~

$F$  must not be superset  
union can be

$\rightarrow R(ABC)$

$A \rightarrow B, B \rightarrow C, C \rightarrow A$

Also  
lossless

$R_1(AB)$

$R_2(BC)$

Dependency preserved

$F_1: A \rightarrow B$

$F_2: B \rightarrow C$

$B \rightarrow A$

$C \rightarrow B$

$F_1 \cup F_2$

:  $A \rightarrow B, B \rightarrow C, B \rightarrow A, C \rightarrow B$

$C^+ = CBA$

$\rightarrow R(ABCD)$

$AB \rightarrow CD$

$D \rightarrow A$

Dependency not preserved !!

$R_1(AD)$

$R_2(BCD)$

→ Find closure of all combos to find  $F_1, F_2$   
and trivially

$F_1: A \rightarrow x$

$F_2: B \rightarrow x$

$C \rightarrow x$

$BC \rightarrow x$

$B \rightarrow x$

$CD \rightarrow x$

$D \rightarrow A$

$B \rightarrow x$

$BD \rightarrow C$

$C$

$F_1 \cup F_2 = D \rightarrow A, BD \rightarrow C$

$(AB)^+ = AB$

Note: This decomposition is lossless hence it is valid

Lossless → mandatory

Dep. pres. → not mandatory but must be  
(sometimes not in BCNF)

$\rightarrow R(ABCDEF\bar{G}\bar{H}IJ)$

$\cancel{A} \rightarrow \cancel{DE}$ ,  $\cancel{B} \rightarrow F$ ,  $\cancel{F} \rightarrow GH$ ,  $\checkmark AB \rightarrow C$ ,  $\cancel{D} \rightarrow IJ$

• Candidate keys :  $(AB)^+ = ABCDEF\bar{G}\bar{H}IJ$   
Therefore AB is CK

• Prime attributes : A, B

• Non-prime — : C, D, E, F, G, H, I, J

Not in 2NF, 3NF or BCNF

Decomposition  $\rightarrow$  2NF, 3NF & BCNF

$R_1(\underline{ABC})$

$\boxed{2nd} \rightarrow AB \rightarrow C$

$R_2(\underline{ADEIJ})$

$A \rightarrow DE$ ,  $D \rightarrow IJ$

$R_3(\underline{BFGH})$

$B \rightarrow F$ ,  $F \rightarrow GH$

$\boxed{3rd} \rightarrow$

also in BCNF  $\rightarrow$

$R_{21}(\underline{ADE})$

$\underline{A} \rightarrow DE$

$R_{22}(\underline{DIJ})$

$D \rightarrow IJ$

$R_{31}(\underline{BF})$

$B \rightarrow F$

$R_{32}(\underline{FGH})$

$F \rightarrow GH$

### DEPENDENCY PRESERVING

$\rightarrow R(ABCDEF)$

$F - \{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

check only  
 $F \subseteq G$

$R_1(A, B, C)$

$F_1: A^+ \rightarrow ABCD$

$B^+ \rightarrow BCD\cancel{A}$

$C^+ \rightarrow CBAB$

$R_2(C, DE)$

$F_2: C^+ \rightarrow DAB$

$D^+ \rightarrow ABCD$

$E^+ \rightarrow E$

as only  
A, B, C  
can derive  
all no need  
to take  
their combis

sudden  
dant

$AB^+ \rightarrow ABCD$

$BC^+ \rightarrow ABCD$

$AC^+ \rightarrow ABCD$

$CD^+ \rightarrow ABCD$

$CE^+ \rightarrow ABCD$

$DE^+ \rightarrow ABCD$

Do  $F_1: A \rightarrow BC$ ,  $B \rightarrow AC$ ,  $C \rightarrow AB$

$F_2: C \rightarrow D$ ,  $D \rightarrow C$

$G_1 = F_1 \cup F_2 = A \rightarrow BC$ ,  $B \rightarrow AC$ ,  $C \rightarrow AB$ ,  $C \rightarrow D$ ,  $D \rightarrow C$

Here  $\boxed{1} \quad \boxed{2} \quad F \subseteq G_1 \quad \& \quad G_1 \subseteq F_1$  (obvious)

$\therefore F \equiv G_1$

preserved

$\rightarrow R(A B C D E)$

$$F = \{ A \rightarrow BCD, B \rightarrow AE, BC \rightarrow AED, D \rightarrow E, C \rightarrow DE \}$$

$R_1(A B)$

$$F_1: A^+ \rightarrow AB \cancel{C} \cancel{D} \cancel{E}$$

$$B^+ \rightarrow BA \cancel{F} \cancel{C} \cancel{D}$$

$R_2(BC)$

$$F_2: B^+ \rightarrow B \cancel{A} \cancel{C} \cancel{D} \cancel{E}$$

$$C^+ \rightarrow \cancel{C} \cancel{D} \cancel{E}$$

$R_3(CDE)$

$$F_3: C^+ \rightarrow \cancel{C} \cancel{D} \cancel{E}$$

$$D^+ \rightarrow \cancel{D} E$$

$$E^+ \rightarrow \cancel{E}$$

$$F_1: A \rightarrow B, B \rightarrow A$$

$$F_2: B \rightarrow C$$

$$F_3: C \rightarrow DE, D \rightarrow E$$

$$F_1 \cup F_2 \cup F_3 = A \rightarrow B, B \rightarrow A, B \rightarrow C, C \rightarrow DE, D \rightarrow E$$

$$A^+ = ABCDE$$

$$B^+ = BACDE$$

$$BC^+ = BCDFA$$

$$D^+ = DE$$

$$C^+ = CDE$$

$$\therefore F \subseteq G$$

$F$  will cover  $G$  always  $\therefore G \subseteq F$

$$\therefore F \equiv G \quad \underline{\text{preserved}}$$

$\rightarrow R(A B C D)$

$$F: \{ A \rightarrow B, C \rightarrow D \}$$

$R_1(AC), R_2(BD)$

$$F_1: A \rightarrow AB$$

$$C \rightarrow \cancel{C} \cancel{D}$$

$$F_2: B \rightarrow B'$$

$$D \rightarrow \cancel{D}$$

$F_1$  is empty

not preserved

$F_2$  is empty

$F_1 \cup F_2$  is empty

$\rightarrow R(ABCDEF)$

$$F: \{ A \rightarrow BCD, BC \rightarrow AED, D \rightarrow E \}$$

$R(AB)$

$$A \rightarrow AB \cancel{C} \cancel{D} \cancel{E} \cancel{F}$$

$$B \rightarrow B'$$

$R_2(BC)$

$$B \rightarrow B$$

$$C \rightarrow \cancel{C}$$

$R_3(CDE)$

$$C \rightarrow \cancel{C}$$

$$CE \rightarrow \cancel{C} \cancel{E}$$

$$DE \rightarrow \cancel{D} \cancel{E}$$

$$D \rightarrow \cancel{D} E$$

$$CD \rightarrow \cancel{C} \cancel{D} E$$

$$F_1: A \rightarrow B$$

$$F_2: \emptyset$$

$$F_3: D \rightarrow E \quad \emptyset$$

$$G = F_1 \cup F_2 \cup F_3 = A \rightarrow B, D \rightarrow E$$

→  $R(ABC \rightarrow D)$

$F: \{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

$R_1(AB)$

$A^+ \rightarrow AB \text{ & } \cancel{B}$

$B^+ \rightarrow A \cancel{B} \text{ & } \cancel{B}$

$F_1: \{A \rightarrow B, B \rightarrow A\}$

$R_2(CD)$

$C^+ \rightarrow ABC \cancel{D}$

$D^+ \rightarrow A \cancel{B} \text{ & } \cancel{D}$

$F_2: \{B \rightarrow C, C \rightarrow B\}$

$R_3(CD)$

$C^+ \rightarrow ABD$

$D^+ \rightarrow ABCN$

$F_3: \{C \rightarrow D, D \rightarrow C\}$

$G = F_1 \cup F_2 \cup F_3: \{A \rightarrow B, B \rightarrow A, B \rightarrow C, C \rightarrow B, C \rightarrow D, D \rightarrow C\}$

$F \subseteq G \quad \& \quad G \subseteq F$

∴  $F \equiv G$  preserved

→  $R(ABC \rightarrow DEF)$

$F: \{AB \rightarrow C, C \rightarrow D, D \rightarrow EF, E \rightarrow A, D \rightarrow B, E \rightarrow F\}$

$R_1(ABC)$

$A^+ \rightarrow A \quad AB \rightarrow ABCDEF$

$B^+ \rightarrow B$

$C^+ \rightarrow CDEFAB$

$R_2(CDE)$

$C^+ = CDEFAB$

$D^+ = DEFA \cancel{BC}$

$E^+ = EFA$

$R_3(EF)$

$E^+ = EFA$

$F^+ = FA$

$F_1: \{C \rightarrow AB, AB \rightarrow C\}$

$F_2: \{C \rightarrow DE, D \rightarrow E\}$

$F_3: \{E \rightarrow F\}$

$G = F_1 \cup F_2 \cup F_3 = \{C \rightarrow AB, AB \rightarrow C, C \rightarrow DE, D \rightarrow E, E \rightarrow F\}$

## DECOMPOSITION

1NF  $\rightarrow$  2NF

$$\rightarrow R(ABCD) \quad F: \{ A \rightarrow B, B \rightarrow C \}$$

Find CK  
 $AD^+ = ABCD \quad \therefore AD \text{ is CK}$

$\downarrow$   
 Prime attr. = A, D

Decompose  
 $\downarrow$   
 NPA = B, C

$A^+ = ABC$

$R_1(ABC)$

$A^+ = ABC$

$B^+ = BC$

$C^+ = C$

$F_1: \{ A \rightarrow BC, B \rightarrow C \}$

CK = A

$R_2\{AD\}$  BCNF ✓

$A^+ = ABCD$

$D^+ = D$

$\bullet$

$F_2: \{ \phi \} \neq \phi$

- Make separate

table for PD

- LN table of CK mostly

Find depn.  
for new  
tables

CKs for  
new tables  
 $\downarrow$   
 check if  
decomps into

2NF  
if not  
decompose  
further

Now it is in 2NF

Dependency preserved & Lossless

$$\rightarrow R(ABCD)$$

$$F: \{ A \rightarrow B, C \rightarrow D \}$$

$AC^+ = ABCD \quad \therefore AC \text{ is CK}$

PA = A, C      NPA = B, D

$A^+ = AB \quad C^+ = CD$

$R_1(AB)$

$R_2(CD)$

$R_3(AC)$

$A^+ \rightarrow BA'$

$C^+ \rightarrow CD$

$A^+ = AB$

$B^+ \rightarrow B'$

$D^+ = D$

$C^+ = CN$

$F_1 = \{ A \rightarrow B \}$

$F_2 = \{ C \rightarrow D \}$

$F_3 = \phi$

CK = A

CK = C

Def. Pres ✓, Lossless

2NF  $\rightarrow$  3NF

$\rightarrow R(A, B, C, D)$

$$F: \{ A \rightarrow B, \underline{B \rightarrow C}, \underline{C \rightarrow D} \}$$

$$A^+ = ABCD \quad \therefore A \text{ is CK}$$

$$PA = A, NPA = B, C, D$$

$$B^+ = BCD$$

$$R_1(\underline{BCD})$$

$$B^+ = BCD$$

$$C^+ = CD$$

$$D^+ = D$$

$$CD^+ = CD$$

$$C^+ = CD$$

$$R_2(\underline{CD})$$

$$C^+ = CD$$

$$D^+ = D$$

$$R_3(\underline{AB})$$

$$A^+ = ABCD$$

$$B^+ = BCD$$

2NF

$$\rightarrow F_1: \{ B \rightarrow CD, \underline{C \rightarrow D} \}$$

$$B^+ = BCD$$

$\therefore B \text{ is CK}$

$$C^+ = CD$$

BCNF

$$R_{11}(\underline{CD})$$

BCNF

$$R_{12}(BC)$$

$$C^+ = CD$$

$$B^+ = BC$$

$$D^+ = D$$

$$C^+ = CD$$

$$F_{11}: \{ C \rightarrow D \}$$

$$F_{12}: \{ B \rightarrow C \}$$

BCNF

$$F_2: \{ C \rightarrow D \}$$

C is CK

BCNF

$$F_3: \{ A \rightarrow B \}$$

A is CK

$$R_{12}(BC)$$

$$F_{12}: \{ B \rightarrow C \}$$

Def.

$$R_2(CD)$$

$$F_2: \{ C \rightarrow D \}$$

pros

$$R_3(AB)$$

$$F_3: \{ A \rightarrow B \}$$

& busses

$\rightarrow R(ABCDEFGH)$

F:  $\{A \rightarrow BD, B \rightarrow C, E \rightarrow FG_1, AE \rightarrow H\}$

$$AE^+ = AEBDCFG_1H$$

so AE is CK

PA = A, E

NPA = B, C, D, F, G, H

INFV

2NF<sup>X</sup>:  $A \rightarrow BD, E \rightarrow FG_1$  (PD)

3NF<sup>X</sup>:  $B \rightarrow C$  (TD)

BCNF<sup>X</sup>

$R(ABCDEF GH)$  2NF<sup>X</sup>

R1(ABCD)

$$A^+ = ABCD$$

$$B^+ = BC$$

$$C^+ = \emptyset$$

$$D^+ = D$$

$$BC^+ = BD$$

$$CD^+ = CD$$

$$BCD^+ = BCD$$

R2(EFG<sub>1</sub>)

$$E^+ = EFG_1$$

$$F^+ = F$$

$$G_1^+ = G_1$$

$$FG_1^+ = FG_1$$

R3(HAE)

$$H^+ = H$$

$$A^+ = ABDG$$

$$E^+ = EFG_1$$

$$AH^+ = ABDCGH$$

$$HE^+ = HEG_1$$

$$AE^+ = ABDCFG_1H$$

$A \rightarrow BCD$   $B \rightarrow C$

CK = A

2NFV

PA = A, NPA = B, C, D

$B \rightarrow C$  TD

$E \rightarrow FG_1$

CK = E

2NFV

PA = E NPA = F, G<sub>1</sub>

3NFV

$\oplus AE \rightarrow H$

CK = AE

2NFV

PA = A, E NPA = H

3NFV

BCNFV

$\downarrow$

R<sub>11</sub>(BC)

$$B^+ = BC$$

$$C^+ = C$$

$B \rightarrow C$

CK = B

BCNFV

R<sub>12</sub>(ADB)

$$A^+ = ABD$$

$$B^+ = B$$

$A \rightarrow BD$

CK = A

BCNFV

Lossless

F1 U F2 U F3 = { $B \rightarrow C, A \rightarrow BD, E \rightarrow FG_1, AE \rightarrow H$ } Totally Preserved

$$A^+ = ABDC \quad B^+ = BC \quad E^+ = EFG_1 \quad AE^+ = AEHFG_1BD$$

Problem → ER Diagram → Relational Model → Normalization → Hashing / Indexing  
→ storing, retrieving, modifying data

Page No.

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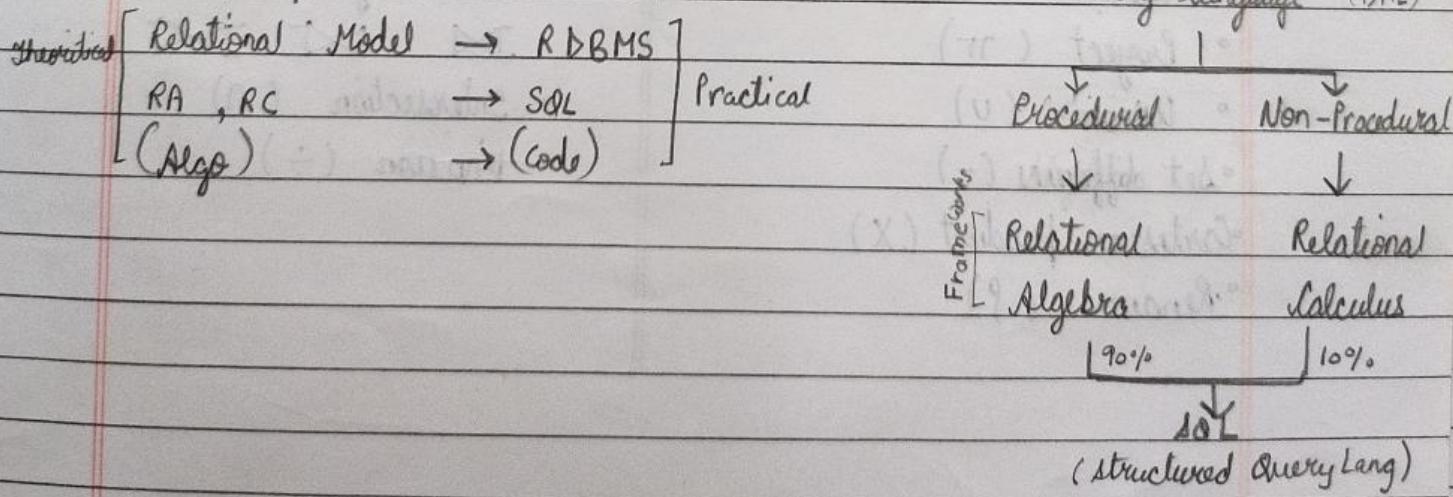
## Query Languages DML

languages used to retrieve, store or modify the data stored in DBMS

Types:

- 1) Procedural: While using procedural languages, user instruct the system to perform a sequence of operations in order to produce desired result.
  - User tells what data is to be retrieved & how to be retrieved.
- 2) Non-procedural: Here user describe the desired info without giving the specific procedure for obtaining that info.

Imp points:



## RELATIONAL ALGEBRA

Theoretical framework / algo

- It is a formal query language associated with relational model.
- It defines some operators & use relations (tables) as operands.
- Every operator in relational algebra takes one or two relations as input argument & generates a single relation as a result (with no name).
- RA doesn't consider duplicacy as it is based on set theory.
- In each query, we describe a step by step procedure for computing the desired result. So it is procedural.
- English keywords are not used.

### OPERATORS

#### Basic / fundamental

- Select ( $\sigma$ )
- Project ( $\pi$ )
- Union ( $\cup$ )
- Set difference (-)
- Cartesian product ( $\times$ )
- Rename ( $\rho$ )

#### Derived

- Natural join ( $\bowtie$ )
- $\bowtie$ ,  $\bowtie\Gamma$ ,  $\bowtie\Delta$
- Intersection ( $\cap$ )
- Division ( $\div$ )

Branch	Account	Depositor	Customer	Borrower	Loan
Branch-name	Account-no.	Customer-name	Last-name	Last-name	Loan-no.
Branch-city	Branch-name	Account-no.	Cust-street	Loan-no.	branch-name
Assets	Balance		Cust-city		amount

*relational* :  $>$ ,  $<$ ,  $=$ ,  $\geq$ ,  $\leq$ ,  $\neq$

Logical :  $\wedge$ ,  $\vee$ ,  $\neg$  (calculus)  
and or not (algebra)

Select (-) horizontal partitioning

It is a fundamental unary operator which is used to find tuples (rows) in a relation based on some conditions

Syntax :  $\sigma_{\text{predicate}}^{\text{condition}}$  (table name)

- works same as 'where' clause in SQL
  - Min no. of tuples selected = 0
  - Max no. of tuples selected = all

S_Id	Name	Branch
1	A	CS
2	B	ME
3	C	CS
4	D	CS
5	E	EE
6	F	EC
7	G	EE

Examples :  $\sigma_{\text{sid}} \leq 7$  (Student) all

o Branch - 'Civil' ( Student ) o

Examples:

- Find the details of accounts having balance  $\geq 10,000$ ?  
 ↗ Balance  $\geq 10,000$  (Account)
- Find details of the customers who live in Delhi  
 ↗ cust-city = 'Delhi' (Customer)
- Find the details of those loans having amount  $\leq 5000$  & from north-delhi branch  
v can change order ↗ amount  $\leq 5000$  (↗ Branch-name = 'North-Delhi' (loan))  
 (Nested query)
- or  
 ↗ amount  $\leq 5000$  and Branch-name = 'North-Delhi' (loan)
- Find those branch details which are in Delhi or have assets more than 10,00,000  
 ↗ Branch-city = 'Delhi' ↗ Assets  $> 10,00,000$  (Branch)

## Project ( $\Pi$ )

It is a fundamental unary operator used to select desired columns of a relation

Syntax :  $\Pi_{\text{Column\_name}}$  (table name)

- works same as 'select' clause in SQL

Examples :  $\Pi_{\text{name}}$  (Student)

→ all Branch name of the bank

$\Pi_{\text{Branch\_name}}$  (Branch)

→ Find all the account\_no. along with their balance

$\Pi_{\text{accountno., Balance}}$  (Account)

→ Find the name of all the customer who have loan

$\Pi_{\text{Cust\_name}}$  (Borrower)

→ Find all the details about branch

(branch)

Select & project combined

Select → Project

→ Find the names of all students from CS branch

$\Pi \text{ name} (\sigma \text{ Branch} = 'CS' \text{ student})$

→ Find their account no. where balance is less than 1000

$\Pi \text{ account-no} (\sigma \text{ balance} < 1000 \text{ student})$

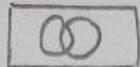
→ Find those loan no. which are from CP branch with amount > 1000

$\Pi \text{ loan-no.} (\sigma \text{ branch-name} = 'CP', \text{ amount} > 1000 \text{ loan})$

→ Find branch name and branch-city with assets more than 100000

$\Pi \text{ branch-name, branch-city} (\sigma \text{ Assets} > 100000 \text{ Branch})$

$$A \cap B = A - (A - B)$$



Page No. \_\_\_\_\_

Date \_\_\_\_\_

- R & S  
must have same  
attributes  
• duplicates  
eliminated

$\cup$  vs  $\cap$  vs  $\setminus$   
Union / Intersection and set difference  
(only on compatible tables)

Binary operators

→ Find the name of customers who have loan or amount or both.  
→ If both  
→ only account

$$\pi_{\text{cust\_name}} (\text{depositor}) \cup \pi_{\text{cust\_name}} (\text{borrower})$$

→ Find the name of a branch who have amount but not loan?

$$\pi_{\text{branch\_name}} (\text{Account}) - \pi_{\text{branch\_name}} (\text{loan})$$

→ Find the name of a customer who neither have a loan nor an account

$$\pi_{\text{cust\_name}} (\text{Customer}) - (\pi_{\text{cust\_name}} (\text{Account depositor}) \setminus \pi_{\text{cust\_name}} (\text{Borrower}))$$

Demerit  
Unnecessary/  
redundant/  
surplus  
tuples

coz order of columns doesn't matter

Commutative in DBMS | Also associative

Cartesian Product (X) tables may not contain common attr.

It is a fundamental binary operator used to combine two tables

$R_1$

Rows  $\rightarrow |R_1| = m \quad |R_2| = n \quad |R_1 \times R_2| = mn$

columns  $\rightarrow R_1(1, 2, \dots, n), R_2(1, 2, \dots, m)$

$R_1 \times R_2(1, 2, \dots, m+n)$

		R <sub>2</sub>		
A	B	C	D	F
1	a	c	d	f
2	b	p	l01	y
3	c	q	l02	z

$R_1 \times R_2$

A	B	C	D	F
1	a	p	l01	y
1	a	q	l02	z
2	b	p	l01	y
2	b	q	l02	z
3	c	p	l01	y
3	c	q	l02	z

Example :

$\rightarrow$  Find customer name having account balance < 100

$\Pi_{\text{cust\_name}} (\sigma_{\substack{\text{Account\_Ano} = \text{Depositor\_Ano} \\ \uparrow \text{balance} < 100}} (\text{Account} \times \text{Depositor}))$

$\rightarrow$  Find those account no. which are in Delhi

$\Pi_{\text{Account\_no.}} (\sigma_{\substack{\text{Account\_Branch\_name} = \text{Branch\_Branch\_name} \\ \text{and } \text{Branch\_city} = \text{'Delhi}'}} (\text{Branch} \times \text{Account}))$

$\rightarrow$  Find those customer names who have a loan from a branch having assets more than 10,00,000

$\Pi_{\text{cust\_name}} (\sigma_{\substack{\text{assets} > 1000000 \\ \text{and } \text{Branch\_Branch\_name} = \text{loan\_branch\_name} \\ \text{and } \text{loan\_loan\_no.} = \text{borrower\_loan\_no.}}} (\text{Branch} \times \text{Borrower} \times \text{loan}))$

2 tables combined - 2 conditions to remove redundancy  
3 tables — — —

## Rename ( $\rho$ )

used to rename a relation

example :  $\rho(A, B)$

(it will rename relation A to B)

Joins = cartesian product + selection condition

Joins are used to combine relations based on some conditions.

Two tuples from the relations, on which join is applied, pairs only if given condition satisfies.

Types :

Theta Join ( $\Delta_\theta$ )

Combines tuples from diff. relations only if given theta condition is satisfied.

Syntax :  $R_1 \Delta_\theta R_2$

eg : Student  $\Delta_{\text{Student.Std} = \text{Subject.Class}}$  Subject

SID	Name	Std		Class	Subject		SID	Name	Std	Class	Subject
101	A	10		10	Math		101	A	10	10	Math
102	B	11		10	Music		101	A	10	10	Music
				11	Music		102	B	11	11	Music
				11	Sports		102	B	11	11	Sports

Student

Subject

## 2) Equijoin ( $\bowtie$ condition)

It then combines tuples from diff relations based on some equality condition.

## 3) Natural Join ( $\bowtie$ )

Joins tuples from diff relations only if common attributes have equal values.

- Works only if two relations have atleast one common attribute with same name & domain.

Syntax :  $R_1 \bowtie R_2$

## 4) Outer Joins

Includes all the tuples from the participating relations.

### i) Left Join ( $\bowtie L$ )

All the tuples from left relation are included. If right relation doesn't have matching tuple, NULL is displayed.

Syntax :  $R \bowtie L S$

### ii) Right Join ( $\bowtie R$ )

All tuples from right relation are included. If left relation doesn't have matching tuple, NULL is displayed.

Syntax :  $R \bowtie R S$

### iii) Full outer join ( $\bowtie F$ )

All the tuples from both the relations are displayed. If matching tuples are not found in any of the relation, NULL is displayed.

Syntax :  $R \bowtie F S$

~~blocks - many lots  
records - 1000 - 500  
Data~~

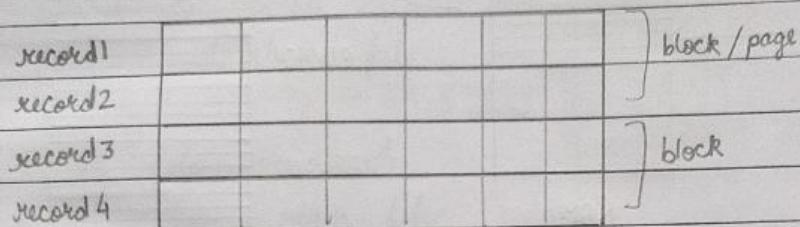
(secondary storage)

- Contiguous
  - Indexed
  - Linked

## File Structures

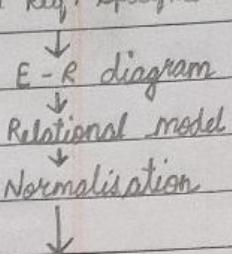
(data structure - very flexible)

(set of records)



# SRS

(Software Req. Specification)



## File Structure

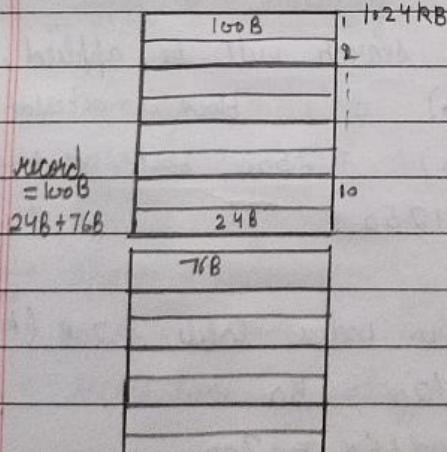
orientation : sorted file

- Can be sorted only according to one attribute  
(Search key)
  - Searching will be fast
  - Insertion & deletion will be difficult

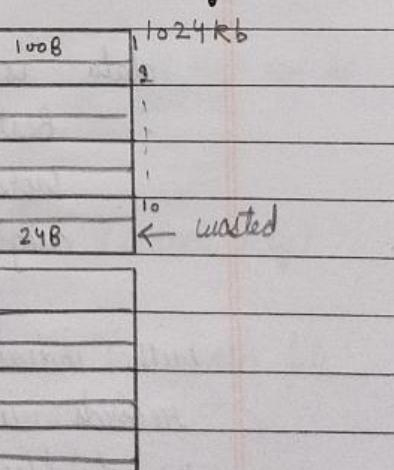
## unsorted file

- Random order, any record can be placed anywhere
  - Set searching will be slow
  - Insertion and deletion will be easy

## Spanned mapping



## unspanned mapping



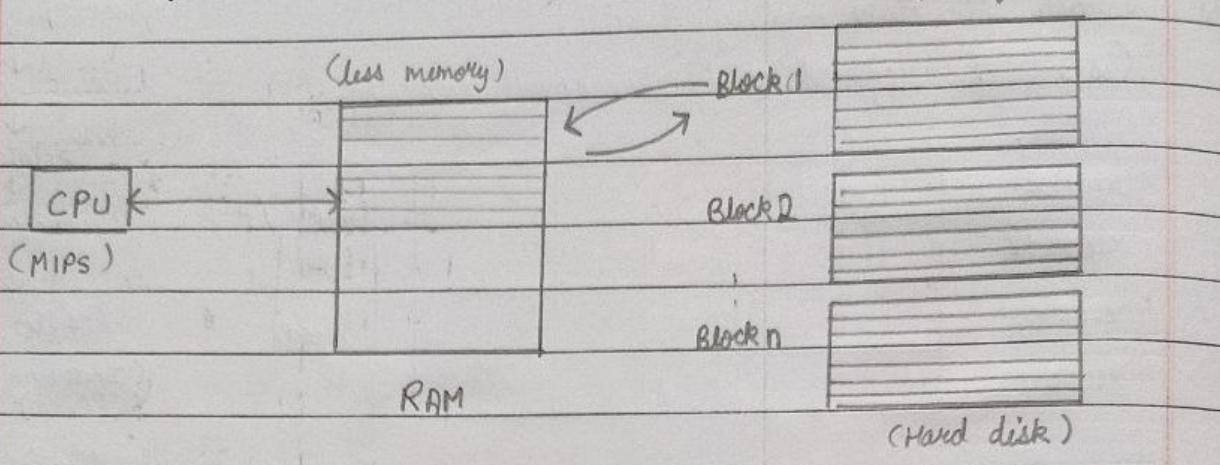
- File undergoes internal fragmentation & stored in next multiple blocks in case previous block is full.
  - efficient storage but search time ↑ (2 blocks need to be searched)

- File is stored in next block

No internal fragmentation

  - not efficient in case of storage  
but search is fast

→ accessing records from a file



When a record needs to be searched, complete blocks are transferred to RAM one by one & searched. Cost req. for the process - I/O cost

eg: A hard disk has block size = 1000 B, each record size = 250B  
 If total records = 10,000 & file is unsorted. What is avg TC?  
 no. of records we can put in a block =  $1000 / 250 = 4$   
 no. of blocks required to store 10,000 records =  $\frac{10,000}{4} = 2500$

Data is unsorted, linear search will be applied,

∴ Best case  $TC = O(1) = 1$  block is accessed

Worst case  $TC = O(n) = 2500$  blocks are accessed

$$\text{avg case} = \frac{2500}{2} = 1250$$

With indexing (Record size in index table = 20B (key + 16B))

$$\text{Records in a block} = \frac{1000}{20} = 50$$

$$\text{no. of blocks required} = \frac{10,000}{50} = 200$$

$$\text{no. of blocks accessed} = 1 + \log_2 200 \approx 1 + 8 = 9$$

block search time  $>>$  record search time  
 (negligible)  
 Index file must be sorted.

Page No.

Data

even binary search takes time  
 in case of large files

Main File

## INDEXING (optional)

It is a technique which allows to access records from a database file

quickly by maintaining idx files of memory blocks

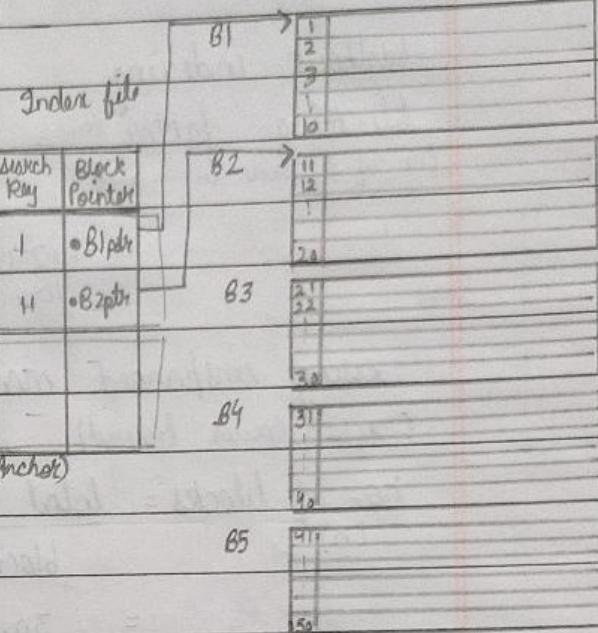
Index files are much smaller than main files

$\therefore$  access time  $\downarrow$

- no. of blocks of index files are less

bcz record size  $\downarrow$  as well as no. of records dec (except rec.)

- search is always applied on blocks



size of index file is small

- dense index - unsorted file, each ~~rec~~ <sup>value</sup> in ind file

- sparse index - sorted file, few rec. in ind file (eg 1 rec from a block)

## Types of Indexing

exact block can be searched.

### 1) Primary Indexing

above eg

- When main file is sorted (acc. to PK)
  - Primary key is used as anchor attribute (search key)
  - sparse indexing
  - no of records in index file = no. of blocks in main file
  - access time =  $\log_2 n + 1$  (binary search)
- n = no. of blocks in index file

2<sup>n</sup>  
 blocks  
 automatically  
 made  
 when u  
 make  
 PK

block size is hardware property  
record size is decided by the user

Page No.  
Date  
one record  $\rightarrow$  1 block

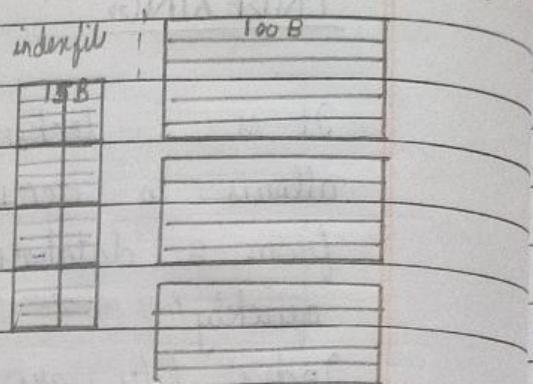
Total block size = 1024B

### Numerical

without indexing

$$\text{blocking factor} = \frac{\text{Total block size}}{\text{Record size}}$$

$$= \frac{1024}{100} = 10.24 \approx 11$$



using unspanned mapping = 10 records  
(use lower bound)



$$\text{no. of blocks} = \frac{\text{total no. of records}}{\text{blocking factor}}$$

$$= \frac{30,000}{10} = 3000 \text{ blocks}$$

[always takes upper bound]

primary  
(sorted)  
 $\therefore$  binary search

$$\text{access time} = O(\log_2 n)$$

$$= \log_2 3000 \approx 11 \dots \approx 12 \text{ units}$$

with indexing

$$\text{blocking factor} = \frac{\text{total block size}}{\text{Record size}} = \frac{1024}{15} = 68$$

more records

(lower bound)

$$\text{no. of blocks} = \frac{\text{total no. of records in index fil}}{\text{blocking factor}}$$

primary  $\xrightarrow{fn}$  ordered  $\Rightarrow$  sparse  
 $\therefore$  1 record for each block

$$= \frac{\text{total no. of blocks in main file (n)}}{\text{blocking factor}}$$

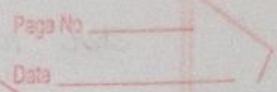
$$= \frac{3000}{68} = 45 \leftarrow \text{block reduced to much extent}$$

index fil  
(always sorted)  
 $\therefore$  binary search

$$\text{access time} = \log_2 45 + 1 = 5.5 + 1 \approx 6 + 1 \approx 7$$

Hence, access time decreased using primary indexing

Binary / Cluster index - atleast 1



many record  $\rightarrow$  1 block  
exact block can't be searched

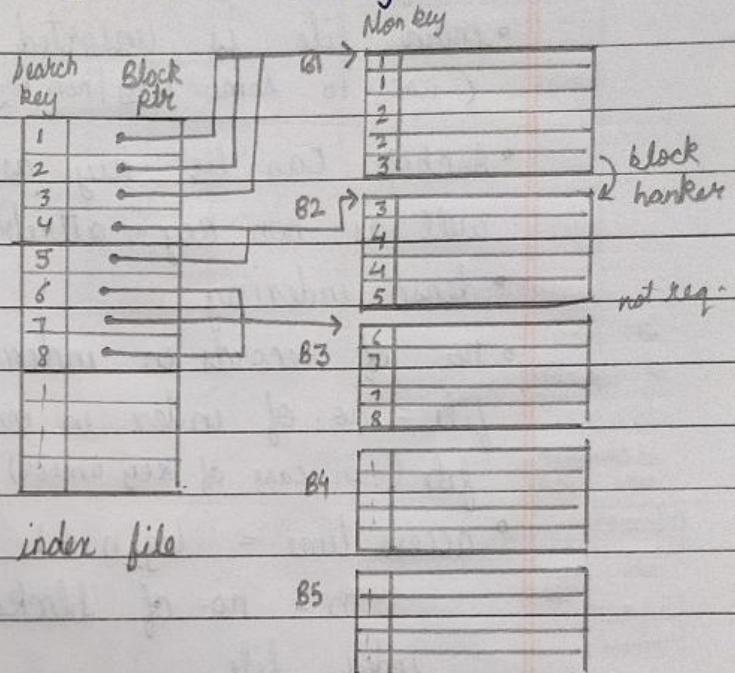
### 2) Clustering index

- when main file is sorted (acc. to non key attribute)
- there will be one record for each unique value of non-key attribute
- sparse (as well as dense)
- Non key attribute is used as anchor attribute
- access time  $\geq \log_2 n + 1$

= if  
1 block  
multiple  
blocks.

$n = \text{no. of blocks in}$   
index file

block hanker is used



Main file

there may be multiple index files for a main file

a file can be sorted acc to one attr. but unsorted acc. to another

Page No \_\_\_\_\_  
Date \_\_\_\_\_

many records  $\rightarrow$  1 block

exact block is searched

### 3) Secondary Index

mostly primary indexing is done

- main file is unsorted  
(acc. to some key/non key attr.)

- Anchor can be key as well as non key attribute.

- dense indexing

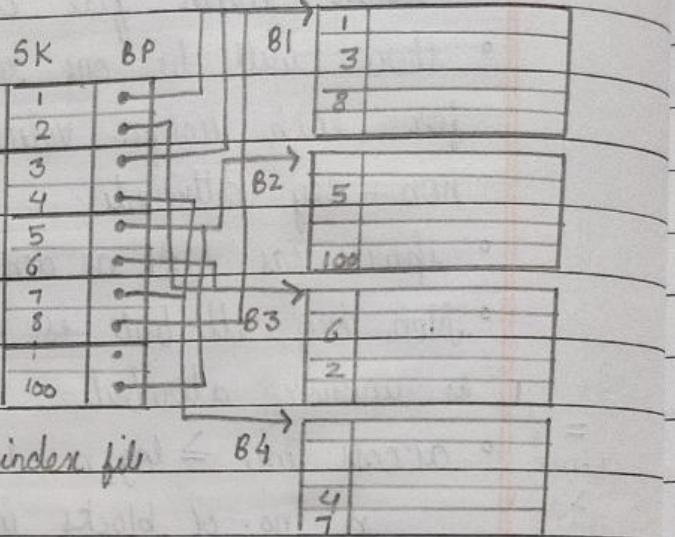
- no. of records in index

In case  
of non-key  
various  
techniques  
are used

file = no. of index in main file (in case of key anchor)

- access time =  $\log_2 n + 1$

n = no. of blocks in index file.



main file

no of pointers to a block in  
main file = no of records in it.



→ without secondary indexing :

$$\text{blocking factor} = \frac{1024}{100} = 10$$

no. of blocks for main file ( $n$ ) =

$$\text{total records} = 30,000$$

$$\text{blocking factor} = \frac{3000}{10} = 300$$

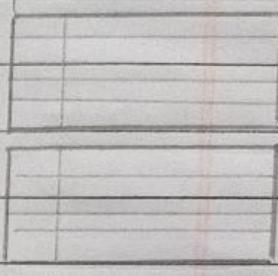
Index file

SK BP

15B.

Main file

100 MB



30000 records

total block size = 1024B

with secondary indexing :

$$\text{blocking factor} = \frac{1024}{15} = 68$$

no. of blocks for index file = total records in index file

blocking factor

= total records in main file

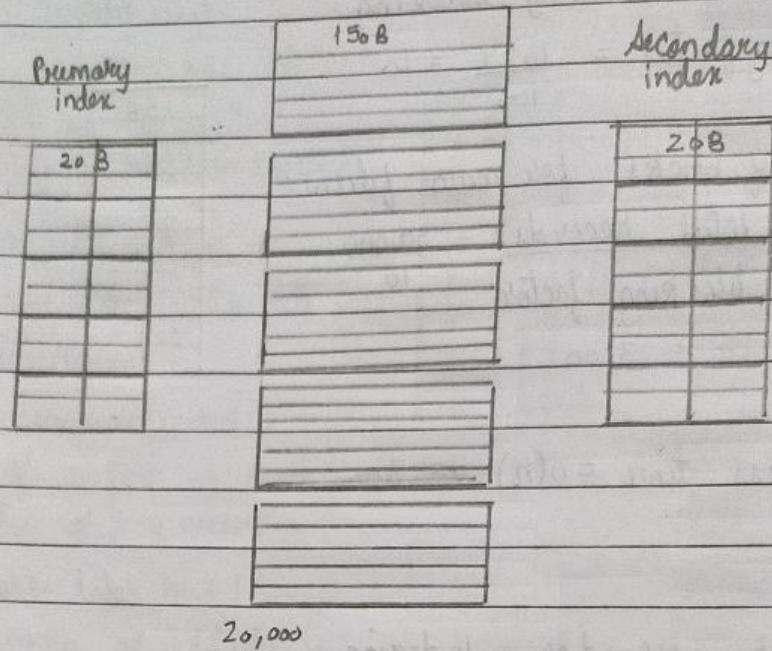
blocking factor

$$= 30000 / 68 = 442$$

$$\text{access time} = \log_2 442 \approx 9 + 1 \approx 10$$

index file  
sorted  
binary search

Block size = 2048 B



$$\text{Blocking factor} = \frac{2048}{150} \approx 13$$

$$\text{no. of blocks} = \frac{20,000}{13} = 1538.4 \approx 1539$$

In case of sorted file, access time =  $O(\log_2 n)$

$$\log_2 1539 \approx 11$$

In case of unsorted file, access time =  $O(n)$

$$\approx 1539$$

Primary indexing :

$$\text{deblocking factor} = \frac{2048}{20} = 102.8 \approx 102$$

$$\text{no. of blocks} = \frac{1539}{102} = 15. - \approx 16$$

$$\text{access time} = \log_2 16 + 1 = 4 + 1 = 5$$

Secondary indexing :

$$\text{blocking factor (sec. index file)} \approx 102$$

$$\text{no. of blocks} = \frac{20,000}{102} \approx 196. - \approx 197$$

$$\text{access time} = \log_2 197 + 1 = 7. - + 1 \approx 8 + 1 \approx 9$$

sparse → dense      sparse ← sparse

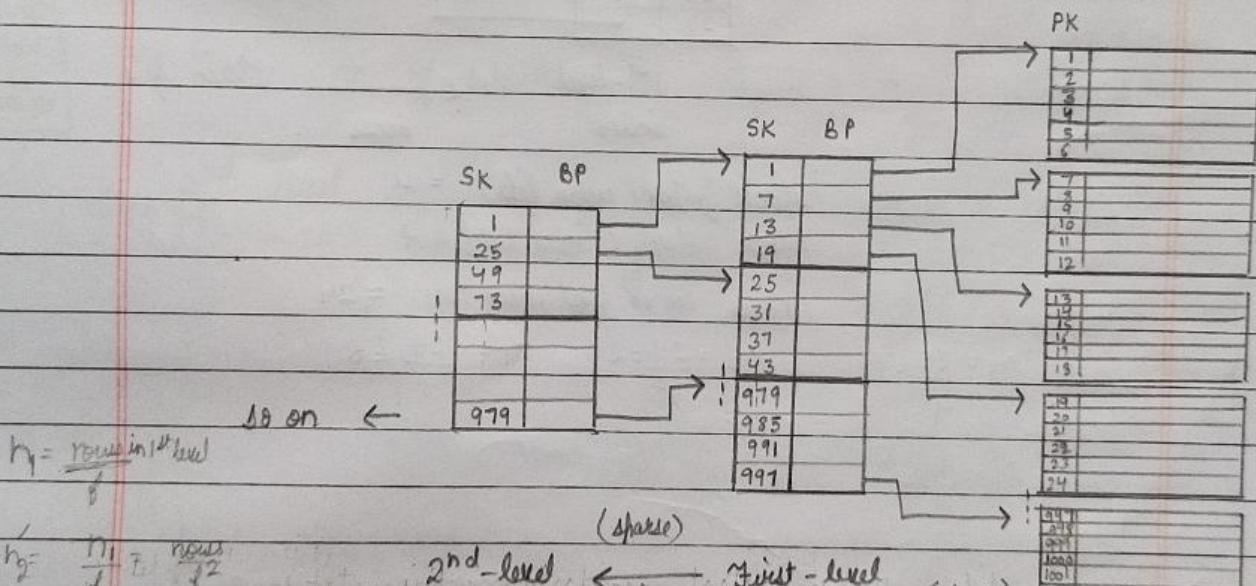
Page No.

Date

## Multilevel Indexing

(index of index)

- It is a technique in which index (first-level) is broken down into further smaller indices in order to make outer most level small enough to fit in a single block.
- ~~access~~ time complexity ↓
- It can be created for any type of first-level index (primary, sec or clustering) as long as the first-level index consists of more than one disk block.
- A third level index is required only if 2<sup>nd</sup> needs more than 1 block.
- Last level index → top index level (root)



$$h_1 = \frac{n_1}{f} = \frac{\text{rows}}{f^2}$$

$$n_2 = n_1 = \frac{\text{rows}}{f^2}$$

$$\therefore n_2 = \frac{\text{rows in 1st level}(h_1)}{f^2}$$

$f^2$  should be 1

2<sup>nd</sup>-level  
index

(sparse)

First-level  
index

primary  
indexing  
(always)

(sparse)

Main file

primary  
indexing

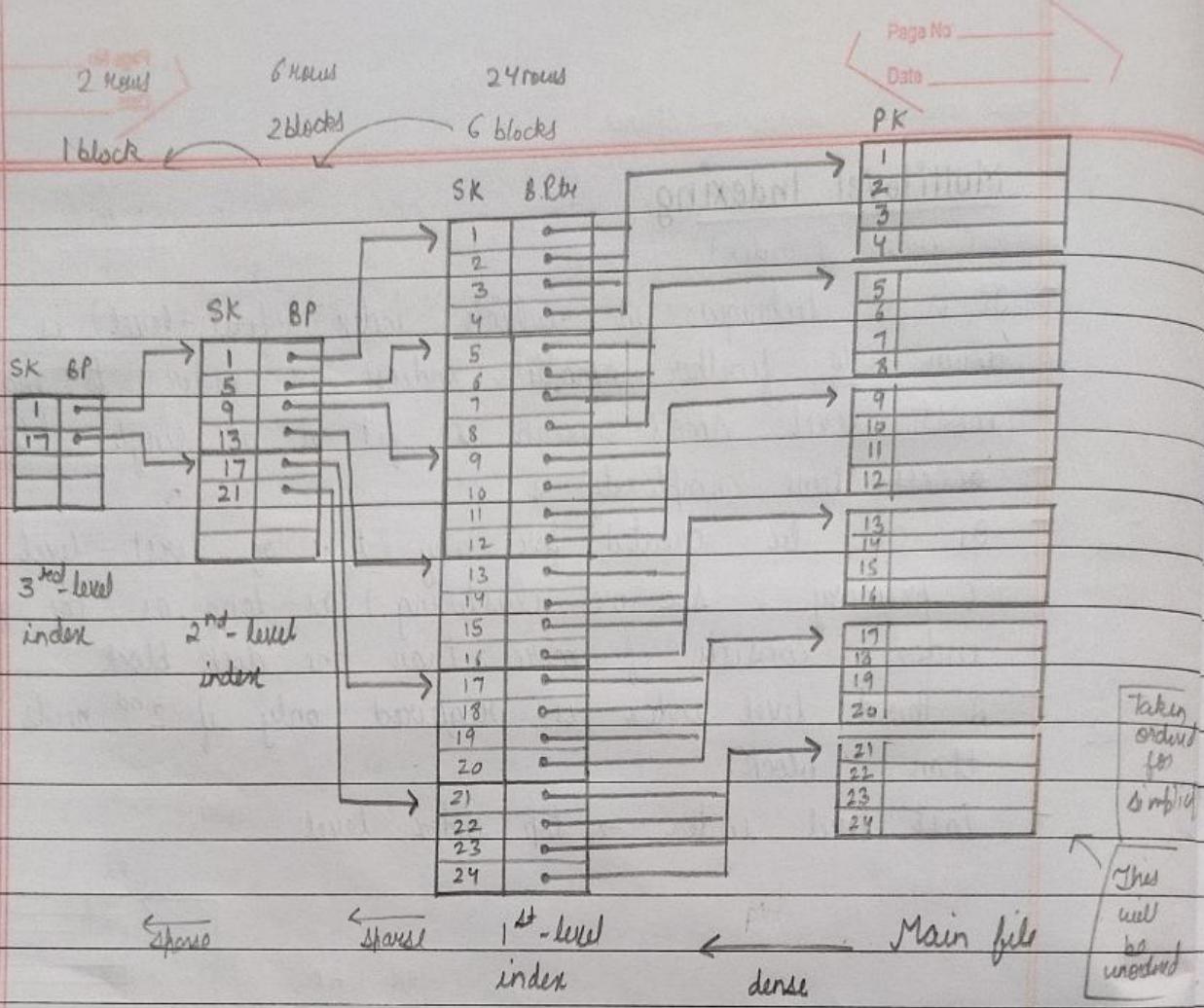
(can be sec/clust.)

- Multi-level indices of first-level index file is always primary bcz index file is always sorted and search key is unique.

$f^2 = h_1$  — Let index blocking factor =  $f_0$ , then each time no. of blocks reduce by a factor  $f_0$ .

$$\text{no. of blocks at } t^{\text{th}} \text{ level} = n_t = \frac{\text{rows in 1st level}(h_1)}{f_0^t}$$

$$n_t \text{ should be 1} \therefore t = \frac{h_1}{(f_0)^t} \Rightarrow t = \log_{f_0}(h_1) \quad f_0^t \quad \text{Block access} = t + 1$$



Block factor (main file) = 4

Block factor (index file)  $b_0 = 4$  (Assume not possible practically)

rows in 1<sup>st</sup> level index ( $n_1$ ) = 24

make  
upper  
write

$$n_3 = \frac{24}{4^3} = 1 \quad n_2 = \frac{24}{4^2} = 2 \quad n_1 = \frac{24}{4} = 6$$

$$t = \log_4 24 = 3 \quad (\text{upper limit})$$

→ main file rows = 30,000, row size = 100B

Block size = 1024 bytes

We constructed a secondary index on a non ordering key field of the file that is key = 9B, ptr = 6B

Levels = ? index block size  $b_0 = 1024 / (6+6) = 1024 / 12 = 84$

Record.  $t = n_1 = 30000$  (sec. on key attr. → dense)

$$\therefore t = \log_{84} 30000 = 3 \text{ levels.}$$

or block access =  $t + 1 = 4$

1<sup>st</sup> level rows = 30000, block factor  $i_1 = 68$   $n_1 = \frac{30000}{68} = 442$

2<sup>nd</sup> level rows = 442, block factor  $i_2 = 68$   $n_2 = 442 / 68 = 7$

3<sup>rd</sup> level rows = 7, block factor  $i_3 = 68$   $n_3 = 7 / 68 = 1$

→ Consider a file of 16384 records. Each record is 32B & key field is 6B. The file is ordered on a non-key field and the file organization is unsparsed. The file is stored in a file system with block size 1024B & size of block pointer is 10B

If sec. index is built on the key field of the file & a multi-level index is used to store the sec. index, the no. of first level & 2<sup>nd</sup> level blocks are —, —?

1<sup>st</sup> level : no. of records  $x_1 = 16384$

(dense) index block factor  $f_0 = \frac{1024}{10+6} = \frac{1024}{16} = 2^{10}$   
 $= 2^6 = 64$

no. of blocks  $n_1 = \frac{16384}{64} = 256$  blocks

2<sup>nd</sup> level : no. of records  $x_2 = 256$

(sparse) index block factor  $f_0 = 64$

no. of blocks  $n_2 = \frac{256}{64} = \frac{2^8}{2^6} = 2^2 = 4$  blocks

→ Block size = 1024 index = 16B Records = 100000

record size = 100B

Suppose we convert sparse index into multi-level index then which level will be top level of multi-level index

rows in 1<sup>st</sup> level = ~~100000~~ blocks in main file  
 (sparse) ( $n_1$ ) =  $\frac{100,000}{100} = \frac{100000}{10} = 10,000$

index block size  $f_0 = \frac{1024}{16} = 64$

$t = \log_{64} 10000 = 3$

3<sup>rd</sup> level is the top level.

## Balanced Search Trees

AVL Tree

Red Black Tree

Splay Tree

B-Tree

B+ Tree

Trie

Treap

Segment Tree

Interval Tree

## TRANSACTION

Transaction is an independent unit of work (set of instructions) performed by DBMS against a database.

A transaction usually changes the state of database.

ACID Properties These properties must be followed by a transaction

- **Atomicity**: It ensures that either the entire transaction takes place at once or doesn't happen at all.
  - It should work as an atomic unit & must not occur partially
  - It is managed by 'transaction management component' of DBMS

any uncommitted transaction will be aborted after some time automatically

eg :

$X = 500$ Read (X) $X = X - 100$ write (X) $X = 400$	$Y = 200$ Read (Y) $Y = Y + 100$ write (Y) $Y = 300$
$X + Y \text{ (before transaction)} = X + Y \text{ (after transaction)}$ $500 + 200 = 400 + 300$	

- **Consistency**: If database was consistent before transaction, it must be consistent after the transaction
  - It ensures the correctness of database.
  - In the above example, the total amount before and after the transaction is constant ∴ it is consistent
  - All the constraints should be maintained

- Isolation Transactions must occur in isolation concurrently without leading to the inconsistency of DB.
- The intermediate states of must be invisible to other transactions.
- It is managed by 'concurrency control component' of DBMS

eg:  $x = y = 500$

T	R(x) $x = x * 100$ w(x) R(y) $y = y - 50$ w(y)	T'	R(x) R(y) $z = x + y$ w(z)
---	---	----	-------------------------------------

If T' reads x,y from intermediate state of T, where x is updated but y is still not updated, it will lead to inconsistency

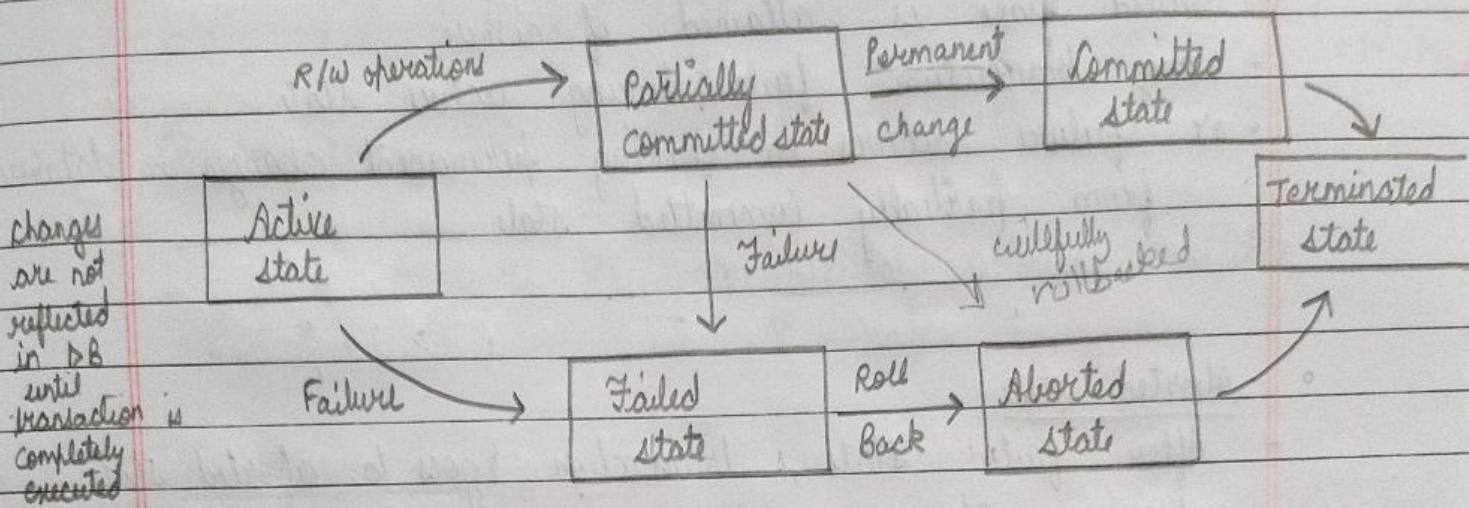
- Durability : It ensures that once the transaction has been completed, the updates & modifications in the database must persist even if a system failure occurs.
    - Changes must be made permanent.
    - Maintained by 'recovery management component' of DBMS
- failures : comp. failure, transaction error, disk failure, power failure

### Operations:

- Read (A) Reads value of A from database and stores it in buffer in main memory.
- Write (A) writes the value of A into the buffer
- Commit After all instructions are executed, changes are made permanent in database.
- Rollback If transaction doesn't execute completely, all changes made by it (in buffer) are undone. (database remains unchanged)

## Transaction States

$$DB \xrightarrow{T} DB' : T \rightarrow \boxed{\text{only}}$$



- Active state:

- This state begins at the execution of first read/write instruction and ends at the last one
- If all the instructions are performed without any error, it goes to 'partially committed stat', if any instruction fails, it goes to 'failed stat'.

- Partially committed state:

- After completion of all the read/write operations, changes are made in local buffer (main memory).
- If changes are made permanent, it goes to committed stat else, it goes to failed stat.

- Committed state:

This stat is attained when changes are made permanent in the database after the complet execution of transaction

- Failed state:
  - Failed state is attained if either
    - any transaction fails during active stat.
    - or failure occurs in making permanent changes in database from partially committed stat.
  
- Aborted state
  - After failed stat, transaction goes to aborted stat wherein changes which are made in local buffer are deleted or roll back and database remains in the actual stat.
  
- Terminated stat deallocation of resources
  - After committed Terminated stat is attained if,
    - changes are made permanent in database (from committed)
    - changes are roll back & database remains same (from aborted)

Advantages of Concurrency multiple transaction run parallelly

- waiting time ↓
- response time ↓
- resource utilization efficient
- efficiency ↑

Disadv.

- complex management
- may lead to inconsistency

## Dirty read problem

## Concurrency

It is a property of DBMS which allows multiple transactions to execute simultaneously.

### Advantages :

- Improved throughput : no. of transactions that can be executed in a given amount of time is called as throughput. When multiple transactions execute simultaneously , throughput inc.
- Efficient resource utilisation : Various system resources like disks and CPU are utilised concurrently . When a transaction is using CPU , other can use disk to fetch data
- Reduced waiting time : In serial execution of transactions , waiting time for the transactions present in queue is more But for concurrent execution waiting time is reduced .

- Main conflicts
- WR
  - RW
  - WW

Page No.

Date

## Problems (due to concurrency)

When only read operations are performed, concurrency works well. But a transaction involves both read and write operations.

∴ When multiple transactions execute concurrently in an uncontrolled manner, it leads to several problems:

- Temporary update / Dirty read problem:

T <sub>1</sub>	T <sub>2</sub>
w	r

A dirty read problem occurs when temporarily updated value of a transaction (not committed yet) is used by another transaction but the latter

former fails.  
Now the former transaction reverts back and database remains unchanged but the temporarily updated value of its intermediate state is used which creates a problem.

$X = 10$ (initially)	T <sub>1</sub>	T <sub>2</sub>
	$X = 10 \quad R(X)$	
	$X = 11 \quad X = X + 1$	
	$X = 11 \quad W(X)$	
		$R(X) \quad X = 11$
		$X = X + 2 \quad X = 13$
		$W(X) \quad X = 13$

(failure)  
rollback

Now T<sub>1</sub> is roll back ∴ no changes in database  
so on executing T<sub>2</sub>  $X = 10 + 2 = 12$   
But at the end of T<sub>2</sub>  $X = 13$  is committed

- Unrepeatable Read Problem:

T <sub>1</sub>	T <sub>2</sub>
r	
w	r

Unrepeatable problem occurs when read operations of the same transaction read different values of the same variable due to ongoing write operations in some other transaction.

values come from lower time → higher

$X = 10$	T <sub>1</sub>	T <sub>2</sub>
	$X = 10 \quad R(X)$	
	$X = 11 \quad X = X + 1$	$R(X) \quad X = 10$
	$W(X)$	
		$R(X) \quad X = 11$

$T_1$	$T_2$
$R$	$R$

### • Phantom Read problem:

Phantom read problem occurs when a transaction reads a variable once but when it tries to read that same variable again, an error occurs saying the variable doesn't exist bcz it is already deleted by some other transaction in between.

$T_1$	$T_2$
$R(x)$	$R(x)$

$T_1$	$T_2$
$\text{Delete}(x)$	$\text{Read}(x)$

### • Incorrect summary problem:

It occurs when a transaction is applying the aggregate function on some record while another transaction is updating these records.

The aggregate function may calculate some values before update while others are already updated.

$A=1$	$T_1$	$T_2$
$B=2$		
$C=3$		

$\text{sum}=1$	$R(A)$
	$\text{sum}=\text{sum}+A$

$B=3$	$R(B)$
	$B=B+1$
	$w(B)$

$\text{sum}=4$	$R(B)$
	$\text{sum}=\text{sum}+B$

$\text{sum}=7$	$R(C)$
	$\text{sum}=\text{sum}+C$

$C=4$	$R(C)$
	$C=C+1$
	$w(C)$

Here sum should be either 6 or 8

but sum = 7

### • Lost update problem:

In this problem, update done to a data item by a transaction is lost as it is overwritten by the update done by another transaction.

$X=1$	$T_1$	$T_2$
-------	-------	-------

$R(X)$
--------

$X=2$	$X=X+1$
-------	---------

$X=10$
--------

$w(X)$
--------

$X=2$  needed to be stored  
but  $X=10$  is stored

Schedule set of transactions

It is a series of operations of different transactions executing concurrently.

- If there are  $n$  transactions with  $n_1, n_2, \dots, n_n$  instructions respectively then, schedule has  $n_1 + n_2 + \dots + n_n$  instructions.
- Order of instructions of a transaction must remain the same in the schedule.

There must be only 1 instruction in 1 row.

$$\text{Total no. of schedules} = \frac{(n_1 + n_2 + n_3 + \dots + n_n)!}{n_1! n_2! \dots n_n!}$$

### Types of schedules

No concurrency  
 serial schedule: In this type of schedule, one transaction is completely executed before starting another transaction.  
 i.e. if all transactions are following ACID properties, then

- no. of schedules possible for  $n$  transactions :  $n!$

- No concurrency problems
- But inefficient

S	$T_1$	$T_2$
	R(A)	
	W(A)	
	R(B)	
	W(B)	
	R(B)	
	W(B)	
	R(A)	
	W(A)	

Non-serial schedule: In this type of schedule, operations of different transactions are interleaved.

- May lead to concurrency problems
- no. of schedules possible for  $n$

transactions with  $n_1, n_2, \dots, n_n$  instructions:

$$(n_1 + n_2 + \dots + n_n)! - n!$$

$$n_1! n_2! \dots n_n!$$

Total

serial

T <sub>1</sub>	T <sub>2</sub>
R(A)	
W(A)	
	R(B)
	W(B)
	R(A)
	W(A)

### Types of Schedules

#### Based on Serializability

- Serializable (Result equi)-check
- Conflict Serializable (Conflict equi)
- View Serializable (View equi)

#### Based on Recoverability

- Ir-Recoverable
- Recoverable
- Cascade Rollback-Recoverable
- Cascade Less Rollback-Recoverable
- Strict Recoverable

If a schedule is conflict serializable, it is consistent but vice versa is not true

Page No.

Date

## Conflict serializability

We do not swap instructions of same transaction this will change the order of transaction violates condition of schedules

- A serial schedule is always consistent
  - A <sup>non-serial</sup> schedule is said to be conflict serializable if it can be converted to make equivalent to serial schedule by swapping  $\leftrightarrow$  non-conflicting instructions
- A conflict serializable schedule is consistent

conflicting instructions:

- # Two operations are said to be conflicting if
  - they belong to different transactions
  - They operal on same data item
  - at least one of them is write operation

Changes in T		changes in Database	
R(A)		w(A)	
	w(A)		R(A)
	w(A)		R(A)
R(A)		w(A)	w(A)

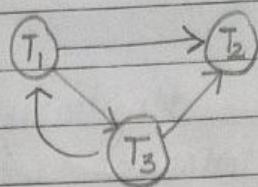
eg: $T_1$   $T_2$		$T_1$   $T_2$		Non-conf.
R(A)		R(A)		R(A)
w(A)		w(A)		w(B)
diff data items	$\rightarrow$	R(A)		R(A)
non-conflicting	(R(B))	w(A)		R(A)
			R(A)	R(A)
			w(A)	
			R(B)	
			w(B)	

We will find conflicting instructions & try to obtain a valid serial order if cycle forms X else we are not swapping here (becomes lengthy)

Page No.  
Date

### Examples

$T_1$	$T_2$	$T_3$
$R(x)$		
	$R(z)$	
		$w(z)$
	$R(y)$	
		$w(y)$
		$w(x)$
		$w(z)$
		$w(x)$



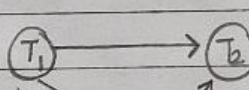
$T_1 \rightarrow T_2$   
edge depicts that  $T_1$  will execute before  $T_2$

Stop as the cycle completes - Not conflict serializable

(if cycle doesn't form & all the operations are scanned - conflict serializable)

(Total  $3! = 6$  serial schedules can be formed. Swapping the non-conflicting operations to form many of those serial schedules is diff.)

$T_1$	$T_2$	$T_3$
$R(X)$		
	$R(Y)$	
		$R(Y)$
	$w(X)$	
		$w(X)$
		$w(X)$
		$R(X)$
		$w(X)$



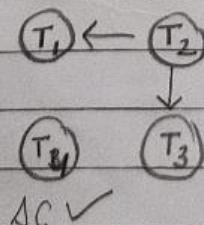
not conflict  
serializable  
order:  $T_1, T_3, T_2$

$T_1$	$T_2$	$T_3$
$R(a)$		
	$R(b)$	
		$R(c)$
		$w(c)$
		$w(b)$
		$w(a)$

$T_1, T_2$   
 $T_3$   
no edge  
all 6  
combinations  
possible  
conflict  
serializable

If  $T_1 \rightarrow T_2$  : CSV (3) combined  
 $T_3$   
If  $T_1 \rightarrow T_2 \rightarrow T_3$  CSV (1) combined  
 $T_1, T_3, T_2$   
 $T_1, T_2, T_3$   
 $T_3, T_1, T_2$

$T_1$	$T_2$	$T_3$	$T_4$
$R(X)$			
	$w(X)$		
		$C$	
		$w(X)$	
		$C$	
		$w(Y)$	
		$R(Z)$	
		$C$	
		$R(X)$	
		$R(Y)$	
		$C$	



AC ✓

$O(n^2)$