

# Matlab for Finance Course: Session 3

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# REVIEW OF SESSION 2

- MATLAB Basics
  - Scripts and Editor
  - Executing Scripts
  - Debugging Tools
- Data Manipulation
  - Array Operations
  - Matrix Operations
  - Array Indexing
- Programming Concepts
  - Boolean Logic
  - Control Flow (if-else, while, for, switch)
  - Error Handling
- Best Practices
  - Common Mistakes
  - Performance Tips

# SESSION OBJECTIVES

- MATLAB Fundamentals
  - Function creation and usage
  - File I/O operations
  - Data formatting and display
- Data Handling
  - Stock data import (`hist_stock_data`)
  - Time series manipulation
  - Matrix operations
- Financial Analysis
  - Returns calculation
  - Statistical analysis
  - Volatility estimation
- Risk Measures
  - VaR and CVaR implementation
  - Backtesting framework

The presentation includes MATLAB implementation for all topics except time series manipulation

# FUNCTIONS - Basic Structure

- Functions in MATLAB are defined in separate files with the .m extension
- Basic function structure:

```
1 function [output1, output2] = myFunction(input1, input2)
2     % Function description/help comment
3     % input1: description of first input
4     % input2: description of second input
5     % output1: description of first output
6     % output2: description of second output
7
8     % Function body
9     output1 = someCalculation(input1);
10    output2 = anotherCalculation(input2);
11 end
```

- Function name must match the filename (e.g., myFunction.m)
- Help comments are displayed when using `help myFunction`

# FUNCTIONS - Example

- Example of a plotting function:

```
1 function [y, h] = mysin_func(x)
2     % mysin takes the input argument and returns the
3     % sin of the argument and plots the result
4     y = sin(x);
5     h = figure;
6     plot(x, y);
7     xlabel("x");
8     ylabel("sin(x)");
9 end
```

- Call the function:

```
1 [y, h] = mysin_func(0:pi/50:2*pi);
```

# FILE TYPES

Most financial data that will be imported into MATLAB will come in three main forms:

- .csv: Comma Separated Values

```
1 Date,Open,High,Low,Close
2 2024-01-01,100.5,101.2,99.8,100.9
```

- .tsv: Tab Separated Values

```
1 Date    Open    High    Low    Close
2 2024-01-01 100.5  101.2  99.8   100.9
```

- .txt: Text data in some format

```
1 # Financial Data
2 100.5 101.2 99.8 100.9
```

Other types of data that will be imported include:

- .xls: Excel files
- .xml: Extensible Markup Language
- .mat: MATLAB binary files (loaded using `load data.mat`)

It is important to understand the organisation of different data types in order to understand the memory requirements for data.

# FILE FUNCTIONS

Command	Meaning
<code>fopen(filename)</code>	Open a file
<code>fclose(fid)</code>	Close a file
<code>fread(fid)</code>	Read binary data
<code>fwrite(fid,A,precision)</code>	Write binary data
<code>fprintf(fid,A,precision)</code>	Write formatted data
<code>fscanf(fid,format)</code>	Read formatted data
<code>sprintf(format,A)</code>	Write to a string
<code>sscanf(s,format)</code>	Read string
<code>ferror(fid)</code>	Query about errors
<code>feof(fid)</code>	Test for end of file
<code>fseek(fid,offset,origin)</code>	Set the file position indicator

- Writing and reading numeric data:

```
1 A = [1 2 3 4 5];  
2 fid = fopen('some_data.txt', 'w');  
3 fwrite(fid, A);  
4 fclose(fid);  
5  
6 fid = fopen('some_data.txt', 'r');  
7 fread(fid)  
8 fclose(fid);
```

- Writing and reading text:

```
1 str = 'this is a test';  
2 fid = fopen('test.txt', 'w');  
3 fwrite(fid, str, 'char');  
4 fclose(fid);
```



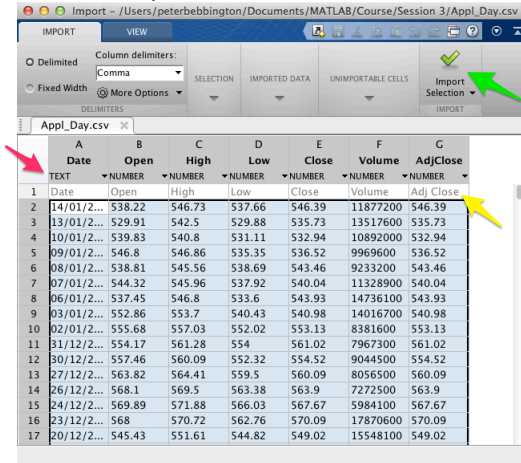
# TIMES TABLE EXAMPLE

```
1 display('Times Table:')
2 fprintf(1,' X '); % Write to command window
3 for i = 0:9
4     fprintf(1,'%2d ',i);
5 end
6 fprintf(1,'\n');
7 for i = 0:9
8     fprintf(1,'%2d ',i);
9     for j = 0:9
10        fprintf(1,'%2d ',i*j);
11    end
12    fprintf(1,'\n');
13 end
```

Output shows formatted multiplication table 0-9

# IMPORT TOOL

- Simply drag and drop a “.csv” file to the command window of Matlab to import data



Import - /Users/peterbebbington/Documents/MATLAB/Course/Session 3/Apl\_Day.csv

IMPORT VIEW

Delimited Column delimiters: Comma  
Fixed Width More Options

SELECTION IMPORTED DATA UNIMPORTABLE CELLS Import Selection IMPORT

Appl\_Day.csv

	A Date	B Open	C High	D Low	E Close	F Volume	G AdjClose
	TEXT	NUMBER	NUMBER	NUMBER	NUMBER	NUMBER	NUMBER
1	Date	Open	High	Low	Close	Volume	Adj Close
2	14/01/2...	538.22	546.73	537.66	546.39	11877200	546.39
3	13/01/2...	529.91	542.5	529.88	535.73	13517600	535.73
4	10/01/2...	539.83	540.8	531.11	532.94	10892000	532.94
5	09/01/2...	546.8	546.86	535.35	536.52	9969600	536.52
6	08/01/2...	538.81	545.56	538.69	543.46	9233200	543.46
7	07/01/2...	544.32	545.96	537.92	540.04	11328900	540.04
8	06/01/2...	537.45	546.8	533.6	543.93	14736100	543.93
9	03/01/2...	552.86	553.7	540.43	540.98	14016700	540.98
10	02/01/2...	555.68	557.03	552.02	553.13	8381600	553.13
11	31/12/2...	554.17	561.28	554	561.02	7967300	561.02
12	30/12/2...	557.46	560.09	552.32	554.52	9044500	554.52
13	27/12/2...	563.82	564.41	559.5	560.09	8056500	560.09
14	26/12/2...	568.1	569.5	563.38	563.9	7272500	563.9
15	24/12/2...	569.89	571.88	566.03	567.67	5984100	567.67
16	23/12/2...	568	570.72	562.76	570.09	17870600	570.09
17	20/12/2...	545.43	551.61	544.82	549.02	15548100	549.02

- You can edit; data type (pink arrow), data field name (yellow arrow) and import data (green arrow)

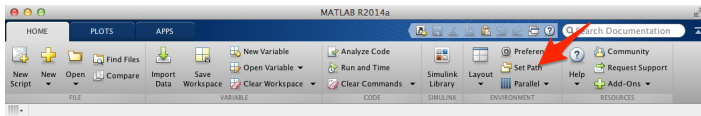
- Now that we have the data in Matlab we can create a workspace

```
1 >> whos
2   Name      Size      Bytes Class      Attributes
3   Date      252x1      2016  double
4   High      252x1      2016  double
5   Low       252x1      2016  double
6   Open      252x1      2016  double
7   Volume    252x1      2016  double
8   Close     252x1      2016  double
```

- >> clear

# HIST\_STOCK\_DATA

- Download the function from MATLAB File Exchange:  
[hist\\_stock\\_data.m](#)
- Place the file in either:
  - Your current working directory, or
  - The MATLAB folder (requires adding to path)



- Function usage:  
`hist_stock_data('StartDate', 'EndDate',  
'ticker1', 'ticker2', ...)`

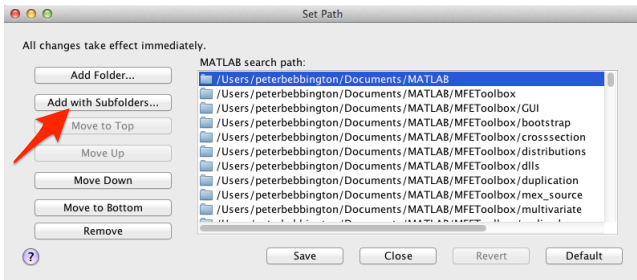
# HIST\_STOCK\_DATA EXAMPLE

```
1 >> stocks = hist_stock_data('1/1/2023', '12/31/2023',  
    'AAPL', 'MSFT');  
2 >> stocks(1)  
3     Date: [252×1 double]  
4     Open: [252×1 double]  
5     High: [252×1 double]  
6     Low: [252×1 double]  
7     Close: [252×1 double]  
8     Volume: [252×1 double]  
9     Ticker: 'AAPL'  
10  
11 >> stocks(2)  
12     Date: [252×1 double]  
13     Open: [252×1 double]  
14     High: [252×1 double]  
15     Low: [252×1 double]  
16     Close: [252×1 double]  
17     Volume: [252×1 double]  
18     Ticker: 'MSFT'
```

- Matlab has its own Econometrics toolbox with rich functionality
- There are also third-party toolboxes that can be installed which can help with time series analysis for summer projects
- Two recommended toolboxes:
  - MFEToolbox: [www.kevinsheppard.com](http://www.kevinsheppard.com)
  - JPLV7: [www.spatial-econometrics.com](http://www.spatial-econometrics.com)

# INSTALLING TOOLBOXES

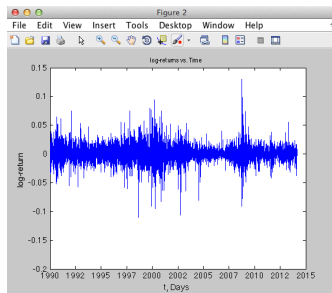
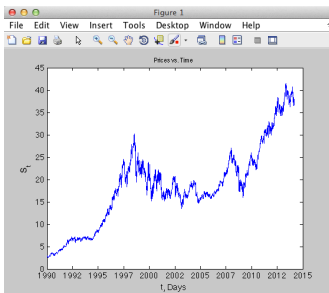
- As we did for `hist_stock_data` put the toolboxes in a folder sensible such as the Matlab folder in “My Documents” or Documents.



- Click “Add with Subfolders...” (red arrow) and Locate the two toolboxes and save.

# FINANCIAL SERIES

- A good starting point when analyzing financial time series is to plot basic quantities against time, such as price, log-returns, volume, etc...





# SAMPLE STATISTICS: Basic Moments

- Basic statistics measure the shape and central tendencies of returns

```
1 % Basic Statistics
2 mean_lr    = mean(lreturns); % First moment
3 std_lr     = std(lreturns);  % Second moment (volatility)
4 ske_lr     = skewness(lreturns); % Third moment (asymmetry)
5 kurt_lr    = kurtosis(lreturns); % Fourth moment (tail
    thickness)
```

- For financial returns, we typically expect:
  - Mean close to zero
  - Significant volatility
  - Negative skewness (more extreme losses than gains)
  - High kurtosis (fat tails)

- Statistical tests help verify stylized facts of returns

```
1 % Serial Correlation Tests
2 sacf_lr   = sacf(lreturns, 1, 1, 0); % Return predictability
3 sacf_lr2  = sacf(lreturns.^2, 1, 1, 0); % Volatility
           clustering
4
5 % Normality Tests
6 [jb_lr, pval] = jarquebera(lreturns); % Jarque-Bera test
7 kst_lr       = kstest(lreturns);      % Kolmogorov-Smirnov
```

- Test Interpretations:
  - Serial correlation tests check for time dependencies
  - Normality tests verify distribution assumptions

- Any Gaussian distributed random variable can be normalized:

$$X \sim \mathcal{N}(\mu, \sigma^2)$$

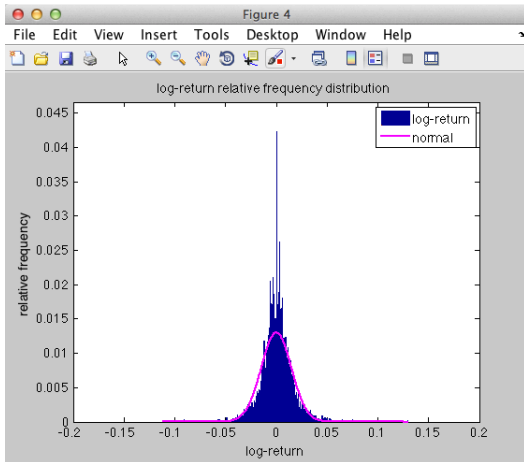
$$Z = \frac{X - \mu}{\sigma} \quad (\text{standardization})$$

$$X = \sigma Z + \mu \quad (\text{reconstruction})$$

- Analysis of return time series is better in this form for comparison between different time series such as a portfolio

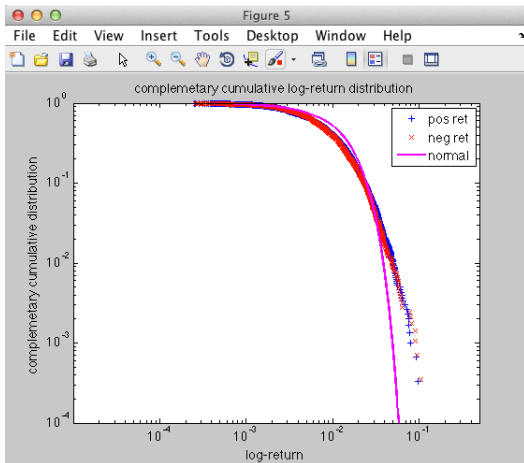
# COMPARISON WITH A GAUSSIAN

- Here we make a comparison of the empirical histogram against a parametrized normal distribution



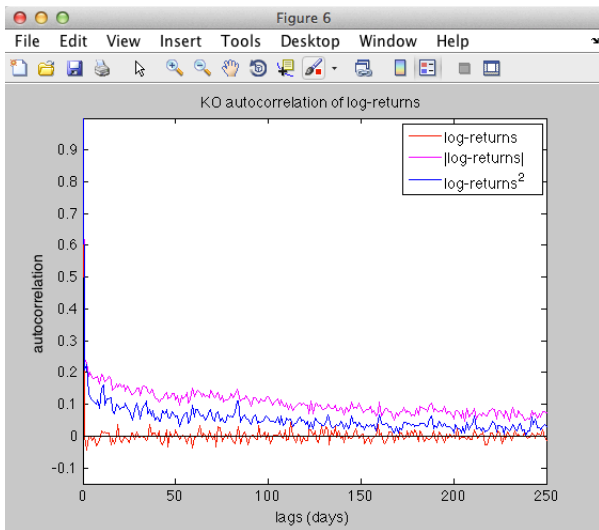
# COMPLEMENTARY CUMULATIVE DISTRIBUTION

- We see in this log-log plot the empirical time series differs from the tails of a normal distribution, indicating heavier tails in the data



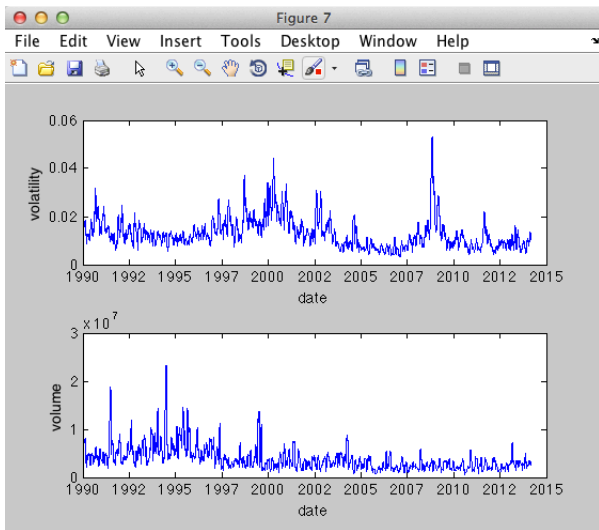
# AUTOCORRELOGRAM

- Shows correlation between returns at different time lags
- Helps identify patterns and dependencies in the time series



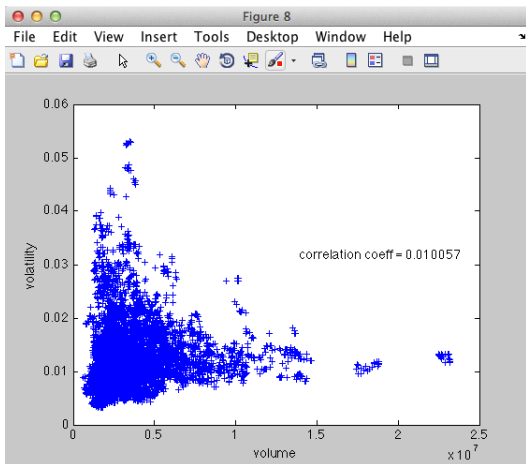
# VOLATILITY

- Volatility measures the dispersion of returns over time
- Calculated using a rolling window of 252 trading days



# VOLATILITY Vs. VOLUME

- Higher trading volume often associated with higher volatility
- Correlation coefficient indicates strength of relationship

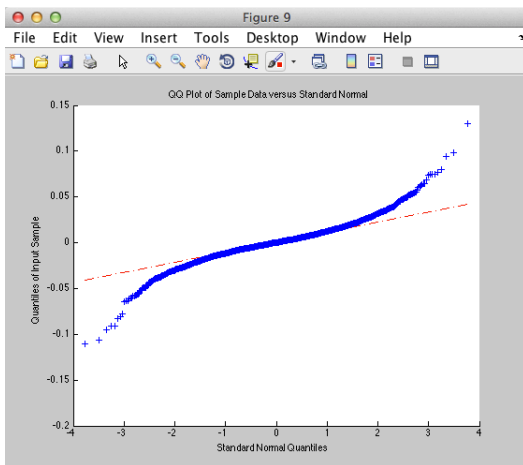


- Important for trading strategy and risk management



# QQPLOT (QUANTILE-QUANTILE PLOT)

- Compares empirical distribution against theoretical normal
- Straight line indicates normality; deviations show fat tails



- Financial returns typically show deviations at the tails

# VALUE AT RISK (VaR) - Mathematical Definition

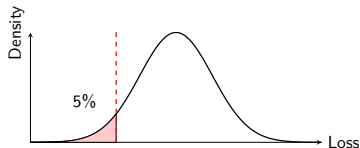
- VaR is formally defined as:

$$\text{VaR}_\alpha \triangleq \inf\{l \in \mathbb{R} : F_L(l) \geq \alpha\}$$

- Breaking down the equation:
  - $\text{VaR}_\alpha$ : Value at Risk at confidence level  $\alpha$
  - $\inf$ : Infimum (minimum value)
  - $l \in \mathbb{R}$ : Loss value in real numbers
  - $F_L(l)$ : Cumulative distribution function of losses
  - $\geq \alpha$ : Probability threshold (e.g., 0.95)
- In simpler terms:
  - VaR is the smallest loss value
  - Where the probability of exceeding this loss
  - Is less than or equal to  $1 - \alpha$  (e.g., 5%)

# VALUE AT RISK (VaR) - Visualization

- VaR represents a threshold where probability of larger losses is  $1 - \alpha$



- Example interpretation:
  - $\text{VaR}_{95\%} = \$100$  means there's a 5% chance of losing more than \$100
  - Red area shows probability of extreme losses

# VAR ESTIMATION IN MATLAB

- Parametric estimation (assuming normal distribution):  
`ValueAtRisk = portvrisk(PortReturn, PortRisk,  
RiskThreshold, PortValue)`
- Function parameters:
  - PortReturn: Expected portfolio return
  - PortRisk: Portfolio standard deviation
  - RiskThreshold: Confidence level (e.g., 0.95)
  - PortValue: Current portfolio value
- Limitations:
  - Assumes normal distribution
  - May underestimate tail risk
  - Compare with empirical estimation

# CONDITIONAL VALUE AT RISK (CVaR) - Mathematical Definition

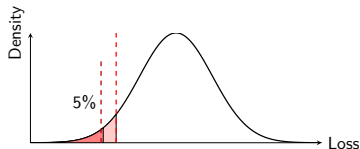
- CVaR is formally defined as:

$$\text{CVaR}_\alpha = \mathbb{E}[L|L \geq \text{VaR}_\alpha] = \frac{1}{1-\alpha} \int_\alpha^1 \text{VaR}_\gamma(L) d\gamma$$

- Breaking down the equation:
  - $\text{CVaR}_\alpha$ : Expected loss exceeding VaR
  - $\mathbb{E}[L|L \geq \text{VaR}_\alpha]$ : Conditional expectation
  - $\frac{1}{1-\alpha}$ : Normalization factor
  - $\text{VaR}_\gamma(L)$ : VaR at confidence level  $\gamma$
- In simpler terms:
  - CVaR is the average loss in the worst  $(1-\alpha)\%$  of cases
  - More conservative than VaR
  - Accounts for the shape of the tail distribution

# CONDITIONAL VALUE AT RISK (CVaR) - Visualization

- CVaR measures the average loss beyond VaR



- Example interpretation:
  - If  $\text{VaR}_{95\%} = \$100$ ,  $\text{CVaR}_{95\%}$  might be  $\$150$
  - CVaR represents average loss in worst 5
  - Darker red area shows the region CVaR measures

- Conditional Value at Risk (CVaR) calculations:

```
1 % Parametric CVaR
2 m = mean(lreturns(:,1));
3 s = std(lreturns(:,1));
4 CVaR_95 = -m + s*(normpdf(norminv(0.05,0,1),0,1))/(1-0.95);
5 CVaR_99 = -m + s*(normpdf(norminv(0.01,0,1),0,1))/(1-0.99);
6
7 % Empirical CVaR
8 CVaR_95_emp = -mean(slr(1:ceil(N*0.05))); % 5% loss
9 CVaR_99_emp = -mean(slr(1:ceil(N*0.01))); % 1% loss
```

- CVaR represents the expected loss exceeding VaR
- Also known as Expected Shortfall (ES)
- More coherent risk measure than VaR

# COMPARISON OF RISK MEASURES

- Key differences between VaR and CVaR:
  - VaR: Maximum loss at confidence level
  - CVaR: Average loss beyond VaR

Property	VaR	CVaR
Coherence	No	Yes
Tail Sensitivity	Limited	High
Ease of Calculation	Higher	Lower
Regulatory Use	Basel II	Basel III



# PORTFOLIO RISK ANALYSIS

- Portfolio risk calculations in MATLAB:

```
1 % Portfolio weights
2 w = [0.6 0.4]; % 60% Stock1, 40% Stock2
3
4 % Portfolio return
5 port_return = w * returns;
6
7 % Portfolio variance
8 port_var = w * cov(returns) * w';
9
10 % Portfolio VaR
11 port_VaR = portvrisk(port_return, sqrt(port_var), 0.95, 1);
```

- Key considerations:

- Correlation between assets
- Diversification benefits
- Rebalancing frequency

# BACKTESTING RISK MEASURES

- Verify accuracy of risk measures:

```
1 % Count VaR violations
2 violations = sum(returns < -VaR_95);
3 violation_rate = violations/length(returns);
4
5 % Kupiec test
6 [h,p] = kupiectest(violations, length(returns), 0.05);
```

- Testing approaches:
  - Violation ratio analysis
  - Independence tests
  - Dynamic backtesting

# BACKTESTING - OVERVIEW

- Purpose of Backtesting:
  - Validate risk model accuracy
  - Meet regulatory requirements
  - Improve risk estimation
- Key Concepts:
  - VaR violation: When actual loss exceeds VaR estimate
  - Expected violation frequency:  $(1 - \alpha)$  for  $\text{VaR}_\alpha$
  - Example: For 95% VaR, expect violations in 5% of cases
- Backtesting Period:
  - Typically 250-500 trading days
  - Basel requirement: Minimum 250 days
  - Need sufficient data for statistical significance

- Basic VaR Violation Test:

```
1 % Count VaR violations
2 violations = sum(returns < -VaR_95);
3 violation_rate = violations/length(returns);
4
5 % Expected rate for 95% VaR is 0.05
6 excess = (violation_rate - 0.05)/0.05;
7 fprintf('Violation excess: %.2f%%\n', excess*100);
```

- Rolling Window Analysis:

```
1 window = 252; % One trading year
2 for t = window:length(returns)
3     % Estimate VaR using rolling window
4     rolling_var = std(returns(t-window+1:t));
5     rolling_VaR = norminv(0.05)*rolling_var;
6
7     % Check for violation
8     violations(t) = returns(t) < -rolling_VaR;
9 end
```

# STATISTICAL TESTS FOR BACKTESTING

- Kupiec Test (Unconditional Coverage):
  - Tests if violation frequency matches expected rate
  - Null hypothesis: Observed rate = Expected rate
  - Uses likelihood ratio test
- Christoffersen Test (Conditional Coverage):
  - Tests independence of violations
  - Checks for violation clustering
  - Combines tests for frequency and independence
- Dynamic Quantile Test:
  - Tests if violations are predictable
  - Uses regression-based approach
  - More powerful than basic tests

- Traffic Light Approach (Basel):

Zone	Violations	Multiplier
Green	0-4	3.00
Yellow	5-9	3.40-3.85
Red	10+	4.00

- Duration-Based Tests:

```
1 % Time between violations
2 durations = diff(find(violations));
3 [h,p] = duration_test(durations, alpha);
```

- Multiple VaR Levels:
  - Test at different confidence levels
  - Compare 95%, 99%, 99.9% VaR
  - Check consistency across levels

# INTERPRETING BACKTESTING RESULTS

- Common Issues:
  - Too many violations: Model underestimates risk
  - Too few violations: Model too conservative
  - Clustered violations: Model misses regime changes

# KUPIEC TEST (UNCONDITIONAL COVERAGE)

- Purpose:
  - Tests if the observed violation frequency equals expected rate
  - Known as Proportion of Failures (POF) test
  - Fundamental VaR validation tool
- Test Statistics:
  - Let  $N$  = number of violations
  - Let  $T$  = total number of observations
  - Let  $p$  = expected violation rate (e.g., 0.05 for 95% VaR)
  - Let  $\hat{p} = N/T$  = observed violation rate
- Likelihood Ratio Test:

$$LR_{POF} = -2 \ln \left[ \frac{(1-p)^{T-N} p^N}{(1-\hat{p})^{T-N} \hat{p}^N} \right] \\ \sim \chi^2(1)$$



# KUPIEC TEST - IMPLEMENTATION

```
1 function [h, pValue, stat] = kupiectest(violations, T, p)
2     % violations: number of VaR violations
3     % T: total number of observations
4     % p: expected violation rate (e.g., 0.05 for 95% VaR)
5
6     % Observed violation rate
7     p_hat = violations/T;
8
9     % Compute likelihood ratio statistic
10    if p_hat == 0
11        stat = -2*log((1-p)^T);
12    else
13        stat = -2*log((1-p)^(T-violations) * p^violations) ...
14            + 2*log((1-p_hat)^(T-violations) *
15                p_hat^violations);
16
17    end
18
19    % Test against chi-square distribution
20    pValue = 1 - chi2cdf(stat, 1);
21    h = (pValue < 0.05); % Reject at 5% significance
```

# INTERPRETING KUPIEC TEST RESULTS

- Null Hypothesis:
  - $H_0$ : The model's violation rate equals the expected rate
  - $H_1$ : The model's violation rate differs from expected
- Decision Rules:
  - Reject  $H_0$  if  $LR_{POF} > \chi^2_{1,\alpha}$
  - Typical significance level  $\alpha = 0.05$
  - Critical value  $\chi^2_{1,0.05} = 3.841$
- Limitations:
  - Only tests violation frequency
  - Ignores clustering of violations
  - Low power for small samples
  - Should be combined with other tests