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\mathbf{1},\mathbf{1},\mathbf{1}
In [143...
           Patrick Ballou
           ID: 801130521
           ECGR 4105
           Homework 1
           Problem 3
           '\nPatrick Ballou\nID: 801130521\nECGR 4105\nHomework 1\nProblem 3\n'
Out[143]:
In [144...
           import numpy as np
           import pandas as pd
           import matplotlib.pyplot as plt
           import seaborn as sns
           from sklearn.model selection import train test split
           from sklearn.preprocessing import MinMaxScaler, StandardScaler
           SS = StandardScaler()
           MM = MinMaxScaler()
In [145... #create pandas dataframe and print first 5 rows
           df = pd.read csv("Housing.csv")
           df_{copy} = df_{copy}()
           df.head()
Out[145]:
                             bedrooms bathrooms stories mainroad guestroom basement hotwaterheating
           0 13300000 7420
                                     4
                                                2
                                                        3
                                                                yes
                                                                            no
                                                                                      no
                                                                                                      n
           1 12250000 8960
                                                4
                                                        4
                                                                yes
                                                                            no
                                                                                      no
                                                                                                      n
           2 12250000 9960
                                     3
                                                2
                                                        2
                                                                yes
                                                                            no
                                                                                      yes
                                                                                                      n
           3 12215000 7500
                                                2
                                                        2
                                                                yes
                                                                            no
                                                                                      yes
           4 11410000 7420
                                     4
                                                1
                                                        2
                                                                yes
                                                                           yes
                                                                                      yes
                                                                                                      n
           #categorical inputs that need to be mapped to numbers
In [146...
           non_num_varlist = ["mainroad", "guestroom", "basement", "hotwaterheating", "airconditi
           #mapping function
           def to num(x):
               return x.map({"yes": 1, "no": 0})
           #map inputs and output new dataframe
In [147...
           df[non_num_varlist] = df_copy[non_num_varlist].apply(to_num) #copy df is to avoid prot
           df.head()
```

```
Out[147]:
                 price area bedrooms bathrooms stories mainroad guestroom basement hotwaterheating
                                                                                   0
           0 13300000
                      7420
                                   4
                                              2
                                                     3
                                                               1
                                                                          0
           1 12250000 8960
                                              4
                                                     4
                                                               1
                                                                          0
                                                                                   0
           2 12250000 9960
                                   3
                                              2
                                                     2
                                                               1
                                                                          0
                                                                                   1
           3 12215000 7500
                                              2
                                                     2
                                                                          0
                                                                                   1
           4 11410000 7420
                                   4
                                              1
                                                     2
                                                               1
                                                                          1
                                                                                   1
 In [148...
          #train/test split, random state functions as seed
           df_train, df_test = train_test_split(df, train_size=.8, test_size=.2, random_state=7)
 In [149... #create arrays of relevent inputs for this problem
           #part a
           vars = ['area', 'bedrooms', 'bathrooms', 'stories', 'parking', 'price']
           train_set = df_train[vars]
           test_set = df_test[vars]
           #part b
           vars_b = ['area', 'bedrooms', 'bathrooms', 'stories', 'mainroad', 'guestroom', 'baseme
           train set b = df train[vars b]
           test set b = df test[vars b]
 In [150...
          #scale two different ways
           #part a
           ss train set = SS.fit transform(train set)
           ss_test_set = SS.fit_transform(test_set)
           mm_train_set = MM.fit_transform(train_set)
           mm test set = MM.fit transform(test set)
           #part b
           ss_train_set_b = SS.fit_transform(train_set_b)
           ss test set b = SS.fit transform(test set b)
           mm train set b = MM.fit transform(train set b)
           mm_test_set_b = MM.fit_transform(test_set_b)
 In [151...
          #create variables for test and train set since they are different sizes
           m train = len(train set)
           m test = len(test set)
           #standard scaler train
           ss Y train = ss train set[:,-1]
           ss_x_train = ss_train_set[:,0:6]
           ss x 0 train = np.ones((m train,1))
           ss_X_train = np.hstack((ss_x_0_train, ss_x_train))
           #standard scaler test
           ss_Y_test = ss_test_set[:,-1]
```

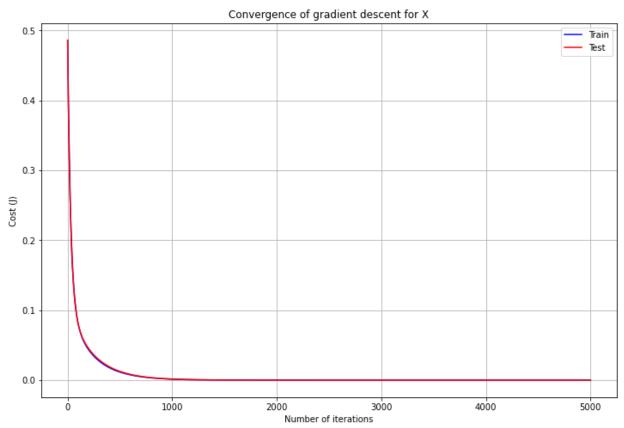
ss\_x\_test = ss\_test\_set[:, 0:6]

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ss \times 0 \text{ test} = np.ones((m \text{ test},1))
          ss_X_test = np.hstack((ss_x_0_test, ss_x_test))
          #min max train
          mm_Y_train = mm_train_set[:,-1]
          mm x train = mm train set[:,0:6]
          mm_x_0_train = np.ones((m_train,1))
          mm_X_train = np.hstack((mm_x_0_train, mm_x_train))
          #Min max test
          mm_Y_test = mm_test_set[:,-1]
          mm_x_test = mm_test_set[:, 0:6]
          mm_x_0_{test} = np.ones((m_{test,1}))
          mm X test = np.hstack((mm x 0 test, mm x test))
In [152... #same thing but for part b
          m_train_b = len(train_set_b)
          m test b = len(test set b)
          #standard scaler train
          ss_Y_train_b = ss_train_set_b[:,-1]
          ss x train b = ss train set b[:,0:12]
          ss x 0 train b = np.ones((m train b,1))
          ss_X_train_b = np.hstack((ss_x_0_train_b, ss_x_train_b))
          #standard scaler test
          ss_Y_test_b = ss_test_set_b[:,-1]
          ss x test b = ss test set b[:, 0:12]
          ss_x_0_{test_b} = np.ones((m_{test_b,1}))
          ss_X_test_b = np.hstack((ss_x_0_test_b, ss_x_test_b))
          #min max train
          mm_Y_train_b = mm_train_set_b[:,-1]
          mm_x_train_b = mm_train_set_b[:,0:12]
          mm_x_0_train_b = np.ones((m_train_b,1))
          mm_X_train_b = np.hstack((mm_x_0_train_b, mm_x_train_b))
          #Min max test
          mm_Y_test_b = mm_test_set_b[:,-1]
          mm_x_{test_b} = mm_{test_set_b} (:, 0:12)
          mm \times 0 \text{ test } b = np.ones((m \text{ test } b, 1))
          mm_X_test_b = np.hstack((mm_x_0_test_b, mm_x_test_b))
In [153... #initialize theta, # of iterations, lambda, and learning rate
          #part a
          iterations = 5000
          ss theta = np.zeros(7)
          ss_alpha = .007
          ss_lambda = .01
          mm theta = np.zeros(7)
          mm = .02
          mm_lambda = .01
```

#part b

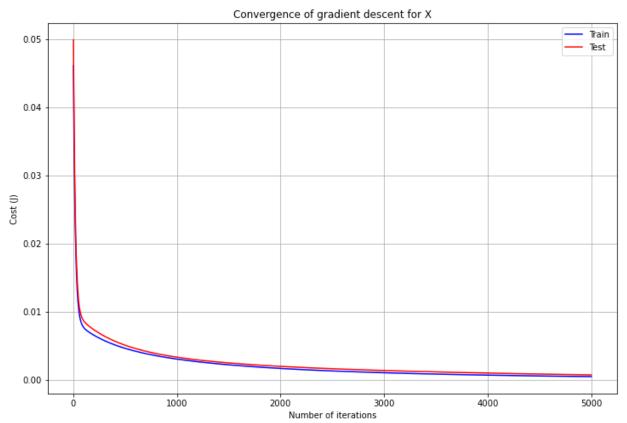
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iterations b = 5000
          ss_theta_b = np.zeros(13)
          ss_alpha_b = .008
          ss lambda b = .01
         mm_theta_b = np.zeros(13)
         mm_alpha_b = .01
         mm_lambda_b = .01
In [154... #initialize cost history arrays
          ss_train_cost_history = np.zeros(iterations)
          ss_test_cost_history = np.zeros(iterations)
         mm_train_cost_history = np.zeros(iterations)
         mm test cost history = np.zeros(iterations)
          ss_train_cost_history_b = np.zeros(iterations_b)
          ss_test_cost_history_b = np.zeros(iterations_b)
         mm_train_cost_history_b = np.zeros(iterations_b)
         mm_test_cost_history_b = np.zeros(iterations_b)
In [155... #loss function
         def compute_cost(X, y, theta, m):
             predictions = X.dot(theta)
             errors = np.subtract(predictions, y)
              sqrErrors = np.square(errors)
             J = (1/(2*m))*np.sum(sqrErrors)
             return J
In [156... | #gradient descent function with parameter penalties
         def gradient_descent(x_train, y_train, x_test, y_test, theta, alpha, iterations, m_tra
             for i in range(iterations):
                  predictions = x_train.dot(theta)
                  errors = np.subtract(predictions, y_train)
                  sum_delta = (alpha/m_train) * (x_train.transpose().dot(errors) + lambda_val*th
                  theta -= sum delta
                  train_cost_history[i] = compute_cost(x_train, y_train, theta, m_train)
                  test_cost_history[i] = compute_cost(x_test, y_test, theta, m_test)
             return theta, train_cost_history, test_cost_history
In [157...
         #part a
         #standard scaler
          ss_theta, ss_train_cost_history, ss_test_cost_history = gradient_descent(ss_X_train, s
          print("Final theta values for part a with standard scaler:", ss_theta)
          #min max
         mm_theta, mm_train_cost_history, mm_test_cost_history = gradient_descent(mm_X_train, n
          print("Final theta values for part b with minmax:", mm_theta)
          #part b
          #standard scaler
          ss_theta_b, ss_train_cost_history_b, ss_test_cost_history_b = gradient_descent(ss_X_tr
          print("Final theta values for part b with standard scaler:", ss_theta_b)
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#min max
         mm_theta_b, mm_train_cost_history_b, mm_test_cost_history_b = gradient_descent(mm_X_tr
         print("Final theta values for part b with min max:", mm theta b)
         Final theta values for part a with standard scaler: [1.09630087e-19 3.34579794e-05 3.
         13108949e-06 2.30000087e-05
          1.90017083e-05 1.04089160e-05 9.99928187e-01]
         Final theta values for part b with minmax: [0.00846087 0.16315827 0.0167544 0.102277
         21 0.0378647 0.02180989
          0.70661407]
         Final theta values for part b with standard scaler: [8.31713901e-20 5.02435226e-05 2.
         42229549e-06 3.74117279e-05
          3.12363430e-05 1.03020582e-05 4.63544621e-06 2.00094575e-05
          1.41884234e-05 2.99677873e-05 1.49921293e-05 1.69864908e-05
          9.99869549e-01]
         Final theta values for part b with min max: [0.00116796 0.15461798 0.04162156 0.13521
         804 0.06933473 0.02519822
          0.01685638 0.02061556 0.04478528 0.04438587 0.05547643 0.0333198
          0.43023494]
         #plot standard scaler train and test loss vs iterations for part a
In [158...
         plt.rcParams["figure.figsize"] = (12,8)
         plt.plot(range(1, iterations + 1), ss_train_cost_history, color='blue', label='Train'
         plt.plot(range(1, iterations + 1), ss_test_cost_history, color='red', label='Test')
         plt.grid()
         plt.legend()
         plt.xlabel('Number of iterations')
         plt.ylabel('Cost (J)')
         plt.title('Convergence of gradient descent for X')
         print("Standard scaler training cost:", ss_train_cost_history[-1])
         print("Standard scaler testing cost:", ss_test_cost_history[-1])
         Standard scaler training cost: 1.1257937437554153e-09
         Standard scaler testing cost: 1.2092123592210432e-09
```



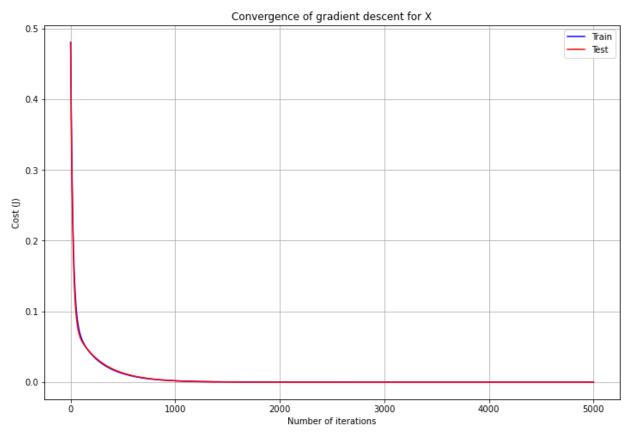
```
In [159... #plot Min max train and test loss vs iterations for part a
   plt.plot(range(1, iterations + 1), mm_train_cost_history, color='blue', label='Train')
   plt.plot(range(1, iterations + 1), mm_test_cost_history, color='red', label='Test')
   plt.grid()
   plt.legend()
   plt.xlabel('Number of iterations')
   plt.ylabel('Cost (J)')
   plt.title('Convergence of gradient descent for X')
   print("Min max training cost:", mm_train_cost_history[-1])
   print("Min max testing cost:", mm_test_cost_history[-1])
```

Min max training cost: 0.0005096466463897371 Min max testing cost: 0.0007646685550530708



```
In [160... #plot standard scaler train and test loss vs iterations for part b
plt.plot(range(1, iterations_b + 1), ss_train_cost_history_b, color='blue', label='Traplt.plot(range(1, iterations_b + 1), ss_test_cost_history_b, color='red', label='Test'plt.grid()
plt.legend()
plt.xlabel('Number of iterations')
plt.ylabel('Cost (J)')
plt.title('Convergence of gradient descent for X')
print("Standard scaler training cost part b:", ss_train_cost_history_b[-1])
print("Standard scaler testing cost part b:", ss_test_cost_history_b[-1])
```

Standard scaler training cost part b: 2.8337931624083455e-09 Standard scaler testing cost part b: 2.9944181125407805e-09



```
In [161... #plot Min max train and test loss vs iterations for part b
   plt.plot(range(1, iterations_b + 1), mm_train_cost_history_b, color='blue', label='Tra
   plt.plot(range(1, iterations_b + 1), mm_test_cost_history_b, color='red', label='Test'
   plt.grid()
   plt.legend()
   plt.vlabel('Number of iterations')
   plt.ylabel('Cost (J)')
   plt.title('Convergence of gradient descent for X')
   print("Min max training cost part b:", mm_train_cost_history_b[-1])
   print("Min max testing cost part b:", mm_test_cost_history_b[-1])
```

Min max training cost part b: 0.001435776583380898 Min max testing cost part b: 0.001589437180705151

