

Matlab for Finance Course: Session 3

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REVIEW OF SESSION 2

- MATLAB Basics
 - Scripts and Editor
 - Executing Scripts
 - Debugging Tools
- Data Manipulation
 - Array Operations
 - Matrix Operations
 - Array Indexing
- Programming Concepts
 - Boolean Logic
 - Control Flow (if-else, while, for, switch)
 - Error Handling
- Best Practices
 - Common Mistakes
 - Performance Tips

SESSION OBJECTIVES

- MATLAB Fundamentals
 - Function creation and usage
 - File I/O operations
 - Data formatting and display
- Data Handling
 - Stock data import (`getMarketDataViaTiingo`)
 - Time series manipulation
 - Matrix operations
- Financial Analysis
 - Returns calculation
 - Statistical analysis
 - Volatility estimation
- Risk Measures
 - VaR and CVaR implementation
 - Backtesting framework

The presentation includes MATLAB implementation for all topics.

FUNCTIONS - Basic Structure

- Functions in MATLAB are defined in separate files with the .m extension
- Basic function structure:

```
1 function [output1, output2] = myFunction(input1, input2)
2     % Function description/help comment
3     % input1: description of first input
4     % input2: description of second input
5     % output1: description of first output
6     % output2: description of second output
7
8     % Function body
9     output1 = someCalculation(input1);
10    output2 = anotherCalculation(input2);
11 end
```

- Function name must match the filename (e.g., myFunction.m)
- Help comments are displayed when using `help myFunction`

FUNCTIONS - Example

- Example of a plotting function:

```
1 function [y, h] = mysin_func(x)
2     % mysin takes the input argument and returns the
3     % sin of the argument and plots the result
4     y = sin(x);
5     h = figure;
6     plot(x, y);
7     xlabel("x");
8     ylabel("sin(x)");
9 end
```

- Call the function:

```
1 [y, h] = mysin_func(0:pi/50:2*pi);
```

FILE TYPES

Most financial data that will be imported into MATLAB will come in three main forms:

- .csv: Comma Separated Values

```
1 Date,Open,High,Low,Close
2 2024-01-01,100.5,101.2,99.8,100.9
```

- .tsv: Tab Separated Values

```
1 Date    Open    High    Low    Close
2 2024-01-01 100.5  101.2  99.8   100.9
```

- .txt: Text data in some format

```
1 # Financial Data
2 100.5 101.2 99.8 100.9
```

Other types of data that will be imported include:

- .xls: Excel files
- .xml: Extensible Markup Language
- .mat: MATLAB binary files (loaded using `load data.mat`)

It is important to understand the organisation of different data types in order to understand the memory requirements for data.

FILE FUNCTIONS

Command	Meaning
<code>fopen(filename)</code>	Open a file
<code>fclose(fid)</code>	Close a file
<code>fread(fid)</code>	Read binary data
<code>fwrite(fid,A,precision)</code>	Write binary data
<code>fprintf(fid,A,precision)</code>	Write formatted data
<code>fscanf(fid,format)</code>	Read formatted data
<code>sprintf(format,A)</code>	Write to a string
<code>sscanf(s,format)</code>	Read string
<code>ferror(fid)</code>	Query about errors
<code>feof(fid)</code>	Test for end of file
<code>fseek(fid,offset,origin)</code>	Set the file position indicator

- Writing and reading numeric data:

```
1 A = [1 2 3 4 5];  
2 fid = fopen('some_data.txt', 'w');  
3 fwrite(fid, A);  
4 fclose(fid);  
5  
6 fid = fopen('some_data.txt', 'r');  
7 fread(fid)  
8 fclose(fid);
```

- Writing and reading text:

```
1 str = 'this is a test';  
2 fid = fopen('test.txt', 'w');  
3 fwrite(fid, str, 'char');  
4 fclose(fid);
```

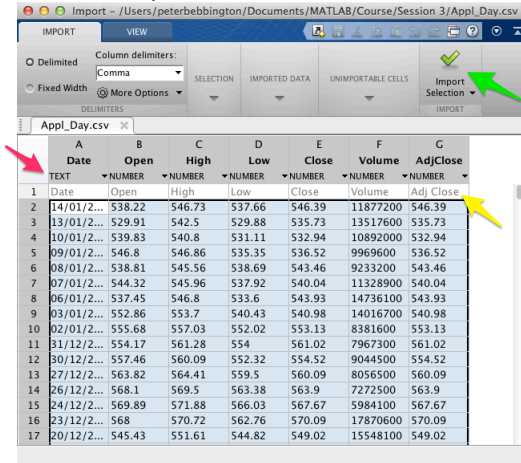

TIMES TABLE EXAMPLE

```
1 display('Times Table:')
2 fprintf(1,' X '); % Write to command window
3 for i = 0:9
4     fprintf(1,'%2d ',i);
5 end
6 fprintf(1,'\n');
7 for i = 0:9
8     fprintf(1,'%2d ',i);
9     for j = 0:9
10        fprintf(1,'%2d ',i*j);
11    end
12    fprintf(1,'\n');
13 end
```

Output shows formatted multiplication table 0-9

IMPORT TOOL

- Simply drag and drop a “.csv” file to the command window of Matlab to import data



Import - /Users/peterbebbington/Documents/MATLAB/Course/Session 3/Apl_Day.csv

IMPORT VIEW

Delimited Column delimiters: Comma ☐ Fixed Width ☒ More Options

SELECTION IMPORTED DATA UNIMPORTABLE CELLS Import Selection IMPORT

Appl_Day.csv

	A Date	B Open	C High	D Low	E Close	F Volume	G AdjClose
	TEXT	NUMBER	NUMBER	NUMBER	NUMBER	NUMBER	NUMBER
	Date	Open	High	Low	Close	Volume	Adj Close
1							
2	14/01/2...	538.22	546.73	537.66	546.39	11877200	546.39
3	13/01/2...	529.91	542.5	529.88	535.73	13517600	535.73
4	10/01/2...	539.83	540.8	531.11	532.94	10892000	532.94
5	09/01/2...	546.8	546.86	535.35	536.52	9969600	536.52
6	08/01/2...	538.81	545.56	538.69	543.46	9233200	543.46
7	07/01/2...	544.32	545.96	537.92	540.04	11328900	540.04
8	06/01/2...	537.45	546.8	533.6	543.93	14736100	543.93
9	03/01/2...	552.86	553.7	540.43	540.98	14016700	540.98
10	02/01/2...	555.68	557.03	552.02	553.13	8381600	553.13
11	31/12/2...	554.17	561.28	554	561.02	7967300	561.02
12	30/12/2...	557.46	560.09	552.32	554.52	9044500	554.52
13	27/12/2...	563.82	564.41	559.5	560.09	8056500	560.09
14	26/12/2...	568.1	569.5	563.38	563.9	7272500	563.9
15	24/12/2...	569.89	571.88	566.03	567.67	5984100	567.67
16	23/12/2...	568	570.72	562.76	570.09	17870600	570.09
17	20/12/2...	545.43	551.61	544.82	549.02	15548100	549.02

- You can edit; data type (pink arrow), data field name (yellow arrow) and import data (green arrow)

- Now that we have the data in Matlab we can create a workspace

```
1 >> whos
2   Name      Size      Bytes Class      Attributes
3   Date      252x1      2016  double
4   High      252x1      2016  double
5   Low       252x1      2016  double
6   Open      252x1      2016  double
7   Volume    252x1      2016  double
8   Close     252x1      2016  double
```

- >> clear

- We'll use Tiingo API to download historical stock data
- Steps to get started:
 - Sign up for free account at [Tiingo](#)
 - Generate API key from your account dashboard
 - Set up API key in MATLAB:

```
setenv('TIINGO_API_KEY', 'your_api_key_here');
```

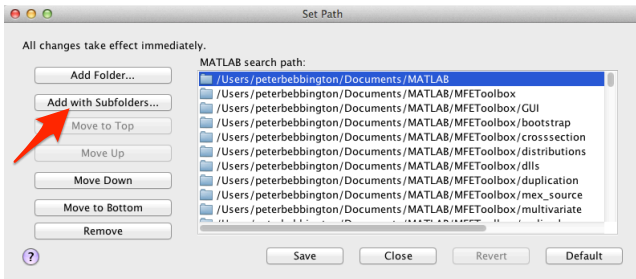
- Advantages of Tiingo:
 - Reliable and maintained API
 - High-quality financial data
 - Free tier available for academic use

TIINGO API EXAMPLE

```
% Download one year of daily data for AAPL and MSFT
>> startdt = '2023-01-01';
>> enddt = '2023-12-31';
% Get AAPL data
>> aapl = tiingo_prices('AAPL', startdt, enddt, 'daily');
% Get MSFT data
>> msft = tiingo_prices('MSFT', startdt, enddt, 'daily');
% Data structure example:
>> aapl
    date: [252x1 datetime]
   open: [252x1 double]
   high: [252x1 double]
    low: [252x1 double]
  close: [252x1 double]
 volume: [252x1 double]
```

- Matlab has its own Econometrics toolbox with rich functionality
- There are also third-party toolboxes that can be installed which can help with time series analysis for summer projects
- Two recommended toolboxes:
 - MFEToolbox: www.kevinsheppard.com
 - JPLV7: www.spatial-econometrics.com

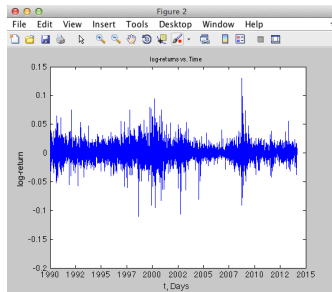
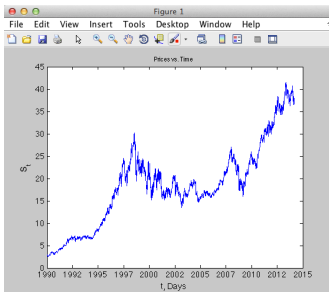
INSTALLING TOOLBOXES



- Click “Add with Subfolders...” (red arrow) and Locate the two toolboxes and save.

FINANCIAL SERIES

- A good starting point when analyzing financial time series is to plot basic quantities against time, such as price, log-returns, volume, etc...



SAMPLE STATISTICS: Basic Moments

- Basic statistics measure the shape and central tendencies of returns

```
1 % Basic Statistics
2 mean_lr    = mean(lreturns); % First moment
3 std_lr     = std(lreturns);  % Second moment (volatility)
4 ske_lr     = skewness(lreturns); % Third moment (asymmetry)
5 kurt_lr    = kurtosis(lreturns); % Fourth moment (tail
    thickness)
```

- For financial returns, we typically expect:
 - Mean close to zero
 - Significant volatility
 - Negative skewness (more extreme losses than gains)
 - High kurtosis (fat tails)

- Statistical tests help verify stylized facts of returns

```
1 % Serial Correlation Tests
2 sacf_lr   = sacf(lreturns, 1, 1, 0); % Return predictability
3 sacf_lr2  = sacf(lreturns.^2, 1, 1, 0); % Volatility
           clustering
4
5 % Normality Tests
6 [jb_lr, pval] = jarquebera(lreturns); % Jarque-Bera test
7 kst_lr       = kstest(lreturns);      % Kolmogorov-Smirnov
```

- Test Interpretations:
 - Serial correlation tests check for time dependencies
 - Normality tests verify distribution assumptions

- Any Gaussian distributed random variable can be normalized:

$$X \sim \mathcal{N}(\mu, \sigma^2)$$

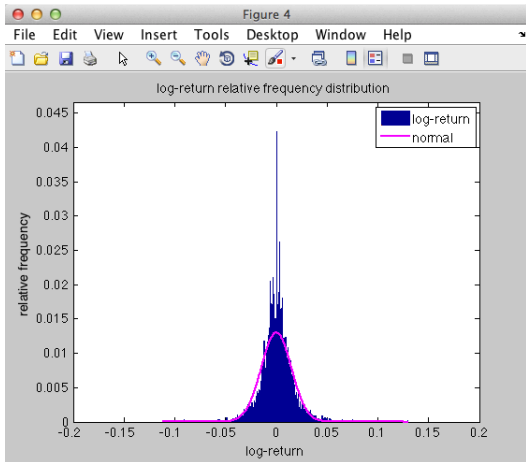
$$Z = \frac{X - \mu}{\sigma} \quad (\text{standardization})$$

$$X = \sigma Z + \mu \quad (\text{reconstruction})$$

- Analysis of return time series is better in this form for comparison between different time series such as a portfolio

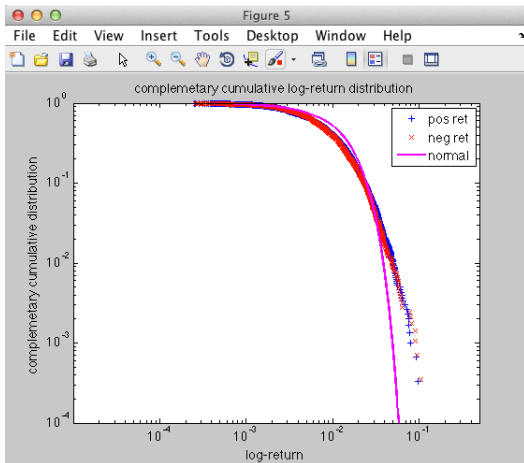
COMPARISON WITH A GAUSSIAN

- Here we make a comparison of the empirical histogram against a parametrized normal distribution



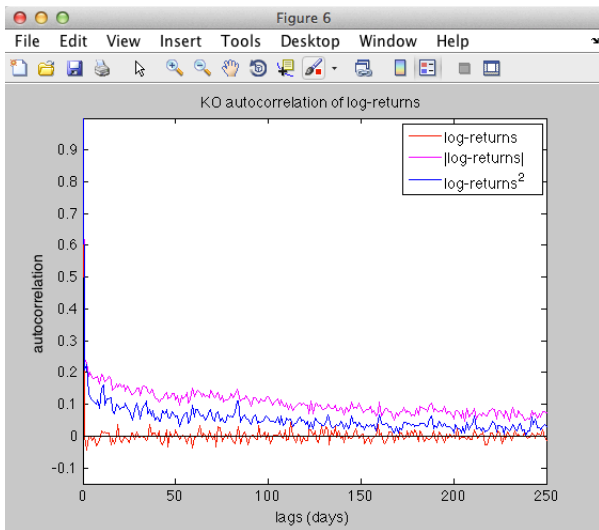
COMPLEMENTARY CUMULATIVE DISTRIBUTION

- We see in this log-log plot the empirical time series differs from the tails of a normal distribution, indicating heavier tails in the data



AUTOCORRELOGRAM

- Shows correlation between returns at different time lags
- Helps identify patterns and dependencies in the time series



VOLATILITY CALCULATION: The Cumsum Trick

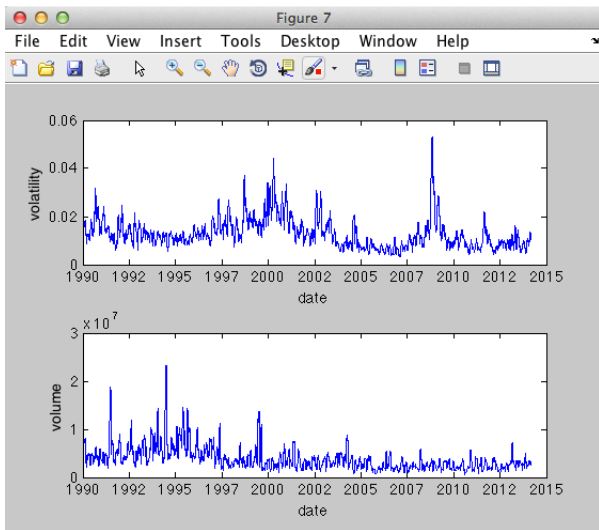
- Efficient method to calculate rolling window volatility using cumulative sums

```
1 % Step 1: Calculate cumulative sums
2 window = 252; % Trading days in a year
3 Y1 = cumsum(lreturns(:,1), 1); % Cumsum of returns
4 Y2 = cumsum(lreturns(:,1).^2, 1); % Cumsum of squared returns
5 % Step 2: Calculate rolling window volatility
6 volatility = sqrt(
7     (Y2((window+1):end) - Y2(1:(end-window))) / window %
8     Variance
9     - ((Y1((window+1):end) - Y1(1:(end-window))) / window).^2
10    % Mean^2);
```

- Key advantages:
 - Vectorized operations (faster than loops)
 - Memory efficient (only stores cumsum)
 - Based on variance formula: $\sigma^2 = E[X^2] - (E[X])^2$
- Window calculations:
 - $Y2(t+w) - Y2(t)$: Sum of squared returns in window
 - $Y1(t+w) - Y1(t)$: Sum of returns in window
 - Division by window gives rolling means

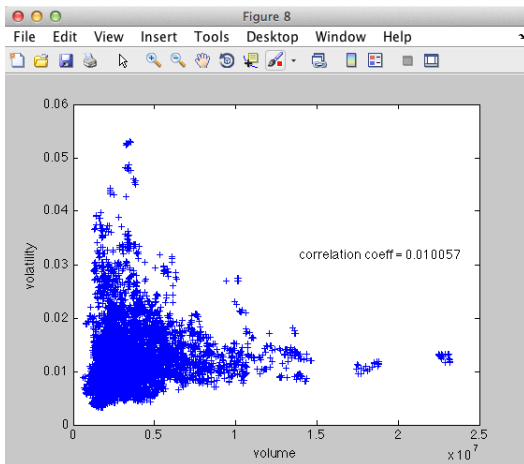
VOLATILITY

- Volatility measures the dispersion of returns over time
- Calculated using a rolling window of 252 trading days



VOLATILITY Vs. VOLUME

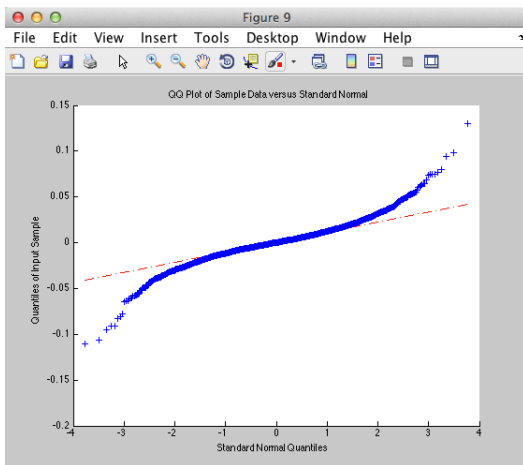
- Higher trading volume often associated with higher volatility
- Correlation coefficient indicates strength of relationship



- Important for trading strategy and risk management

QQPLOT (QUANTILE-QUANTILE PLOT)

- Compares empirical distribution against theoretical normal
- Straight line indicates normality; deviations show fat tails



- Financial returns typically show deviations at the tails

VALUE AT RISK (VaR) - Mathematical Definition

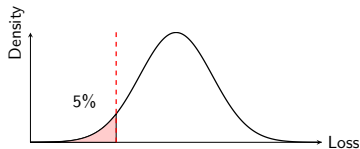
- VaR is formally defined as:

$$\text{VaR}_\alpha \triangleq \inf\{l \in \mathbb{R} : F_L(l) \geq \alpha\}$$

- Breaking down the equation:
 - VaR_α : Value at Risk at confidence level α
 - \inf : Infimum (minimum value)
 - $l \in \mathbb{R}$: Loss value in real numbers
 - $F_L(l)$: Cumulative distribution function of losses
 - $\geq \alpha$: Probability threshold (e.g., 0.95)
- In simpler terms:
 - VaR is the smallest loss value
 - Where the probability of exceeding this loss
 - Is less than or equal to $1 - \alpha$ (e.g., 5%)

VALUE AT RISK (VaR) - Visualization

- VaR represents a threshold where probability of larger losses is $1 - \alpha$



- Example interpretation:
 - $\text{VaR}_{95\%} = \$100$ means there's a 5% chance of losing more than \$100
 - Red area shows probability of extreme losses

VAR ESTIMATION IN MATLAB

- Parametric estimation (assuming normal distribution):
`ValueAtRisk = portvrisk(PortReturn, PortRisk,
RiskThreshold, PortValue)`
- Function parameters:
 - PortReturn: Expected portfolio return
 - PortRisk: Portfolio standard deviation
 - RiskThreshold: Confidence level (e.g., 0.95)
 - PortValue: Current portfolio value
- Limitations:
 - Assumes normal distribution
 - May underestimate tail risk
 - Compare with empirical estimation

CONDITIONAL VALUE AT RISK (CVaR) - Mathematical Definition

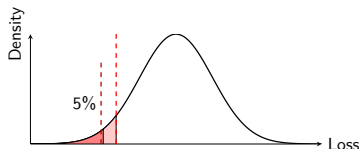
- CVaR is formally defined as:

$$\text{CVaR}_\alpha = \mathbb{E}[L|L \geq \text{VaR}_\alpha] = \frac{1}{1-\alpha} \int_\alpha^1 \text{VaR}_\gamma(L) d\gamma$$

- Breaking down the equation:
 - CVaR_α : Expected loss exceeding VaR
 - $\mathbb{E}[L|L \geq \text{VaR}_\alpha]$: Conditional expectation
 - $\frac{1}{1-\alpha}$: Normalization factor
 - $\text{VaR}_\gamma(L)$: VaR at confidence level γ
- In simpler terms:
 - CVaR is the average loss in the worst $(1-\alpha)\%$ of cases
 - More conservative than VaR
 - Accounts for the shape of the tail distribution

CONDITIONAL VALUE AT RISK (CVaR) - Visualization

- CVaR measures the average loss beyond VaR



- Example interpretation:
 - If $\text{VaR}_{95\%} = \$100$, $\text{CVaR}_{95\%} = \$130$ for normally distributed returns
 - CVaR represents average loss in worst 5% of cases
 - Darker red area shows the region CVaR measures

- Conditional Value at Risk (CVaR) calculations:

```
1 % Parametric CVaR
2 m = mean(lreturns(:,1));
3 s = std(lreturns(:,1));
4 CVaR_95 = -m + s*(normpdf(norminv(0.05,0,1),0,1))/(1-0.95);
5 CVaR_99 = -m + s*(normpdf(norminv(0.01,0,1),0,1))/(1-0.99);
6
7 % Empirical CVaR
8 CVaR_95_emp = -mean(slr(1:ceil(N*0.05))); % 5% loss
9 CVaR_99_emp = -mean(slr(1:ceil(N*0.01))); % 1% loss
```

- CVaR represents the expected loss exceeding VaR
- Also known as Expected Shortfall (ES)
- More coherent risk measure than VaR

INTERPRETING VAR RESULTS

- Sample VaR Results:

Method	95% VaR	99% VaR
Parametric	1.75%	2.49%
Empirical	1.56%	3.10%

- Key Insights:

- Parametric assumes normal distribution
- Empirical uses actual historical data
- Difference suggests non-normal distribution
- Higher empirical 99% VaR indicates fat tails

- Practical Example (for \$1,000,000 portfolio):

- 95% Parametric: Max loss of \$17,520
- 95% Empirical: Max loss of \$15,612
- 99% Parametric: Max loss of \$24,894
- 99% Empirical: Max loss of \$30,968

- Recommendation:

- Rely more on empirical values
- Better captures actual risk characteristics
- More conservative at higher confidence levels

COMPARISON OF RISK MEASURES

- Key differences between VaR and CVaR:
 - VaR: Maximum loss at confidence level
 - CVaR: Average loss beyond VaR

Property	VaR	CVaR
Coherence	No	Yes
Tail Sensitivity	Limited	High
Ease of Calculation	Higher	Lower
Regulatory Use	Basel II	Basel III

BACKTESTING - OVERVIEW

- Purpose of Backtesting:
 - Validate risk model accuracy
 - Meet regulatory requirements
 - Improve risk estimation
- Key Concepts:
 - VaR violation: When actual loss exceeds VaR estimate
 - Expected violation frequency: $(1 - \alpha)$ for VaR_α
 - Example: For 95% VaR, expect violations in 5% of cases
- Backtesting Period:
 - Typically 250-500 trading days
 - Basel requirement: Minimum 250 days
 - Need sufficient data for statistical significance

BACKTESTING RISK MEASURES

- Verify accuracy of risk measures:

```
1 % Count VaR violations
2 violations = sum(returns < -VaR_95);
3 violation_rate = violations/length(returns);
4 % Kupiec test
5 [h,p] = kupiectest(violations, length(returns), 0.05);
```

- Testing approaches:
 - Violation ratio analysis
 - Compares actual violations to expected frequency
 - For 95% VaR, expect violations 5% of the time
 - Ratio > 1 indicates model underestimates risk
 - Independence tests
 - Examines clustering of violations
 - Uses Christoffersen's test for independence
 - Clustering suggests model weakness in stress periods
 - Dynamic backtesting
 - Uses rolling windows (typically 250 days)
 - Updates risk estimates with new data
 - Better captures changing market conditions

- Basic VaR Violation Test:

```
1 % Count VaR violations
2 violations = sum(returns < -VaR_95);
3 violation_rate = violations/length(returns);
4
5 % Expected rate for 95% VaR is 0.05
6 excess = (violation_rate - 0.05)/0.05;
7 fprintf('Violation excess: %.2f%%\n', excess*100);
```

- Rolling Window Analysis:

```
1 window = 252; % One trading year
2 for t = window:length(returns)
3     % Estimate VaR using rolling window
4     rolling_var = std(returns(t-window+1:t));
5     rolling_VaR = norminv(0.05)*rolling_var;
6
7     % Check for violation
8     violations(t) = returns(t) < -rolling_VaR;
9 end
```

STATISTICAL TESTS FOR BACKTESTING

- Kupiec Test (Unconditional Coverage):
 - Tests if violation frequency matches expected rate
 - Null hypothesis: Observed rate = Expected rate
 - Uses likelihood ratio test
- Christoffersen Test (Conditional Coverage):
 - Tests independence of violations
 - Checks for violation clustering
 - Combines tests for frequency and independence
- Dynamic Quantile Test:
 - Tests if violations are predictable
 - Uses regression-based approach
 - More powerful than basic tests

ADVANCED BACKTESTING TECHNIQUES

- Purpose of Multipliers:
 - Determines capital requirements for market risk
 - Penalizes banks for inaccurate VaR models
 - Formula: $\text{Capital} = \text{VaR} \times \text{Multiplier}$
- Traffic Light Approach (Basel):

Zone	Violations	Multiplier
Green	0-4	3.00
Yellow	5-9	3.40-3.85
Red	10+	4.00

- Duration-Based Tests:

```
1 % Time between violations
2 durations = diff(find(violations));
3 [h,p] = duration_test(durations, alpha);
```

- Multiple VaR Levels:
 - Test at different confidence levels
 - Compare 95%, 99%, 99.9% VaR
 - Check consistency across levels

KUPIEC TEST (UNCONDITIONAL COVERAGE)

- Purpose:
 - Tests if the observed violation frequency equals expected rate
 - Known as Proportion of Failures (POF) test
 - Fundamental VaR validation tool
- Test Statistics:
 - Let N = number of violations
 - Let T = total number of observations
 - Let p = expected violation rate (e.g., 0.05 for 95% VaR)
 - Let $\hat{p} = N/T$ = observed violation rate
- Likelihood Ratio Test:

$$LR_{POF} = -2 \ln \left[\frac{(1-p)^{T-N} p^N}{(1-\hat{p})^{T-N} \hat{p}^N} \right] \\ \sim \chi^2(1)$$

INTERPRETING KUPIEC TEST RESULTS

- Null Hypothesis:
 - H_0 : The model's violation rate equals the expected rate
 - H_1 : The model's violation rate differs from expected
- Decision Rules:
 - Reject H_0 if $LR_{POF} > \chi^2_{1,\alpha}$
 - Typical significance level $\alpha = 0.05$
 - Critical value $\chi^2_{1,0.05} = 3.841$
- Limitations:
 - Only tests violation frequency
 - Ignores clustering of violations
 - Low power for small samples
 - Should be combined with other tests

BACKTESTING RESULTS

- Detailed analysis of VaR model performance:

Metric	95% VaR	99% VaR
Actual Violations	142	69
Expected Violations	187	37
Violation Rate	3.79%	1.84%
Kupiec Test p-value	0.0004	0.0000
Model Rejected	Yes	Yes

- Distribution characteristics:
 - Mean Return: 0.033%
 - Standard Deviation: 1.078%
 - Skewness: -0.783
 - Kurtosis: 12.630
- Key findings:
 - 95% VaR overestimates risk (conservative)
 - 99% VaR underestimates risk (inadequate)
 - Heavy-tailed return distribution
 - Both models rejected by Kupiec test