

1 SEARCH FOR  $t\bar{t}Z' \rightarrow t\bar{t}t\bar{t}$  PRODUCTION IN THE MULTILEPTON FINAL STATE IN  
2  $pp$  COLLISIONS AT  $\sqrt{s} = 13$  TEV WITH THE ATLAS DETECTOR

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12

## ABSTRACT

13 This dissertation presents a search for a new beyond-the-Standard-Model (BSM) particle  
14 at the Large Hadron Collider (LHC). Many BSM models predict a new heavy vector boson  
15 ( $Z'$ ) that couples primarily to the top quark in both production and decay (topophilic). The  
16 search is performed in multilepton events consistent with four-top-quark ( $t\bar{t}t\bar{t}$ ) production,  
17 due to the distinctive signature of the multilepton final states and its robustness against  
18 common background processes at the LHC. Analysis data was collected by the ATLAS  
19 detector from 2015 to 2018, using proton-proton collisions at the LHC at a center-of-mass  
20 energy of 13 TeV. No statistically significant deviation from Standard Model predictions is  
21 observed. Exclusion limits are set on the production cross section of the targeted topophilic  
22 particle in the mass range between 1 TeV and 3 TeV.

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## KEY TO ABBREVIATIONS

### Physical & Mathematical Quantities

<sup>239</sup>  $\chi^2$  chi-squared

<sup>240</sup>  $d_0$  transverse impact parameter

<sup>241</sup>  $\Delta R$  angular distance

<sup>242</sup>  $\sqrt{s}$  center-of-mass energy

<sup>243</sup>  $\eta$  pseudorapidity

<sup>244</sup>  $E_T$  transverse energy

<sup>245</sup>  $E_T^{\text{miss}}$  missing transverse energy

<sup>246</sup>  $\Gamma$  decay width

<sup>247</sup>  $\gamma_5$  chirality projection operator

<sup>248</sup>  $\gamma_\mu$  Dirac matrices

<sup>249</sup>  $H_0$  null hypothesis

<sup>250</sup>  $H_T$  scalar sum of transverse momenta  $p_T$  of all objects in an event

<sup>251</sup>  $\mathcal{L}$  Lagrangian

<sup>252</sup>  $\mathcal{L}(\theta)$  likelihood function

<sup>253</sup>  $L$  instantaneous luminosity

<sup>254</sup>  $m_{\ell\ell}$  dilepton invariant mass

<sup>255</sup>  $\mu$  signal strength

<sup>256</sup>  $\mu_F$  factorization scale

<sup>257</sup>  $\mu_R$  renormalization scale

<sup>258</sup>  $N_{\text{jets}}$  number of jets/jet multiplicity

<sup>259</sup>  $\mathcal{O}(n)$  on the order of  $n$

<sup>260</sup>  $\mathcal{P}$  Poisson probability

<sup>261</sup>  $p_T$  transverse momentum

- <sup>262</sup>  $Q$  electric charge  
<sup>263</sup>  $q_\mu$  profile likelihood ratio  
<sup>264</sup>  $\sigma$  standard deviation  
<sup>265</sup>  $\sigma[b]$  cross-section  
<sup>266</sup>  $z_0$  longitudinal impact parameter

## Particles & Processes

- <sup>267</sup>
- <sup>268</sup>  $\gamma^*$  virtual photon  
<sup>269</sup>  $gg$  gluon-gluon fusion  
<sup>270</sup>  $pp$  proton-proton  
<sup>271</sup> PbPb lead-lead  
<sup>272</sup>  $q$  quark  
<sup>273</sup>  $q\bar{q}$  quark-antiquark pair  
<sup>274</sup>  $t\bar{t}$  top/anti-top quark pair  
<sup>275</sup>  $t\bar{t}X$  top pair in association with another particle  
<sup>276</sup>  $t\bar{t}t\bar{t}$  four-top-quark  
<sup>277</sup>  $V$  massive vector bosons ( $W^\pm, Z$ )  
<sup>278</sup>  $H$  Higgs in association with a vector boson

## Acronyms

- <sup>279</sup>
- <sup>280</sup> **1LOS** one lepton, or two leptons of opposite charges  
<sup>281</sup> **2HDM** two-Higgs doublet model  
<sup>282</sup> **AF3** AtlFast3 fast simulation  
<sup>283</sup> **ALICE** A Large Ion Collider Experiment  
<sup>284</sup> **ATLAS** A Toroidal LHC ApparatuS  
<sup>285</sup> **AWAKE** Advanced WAKEfield Experiment  
<sup>286</sup> **BDT** boosted decision tree  
<sup>287</sup> **BR** branching ratio

- <sup>288</sup> **BSM** Beyond the Standard Model
- <sup>289</sup> **CB** combined muon
- <sup>290</sup> **CERN** European Organization for Nuclear Research
- <sup>291</sup> **CKM** Cabibbo-Kobayashi-Maskawa matrix
- <sup>292</sup> **CL** confidence level
- <sup>293</sup> **CMS** Compact Muon Solenoid
- <sup>294</sup> **CP** charge-parity symmetry
- <sup>295</sup> **CR** control region
- <sup>296</sup> **CSC** Cathode Strip Chambers
- <sup>297</sup> **CTP** Central Trigger Processor
- <sup>298</sup> **ECIDS** Electron Charge ID Selector
- <sup>299</sup> **EFT** effective field theory
- <sup>300</sup> **EM** electromagnetic
- <sup>301</sup> **EW** electroweak
- <sup>302</sup> **FASER** ForwArd Search ExpeRiment
- <sup>303</sup> **FCal** forward calorimeter
- <sup>304</sup> **FS** full detector simulation
- <sup>305</sup> **GNN** graph neural network
- <sup>306</sup> **GRL** Good Run List
- <sup>307</sup> **GSC** Global Sequential Calibration
- <sup>308</sup> **GSF** Gaussian-sum filter
- <sup>309</sup> **GUT** Grand Unified Theory
- <sup>310</sup> **HEC** hadronic endcap calorimeter
- <sup>311</sup> **HF** heavy-flavor
- <sup>312</sup> **HL-LHC** High-Luminosity Large Hadron Collider
- <sup>313</sup> **HLT** High-Level Trigger
- <sup>314</sup> **ID** Inner Detector

- <sup>315</sup> **IP** interaction point
- <sup>316</sup> **JER** jet energy resolution
- <sup>317</sup> **JES** jet energy scale
- <sup>318</sup> **JVT** Jet Vertex Tagger
- <sup>319</sup> **KATRIN** Karlsruhe Tritium Neutrino Experiment
- <sup>320</sup> **L1** Level 1
- <sup>321</sup> **LAr** liquid argon
- <sup>322</sup> **LF** light-flavor
- <sup>323</sup> **LH** likelihood
- <sup>324</sup> **LHC** Large Hadron Collider
- <sup>325</sup> **LHCb** Large Hadron Collider beauty
- <sup>326</sup> **LINAC** linear accelerator
- <sup>327</sup> **LLH** log-likelihood
- <sup>328</sup> **LO** leading order
- <sup>329</sup> **MC** Monte Carlo simulation
- <sup>330</sup> **ME** matrix element
- <sup>331</sup> **ML** multilepton
- <sup>332</sup> **MS** Muon Spectrometer
- <sup>333</sup> **MDT** Monitored Drift Tubes
- <sup>334</sup> **MET** missing transverse energy
- <sup>335</sup> **NF** normalization factor
- <sup>336</sup> **NNJvt** Neural Network-based Jet Vertex Tagger
- <sup>337</sup> **NLO** next-to-leading order
- <sup>338</sup> **NNLO** next-to-next-to-leading order
- <sup>339</sup> **NP** nuisance parameter
- <sup>340</sup> **OP** operating point (also working point)
- <sup>341</sup> **OS** opposite-sign

- <sup>342</sup> **PCBT** pseudo-continuous  $b$ -tagging
- <sup>343</sup> **PDF** parton distribution function
- <sup>344</sup> **POI** parameter of interest
- <sup>345</sup> **PS** parton shower
- <sup>346</sup> **PV** primary vertex
- <sup>347</sup> **QCD** quantum chromodynamics
- <sup>348</sup> **QED** quantum electrodynamics
- <sup>349</sup> **QFT** quantum field theory
- <sup>350</sup> **QmisID** charge mis-identification
- <sup>351</sup> **RPC** Resistive Plate Chamber
- <sup>352</sup> **SCT** Semiconductor Tracker
- <sup>353</sup> **SF** scale factor
- <sup>354</sup> **SM** Standard Model
- <sup>355</sup> **SR** signal region
- <sup>356</sup> **SS** same-sign
- <sup>357</sup> **SSB** spontaneous symmetry breaking
- <sup>358</sup> **SS2L** same-sign dilepton
- <sup>359</sup> **SSML** same-sign dilepton, or more than two leptons of any charges
- <sup>360</sup> **TDAQ** Trigger and Data Acquisition
- <sup>361</sup> **TGC** Thin-Gap Chamber
- <sup>362</sup> **TRT** Transition Radiation Tracker
- <sup>363</sup> **VEV** vacuum expectation value
- <sup>364</sup> **VR** validation region
- <sup>365</sup> **UE** underlying-event

# <sup>366</sup> Chapter 1. Introduction

<sup>367</sup> The 20<sup>th</sup> century ushered in a revolutionary period for mankind's understanding of the  
<sup>368</sup> fundamental nature of matter and the forces that govern our universe with the development  
<sup>369</sup> of special relativity and quantum mechanics, which redefined our understanding of space,  
<sup>370</sup> time, energy and matter at the furthest extremes of scale from the vast reaches of the cosmos  
<sup>371</sup> to the tiniest constituents of matter. Building on these principles, Quantum Electrodynamics  
<sup>372</sup> (QED) [4–6] was developed as the first successful quantum field theory (QFT) describing  
<sup>373</sup> electromagnetism. The discovery of beta decay [7] and its paradoxical behaviors within the  
<sup>374</sup> framework of QED prompted the prediction of neutrinos and development of the theory of  
<sup>375</sup> weak interaction.

<sup>376</sup> At around the same time, a spectrum of strongly interacting particles was discovered  
<sup>377</sup> [8] as particle accelerators probed deeper into atomic nuclei, leading to the formation of  
<sup>378</sup> the quark model in the 1960s and with it a hypothesized new binding force, the strong  
<sup>379</sup> force. However, the QFT framework remained incapable of describing the weak and strong  
<sup>380</sup> interactions until advancements in gauge theory and the quantization of non-Abelian gauge  
<sup>381</sup> via QFT resulted in the formation of Yang-Mills theory [9, 10]. This sparked a renaissance  
<sup>382</sup> in modern physics with the unification of electromagnetism and weak force in 1967 under  
<sup>383</sup> the framework of electroweak (EW) [11] theory, as well as the development of Quantum  
<sup>384</sup> Chromodynamics (QCD) [12, 13] to describe the strong force binding quarks.

<sup>385</sup> At this point, the prediction of massless bosons within EW formalism remained a contra-  
<sup>386</sup> diction to the predicted massive  $W^\pm$  and  $Z$  bosons that mediate the weak force. This was  
<sup>387</sup> resolved by the introduction of EW spontaneous symmetry breaking and the Higgs mech-  
<sup>388</sup> anism in 1964 [14–16], which explained the generation of masses for both the EW bosons

389 and fermions. Together, these developments culminated in the Standard Model of parti-  
390 cle physics SM [17], a comprehensive theory that described the electromagnetic, weak, and  
391 strong interactions, classified all known fundamental particles and predicted mathematically  
392 consistent but not yet observed particles. Following its inception, particles predicted by the  
393 Standard Model were gradually observed experimentally, starting with the gluon in 1979  
394 [18], then the  $W^\pm$  and  $Z$  bosons [19, 20], and finally the top quark in 1995 [21, 22]. The  
395 final missing piece was confirmed as the Higgs boson was observed in 2012 independently  
396 by the ATLAS [23] and CMS [24] detectors at the Large Hadron Collider, completing the  
397 Standard Model after a 40-year search and cementing it as the most successful framework  
398 so far describing fundamental constituents of matter and their governing forces.

399 Despite its successes, the Standard Model remains incomplete. Key unanswered questions  
400 include the nature of dark matter [25], which makes up about 27% of the universes energy  
401 content but has no explanation within the Standard Model; the origin of neutrino masses and  
402 their oscillations [26]; the observed matter-antimatter asymmetry in the universe; possible  
403 unification of the EW and strong interaction into a Grand Unified Theory (GUT); and the  
404 hierarchy problem describing the large discrepancy in scales between forces and the apparent  
405 lightness of the Higgs boson compared to values predicted from quantum corrections.

406 After the discovery of the Higgs boson, efforts have been underway to construct new  
407 hypotheses and models in search of beyond the Standard Model (BSM) physics via different  
408 avenues, one of which being direct searches at colliders for new resonances or particles not  
409 predicted by the SM. In particular, the top quark possesses large mass and strong coupling to  
410 the Higgs boson [27] which gives it a special role in many proposed BSM models as a possible  
411 connection with strong coupling to new particles and heavy resonances. In addition, the  
412 top quark has a clean decay signature with well-understood final states and is produced in

abundance at the LHC from  $pp$  collisions in the form of top pairs  $t\bar{t}$  [28, 29]. This dissertation presents a search for the production of a heavy resonance that couples preferentially to top quark (top-philic) in association with a top pair ( $t\bar{t}$ ) in the final state with either two leptons of the same electric charge or at least three leptons (SSML). The search is performed in proton-proton collisions at  $\sqrt{s} = 13$  TeV with the ATLAS detector [30] via the four-top ( $t\bar{t}t\bar{t}$ ) production channel.

A similar search for top-philic heavy resonances was performed using  $t\bar{t}t\bar{t}$  final state containing either one lepton or two opposite-sign leptons (1LOS) [31] with a much larger branching ratio of 56% and larger irreducible background of SM processes. Despite the small cross-section within the SM, the  $t\bar{t}t\bar{t}$  SSML final state provides heightened sensitivity to BSM physics and higher signal-to-background ratio than inclusive resonance searches (e.g. in dijet or dilepton final states) due to the distinctive signal signature and suppression of large SM background processes present in  $t\bar{t}$ -associated production i.e. diboson ( $VV$ ),  $t\bar{t}$  production with an additional boson ( $t\bar{t}V/ttH+jets$ ) or with additional light leptons from heavy-flavor decays ( $t\bar{t} + HF$ ). The cross-section for  $t\bar{t}t\bar{t}$  production can be enhanced by many proposed BSM models including supersymmetric gluino pair-production [32, 33], scalar gluon pair-production [34, 35], top-quark-compositeness models [36, 37], effective field theory (EFT) operators [29, 38–41] and two-Higgs-doublet models (2HDM) [42–46]. Searching within this channel is particularly motivated by the recent observed excess in the measurement of four-top production in the SSML final state at the LHC by the ATLAS detector [47] with a measured cross-section of  $24^{+7}_{-6}$  fb, almost double the SM prediction of  $13.4^{+1.0}_{-1.8}$  fb.

A simplified color-singlet vector boson model [2] is employed for the search to minimize parameter dependency on model choice. Data-driven background estimation methods are implemented for  $t\bar{t}W$ - one of the dominant irreducible backgrounds in the analysis - and

437 the charge misidentification background to rectify mismodeling related to jet multiplicity  
438 in simulated background that were not covered in the previous 1LOS  $t\bar{t}Z'$  search [31] and  
439 SSML  $t\bar{t}H/A \rightarrow t\bar{t}t\bar{t}$  search [48]. These methods are employed similarly to that in previous  
440 SM  $t\bar{t}t\bar{t}$  analyses [47, 49].

441 This dissertation is organized as follows. Chapter 2 presents the formalism of the SM and  
442 relevant BSM concepts. Chapter 3 provides an introduction to the LHC and ATLAS detector.  
443 Chapter 4 describes the reconstruction and identification of physics object from detector  
444 signals. Chapter 5 defines the data and simulated samples used in the analysis. Chapter 6  
445 describes the analysis strategy, including object definition, analysis region description and  
446 background estimation methods. Chapter 7 summarizes the uncertainties involved in the  
447 analysis. Chapter 8 presents the statistical interpretation and analysis results. Finally,  
448 Chapter 9 discusses a summary of the analysis and future outlook.

# 449 Chapter 2. Theoretical Overview

## 450 2.1 The Standard Model

451 The Standard Model of Physics (SM) [50] is currently the most successful formalism to  
452 describe the physical world at a microscopic scale by providing descriptions for all currently  
453 known elementary particles, along with three out of four fundamental forces (electromag-  
454 netism, weak force, strong force) with the exception of gravity. The SM is however not  
455 perfect, and there remain unanswered questions that require development and discovery of  
456 new physics beyond the Standard Model (BSM). This chapter describes an overview of  
457 important components within the SM and relevant BSM aspects for this analysis.

### 458 2.1.1 Elementary particles

459 Elementary particles in the SM can be classified into two groups: bosons consisting  
460 of particles following Bose-Einstein statistics with integer spin, and fermions consisting of  
461 particles following Fermi-Dirac statistics with half-integer spin. Fermions are the building  
462 blocks of composite particles and consequently all known matter, and can be further classified  
463 into quarks & leptons. Bosons act as force mediators for all fundamental forces described by  
464 the SM, and can either be a scalar boson with spin 0 or vector gauge bosons with spin 1. For  
465 each elementary particle, there also exists a corresponding antiparticle with identical mass  
466 and opposite charge (electric or color). Figure 2.1 shows all known elementary particles in  
467 the SM.

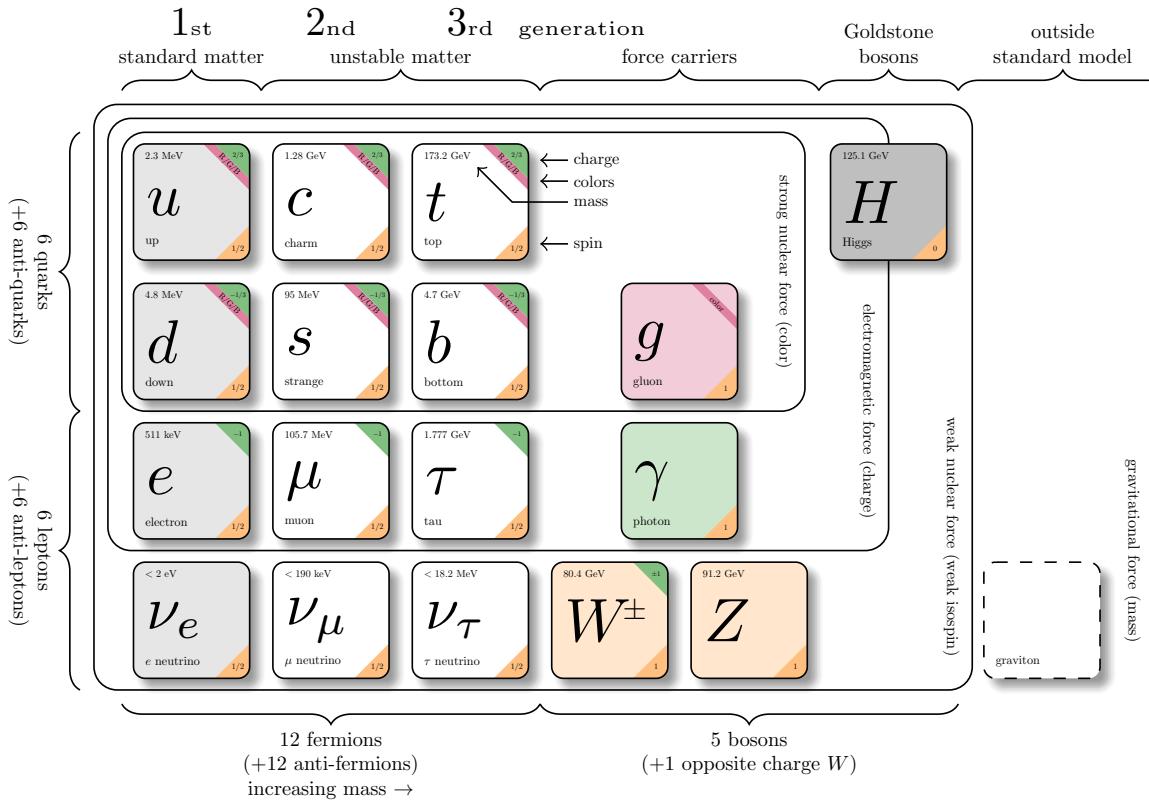


Figure 2.1: Particles within the SM and their properties [51].

## 468 Fermions

469 Fermions consist of quarks and leptons with six flavors each, grouped into three genera-  
 470 tions of doublets. The six quark flavors are up ( $u$ ), down ( $d$ ), charm ( $c$ ), strange ( $s$ ), bottom  
 471 ( $b$ ) and top ( $t$ ), arranged in increasing order of mass. The quark flavors form three doublets  
 472 ( $u, d$ ), ( $c, s$ ) and ( $t, b$ ), with each doublet containing one quark with electric charge of  $+2/3$   
 473 ( $u, s, t$ ), and the other with charge of  $-1/3$  ( $d, c, b$ ). Each quark also possesses a property  
 474 known as color charge, with possible values of red ( $R$ ), green ( $G$ ), blue ( $B$ ) or their corre-  
 475 sponding anticolor ( $\bar{R}, \bar{G}, \bar{B}$ ). Color charge follows color confinement rules, which allows  
 476 only configurations of quarks with total neutral color charge to exist in isolation. Neutral

477 charge configurations can be formed from either a set of three colors ( $R, G, B$ ), a set of a  
478 color and its anticolor, or any combination of the two. Consequently, quarks can only exist  
479 in bound states called hadrons and no isolated quark can be found in a vacuum. Quarks are  
480 the only elementary particles in the SM that can interact with all four fundamental forces.

481 The three leptons doublets consist of three charged leptons: electron ( $e$ ), muon ( $\mu$ ), tau  
482 ( $\tau$ ), and their respective neutrino flavors: electron neutrino ( $\nu_e$ ), muon neutrino ( $\nu_\mu$ ), tau  
483 neutrino ( $\nu_\tau$ ). Charged leptons carry an electric charge of  $-1$ , while their antiparticles carry  
484 the opposite charge ( $+1$ ) and their corresponding neutrino flavors carry no charge. Charged  
485 leptons interact with all fundamental forces except the strong force, while neutrinos only  
486 interact with the weak force and gravity.

## 487 **Bosons**

488 The SM classifies bosons into two types: one scalar boson with spin 0 known as the  
489 Higgs ( $H$ ) boson, and vector gauge bosons with spin 1 known as gluons ( $g$ ), photon ( $\gamma$ ),  $W^\pm$   
490 and  $Z$  bosons [25]. Gluons and photon are massless, while the  $W^\pm$ ,  $Z$  and  $H$  bosons are  
491 massive. Each vector gauge boson serves as the mediator for a fundamental force described  
492 by the SM. Gluons are massless particles mediating the strong interaction by carrying color  
493 charges between quarks following quantum chromodynamics (QCD). Each gluon carries a  
494 non-neutral color charge out of eight linearly independent color states in the gluon color octet  
495 [52]. The photon is the massless and charge-neutral mediator particle for the electromagnetic  
496 interaction following quantum electrodynamics (QED). The  $W^\pm$  and  $Z$  bosons are massive  
497 mediator particles for the weak interaction, with the  $W^\pm$  boson carrying an electric charge  
498 of  $\pm 1$  while the  $Z$  boson is charge neutral.

499 Other than the vector gauge boson, the only scalar boson in the SM is the massive and

500 charge neutral Higgs boson [25]. The Higgs boson does not mediate any fundamental force  
 501 like vector bosons, but serve to provide the rest mass for all massive elementary particles in  
 502 the SM through the Higgs mechanism described in section 2.1.2.3.

503 **Top quark**

504 As of now, the top quark ( $t$ ) is the heaviest particle in the SM with mass of about 173 GeV  
 505 [53], approaching the EW symmetry breaking scale. Its high mass gives the top quark the  
 506 strongest Yukawa coupling to the Higgs boson ( $y_t \approx 1$ ) [27] and exotic resonances in many  
 507 proposed BSM models [54–57], making the top quark and its processes attractive vehicles  
 508 with which to probe new physics.

509 Due to its mass, the top quark has a  
 510 very short lifetime of  $10^{-24}$  s [25] and de-  
 511 cays before it can hadronize following color  
 512 confinement. The top quark decays to a  $W$   
 513 boson and a  $b$ -quark with a branching ratio  
 514 of almost 100%. The  $W$  boson can subse-  
 515 quently decay to a quark-antiquark pair or  
 516 to a lepton-neutrino pair (Figure 2.2), with  
 517 branching ratios of approximately 68% and  
 518 32% respectively. All lepton flavors have  
 519 similar branching ratios during a leptonic  $W$   
 520 decay.

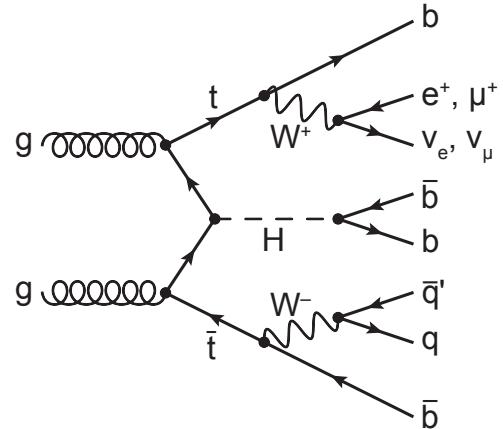


Figure 2.2: Feynman diagram for  $t\bar{t}$  production and subsequent decay processes [58]. Top quark decays into a  $W$ -boson and  $b$ -quarks, and  $W$ -boson can decay to a  $q\bar{q}$  or a  $\ell\nu_\ell$  pair.

### 521 2.1.2 Mathematical formalism

522 The SM can be described within the formalism of quantum field theory (QFT) with the  
 523 Lagrangian [59]

$$\mathcal{L}_{\text{SM}} = \mathcal{L}_{\text{QCD}} + \underbrace{(\mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{fermion}} + \mathcal{L}_{\text{Higgs}} + \mathcal{L}_{\text{Yukawa}})}_{\mathcal{L}_{\text{EW}}} \quad (2.1)$$

524 where  $\mathcal{L}_{\text{QCD}}$  is the QCD term and  $\mathcal{L}_{\text{EW}}$  is the electroweak (EW) term of the Lagrangian.  
 525 Formalism of QFT within the SM treats particles as excitations [60] of their corresponding  
 526 quantum fields i.e. fermion field  $\psi$ , electroweak boson fields  $W_{1,2,3}$  &  $B$ , gluon fields  $G_\alpha$  and  
 527 Higgs field  $\phi$ .

528 The foundation of modern QFT involves gauge theory. A quantum field has gauge sym-  
 529 metry if there exists a continuous gauge transformation that when applied to every point in  
 530 a field (local gauge transformation) leaves the field Lagrangian unchanged. The set of gauge  
 531 transformations of a gauge symmetry is the symmetry group of the field which comes with  
 532 a set of generators, each with a corresponding gauge field. Under QFT, the quanta of these  
 533 gauge fields are called gauge bosons.

534 The SM Lagrangian is gauge invariant under global Poincaré symmetry and local  $SU(3)_C \times$   
 535  $SU(2)_L \times U(1)_Y$  gauge symmetry, with the  $SU(3)_C$  symmetry group corresponding to the  
 536 strong interaction and  $SU(2)_L \times U(1)_Y$  to the EW interaction. Global Poincaré symmetry  
 537 ensures that  $\mathcal{L}_{\text{SM}}$  satisfies translational symmetry, rotational symmetry and Lorentz boost  
 538 frame invariance [61]. These symmetries give rise to corresponding conservation laws, which  
 539 lead to conservation of momentum, angular momentum and energy in the SM as a result of  
 540 Noether's theorem [62].

541    **2.1.2.1    Quantum chromodynamics**

542    Quantum chromodynamics is a non-Abelian gauge theory i.e. Yang-Mills theory [9, 10]  
 543    describing the strong interaction between quarks in the SM with the gauge group  $SU(3)_C$ ,  
 544    where  $C$  represents conservation of color charge under  $SU(3)_C$  symmetry. According to  
 545    QFT, quarks can be treated as excitations of the corresponding quark fields  $\psi$ . The free Dirac  
 546    Lagrangian for the quark fields  $\mathcal{L}_0 = \bar{\psi}(i\gamma^\mu\partial_\mu - m)\psi$  is invariant under global  $SU(3)$  sym-  
 547    metry, but not under local  $SU(3)_C$  symmetry. To establish invariance under local  $SU(3)_C$   
 548    symmetry, the gauge covariant derivative  $D_\mu$  is defined so that

$$D_\mu\psi = (\partial_\mu - ig_s G_\mu^a T_a)\psi, \quad (2.2)$$

549    where  $g_s = \sqrt{4\pi\alpha_s}$  is the QCD coupling constant,  $G_\mu^a(x)$  are the eight gluon fields, and  
 550     $T_a$  are generators of  $SU(3)_C$ , represented as  $T_a = \lambda_a/2$  with  $\lambda_a$  being the eight Gell-Mann  
 551    matrices [52]. Let the gluon field strength tensors  $G_{\mu\nu}^a$  be

$$G_{\mu\nu}^a \equiv \partial_\mu G_\nu^a - \partial_\nu G_\mu^a - g_s f^{abc} G_\mu^b G_\nu^c, \quad (2.3)$$

552    where  $f^{abc}$  are the structure constants of  $SU(3)_C$ . The gauge invariant QCD Lagrangian  
 553    can then be written as

$$\begin{aligned} \mathcal{L}_{\text{QCD}} &= \bar{\psi}(i\gamma^\mu D_\mu - m)\psi - \frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu} \\ &= \underbrace{-\frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu}}_{\text{gluon kinematics}} + \underbrace{\bar{\psi}(i\gamma^\mu\partial_\mu - m)\psi}_{\text{quark kinematics}} + \underbrace{\bar{\psi}^i(g_s\gamma^\mu(T_a)_{ij}G_\mu^a)\bar{\psi}^j}_{\text{quark-gluon interaction}} \end{aligned} \quad (2.4)$$

<sup>554</sup> where  $i, j$  are color indices with integer values from 1 to 3. Gluons are forced to be massless  
<sup>555</sup> from the lack of a gluon mass term to maintain gauge invariance for the Lagrangian.

<sup>556</sup> **2.1.2.2 Electroweak theory**

<sup>557</sup> The electroweak interaction is the unified description of the weak interaction and electro-  
<sup>558</sup> magnetism under the  $SU(2)_L \times U(1)_Y$  symmetry group, where  $L$  represents the left-handed  
<sup>559</sup> chirality of the weak interaction and  $Y$  represents the weak hypercharge quantum number.  
<sup>560</sup> Fermions can have either left-handed or right-handed chirality with the exception of neutr-  
<sup>561</sup>inos which can only have left-handed chirality within the SM framework. Fermions in the  
<sup>562</sup> SM can be divided into left-handed doublets and right-handed singlets

$$\psi_L = \begin{pmatrix} \nu_e \\ e_L \end{pmatrix}, \begin{pmatrix} \nu_\mu \\ \mu_L \end{pmatrix}, \begin{pmatrix} \nu_\tau \\ \tau_L \end{pmatrix}, \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \begin{pmatrix} c_L \\ s_L \end{pmatrix}, \begin{pmatrix} t_L \\ b_L \end{pmatrix} \quad (2.5)$$

$$\psi_R = e_R, \mu_R, \tau_R, u_R, d_R, c_R, s_R, t_R, b_R.$$

<sup>563</sup> where  $g'$  is the  $B_\mu$  coupling constant and  $B_\mu(x)$  is a vector gauge field that transforms under  
<sup>564</sup>  $U(1)_Y$  as

$$B_\mu \rightarrow B_\mu + \frac{1}{g'} \partial_\mu \theta(x). \quad (2.6)$$

<sup>565</sup> Right-handed fermion singlets are not affected by  $SU(2)_L$  transformation, so the fermion  
<sup>566</sup> fields  $\psi$  transform under  $SU(2)_L$  as

$$\psi_L \rightarrow e^{iI_3\vec{\theta}(x)\cdot\vec{\sigma}/2}\psi_L \quad (2.7)$$

$$\psi_R \rightarrow \psi_R.$$

<sup>567</sup> where  $\vec{\sigma}/2$  are generators of  $SU(2)_L$  with  $\vec{\sigma}$  being the Pauli matrices. In order to preserve  
<sup>568</sup> local symmetry, the gauge covariant derivative for  $SU(2)_L$  and  $U(1)_Y$  can be defined [63] so

<sup>569</sup> that the gauge covariant derivative for  $SU(2)_L \times U(1)_Y$  can be written as

$$\begin{aligned} D_\mu \psi_L &= \left( \partial_\mu - ig' \frac{Y_L}{2} B_\mu - ig \frac{\sigma_i}{2} W_\mu^i \right) \psi_L \\ D_\mu \psi_R &= \left( \partial_\mu - ig' \frac{Y_R}{2} B_\mu \right) \psi_R. \end{aligned} \quad (2.8)$$

<sup>570</sup> where  $B_\mu(x)$  is a vector gauge field associated with  $U(1)_Y$  and  $W_\mu^i(x)$  ( $i = 1, 2, 3$ ) are three  
<sup>571</sup> vector gauge fields associated with  $SU(2)_L$ . The  $B_\mu$  and  $W_\mu^i$  gauge fields transform under  
<sup>572</sup> their corresponding symmetry groups  $U(1)_Y$  and  $SU(2)_L$  as

$$\begin{aligned} B_\mu &\rightarrow B_\mu + \frac{1}{g'} \partial_\mu \theta(x) \\ W_\mu^i &\rightarrow W_\mu^i + \frac{2}{g} \partial_\mu \theta_a(x) + \epsilon^{ijk} \theta_j(x) W_\mu^k, \end{aligned} \quad (2.9)$$

<sup>573</sup> where  $g'$  is the  $B_\mu$  gauge coupling constant,  $g$  is the  $W_\mu^i$  gauge coupling constants and  $\epsilon^{ijk}$   
<sup>574</sup> is the  $SU(2)_L$  structure constant. Similar to section 2.1.2.1, the kinetic term is added by  
<sup>575</sup> defining field strengths for the four gauge fields

$$\begin{aligned} B_{\mu\nu} &\equiv \partial_\mu B_\nu - \partial_\nu B_\mu \\ W_{\mu\nu}^i &\equiv \partial_\mu W_\nu^i - \partial_\nu W_\mu^i - g e^{ijk} W_\mu^j W_\nu^k. \end{aligned} \quad (2.10)$$

<sup>576</sup> The local  $SU(2)_L \times U(1)_Y$  invariant EW Lagrangian [63] is then

$$\begin{aligned} \mathcal{L}_{\text{EW}} &= i\bar{\psi}(\gamma^\mu D_\mu)\psi - \frac{1}{4}W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4}B_{\mu\nu} B^{\mu\nu} \\ &= \underbrace{i\bar{\psi}(\gamma^\mu \partial_\mu)\psi}_{\text{fermion kinematics}} - \underbrace{\bar{\psi}\left(\gamma^\mu g' \frac{Y}{2} B_\mu\right)\psi}_{\text{fermion-gauge boson interaction}} - \underbrace{\bar{\psi}_L\left(\gamma^\mu g \frac{\sigma_i}{2} W_\mu^i\right)\psi_L}_{\text{boson kinematics \& self-interaction}} - \underbrace{\frac{1}{4}W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4}B_{\mu\nu} B^{\mu\nu}}_{\text{boson kinematics \& self-interaction}}. \end{aligned} \quad (2.11)$$

577 Under  $\approx 159.5$  GeV, the EW symmetry  $SU(2)_L \times U(1)_Y$  undergoes spontaneous symmetry  
 578 breaking [64] into  $U(1)_{\text{QED}}$  symmetry, which corresponds to a separation of the weak and  
 579 electrodynamic forces. Electroweak spontaneous symmetry breaking replaces the four mass-  
 580 less and similarly-behaved EW gauge bosons  $B_\mu$  and  $W_\mu^i$  with the EM boson  $\gamma$  and the weak  
 581 bosons  $Z/W^\pm$ , as well as giving the  $Z$  and  $W^\pm$  bosons masses via the Higgs mechanism.  
 582 This is due to a specific choice of gauge for the Higgs field leading to the reparameterization  
 583 of the EW bosons  $B_\mu$  and  $W_\mu^i$  to  $W^\pm/Z/\gamma$  using the relations

$$\begin{aligned}
 W_\mu^\pm &\equiv \frac{1}{\sqrt{2}} (W_\mu^1 \mp iW_\mu^2) \\
 \begin{pmatrix} A_\mu \\ Z_\mu \end{pmatrix} &\equiv \begin{pmatrix} \cos \theta_W & \sin \theta_W \\ -\sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} B_\mu \\ W_\mu^3 \end{pmatrix}
 \end{aligned} \tag{2.12}$$

584 where  $\theta_W \equiv \cos^{-1} (g/\sqrt{g^2 + g'^2})$  is the weak mixing angle. The boson kinetic term can also  
 585 be refactorized to extract cubic (three vertices) and quartic (four vertices) self-interactions  
 586 among the gauge bosons [63]. The Lagrangian can then be rewritten as

$$\begin{aligned}
 \mathcal{L} = & \underbrace{eA_\mu \bar{\psi} (\gamma^\mu Q) \psi}_{\text{electromagnetism}} + \underbrace{\frac{e}{2 \sin \theta_W \cos \theta_W} \bar{\psi} \gamma^\mu (v_f - a_f \gamma_5) \psi Z_\mu}_{\text{neutral current interaction}} \\
 & + \underbrace{\frac{g}{2\sqrt{2}} \sum_{\psi_L} [\bar{f}_2 \gamma^\mu (1 - \gamma_5) f_1 W_\mu^+ + \bar{f}_1 \gamma^\mu (1 - \gamma_5) f_2 W_\mu^-]}_{\text{charged current interaction}} \\
 & + \underbrace{\mathcal{L}_{\text{kinetic}} + \mathcal{L}_{\text{cubic}} + \mathcal{L}_{\text{quartic}}}_{\text{boson self-interaction}}
 \end{aligned} \tag{2.13}$$

587 where  $\gamma_5 = i\gamma^0\gamma^1\gamma^2\gamma^3$  is the chirality projection operator,  $a_f = I_3$ ,  $v_f = I_3(1 - 4|Q| \sin^2 \theta_W)$   
 588 and  $f_1, f_2$  are up and down type fermions of a left-handed doublet.

589    **2.1.2.3 Higgs mechanism**

590    So far, the EW bosons are massless since the mass terms  $-m\bar{\psi}\psi$  for fermions and  
 591     $-mA^\mu A_\mu$  for bosons are not invariant under the EW Lagrangian symmetries. The parti-  
 592    cles must then acquire mass under another mechanism. The Brout-Engler-Higgs mechanism  
 593    [14–16] was introduced in 1964 to rectify this issue and verified in 2012 with the discovery  
 594    of the Higgs boson [23, 24].

595    The Higgs potential is expressed as

$$V(\phi^\dagger \phi) = \mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2 \quad (2.14)$$

596    where  $\mu^2$  and  $\lambda > 0$  are arbitrary parameters, and the  $SU(2)_L$  doublet  $\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$  is the Higgs  
 597    field with complex scalar fields  $\phi^+$  and  $\phi^0$  carrying +1 and 0 electric charge respectively.

598    The Lagrangian for the scalar Higgs field is

$$\mathcal{L}_H = (\partial_\mu \phi)^\dagger (\partial^\mu \phi) - V(\phi^\dagger \phi). \quad (2.15)$$

599    Since the potential  $V(\phi^\dagger \phi)$  is constrained by  $\lambda > 0$ , the ground state is solely controlled by  
 600     $\mu$ . If  $\mu^2 > 0$ , the ground state energy is  $\phi = 0$ , and the EW bosons would remain massless.  
 601    If  $\mu^2 < 0$ , the ground state is

$$|\phi|^2 = -\frac{\mu^2}{2\lambda} \equiv \frac{v^2}{\sqrt{2}}, \quad (2.16)$$

602    where  $v$  is defined as the vacuum expectation value (VEV). The standard ground state for  
 603    the Higgs potential without loss of generality can be chosen as  $\phi(0) = 1/\sqrt{2}(0)_v$ .

604    Having  $U(1)$  symmetry allows any  $-e^{i\theta} \sqrt{\mu^2/\lambda}$  to be a ground state energy for the Higgs

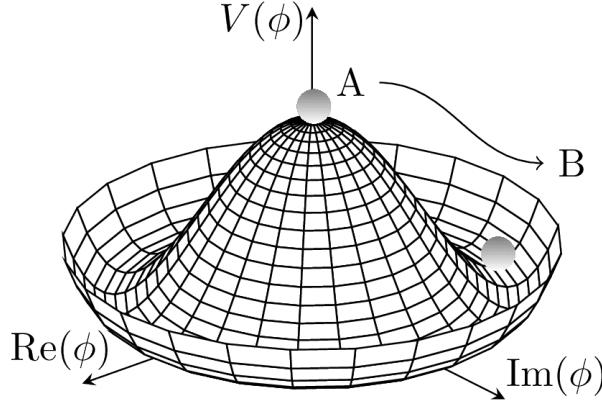


Figure 2.3: Illustration of a common representation of the Higgs potential [65]. Before SSB, the ground state  $\phi(0)$  is located at A which is symmetric with respect to the potential. A perturbation to this state fixes the ground state energy  $|\phi(0)|^2$  to a particular value at B, "spontaneously" breaking the symmetry and degeneracy in  $|\phi(0)|^2$ .

605 Lagrangian. This degeneracy results in spontaneous symmetry breaking of the  $SU(2)_L \times$   
 606  $U(1)_Y$  symmetry into  $U(1)_{\text{EM}}$  symmetry when the Higgs field settles on a specific vacuum  
 607 state as a result of a perturbation or excitation (Figure 2.3). The spontaneous symmetry  
 608 breaking introduces three massless (Nambu-Goldstone [66]) vector gauge boson  $\xi$  and a  
 609 massive scalar boson  $\eta$ , each corresponds to a generator of the gauge group. The vector field  
 610 for  $\xi$  and  $\eta$  are real fields parameterized as  $\xi \equiv \phi^+ \sqrt{2}$  and  $\eta \equiv \phi^0 \sqrt{2} - v$  [67]. The Higgs  
 611 field now becomes

$$\phi = \frac{v + \eta + i\xi}{\sqrt{2}} = \frac{1}{\sqrt{2}} e^{i\xi} \cdot \frac{\sigma}{2v} \begin{pmatrix} 0 \\ v + \eta \end{pmatrix}. \quad (2.17)$$

612 Due to  $U(1)_{\text{EM}}$  invariance, a unitary gauge with the transformation  $\phi \rightarrow \exp(-i\xi \cdot) \frac{\sigma}{2v}$  can  
 613 be chosen for the Higgs field to eliminate the massless bosons and incorporate them into the  
 614 EM/weak bosons via Equation 2.12. This leaves the massive  $\eta$  which can now be observed as  
 615 an excitation of the Higgs field from the standard ground state and must be the Higgs boson  
 616  $h$ . Using the EW covariant derivative from Equation 2.8, the Higgs Lagrangian around the

617 vacuum state becomes

$$\begin{aligned}\mathcal{L}_H &= (D_\mu \phi)^\dagger (D^\mu \phi) - \mu^2 \left( \frac{v+h}{\sqrt{2}} \right)^2 - \lambda \left( \frac{v+h}{\sqrt{2}} \right)^4 \\ &= (D_\mu \phi)^\dagger (D^\mu \phi) - \frac{1}{2} \mu^2 h^2 - \lambda v h^3 - \frac{\lambda}{4} h^4 - \dots\end{aligned}\tag{2.18}$$

618 The Higgs mass can be extracted from the quadratic term as  $m_H = \sqrt{-2\mu^2}$ . The kinetic

619 term in the Lagrangian can be written as

$$\begin{aligned}(D_\mu \phi)^\dagger (D^\mu \phi) &= \frac{1}{2} (\partial_\mu h)^2 + \frac{g^2}{8} (v+h)^2 \left| W_\mu^1 - i W_\mu^2 \right|^2 + \frac{1}{8} (v+h)^2 (g' W_\mu - g B_\mu) \\ &= \frac{1}{2} (\partial_\mu h)^2 + (v+h)^2 \left( \frac{g^2}{4} W_\mu^+ W^{-\mu} + \frac{1}{8} (g^2 + g'^2) Z_\mu^0 Z^{0\mu} \right).\end{aligned}\tag{2.19}$$

620 Masses for the EW bosons can be extracted from the quadratic terms

$$m_{W^\pm} = \frac{v}{2} g, \quad m_Z = \frac{v}{2} \sqrt{g^2 + g'^2}, \quad m_\gamma = 0.\tag{2.20}$$

621 However, the fermion mass term  $-m\bar{\psi}\psi$  still breaks EW invariance after spontaneous symmetry breaking. Instead, fermions acquire mass by replacing the mass term with a gauge invariant Yukawa term in the EW Lagrangian representing fermions' interactions with the 623 Higgs field [67]

$$\begin{aligned}\mathcal{L}_{\text{Yukawa}} &= -c_f \frac{v+h}{\sqrt{2}} (\bar{\psi}_R \psi_L + \bar{\psi}_L \psi_R) \\ &= -\underbrace{\frac{c_f}{\sqrt{2}} v (\bar{\psi} \psi)}_{\text{fermion mass}} - \underbrace{\frac{c_f}{\sqrt{2}} (h \bar{\psi} \psi)}_{\text{fermion-Higgs interaction}},\end{aligned}\tag{2.21}$$

625 where  $c_f$  is the fermion-Higgs Yukawa coupling. The fermion mass is then  $m_f = c_f v / \sqrt{2}$ .

## 626 2.2 Beyond the Standard Model: $t\bar{t}Z' \rightarrow t\bar{t}t\bar{t}$

627 This analysis uses the  $t\bar{t}t\bar{t}$  final state signal signature to search for the existence of a  
628 heavy neutral BSM resonance that couples strongly to the top quark, nominally named  
629  $Z'$ . The cross-section for  $t\bar{t}t\bar{t}$  production at the LHC can be enhanced by many possible  
630 BSM models, in particular production of heavy scalars and pseudoscalar bosons predicted in  
631 Type-II two-Higgs-doublet models (2HDM) [42–46] or possible production of a heavy neutral  
632 resonance boson  $Z'(\rightarrow t\bar{t})$  in association with a  $t\bar{t}$  pair [68, 69]. The  $t\bar{t}Z'$  production mode  
633 and consequently  $t\bar{t}t\bar{t}$  signal signature can provide a more sensitive channel for searches by  
634 avoiding contamination from the large SM  $gg \rightarrow t\bar{t}$  background in an inclusive  $Z' \rightarrow t\bar{t}$   
635 search.

### 636 2.2.1 Top-philic vector resonance

637 Many BSM models extend the SM by adding to the SM gauge group additional  $U(1)'$   
638 gauge symmetries [70, 71], each with an associated vector gauge boson ( $Z'$ ). In the case of  
639 a BSM global symmetry group with rank larger than the SM gauge group, the symmetry  
640 group can spontaneously break into  $G_{\text{SM}} \times U(1)'^n$ , where  $G_{\text{SM}}$  is the SM gauge group  
641  $SU(3)_C \times SU(2)_L \times U(1)_Y$  and  $U(1)'^n$  is any  $n \geq 1$  number of  $U(1)'$  symmetries. The  
642 existence of additional vector boson(s)  $Z'$  would open up many avenues of new physics e.g.  
643 extended Higgs sectors from  $U(1)'$  symmetry breaking [72, 73], existence of flavor-changing  
644 neutral current (FCNC) mediated by  $Z'$  [74], and possible exotic production from heavy  $Z'$   
645 decays [75].

646 Due to the top quark having the largest mass out of all known elementary particles in the  
647 SM, many BSM models [3, 41–46, 76] predict 'top-philic' vector resonances that have much

648 stronger coupling to the top quark compared to other quarks. Previous BSM  $t\bar{t}t\bar{t}$  search at  
 649 the LHC for top-philic resonances [31] with a similar model in the single-lepton final state  
 650 and similar mass ranges set upper limits on observed (expected)  $Z'$  production cross section  
 651 between 21 (14) fb to 119 (86) fb depending on parameter choice. This analysis is also moti-  
 652 vated by the recent observation of SM  $t\bar{t}t\bar{t}$  production in the same-sign multilepton (SSML)  
 653 channel by ATLAS [47] and CMS [77] at  $6.1\sigma$  and  $5.6\sigma$  discovery significance respectively.  
 654

A simplified top-philic color-singlet vector particle model [2, 3] is employed in the search.  
 655 The interaction Lagrangian assumes the  $Z'$  couples dominantly the top quark and has the  
 656 form

$$\begin{aligned}\mathcal{L}_{Z'} &= \bar{t}\gamma_\mu(c_L P_L + c_R P_R) t Z'^\mu \\ &= c_t \bar{t}\gamma_\mu (\cos\theta P_L + \sin\theta P_R) t Z'^\mu,\end{aligned}\tag{2.22}$$

657 where  $c_t = \sqrt{c_L^2 + c_R^2}$  is the  $Z'$ -top coupling strength,  $P_{L/R} = (1 \mp \gamma_5)/2$  are the chirality  
 658 projection operators, and  $\theta = \tan^{-1}(c_R/c_L)$  is the chirality mixing angle. Expanding the  
 659 Lagrangian results in

$$\mathcal{L}_{Z'} = \frac{1}{\sqrt{2}} \bar{t}\gamma_\mu \left[ \sin\left(\theta + \frac{\pi}{4}\right) - \left( \sqrt{2} \cos\left(\theta + \frac{\pi}{4}\right) \right) \gamma_5 \right] t Z'^\mu,\tag{2.23}$$

660 which bears striking resemblance to the EW Lagrangian neutral current interaction term in  
 661 Equation 2.13, showing the similarity between the  $Z'$  and the  $Z$  boson that acquires mass  
 662 from  $SU(2)_L \times U(1)_Y$  spontaneous symmetry breaking. Assuming the  $Z'$  mass  $m_{Z'}$  is much  
 663 larger than the top mass ( $m_t^2/m_{Z'}^2 \approx 0$ ), the  $Z'$  decay width at leading-order (LO) can be  
 664 approximated as

$$\Gamma(Z' \rightarrow t\bar{t}) \approx \frac{c_t^2 m_{Z'}}{8\pi}.\tag{2.24}$$

665 It can be observed that  $\Gamma/m_{Z'} \approx c_t^2/8\pi \ll 1$  for  $c_t \approx 1$ , which suggests a very narrow and  
 666 well-defined resonance peak, validating the narrow-width approximation for the choice of  
 667  $c_t = 1$ .

## 668 2.2.2 Production channels

669 The main production channels at the LHC proton-proton collider for the aforementioned  
 670 heavy topophilic color singlet  $Z'$  are at tree level and loop level, with the one-loop level  
 671 being the dominant processes [2]. Loop level processes are dependent on the chirality angle  
 672  $\theta$ , where  $\theta = \pi/4$  suppresses all but gluon-initiated box sub-processes. To minimize model  
 673 dependence, only the tree level production was considered for this analysis by choosing  
 674  $\theta = \pi/4$ . Figure 2.4 illustrates several tree level  $Z'$  production processes.

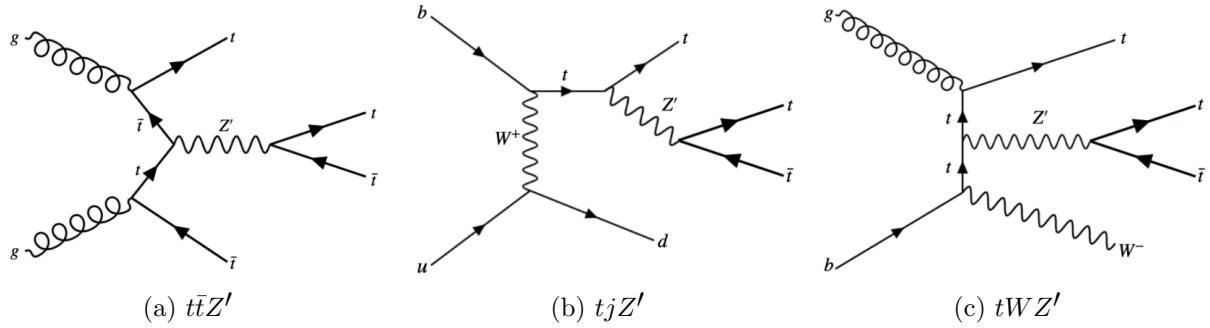


Figure 2.4: Feynman diagrams for tree level  $Z'$  production in association with (a)  $t\bar{t}$ , (b)  $tj$  (light quark) and (c)  $tW$ , decaying to final states containing (a)  $t\bar{t}\bar{t}\bar{t}$  or (b)(c)  $t\bar{t}\bar{t}$  [2].

675 The tree level  $t\bar{t}$ -associated process  $t\bar{t}Z'$  is the targeted production channel for the search  
 676 in this dissertation. The  $t\bar{t}Z'$  cross-section at LO in QCD is shown in Figure 2.5. Con-  
 677 tributions from the single-top-associated channels  $tjZ'$  and  $tWZ'$  are not considered due  
 678 to a smaller cross-section by a factor of two compared to  $t\bar{t}Z'$  due to suppression in the  
 679 three-body phase space [2]. Additionally,  $t\bar{t}Z' \rightarrow t\bar{t}\bar{t}\bar{t}$  production is independent of  $\theta$  while  
 680  $tjZ'$  and  $tWZ'$  are minimally suppressed under pure left-handed interactions ( $\theta = 0$ ) and

- 681 maximally suppressed under pure right-handed interactions ( $\theta = \pi/2$ ); both channels are  
682 affected by the choice of  $\theta = \pi/4$  to suppress loop level production.

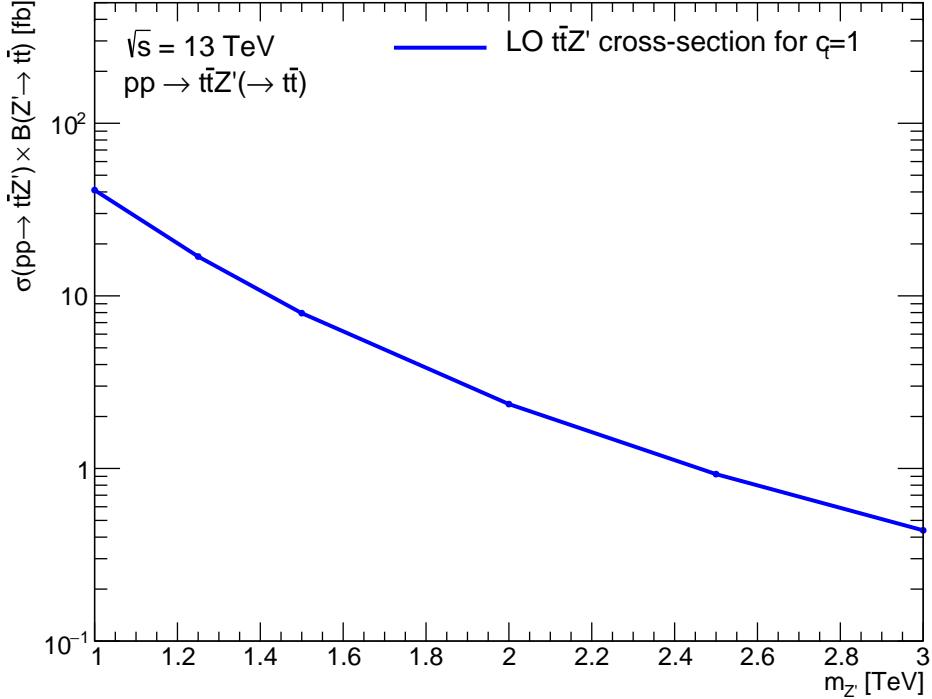


Figure 2.5: Theoretical  $t\bar{t}Z'$  production cross-section times  $Z' \rightarrow t\bar{t}$  branching ratio as a function of the  $Z'$  mass at LO in QCD coupling to top with  $c_t = 1$  under a simplified topophilic model [1–3].

### 683 2.2.3 Decay modes

- 684 The different  $W$  boson decay modes shown in Figure 2.2 result in many different final  
685 states for  $t\bar{t}Z'/t\bar{t}t\bar{t}$  decay, which can each be classified into one of three channels shown in  
686 Figure 2.6: all hadronic decays; exactly one lepton or two opposite-sign leptons (1LOS);  
687 exactly two same-sign leptons or three or more leptons (SSML). The branching ratio for  
688 each channel is shown in Figure 2.6. The all hadronic and 1LOS channels have much larger  
689 branching ratios compared to SSML channel but suffer heavily from  $gg \rightarrow t\bar{t}$  background

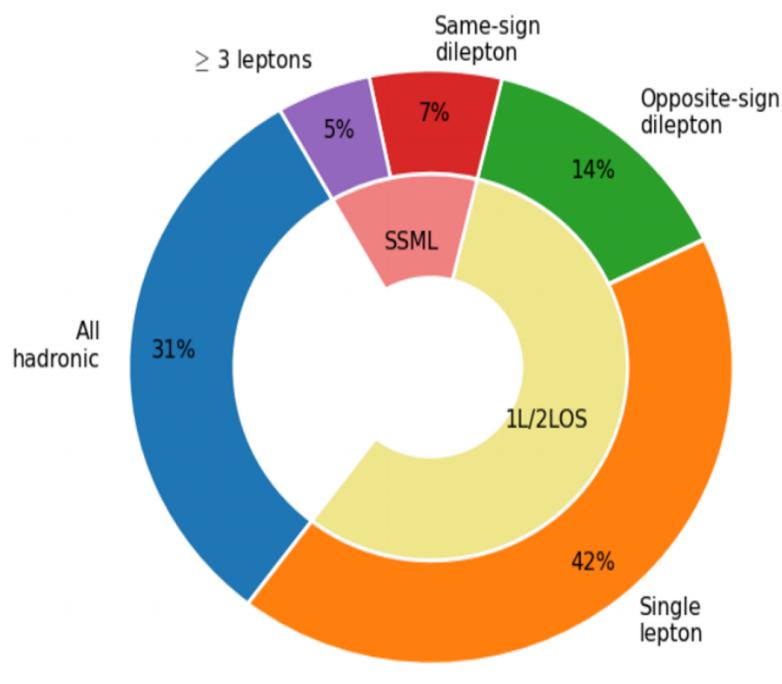


Figure 2.6: Branching ratios for  $t\bar{t}t\bar{t}$  decay [78]. The same-sign dilepton and multilepton channels together forms the SSML channel.

- <sup>690</sup> contamination, giving the SSML channel better sensitivity at the cost of lower statistics.
- <sup>691</sup> This is also the targeted channel for this analysis.

## 692 Chapter 3. LHC & ATLAS Experiment

### 693 3.1 The Large Hadron Collider

694 Predictions from theoretical models are evaluated against experimental data collected  
695 from particle detectors. This chapter provides a detailed overview of the Large Hadron  
696 Collider (LHC) and the ATLAS detector, one of the key experiments designed to study  
697 high-energy collisions at the LHC.

#### 698 3.1.1 Overview

699 The Large Hadron Collider [79] (LHC) is currently the world's largest particle collider  
700 with a circumference of almost 27 km. Built by CERN on the border of Switzerland and  
701 France, the LHC is designed as a particle collider for proton-proton ( $pp$ ), sometimes heavy  
702 ions i.e. lead-lead (PbPb) and proton-lead ( $pPb$ ) beams at TeV-scale energies. Two beams  
703 of particles are injected into the LHC in opposite directions and allowed to collide at the  
704 center of four major experiments:

- 705 • **A Toroidal LHC ApparatuS** (ATLAS) [30] and **Compact Muon Solenoid** (CMS)  
706 [80]: multi-purpose detectors, designed to target a variety of phenomena including SM,  
707 BSM and heavy-ion physics.
- 708 • **Large Ion Collider Experiment** (ALICE) [81]: specialized detector to record ion  
709 collisions and study heavy-ion physics.
- 710 • **Large Hadron Collider beauty** (LHCb) [82]: detector dedicated to study properties  
711 of  $b$ -quarks and  $b$ -hadrons.

712 Aside from the four major experiments, the LHC also houses smaller experiments e.g.  
 713 AWAKE [83], FASER [84], KATRIN [85], that either share an interaction point with one of  
 714 the above experiments or make use of particle beams pre-LHC injection.

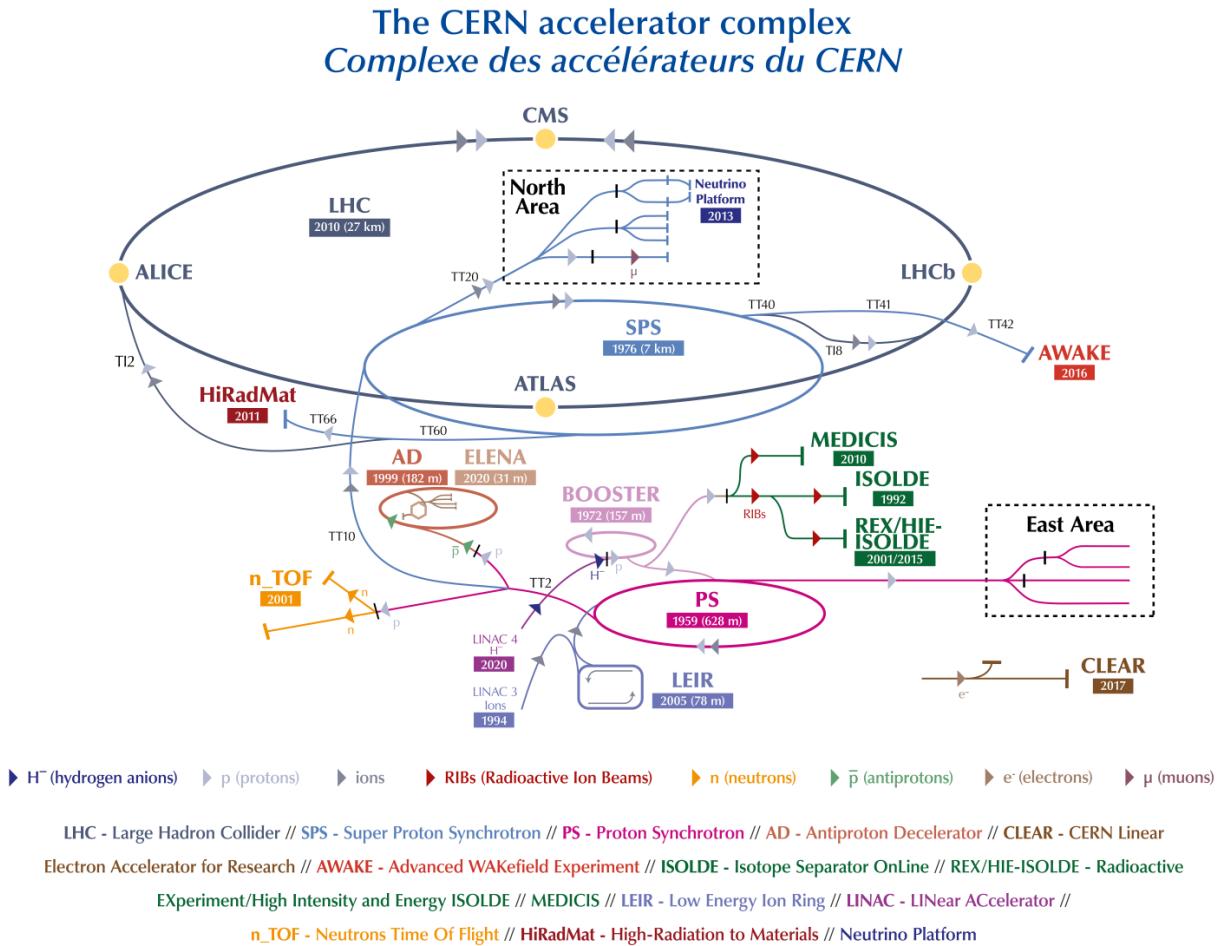


Figure 3.1: The full CERN accelerator complex as of 2022 [86].

715 The majority of the LHC operational time is dedicated to studying  $pp$  collisions of up to  
 716  $\sim 13$  TeV center-of-mass energy, denoted as  $\sqrt{s}$ . Reaching collision energy requires a sequence  
 717 of accelerators within the CERN accelerator complex, shown in Figure 3.1. Proton produc-  
 718 tion starts at LINAC 4, where hydrogen atoms are accelerated to 160 MeV then stripped  
 719 of electrons. The leftover proton beams are injected into the Proton Synchrotron Booster

720 (PSB) and accelerated to 2 GeV before being transferred into the Proton Synchrotron (PS).  
 721 Here, the beams are ramped up to 26 GeV then injected into the Super Proton Synchrotron  
 722 (SPS) to further raise the energy threshold to 450 GeV. The beams are finally injected into  
 723 the LHC in opposite directions, continuously increasing in energy up to 6.5 TeV per beam,  
 724 reaching the 13 TeV center-of-mass energy threshold necessary for collision during Run 2.  
 725 As of the start of Run 3 in 2022, proton beams can now be ramped up to 6.8 TeV per beam  
 726 for a total of  $\sqrt{s} = 13.6$  TeV.

### 727 3.1.2 LHC operations

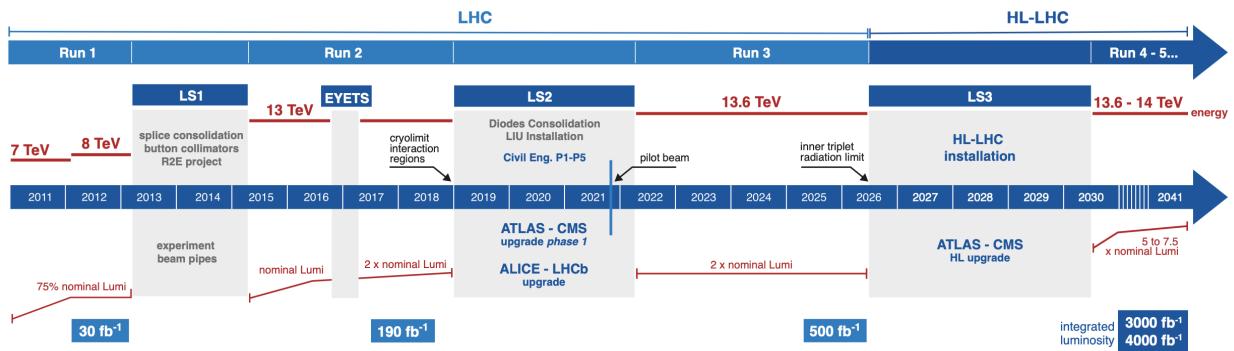


Figure 3.2: Current and future timeline of LHC operations with corresponding center-of-mass energies and projected integrated luminosities. [87].

728 Operations at the LHC are defined in periods of data-taking and shut-down known as  
 729 runs and long shutdowns respectively; the first period (Run 1) started with first collisions  
 730 at the LHC in 2010 at  $\sqrt{s} = 7$  TeV [88]. Upgrades are usually carried out for detectors and  
 731 accelerators during long shutdowns, raising the maximum energy threshold in preparation  
 732 for the next run. An overview of the LHC runtime and corresponding center-of-mass energies  
 733 are summarized in Figure 3.2. During Run 2 from 2015-2018, the ATLAS detector recorded  
 734 a total of  $1.1 \times 10^{16}$   $pp$  collisions at  $\sqrt{s} = 13$  TeV, which corresponds to an integrated

735 luminosity of  $140 \pm 0.83\% \text{ fb}^{-1}$  that passed data quality control and are usable for analyses  
736 [89]. This is also the data set used for the analysis in this dissertation.

### 737 3.1.3 Physics at the LHC

738 The majority of physics studied at the LHC focus primarily on QCD proton-proton hard  
739 scattering processes and the resulting products. Hard scattering processes involve large  
740 momentum transfer compared to the proton mass e.g. top pair production ( $gg \rightarrow t\bar{t}$ ) and  
741 Higgs production ( $gg \rightarrow H$ ), and can be predicted using perturbative QCD [90]. Hard  
742 processes probe distance scales much lower than the proton radius and can be considered  
743 collisions between the constituent quarks and gluons i.e. partons. Soft processes involve  
744 lower momentum transfer between partons and are dominated by less well-understood non-  
745 perturbative QCD effects. The hard interaction between two partons are represented by a  
746 parton distribution function (PDF)  $f_i(x, Q^2)$ , which describes the probability of interacting  
747 with a constituent parton  $i$  that carries a fraction  $x$  of the external hadron's momentum  
748 when probed at a momentum scale of  $Q^2$  [91]. Other partons within the hadron that did  
749 not participate in the collision can still interact via lower momentum underlying-events  
750 (UE). The probability of a particular interaction occurring is defined as its cross-section  
751  $\sigma[b]$ . Figure 3.3 gives an overview of SM processes produced within the LHC and their  
752 cross-sections.

## 753 3.2 The ATLAS detector

754 One of the four main experiments at the LHC is ATLAS [30], designed as a multi-purpose  
755 detector for the role of studying high-energy physics in  $pp$  and heavy-ion collisions. ATLAS

## Standard Model Production Cross Section Measurements

Status: October 2023

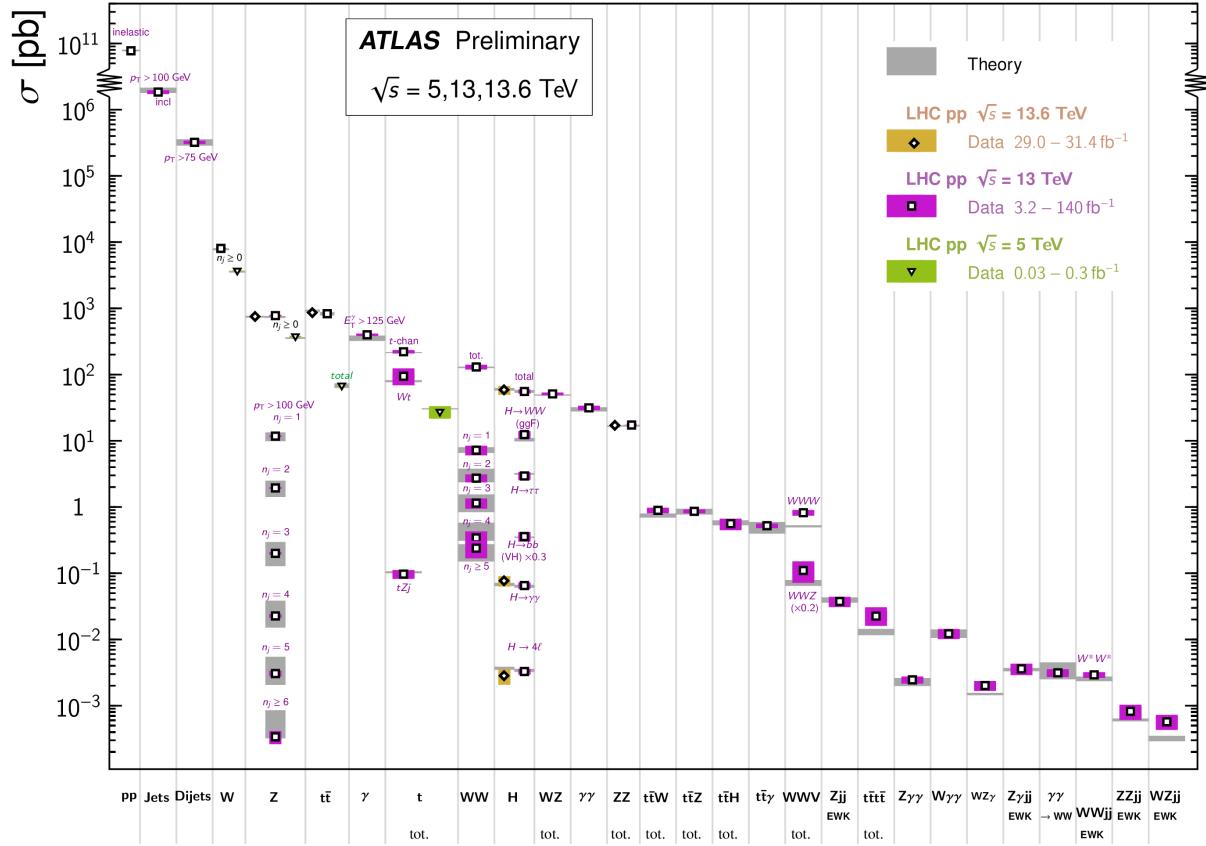


Figure 3.3: Summary of predicted and measured cross-section for SM processes at the LHC at different center-of-mass energies [92].

756 is a detector with symmetric cylindrical geometry with dimensions of 44 m in length and 25  
 757 m in diameter, covering a solid angle of almost  $4\pi$  around the collision point. The detector is  
 758 built concentrically around the beamline with the collision point at the center to maximally  
 759 capture signals produced by interactions. Figure 3.4 shows a slice of the ATLAS detector.  
 760 From the inside out, the main ATLAS subdetector system consists of the inner detector  
 761 (ID), calorimeter systems (electromagnetic and hadronic) and the muon spectrometer (MS).  
 762 The ATLAS detector uses a right-handed coordinate system [30] designed to align with  
 763 the geometry of a collision interaction, with the origin set at the interaction point, the  $z$ -axis

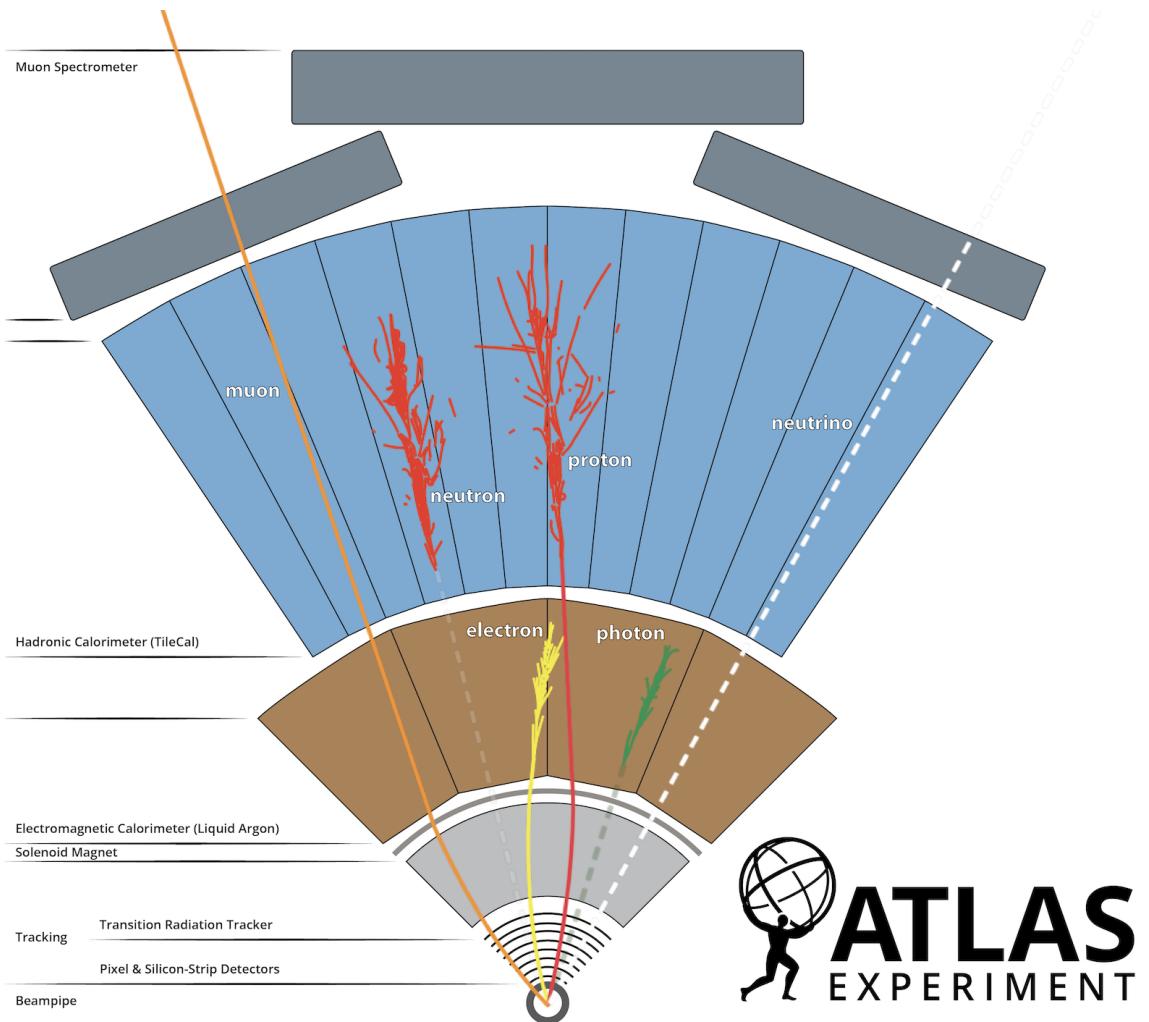


Figure 3.4: A cross section slice of the ATLAS detector showing different subsystems along with visualization of different types of particles traveling through the detector [93].

764 following (either of) the beamline and the  $x$ -axis pointing towards the center of the LHC  
 765 ring. In cylindrical coordinates, the polar angle  $\theta$  is measured from the beam axis, and  
 766 the azimuthal angle  $\phi$  is measured along the transverse plane ( $xy$ -plane) starting at the  $x$ -  
 767 axis. Additional observables are defined for physics purposes: the pseudorapidity defined as  
 768  $\eta = -\ln \tan(\theta/2)$ ; angular distance within the detector defined as  $\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$ ; and  
 769 transverse momentum  $p_T$  (transverse energy  $E_T$ ) defined as the component of the particle's  
 770 momentum (energy) projected onto the transverse plane.

### 771 3.2.1 Inner detector

772 The innermost part of ATLAS is the inner detector (ID) [30], constructed primarily for  
773 the purpose of measuring and reconstructing charged tracks within the  $|\eta| < 2.5$  region with  
774 high momentum resolution ( $\sigma_{p_T}/p_T = 0.05\% \pm 1\%$ ). Figure 3.5 shows the composition of  
775 the ID with three subsystems, the innermost being the pixel detector, then Semiconductor  
776 Tracker (SCT), and the Transition Radiation Tracker (TRT) on the outermost layer; all of  
777 which are surrounded by a solenoid magnet providing a magnetic field of 2 T.

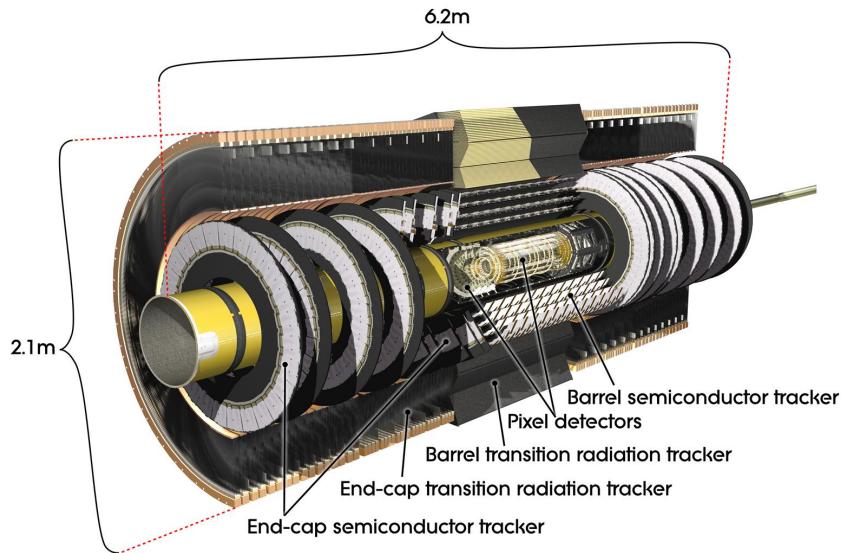


Figure 3.5: Cutaway illustration of the inner detector along with its subsystems [94].

### 778 Pixel detector

779 The pixel detector subsystem [30] consists of 250  $\mu\text{m}$  silicon semiconductor pixel layers  
780 with about 80.4 million readout channels, reaching a spatial resolution of 10  $\mu\text{m}$  in the  
781  $R - \phi$  (transverse) plane and 115  $\mu\text{m}$  in the  $z$ -direction for charged tracks. Charged particles  
782 passing through the pixel detector ionize the silicon layers and produce electron-hole pairs;

783 the electrons drift towards the detector's electrode under an applied electric field and the  
784 resulting electric signals are collected in read-out regions. The pixel detector is used primarily  
785 for impact parameter measurement, pile-up suppression, vertex finding and seeding for track  
786 reconstruction.

### 787 Semiconductor Tracker

788 The Semiconductor Tracker (SCT) [30] functions similarly to the pixel detector, using  
789 silicon semiconductor microstrips totaling about 6.3 million read-out channels, reaching a  
790 per layer resolution of 17  $\mu\text{m}$  in the  $R\text{-}\phi$  plane and 580  $\mu\text{m}$  in the  $z$ -direction [30]. The  
791 SCT plays an important role in precise  $p_{\text{T}}$  measurement of charged particles as well as track  
792 reconstruction.

### 793 Transition Radiation Tracker

794 The outermost layer of the ID, the Transition Radiation Tracker (TRT) [30], consists of  
795 layers of 4 mm diameter straw tubes filled with a xenon-based gas mixture and a 30  $\mu\text{m}$   
796 gold-plated wire in the center. The TRT contains a total of about 351 thousand readout  
797 channels with a resolution of 130  $\mu\text{m}$  for each straw tube in the  $R\text{-}\phi$  plane, and provides  
798 extended track measurement, particularly estimation of track curvature under the solenoidal  
799 magnetic field. Importantly, the TRT also serves to identify electrons through absorption of  
800 emitted transition-radiation within the Xe-based gas mixture.

## 801 3.2.2 Calorimeter systems

802 Surrounding the ID is the ATLAS calorimeter system [30] with electromagnetic (EM) and  
803 hadronic calorimeters, covering a range of  $|\eta| < 4.9$ . The calorimeters are sampling calorime-

804 ters with alternating absorbing layers to stop incoming particles and active layers to collect  
 805 read-out signals from energy deposits. Incoming particles passing through the calorimeters  
 806 interact with the absorbing layers, producing EM or hadronic showers of secondary particles.  
 807 The particle showers deposit energy in the corresponding layer of the calorimeters, which  
 808 are collected and aggregated to identify and reconstruct the original particle's energy and  
 809 direction. Figure 3.6 shows a schematic overview of the ATLAS calorimeter system.

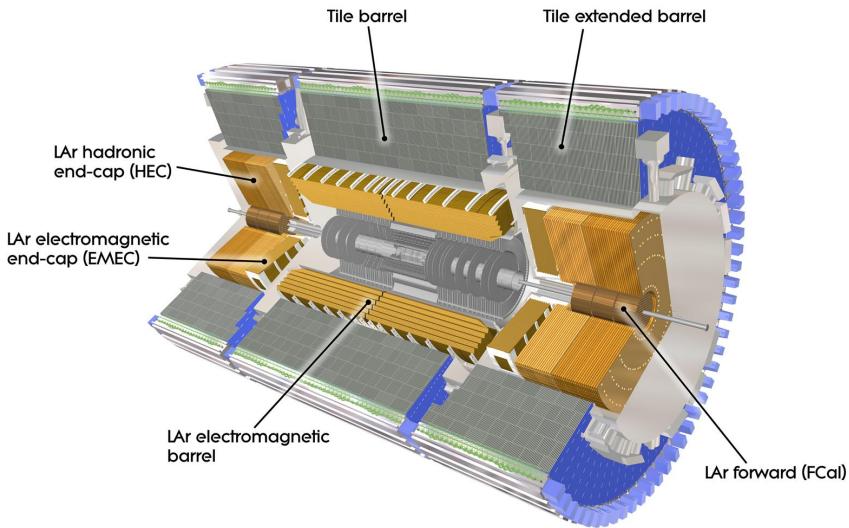


Figure 3.6: Cutaway illustration of the calorimeter system including the EM, hadronic and LAr forward calorimeters [95].

## 810 Electromagnetic calorimeter

811 The EM calorimeter [30] covers the innermost part of the calorimeter system, with lead  
 812 (Pb) absorbing layers and liquid argon (LAr) active layers to capture the majority of electrons  
 813 and photons exiting the ID. The EM calorimeter is divided into regions depending on  $\eta$   
 814 coverage: a barrel region ( $|\eta| < 1.475$ ), two endcap regions ( $1.375 < |\eta| < 3.2$ ) and a  
 815 transition region ( $1.372 < |\eta| < 1.52$ ). The endcap calorimeters are further divided into an

816 outer wheel region ( $1.372 < |\eta| < 2.5$ ) and an inner wheel region ( $2.5 < |\eta| < 3.2$ ) in order  
817 to provide precise coverage within the same  $\eta$  range as the ID. Overlap between the barrel  
818 and endcap regions compensates for the lower material density in the transition region.

819 **Hadronic calorimeter**

820 The hadronic calorimeter [30] covers up to  $|\eta| < 4.9$  and is comprised of three parts: the  
821 tile calorimeter with a barrel region ( $|\eta| < 1.0$ ) and extended barrel regions ( $0.8 < |\eta| < 1.7$ );  
822 the hadronic endcap calorimeter (HEC) covering  $1.5 < |\eta| < 3.2$ ; and the forward calorimeter  
823 (FCal) covering  $3.2 < |\eta| < 4.9$ . The tile calorimeter covers the EM calorimeter barrel region  
824 and uses steel as material for the absorbing layers with scintillating tiles for the active layers.  
825 Signals captured by scintillating tiles are read out from both sides using photomultiplier  
826 tubes. The HEC calorimeter covers the endcap regions of the EM calorimeter and uses a  
827 copper-LAr calorimeter layer scheme. The FCal is located close to the beamline providing  
828 coverage for particles traveling close to parallel with the beam axis. The subdetector contains  
829 three modules: one with copper absorbing layers optimized for EM measurements, and two  
830 with tungsten absorbing layers targeting hadronic cascades. All modules in the FCal use  
831 LAr as the active layer.

832 **3.2.3 Muon spectrometer**

833 Generally, the only particles that penetrate past the calorimeter layer are muons and  
834 neutrinos. The muon spectrometer (MS) [30] is situated on the outermost of the ATLAS  
835 detector and aims to track and measure muons within  $|\eta| < 2.7$ . The MS utilizes an array  
836 of toroid magnets to provide a magnetic field perpendicular to the muon trajectory, bending  
837 the track in order to measure its curvature. The magnetic field is powered by a large barrel

838 toroid ( $|\eta| < 1.4$ ) with strength of 0.5 T and two endcap toroid magnets ( $1.6 < |\eta| < 2.7$ ) of  
839 1 T. Both types contribute to the magnetic field in the transition region ( $1.4 < |\eta| < 1.6$ ).

840 To measure the muon itself, four types of large gas-filled chambers known as muon cham-  
841 bers [30] are designed and constructed for two main goals: triggering on potential muon  
842 candidates entering the MS and tracking their trajectories through the detector with high  
843 precision. The tracking system include Monitored Drift Tubes (MDTs), which record muon  
844 track information over the entire MS  $\eta$  range ( $|\eta| < 2.7$ ). The MDTs are built with multi-  
845 ple layers of drift tubes and filled with a mixture of 93% Ar and 7% CO<sub>2</sub>. Muons passing  
846 through drift tubes in the MDT ionize the gas within each tube; signals are then recorded  
847 as freed electrons drift to read-out channels under an applied electric field. In the forward  
848 region ( $2.0 < |\eta| < 2.7$ ), Cathode Strip Chambers (CSCs) are included along with MDTs.  
849 The CSCs are multiwire proportional chambers built with higher granularity and shorter  
850 drift time than the MDTs to handle tracking in an environment with high background rates

851 .

852 The MS trigger system includes Resistive Plate Chambers (RPCs) [30], which provide  
853 triggering in the barrel region ( $|\eta| < 1.05$ ) using parallel electrode plates made of resistive  
854 materials with a gas mixture inbetween. High voltage is applied to the plates, accelerat-  
855 ing the electrons freed from ionized gas and creating a fast avalanche of charge, which is  
856 collected on external read-out strips almost instantaneously. Triggering and coarse position  
857 measurements in the endcap region ( $1.05 < |\eta| < 2.5$ ) is handled by Thin-Gap Chambers  
858 (TGCs). Similar to CSCs, TGCs are multiwire proportional chambers with a small wire gap  
859 ("thin-gap") and high applied voltage across the gap, resulting in fast response time giving  
860 TGCs the capabilities to identify muon candidates in real time.

861 **3.2.4 Trigger & data acquisition**

862     The LHC produces a colossal amount of collision data at a bunch crossing rate of 40 MHz  
863    with bunch spacing of 25 ns. The ATLAS Trigger and Data Acquisition (TDAQ) system [96]  
864    synchronously identifies and records interesting events for in-depth analysis. The ATLAS  
865    trigger system in Run 2 consists of two steps: Level-1 (L1) trigger and High-Level Trigger  
866    (HLT). Events failing any step in the trigger chain are permanently lost.

867     The L1 trigger hardware is divided into L1 calorimeter triggers (L1Calo) and L1 muon  
868    triggers (L1Muon) [96]. L1Calo trigger uses information from ATLAS calorimeter system  
869    to quickly identify signs of high  $p_T$  objects e.g. EM clusters, jets and missing transverse  
870    energy  $E_T^{\text{miss}}$  (section 4.4). Similarly, L1Muon uses information from the RPCs and TGCs  
871    of the MS to make quick decisions on potentially interesting muon candidates. Outputs  
872    from L1Calo and L1Muon are fed into the L1 topological trigger (L1Topo) for additional  
873    filtering based on event topology and multi-object correlation, allowing for more selective  
874    and physics-motivated triggering. Decisions from all three types of L1 triggers are provided  
875    as inputs for the Central Trigger Processor (CTP) for a final Level-1 Accept (L1A) decision.

876     The entire L1 trigger chain results in a 2.5  $\mu\text{s}$  latency and reduces the event rate to 100 kHz.

877     Events passing L1 triggers are sent to HLTs before being saved to offline storage at  
878    CERN data centers. HLTs are software-based triggers used for more complex and specific  
879    selections on physics objects required by targeted analysis goals, in turn requiring more  
880    computing power with longer latency. After HLT selections, the event rate is reduced to 1  
881    kHz on average [96]. Overall, the full trigger chain reduces the event rate for ATLAS by  
882    approximately a factor of  $4 \times 10^4$ .

883 **Chapter 4. Particle Reconstruction & Identifi-**  
884 **fication**

885 Activity within the ATLAS detector is recorded as raw electronic signals, which can  
886 be utilized by ATLAS reconstruction software to derive physics objects for analysis. This  
887 chapter describes the reconstruction and identification of basic objects (e.g. interaction  
888 vertices, tracks, topological clusters of energy deposits) and subsequently of complex physics  
889 objects i.e. particles and particle signatures.

890 **4.1 Primary reconstruction**

891 **4.1.1 Tracks**

892 Charged particles traveling through the ATLAS detector deposit energy in different layers  
893 of the ID and MS. The ID track reconstruction software consists of two algorithm chains:  
894 inside-out and outside-in track reconstruction [97–99].

895 The inside-out algorithm is primarily used for the reconstruction of primary particles  
896 i.e. particles directly produced from  $pp$  collisions or decay products of short-lived particles.  
897 The process starts by forming space points from seeded hits in the silicon detectors within  
898 the pixel & SCT detectors. Hits further away from the interaction vertex are added to  
899 the track candidate using a combinatorial Kalman filter [100] pattern recognition algorithm.  
900 Track candidates are then fitted with a  $\chi^2$  filter [101] and loosely matched to a fixed-sized  
901 EM cluster. Successfully matched track candidates are re-fitted with a Gaussian-sum filter  
902 (GSF) [102], followed by a track scoring strategy to resolve fake tracks & hit ambiguity

903 between different tracks [103]. The track candidate is then extended to the TRT to form  
904 final tracks satisfying  $p_T > 400$  MeV. The outside-in algorithm handles secondary tracks  
905 mainly produced from long-lives particles or decays of primary particles by back-tracking  
906 from TRT segments, which are then extended inward to match silicon hits in the pixel and  
907 SCT detectors to form track reconstruction objects.

### 908 4.1.2 Vertices

909 Vertices represent the point of interaction or decay for particles within the ATLAS de-  
910 tector. Primary vertices (PVs) are defined as the point of collision for hard-scattering  $pp$   
911 interactions, while secondary or displaced vertices result from particle decays occurring at a  
912 distance from its production point.

913 Reconstruction of PVs is crucial to accurately profile the kinematic information of an  
914 event and form a basis for subsequent reconstruction procedures. Primary vertex recon-  
915 struction occurs in two stages: vertex finding and vertex fitting [104]. The vertex finding  
916 algorithm uses the spatial coordinates of reconstructed tracks to form the seed for a vertex  
917 candidate. An adaptive vertex fitting algorithm [105] then iteratively evaluates track-vertex  
918 compatibility to estimate a new best vertex position. Less compatible tracks are down-  
919 weighted in each subsequent iteration, and incompatible tracks are removed and can be  
920 used for another vertex seed; the process is repeated until no further PV can be found.  
921 All reconstructed vertices without at least two matched tracks are considered invalid and  
922 discarded.

923 Secondary vertex reconstruction uses the Secondary Vertex Finder (SVF) algorithm [106]  
924 which is primarily designed to reconstruct  $b$ - and  $c$ -hadrons for flavor tagging purposes. The  
925 SVF aims to reconstruct one secondary vertex per jet and only considers tracks that are

926 matched to a two-track vertex and contained within a  $p_T$ -dependent cone around the jet  
927 axis. The tracks are then used to reconstruct a secondary vertex candidate using an iterative  
928 process similar to the PV vertex fitting procedure.

929 **Pile-up**

930 At high luminosities, multiple interactions can be associated with one bunch crossing,  
931 resulting in many PVs. The effect is called pile-up [107], and usually result from soft QCD  
932 interactions. Pile-up can be categorized into two types: in-time pile-up, stemming from  
933 additional  $pp$  collisions in the same bunch crossing that is not the hard-scatter process; out-  
934 of-time pile-up, resulting from leftover energy deposits in the calorimeters from other bunch  
935 crossings.

936 **4.1.3 Topological clusters**

937 Topological clusters (topo-clusters) [108] consist of clusters of spatially related calorimeter  
938 cell signals. Topo-clusters are primarily used to reconstruct hadron- and jet-related objects  
939 in an effort to extract signal while minimizing electronic effects and physical fluctuations, and  
940 also allow for recovery of energy lost through bremsstrahlung or photon conversions. Cells  
941 with signal-to-noise ratio  $\zeta_{\text{cell}}^{\text{EM}}$  passing a primary seed threshold are seeded into a dynamic  
942 topological cell clustering algorithm as part of a proto-cluster. Neighboring cells satisfying a  
943 cluster growth threshold are collected into the proto-cluster. If a cell is matched to two proto-  
944 clusters, the clusters are merged. Two or more local signal maxima in a cluster satisfying  
945  $E_{\text{cell}}^{\text{EM}} > 500 \text{ MeV}$  suggest the presence of multiple particles in close proximity, and the cluster  
946 is split accordingly to maintain good resolution of the energy flow. The process continues  
947 iteratively until all cells with  $\zeta_{\text{cell}}^{\text{EM}}$  above a principal cell filter level have been matched to a

948 cluster.

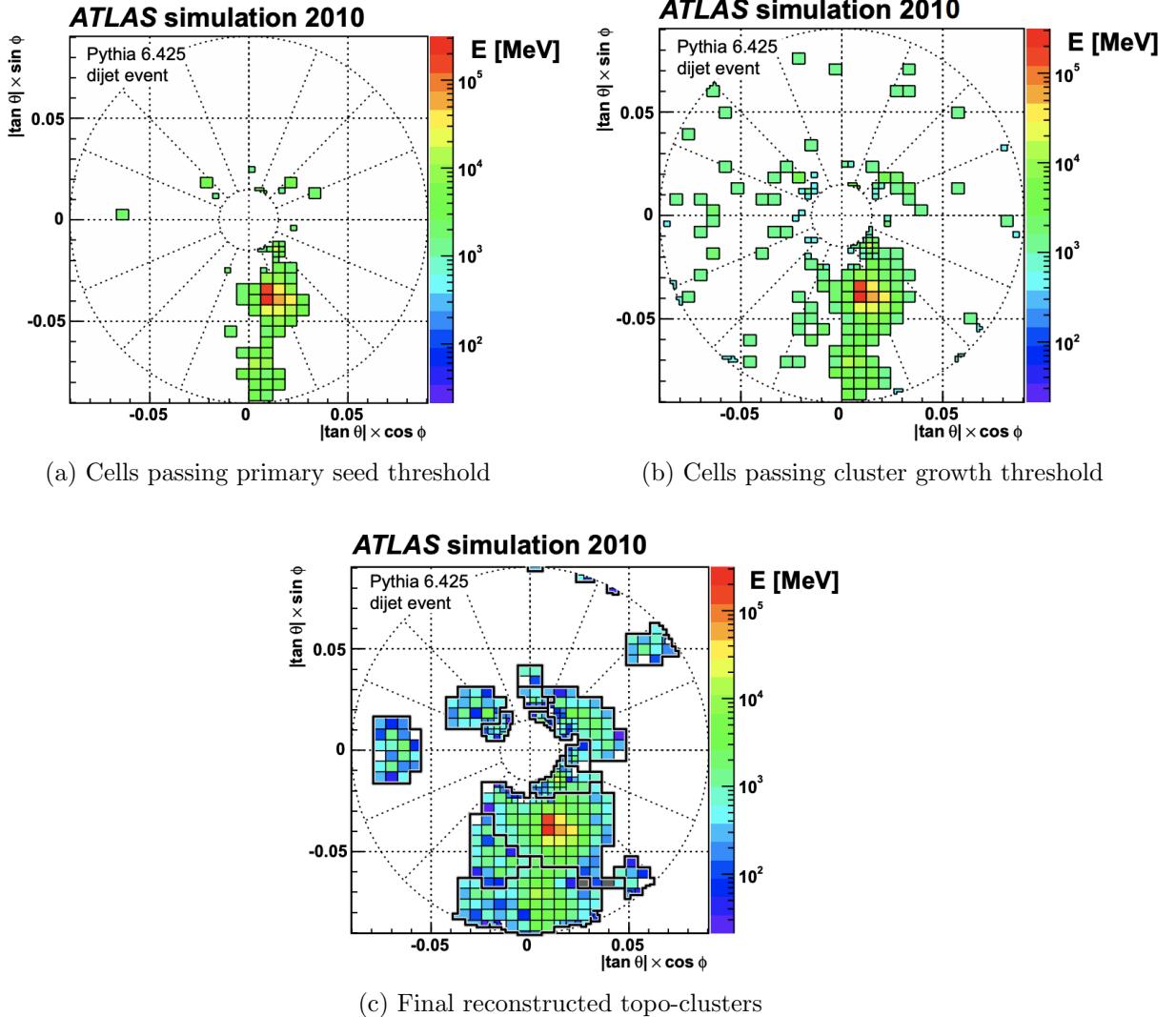


Figure 4.1: Stages of topo-cluster formation corresponding to each threshold. In (a), proto-clusters are seeded from cells with adequate signal significance  $\zeta_{\text{cell}}^{\text{EM}}$ . The clusters are further merged and split in (b) following a predefined cluster growth threshold. The process stops in (c) when all sufficiently significant signal hits have been matched to a cluster [108].

## 949 4.2 Jets

950 Quarks, gluons and other hadrons with non-neutral color charge cannot be observed  
951 individually due to QCD color confinement, which forces a non-color-neutral hadron to

952 almost immediately undergo hadronization, producing a collimated cone of color-neutral  
953 hadrons defined as a jet. Jet signals can be used to reconstruct and indirectly observe the  
954 quarks or gluons from which the jet originated in the original hard-scattering process.

### 955 4.2.1 Jet reconstruction

956 The ATLAS jet reconstruction pipeline is largely carried out using a particle flow (PFlow)  
957 algorithm combined with an anti- $k_t$  jet clustering algorithm. The PFlow algorithm [109]  
958 utilizes topo-clusters along with information from both the calorimeter systems and the ID in  
959 order to make use of the tracker system’s advantages in low-energy momentum resolution and  
960 angular resolution. First, the energy from charged particles is removed from the calorimeter  
961 topo-clusters; then, it is replaced by particle objects created using the remaining energy in  
962 the calorimeter and tracks matched to topo-clusters. The ensemble of ”particle flow objects”  
963 and corresponding matched tracks are used as inputs for the iterative anti- $k_t$  algorithm [110].

964 The main components of the anti- $k_t$  algorithm involve the distance  $d_{ij}$  between two  
965 jet candidates  $i$  and  $j$ , and the distance  $d_{iB}$  between the harder jet candidate of the two  
966 (defined as  $i$ ) and the beamline  $B$ . If  $d_{ij} < d_{iB}$ , then the two jet candidates are combined  
967 and returned to the pool of candidates; otherwise, jet candidate  $i$  is considered a jet and  
968 removed from the pool. The distance  $d_{ij}$  is inversely proportional to a predefined radius  
969 parameter  $\Delta R$  in order to control reconstruction quality for small- $R$  and large- $R$  jets. This  
970 analysis uses  $\Delta R = 0.4$  to better handle heavily collimated small- $R$  jets resulting from parton  
971 showers.

972 The anti- $k_t$  jets so far have only been reconstructed at the EM level and need to be  
973 calibrated to match the energy scale of jets reconstructed at particle level. This is done  
974 via a MC-based jet energy scale (JES) calibration sequence, along with further calibrations

975 to account for pile-up effects and energy leakage. The full JES calibration sequence is  
 976 shown in Figure 4.2. All calibrations except origin correction are applied to the jet's four-  
 977 momentum i.e. jet  $p_T$ , energy and mass. Afterwards, a jet energy resolution (JER) [111]  
 978 calibration step is carried out in a similar manner to JES to match the resolution of jets in  
 979 dijet events. To further suppress pile-up effects, a neural-network based jet vertex tagger  
 980 (NNJvt) discriminant was developed based on the previous jet vertex tagger (JVT) algorithm  
 981 [107] and applied to low- $p_T$  reconstructed jets.

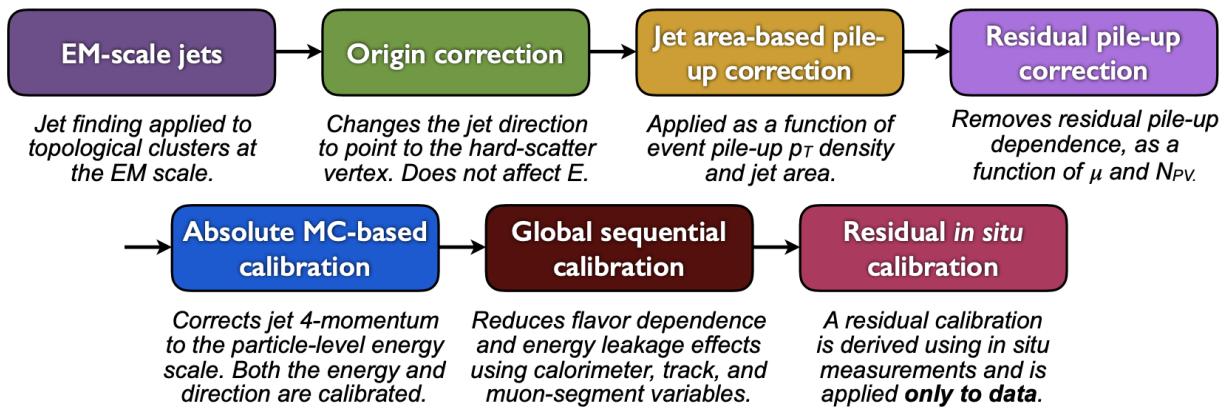


Figure 4.2: Jet energy scale calibration sequence for EM-scale jets [112].

### 982 4.2.2 Flavor tagging

983 Identifying and classifying hadronic jets are important tasks for ATLAS physics, for  
 984 example analyses involving Higgs decays  $H \rightarrow b\bar{b}$  or top quarks. Flavor tagging or  $b$ -tagging  
 985 is the process of identifying jets containing  $b$ -hadrons,  $c$ -hadrons, light-hadrons ( $uds$ -hadrons)  
 986 or jets from hadronically decaying  $\tau$  leptons. Distinguishing  $b$ -jets is possible due to their  
 987 characteristically long lifetime ( $\tau \approx 1.5$  ps), displaced secondary decay vertex and high decay  
 988 multiplicity.

989 Usage of  $b$ -tagging in this analysis is done via five operating points (OPs), corresponding

990 to 65%, 70%, 77%, 85% and 90%  $b$ -jet tagging efficiency  $\varepsilon_b$  in simulated  $t\bar{t}$  events, in order  
991 from the tightest to loosest discriminant cut point. The OPs are defined by placing selections  
992 on the tagger output to provide a predefined  $\varepsilon_b$  level; the selection cuts act as a variable  
993 trade-off between  $b$ -tagging efficiency and  $b$ -jet purity i.e.  $c$ - or light-jet rejection. For this  
994 analysis, a jet is considered  $b$ -tagged if it passes the 85% OP. The  $b$ -tagged jet is then  
995 assigned a pseudo-continuous  $b$ -tagging (PCBT) score, which quantifies a jet's ability to  
996 satisfy different OPs. The score can take integer values between 1 and 6, where a score of 6  
997 is assigned to jets passing all OP thresholds; a score of 2 for jets that pass only the tightest  
998 OP (90%); and a score of 1 for jets that pass no OP. A value of -1 is also defined for any jet  
999 that does not satisfy  $b$ -tagging criteria. Since the targeted  $t\bar{t}t\bar{t}$  final states contain at least  
1000 four  $b$ -hadrons from top and  $W$  decays, a  $b$ -tagging OP of 85% is used to maintain high  
1001 purity during  $b$ -tagged jet selections in the signal region.

1002 **GN2  $b$ -tagging algorithm**

1003 For this analysis,  $b$ -jets are identified and tagged with the GN2v01  $b$ -tagger [113]. The  
1004 GN2 algorithm uses a Transformer-based model [114] modified to incorporate domain knowl-  
1005 edge and additional auxiliary physics objectives: grouping tracks with a common vertex and  
1006 predicting the underlying physics process for a track. The network structure is shown in  
1007 Figure 4.3. The GN2  $b$ -tagger form the input vector by concatenating 2 jet variables and  
1008 19 track reconstruction variables (for up to 40 tracks), normalized to zero mean and unit  
1009 variance. The output consists of a track-pairing output layer of size 2, a track origin clas-  
1010 sification layer of 7 categories, and a jet classification layer of size 4 for the probability of  
1011 each jet being a  $b$ -,  $c$ -, light- or  $\tau$ -jet respectively. For  $b$ -tagging purpose, a discriminant is

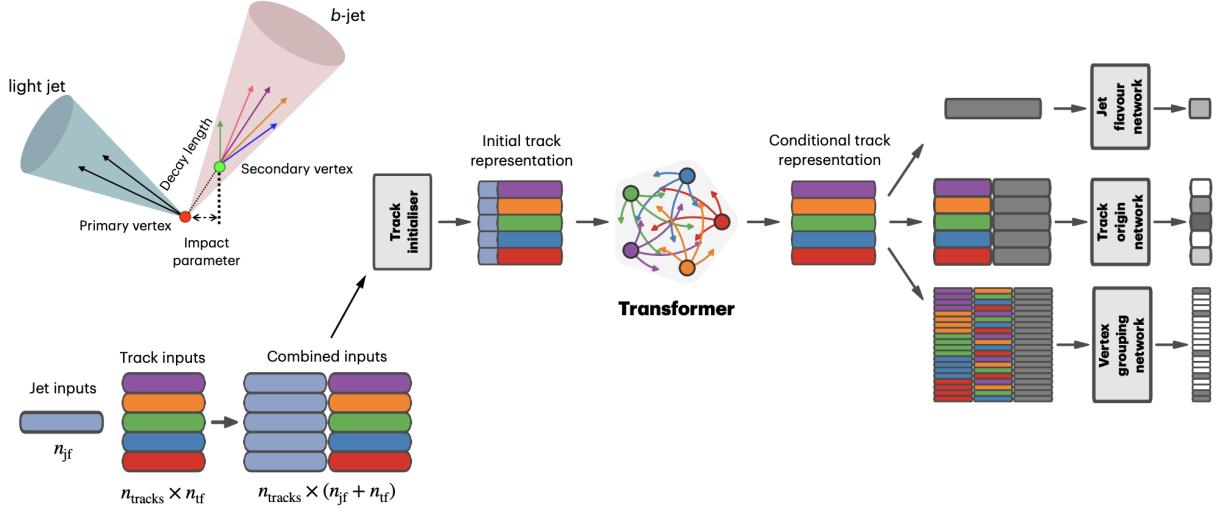


Figure 4.3: Overview of the GN2 architecture. The number of jet and track features are represented by  $n_{\text{jf}}$  and  $n_{\text{tf}}$  respectively. The global jet representation and track embeddings output by the Transformer encoder are used as inputs for three task-specific networks [113].

<sub>1012</sub> defined using these four outputs

$$D_b = \ln \left( \frac{p_b}{f_c p_c + f_\tau p_\tau + (1 - f_c - f_\tau) p_{\text{light}}} \right) \quad (4.1)$$

<sub>1013</sub> where  $p_x$  is the probability of the jet being an  $x$ -jet as predicted by GN2, and  $f_c, f_\tau$  are tun-  
<sub>1014</sub> able free parameters controlling balance between  $c$ - and light-jet rejection. Simulated SM  $t\bar{t}$   
<sub>1015</sub> and BSM  $Z'$  events from  $pp$  collisions were used as training and evaluation samples. In order  
<sub>1016</sub> to minimize bias, both  $b$ - and light-jet samples are re-sampled to match  $c$ -jet distributions.  
<sub>1017</sub> Figure 4.4 shows the performance of GN2 compared to the previous convolutional neural  
<sub>1018</sub> network-based standard  $b$ -tagging algorithm DL1d, in terms of  $c$ -, light- and  $\tau$ -jet rejection  
<sub>1019</sub> as a function of  $b$ -tagging efficiency. The network gives a factor of 1.5-4 improvement in  
<sub>1020</sub> experimental applications compared to DL1d [113], without dependence on the choice of  
<sub>1021</sub> MC event generator or inputs from low-level flavor tagging algorithm.

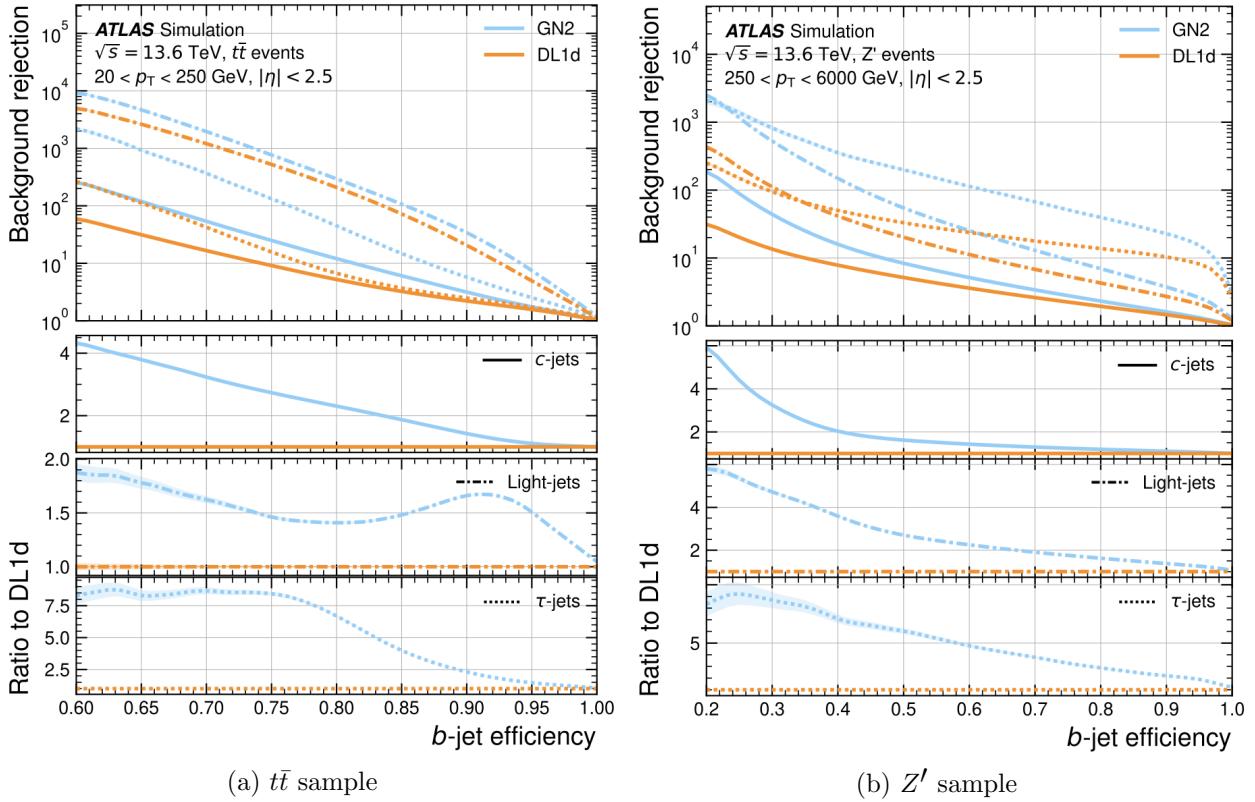


Figure 4.4: The  $c$ -, light- and  $\tau$ -jet rejection rate as a function of  $b$ -tagging efficiency for GN2 and DL1d using (a) jets in the  $t\bar{t}$  sample, and (b) jets in the  $Z'$  sample. The performance ratios of GN2 to DL1d are shown in the bottom panels [113].

## 1022 Efficiency calibration

1023 Due to imperfect description of detector response and physics modeling effects in simu-  
 1024 lation, the  $b$ -tagging efficiency predicted by MC simulation  $\varepsilon_b^{\text{sim}}$  requires a correction factor  
 1025 to match the efficiency measured in collision data  $\varepsilon_b^{\text{data}}$ . The correction scale factors (SFs)  
 1026 are defined as  $\text{SF} = \varepsilon_b^{\text{data}} / \varepsilon_b^{\text{sim}}$  and are determined by data-to-MC calibration using samples  
 1027 enriched in dileptonic  $t\bar{t}$  decays [115]. The resulting SFs are applied to MC simulated jets  
 1028 individually.

## 1029 4.3 Leptons

1030 Lepton reconstruction in ATLAS involves electron and muon reconstruction since tau  
1031 decays quickly, and depending on decay mode can be reconstructed using either jets or light  
1032 leptons. From here on out within this dissertation, leptons will be used exclusively to refer to  
1033 electrons and muons. Leptons can be classified into two categories: prompt leptons resulting  
1034 from heavy particle decays and non-prompt leptons resulting from detector or reconstruction  
1035 effects, or from heavy-flavor hadron decays.

### 1036 4.3.1 Electrons

1037 Electrons leave energy signature in the detector by interacting with the detector materials  
1038 and losing energy in the form of bremsstrahlung photons. A bremsstrahlung photon can  
1039 produce an electron-positron pair which can itself deposit signals in the detector, creating a  
1040 cascade of particles that can leave multiple of either tracks in the ID or EM showers in the  
1041 calorimeters, all of which are considered part of the same EM topo-cluster. Electron signal  
1042 signature has three characteristic components: localized energy deposits in the calorimeters,  
1043 multiple tracks in the ID and compatibility between the above tracks and energy clusters in  
1044 the  $\eta \times \phi$  plane [116]. Electron reconstruction in ATLAS follows these steps accordingly.

1045 Seed-cluster reconstruction and track reconstruction are performed sequentially in ac-  
1046 cordance with the iterative topo-clustering algorithm and track reconstruction method de-  
1047 scribed in section 4.1. The seed-cluster and GSF-refitted track candidate not associated  
1048 with a conversion vertex are matched to form an electron candidate. The cluster energy is  
1049 then calibrated using multivariate techniques on data and simulation to match the original  
1050 electron energy.

1051 **Electron identification**

1052 Additional LH-based identification selections using ID and EM calorimeter information  
1053 are implemented to further improve the purity of reconstructed electrons in the  $|\eta| < 2.47$  re-  
1054 gion of the detector [116]. The electron LH function is built with the signal being prompt elec-  
1055 trons and background being objects with similar signature to prompt electrons i.e. hadronic  
1056 jet deposits, photon conversions or heavy-flavor hadron decays. Three identification OPs  
1057 are defined for physics analyses: *Loose*, *Medium* and *Tight*, optimized for 9 bins in  $|\eta|$  and  
1058 12 bins in  $E_T$  with each OP corresponding to a fixed efficiency requirement for each bin.  
1059 For typical EW processes, the target efficiencies for *Loose*, *Medium* and *Tight* start at 93%,  
1060 88% and 80% respectively and increase with  $E_T$ . Similar to  $b$ -tagging OPs, the electron  
1061 identification OPs represent a trade-off in signal efficiency and background rejection. The  
1062 electron efficiency are estimated using tag-and-probe method on samples of  $J/\Psi \rightarrow ee$  and  
1063  $Z \rightarrow ee$  [116]. The *Tight* electron identification OP is used for this analysis.

1064 **Electron isolation**

1065 A characteristic distinction between prompt electrons and electrons from background  
1066 processes is the relative lack of activity in both the ID and calorimeters within an  $\Delta\eta \times \Delta\phi$   
1067 area surrounding the reconstruction candidate. Calorimeter-based and track-based electron  
1068 isolation variables [116] are defined to quantify the amount of activity around the electron  
1069 candidate using topo-clusters and reconstructed tracks respectively.

1070 Calorimeter-based isolation variables  $E_T^{\text{cone}XX}$  are computed by first summing the energy  
1071 of topo-clusters with barycenters falling within a cone of radius  $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} =$   
1072  $XX/100$  around the direction of the electron candidate. The final isolation variables are

1073 obtained by subtracting from the sum the energy belonging to the candidate electron at the  
1074 core of the cone, then applying corrections for pile-up effects and energy leakage outside of  
1075 the core. Similar to calorimeter-based variables, track-based isolation variables  $p_T^{\text{varcone}XX}$   
1076 are calculated by summing all track  $p_T$  within a cone of radius  $\Delta R$  around the electron  
1077 candidate, minus the candidate's contribution. The cone radius is variable as a function of  
1078  $p_T$  and is described as

$$\Delta R \equiv \min \left( \frac{10}{p_T}, \Delta R_{\max} \right), \quad (4.2)$$

1079 where  $p_T$  is expressed in GeV and  $\Delta R_{\max}$  is the maximum cone size, defined to account for  
1080 closer proximity of decay products to the electron in high-momentum heavy particle decays.  
1081 Four isolation operating points are implemented to satisfy specific needs by physics analyses:  
1082 *Loose*, *Tight*, *HighPtCaloOnly* and *Gradient* [116]. For this analysis, electrons isolation uses  
1083 *Tight* requirements.

## 1084 Electron charge misidentification

1085 Charge misidentification is a crucial irreducible background, particularly for analyses  
1086 with electron charge selection criteria. Electron charge is determined by the curvature of  
1087 the associated reconstructed track, and misidentification of charge can occur via either an  
1088 incorrect curvature measurement or an incorrectly matched track. Inaccurate measurement  
1089 is more likely for high energy electrons due to the small curvature in track trajectories at  
1090 high  $p_T$ , while track matching error usually results from bremsstrahlung pair-production  
1091 generating secondary tracks in close proximity [116]. Suppression of charge misidentification  
1092 background in Run 2 is additionally assisted by a boosted decision tree discriminant known

1093 as the Electron Charge ID Selector (ECIDS). For this analysis, all electrons are required to  
1094 pass the ECIDS criterion.

1095 **4.3.2 Muons**

1096 Muons act as minimum-ionizing particles, leaving tracks in the MS or characteristics  
1097 energy deposits in the calorimeter and can be reconstructed globally using information from  
1098 the ID, MS and calorimeters. Five reconstruction strategies corresponding to five muon  
1099 types [117] are utilized in ATLAS:

- 1100 • Combined (CB): the primary ATLAS muon reconstruction method. Combined muons  
1101 are first reconstructed using MS tracks then extrapolated to include ID tracks (outside-in strategy). A global combined track fit is performed on both MS and ID tracks.
- 1103 • Inside-out combined (IO): complementary to CB reconstruction. IO muon tracks are  
1104 extrapolated from ID to MS, then fitted with MS hits and calorimeter energy loss in a  
1105 combined track fit.
- 1106 • MS extrapolated (ME): ME muons are defined as muons with a MS track that cannot  
1107 be matched to an ID track using CB reconstruction. ME muons allow extension of  
1108 muon reconstruction acceptance to regions not covered by the ID ( $2.5 < |\eta| < 2.7$ )
- 1109 • Segment-tagged (ST): ST muons are defined as a successfully matched ID track that  
1110 satisfies tight angular matching criteria to at least one reconstructed MDT or CSC  
1111 segment when extrapolated to the MS. MS reconstruction is used primarily when  
1112 muons only crossed one layer of MS chambers.
- 1113 • Calorimeter-tagged (CT): CT muons are defined as an ID track that can be matched to

1114 energy deposits consistent with those of a minimum-ionizing particle when extrapolated  
1115 through the calorimeter. CT reconstruction extends acceptance range to regions in the  
1116 MS with sparse instrumentation ( $|\eta| < 0.1$ ) with a higher  $p_T$  threshold of 5 GeV,  
1117 compared to the 2 GeV threshold used by other muon reconstruction algorithms due  
1118 to large background contamination at the low  $p_T$  range of  $15 < p_T < 100$  GeV [118].

## 1119 Muon identification

1120 Reconstructed muons are further filtered by identification criteria to select for high-  
1121 quality prompt muons. Requirements include number of hits in the MS and ID, track fit  
1122 properties and compatibility between measurements of the two systems. Three standard  
1123 OPs (*Loose*, *Medium*, *Tight*) are defined to better match the needs of different physics  
1124 analyses concerning prompt muon  $p_T$  resolution, identification efficiency and non-prompt  
1125 muon rejection. The default identification OP for ATLAS physics and also the OP used in  
1126 this analysis is *Medium*, which provides efficiency and purity suitable for a wide range of  
1127 studies while minimizing systematic uncertainties [117].

## 1128 Muon isolation

1129 Muons from heavy particle decays are often produced in an isolated manner compared to  
1130 muons from semileptonic decays, and is therefore an important tool for background rejection  
1131 in many physics analyses. Muon isolation strategies are similar to that of electron in section  
1132 4.3.1, with track-based and calorimeter-based isolation variables. Seven isolation OPs are  
1133 defined using either or both types of isolation variables, balancing between prompt muon  
1134 acceptance and non-prompt muon rejection. The full definition and description for the muon  
1135 isolation OPs are detailed in Ref. [117].

## 1136 4.4 Missing transverse momentum

1137 Collisions at the LHC happen along the  $z$ -axis of the ATLAS coordination system between  
1138 two particle beam of equal center-of-mass energy. By conservation of momentum, the sum of  
1139 transverse momenta of outgoing particles should be zero. A discrepancy between measured  
1140 momentum and zero would then suggest the presence of undetectable particles, which would  
1141 consist of either SM neutrinos or some unknown BSM particles, making missing transverse  
1142 momentum ( $E_T^{\text{miss}}$ ) an important observable to reconstruct.

1143 Reconstructing  $E_T^{\text{miss}}$  utilizes information from fully reconstructed leptons, photons, jets  
1144 and other matched track-vertex objects not associated with a prompt object (soft signals),  
1145 defined with respect to the  $x(y)$ -axis as

$$E_{x(y)}^{\text{miss}} = - \sum_{i \in \{\text{hard objects}\}} p_{x(y),i} - \sum_{j \in \{\text{soft signals}\}} p_{x(y),j}, \quad (4.3)$$

1146 where  $p_{x(y)}$  is the  $x(y)$ -component of  $p_T$  for each particle [119]. The following observables  
1147 can then be defined:

$$\begin{aligned} \mathbf{E}_T^{\text{miss}} &= (E_x^{\text{miss}}, E_y^{\text{miss}}), \\ E_T^{\text{miss}} &= |\mathbf{E}_T^{\text{miss}}| = \sqrt{(E_x^{\text{miss}})^2 + (E_y^{\text{miss}})^2}, \\ \phi^{\text{miss}} &= \tan^{-1}(E_y^{\text{miss}}/E_x^{\text{miss}}), \end{aligned} \quad (4.4)$$

<sub>1148</sub> where  $E_T^{\text{miss}}$  represents the magnitude of the missing transverse energy vector  $\mathbf{E}_T^{\text{miss}}$ , and  
<sub>1149</sub>  $\phi^{\text{miss}}$  its direction in the transverse plane. The vectorial sum  $\mathbf{E}_T^{\text{miss}}$  can be broken down into

$$\mathbf{E}_T^{\text{miss}} = - \underbrace{\sum_{\text{selected electrons}} \mathbf{p}_T^e - \sum_{\text{selected muons}} \mathbf{p}_T^\mu - \sum_{\text{accepted photons}} \mathbf{p}_T^\gamma - \sum_{\text{accepted } \tau\text{-leptons}} \mathbf{p}_T^\tau}_{\text{hard term}} - \underbrace{\sum_{\text{accepted jets}} \mathbf{p}_T^{\text{jet}} - \sum_{\text{unused tracks}} \mathbf{p}_T^{\text{track}}}_{\text{soft term}}. \quad (4.5)$$

<sub>1150</sub> Two OPs are defined for  $E_T^{\text{miss}}$ , *Loose* and *Tight*, with selections on jet  $p_T$  and JVT criteria  
<sub>1151</sub> [120]. The *Tight* OP is used in this analysis; *Tight* reduces pile-up dependence of  $E_T^{\text{miss}}$   
<sub>1152</sub> by removing the phase space region containing more pile-up than hard-scatter jets, at the  
<sub>1153</sub> expense of resolution and scale at low pile-up,

## <sub>1154</sub> 4.5 Overlap removal

<sub>1155</sub> Since different objects are reconstructed independently, it is possible for the same de-  
<sub>1156</sub> tector signals to be used to reconstruct multiple objects. An overlap removal strategy is  
<sub>1157</sub> implemented to resolve ambiguities; the overlap removal process for this analysis applies  
<sub>1158</sub> selections in Table 4.1 sequentially, from top to bottom.

Table 4.1: Overlap removal process for this analysis, applied sequentially from top to bottom.

Remove	Keep	Matching criteria
Electron	Electron	Shared ID track, $p_{T,1}^e < p_{T,2}^e$
Muon	Electron	Shared ID track, CT muon
Electron	Muon	Shared ID track
Jet	Electron	$\Delta R < 0.2$
Electron	Jet	$\Delta R < 0.4$
Jet	Muon	( $\Delta R < 0.2$ or ghost-associated) & $N_{\text{track}} < 3$
Muon	Jet	$\Delta R < \min(0.4, 0.04 + 10\text{GeV}/p_T^\mu)$

## 1159 4.6 Object definition

1160 Table 4.2 summarizes the selections on physics objects used in this analysis. Each se-  
1161 lection comes with associated calibration scale factors (SFs) to account for discrepancies  
1162 between data and MC simulation, and are applied multiplicatively to MC event weights.

Table 4.2: Summary of object selection criteria used in this analysis.  $\ell_0$  refers to the leading lepton in the event.

Selection	Electrons	Muons	Jets
$p_T$ [GeV]	$> 15$ $p_T(\ell_0) > 28$	$> 15$	$> 20$
$ \eta $	$1.52 \leq  \eta  < 2.47$ $< 1.37$	$< 2.5$	$< 2.5$
Identification	<i>TightLH</i> pass ECIDS ( $ee/e\mu$ )	<i>Medium</i>	NNJvt <i>FixedEffPt</i> ( $p_T < 60$ , $ \eta  < 2.4$ )
Isolation	<i>Tight_VarRad</i>	<i>PflowTight_VarRad</i>	
Track-vertex assoc.			
$ d_0^{\text{BL}}(\sigma) $	$< 5$	$< 3$	
$ \Delta z_0^{\text{BL}} \sin \theta $ [mm]	$< 0.5$	$< 0.5$	

# 1163 Chapter 5. Data & Simulated Samples

## 1164 5.1 Data samples

1165 Data samples used in this analysis were collected by the ATLAS detector during the Run  
1166 2 data-taking campaign between 2015-2018. The samples contain  $pp$  collisions at center-of-  
1167 mass energy of  $\sqrt{s} = 13$  TeV with 25 ns bunch-spacing, which corresponds to an integrated  
1168 luminosity of  $140 \text{ fb}^{-1}$  with an uncertainty of 0.83% [89]. The HLT trigger strategy is similar  
1169 to that of previous  $t\bar{t}t\bar{t}$  observation analysis [47] and include single lepton and dilepton  
1170 triggers. Calibration for di-muon and electron-muon triggers were not ready for the samples  
1171 used in this analysis, and are therefore not included. Events are also required to contain at  
1172 least one lepton matched to the corresponding object firing the trigger. Triggers utilized in  
1173 this analysis are summarized in Table 5.1, with efficiency close to 100% when used together.

## 1174 5.2 Monte Carlo samples

1175 Monte Carlo simulated samples are used to estimate signal acceptance before unblinding,  
1176 profile the physics background for the analysis and to study object optimizations. Simulated  
1177 samples for this analysis use are generated from ATLAS generalized MC20a/d/e samples for  
1178 Run 2, using full detector simulation (FS) and fast simulation (AF3) to simulate detector  
1179 response. MC samples used and simulation processes are summarized in Table 5.2.

Table 5.1: Summary of all HLT triggers used in this analysis. Events are required to pass at least one trigger.

Trigger	Data period			
	2015	2016	2017	2018
Single electron triggers				
HLT_e24_lhmedium_L1EM20VH	✓	-	-	-
HLT_e60_lhmedium	✓	-	-	-
HLT_e120_lhloose	✓	-	-	-
HLT_e26_lhtight_nod0_ivarloose	-	✓	✓	✓
HLT_e60_lhmedium_nod0	-	✓	✓	✓
HLT_e140_lhloose_nod0	-	✓	✓	✓
Di-electron triggers				
HLT_2e12_lhloose_L12EM10VH	✓	-	-	-
HLT_2e17_lhvloose_nod0	-	✓	-	-
HLT_2e24_lhvloose_nod0	-	-	✓	✓
HLT_2e17_lhvloose_nod0_L12EM15VHI	-	-	-	✓
Single muon trigger				
HLT_mu20_iloose_L1MU15	✓	-	-	-
HLT_mu40	✓	-	-	-
HLT_mu26_ivarmedium	-	✓	✓	✓
HLT_mu50	-	✓	✓	✓

### <sup>1180</sup> 5.2.1 $t\bar{t}Z'$ signal samples

<sup>1181</sup> Signal  $t\bar{t}Z'$  samples were generated based on the simplified topophilic resonance model in  
<sup>1182</sup> section 2.2.1. Six  $Z'$  mass points were utilized for the generation of the signal sample: 1000,  
<sup>1183</sup> 1250, 1500, 2000, 2500 and 3000 GeV. The top- $Z'$  coupling  $c_t$  is chosen to be 1 for a narrow  
<sup>1184</sup> resonance peak, and the chirality angle  $\theta$  is chosen to be  $\pi/4$  to suppress loop production  
<sup>1185</sup> of  $Z'$ . The samples were then generated with MADGRAPH5\_AMC@NLO v.3.5.0 [121] at  
<sup>1186</sup> LO with the NNPDF3.1LO [122] PDF set interfaced with PYTHIA8 [123] using A14 tune  
<sup>1187</sup> and NNPDF2.3lo PDF set for parton showering and hadronization. The resonance width is  
<sup>1188</sup> calculated to be 4% for  $c_t = 1$ .

Table 5.2: Summary of all Monte-Carlo samples used in this analysis.  $V$  refers to an EW ( $W^\pm/Z/\gamma^*$ ) or Higgs boson. Matrix element (ME) order refers to the order in QCD of the perturbative calculation. Tune refers to the underlying-event tune of the parton shower (PS) generator.

Process	ME Generator	ME Order	ME PDF	PS	Tune	Sim.
<b>Signals</b>						
$t\bar{t}Z'$	MADGRAPH5_AMC@NLO LO		NNPDF3.1LO		PYTHIA8 A14	FS
<b><math>t\bar{t}t\bar{t}</math> and <math>t\bar{t}\bar{t}</math></b>						
$t\bar{t}t\bar{t}$	MADGRAPH5_AMC@NLO NLO		NNPDF3.0nlo		PYTHIA8 A14	AF3
	MADGRAPH5_AMC@NLO NLO		MMHT2014 LO		HERWIG7 H7-UE-MMHT	AF3
	SHERPA	NLO	NNPDF3.0nnlo		HERWIG7 SHERPA	FS
$t\bar{t}\bar{t}$	MADGRAPH5_AMC@NLO LO		NNPDF2.3lo		PYTHIA8 A14	AF3
<b><math>t\bar{t}V</math></b>						
$t\bar{t}H$	POWHEGBOX v2	NLO	NNPDF3.0nlo		PYTHIA8 A14	FS
	POWHEGBOX v2	NLO	NNPDF3.0nlo		HERWIG7 H7.2-Default	FS
$t\bar{t}(Z/\gamma^*)$	MADGRAPH5_AMC@NLO NLO		NNPDF3.0nlo		PYTHIA8 A14	FS
	SHERPA	NLO	NNPDF3.0nnlo		SHERPA SHERPA	FS
$t\bar{t}W$	SHERPA	NLO	NNPDF3.0nnlo		SHERPA SHERPA	FS
	SHERPA	LO	NNPDF3.0nnlo		SHERPA SHERPA	FS
<b><math>t\bar{t}</math> and Single-Top</b>						
$t\bar{t}$	POWHEGBOX v2	NLO	NNPDF3.0nlo		PYTHIA8 A14	FS
$tW$	POWHEGBOX v2	NLO	NNPDF3.0nlo		PYTHIA8 A14	FS
$t(q)b$	POWHEGBOX v2	NLO	NNPDF3.0nlo (s)		PYTHIA8 A14	FS
			NNPDF3.0nlo 4f (t)			FS
$tWZ$	MADGRAPH5_AMC@NLO NLO		NNPDF3.0nlo		PYTHIA8 A14	FS
$tZ$	MADGRAPH5_AMC@NLO LO		NNPDF3.0nlo 4f		PYTHIA8 A14	FS
<b><math>t\bar{t}VV</math></b>						
$t\bar{t}WW$	MADGRAPH5_AMC@NLO LO		NNPDF3.0nlo		PYTHIA8 A14	FS
$t\bar{t}WZ$	MADGRAPH	LO	NNPDF3.0nlo		PYTHIA8 A14	AF3
$t\bar{t}HH$	MADGRAPH	LO	NNPDF3.0nlo		PYTHIA8 A14	AF3
$t\bar{t}WH$	MADGRAPH	LO	NNPDF3.0nlo		PYTHIA8 A14	AF3
$t\bar{t}ZZ$	MADGRAPH	LO	NNPDF3.0nlo		PYTHIA8 A14	AF3
<b><math>V(VV)+\text{jets}</math> and <math>VH</math></b>						
$V+\text{jets}$	SHERPA	NLO	NNPDF3.0nnlo		SHERPA SHERPA	FS
$VV+\text{jets}$	SHERPA	NLO	NNPDF3.0nnlo		SHERPA SHERPA	FS
		LO ( $gg \rightarrow VV$ )				FS
$VVV+\text{jets}$	SHERPA	NLO	NNPDF3.0nnlo		SHERPA SHERPA	FS
$VH$	POWHEGBOX v2	NLO	NNPDF3.0aznlo		PYTHIA8 A14	FS

<sub>1189</sub> **5.2.2 Background samples**

<sub>1190</sub> **SM  $t\bar{t}t\bar{t}$  background**

<sub>1191</sub> The nominal SM  $t\bar{t}t\bar{t}$  sample was generated with MADGRAPH5\_AMC@NLO [121] at  
<sub>1192</sub> NLO in QCD with the NNPDF3.0nlo [122] PDF set and interfaced with PYTHIA8.230 [123]  
<sub>1193</sub> using A14 tune [124]. Decays for top quarks are simulated at LO with MADSPIN [125,  
<sub>1194</sub> 126] to preserve spin information, while decays for  $b$ - and  $c$ -hadrons are simulated with  
<sub>1195</sub> EVTGEN v1.6.0 [127]. The renormalization and factorization scales  $\mu_R$  and  $\mu_F$  are set  
<sub>1196</sub> to  $1/4\sqrt{m^2 + p_T^2}$ , which represents the sum of transverse mass of all particles generated  
<sub>1197</sub> from the ME calculation [128]. The ATLAS detector response was simulated with AF3.  
<sub>1198</sub> Additional auxiliary  $t\bar{t}t\bar{t}$  samples are also generated to evaluate the impact of generator and  
<sub>1199</sub> PS uncertainties as shown in 5.2.

<sub>1200</sub>  **$t\bar{t}W$  background**

<sub>1201</sub> Nominal  $t\bar{t}W$  sample was generated using SHERPA v2.2.10 [129] at NLO in QCD with  
<sub>1202</sub> the NNPDF3.0nnlo [122] PDF with up to one extra parton at NLO and two at LO, which  
<sub>1203</sub> are matched and merged with the SHERPA PS based on Catani-Seymour dipole factorization  
<sub>1204</sub> [130] using the MEPS@NLO prescription [131–134] and a merging scale of 30 GeV. Higher-  
<sub>1205</sub> order ME corrections are provided in QCD by the OpenLoops 2 library [135–137] and in  
<sub>1206</sub> EW from  $\mathcal{O}(\alpha^3) + \mathcal{O}(\alpha_S^2\alpha^2)$  (LO3 & NLO2) via two sets of internal event weights. An  
<sub>1207</sub> alternative sample with only EW corrections at LO from  $\mathcal{O}(\alpha_S\alpha^3)$  (NLO3) diagrams were  
<sub>1208</sub> also simulated with the same settings.

1209  **$t\bar{t}(Z/\gamma^*)$  background**

1210 Nominal  $t\bar{t}(Z/\gamma^*)$  samples were generated separately for different ranges of dilepton in-  
1211 variant mass  $m_{\ell\ell}$  to account for on-shell and off-shell  $Z/\gamma^*$  production. Sample for  $m_{\ell\ell}$   
1212 between 1 and 5 GeV was produced using MADGRAPH5\_AMC@NLO [121] at NLO with  
1213 the NNPDF3.0nlo [122] PDF set, interfaced with PYTHIA8.230 [123] using A14 tune [124] and  
1214 NNPDF2.3l0 PDF set. Sample for  $m_{\ell\ell} < 5$  GeV was produced with SHERPA v2.2.10 [129]  
1215 at NLO using NNPDF3.0nnl0 PDF set. To account for generator uncertainty, an alternative  
1216  $m_{\ell\ell} > 5$  GeV sample was generated with identical settings to the low  $m_{\ell\ell}$  sample. The  
1217 ATLAS detector response was simulated with full detector simulation (FS).

1218  **$t\bar{t}H$  background**

1219 Generation of  $t\bar{t}H$  background was done using POWHEGBox [138–141] at NLO in QCD  
1220 with the NNPDF3.0nlo PDF [122] set. The nominal sample is interfaced with PYTHIA8.230  
1221 [123] using the A14 tune [124] and the NNPDF2.3l0 [142] PDF set. Detector response is  
1222 simulated using FS. An alternative  $t\bar{t}H$  sample generated similarly, but instead interfaced  
1223 with HERWIG7.2.3 [143, 144] to study the impact of parton shower and hadronization model.  
1224 Detector response for the alternative sample is simulated using AF3.

1225  **$t\bar{t}t$  background**

1226 The  $t\bar{t}t$  sample is generated using MADGRAPH5\_AMC@NLO [121] at LO in QCD, inter-  
1227 faced with PYTHIA8 [123] using the A14 tune [124]. The sample is produced in the five-flavor  
1228 scheme [145] to prevent LO interference with  $t\bar{t}t\bar{t}$ .

1229  **$t\bar{t}$  background**

1230 The  $t\bar{t}$  sample is modeled with POWHEGBox [138–141] at NLO in QCD with the NNPDF3.0nlo  
1231 [122] PDF set and the  $h_{\text{damp}}$  parameter set to  $1.5m_{\text{top}}$  [146]. Events are interfaced with  
1232 PYTHIA8.230 [123] using the A14 tune [124] and the NNPDF2.3lō [142] PDF set.

1233 **Single-top ( $tW$  &  $t(q)b$ ) background**

1234 Single-top  $tW$ -associated production is modeled using the POWHEGBox generator [138–  
1235 141] at NLO in QCD in the five-flavor scheme [145] with the NNPDF3.0nlo [122] PDF set. In-  
1236 terference with  $t\bar{t}$  production [146] is handled using the diagram removal scheme [147]. Single-  
1237 top  $t(q)b$  production is modeled using the POWHEGBox generator at NLO in QCD with the  
1238 s-channel production modeled in the five-flavor scheme with the NNPDF3.0nlo PDF set, while  
1239 the t-channel production is modeled in the four-flavor scheme with the NNPDF3.0nlo 4f [122]  
1240 PDF set. The  $t\bar{t}WW$  contributions are normalized to NLO theoretical cross section. All  
1241 single-top samples are interfaced with PYTHIA8.230 [123] using the A14 tune [124] and the  
1242 NNPDF2.3lō [142] PDF set.

1243  **$tWZ +\text{jets}$  background**

1244 The  $tWZ$  sample is generated using MADGRAPH5\_AMC@NLO [121] at NLO in QCD  
1245 with the NNPDF3.0nlo [122] PDF set, interfaced with PYTHIA8.212 [123] using the A14 tune  
1246 [124] and the NNPDF2.3lō [142] PDF set.

1247  **$tZ$  &  $t\bar{t}VV$  background**

1248 Production of  $tZ$  is modeled using MADGRAPH5\_AMC@NLO [121] at NLO in QCD  
1249 with scale of  $H_T/6$  and the NNPDF3.0nlo 4f [122] PDF set. Production of  $t\bar{t}WW$  is modeled

1250 using `MADGRAPH5_AMC@NLO` [121] at LO, while production of  $t\bar{t}WZ$ ,  $t\bar{t}HH$ ,  $t\bar{t}WH$  and  
1251  $t\bar{t}ZZ$  are modeled using `MADGRAPH` at LO. All  $t\bar{t}VV$  samples use the `NNPDF3.0nlo` [122]  
1252 PDF set, and all samples in this section are interfaced with `PYTHIA8` [123] using the A14  
1253 tune [124].

#### 1254 Single boson ( $V$ ) +jets background

1255 Production of  $V$ +jets is modeled with `SHERPA v2.2.10` [129] using NLO ME for up to two  
1256 jets and LO ME for up to four jets, with the `NNPDF3.0nlo` [122] PDF set. Matrix elements  
1257 are calculated with the Comix [148] and OpenLoops libraries [135, 136] and matched with  
1258 the `SHERPA` PS based on Catani-Seymour dipole factorization [130] using the MEPS@NLO  
1259 prescription [131–134]. The sample is normalized to the NNLO [149] theoretical cross section.

#### 1260 Diboson ( $VV$ ) +jets background

1261 Diboson samples are simulated with `SHERPA v2.2.14` [129] with the `NNPDF3.0nlo` [122]  
1262 PDF set. Fully leptonic and semileptonic final states are generated using NLO ME for up to  
1263 one extra parton and LO ME for up to three extra parton emissions. Loop-induced processes  
1264 are generated using LO ME for up to one extra parton. Matrix elements are matched and  
1265 merged with the `SHERPA` PS based on Catani-Seymour dipole factorization [130] using the  
1266 MEPS@NLO prescription [131–134]. Virtual QCD ME corrections are provided by the  
1267 OpenLoops library [135, 136].

#### 1268 Triboson ( $VVV$ ) +jets background

1269 The triboson sample is modeled with `SHERPA v2.2.10` [129] using factorized gauge boson  
1270 decays. Matrix elements for the inclusive process at NLO and up to two extra partons at

<sub>1271</sub> LO are matched and merged with the SHERPA PS based on Catani-Seymour dipole factor-  
<sub>1272</sub> ization [130] using the MEPS@NLO prescription [131–134]. Virtual QCD ME corrections  
<sub>1273</sub> are provided by the OpenLoops library [135, 136].

<sub>1274</sub> ***VH* background**

<sub>1275</sub> Generation of  $WH$  and  $ZH$  samples is performed using PowhegBox [138–141] at NLO  
<sub>1276</sub> with the NNPDF3.0aznlo [122] PDF set, interfaced with PYTHIA8.230 [123] using the A14  
<sub>1277</sub> tune [124] and the NNPDF2.3l0 [142] PDF set.

<sub>1278</sub> **Chapter 6. Analysis Strategy**

<sub>1279</sub> **6.1 Event selection**

<sub>1280</sub> Events for the analysis first are preselected following a list of criteria to optimize for event  
<sub>1281</sub> quality and background rejection. The following criteria are applied sequentially from top  
<sub>1282</sub> to bottom along with cleaning and veto cuts

<sub>1283</sub> 1. **Good Run List (GRL)**: data events must be part of a predefined list of suitable  
<sub>1284</sub> runs and luminosity blocks [[150](#)].

<sub>1285</sub> 2. **Primary vertex**: events must have at least one reconstructed vertex matched to 2 or  
<sub>1286</sub> more associated tracks with  $p_T > 500$  MeV.

<sub>1287</sub> 3. **Trigger**: events must be selected by at least one trigger in Table 5.1.

<sub>1288</sub> 4. **Kinematic selection**: events must have exactly two *Tight* leptons with the same  
<sub>1289</sub> electric charge, or at least three *Tight* leptons of any charge. The leading lepton must  
<sub>1290</sub> have  $p_T > 28$  GeV, and all leptons must satisfy  $p_T > 15$  GeV.

<sub>1291</sub> Events are separated into two channels based on the number of leptons: same-sign di-  
<sub>1292</sub> lepton (SS2L) for events with exactly two leptons of the same charge, or multilepton (ML)  
<sub>1293</sub> for events with three or more leptons. The channels are further separated into regions defined  
<sub>1294</sub> in section 6.2 to prepare for analysis.

<sub>1295</sub> Additional selections are applied based on the lepton flavors present. In the SS2L channel,  
<sub>1296</sub> if both leptons are electrons, the invariant mass  $m_{ll}$  must satisfy  $m_{ll} < 81$  GeV and  $m_{ll} > 101$   
<sub>1297</sub> GeV to suppress background involving  $Z$ -bosons. In the ML channel, the same criteria must  
<sub>1298</sub> be satisfied for every opposite-sign same-flavor pair of leptons in an event.

### 1299 6.1.1 Event categorization

1300 Simulated events are categorized using truth information of leptons ( $e/\mu$ ) and their orig-  
1301 inating MC particle (mother-particle). Each lepton can be classified as either prompt or  
1302 non-prompt, with non-prompt leptons further categorized for background estimation pur-  
1303 poses. If an event contains only prompt leptons, the event is classified as its corresponding  
1304 process. If the event contains one non-prompt lepton, the event is classified as the corre-  
1305 sponding type of the non-prompt lepton. If the event contains more than one non-prompt  
1306 lepton, the event is classified as other.

1307 • **Prompt:** if the lepton originates from  $W/Z/H$  boson decays, or from a mother-  
1308 particle created by a final state photon.

1309 • **Non-prompt:**

1310 – **Charge-flip ( $e$  only):** if the reconstructed charge of the lepton differs from that  
1311 of the first mother-particle.

1312 – **Material conversion ( $e$  only):** if the lepton originated from a photon conversion  
1313 and the mother-particle is an isolated prompt photon, non-isolated final state  
1314 photon, or heavy boson.

1315 –  **$\gamma^*$ -conversion ( $e$  only):** if the lepton originated from a photon conversion and  
1316 the mother-particle is a background electron.

1317 – **Heavy flavor decay:** if the lepton originated from a  $b$ - or  $c$ -hadron.

1318 – **Fake:** if the lepton originated from a light- or  $s$ -hadron, or if the truth type of  
1319 the lepton is hadron.

1320 – **Other:** any lepton that does not belong to one of the above categories.

## 1321 6.2 Analysis regions

1322 Events are selected and categorized into analysis regions belonging to one of two types:  
 1323 control regions (CRs) enriched in background events, and signal regions (SRs) enriched in  
 1324 signal events. This allows for the examination and control of backgrounds and systematic  
 1325 uncertainties, as well as study of signal sensitivities. The signal is then extracted from the  
 1326 SRs with a profile LH fit using all regions. The full selection criteria for each region are  
 1327 summarized in Table 6.1. The post-fit background compositions in different CRs and SR  
 1328 sub-regions are shown in Figure 6.1.

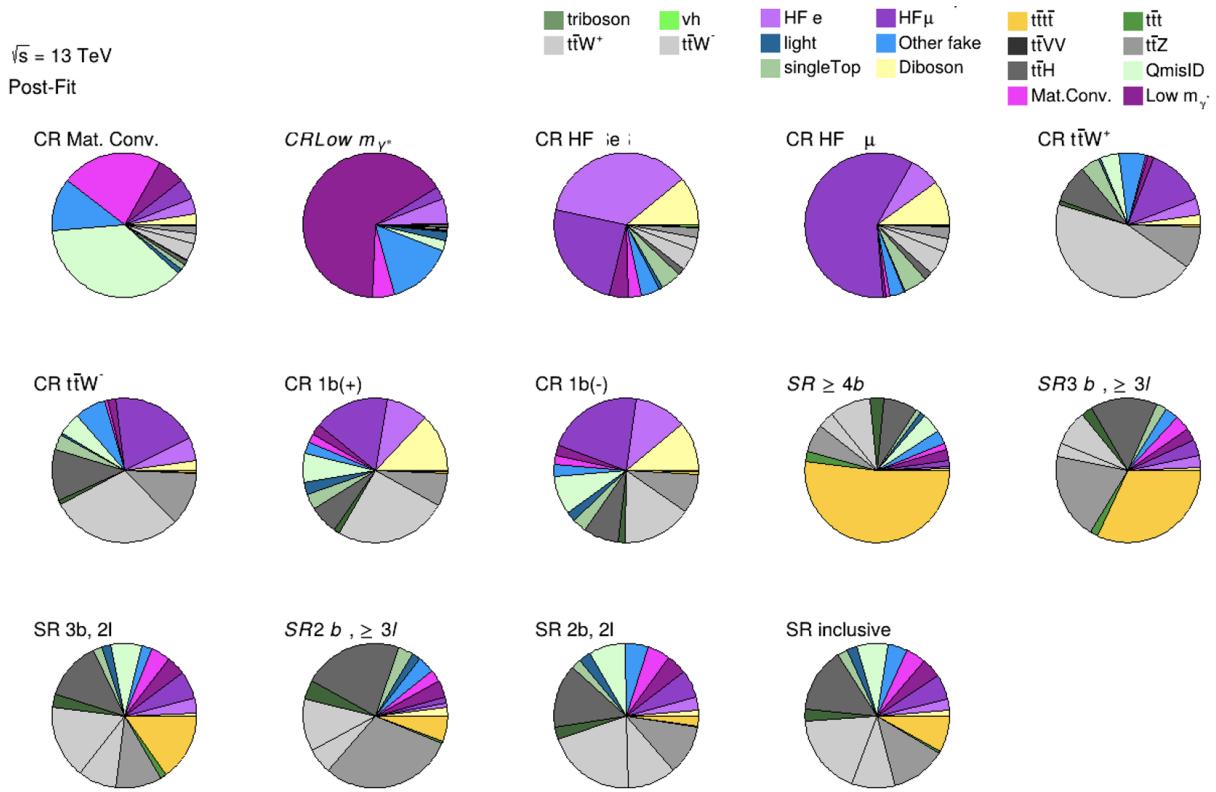


Figure 6.1: Post-fit background composition in each analysis region and sub-region. The fit was performed using ideal pseudo-datasets (Asimov data) in the SR.

Table 6.1: Definitions of signal, control and validation regions (VR) used in this analysis.  $N_{\text{jets}}$  and  $N_b$  refers to the number of jets and number of  $b$ -tagged jets respectively.  $\ell_1$  refers to the leading lepton,  $\ell_2$  refers to the subleading lepton and so on.  $H_T$  refers to the  $p_T$  scalar sum of all leptons and jets in the event.  $m_{\ell\ell}$  refers to the dilepton invariant mass, which must not coincide with the  $Z$ -boson mass range of 81-101 GeV for SS2L+3L events.

Region	Channel	$N_{\text{jets}}$	$N_b$	Other selections	Fitted variable
CR Low $m_{\gamma^*}$	SS $e\ell$	[4, 6)	$\geq 1$	$\ell_1/\ell_2$ is from virtual photon decay $\ell_1 + \ell_2$ not from material conversion	event yield
CR Mat. Conv.	SS $e\ell$	[4, 6)	$\geq 1$	$\ell_1/\ell_2$ is from material conversion $\ell_1 + \ell_2$ not conversion candidates	event yield
CR HF $\mu$	$\ell\mu\mu$	$\geq 1$	1	$100 < H_T < 300$ GeV $E_T^{\text{miss}} > 35$ GeV total charge = $\pm 1$	$p_T(\ell_3)$
CR HF $e$	$e\ell\ell$	$\geq 1$	1	$\ell_1 + \ell_2$ not conversion candidates $100 < H_T < 275$ GeV $E_T^{\text{miss}} > 35$ GeV total charge = $\pm 1$	$p_T(\ell_3)$
CR $t\bar{t}W^+$	SS $\ell\mu$	$\geq 4$	$\geq 2$	$ \eta(e)  < 1.5$ for $N_b = 2$ : $H_T < 500$ GeV or $N_{\text{jets}} < 6$ for $N_b \geq 3$ : $H_T < 500$ GeV total charge > 0	$N_{\text{jets}}$
CR $t\bar{t}W^-$	SS $\ell\mu$	$\geq 4$	$\geq 2$	$ \eta(e)  < 1.5$ for $N_b = 2$ : $H_T < 500$ GeV or $N_{\text{jets}} < 6$ for $N_b \geq 3$ : $H_T < 500$ GeV total charge < 0	$N_{\text{jets}}$
CR 1b(+)	SS2L+3L	$\geq 4$	1	$\ell_1 + \ell_2$ not from material conversion $H_T > 500$ GeV total charge > 0	$N_{\text{jets}}$
CR 1b(-)	SS2L+3L	$\geq 4$	1	$\ell_1 + \ell_2$ not from material conversion $H_T > 500$ GeV total charge < 0	$N_{\text{jets}}$
VR $t\bar{t}Z$	3L $\ell^\pm\ell^\mp$	$\geq 4$	$\geq 2$	$m_{\ell\ell} \in [81, 101]$ GeV	$N_{\text{jets}}, m_{\ell\ell}$
VR $t\bar{t}W +1b$	SS2L+3L			CR $t\bar{t}W^\pm$    CR 1b( $\pm$ )	$N_{\text{jets}}$
VR $t\bar{t}W +1b+SR$	SS2L+3L			CR $t\bar{t}W^\pm$    CR 1b( $\pm$ )    SR	$N_{\text{jets}}$
SR	SS2L+3L	$\geq 6$	$\geq 2$	$H_T > 500$ GeV $m_{\ell\ell} \notin [81, 101]$ GeV	$H_T$

<sub>1329</sub> **6.2.1 Signal regions**

<sub>1330</sub> All events selected for the SR must satisfy the following criteria:

- <sub>1331</sub> • Contains 6 or more jets, with at least 2 jets  $b$ -tagged at the 85% OP.
- <sub>1332</sub> • Scalar sum of the transverse momenta of all leptons and jets  $H_T > 500$  GeV.
- <sub>1333</sub> • Dilepton invariant mass  $m_{\ell\ell}$  does not coincide with the  $Z$ -boson mass range of 81 – 101 <sub>1334</sub> GeV

<sub>1335</sub> The SR is further divided into sub-regions by the number of  $b$ -tagged jets and leptons <sub>1336</sub> present to study signal behavior and sensitivity with respect to the selection variables.

Table 6.2: Definitions of SR sub-regions. Events are sorted into different sub-regions based on the number of  $b$ -tagged jets and leptons present.

Sub-region	Selection criteria	
	$b$ -jets	leptons
SR 2b2l	$N_b = 2$	$N_l = 2$
SR 2b3l4l	$N_b = 2$	$N_l \geq 3$
SR 3b2l	$N_b = 3$	$N_l = 2$
SR 3b3l4l	$N_b = 3$	$N_l \geq 3$
SR 4b	$N_b \geq 4$	

<sub>1337</sub> **Signal extraction**

<sub>1338</sub> Signal extraction in the SR is performed via a binned profile likelihood (LH) fit as de-

<sub>1339</sub> scribed in section 8.1 using  $H_T$  as the discriminant observable. The discriminant observable

<sub>1340</sub> for a LH fit serves as the set of observed data upon which the LH function is constructed.

<sub>1341</sub> Ideally, the chosen observable shows significant separation between the functional forms of

<sub>1342</sub> the signal and background distributions, allowing for effective separation of the two. Fig-

<sub>1343</sub> ure 6.2 shows several pre-fit kinematic distributions in the inclusive SR. From empirical

1344 optimization studies,  $H_T$  possesses good discriminating power compared to other observ-  
1345 ables constructed using event-level information.

### 1346 6.2.2 Control regions

1347 Control regions are defined for each background to be enriched in the targeted process, in  
1348 order to maximize the background's purity and minimize contamination from other sources  
1349 within the region. This helps to constrain and reduce correlation between background nor-  
1350 malization factors in the final fit. Fit variables and selection criteria are determined via  
1351 optimization studies performed on CRs that aimed to achieve the largest discriminating  
1352 power possible between the target background and other event types.

#### 1353 $t\bar{t}W$ background CRs

1354 Theoretical modeling for  $t\bar{t}W + \text{jets}$  background in the phase space of this analysis suffers  
1355 from large uncertainties, especially at high jet multiplicities [151]. A data-driven method was  
1356 employed in a similar manner to the SM  $t\bar{t}t\bar{t}$  observation analysis [47] to mitigate this effect  
1357 and is described in further details in section 6.3.3. The method necessitates the definition of  
1358 two groups of dedicated CRs to estimate the flavor composition and normalization of  $t\bar{t}W$   
1359 + jets background: CR  $t\bar{t}W + \text{jets}$  to constrain flavor composition, and CR 1b to constrain  
1360 the jet multiplicity spectrum. These are further split into CR  $t\bar{t}W^\pm$  and CR 1b( $\pm$ ) due to  
1361 the pronounced asymmetry in  $t\bar{t}W$  production from  $pp$  collisions, with  $t\bar{t}W^+$  being produced  
1362 at approximately twice the rate of  $t\bar{t}W^-$  [152].

1363 Events in CR  $t\bar{t}W^\pm$  are required to contain at least two  $b$ -tagged jets similar to the SR  
1364 to determine the  $t\bar{t}W$  normalization within an SR-related phase space. Orthogonality with  
1365 SR is ensured by requiring  $H_T < 500$  GeV or  $N_{\text{jets}} < 6$  when  $N_b = 2$ , and  $H_T < 500$

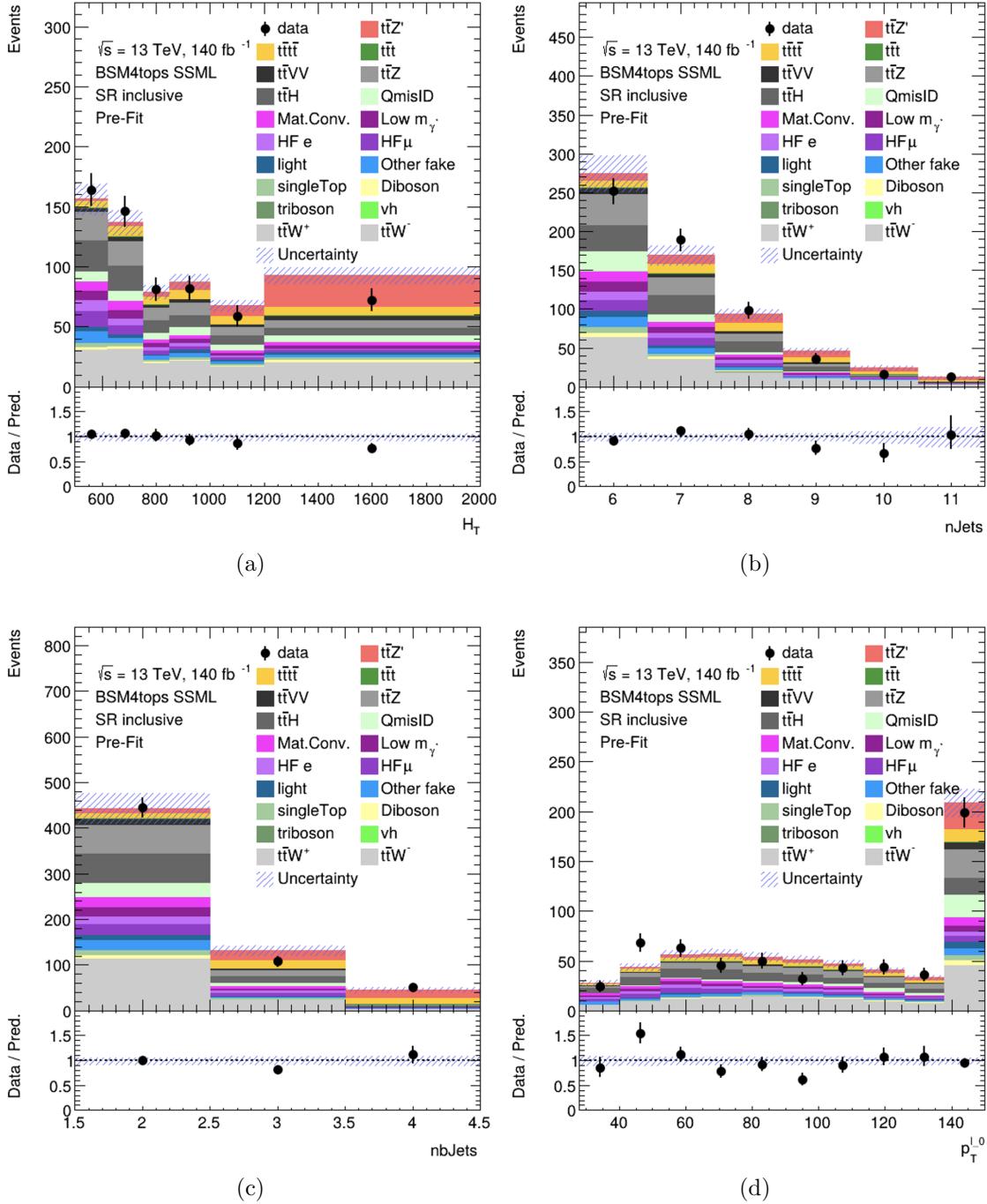


Figure 6.2: Pre-fit kinematic distributions and event compositions in the inclusive SR for (a)  $H_T$  i.e. scalar sum of  $p_T$  of all objects in the event, (b) jet multiplicity, (c)  $b$ -jet multiplicity, (d) leading lepton  $p_T$ . The shaded band represents the uncertainty in the total distribution. The first and last bins of each distribution contain underflow and overflow events respectively.

1366 GeV when  $N_b \geq 3$ . Events in CR 1b( $\pm$ ) are required to have  $H_T > 500$  GeV and at least  
 1367 four jets to encompass events with high  $N_{\text{jets}}$ , which can be used to determine the  $t\bar{t}W$  jet  
 1368 multiplicity spectrum for fitting  $a_{0,1}$ . The selection criteria also include exactly one  $b$ -tagged  
 1369 jet to maintain orthogonality with the SR.

### 1370 **Fake/non-prompt background CRs**

1371 Selection for fake/non-prompt CRs are determined using the `DFCommonAddAmbiguity`  
 1372 (`DFCAA`) variable for reconstructed leptons.

Table 6.3: List of possible assigned values for DFCAA.

DFCAA	Description
-1	No 2nd track found
0	2nd track found, no conversion found
1	Virtual photon conversion candidate
2	Material conversion candidate

1373 Four CRs are defined for the three main types of fake/non-prompt backgrounds in the  
 1374 analysis - virtual photon ( $\gamma^*$ ) conversion, photon conversion in detector material (Mat.  
 1375 Conv.) and heavy flavor decays (HF). The full selection criteria for fake/non-prompt CRs  
 1376 are shown in Table 6.1.

- 1377 • **Low  $m_\gamma^*$ :** events with an  $e^+e^-$  pair produced from a virtual photon.

1378 Events are selected if there are two same-sign leptons with at least one electron recon-  
 1379 structed as an internal conversion candidate, and neither reconstructed as a material  
 1380 conversion candidate.

- 1381 • **Mat. Conv.:** events with an electron originating from photon conversion within the  
 1382 detector material.

1383 Events are selected if there are two same-sign leptons with at least one electron recon-  
1384 structed as a material conversion candidate.

1385 • **HF  $e(\mu)$ :** events with a reconstructed non-prompt lepton from semi-leptonic decays of  
1386  $b$ - and  $c$ -hadrons (heavy flavor decays).

1387 Events are selected if there are three leptons with at least two electrons (muons), with  
1388 no lepton reconstructed as a conversion candidate.

## 1389 6.3 Background estimation

1390 Background in this analysis consist of SM processes that can result in a signal signature  
1391 similar to a  $t\bar{t}t\bar{t}$  SSML final state and can be divided into two types, reducible and irreducible.

1392 Reducible background consists of processes that do not result in a SSML final state physically,  
1393 but are reconstructed as such due to detector and reconstruction effects. The main types  
1394 of reducible background considered are charge misidentification (QmisID) and fake/non-

1395 prompt leptons. Fake/non-prompt lepton backgrounds contaminate the SR when a non-  
1396 prompt lepton is reconstructed as a prompt lepton in a  $t\bar{t}$ -associated process, leading to  
1397 a similar final state to that of SSML  $t\bar{t}t\bar{t}$ . These backgrounds are estimated using the

1398 template fitting method described in subsection 6.3.1, where MC simulations are normalized  
1399 to their theoretical SM cross section via floating normalization factors (NFs) constrained by

1400 the corresponding CRs. Lepton charge misidentification background contaminates the SR  
1401 similarly when one of the two leptons in a  $t\bar{t}$ -associated process with two opposite-sign leptons

1402 is misidentified, producing a SS2L  $t\bar{t}t\bar{t}$  final state. Charge misidentification background is  
1403 estimated using a data-driven method described in section 6.3.2 along with ECIDS described

1404 in section 4.3.1.

1405 Irreducible background consists of SM processes that result in SSML final states with all  
1406 leptons being prompt. The dominating background in the SR are SM  $t\bar{t}t\bar{t}$ ,  $t\bar{t}W$ ,  $t\bar{t}Z$ , and  
1407  $t\bar{t}H$  production with smaller contributions from  $VV$ ,  $VVV$ ,  $VH$  and rarer processes like  
1408  $t\bar{t}VV$ ,  $tWZ$ ,  $tZq$  and  $t\bar{t}t$ . Most irreducible backgrounds are estimated using template fitting  
1409 method, with the exception of  $t\bar{t}W$  +jets background. The  $t\bar{t}W$  +jets background is instead  
1410 given four dedicated CRs, and estimated using a data-driven method with a fitted function  
1411 parameterized in  $N_{\text{jets}}$ . All CRs and SR are included in the final profile LH fit to data.

### 1412 6.3.1 Template fitting for fake/non-prompt estimation

1413 The template fitting method is a semi-data-driven approach [151] that estimates fake/non-  
1414 prompt background distributions by fitting the MC kinematic profile of background processes  
1415 arising from fake/non-prompt leptons to data. The four main sources of fake/non-prompt  
1416 leptons are generated from  $t\bar{t}$  +jets samples and are constrained by four CRs enriched with  
1417 the corresponding backgrounds. Each of the aforementioned background is assigned a free-  
1418 floating NF resulting in  $\text{NF}_{\text{HF } e}$ ,  $\text{NF}_{\text{HF } \mu}$ ,  $\text{NF}_{\text{Mat. Conv.}}$  and  $\text{NF}_{\text{Low } m_{\gamma^*}}$ . The NFs are fitted  
1419 simultaneously with the signal within their constraining CRs.

### 1420 6.3.2 Charge misidentification data-driven estimation

1421 The  $ee$  and  $e\mu$  channels in the SS2L  $t\bar{t}t\bar{t}$  region are contaminated with opposite-sign  
1422 (OS) dilepton  $t\bar{t}$ -associated events where one electron has its charge misidentified. Charge  
1423 misidentification (QmisID) largely affects electrons due to muons' precise curvature informa-  
1424 tion using ID and MS measurements and low bremsstrahlung rate. The charge flip rates are  
1425 significant at higher  $p_T$  and varies with  $|\eta|$  which is proportional to the amount of detector

1426 material the electron interacted with.

1427 The charge flip probability  $\epsilon$  is estimated in this analysis with a data-driven method  
1428 [153] using a sample of  $Z \rightarrow e^+e^-$  events with additional constraints on the invariant mass  
1429  $m_{ee}$  to be within 10 GeV of the  $Z$ -boson mass. The  $Z$ -boson mass window is defined to  
1430 be within  $4\sigma$  to include most events within the peak, and is determined by fitting the  $m_{ee}$   
1431 spectrum of the two leading electrons to a Breit-Wigner function, resulting in a range of  
1432 [65.57, 113.49] for SS events and [71.81, 109.89] for OS events. Background contamination  
1433 near the peak is assumed to be uniform and subtracted using a sideband method. Since the  
1434  $Z$ -boson decay products consist of a pair of opposite-sign electrons, all same-sign electron  
1435 pairs are considered affected by charge misidentification.

1436 Let  $N_{ij}^{\text{SS}}$  be the number of events with SS electrons with the leading electron in the  
1437  $i^{\text{th}}$  2D bin in  $(p_T, |\eta|)$  and the sub-leading electron in the  $j^{\text{th}}$  bin. Assuming the QmisID  
1438 probabilities of electrons in an event are uncorrelated,  $N_{ij}^{\text{SS}}$  can be estimated as

$$N_{ij}^{\text{SS}} = N_{ij}^{\text{tot}} [\epsilon_i(1 - \epsilon_j) + \epsilon_j(1 - \epsilon_i)], \quad (6.1)$$

1439 where  $N_{ij}^{\text{tot}}$  is the total number of events in the  $i^{\text{th}}$  and  $j^{\text{th}}$  bin regardless of charge, and  
1440  $\epsilon_{i(j)}$  is the QmisID rate in the  $i^{\text{th}}(j^{\text{th}})$  bin. Assuming  $N_{ij}^{\text{SS}}$  follows a Poisson distribution  
1441 around the expectation value  $\bar{N}_{ij}^{\text{SS}}$ , the  $(i, n)^{\text{th}}$  rate  $\epsilon$  can be estimated by minimizing a  
1442 negative-LLH function parameterized in  $p_T$  and  $|\eta|$ ,

$$\begin{aligned}
-\ln(\mathcal{L}(\epsilon|N_{\text{SS}})) &= -\ln \prod_{ij} \frac{(N_{ij}^{\text{tot}})^{N_{ij}^{\text{SS}}} \cdot e^{N_{ij}^{\text{tot}}}}{N_{ij}^{\text{SS}}!} \\
&= -\sum_{ij} \left[ N_{ij}^{\text{SS}} \ln(N_{ij}^{\text{tot}}(\epsilon_i(1-\epsilon_j) + \epsilon_j(1-\epsilon_i))) - N_{ij}^{\text{tot}}(\epsilon_i(1-\epsilon_j) + \epsilon_j(1-\epsilon_i)) \right]. \tag{6.2}
\end{aligned}$$

1443 The QmisID rates are then calculated separately for SR and CRs with different electron  
 1444 definitions i.e. CR Low  $m_{\gamma^*}$ , CR Mat. Conv., CR  $t\bar{t}W^\pm$ , using events from data after  
 1445 applying region-specific lepton selections and ECIDS. The events are required to satisfy  
 1446 SS2L kinematic selections but contains OS electrons. The following weight is applied to OS  
 1447 events to correct for misidentified SS events within the region,

$$w = \frac{\epsilon_i + \epsilon_j - 2\epsilon_i\epsilon_j}{1 - \epsilon_i - \epsilon_j + 2\epsilon_i\epsilon_j}. \tag{6.3}$$

1448 The QmisID rates calculated for SR and CR  $t\bar{t}W$  are shown in Figure 6.3

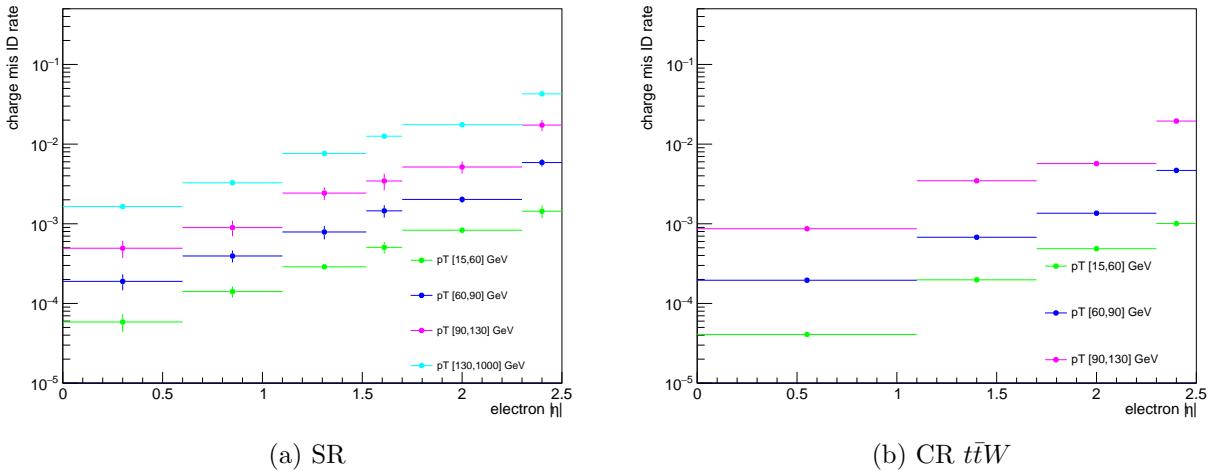


Figure 6.3: Charge flip rate calculated for SR and CR  $t\bar{t}W$  in bins of  $|\eta|$  and  $p_T$ .

1449        The QmisID rates obtained after applying  $w$  contain a dependency on jet multiplicity  
 1450        and are underestimated at higher  $N_{\text{jets}}$ . This dependency affect the SR which require events  
 1451        with  $\geq 6$  jets, and is corrected by applying a correction factor  $SF_{i,n} = \epsilon_{i,n}/\epsilon_{i,N}$  where  $N$  is  
 1452        the inclusive bin containing all  $N_{\text{jets}}$  and  $\epsilon_{i,n}$  is the QmisID rate obtained from Equation 6.2  
 1453        in the  $(i, n)^{\text{th}}$  2D bin in  $(p_{\text{T}}, N_{\text{jets}})$ . Jet multiplicity and consequently the obtained SFs are  
 1454        assumed to be independent of  $|\eta|$ .

### 1455        6.3.3 $t\bar{t}W$ background data-driven estimation

1456        Previously, the  $t\bar{t}W$  background in  $t\bar{t}t\bar{t}$  final state analyses was handled by assigning large  
 1457        ad-hoc systematic uncertainties to  $t\bar{t}W$  events with 7 or more jets [49]. A semi-data-driven  
 1458        method [154] was shown to be effective in the SM  $t\bar{t}t\bar{t}$  observation analysis [47] by improving  
 1459         $t\bar{t}W$  modeling, especially in the showering step and switching  $t\bar{t}W$  systematic uncertainties  
 1460        from predominantly modeling to statistical.

1461        The data-driven method applies correction factors obtained from a fitted function pa-  
 1462        rameterized in  $N_{\text{jets}}$  to  $t\bar{t}W$  MC kinematic distibutions. The QCD scaling patterns [155] can  
 1463        be represented by ratio of successive exclusive jet cross-sections

$$R_{(n+1)/n} = \frac{\sigma_{n+1}}{\sigma_n} = e^{-b} + \frac{\bar{n}}{n+1} = a_0 + \frac{a_1}{1+(j-4)}, \quad (6.4)$$

1464        where  $a_{0(1)}$  and  $b$  are constants,  $n$  is the number of jets in addition to the hard process,  $j$   
 1465        is the inclusive number of jets, and  $\bar{n}$  is the expectation value for the Poisson distribution  
 1466        of exclusive jet cross-section at jet multiplicity  $n$ . The  $t\bar{t}W$  ME for SS2L events gives 4 jets  
 1467        in the hard process, so  $n$  is defined starting from the 5<sup>th</sup> jets and the inclusive number of  
 1468        jets  $j = n + 4$ . The two terms in Equation 6.4 correspond to staircase and Poisson scaling

1469 in cross section between successive jet multiplicities and are sensitive to high and low jet  
1470 multiplicity events respectively [155]. The scaling pattern can then be reparameterized in  
1471  $a_0$  and  $a_1$  to obtain the  $t\bar{t}W$  yield at  $j' \equiv j + 1$  jets

$$\text{Yield}_{t\bar{t}W(j')} = \text{Yield}_{t\bar{t}W(N_{\text{jets}}=4)} \times \prod_{j=4}^{j'-1} \left( a_0 + \frac{a_1}{1+(j-4)} \right) \quad (6.5)$$

1472 with  $j \geq 4$ . The  $t\bar{t}W$  yield in the 4-jet bin can be represented by a NF applied to  $t\bar{t}W$  MC  
1473 simulation

$$\text{Yield}_{t\bar{t}W(N_{\text{jets}}=4)} = \text{NF}_{t\bar{t}W(N_{\text{jets}}=4)} \times \text{MC}_{t\bar{t}W(N_{\text{jets}}=4)}. \quad (6.6)$$

1474 To account for the asymmetry in  $t\bar{t}W^+$  and  $t\bar{t}W^-$  cross-sections,  $\text{NF}_{t\bar{t}W(N_{\text{jets}}=4)}$  is further  
1475 split into  $\text{NF}_{t\bar{t}W^\pm(N_{\text{jets}}=4)}$  assuming the scaling is the same for both processes. Both NFs  
1476 are left free-floating to constrain  $t\bar{t}W$  yields in the 4-jet bin within CR 1b(+) and CR 1b(-).  
1477 The final  $N_{\text{jets}}$ -parameterized function can then be represented by  $\text{NF}_{t\bar{t}W(j')}$  as

$$\text{NF}_{t\bar{t}W(j')} = \left( \text{NF}_{t\bar{t}W^+(N_{\text{jets}}=4)} + \text{NF}_{t\bar{t}W^-(N_{\text{jets}}=4)} \right) \times \prod_{j=4}^{j'-1} \left( a_0 + \frac{a_1}{1+(j-4)} \right). \quad (6.7)$$

1478 The normalization is calculated and applied separately for each sub-sample of  $t\bar{t}W^+$  and  
1479  $t\bar{t}W^-$  in a  $N_{\text{jets}}$  bin for  $4 \leq N_{\text{jets}} < 10$ . Due to small contributions in the CRs, events  
1480 with  $N_{\text{jets}} < 4$  and  $N_{\text{jets}} \geq 10$  are not normalized with this scheme. Instead,  $N_{\text{jets}} < 4$   
1481 events are fitted by propagating the normalization in the 4-jet bin without additional shape  
1482 correction. The correction factor for  $t\bar{t}W$  events with  $N_{\text{jets}} \geq 10$  is obtained by summing  
1483 up the overflow from  $N_{\text{jets}} = 10$  to  $N_{\text{jets}} = 12$ , described as  $\sum_{j'=10}^{12} \prod_{j=4}^{j'-1} \left( a_0 + \frac{a_1}{1+(j-4)} \right)$ .  
1484 Events with  $N_{\text{jets}} \geq 13$  are negligible and are not included in the sum.

1485      The four regions, CR  $t\bar{t}W^\pm$  and CR 1b( $\pm$ ), are constructed to fit  $NF_{t\bar{t}W^\pm(N_{\text{jets}}=4)}$  and  
1486 the scaling parameters  $a_{0(1)}$ , as well as validating the parameterization. Assuming the  $N_{\text{jets}}$   
1487 distribution of  $t\bar{t}W$  is similar across bins of  $N_b$ -jets, a fitted  $N_{\text{jets}}$  distribution in CR 1b( $\pm$ )  
1488 can be used to describe the  $t\bar{t}W$  parameterization at higher  $N_{\text{jets}}$ .

# 1489 Chapter 7. Systematic Uncertainties

1490 Physics analysis inherently incurs uncertainties in the form of statistical and systematic  
1491 uncertainties, depending on the source. Statistical uncertainties occur in this analysis from  
1492 sample size of collected data and simulated MC samples, and from the maximizing of the  
1493 LH function. Systematic uncertainties depend on identifiable sources in the analysis i.e.  
1494 from detector and reconstruction effects (experimental uncertainties) or theoretical modeling  
1495 (theoretical uncertainties). Systematic uncertainties are represented as nuisance parameters  
1496 ( $NP_x$ ) in the profile LH fit. During the fit, systematic uncertainties with negligible impact  
1497 on the final results can be pruned to simplify the statistical model and reduce computational  
1498 complexity. This section outlines all uncertainties considered in this analysis.

## 1499 7.1 Experimental uncertainties

### 1500 7.1.1 Luminosity & pile-up reweighting

1501 The uncertainty on the integrated luminosity of the 2015-2018 Run 2 data set is 0.83%  
1502 [89], obtained by the LUCID-2 detector [156] for the primary luminosity measurements and  
1503 complemented by the ID and calorimeters. Pile-up was modeled in MC and calibrated  
1504 to data through pile-up reweighting, resulting in a set of calibration SFs and associated  
1505 uncertainties.

### 1506 7.1.2 Leptons

1507 In general, calibrating MC simulations to match performance in data incurs uncertainties  
1508 associated obtaining the MC-to-data calibration SFs, which are in turn propagated to observ-

ables in the analysis. The data-to-MC calibration of trigger, reconstruction, identification and isolation efficiencies for electrons and muons incur associated uncertainties, with separate systematic and statistical components for those related to muons. Similarly, electron energy scale, muon momentum scale and resolution are also subjected to calibration uncertainties estimated by re-simulating the events while varying the energy/momenta scale and resolution. Electron has an additional uncertainty related to ECIDS efficiency. Muon has additional uncertainties for charge-independent and charge-dependent momentum scale, as well as detector-specific track resolution. Systematic uncertainties for electron reconstruction, identification, isolation, ECIDS efficiencies and muon ID/MS energy resolution were not ready for the sample version used in this analysis, and are therefore not included.

### 7.1.3 Jets

Experimental uncertainties for jets are dominated by flavor tagging-related uncertainties, with subleading contributions from uncertainties related to JES [112], JER [111] and JVT [157] calibrations.

#### Jet energy scale

Uncertainties associated with JES are determined using data from LHC collisions along with MC simulated samples [112], decomposed into uncorrelated components:

- **Effective NPs:** 15 total  $p_T$ -dependent uncertainty components measured in situ, grouped based on their origin (2 detector-related, 4 modeling-related, 3 mixed, 6 statistical-related)
- **$\eta$  intercalibration:** 6 total components (1 modeling-related, 4 non-closure and 1

1530 statistical-related) associated with the correction of the forward jets' ( $0.8 \leq |\eta| < 4.5$ )  
1531 energy scale to that of the central jets ( $|\eta| < 0.8$ ).

1532 • **Flavor composition & response:** 2 components for relative quark-gluon flavor com-  
1533 positions in background and signal samples, and 2 components for responses to gluon-  
1534 initiated versus quark-initiated jets.

1535 • **Pile-up subtraction:** 4 components, 2 for  $\mu$  (`OffsetMu`) and  $N_{\text{PV}}$  (`OffsetNPV`) mod-  
1536 eling, 1 for residual  $p_{\text{T}}$ -dependency (`PtTerm`) and 1 for topology dependence on the  
1537 per-event  $p_{\text{T}}$  density modeling (`RhoTopology`).

1538 • **Punch-through effect treatment:** 2 terms for GSC punch-through jet response  
1539 deviation between data and MC, one for each detector response simulation method  
1540 (AF3 and FS).

1541 • **Non-closure:** 1 term applied to AF3 sample to account for the difference between  
1542 AF3 and FS simulation.

1543 • **High- $p_{\text{T}}$  single-particle response:** 1 term for the response to high- $p_{\text{T}}$  jets from  
1544 single-particle and test-beam measurements.

1545 •  **$b$ -jets response:** 1 term for the difference between  $b$ -jets and light-jets response.

## 1546 Jet energy resolution

1547 Measurements of JER were performed in bins of  $p_{\text{T}}$  and  $\eta$ , separately in data using in-  
1548 situ techniques and in MC simulation using dijet events [111]. This analysis uses the full  
1549 correlation JER uncertainty scheme provided for Run 2 analysis with 14 total components:

<sub>1550</sub> 12 for effective NPs and 2 for difference between data and MC, separately for AF3 and FS  
<sub>1551</sub> [111].

## <sub>1552</sub> Jet vertex tagging

<sub>1553</sub> The uncertainty associated with JVT is obtained by varying the JVT efficiency SFs  
<sub>1554</sub> within their uncertainty range [157]. This uncertainty accounts for remaining contamination  
<sub>1555</sub> from pile-up jets after applying pile-up suppression and MC generator choice.

## <sub>1556</sub> Flavor tagging

<sub>1557</sub> Calibration SFs for  $b$ -tagging efficiencies and  $c$ -/light-jets mistagging rates are derived as  
<sub>1558</sub> a function of  $p_T$  for  $b$ -,  $c$ -, light-jets and PCBT score. The full set of flavor tagging-related  
<sub>1559</sub> uncertainties was reduced in dimensions by diagonalizing the uncertainty covariance matrix  
<sub>1560</sub> via eigendecomposition [115], resulting in a compact set of orthogonal NPs for this analysis:  
<sub>1561</sub> 85 for  $b$ -jets, 56 for  $c$ -jets and 42 for light-jets.

### <sub>1562</sub> 7.1.4 Missing transverse energy

<sub>1563</sub> Uncertainties on  $E_T^{\text{miss}}$  arise from possible mis-calibration of the soft-track component  
<sub>1564</sub> and are estimated using data-to-MC comparison of the  $p_T$  scale and resolution between  
<sub>1565</sub> the hard and soft  $E_T^{\text{miss}}$  components [119]. These uncertainties are represented by three  
<sub>1566</sub> independent terms: 1 for scale uncertainty and 2 for resolution uncertainty of the parallel  
<sub>1567</sub> and perpendicular components.

<sub>1568</sub> **7.2 Modeling uncertainties**

<sub>1569</sub> **7.2.1 Signal and irreducible background uncertainties**

<sub>1570</sub> The signal and background samples used are modeled using MC simulation. Most uncer-  
<sub>1571</sub> tainties on simulation parameters (e.g. generator choice, PS model) are estimated by varying  
<sub>1572</sub> the relevant parameters and comparing them with the nominal sample. Uncertainties in-  
<sub>1573</sub> volving PDF in particular for most processes in the analysis are set to a flat 1% uncertainty.  
<sub>1574</sub> Cross-section uncertainties were considered for all irreducible background except  $t\bar{t}W$ , which  
<sub>1575</sub> is normalized in dedicated CRs following section 6.3.3. Extra uncertainties for the produc-  
<sub>1576</sub> tion of four or more  $b$ -jets (additional  $b$ -jets) in association with  $t\bar{t}X$  and HF jets were also  
<sub>1577</sub> considered due to a lack of theoretical predictions or dedicated measurements, rendering  
<sub>1578</sub> MC modeling challenging. Uncertainties from missing higher-order QCD corrections in MC  
<sub>1579</sub> simulation are estimated by varying the renormalization scale  $\mu_R$  and factorization scale  $\mu_F$   
<sub>1580</sub> within seven different combinations

$$(\mu_R, \mu_F) = \{(0.5, 0.5), (0.5, 1), (1, 0.5), (1, 1), (1, 2), (2, 1), (2, 2)\}.$$

<sub>1581</sub> Process-specific uncertainty treatments are detailed below.

<sub>1582</sub> **SM  $t\bar{t}t\bar{t}$  background**

<sub>1583</sub> The generator uncertainty for the SM  $t\bar{t}t\bar{t}$  background was evaluated between a nominal  
<sub>1584</sub> sample of MADGRAPH5\_AMC@NLO and SHERPA. The parton shower uncertainty was  
<sub>1585</sub> evaluated between PYTHIA8 and HERWIG. The cross-section uncertainty was estimated to

1586 be 20% computed from a prediction at NLO in QCD+EW [128].

### 1587 $t\bar{t}t$ background

1588 The cross-section uncertainty for  $t\bar{t}t$  was estimated to be 30% computed from a prediction  
1589 at NLO in QCD+EW [128]. Events with additional  $b$ -jets also incur a 50% uncertainty.

### 1590 $t\bar{t}W$ , $t\bar{t}Z$ , $t\bar{t}H$ backgrounds

1591 For  $t\bar{t}W$ ,  $t\bar{t}Z$  and  $t\bar{t}H$  backgrounds, an uncertainty of 50% is assigned to events with one  
1592 additional truth  $b$ -jets that did not originate from a top quark decay, and an added 50%  
1593 uncertainty is assigned to events with two or more [158] additional  $b$ -jets. The generator  
1594 uncertainty was estimated for  $t\bar{t}Z$  using a MADGRAPH5\_AMC@NLO nominal sample and  
1595 a SHERPA sample, and for  $t\bar{t}H$  using POWHEGBOX samples interfaced with PYTHIA8 (nom-  
1596 inal) and HERWIG7. Cross-section uncertainties of 12% and 10% were applied to  $t\bar{t}Z$  and  
1597  $t\bar{t}H$  respectively [159]. No  $t\bar{t}W$  cross-section or PDF uncertainty was considered since the  
1598 normalizations and jet multiplicity spectrum for  $t\bar{t}W$  are estimated using the data-driven  
1599 method described in section 6.3.3.

### 1600 Other backgrounds

1601 Other backgrounds include processes with small overall contribution in the SR. The  
1602 cross-section uncertainty for  $tZ$  and  $tWH$  is considered to be 30% [160, 161]. A conservative  
1603 cross-section uncertainty of 50% is applied to  $t\bar{t}VV$ ,  $VVV$  and  $VH$ . For  $VV$ , the cross-  
1604 section uncertainty is dependent on jet multiplicity and is considered to be 20%/50%/60%  
1605 for events with  $\leq 3/4 \geq 5$  jets [162]. For  $VV$ ,  $t\bar{t}VV$ ,  $VVV$  and  $VH$  events with additional  
1606 truth  $b$ -jets, an uncertainty of 50% is applied.

## 1607 7.2.2 Reducible background uncertainties

1608 Reducible backgrounds consist of  $t\bar{t}/V + \text{HF}$  jets and single top events. Reducible back-  
1609 ground has small contamination within the SR, thus uncertainties related to reducible back-  
1610 ground have minor impact. Treatment for reducible background in this analysis largely  
1611 follows Ref. [47], except for QmisID.

## 1612 Charge misidentification

1613 Uncertainties on the QmisID background originate from the charge flip rates obtained  
1614 using the data-driven method described in section 6.3.2. Four sources of uncertainty were  
1615 considered: statistical uncertainty from the maximum LLH estimation using Equation 6.2;  
1616 uncertainty from choice of the  $Z$ -mass window and sidebands; non-closure uncertainty de-  
1617 fined as the relative difference between the number of SS and OS events; and statistical  
1618 uncertainty from the  $N_{\text{jets}}$  dependency correction SFs. The combined uncertainties from  
1619 all four sources are calculated separately for each region involved in section 6.3.2, and are  
1620 treated as correlated across all regions. Figure 7.1 shows the uncertainty calculated for SR.

## 1621 Internal (low $\gamma^*$ ) and material conversion

1622 The normalization for internal and material conversion backgrounds are free parameters  
1623 in the fit, as a result the only uncertainties evaluated are from the shape of the distributions  
1624 used in the template fit method (see section 6.3.1). The uncertainties on internal (material)  
1625 conversion are estimated based on the difference between data and MC prediction in a region  
1626 enriched in  $Z + \gamma \rightarrow \mu^+\mu^- + e^+e^-$  events.

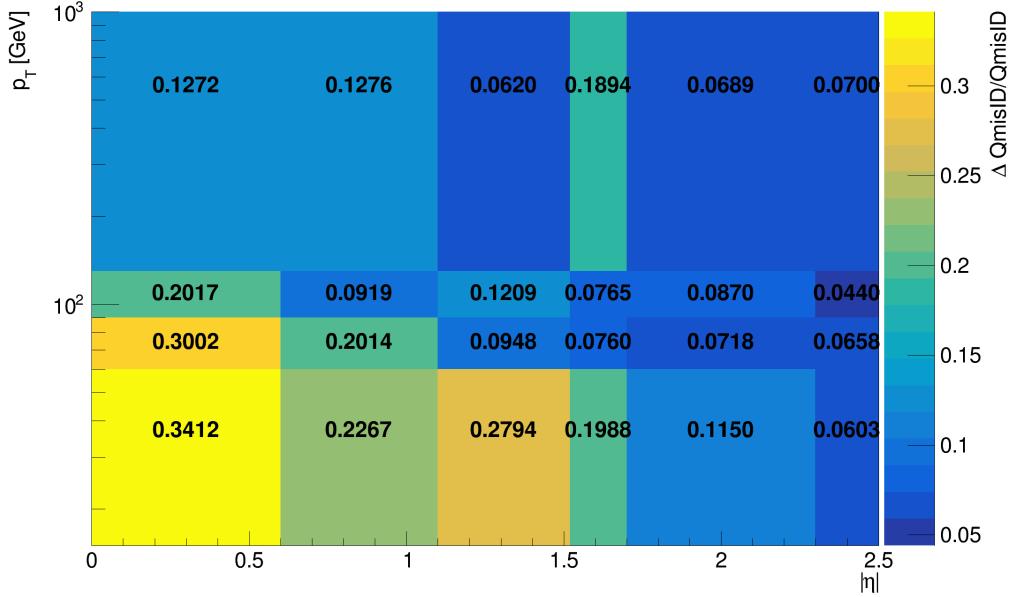


Figure 7.1: Combined QmisID uncertainty rate for SR in bins of  $|\eta|$  and  $p_T$ .

### <sup>1627</sup> Heavy-flavor non-prompt lepton

<sup>1628</sup> Similar to the conversion backgrounds, the uncertainties on non-prompt HF decays come  
<sup>1629</sup> from the shape of the distributions, and are estimated by comparing data and MC prediction  
<sup>1630</sup> between all regions in the analysis on a per bin basis. The events used are required to  
<sup>1631</sup> contain at least one *Loose* reconstructed lepton used in the region selection criteria detailed  
<sup>1632</sup> in Table 6.1 to maintain orthogonality with the SR.

### <sup>1633</sup> Light-flavor decays and other fake/non-prompt backgrounds

<sup>1634</sup> A conservative normalization uncertainty of 100% is assigned for light-flavor non-prompt  
<sup>1635</sup> lepton background [151], and an ad-hoc normalization uncertainty of 30% is applied to all  
<sup>1636</sup> other fake and non-prompt backgrounds. The shape uncertainties for these backgrounds are  
<sup>1637</sup> negligible.

1638 **Chapter 8. Results**

1639 **8.1 Statistical interpretation**

1640 This section provides an overview of the statistical methods needed to interpret the  
1641 collected and simulated data to estimate unknown physics parameters and determine com-  
1642 patibility between data and the analysis hypothesis. For the BSM resonance search, the null  
1643 hypothesis  $H_0$  assumes only SM background contributions and none from any new BSM  
1644 resonance in the data.

1645 **8.1.1 Profile likelihood fit**

1646 Given a set of observed data points  $\mathbf{x} = [x_1, x_2, \dots]$  and unknown parameters  $\boldsymbol{\theta} =$   
1647  $[\theta_1, \theta_2, \dots, \theta_n]$ , the maximum likelihood method aims to find an estimate  $\hat{\boldsymbol{\theta}}$  that maximizes  
1648 the joint probability function  $f(\mathbf{x}, \boldsymbol{\theta})$ , or in other words the set of parameters that gives the  
1649 highest probability of observing the collected data points for a particular model. The func-  
1650 tion to be maximized for this purpose is the log-likelihood (LLH) function  $\ln \mathcal{L}(\mathbf{x}, \boldsymbol{\theta})$  where  
1651  $\mathcal{L}(\mathbf{x}, \boldsymbol{\theta}) \equiv \prod_i f(x_i, \boldsymbol{\theta})$  is defined as the likelihood (LH) function. The LLH is maximized  
1652 when  $\partial/\partial\theta_i (\ln \mathcal{L}) = 0$  for each parameter  $\theta_i$ .

1653 For an usual binned physics analysis, the above variables for the LH function  $\mathcal{L}$  can  
1654 be expressed as nuisance parameters (NP)  $\boldsymbol{\theta}$  and number of events for a model  $N_i(\mu)$  for  
1655 the  $i^{\text{th}}$  bin, where  $\mu$  is the targeted parameter of interest (POI). In this analysis,  $N_i$  is  
1656 assumed to follow a Poisson distribution and depends on the following quantities: the signal  
1657 strength  $\mu$  defined as the ratio of observed to expected cross sections  $\sigma_{\text{obs}}/\sigma_{\text{exp}}$ ; nuisance  
1658 parameters  $\boldsymbol{\theta}$  which represents the effects of systematic uncertainties, implemented in the

1659 LH function as Gaussian constraints; and normalization factors (NFs)  $\boldsymbol{\lambda}$  that control the  
 1660 normalization of background components that do not have a well-known cross section. The  
 1661 Poisson probability of observing exactly  $N_i$  events for an expected number of event  $n_i$  is

$$\mathcal{P}(N_i|n_i(\mu, \boldsymbol{\lambda})) = \frac{n_i^{N_i} e^{-n_i}}{N_i!}. \quad (8.1)$$

1662 The expected Poisson event number in a bin  $i$  can be parameterized as

$$n_i = \mu s_i(\boldsymbol{\theta}) + \sum_j \lambda_j b_{ij}(\boldsymbol{\theta}), \quad (8.2)$$

1663 where  $s_i$  is the number of signal events in bin  $i$  of every region, and  $b_{ij}$  is the number of  
 1664 events for a certain background source index  $j$  in bin  $i$ . The LH function in this analysis  
 1665 can be written as

$$\mathcal{L}(\mathbf{N}|\mu, \boldsymbol{\theta}, \boldsymbol{\lambda}) = \left( \prod_i \mathcal{P}(N_i|n_i) \right) \cdot \prod_k \mathcal{G}(\theta_k), \quad (8.3)$$

1666 where  $\mathcal{G}(\theta_k)$  is the Gaussian constraint for a NP  $k$ . The signal significance  $\mu$  and NFs  $\boldsymbol{\lambda}$  are  
 1667 left unconstrained and are fitted simultaneously in the profile LH fit. Define the profile LH  
 1668 ratio [163] as

$$\lambda(\mu) = \frac{\mathcal{L}(\mu, \hat{\boldsymbol{\theta}}_\mu, \hat{\boldsymbol{\lambda}}_\mu)}{\mathcal{L}(\hat{\mu}, \hat{\boldsymbol{\theta}}, \hat{\boldsymbol{\lambda}})}, \quad (8.4)$$

1669 where  $\hat{\mu}$ ,  $\hat{\boldsymbol{\theta}}$  and  $\hat{\boldsymbol{\lambda}}$  are parameter values that optimally maximizes the LH function, and  $\hat{\boldsymbol{\theta}}_\mu$ ,  
 1670  $\hat{\boldsymbol{\lambda}}_\mu$  are NP and NF values respectively that maximize the LH function for a given signal  
 1671 strength  $\mu$ . Using Neyman-Pearson lemma [164], the optimal test statistic for hypothesis  
 1672 testing is

$$q_\mu \equiv -2 \ln \lambda(\mu), \quad (8.5)$$

1673 where  $q_\mu = 0$  or  $\lambda(\mu) = 1$  corresponds to perfect agreement between the optimal parameter  
 1674  $\hat{\mu}$  obtained from data and the hypothesized value  $\mu$ . From Wilks' theorem [165], the test  
 1675 statistic  $q_\mu$  approaches a  $\chi^2$  distribution and can be evaluated as  $q_\mu = (\mu - \hat{\mu})^2 / \sigma_\mu^2$ .

1676 When evaluating against the background-only hypothesis ( $\mu = 0$ ), it can be assumed  
 1677 that the number of events observed under the signal hypothesis is higher than that of the  
 1678 background-only hypothesis, or  $\mu \geq 0$  according to Equation 8.2. This leads to a corre-  
 1679 sponding lower bound on the test statistic

$$q_0 = \begin{cases} -2 \ln \lambda(0), & \text{if } \hat{\mu} \geq 0, \\ 0, & \text{if } \hat{\mu} < 0. \end{cases} \quad (8.6)$$

### 1680 ***p*-value**

1681 To quantify the incompatibility between the observed data and the background-only hy-  
 1682 pothesis, the *p*-value is defined as  $p = P(q_\mu \geq q_{\mu, \text{obs}} | H_0)$  or in other words, the probability  
 1683 of observing data with a test statistic  $q_\mu$  under the null hypothesis  $H_0$  that is less compat-  
 1684 ible with  $H_0$  than the actual observed data with test statistic  $q_{\mu, \text{obs}}$ . The *p*-value can be  
 1685 expressed in terms of  $q_\mu$  as

$$p_\mu = \int_{q_{\mu, \text{obs}}}^{\infty} f(q_\mu | \mu) dq_\mu, \quad (8.7)$$

1686 where  $f(q_\mu | \mu) dq_\mu$  is the conditional probability density function of  $q_\mu$  given  $\mu$ .

1687 In some cases, it is more convenient to evaluate compatibility using the *Z*-value, defined  
 1688 as the number of standard deviations between the observed data and the mean in a Gaussian

1689 distribution. The  $p$ -value can be converted to  $Z$ -value via the relation

$$Z = \Phi^{-1}(1 - p), \quad (8.8)$$

1690 where  $\Phi$  is the quantile of the standard Gaussian. Rejecting the signal hypothesis usually  
1691 requires a 95% confidence level (CL) which corresponds to a  $p$ -value of 0.05 or a  $Z$ -value of  
1692 1.64, while rejecting the background-only hypothesis generally requires a  $Z$ -value of 5 or a  
1693  $p$ -value of  $2.84 \times 10^{-7}$ .

### 1694 8.1.2 Exclusion limit

1695 If the signal hypothesis is rejected, the exclusion upper limits can still be computed at  
1696 a certain CL (usually 95%) to establish the maximum value of  $\mu$  that is not excluded by  
1697 or in conflict with the observed data. The exclusion limits are calculated based on the CLs  
1698 method [166, 167] under which the test statistic is defined as  $q_\mu = -2 \ln \frac{\mathcal{L}_{s+b}}{\mathcal{L}_b}$  with  $\mathcal{L}_{s+b}$   
1699 being the LH function for the signal and background hypothesis ( $\mu > 0$ ) and  $\mathcal{L}_b$  being the  
1700 LH function for the background-only hypothesis ( $\mu = 0$ ). The  $p$ -value for both hypotheses  
1701 can then be expressed as

$$\begin{aligned} p_{s+b} &= P(q \geq q_{\text{obs}} | s + b) = \int_{q_{\text{obs}}}^{\infty} f(q | s + b) dq \\ p_b &= P(q \geq q_{\text{obs}} | b) = \int_{-\infty}^{q_{\text{obs}}} f(q | b) dq. \end{aligned} \quad (8.9)$$

1702 The signal hypothesis is excluded for a CL  $\alpha$  when the following condition is satisfied

$$\text{CL}_s \equiv \frac{p_{s+b}}{p_b} \geq 1 - \alpha. \quad (8.10)$$

1703 The value of  $\mu$  such that the signal hypothesis leads to  $CL_s = 1 - \alpha = 0.05$  is then the  
1704 exclusion upper limit at a 95% CL. Exclusion limits are usually reported in terms of expected  
1705 and observed limits. The expected limits show the exclusion limits obtained under the  
1706 background-only hypothesis and represent the analysis' sensitivity, while the observed limits  
1707 represent exclusion limits derived from observed data.

## 1708 8.2 Fit results

1709 The signal strength  $\mu$ , background NFs,  $t\bar{t}W$  scaling factors and uncertainty NPs are  
1710 simultaneously fitted using a binned profile LLH fit under the background-only hypothesis  
1711 to the  $H_T$  distribution in the SR and to corresponding distributions shown in Table 6.1 for  
1712 CRs.

1713 Before fitting to real data (unblinded fit), the fit was first performed in both the SR  
1714 and CRs using Asimov pseudo-datasets, in which the simulated data match exactly to MC  
1715 prediction with nominal  $\mu$  set to 0. This is done for the purpose of optimizing object selection  
1716 criteria and region definition, refining background estimation techniques and testing the  
1717 statistical interpretation model for signal extraction described in section 8.1. The fit is then  
1718 performed with Asimov data in the SR and real data in CRs to validate background modeling,  
1719 estimate sensitivity and assess the influence of statistical effects on fitted parameters. Finally,  
1720 the fully unblinded fit is performed with real data in all regions.

1721 The unblinded fit results are presented below. No significant variation is observed in fit  
1722 output behavior using  $t\bar{t}Z'$  samples of different  $m_{Z'}$ ; results fitted using  $m_{Z'} = 2$  TeV are  
1723 shown without substantial loss of generality. The background modeling is evaluated under  
1724 the background-only hypothesis. The fitted background NFs are shown in Table 8.1 and

1725 are consistent with their nominal values within one standard deviation, or two standard  
1726 deviations in the case of  $\text{NF}_{\text{HF } e}$  and  $\text{NF}_{t\bar{t}W+(4j)}$ . Figure 8.1 shows good agreement between  
1727 data and post-fit background distributions in non-prompt background CRs and  $t\bar{t}W$  CRs.

1728 The pre-fit and post-fit background yields are shown in Table 8.2. Except for HF  $e$   
1729 background, post-fit yields for various backgrounds e.g.  $t\bar{t}t\bar{t}$ ,  $t\bar{t}H$ , other fake, etc. are  
1730 increased; the pre-fit to post-fit variations are consistent within  $\pm\sigma$ . Data and total post-fit  
1731 yields are also consistent within  $\pm\sigma$ . Post-fit yield for HF  $e$  background is lowered compared  
1732 to pre-fit yield within within  $2\sigma$  which can be related to the fitted value of  $\text{NF}_{\text{HF } e}$  in  
1733 Table 8.1; however, this difference in pre- and post-fit yields of HF  $e$  background has negligible  
1734 impact on the  $\mu$  as seen in Table 8.3.

1735 Table 8.3 outlines the impact on the signal strength  $\mu$  of various sources of uncertainty  
1736 grouped by their corresponding category. The background sources of uncertainty with the  
1737 largest impact is  $t\bar{t}t\bar{t}$  modeling, in particular  $t\bar{t}t\bar{t}$  generator choice and cross-section uncer-  
1738 tainties, followed by  $t\bar{t}W$  modeling due to their significant contributions in the SR observed  
1739 in Figure 6.1, especially in the more sensitive regions requiring three or more  $b$ -tagged jets.  
1740 The most significant impact on  $\mu$  within the set of instrumental uncertainties are uncertain-  
1741 ties on jet  $b$ -tagging attributable to the high jet and  $b$ -jet multiplicities in the BSM  $t\bar{t}t\bar{t}$  signal  
1742 signature.

1743 No significant excess over SM predictions is observed, and the fitted signal strength  $\mu$  is  
1744 compatible with zero for all  $Z'$  mass points. Figure 8.2 shows the observed and expected  
1745 upper limits at 95% confidence level on the cross-section of  $pp \rightarrow t\bar{t}Z'$  production times  
1746 the branching ratio of  $Z' \rightarrow t\bar{t}$  as a function of the  $Z'$  resonance mass. The  $\pm 1\sigma$  and  $\pm 2\sigma$   
1747 confidence intervals around the expected exclusion limits are also shown. The observed  
1748 exclusion limits range from 7.9 fb to 9.44 fb depending on  $m_{Z'}$ . The distribution of limits

<sub>1749</sub> across  $m_{Z'}$  is flat and show little correlation to signal kinematics and phase space modeling.

<sub>1750</sub> The observed limits exclude  $Z'$  masses below  $\approx 15$  TeV.

Table 8.1: Normalization factors for backgrounds with dedicated CRs, obtained from a simultaneous fit in all CRs and SR under the background-only hypothesis. The nominal pre-fit value is 1 for all NFs and 0 for the scaling factors  $a_0$  and  $a_1$ . Uncertainties shown include both statistical and systematic uncertainties.

Parameter	NF <sub>HF e</sub>	NF <sub>HF <math>\mu</math></sub>	NF <sub>Mat. Conv.</sub>	NF <sub>Low <math>m_{\gamma^*}</math></sub>	$a_0$	$a_1$	NF <sub><math>t\bar{t}W+(4j)</math></sub>	NF <sub><math>t\bar{t}W-(4j)</math></sub>
Fit value	$0.68^{+0.23}_{-0.22}$	$0.97^{+0.17}_{-0.16}$	$0.97^{+0.31}_{-0.28}$	$0.97^{+0.23}_{-0.20}$	$0.39^{+0.11}_{-0.11}$	$0.42^{+0.25}_{-0.24}$	$1.21^{+0.18}_{-0.18}$	$1.10^{+0.26}_{-0.26}$

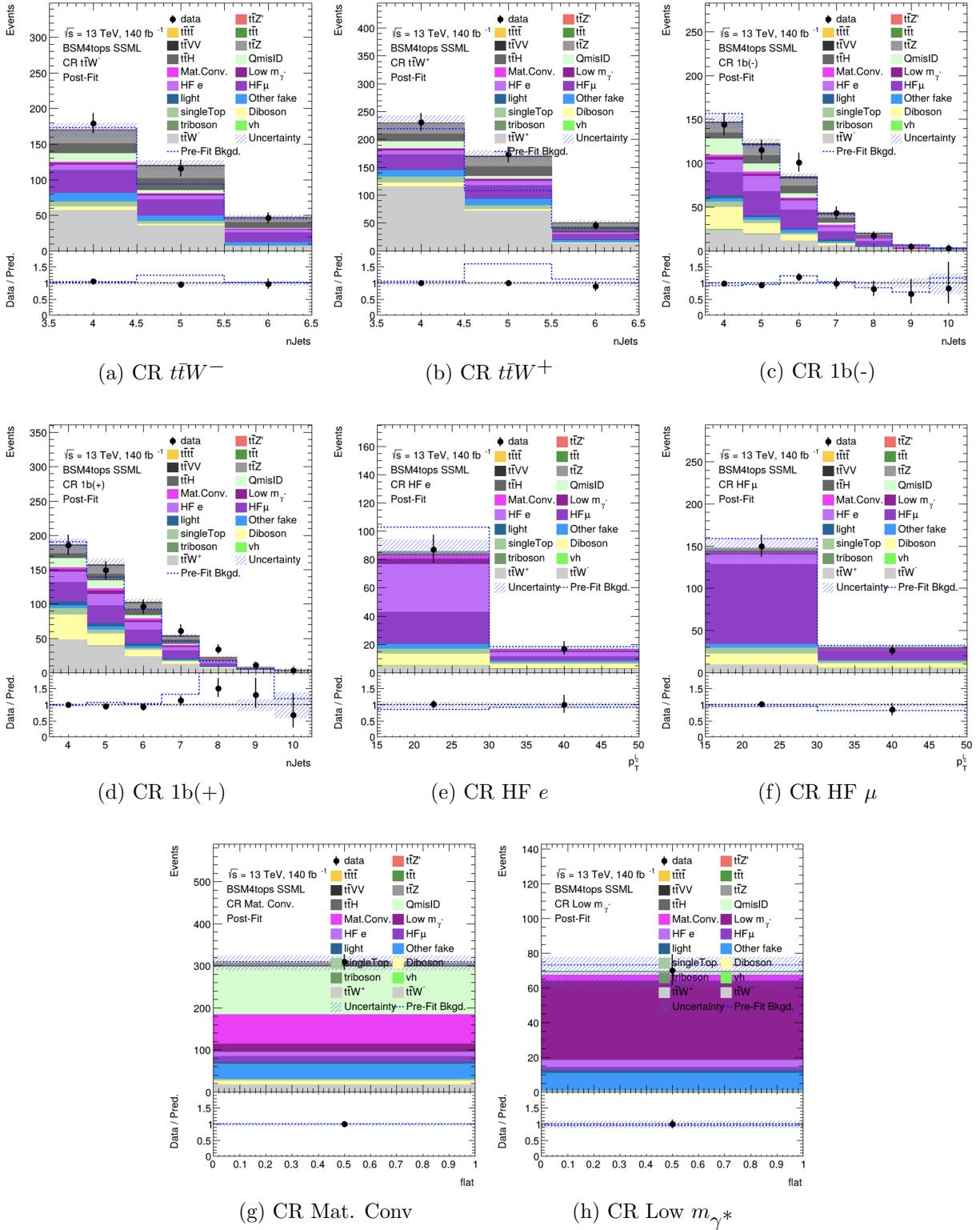


Figure 8.1: Comparison between data and post-fit prediction for the discriminant observable in each CR. Distributions shown are obtained from the fit using the  $t\bar{t}Z'$  signal sample with  $m_{Z'} = 2$  TeV. The lower panel shows the ratio between data and post-fit predictions. The shaded band represents the total uncertainty on the fit. The dashed line represents the pre-fit distribution.

Table 8.2: Pre-fit and post-fit background yields in the inclusive SR. The number of data events and pre-fit estimate signal yields are also shown. Background yields shown are obtained using the  $t\bar{t}Z'$  signal sample with  $m_{Z'} = 2$  TeV. Pre-fit yields for  $t\bar{t}W$  background are set to 0 nominally prior to data-driven normalization. Total yield uncertainty differs from the quadrature sum of constituent uncertainties due to (anti-)correlation effects.

Process	Pre-fit	Post-fit
<b>Background</b>		
$t\bar{t}t\bar{t}$	$42.35 \pm 5.45$	$46.91 \pm 5.19$
$t\bar{t}W^+$	-	$103.93 \pm 15.91$
$t\bar{t}W^-$	-	$55.27 \pm 11.14$
$t\bar{t}Z$	$78.02 \pm 14.12$	$75.57 \pm 11.13$
$t\bar{t}H$	$81.00 \pm 7.10$	$82.90 \pm 7.30$
$t\bar{t}t$	$3.33 \pm 0.59$	$3.37 \pm 0.60$
Single-top ( $tq$ , $tZq$ , $tWZ$ , etc.)	$13.38 \pm 2.87$	$12.69 \pm 2.86$
$t\bar{t}VV/t\bar{t}VH/t\bar{t}HH$	$17.07 \pm 4.66$	$16.44 \pm 4.64$
Charge misidentification	$40.31 \pm 0.32$	$40.33 \pm 0.32$
$VV/VVV/VH$	$10.01 \pm 4.76$	$6.69 \pm 2.75$
Mat. Conv.	$26.20 \pm 0.91$	$25.76 \pm 6.06$
Low $m_{\gamma^*}$	$26.14 \pm 0.66$	$25.62 \pm 4.23$
HF $e$	$21.99 \pm 1.45$	$15.42 \pm 3.70$
HF $\mu$	$31.33 \pm 3.47$	$31.53 \pm 5.06$
Light-flavor decays	$13.47 \pm 0.53$	$13.54 \pm 0.53$
Other fake & non-prompt	$24.90 \pm 2.26$	$26.00 \pm 1.96$
Total background	-	$576.53 \pm 19.86$
<b>Signal <math>t\bar{t}Z' \rightarrow t\bar{t}t\bar{t}</math></b>		
$m_{Z'} = 1$ TeV	$52.83 \pm 1.41$	-
$m_{Z'} = 1.25$ TeV	$52.94 \pm 1.35$	-
$m_{Z'} = 1.5$ TeV	$53.07 \pm 1.47$	-
$m_{Z'} = 2$ TeV	$52.49 \pm 1.43$	-
$m_{Z'} = 2.5$ TeV	$53.07 \pm 1.47$	-
$m_{Z'} = 3$ TeV	$52.45 \pm 1.50$	-
<b>Data</b>		604

Table 8.3: Post-fit impact of uncertainty sources on the signal strength  $\mu$ , grouped by categories. Values shown are obtained from the fit using the  $t\bar{t}Z'$  signal sample with  $m_{Z'} = 2$  TeV. Impact on  $\mu$  is evaluated for each uncertainty category by re-fitting with the corresponding set of NPs fixed to their best-fit values. Total uncertainty differs from the quadrature sum of constituent uncertainties due to correlation between NPs in the fit.

Uncertainty source	$\Delta\mu$	
<b>Signal modeling</b>		
$t\bar{t}Z'$	+0.00	-0.00
<b>Background modeling</b>		
$t\bar{t}\bar{t}$	+0.15	-0.13
$t\bar{t}W$	+0.04	-0.03
$t\bar{t}Z$	+0.02	-0.02
$t\bar{t}H$	+0.02	-0.02
Non-prompt leptons	+0.00	-0.00
Other backgrounds	+0.02	-0.02
<b>Instrumental</b>		
Luminosity	+0.00	-0.00
Jet uncertainties	+0.04	-0.04
Jet flavor tagging ( $b$ -jets)	+0.04	-0.04
Jet flavor tagging ( $c$ -jets)	+0.01	-0.01
Jet flavor tagging (light-jets)	+0.02	-0.01
MC simulation sample size	+0.01	-0.01
Other experimental uncertainties	+0.01	-0.01
Total systematic uncertainty	+0.15	-0.17
<b>Statistical</b>		
$t\bar{t}W$ NFs and scaling factors	+0.01	-0.01
Non-prompt lepton NFs (HF, Mat. Conv., Low $m_{\gamma^*}$ )	+0.00	-0.00
Total statistical uncertainty	+0.25	-0.23
<b>Total uncertainty</b>	+0.29	-0.29

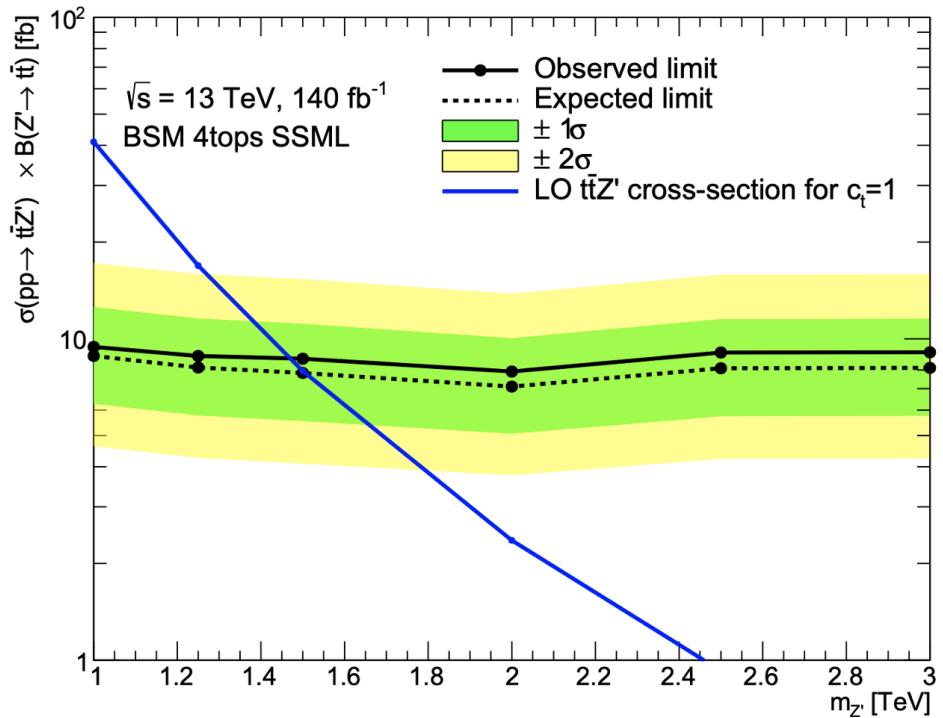


Figure 8.2: Observed (solid line) and expected (dotted line) upper limits as a function of the  $Z'$  mass at 95% CL on the cross-section of  $pp \rightarrow t\bar{t}Z'$  production times the  $Z' \rightarrow t\bar{t}$  branching ratio. The region above the observed limit is excluded. The solid blue line represents the theoretical signal cross-section with  $c_t = 1$  at LO in QCD [3]. The green and yellow bands represent the 68% ( $\pm 1\sigma$ ) and 95% ( $\pm 2\sigma$ ) confidence intervals for the expected upper limits.

# 1751 Chapter 9. Summary

1752 This dissertation presents a search for BSM top-philic heavy vector resonance based on a  
1753 simplified top-philic color singlet  $Z'(\rightarrow t\bar{t})$  model in the top-quark pair associated production  
1754 channel ( $t\bar{t}Z'$ ). The search is performed in the same-sign dilepton and multilepton channel  
1755 of the  $t\bar{t}t\bar{t}$  final states, using the full Run 2 data set collected between 2015 and 2018 by the  
1756 ATLAS detector at the LHC, corresponding to an integrated luminosity of  $140 \text{ fb}^{-1}$  of  $pp$   
1757 collisions at center-of-mass energy  $\sqrt{s} = 13 \text{ TeV}$ .

1758 New data-driven estimation methods for  $t\bar{t}W$  and charge misidentification background  
1759 are employed to improve background modeling and signal sensitivity compared to previous  
1760 analysis [31]. No significant excess over Standard Model predictions is observed. Observed  
1761 exclusion limits at 95% confidence level as a function of the  $Z'$  mass are set on the production  
1762 cross section of  $pp \rightarrow t\bar{t}Z'$  times the  $Z' \rightarrow t\bar{t}$  branching ratio, ranging from  $7.9 \text{ fb}$  (at  $m_{Z'} = 2$   
1763 TeV) to  $9.4 \text{ fb}$  (at  $m_{Z'} = 1 \text{ TeV}$ ) depending on the  $Z'$  mass. This represent a significant  
1764 improvement in the exclusion limit for  $t\bar{t}Z'$  [31], and are currently the most stringent upper  
1765 limits to date. The analysis probes a  $Z'$  mass range from  $1 \text{ TeV}$  to  $3 \text{ TeV}$  under the  
1766 assumption of a top- $Z'$  coupling strength of  $c_t = 1$  and chirality angle  $\theta = \pi/4$ .

1767 Further improvements in analysis strategies, including multivariate techniques for signal  
1768 discrimination, are expected to increase discovery potential in future searches. Looking  
1769 forward, the upcoming Run 3 data at  $\sqrt{s} = 13.6 \text{ TeV}$  will increase the  $pp \rightarrow t\bar{t}t\bar{t}$  cross  
1770 section by at least 19% [168] as well as the total integrated luminosity by about a factor  
1771 of 2 [169]. Run 3 improvements along with prospects of the High-Luminosity LHC will  
1772 significantly enhance sensitivity to BSM physics and offer more opportunities to explore  
1773 top-philic resonances and other exciting new phenomena.

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