

$$\text{Power}(x, n) \Rightarrow x^n$$

Brute Force:

```

power(x, n)
  if n == 1
    return x
  else

```

return  $x * (x, n-1)$

$$\begin{aligned}
 x^n &= x \cdot x^{n-1} \\
 &\quad \swarrow x \cdot x^{n-2} \\
 &\quad \swarrow x \cdot x^{n-2} \\
 &\quad \dots
 \end{aligned}$$

$n$  times

negative power

$$5^{-7} = \left(\frac{1}{5}\right)^7$$

$$x \leftarrow \frac{1}{x} ; n \leftarrow -1 * n$$

Time Complexity:  $O(n)$

Efficient Way:

What is better than  $O(n)$ ?

$O(\lg n) \Rightarrow$  Binary Search

power(x, n)

```

  if n == 1
    return x

```

$p \leftarrow \text{power}(x * x, n/2)$

```

  if n is even
    return p

```

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  else
    return  $p * x$ 

```

power(x, 8)

$p \leftarrow \text{power}(x * x, 4)$

$\text{power}(x^2 * x^2, 2)$

$\text{power}(x^4 * x^4, 1)$

$$n \rightarrow \frac{n}{2} \rightarrow \frac{n}{4} \rightarrow \dots 1$$

$O(\lg n)$