

# Child Errors as a Window into Morphological Acquisition

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# Background: Morphological Acquisition

## Children **learn inflectional morphology**

- From highly **sparse, skewed** input
- On <1000 lemmas
- Despite **exceptions**
- With complex systems of **allomorphy**

**Challenging  
problem!**

# Background: Morphological Acquisition

Children make **systematic errors** cross-linguistically

- **Overregularization:** e.g. “feel-feeled”
  - **Omissions of Marking:** e.g. “Papa have it”
- } **Almost all errors**

Why **these** errors and not others?

What do the errors tell us about:

- Acquisition?
- The resulting grammar?

} **Models of morphological acquisition should address these questions**

# Outline

**Why computational modeling?**

**What makes a good model?**

**Previous work: The Past Tense Debate**

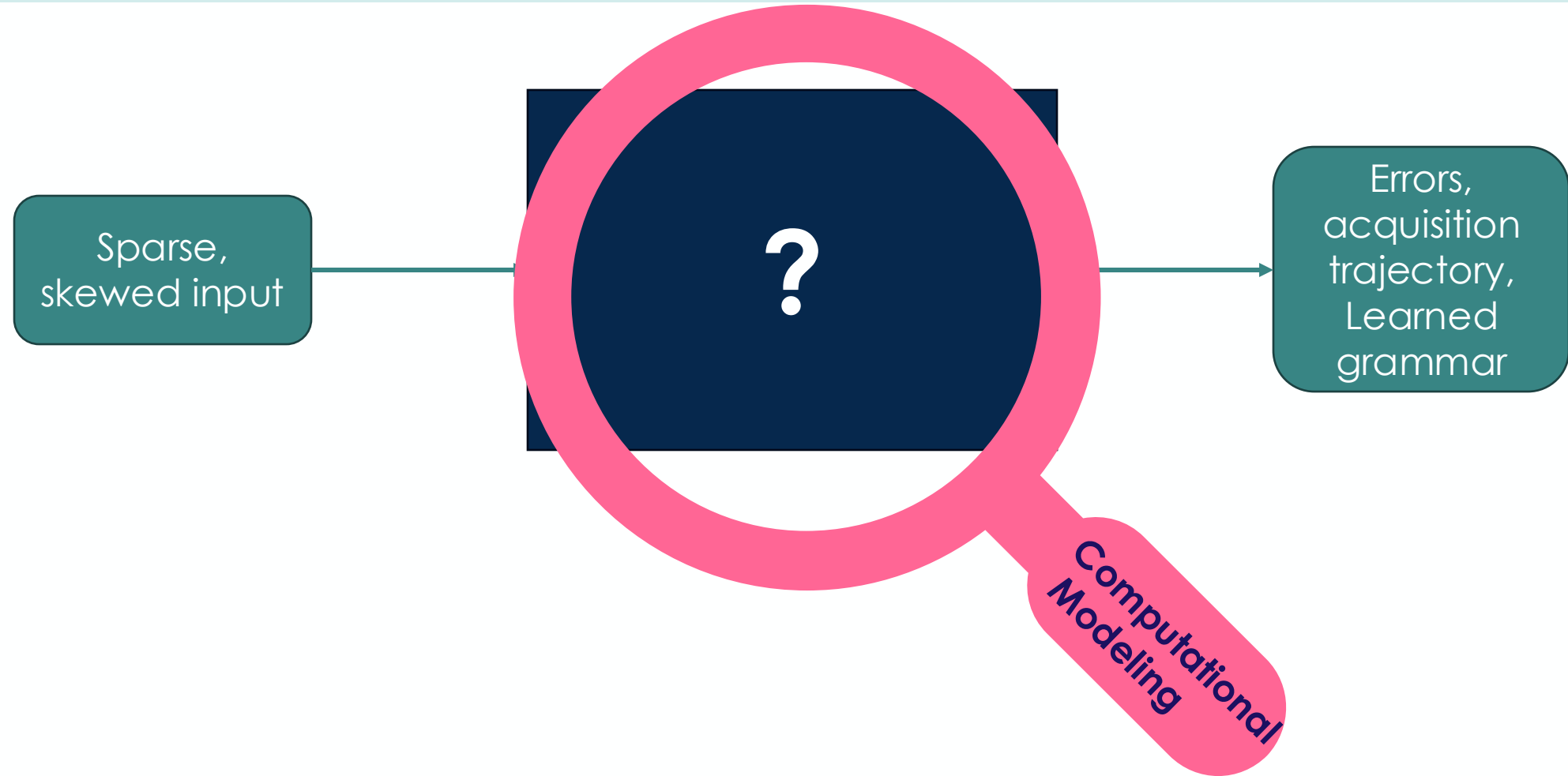
**Proposal**

- **ATP:** mapping features to form
- **SCL:** learning inflectional classes

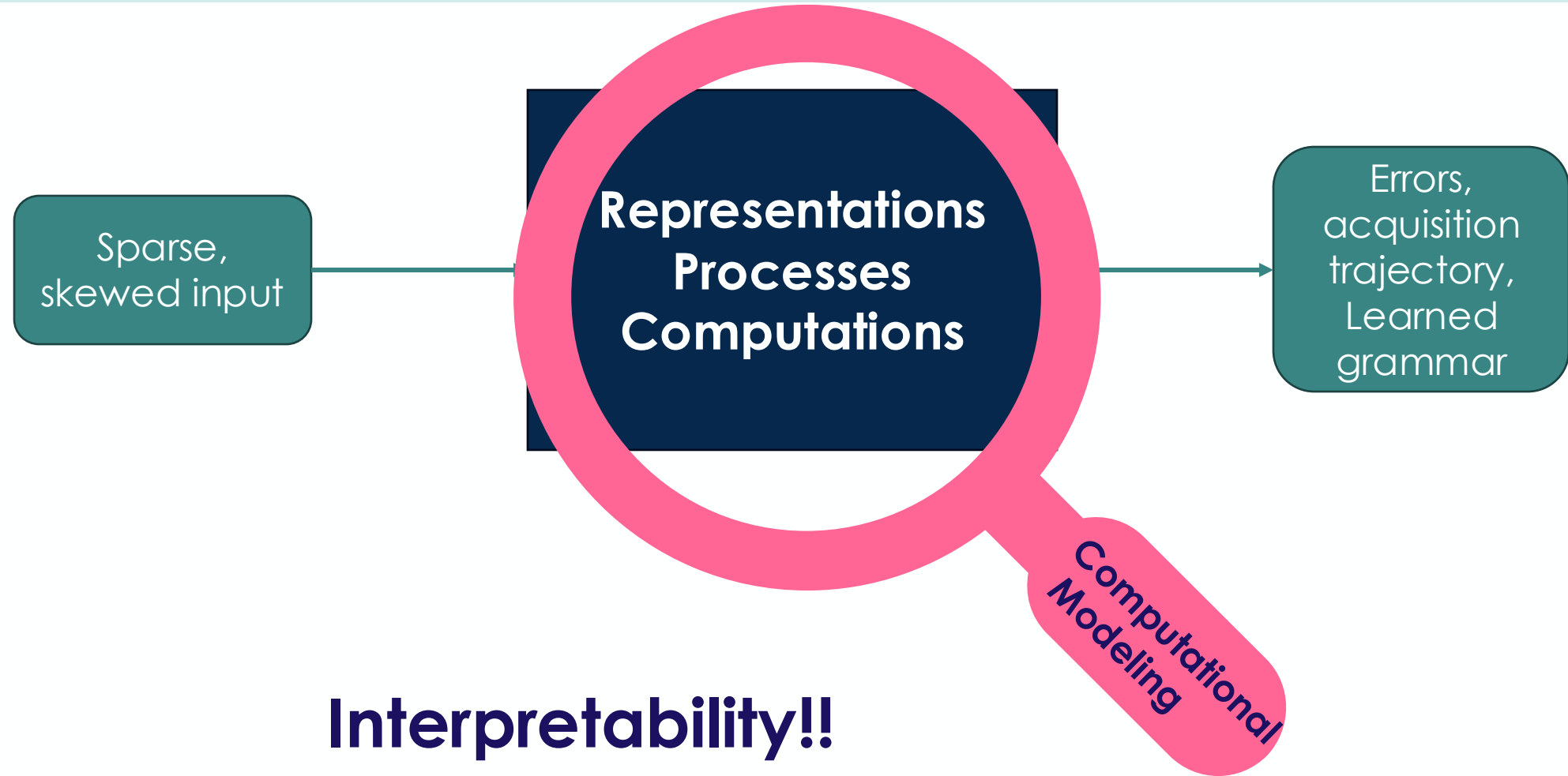
**Discussion & future work**

# Why Computational Modeling?

# A Mechanistic Account



# A Mechanistic Account



# A Mechanistic Account

## What Happens

- Sparse, skewed input
- Errors
- Acquisition trajectories

Description, not  
explanation

## Why it Happens

- What are the **mental computations** that allow the child to learn from this input?
- How do these computations yield the errors we see?
- How do they lead to the trajectories we observe?



# What Makes a Good Mechanistic Account?

# What Makes a Good Model?

## Input:

- *Small* vocabulary
- *Sparse* paradigms

## Errors:

- *Omissions*, not substitutions
- *Over-regularizations*, not over-irregularizations
- Developmental *regression*

**Interpretability:** why does it do what it does?

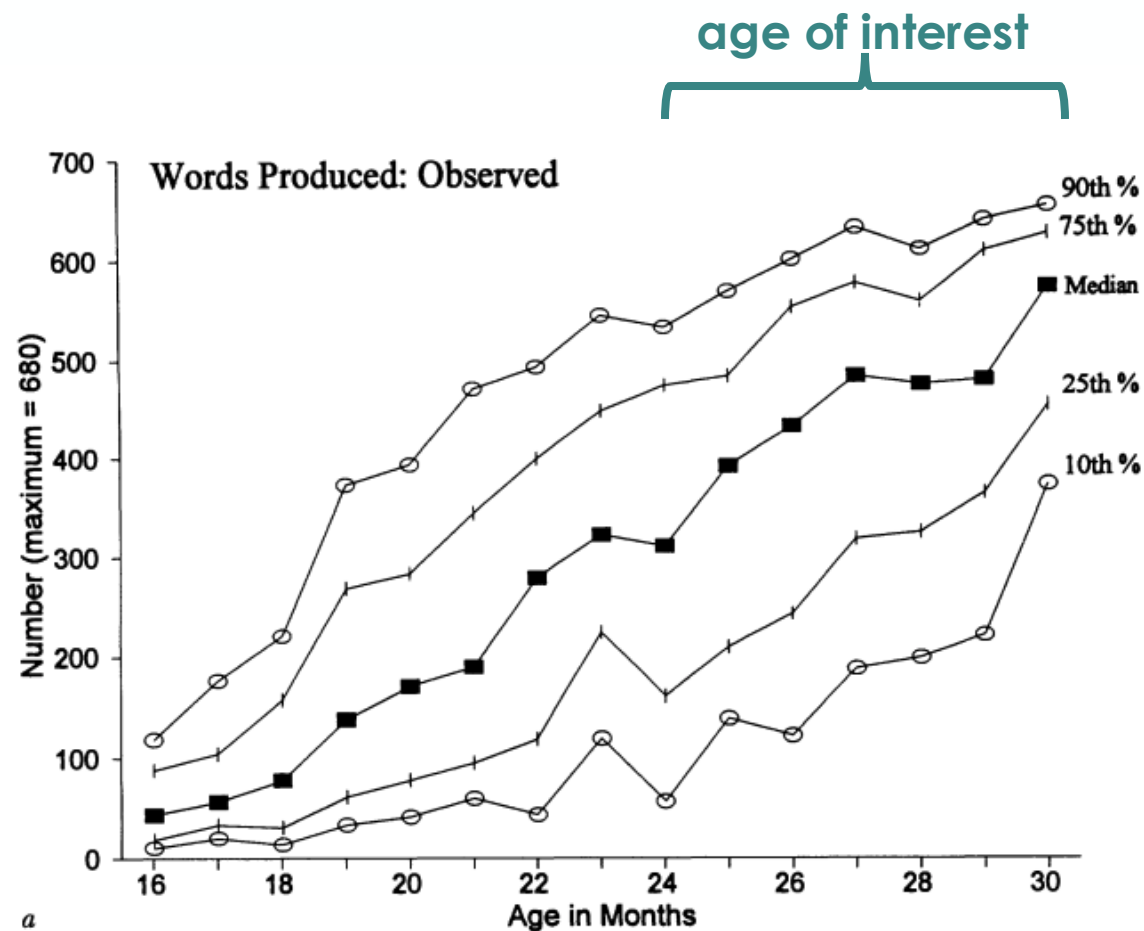
# Input Sparsity: Early Vocabulary

**At 2;0: 200-500 words** cross-linguistically

**At 3;0: <1000 words** cross-linguistically

Early vocabulary makeup:

- ~50% **nouns**
- ~25% **verbs**



(from Fenson et al 1994)

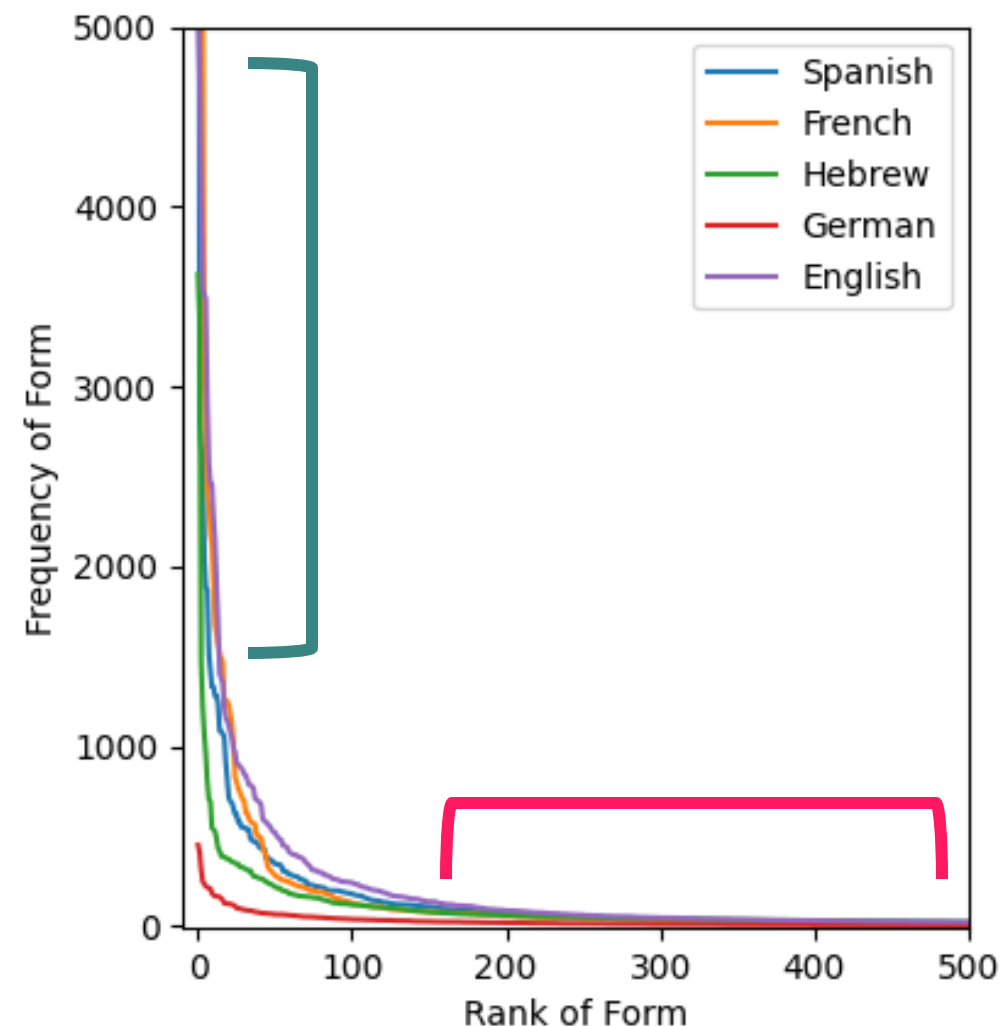
# The Long Tail: Zipf's Law

**Zipf's law:** word *rank* inversely proportional to *frequency*

$$f(r) \propto \frac{1}{r}$$

## Consequences:

- A few forms occur very **frequently**
- Most occur very **rarely (long tail)**



# The Long Tail: Paradigm Saturation

How many of its possible inflected forms does a word **actually occur** in?

$$\text{saturation} = \frac{\# \text{ seen}}{\# \text{ possible}}$$

	Present	Preterite	Imperfect	Conditional	Future
1SG	amo	amé	amaba	amaría	amaré
2SG	amas	amaste	amabas	amarías	amarás
3SG	ama	amó	amaba	amaría	amará
1PL	amamos	amamos	amábamos	amaríamos	amaremos
2PL	amáis	amasteis	amabais	amaríais	amaréis
3PL	aman	amaron	amaban	amarían	amarán

(Chan 2008, Lignos & Yang 2016)

# The Long Tail: Paradigm Saturation

How many of its possible inflected forms does a word **actually occur** in?

$$\text{saturation} = \frac{\# \text{ seen}}{\# \text{ possible}}$$

	Present	Preterite	Imperfect	Conditional	Future
1SG	amo		amaba		amaré
2SG		amaste			
3SG	ama		amaba		
1PL	amamos				
2PL					
3PL					

$$= \frac{7}{\# \text{ possible}}$$

(Chan 2008, Lignos & Yang 2016)

# The Long Tail: Paradigm Saturation

How many of its possible inflected forms does a word **actually occur** in?

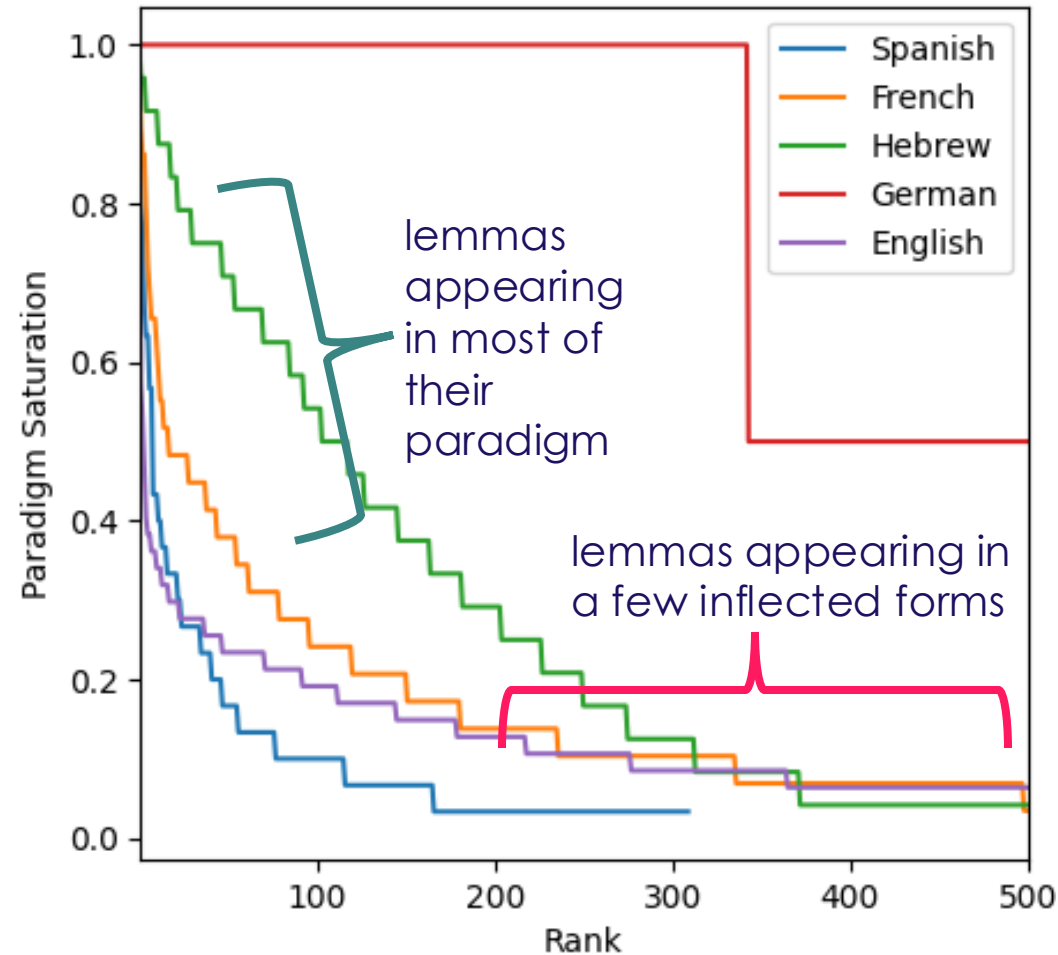
$$\text{saturation} = \frac{\# \text{ seen}}{\# \text{ possible}}$$

	Present	Preterite	Imperfect	Conditional	Future
1SG	<b>amo</b>	trabajé	<b>amaba</b>	trabajía	<b>amaré</b>
2SG	tomas	<b>amaste</b>	mirabas	mirarías	esperás
3SG	<b>ama</b>	esperó	<b>amaba</b>	espería	tomará
1PL	<b>amamos</b>	miramos	mirabamos	tomaríamos	miraremos
2PL	tratáis				
3PL	esperan	miraron	entraban	tratarían	entrarán

$$\begin{aligned} &= \frac{7}{\# \text{ possible}} \\ &= \frac{7}{26} \approx 27\% \end{aligned}$$

(Chan 2008, Lignos & Yang 2016)

# The Long Tail: Paradigm Saturation





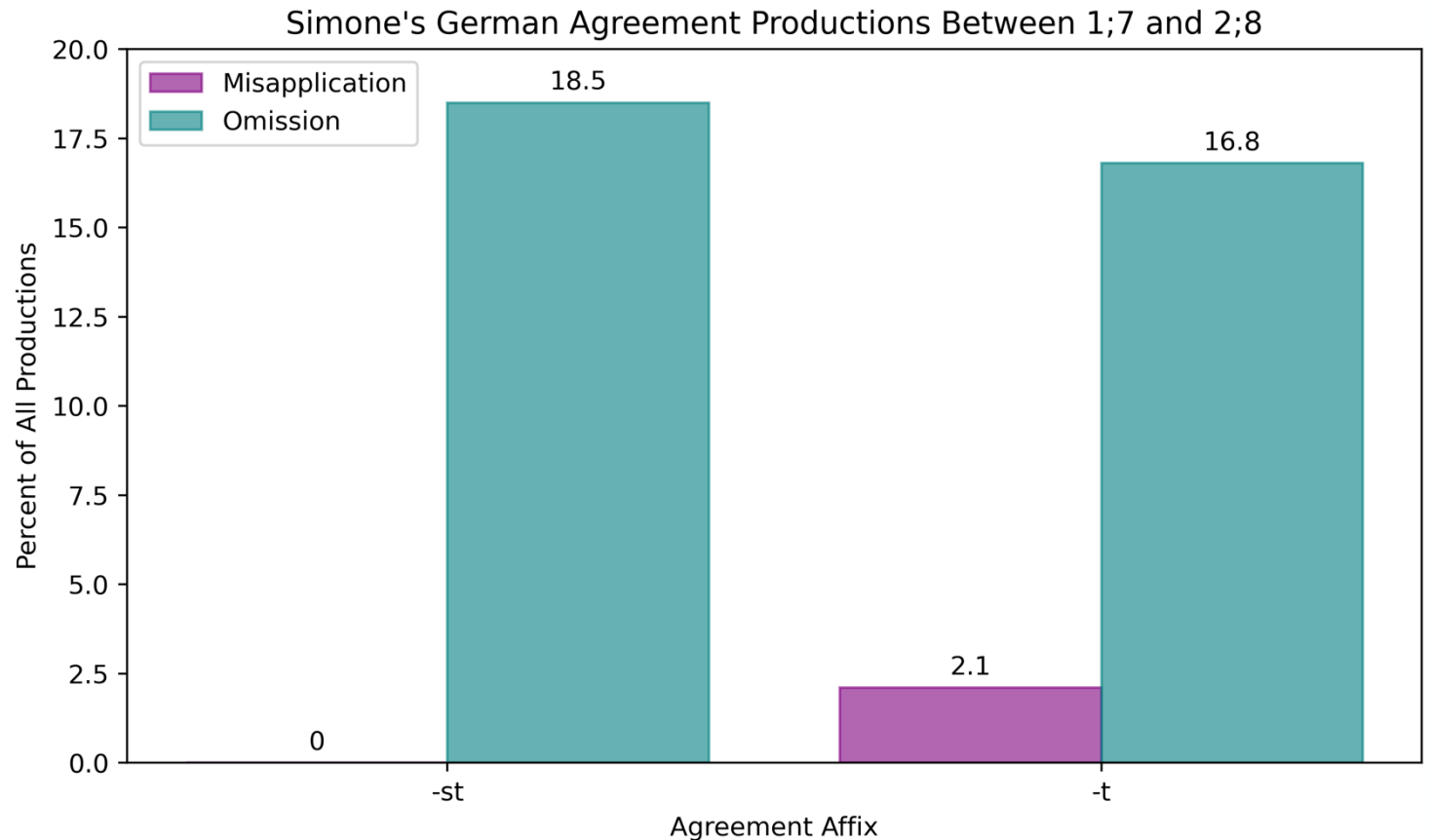
# Errors: Omissions vs. Substitutions

## Omissions

- e.g., “Papa have it”

## Substitutions

- e.g. “I has it”



(Clahsen & Penke 1992, Philips 1995, Legate & Yang 2007)

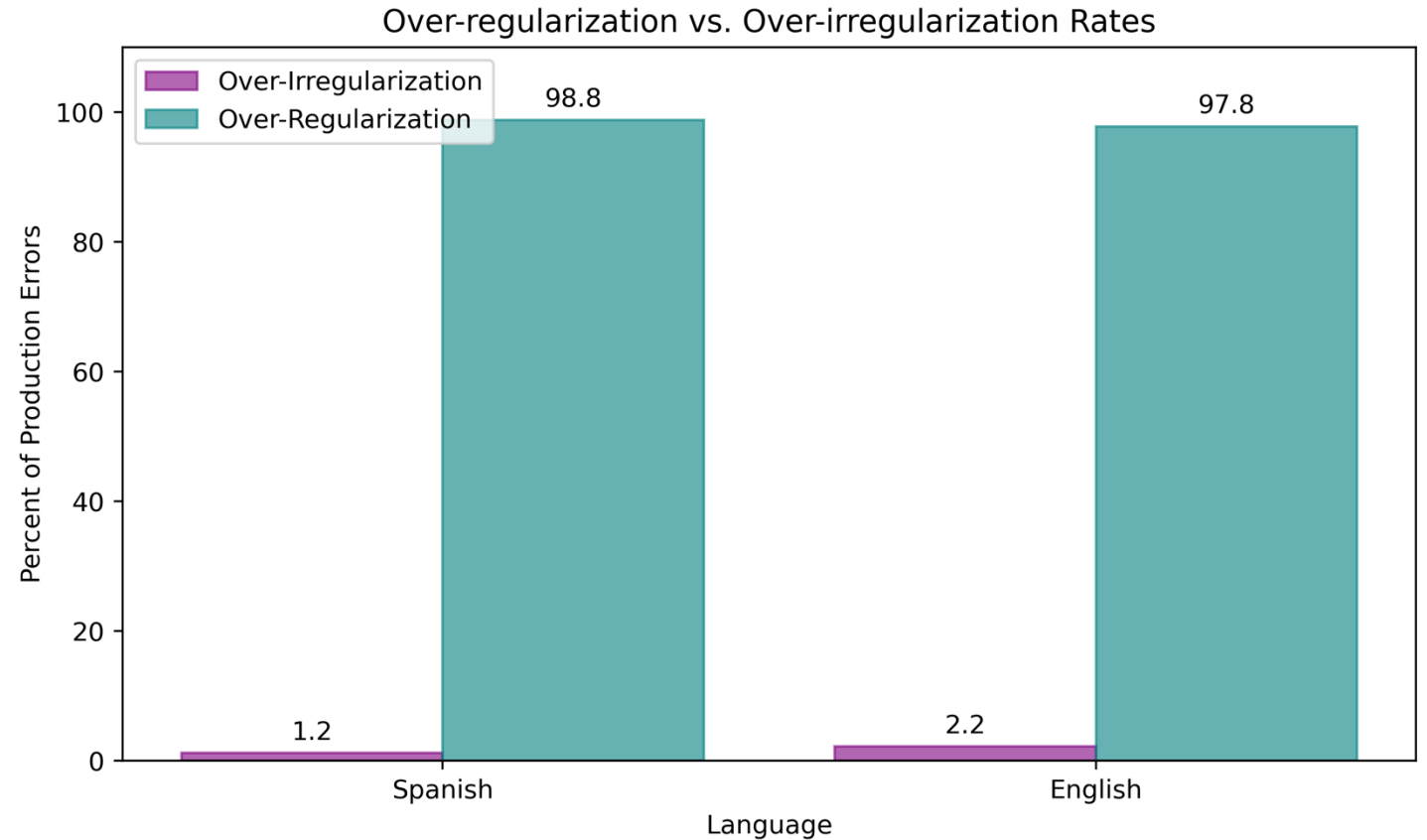
# Errors: Over-regularization

## Over-regularization

- e.g. *feel-feeled*

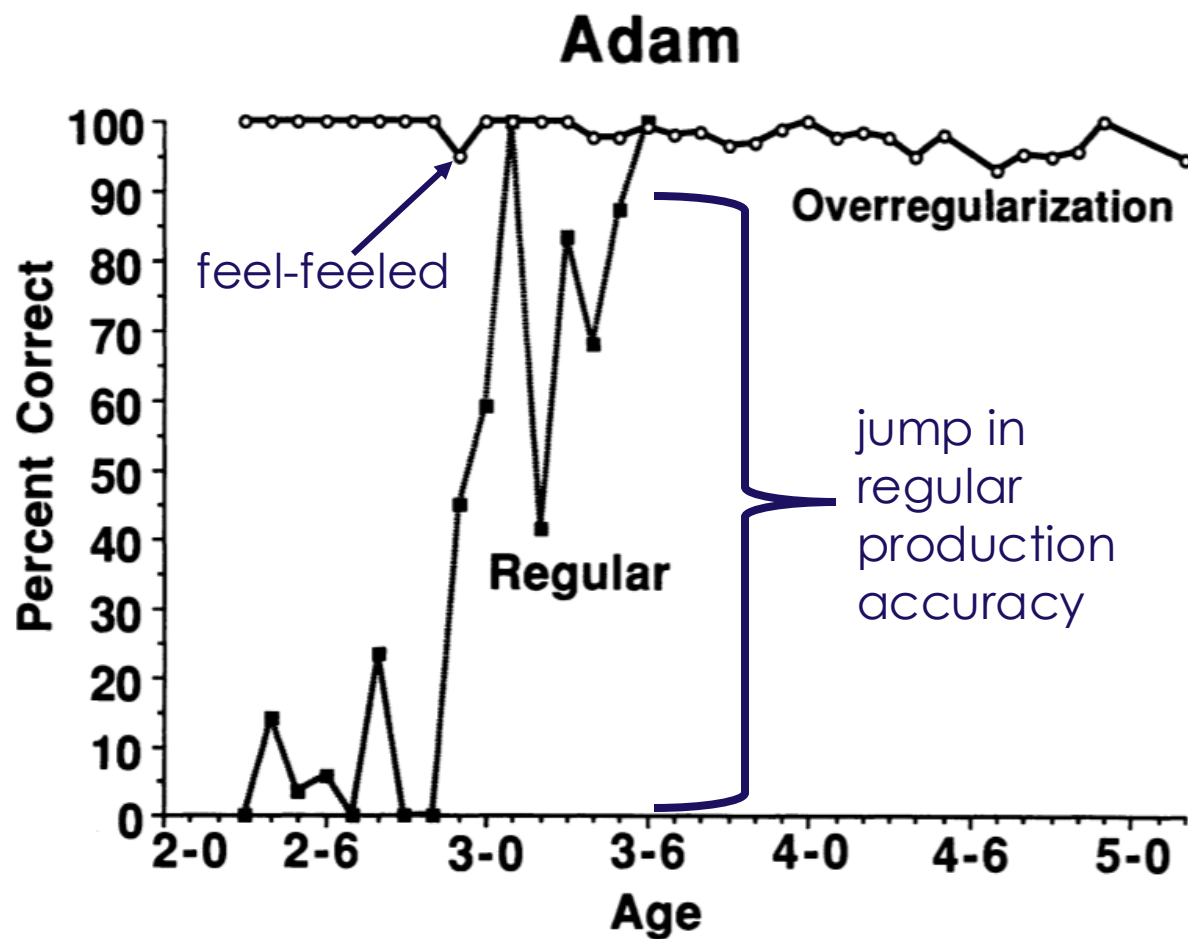
## Over-irregularization

- e.g. *bite-bote*



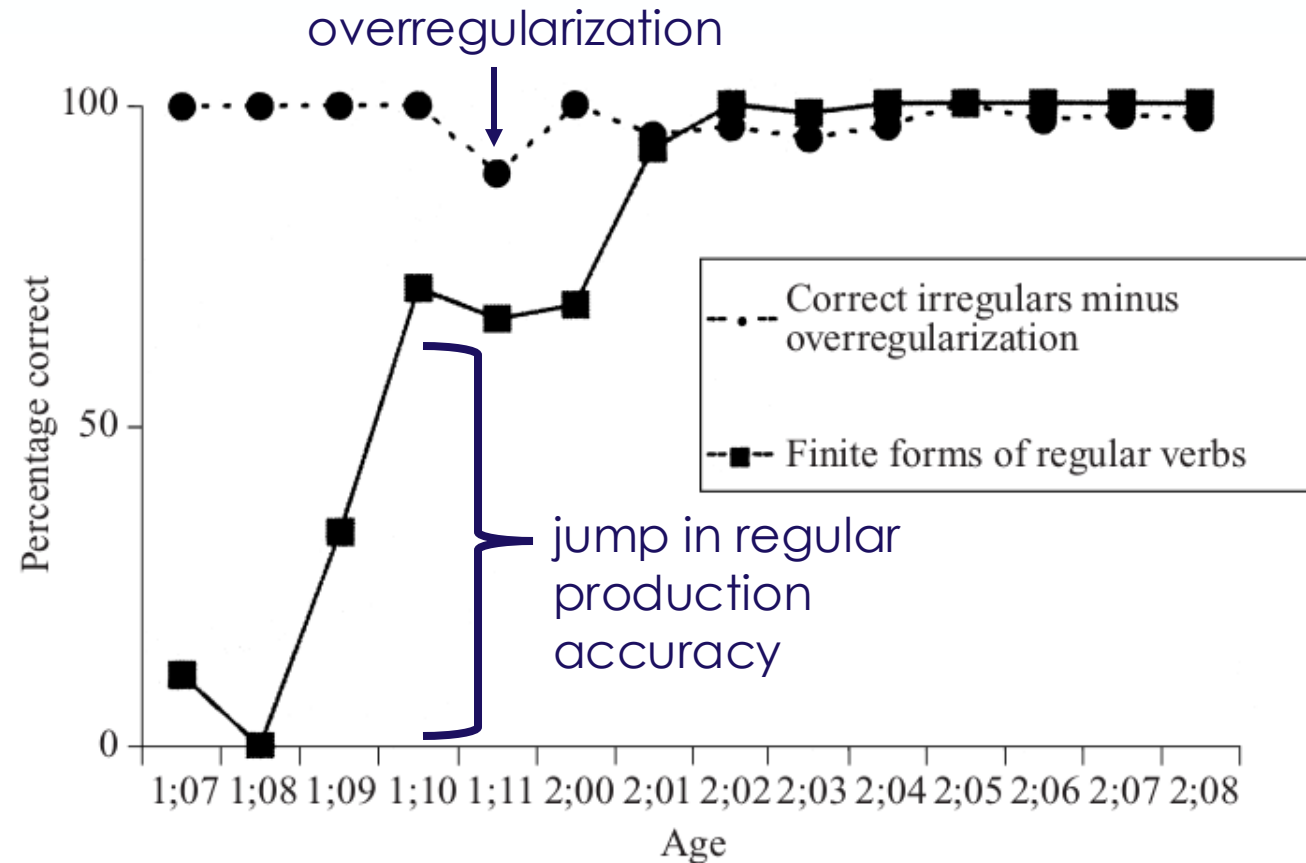
(Maslen et al 2004, Xu & Pinker 1995, Clahsen et al 2002)

# Background: Developmental Regression



(from Marcus et al 1992)

# Background: Developmental Regression



(from Clahsen, Aveledo, and Roca 2002)

# Summary: What Makes a Good Model?

## Learn from:

- *Small* vocabulary
- *Sparse* paradigms

## Errors:

- *Omissions*, not substitutions
- *Over-regularizations*, not over-irregularizations
- Developmental *regression*

**Interpretability:** we want to know why it does what it does

# The Past Tense Debate(s): Are Neural Networks Good Models?

# Are Neural Networks Good Models?

So  
true  
bestie!

Yes, our neural  
network models  
morphological  
acquisition!



James McClelland



David Rumelhart

- ✓ Trained on **plausible data**
- ✓ Exhibits **developmental regression**
- ✓ **Over-regularizes**

# Not Really...

🚨 Not actually trained on **plausible data**

- First trained on **80% irregulars**
- Then trained on **80% regulars**

🚨 **Developmental regression** results from implausible training data

🚨 **Over-irregularizes**

- *sip-sept, type-typed, mail-membled*





# Are we there yet?

Modern  
NNs can be  
plausible  
models!

R&M's  
model just  
wasn't  
advanced  
enough!



Ryan Cotterell

Christo Kirov

✓ Today's NNs **overcome practical limitations!**

- Near 100% test accuracy ✓
- Learn several inflectional classes ✓

✓ Trained on **developmentally representative data**

✓ Main errors = **over-regularizations**

# No, we aren't...

🚨 Still **over-irregularizes** way more than humans

- Predictions don't match well with **wug test judgments**

🚨 No **developmental regression**

🚨 **Implausible training data**

- Trained on **> 3500 verbs in their full paradigm**
- Children know **< 350 verbs** at 3;0
- Would need to see **> 15k unique words** to see 3,500 in full paradigm

Hey, so your model also isn't plausible!

Engineering ≠ science!

This is getting ridiculous



Maria Corkery



Yevgen Matuskevych



Sharon Goldwater

# Summary: The Past Tense Debate(s)

What have we gotten from ~30 years of NN research?

- **Better accuracy**
- **More developed architecture**



Good for engineering!

What haven't we gotten?

- Still **overproduce irregulars**
- Still **no developmental regression**
- Still **data-hungry**



Persistence of issues ⇒  
**fundamental difference  
between neural models &  
human language faculty**

What would they tell us about acquisition, anyway?

- **They aren't interpretable!**

# **Proposal:** Recursive, Rule-based Learning

# Mechanistic Account of Errors

## Past tense debate(s):

Create a model in a certain existing framework

- In this case, **connectionism**

Check whether it can learn from **plausible data**

Check whether it **matches errors**

No a-priori reason to expect either

## What if:

The design of our model was motivated by:

- The need to learn from **small, sparse data**
- The **types of errors** we expect it to make

Expect it to follow developmental patterns!

# Error-Motivated Modeling

Children **over-regularize** & don't **over-irregularize**

Account for this with **rule-based mappings**:

- Learn rule like **PAST**  $\Rightarrow$  **-ed**
- Apply rule when no exception is known
  - **Over-regularization** when exception not yet learned
  - **Developmental regression** when rule first learned

**Abduction of Tolerable Productivity (ATP):** recursively learn productive rules & their exceptions

# Error-Motivated Modelling

Children **omit** inflectional affixes, but don't **substitute** them

Account for this with **initially-underspecified inflectional categories**

- Must learn e.g. that English contrasts **+3SG** with **-3SG**
- Underspecified category can't be productively mapped to form, so **omit inflection**

**Sufficient Contrast Learner (SCL):** recursively learn inflectional categories

# Preliminaries: The TSP

**Intuitions:** given a set of  $N$  items:

- If **most** do  $X$ , then all do  $X$  (**generalization**)
- If **few** do  $X$ , memorize those that do (**lexicalization**)

## Tolerance of exceptions

Generalize a rule applying to  $N$  items with  $e$  exceptions iff:

$$e \leq \theta_N = \frac{N}{\ln N}$$

(Yang 2016)

## Sufficient positive evidence

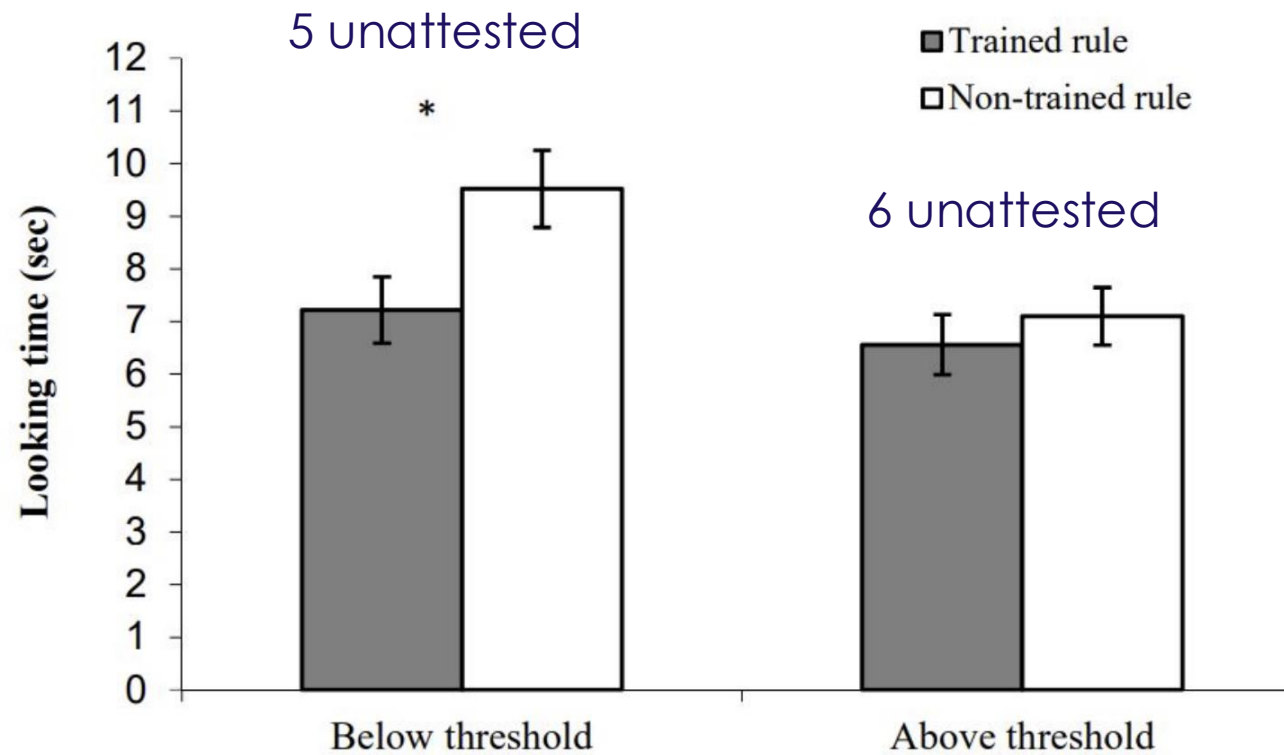
Generalize a rule applying to  $N$  items and seen applying to  $M$  iff:

$$\underbrace{N - M}_{\text{worst-case } e} \leq \theta_N = \frac{N}{\ln N}$$



# Preliminaries: The TSP

Experimental evidence for the *Tolerance-Sufficiency Principle*



$$\theta_{16} = 5.7$$

Emond & Shi (2020)

# Preliminaries: Training Data

Children learn **frequent forms earlier** (Goodman et al 2008)

- Use *most frequent forms from CHILDES*

Children use of **distributional cues** to learn meaning

- Intersect CHILDES with *UniMorph features as a proxy for these cues*

Input: **(lemma, inflected, features)**

Language	Lemma	Inflected	Features
English	walk	walked	{V, PAST, 3, SG}
Spanish	amar	amaban	{V, 3, PL, PAST, IMPFV}
German	Sache	Sachen	{N, FEM, PL}

# Mapping Features to Form: Abduction of Tolerable Productivity

(Belth et al 2021)

# Abduction of Tolerable Productivity

## Apply TSP **recursively**

- Given **N** items, do **enough** of them take **-x affix**?
  - If yes, **productive rule learnt!**
  - If not, **subdivide** into disjoint subsets & **recurse**



Caleb Belth

Me :)

Deniz Beser

Jordan Kodner

Charles Yang

# Abduction of Tolerable Productivity

Apply TSP **recursively**

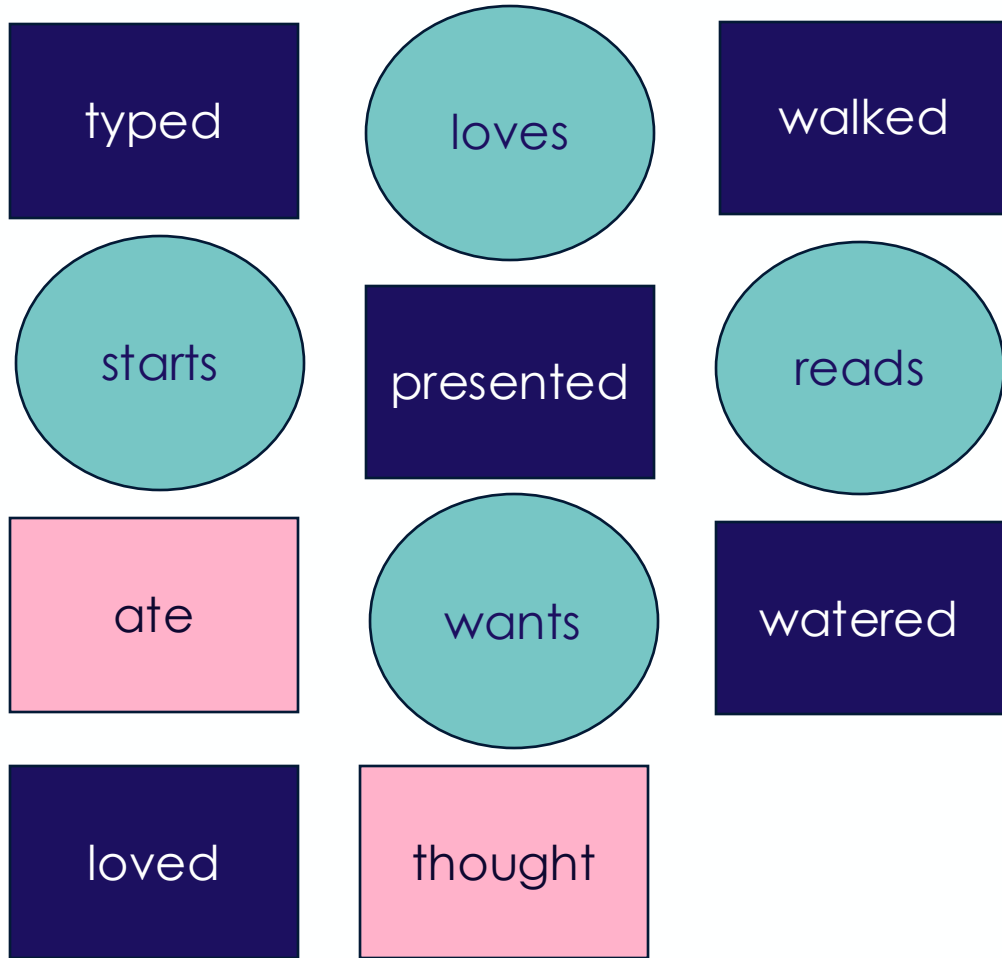
- Given **N** items, do **enough** of them take **-x affix**?
  - If yes, **productive rule learnt!**
  - If not, **subdivide** into disjoint subsets & **recurse**


**Terminate** when:

- Productive rule found (**generalization**)
- No more subdivisions possible (**lexicalization**)

Apply to **English past tense** and **German noun plurals**

# ATP Model: Toy Example



- 11 items: 4 **-s**, 5 **-ed**, 2 **other**
- **Generalize** most frequent?  
  $N - M = 11 - 5 = 6 > \theta_{11} = 4.5$
- **Subdivide!** Hypothesize a rule:

# ATP Model: Toy Example

typed

walked



presented

ate

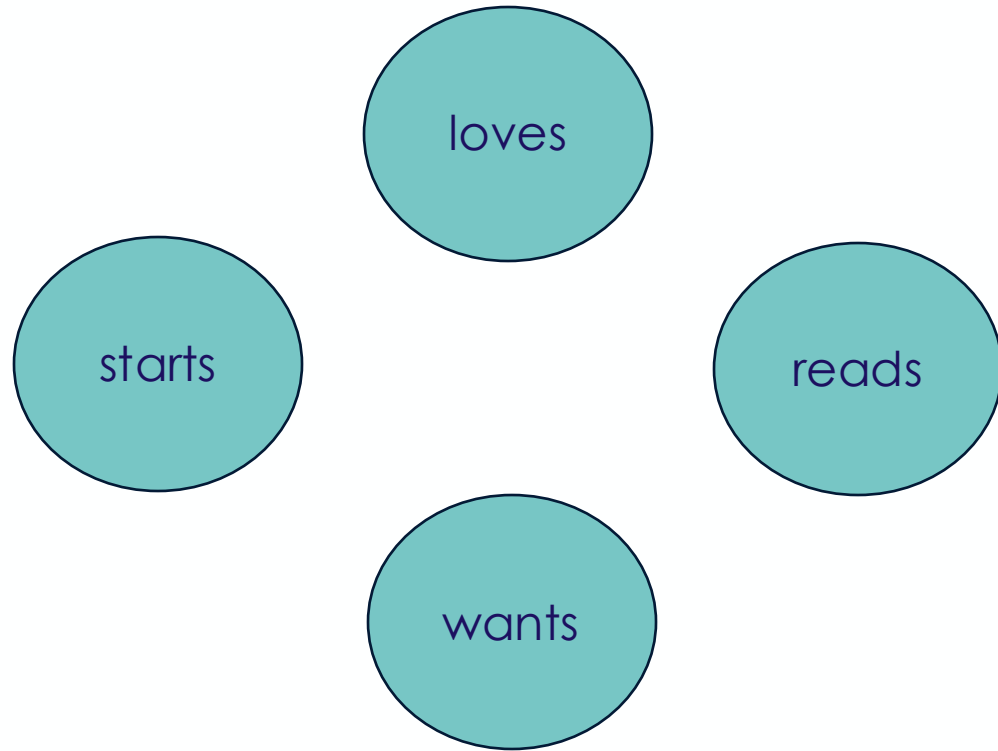
watered



loved

thought

- 11 items: 4 **-s**, 5 **-ed**, 2 **other**
- **Generalize** most frequent?  
  $N - M = 11 - 5 = 6 > \theta_{11} = 4.5$
- **Subdivide!** Hypothesize a rule:
  - PAST → **-ed**
- **Test** the rule:
  - $N - M = 2 < \theta_7 = 3.5$  
- R1 productive! PAST → **-ed**
  - Memorize **ate** and **thought**

# ATP Model: Toy Example

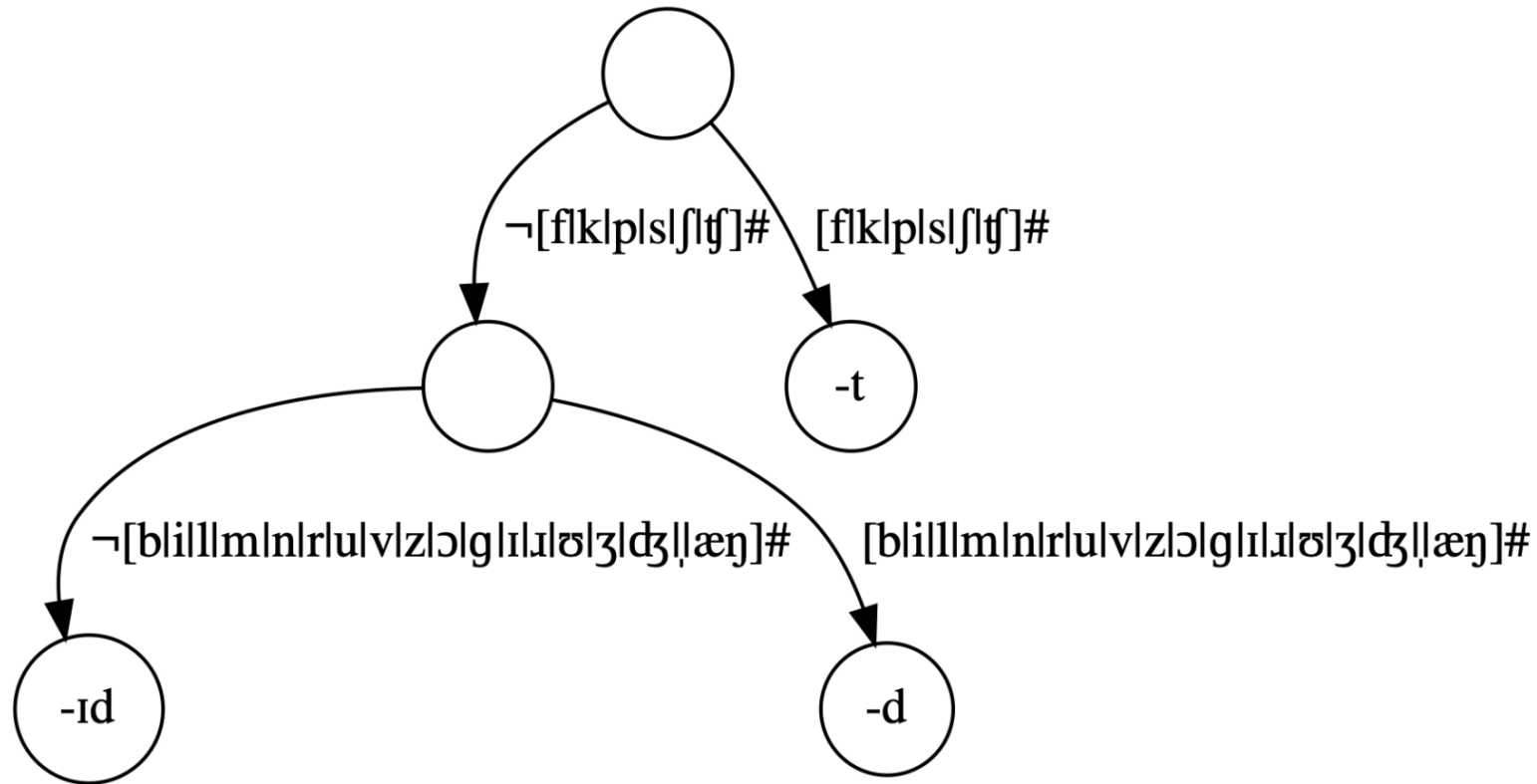


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- **Test** the rule:
  - $N - M = 2 < \theta_7 = 3.5$  
- R1 productive! PAST  $\rightarrow$  **-ed**
  - Memorize **ate** and **thought**
- **Recurse:** PRES,3,SG  $\rightarrow$  **-s**



# ATP Model: Sample learning trace

**English past tense:** morphophonological conditioning



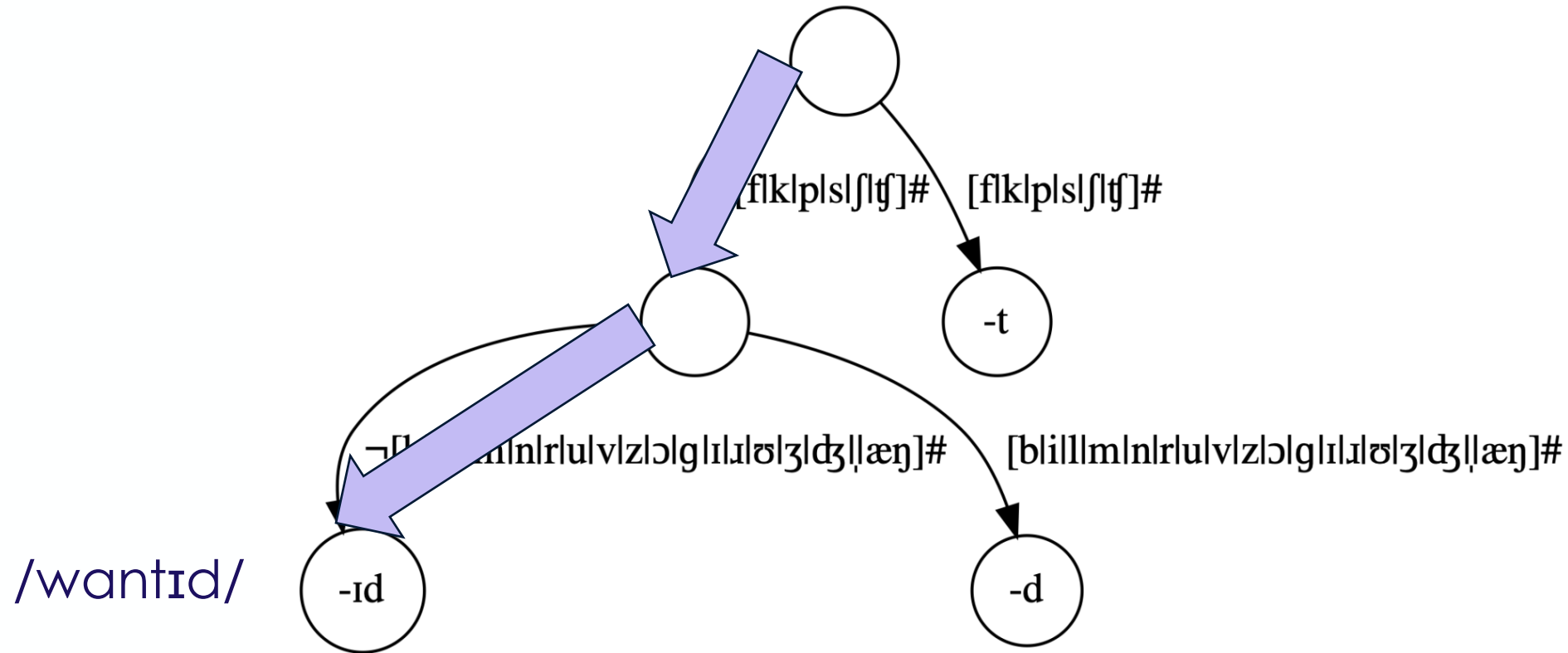
# ATP Model: Inflection and Generation

During test, given **novel forms & features** to inflect  
Traverse decision tree to correct node

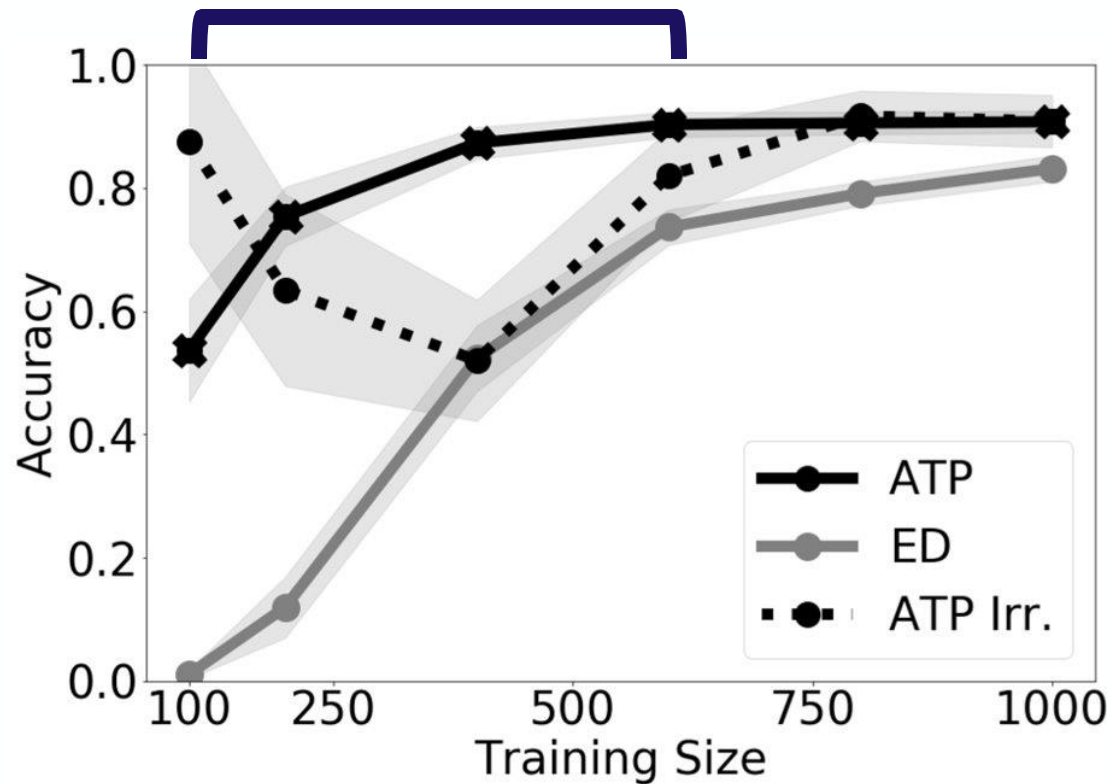
- If node has **productive rule**, apply the rule
- If no **productive rule**, either:
  - Produce unmarked form
  - **Analogize** to a known form at this node

# ATP Model: Sample learning trace

English past tense: inflect /want/



# ATP: English Results



(a) English

Trained on **plausible vocabulary**

- 1000 inflected forms

**Developmental regression and overregularization**

**Mechanistic account of developmental regression**

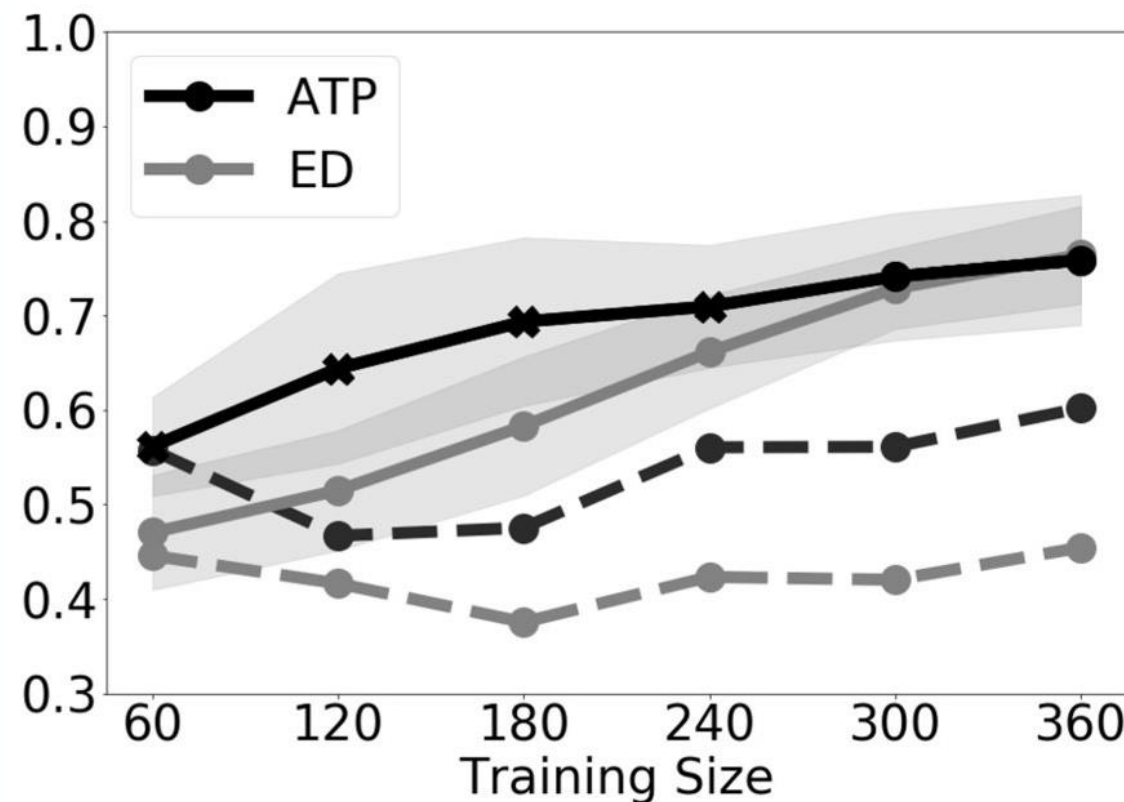
# ATP: German Results

Relies less on gender than K&C

- **Solid lines** = gender info given at test
- **Dashed lines** = gender info not given at test

Trained on **plausible vocabulary**

- **400** inflected forms



(b) German

# ATP: Summary

Children **overregularize**

- *So does ATP!*

Children show **developmental regression** when learning some paradigms

- *So does ATP!*

Children learn from **extremely sparse, skewed input**

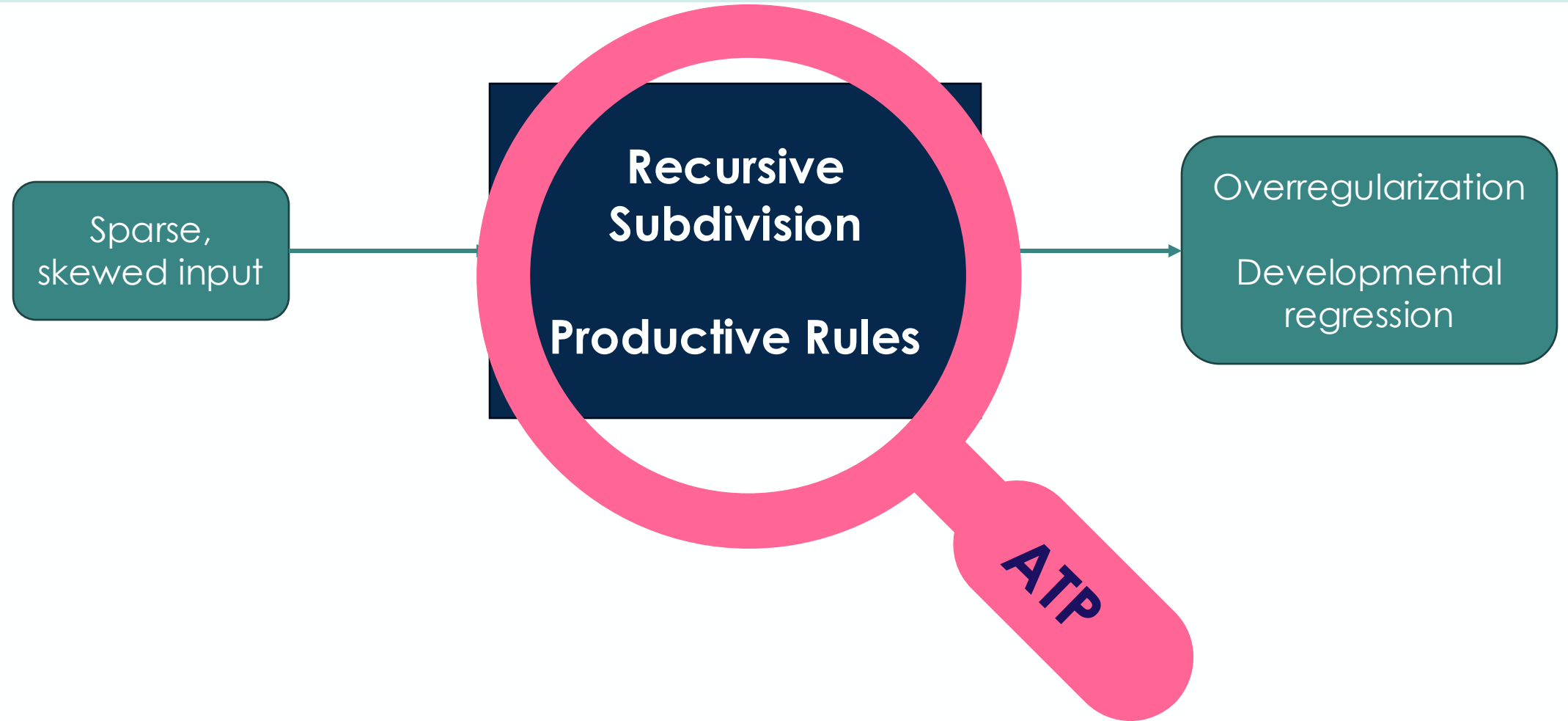
- *So does ATP!*

**ATP gives a mechanistic account of *why* these errors occur and what the resulting grammar looks like**

# ATP: Summary



# ATP: Summary





# Learning which Features are Marked: Sufficient Contrast Learner

(Payne 2022, 2023)

# SCL Model: Preliminaries

**Principle of Contrast:** distinct forms  $\Rightarrow$  distinct meanings

- e.g. *walk* and *walked* must mean something different

**Collisions:** one lemma in multiple inflected forms

- e.g. *walk-walked* tells us that  $\pm$ PAST is marked

**TSP:** when are there enough collisions to learn marking?

- e.g. don't learn from *am-are* that **1 vs. 2** marked in English
- Learn from *walk-walked*, *sing-sang*, etc. that  $\pm$ PAST marked

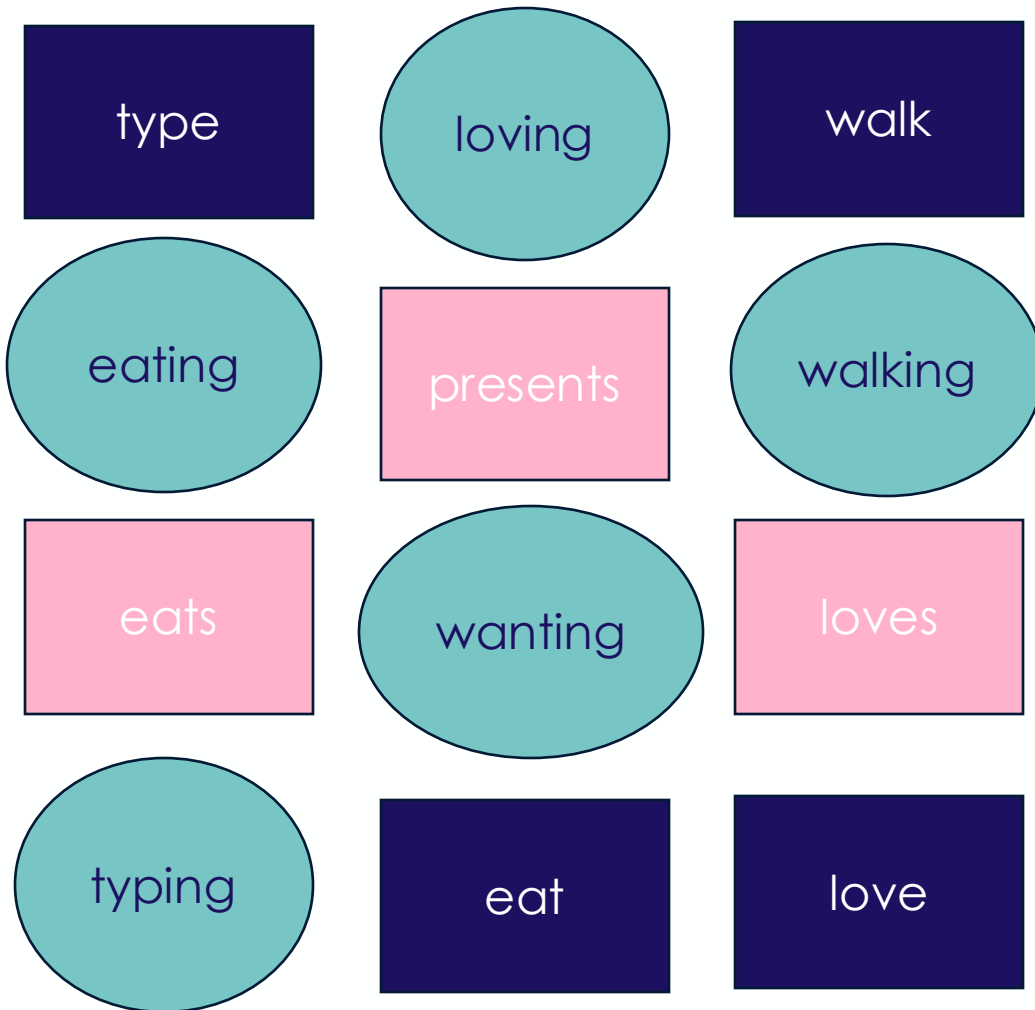
# SCL Model: Collisions

Apply TSP **recursively** again!

- Input taken in **incrementally**
- When  **$j^{th}$  input** encountered, is there a collision?
- If so, do enough forms appearing in **inflection A** also appear in **inflection B** in a different form?
  - If yes, **productive contrast learnt!** Subdivide and recurse
  - If no, **continue** to take in input

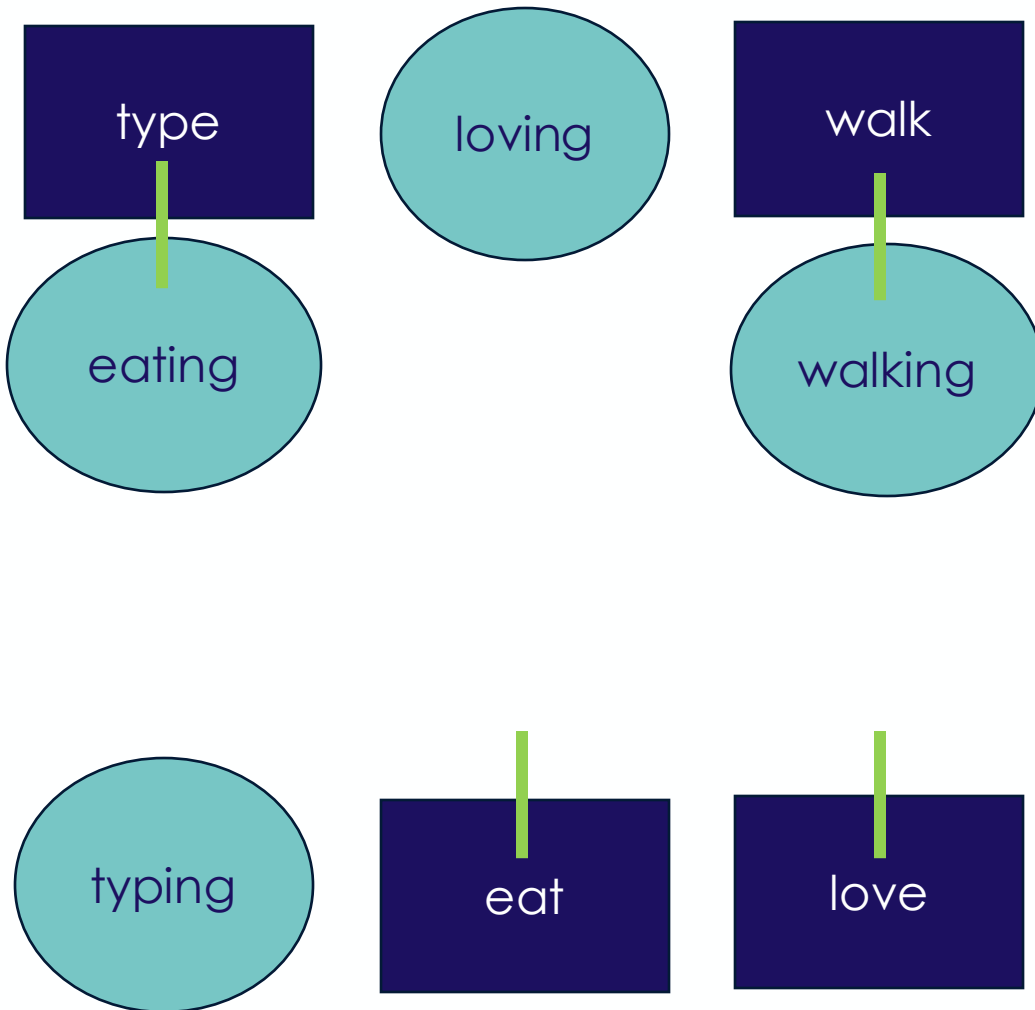
Apply to **English verbs, German noun plurals, Spanish verbs, and Hebrew verbs**


# SCL Model: Toy Example



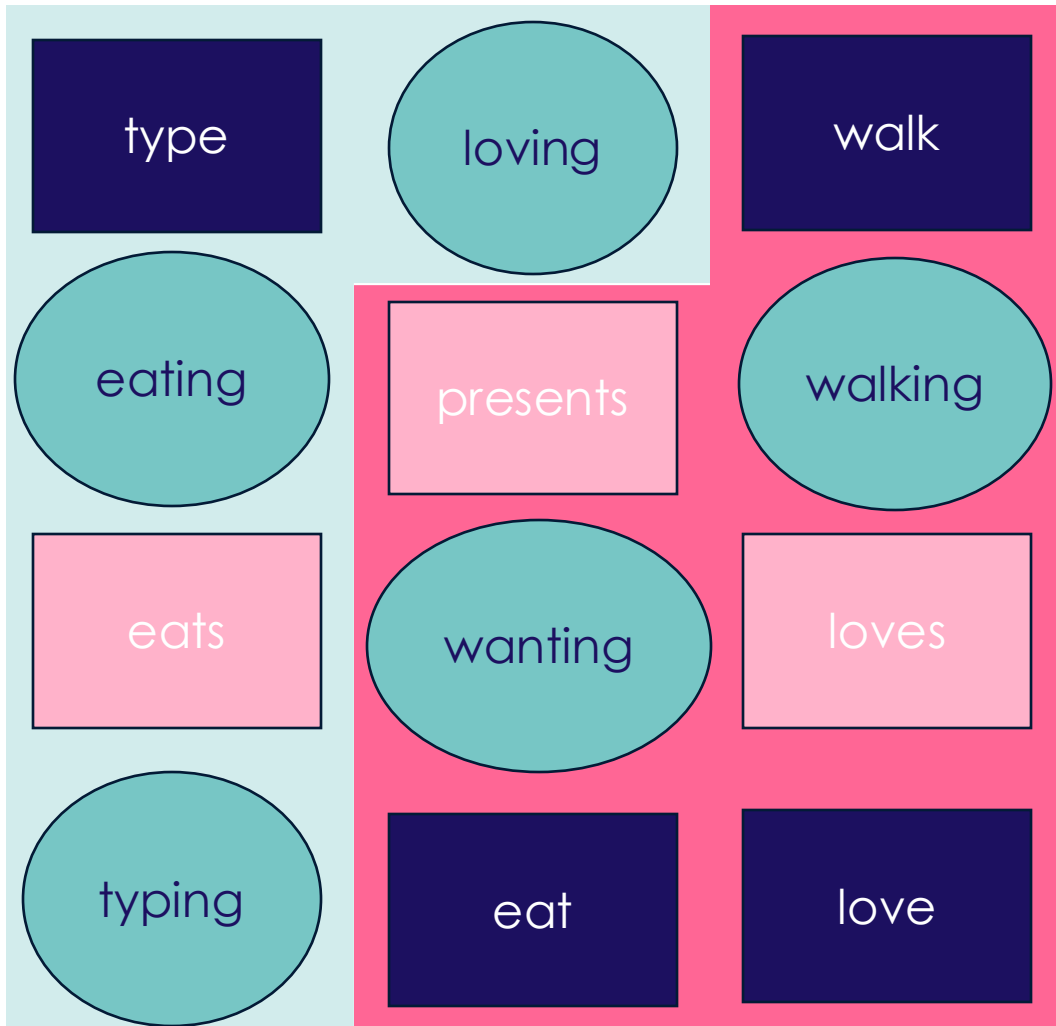
- Collision: **walk-walking**
- **±PARTICIPLE** marked?


# SCL Model: Toy Example



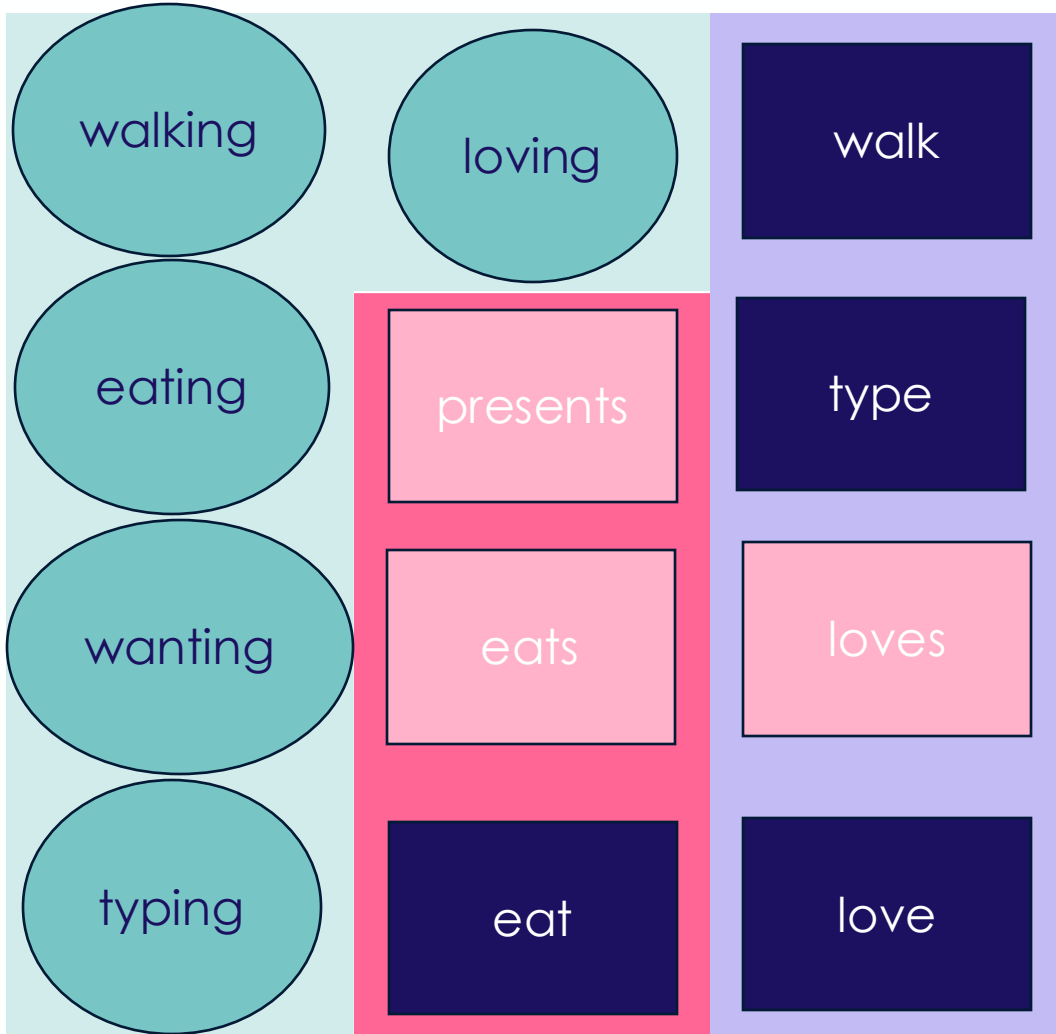
- Collision: **walk-walking**
- **±PARTICIPLE** marked?
  - 5 participles, 4 collisions (not **wanting**)
  - $N - M = 1 < \theta_5 = 3$  
- Contrast 1 productive!  
**±PARTICIPLE** marked


# SCL Model: Toy Example



- Collision: **walk-walking**
- **±PARTICIPLE** marked?
  - 5 participles, 4 collisions (not **wanting**)
  - $N - M = 1 < \theta_5 = 3$  
- Contrast 1 productive! **±PARTICIPLE** marked
- **Subdivide** into **+PARTICIPLE** and **-PARTICIPLE** forms

# SCL Model: Toy Example



- Collision: **walk-walking**
- **±PARTICIPLE** marked?
  - 5 participles, 4 collisions (not **wanting**)
  - $N - M = 1 < \theta_5 = 3$  
- Contrast 1 productive! **±PARTICIPLE** marked
- **Subdivide** into **+PARTICIPLE** and **-PARTICIPLE** forms
- Recursively learn that **± 3SG** marked

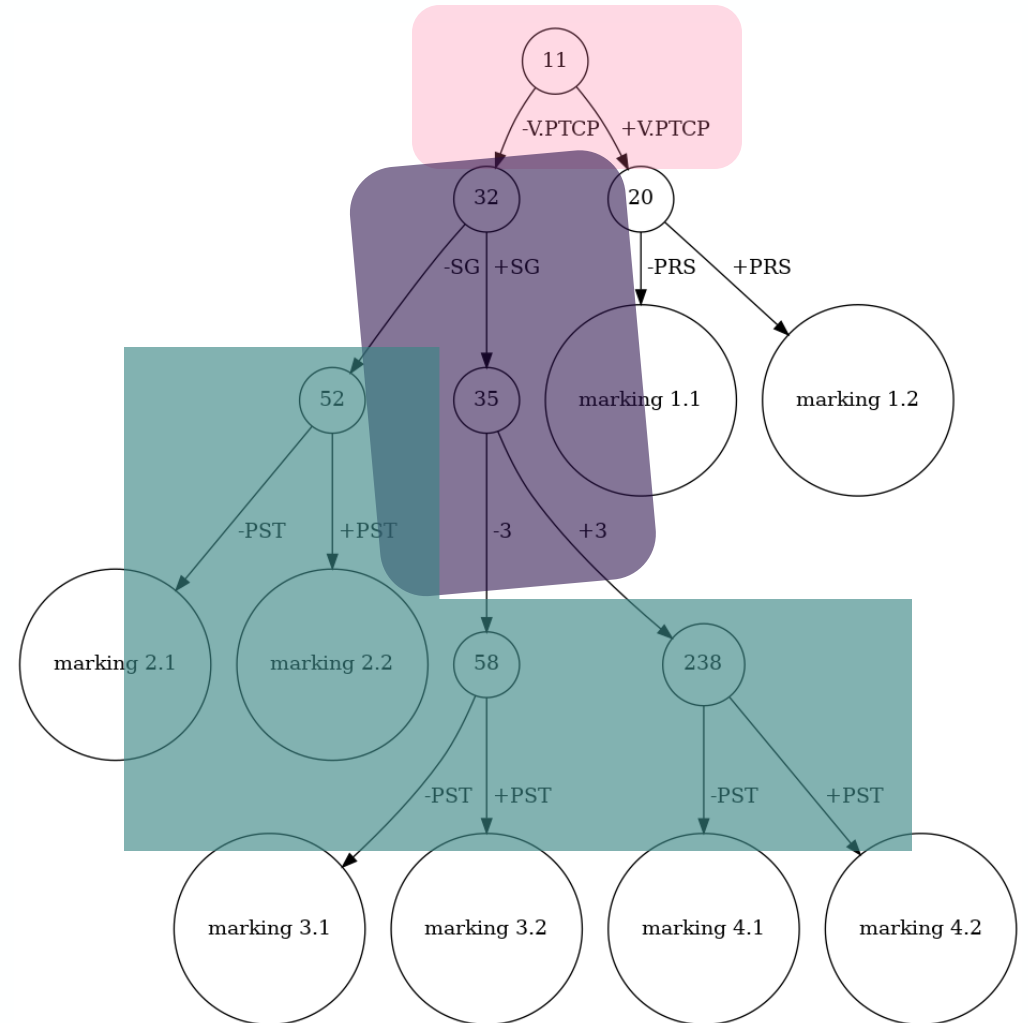
# SCL: English Results

## Plausible **order of acquisition**

1. **PARTICIPLE** (-ing)
2. **3SG** (-s)
3. **PAST** (-ed)

## Plausible vocabulary size:

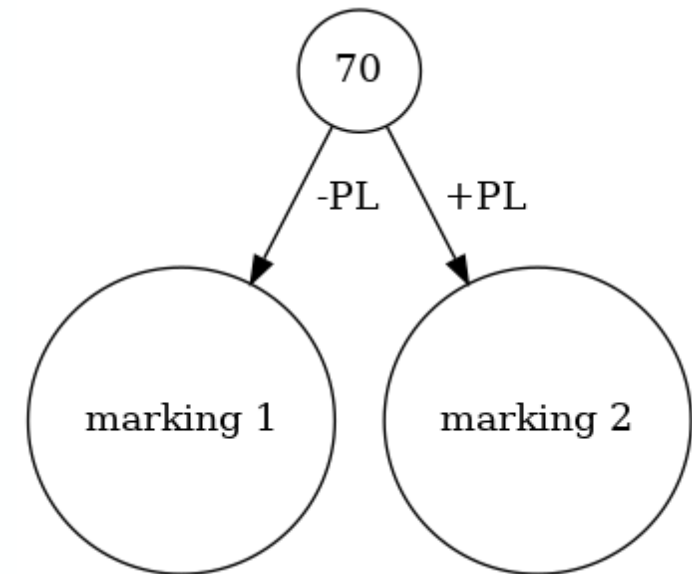
- **112** lemmas
- **238** inflected forms





# SCL: German results

- Plausible vocabulary size:
  - **66** lemmas
  - **70** inflected forms
- Well under vocab size at which plural affix overapplication begins



# SCL: Spanish Results

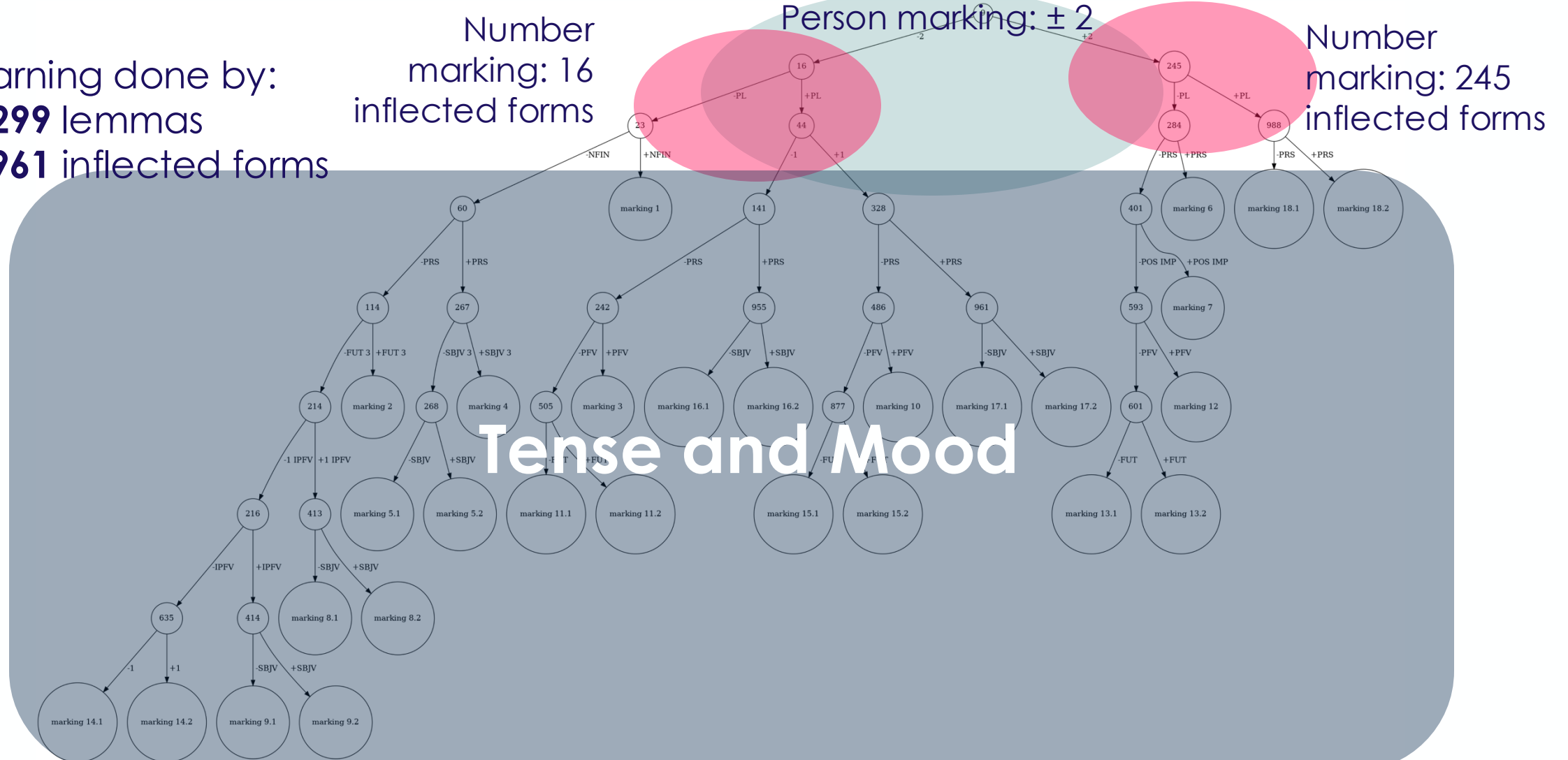
- Spanish order of acquisition:
  - **Finiteness & person marking:** 1;7
  - **Number marking:** 1;7-2;0
    - Second plural emerges later than other agreements in many learners
  - **Tense:** 2;0-2;2
  - **Mood:** 1;7-2;2

(Montrul 2004)

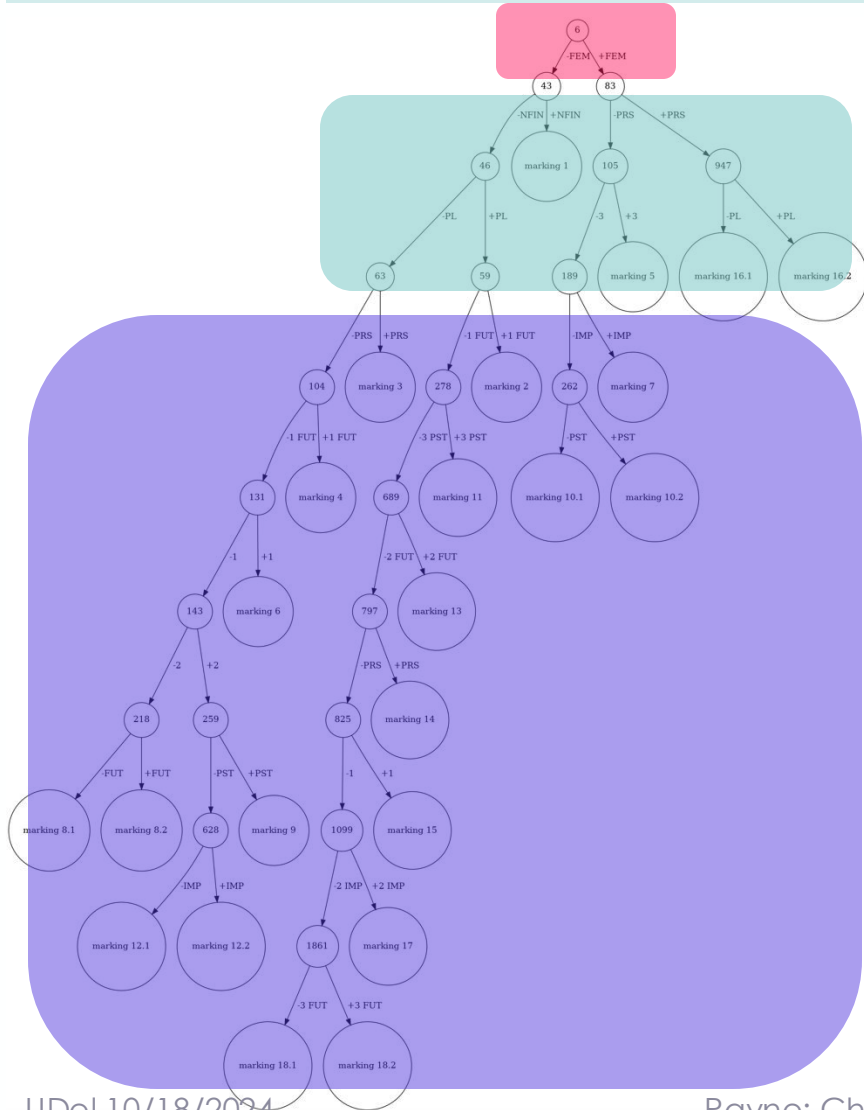
## SCL: Spanish Results

- **299** lemmas
- **961** inflected forms

- **961** inflected forms



# SCL: Hebrew Results



Hebrew order of acquisition:

- **Person, number, gender** before tense
- **Person vs. number** varies
- **Gender** appears before or at the same time as **number**

Our model:

- Order of acquisition:
  - **Gender**, **person & number**, **tense**
- Vocab size:
  - **323** lemmas
  - **1861** inflected forms

# SCL Implications: Root Infinitives

**Root Infinitive (RI) Stage:** stage of omission errors

Cross-linguistically, “**richer**” morphology ⇒ **shorter RI stage**

Richer morphology also means **more subdivision**

- TSP tolerates more exceptions for **smaller *N***
- More subdivision ⇒ **smaller *N***
- Smaller *N* ⇒ **quicker learning** of inflectional categories

SCL gives a **mechanistic account** of cross-linguistic differences

(Philips 1995, Legate & Yang 2007)

# SCL: Summary

Children **omit affixes**

- *SCL gives an account for why!*

Children show clear **order of acquisition effects**

- *So does SCL!*

Children learn from **extremely sparse, skewed input**

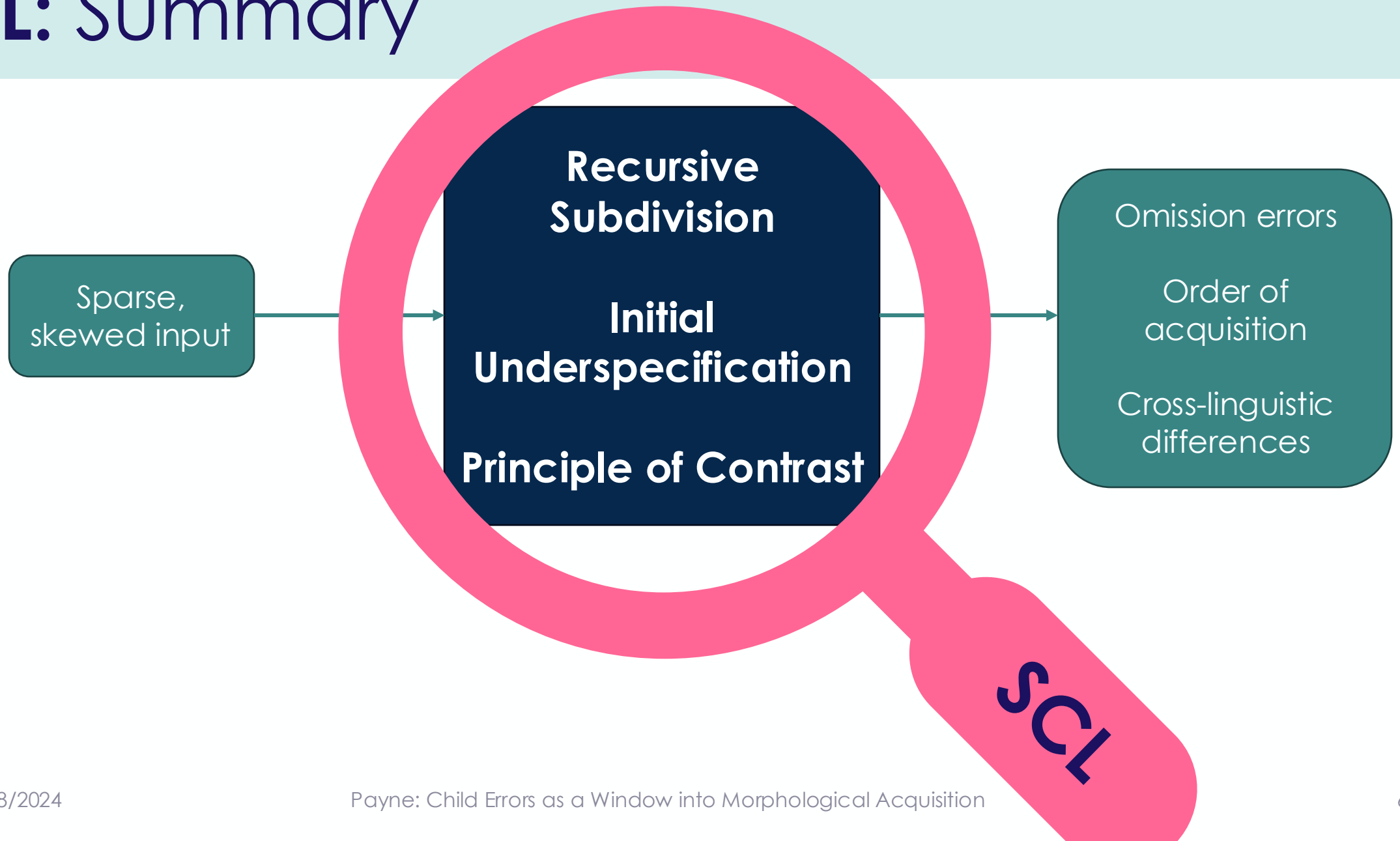
- *So does SCL!*

**SCL gives mechanistic account of order of acquisition, omission errors and cross-linguistic differences in acquisition**

# SCL: Summary



# SCL: Summary





# Discussion & Future Directions

# What Makes a Good Model?

## Input:

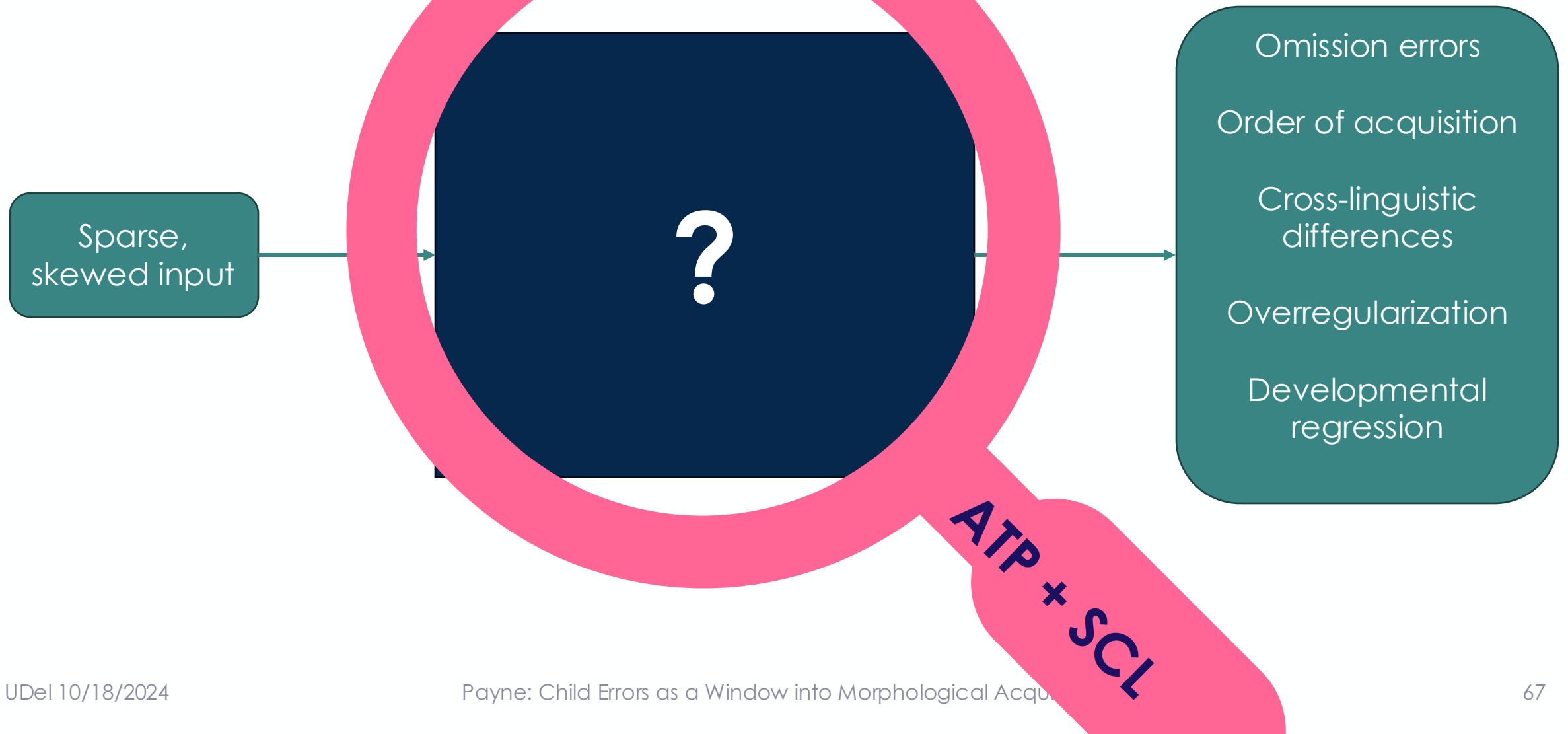
- *Small* vocabulary
- *Sparse* paradigms

## Errors:

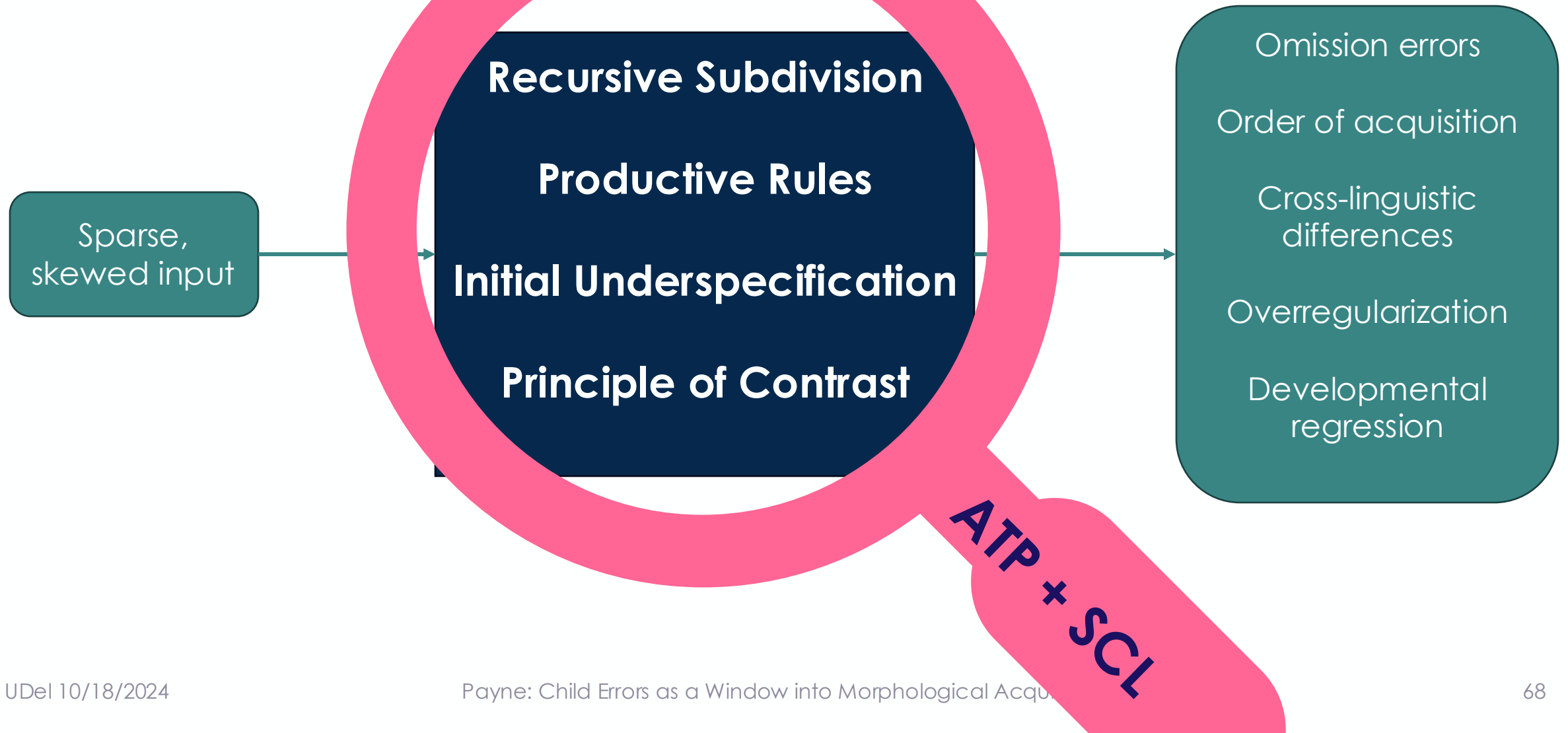
- *Omissions*, not substitutions
- *Over-regularizations*, not over-irregularizations
- Developmental *regression*

**Interpretability:** why does it do what it does?

# A Mechanistic Account



# A Mechanistic Account



# Conclusion: Getting the Right Stuff Wrong

	NNs	ATP	SCL
Learn from plausible data	✗	✓	✓
Account for over-regularization and developmental regression	✗	✓	---
Account for omission and the RI stage	✗	---	✓
Interpretability	✗	✓	✓

# Future Work

**SCL** learns the features required by **ATP**

- **Combination** of these two learning strategies
- First learn the inflectional classes, then map them to form

**Expand ATP:**

- Handle **templatic & agglutinative** morphology

**Expand SCL:**

- Explore model **subdivision predictions**
- Learn features from **distributional information**

# Thank you!!



Caleb Belth  
University of Utah



Deniz Baser  
ISI



Jordan Kodner  
Stony Brook



Charles Yang  
UPenn

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# Background: Earliest Stages

## Early Segmentation

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## Early Understanding of Use

- English learners:
    - **0;6**: segment **-s**
    - **0;8**: segment **-ing**
    - **Both**: not **pseudomorphemes**
  - French learners (0;11):
    - Segment **-e** (infinitive & pastp)
    - Don't segment **pseudomorpheme -U**
- English-learners:
    - **1;7**: can't use **-s** as cue to subject number
    - **5;0**: use **-s** as a cue to subject number in comprehension

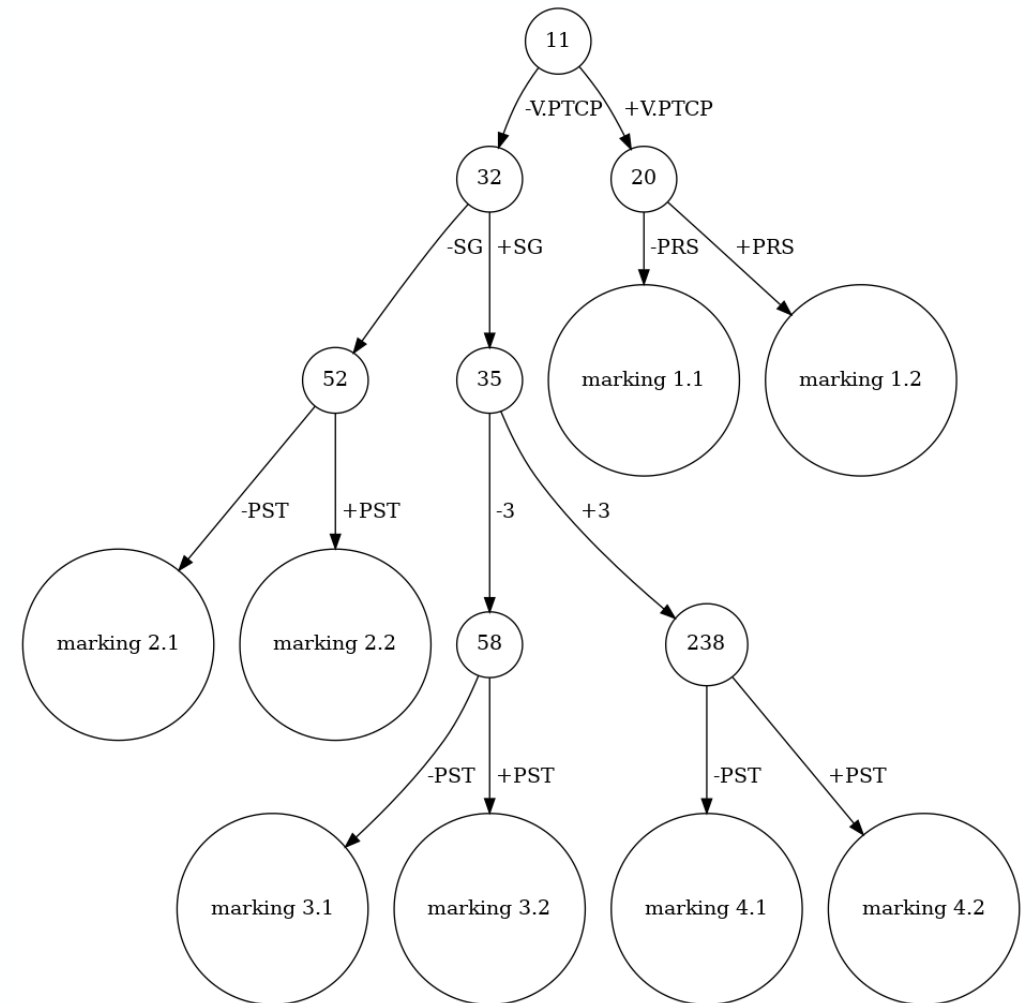
(Kim & Sundara 2021, Marquis & Shi 2012, Soderstrom et al 2002, Johnson et al 2005)



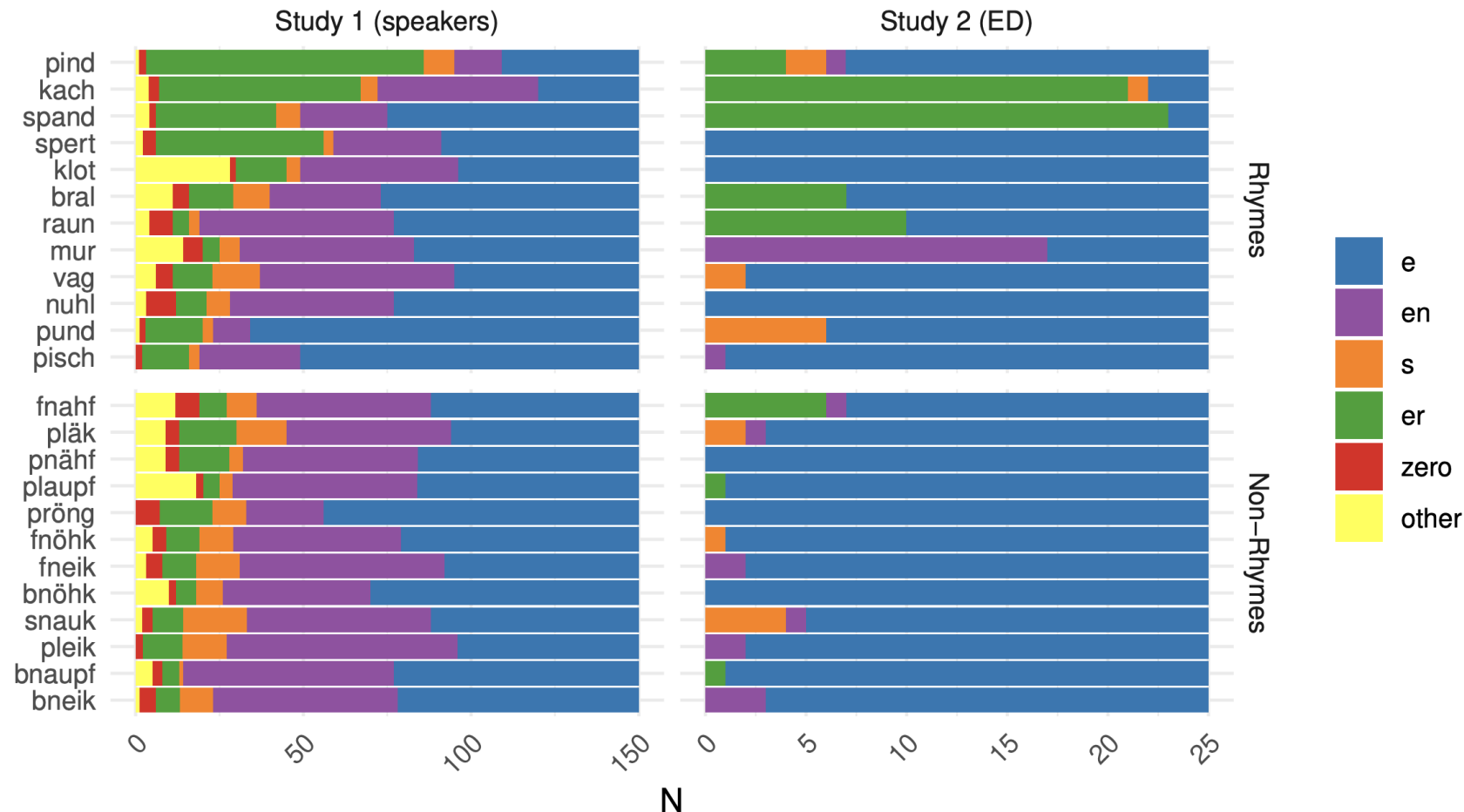
# SCL: English Results

Learning past tense separately for each agreement?

- **Yang, Elman, and Legate (2015):** past tense acquired later for learners of AAE
- **Difference in input** = agreement, not tense
- TSP tolerates *relatively fewer exceptions* for larger  $N$

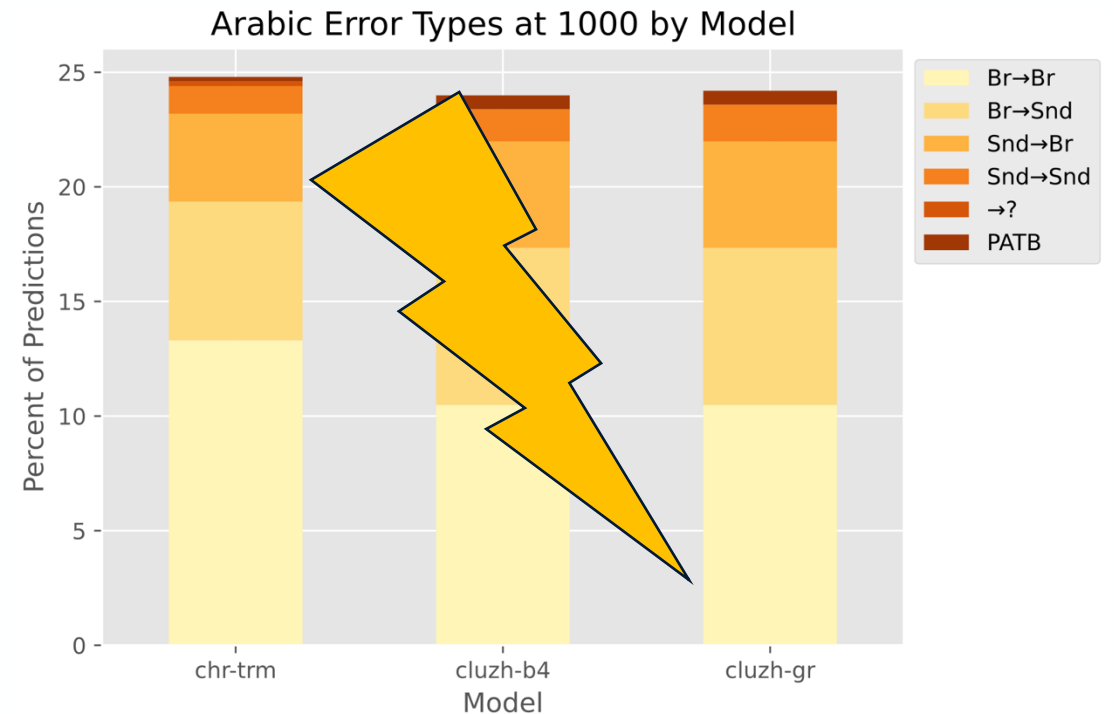
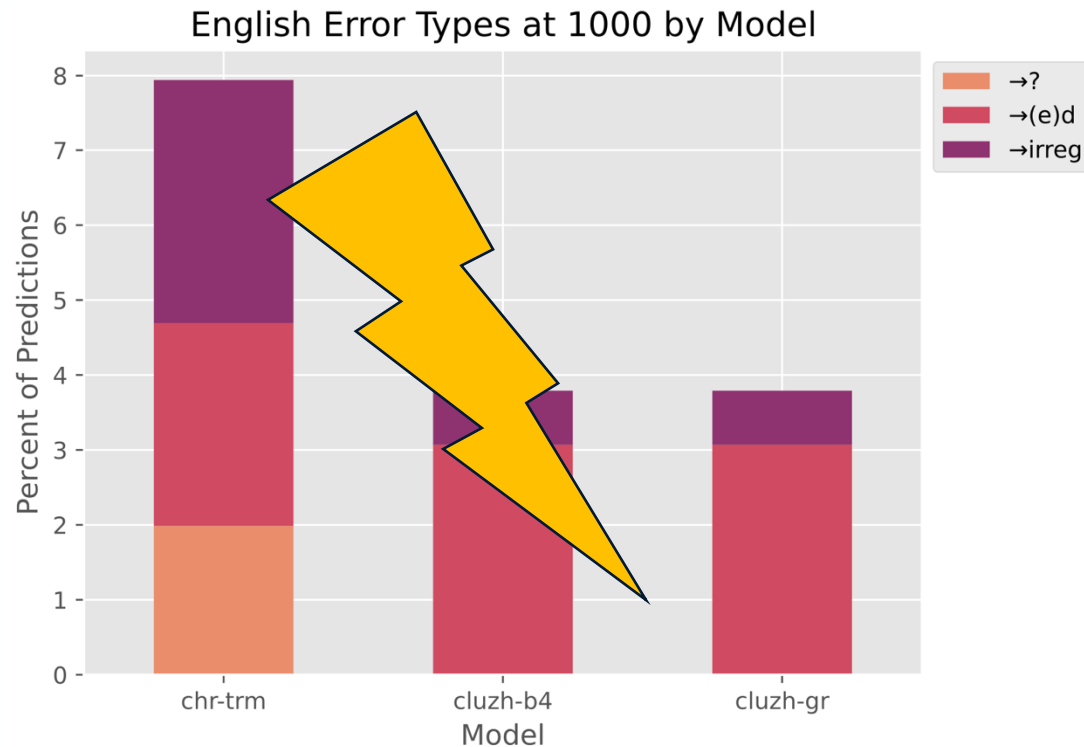


# German Noun Plurals: We really aren't there



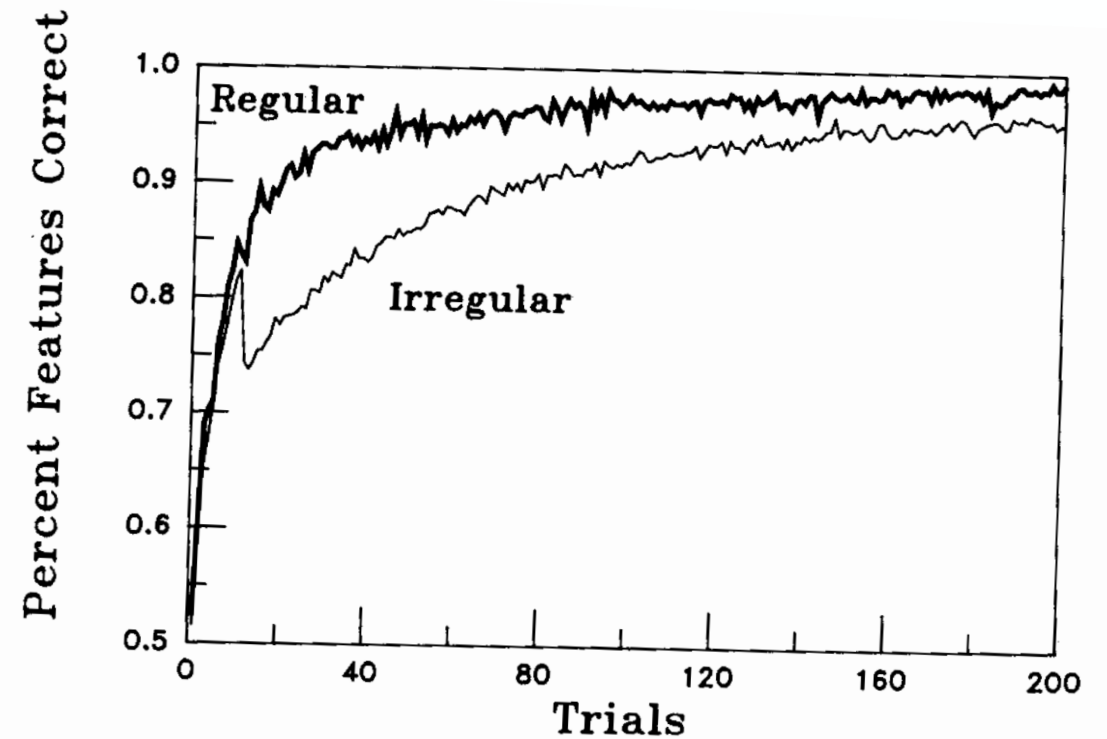
# Other Neural Models: Still not there!

- Ongoing work with **Salam Khalifa, Jordan Kodner & Zoey Liu**: test *more models* on *more paradigms*, find *same problems*



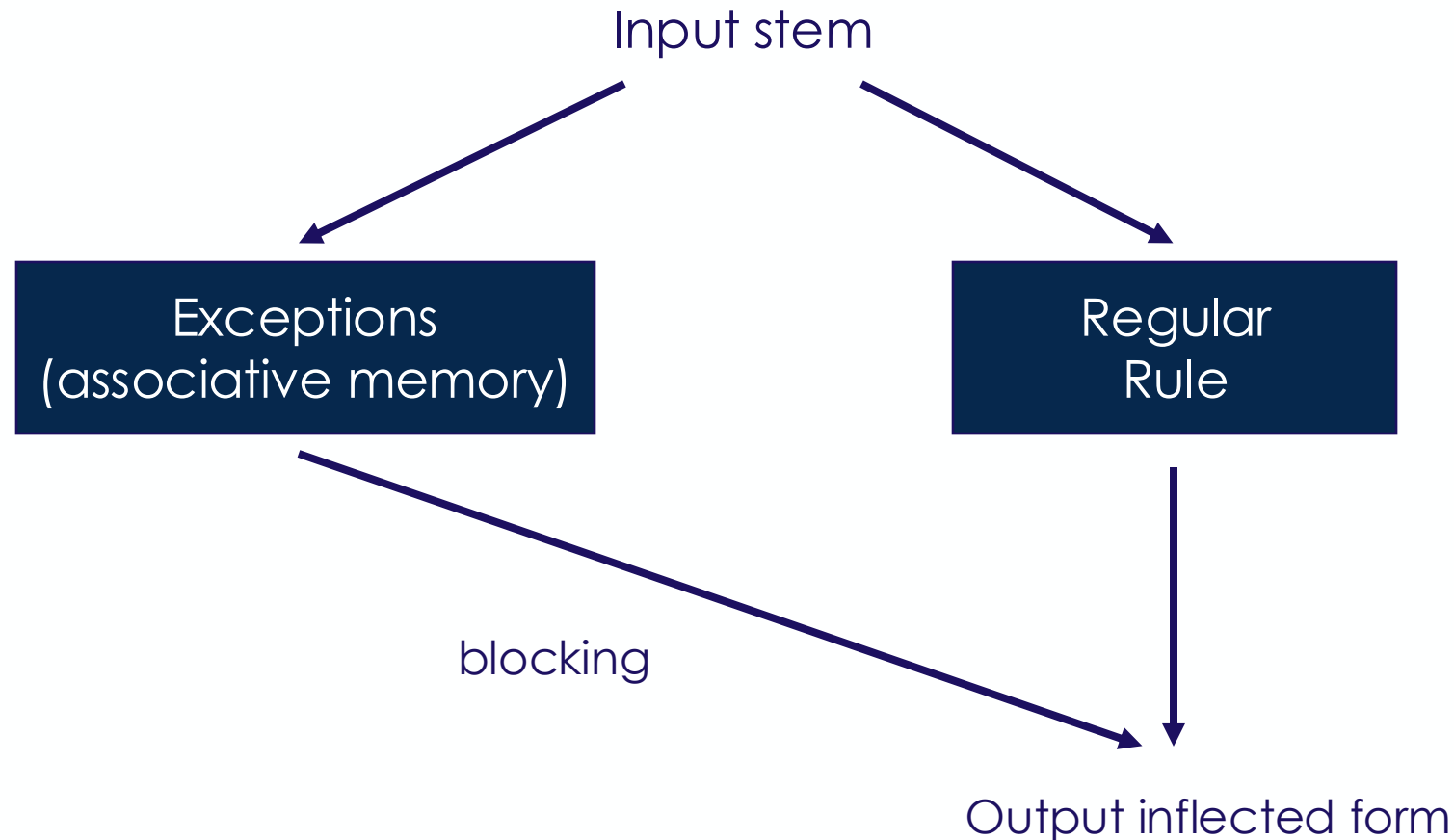
# Background: The Past Tense Debate

- Rumelhart & McClelland: *single-route, connectionist* model can:
  - Exhibit *developmental regression*
  - Exhibit *overregularization*
- ∴ **Rule-like behavior!**



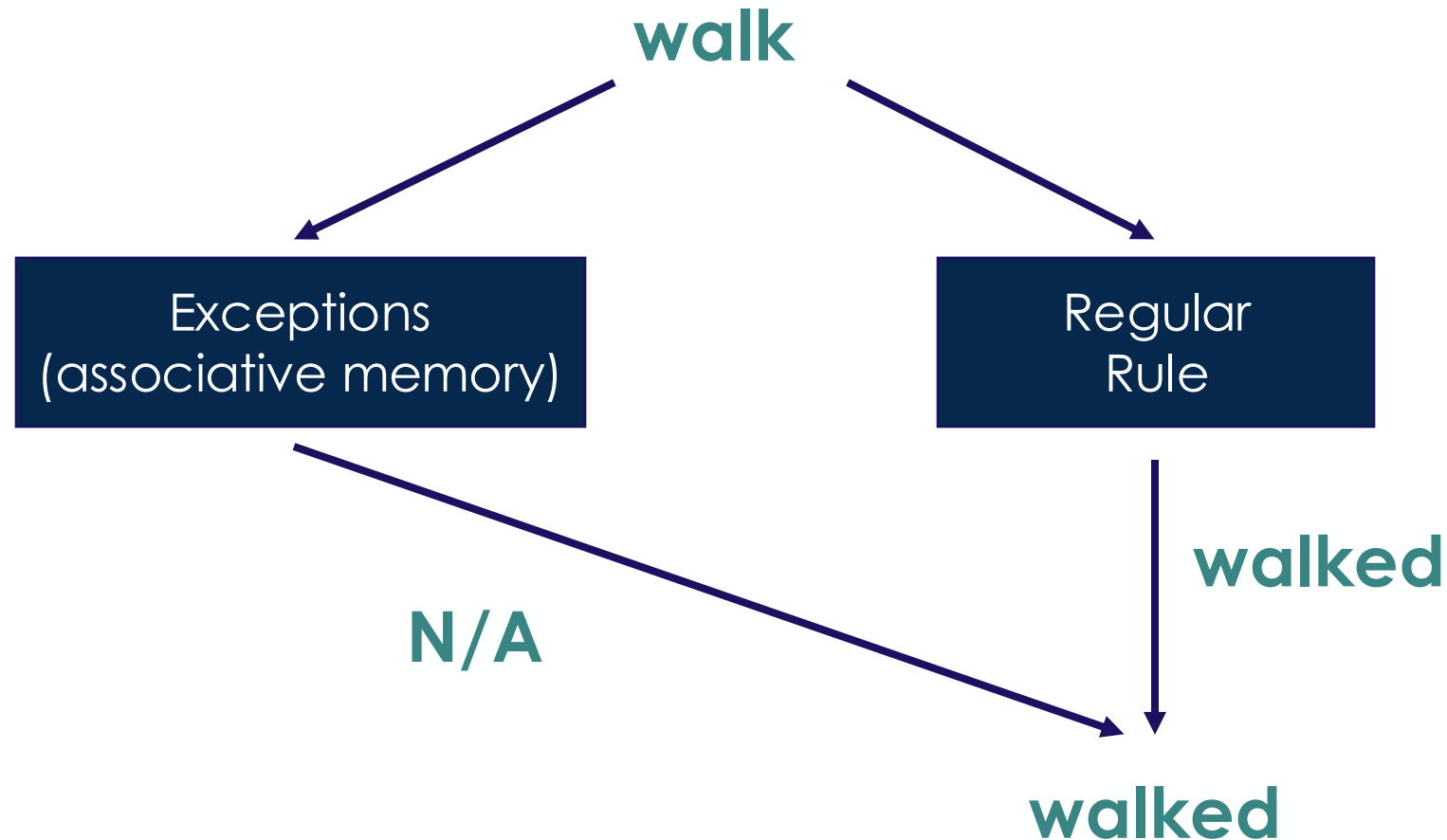
# Background: The Past Tense Debate

Pinker & Prince's *dual-route* model:



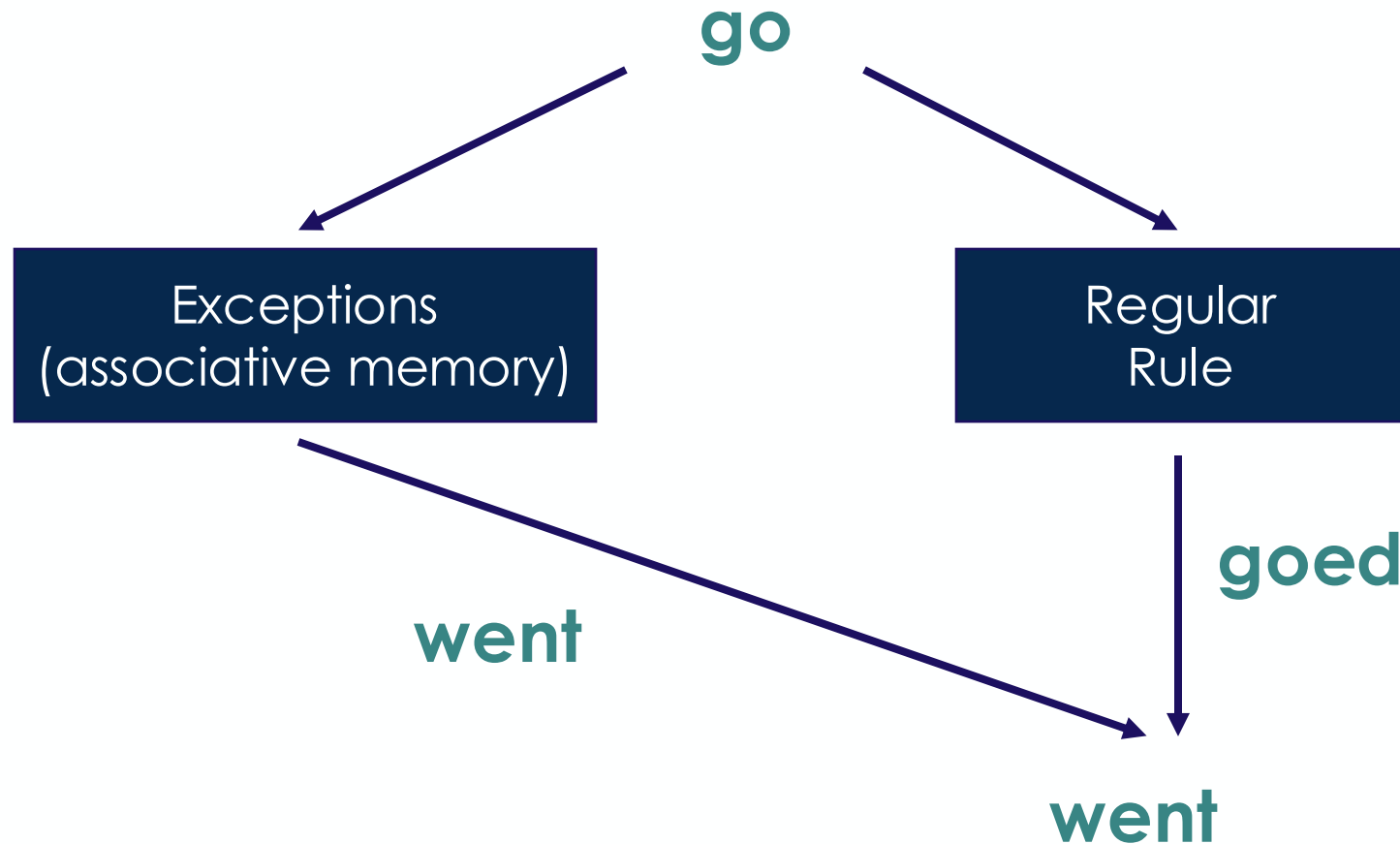
# Background: The Past Tense Debate

Pinker & Prince's *dual-route* model: regular inflection



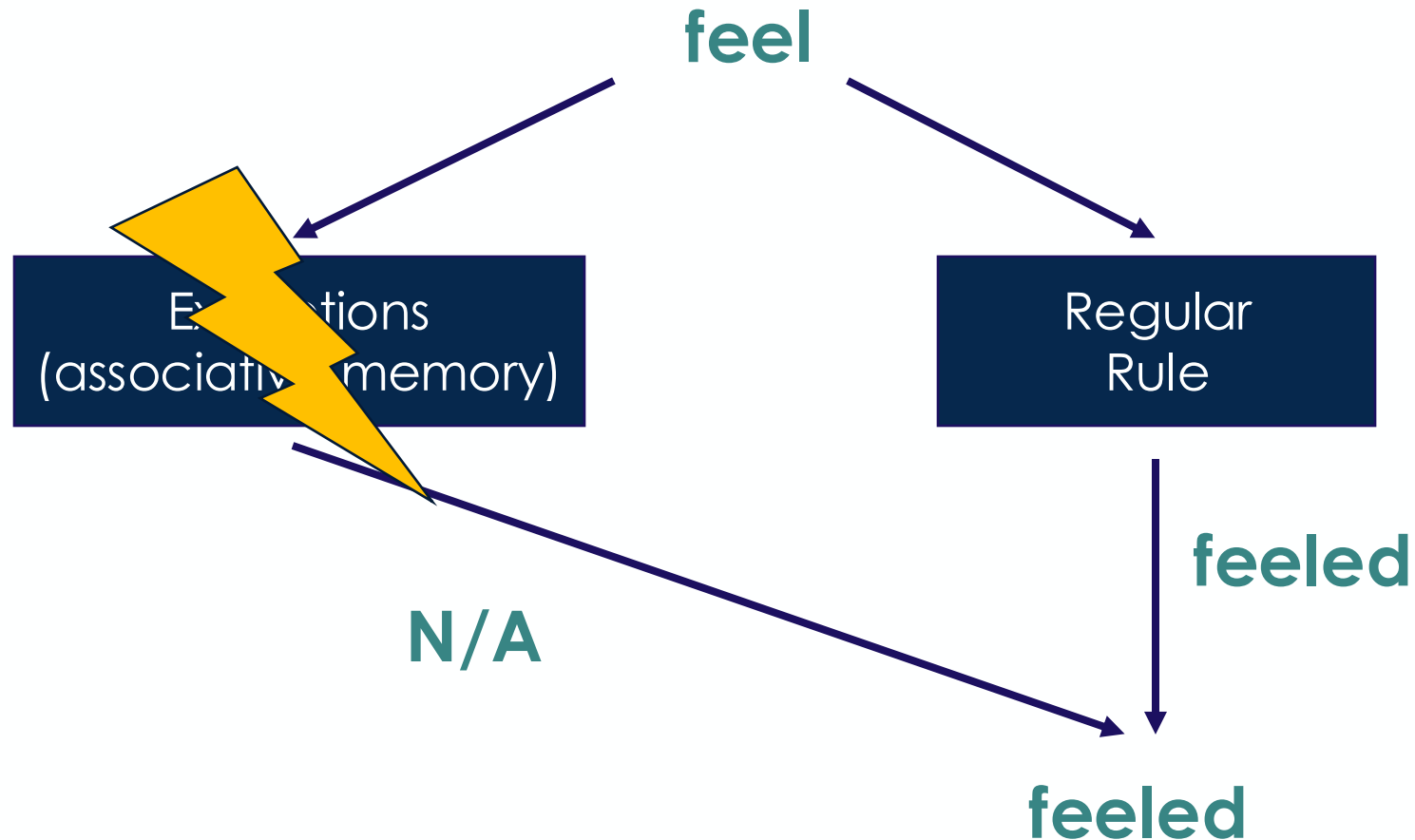
# Background: The Past Tense Debate

Pinker & Prince's *dual-route* model: irregular inflection



# Background: The Past Tense Debate

Pinker & Prince's *dual-route* model: overregularization





# Background: The Past Tense Debate

Pinker & Prince's *dual-route* model:

- Interpretable model of the grammar!
- But how are rules actually learned?

# ATP: German Results

- Correlates better with nonce word predictions than K&C:

	Neuter			Unknown		
	%R	%NR	$\rho$	%R	%NR	$\rho$
-(e)n	0.17	0.04	-0.26	0.19	0.23	0.43
-e	0.27	0.35	-0.14	0.45	0.62	0.01
-Ø	0.11	0.0	0.55	0.07	0.00	0.55
-er	0.44	0.17	0.53	0.29	0.0	0.46
-s	0.01	0.44	0.3	0.01	0.15	0.64
other	0.00	0.00		0.00	0.00	

# ATP: Results

