## AUTO GENERATED INDEX

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composition in 14.5 compositum of K and L in  $\Omega$  in 27.1 computes in 14.10 computes in 14.10 condition (RS) in 16.1 condition (RS) in 5.1 condition  $(RS^*)$  in 18.1 conditions (S1) and (S2) in 10.1 cone  $\pi: C \to S$  over S in 7.2 cone associated to A in 7.1 cone in 9.1cone in 6.1cone in 22.2connected component in 7.1 connected component in 6.26 connected in 16.1 connected in 7.1 connected in 6.26 conormal algebra  $\mathcal{C}_{Z/X,*}$  of Z in X in conormal algebra  $\mathcal{C}_{Z/X,*}$  of Z in X in 6.1 conormal algebra of f in 19.1 conormal algebra of i in 6.1 conormal module in 149.2 conormal sheaf  $C_{Z/X}$  of Z in X in 31.1 conormal sheaf  $C_{Z/X}$  of Z in X in 5.1 conormal sheaf of i in 31.1 conormal sheaf of i in 5.1 conormal sheaf of Z over X in 7.2 conormal sheaf of Z over X in 15.5 conservative in 38.1constant presheaf with value A in 3.2 constant sheaf with value A in 7.4 constant sheaf with value A in 64.1 constant sheaf with value E in 64.1 constant sheaf with value M in 64.1 constant sheaf in 43.1 constant sheaf in 23.1 constant sheaf in 64.1 constant sheaf in 64.1 constant sheaf in 64.1 constructible  $\Lambda$ -sheaf in 28.1 constructible in 15.1 constructible in 71.1 constructible in 71.1 constructible in 71.1 constructible in 27.1

| content ideal of $x$ in 24.1 continuous group cohomology groups in 57.2 continuous in 13.1 contravariant in 3.2 converges to $H^*(K^{\bullet})$ in 24.9 converges to $H^n(Tot(K^{\bullet,\bullet}))$ in 25.2 converges to $H^n(Tot(K^{\bullet,\bullet}))$ in 25.2 coproduct in 5.1 coproduct in 14.7 coregular in 24.7 cosimplicial abelian group in 5.1 cosimplicial object $U$ of $C$ in 5.1 cosimplicial set in 5.1 cotangent complex $L_{X/Y}$ of $X$ over $Y$ in 24.1 cotangent complex $L_{X/Y}$ of $X$ over $Y$ in 26.1 cotangent complex in 3.2 cotangent complex in 18.2 cotangent complex in 20.1 cotangent complex in 22.1 countably indexed in 10.2 coverings of $C$ in 6.2 covering in 3.1 covers $F$ in 15.3 crystal in $\mathcal{O}_{X/S}$ -modules in 11.1 crystal in finite locally free modules in 11.3 crystal in quasi-coherent modules in 11.3 crystalline site in 9.1 curve in 43.1 curve in 67.9 cycle on $X$ in 8.1 cycle on $X$ in 3.1 de $R$ ham complex of $B$ over $A$ in 30.1 de $R$ ham complex of log poles is defined for $Y \subset X$ over $S$ in 15.3 de $R$ ham complex in 30.4 decent in 6.1 decent in 17.1 | Dedekind domain in 120.14 defined in a point $x \in X$ in 49.8 defined in a point $x \in  X $ in 47.4 defines a nodal singularity in 16.2 defines a rational singularity in 19.1 defines a rational singularity in 8.3 deformation category in 16.8 degeneracy of $x$ in 11.1 degenerates at $E_r$ in 20.2 degenerate in 11.1 degree of finite Hilbert stack of $X$ over $Y$ in 18.2 degree of $X$ over $Y$ in 51.8 degree of $X$ over $Y$ in 5.2 degree of $X$ over $Y$ in 5.2 degree of $X$ over $Y$ in 32.1 degree of a zero cycle in 41.1 degree of a zero cycle in 32.1 degree of inseparability in 14.7 degree in 4.1 degree in 4.1 degree in 44.1 degree in 44.1 degree in 46.2 Deligne-Mumford stack in 12.2 depth $x$ at a point in 11.1 depth $x$ at a point in 11.1 depth in 13.1 derived category of $X$ in 12.2 derived category of $X$ in 11.3 derived complete with respect to $X$ in 6.4 derived complete with respect to $X$ in 6.4 derived complete with respect to $X$ in 91.4 derived internal hom in 29.2 derived pullback in 28.2 derived pushforward in 29.2 derived pushforward in 29.2 |
|--|---|
| decent in 6.1  | derived pullback in 28.2  |
| accidenting justination in 10.1  | active velicot product in 11.10   |

derived tensor product in 28.2 dimension of X at x in 9.1 descent datum  $(\mathcal{F}_i, \varphi_{ij})$ dimension of the local ring of  $\mathcal{X}$  at x in quasicoherent sheaves in 2.1 fordescent datum  $(\mathcal{F}_i, \varphi_{ij})$ quasidimension of the local ring of X at x in coherent sheaves in 3.1 10.2dimension of the local ring of the fibre of descent datum  $(N,\varphi)$  for modules with respect to  $R \to A$  in 3.1 f at x in 33.1 descent datum  $(V_i, \varphi_{ij})$  relative to the dimension in 10.1 family  $\{X_i \to S\}$  in 34.3 dimension in 10.1 descent datum  $(V_i, \varphi_{ij})$  relative to the dimension in 9.2family  $\{X_i \to X\}$  in 22.3 dimension in 12.3 descent datum  $(X_i, \varphi_{ij})$  in S relative to direct image functor in 25.1 the family  $\{f_i: U_i \to U\}$  in 3.1 direct image functor in 19.1 descent datum for V/X/S in 34.1 direct image with compact support in 3.3 descent datum for V/Y/X in 22.1 direct image with compact support in 4.4  $descent\ datum\ relative\ to\ X \to S\ \text{in}\ 34.1$ direct image in 35.1 descent datum relative to  $Y \to X$  in 22.1 direct image in 35.3 descent datum in 16.1 direct sum dévissage in 84.1 descent datum in 16.5 direct sum in 3.5 descent morphism for modules in 4.15 directed inverse system in 21.4 determinant of  $(M, \varphi, \psi)$  in 68.13 directed partially ordered set in 21.1 determinant of the finite length Rdirected set in 21.1  $module\ M$  in 68.2directed set in 2.1 differential  $d\varphi: T\mathcal{F} \to T\mathcal{G}$  of  $\varphi$  in 12.3 directed system in 21.4 differential graded (A, B)-bimodule in directed system in 8.1 17.1 directed in 19.1 differential graded (A, B)-bimodule in directed in 19.1 28.1  $discrete\ G$ - $module\ in\ 57.1$ differential graded A-module in 13.1  $discrete\ G$ -set in 2.1 differential graded algebra over R in 3.1 discrete valuation ring in 50.13 differential graded category A over R in discrete in 38.126.1 discriminant of L/K in 20.8 distance between M and M' in 121.5 differential graded direct sum in 26.4 differential graded module in 4.1 distinguished triangle of K(A) in 10.1 differential graded module in 13.1 distinguished triangles in 3.2 differential object in 22.1 distinguished triangle in 8.2 differential operator  $D: \mathcal{F} \to \mathcal{G}$  of order divided power A-derivation in 6.1 k in 29.1divided power envelope of J in B relative differential operator  $D: \mathcal{F} \to \mathcal{G}$  of order to  $(A, I, \gamma)$  in 2.2 k in 34.1divided power ring in 3.1 differential operator  $D: M \to N$  of ordivided power scheme in 7.2 der k in 133.1 divided power structure  $\gamma$  in 7.1 differential operator of order k on X/Sdivided power structure in 2.1 in 29.8 divided power structure in 6.1 different in 9.1 divided power thickening of X relative to dimension function in 20.1 $(S, \mathcal{I}, \gamma)$  in 8.1 dimension of  $\mathcal{X}$  at x in 12.2 divided power thickening in 5.2 dimension of X at x in 10.1 divided power thickening in 7.3

| D16   |  |
|---|--|
| DM over $S$ in $4.2$  | embedded associated point in 4.1   |
| DM  in  4.1   | embedded associated primes in 67.1   |
| DM  in  4.2   | embedded component in 4.1  |
| domain of definition in 49.8                                  | embedded point in 4.1  |
| domain of definition in 47.4                                  | embedded primes of $R$ in 67.1   |
| domain in 2.2   | embedding dimension of $X$ at $x$ in 46.1  |
| dominant in 8.1   | embedding dimension of $X/k$ at $x$ in 46.2  |
| dominant in 49.10   | embedding in 43.1  |
| dominant in 18.1  | enough P objects in 40.2   |
| dominant in 47.6  | enough injectives in 27.4  |
| dominates in 50.1   | enough projectives in 28.4   |
| dominates in 88.2   | enough weakly contractible objects in  |
| dotted arrow in 39.1  | 40.2   |
| double complex in 18.1  | envelope in 22.1   |
| dual numbers in 16.1  | epimorphism in 13.1  |
| dual numbers in 35.1  | equalizer in 10.1  |
| dualizing complex normalized relative to                      | equidimensional in 10.5  |
| $\omega_{\bullet}^{\bullet}$ in 20.5                          | equidimensional in 7.1   |
| dualizing complex in 15.1<br>dualizing complex in 2.2         | equivalence of categories in $2.17$<br>equivalence relation on $U$ over $B$ in $4.1$ |
| 0 1   | equivalence relation on $U$ over $S$ in 3.1  |
| dualizing complex in 2.2<br>effective Cartier divisor in 13.1 | equivalent types in 3.2  |
| effective Cartier divisor in 6.1                              | equivalent in 29.4   |
| effective Cartier divisor in 49.1                             | equivalent in 27.4   |
| effective descent morphism for modules                        | equivalent in 49.1   |
| in 4.15   | equivalent in 61.3   |
| effective epimorphism in 12.1                                 | equivalent in 47.1   |
| effective in 3.5  | equivariant quasi-coherent $\mathcal{O}_X$ -module                                   |
| effective in 2.3  | in 12.1  |
| effective in 3.4  | equivariant quasi-coherent $\mathcal{O}_X$ -module                                   |
| effective in 34.10  | in 10.1  |
| effective in 34.11  | equivariant in 10.1  |
| effective in 8.4  | equivariant in 8.1   |
| effective in 16.1   | essential extension of in 2.1  |
| effective in 16.6   | essential surjection in 3.9  |
| effective in 8.1  | essentially constant inverse system in   |
| effective in 3.3  | 22.2   |
| effective in 22.10  | essentially constant system in 22.2  |
| effective in 22.11  | essentially constant in 22.1   |
| effective in 9.4  | essentially constant in 22.1   |
| Eilenberg-Maclane object $K(A, k)$ in 22.3                    | essentially of finite presentation in 54.1   |
| elementary étale localization of the ring                     | essentially of finite type in 54.1   |
| $map R \to S \ at \ \mathfrak{q} \ \text{in } 6.1$            | essentially surjective in 2.9  |
| elementary étale neighbourhood in 35.1                        | essential in 2.1   |
| elementary étale neighbourhood in 11.5                        | essential in 2.1   |
| elementary distinguished square in 9.1                        | Euler characteristic of $\mathcal{F}$ in 33.1  |
| elementary divisor domain in 124.5                            | Euler characteristic of $\mathcal{F}$ in 17.1  |
| elementary standard in A over $R$ in 2.3                      | Euler-Poincaré function in 26.2  |

| everywhere defined in 14.9  | family of morphisms with fixed target in                |
|---|---|
| everywhere defined in 14.9  | 10.1  |
| $exact \ at \ x_i \ in \ 5.7$   | fibre category in 32.2                                  |
| $exact \ at \ y \ in \ 5.7$   | fibre of $f$ over $s$ in $18.4$                         |
| $exact\ complex\ in\ 5.7$   | fibre product of $V$ and $W$ over $U$ in 7.1            |
| exact couple in 21.1  | fibre product of $V$ and $W$ over $U$ in 10.1           |
| exact functor in 3.3  | fibre product in 6.1                                    |
| exact sequences of graded modules in 26.3                               | fibre product in 17.1                                   |
| exact sequence in 5.7   | fibred category over $C$ in 33.5                        |
| $exact 	ext{ in } 23.1$   | fibred in groupoids in 35.1                             |
| exact in 5.7  | fibres of f are universally bounded in                  |
| exact in 2.1  | 57.1  |
| excellent in 52.1   | fibres of $f$ are universally bounded in 3.1            |
| exceptional divisor in 32.1   | field extension in 6.2                                  |
| exceptional divisor in 17.1   | field of rational functions in 49.6                     |
| exhaustive in 19.1  | field of rational functions in 4.3                      |
| existence part of the valuative criterion                               | field in 2.1  |
| in 39.10  | filtered acyclic in 13.2                                |
| extends in 4.1  | filtered acyclic in 30.7                                |
| extension $E$ of $B$ by $A$ in $6.1$                                    | filtered complex $K^{\bullet}$ of $\mathcal{A}$ in 24.1 |
| extension $j_!\mathcal{F}$ of $\mathcal{F}$ by 0 in 31.5                | filtered derived category of $A$ in 13.5                |
| extension $j_!\mathcal{F}$ of $\mathcal{F}$ by e in 31.5                | filtered derived functor in 8.1                         |
| extension $j_p!\mathcal{F}$ of $\mathcal{F}$ by 0 in 31.5               | filtered differential object in 23.1                    |
| extension $j_p!\mathcal{F}$ of $\mathcal{F}$ by $e$ in 31.5             | filtered injective in 26.1                              |
| extension by 0 in 31.5  | filtered injective in 7.1                               |
| extension by 0 in 31.5  | filtered injective in 30.3                              |
| extension by zero in 19.1   | filtered object of $A$ in 19.1                          |
| extension by zero in 70.1   | filtered quasi-isomorphism in 13.2                      |
| extension by zero in 70.1   | filtered quasi-isomorphism in 7.1                       |
| extension by zero in 26.1   | filtered quasi-isomorphism in 30.6                      |
| extension by zero in 26.1   | filtered in 19.1  |
| extension of $\mathcal{F}$ by the empty set $j_!\mathcal{F}$ in         | filtered in 19.1  |
| 31.3  | final object in 31.1                                    |
|   | final in 12.1   |
| extension of $\mathcal{F}$ by the empty set $j_{p!}\mathcal{F}$ in 31.3 | · ·   |
|   | finer in 47.8   |
| extension of $\mathcal{G}$ by the empty set in 25.1                     | finite Tor-dimension in 12.1                            |
| extension of discrete valuation rings in                                | finite R-module in 5.1                                  |
| 111.1   | finite free in 17.1                                     |
| extension of valuation rings in 123.1                                   | finite global dimension in 109.10                       |
| extremally disconnected in 26.1   | finite injective dimension in 69.1                      |
| face of x in 11.1   | finite locally constant in 43.1                         |
| faithfully flat in 39.1   | finite locally constant in 64.1                         |
| faithfully flat in 39.1   | finite locally constant in 64.1                         |
| faithfully flat in 9.1  | finite locally free of rank r in 78.1                   |
| faithfully flat in 9.3  | finite locally free of rank r in 14.1                   |
| faithful in 2.9   | finite locally free in 78.1                             |
| family of morphisms with fixed target in                                | finite locally free in 14.1                             |
| 6.1   | finite locally free in 23.1                             |

| finite locally free in 48.1                | flat at $x$ over $Y$ in $31.2$                                |
|--|---|
| finite locally free in 46.2                | flat at $x$ in 17.3   |
| finite locally free in 22.1                | flat at $x$ in 20.1   |
| finite presentation at $x \in X$ in 21.1   | flat at $x$ in $30.1$   |
| finite presentation at $x$ in 28.1         | $flat \ at \ x \ in \ 26.2$                                   |
| finite presentation in 6.1                 | flat at a point $x \in X$ in 25.1                             |
| finite presentation in 11.1                | flat base change property in 7.1                              |
| finite presentation in 21.1                | flat base change in 3.4                                       |
| finite presentation in 2.8                 | flat group scheme in 4.5                                      |
| finite projective dimension in 109.2       | $flat\ local\ complete\ intersection\ over\ R$ in             |
| finite projective dimension in 68.1        | 136.1   |
| finite tor dimension in 66.1               | flat over $(Sh(\mathcal{D}), \mathcal{O}')$ in 31.3           |
| finite tor dimension in 66.1               | flat over $S$ at a point $x \in X$ in 25.1                    |
| finite tor dimension in 48.1               | flat over $S$ in 25.1   |
| finite tor dimension in 46.1               | flat over $Y$ at $x \in X$ in 9.3                             |
| finite type at $x \in X$ in 15.1           | flat over Y at a point $x \in X$ in 20.3                      |
| finite type at $x$ in 23.1                 | flat over Y in 20.3   |
| finite type point in 16.3                  | flat over Y in 31.2   |
| finite type point in 25.2                  | flat pullback of $\alpha$ by $f$ in 14.1                      |
| finite type point in 18.2                  | flat pullback of $\alpha$ by $f$ in 10.1                      |
| finite type in 6.1                         | flat-fppf site in 14.1  |
| finite type in 9.1                         | flattening stratification in 21.3                             |
| finite type in 15.1                        | flattening stratification in 21.3                             |
| finite type in 24.1                        | flat in 39.1  |
| finitely generated R-module in 5.1         | flat in 39.1  |
| finitely generated field extension in 6.6  | flat  in  17.1  |
| finitely presented R-module in 5.1         | flat  in  20.1  |
| finitely presented relative to R in 80.2   | flat  in  28.1  |
| finitely presented relative to S in 58.1   | flat  in  28.1  |
| finite in 7.1                              | flat  in  28.1  |
| finite in 7.1                              | flat  in  28.1  |
| finite in 2.1                              | flat in 31.1  |
| finite in 19.1                             | flat  in  31.1  |
| finite in 44.1                             | flat  in  25.1  |
| finite in 45.2                             | flat  in  9.1   |
| finite in 10.1                             | flat  in  9.3   |
| first Chern class in 34.4                  | flat  in  30.1  |
| first order infinitesimal neighbourhood in | flat  in  13.4  |
| 5.1  | flat  in  25.1  |
| first order infinitesimal neighbourhood in | formal algebraic space in 11.1                                |
| 12.1                                       | formal branches of $\mathcal{X}$ through $x_0$ in 4.1         |
| first order thickening in 2.1              | formal modification in 24.1                                   |
| first order thickening in 9.1              | formal object $\xi = (R, \xi_n, f_n)$ of $\mathcal{F}$ in 7.1 |
| first order thickening in 3.3              | formal object in 9.1  |
| flabby in 12.1                             | formal spectrum in 9.9  |
| flasque in 12.1                            | formally étale over $R$ in 150.1                              |
| flat (resp. faithfully flat) in 9.1        | formally étale in 8.1   |
| flat at $x \in X$ in 9.3                   | formally étale in 13.1  |
|  |   |

formally étale in 16.1 formally catenary in 109.1 formally principally homogeneous under G in 11.1 formally principally homogeneous under G in 9.1formally smooth for the n-adic topology in 37.3 formally smooth over R in 138.1 formally smooth over R in 37.1 formally smooth in 11.1 formally smooth in 13.1 formally smooth in 19.1 formally smooth in 8.1 formally unramified over R in 148.1 formally unramified in 6.1 formally unramified in 13.1 formally unramified in 14.1 Fourier-Mukai functor in 8.1 Fourier-Mukai kernel in 8.1 fppf covering of T in 7.1 fppf covering of X in 7.1 fppf sheaf in 4.3fpqc covering of T in 9.1 fpqc covering of X in 9.1 fpqc covering in 15.1 free  $\mathcal{O}$ -module in 17.1 free abelian presheaf on  $\mathcal{G}$  in 18.4 free abelian presheaf in 4.1 free abelian sheaf in 5.1 free module in 55.5 free in 10.2free in 8.2 full subcategory in 2.10 fully faithful in 2.9 function field in 49.6 function field in 4.3 functor of R-linear categories in 24.2 functor of differential graded categories over R in 26.2 functor of graded categories over R in 25.2 functor of monoidal categories in 43.2 functor of symmetric monoidal categories in 43.11 functorial injective embeddings in 27.5 functorial projective surjections in 28.5 functor in 2.8

functor in 29.5 fundamental group in 6.1 G-ring in 50.1G-unramified at  $\mathfrak{q}$  in 151.1 G-unramified at  $x \in X$  in 35.1 G-unramified at x in 38.1G-unramified in 151.1 G-unramified in 35.1 G-unramified in 38.1 Galois category in 3.6 Galois cohomology groups of K with coefficients in M in 57.2 Galois cohomology groups in 57.2 Galois group in 21.3 Galois in 21.1 Galois in 28.1generalizations lift along f in 19.4 generalization in 19.1 generalization in 6.22 generalizing in 19.4 generated by r global sections in 17.1 generated by finitely many global sections in 17.1 generated by global sections in 4.1 generated by global sections in 17.1 generates the field extension in 6.6 generate in 4.1 generator in 36.3 generator in 10.1generic point in 8.6 generic point in 6.12 qenus in 6.3 genus in 8.1 geometric frobenius in 3.4 geometric frobenius in 3.10 geometric genus in 11.1 geometric point lying over x in 19.1 geometric point in 29.1 geometric point in 19.1 geometric quotient in 10.1 geometrically connected over k in 48.3 geometrically connected in 7.1 geometrically connected in 12.1 geometrically integral over k in 49.1 geometrically integral in 9.1 geometrically integral in 14.1 geometrically irreducible over k in 47.4 geometrically irreducible in 8.1

|  | 1.1/4.70                                  |
|--|---|
| geometrically irreducible in 13.1                    | graded(A, B)-bimodule in 28.1             |
| geometrically normal at $x$ in 10.1                  | graded A-module in 4.1                    |
| geometrically normal in 165.2                        | graded A-algebra in 26.3                  |
| geometrically normal in 10.1                         | graded category $A$ over $R$ in 25.1      |
| geometrically pointwise integral at x in             | graded direct sum in 25.4                 |
| 9.1  | graded functor in 25.2                    |
| geometrically pointwise integral in 9.1              | graded ideals in 26.3                     |
| geometrically reduced at $x$ in 6.1                  | graded injective in 25.2                  |
| geometrically reduced at $x$ in 11.1                 | graded module M over a graded A-          |
| geometrically reduced over $k$ in 43.1               | algebra B in 26.3                         |
| geometrically reduced in 6.1                         | graded module in 4.1                      |
| geometrically reduced in 11.1                        | graded module in 26.2                     |
| geometrically regular at $x$ in 12.1                 | graded submodules in 26.3                 |
| geometrically regular over $k$ in 12.1               | $Grassmannian over \mathbf{Z}$ in 22.2    |
| geometrically regular in 166.2                       | Grassmannian over R in 22.2               |
| geometrically unibranch at x in 15.1                 | Grassmannian over S in 22.2               |
| geometrically unibranch at $x$ in 23.2               | Grothendieck abelian category in 10.1     |
| geometrically unibranch at $x$ in 13.1               | Grothendieck group of $X$ in $38.2$       |
| geometrically unibranch in 106.1                     | Grothendieck group of coherent sheaves    |
| geometrically unibranch in 15.1                      | on $X$ in $38.2$                          |
| geometrically unibranch in 23.2                      | group algebraic space over B in 5.1       |
| gerbe over in 11.4                                   | group cohomology groups in 57.2           |
| gerbe over in 28.1                                   | group of infinitesimal automorphisms of   |
| gerbe in 11.1  | x' over $x$ in 19.1                       |
| gerbe in 28.1  | group of infinitesimal automorphisms of   |
| germ of $X$ at $x$ in 20.1                           | $x_0$ in 19.2                             |
| global complete intersection over $k$ in             | group scheme over $S$ in 4.1              |
| 135.1  | groupoid in algebraic spaces over B in    |
| global dimension in 109.10                           | 11.1                                      |
| global finite presentation in 17.1                   | groupoid in functors on $C$ in 21.1       |
| global Lefschetz number in 14.1                      | groupoid over $S$ in 13.1                 |
| global presentation in 17.1                          | groupoid scheme over $S$ in 13.1          |
| global sections in 45.1                              | groupoid in 2.5                           |
| going down in 41.1                                   | Gysin homomorphism in 29.1                |
| going up in 41.1                                     | Gysin homomorphism in 22.1                |
| going up in 41.1<br>going-down theorem in 24.1       |   |
| going-up theorem in 24.1                             | gysin map in 59.4                         |
| 0 0 1  | h covering of T in 34.2                   |
| good quotient in 9.1                                 | H-projective in 43.1                      |
| good reduction in 14.8                               | H-quasi-projective in 40.1                |
| good stratification in 28.2                          | has coproducts of pairs of objects in 5.2 |
| Gorenstein at x in 25.2                              | has enough points in 38.1                 |
| Gorenstein at x in 27.2                              | has fibre products in 6.3                 |
| Gorenstein morphism in 25.2                          | has products of pairs of objects in 4.2   |
| Gorenstein morphism in 27.2                          | has property $(\beta)$ in 17.1            |
| Gorenstein in 21.1                                   | has property $(\beta)$ in 17.1            |
| Gorenstein in 21.1                                   | has property $\mathcal{P}$ at $x$ in 7.5  |
| Gorenstein in 24.1                                   | has property $\mathcal{P}$ at $x$ in 7.5  |
| graded $(\mathcal{A}, \mathcal{B})$ -bimodule in 8.1 | has property $\mathcal{P}$ in 7.2         |
|  |   |

has property  $\mathcal{P}$  in 22.2 homomorphism of graded A-modules in has property  $\mathcal{P}$  in 7.2 has property  $\mathcal{P}$  in 16.2 has property  $\mathcal{P}$  in 34.2 has property Q at x in 22.6 Hausdorff in 6.6 height in 60.330.1 henselian local ring of X at x in 11.7 henselian pair in 11.1 30.10 henselian in 153.1 henselian in 32.2henselization of  $\mathcal{O}_{S,s}$  in 33.2 henselization of S at s in 33.230.7 henselization in 155.3 higher direct images in 35.4 36.1  $Hilbert\ function\ in\ 26.2$ Hilbert polynomial in 59.6 Hilbert polynomial in 35.15 Hilbert polynomial in 26.2 Hodge filtration in 7.1 homogeneous spectrum Proj(R) in 27.2 homogeneous spectrum of A over S in 16.7 homogeneous spectrum of A over X in 11.3 homogeneous spectrum in 57.1 homogeneous spectrum in 8.3 homogeneous in 27.1 homological in 3.5 homology of K in 4.1 homology in 22.3 homomorphism of differential graded  $(\mathcal{A}, \mathcal{B})$ -bimodules in 17.1 homomorphism of differential graded Amodules in 13.1homomorphism of differential graded Oalgebras in 12.1homomorphism of differential graded algebras in 3.2 homomorphism of differential graded modules in 4.1homomorphism of divided power rings in homomorphism of divided power thickenings in 5.2 homomorphismgraded $(\mathcal{A},\mathcal{B})$ bimodules in 8.1

homomorphism of graded O-algebras in homomorphism of systems in 8.6 homomorphism of topological groups in homomorphism of topological modules in homomorphism of topological modules in homomorphism of topological rings in homomorphism of topological rings in gradedhomomorphismsmodules/rings in 26.3 homotopic in 26.1 homotopic in 28.1 homotopic in 5.1 homotopic in 21.1 homotopy between f and g in 5.1homotopy between f and g in 21.1 homotopy category of A in 26.3 homotopy category in 5.3 homotopy category in 21.2 homotopy colimit in 33.1 homotopy equivalence in 13.2 homotopy equivalence in 13.8 homotopy equivalence in 26.6 homotopy equivalent in 13.2 homotopy equivalent in 13.8 homotopy equivalent in 26.6 homotopy from a to b in 26.1 homotopy from a to b in 28.1 homotopy limit in 34.1 horizontal in 28.1 horizontal in 29.1 hypercovering of  $\mathcal{G}$  in 6.1 hypercovering of X in 3.3 hypercovering in 6.1 ideal of definition in 36.1ideal sheaf of denominators of s in 23.10 identifies local rings in 3.1 image of  $\varphi$  in 3.5 image of f in 3.9 image of the short exact sequence under the given  $\delta$ -functor in 3.6

| . 1  |   |
|--|---|
| immediate specialization in 20.1   | interior in 21.1                                      |
| immersion in 10.2  | intersect properly in 13.5                            |
| immersion in 12.1  | intersect properly in 13.5                            |
| immersion in 9.1   | intersection number in 45.3                           |
| impurity of $\mathcal{F}$ above $s$ in 15.2                                  | intersection number in 18.3                           |
| impurity of $\mathcal{F}$ above $y$ in 2.2                                   | intersection with the jth Chern class of              |
| in the same homotopy class in 26.1   | $\mathcal{E}$ in 38.1                                 |
| in the same homotopy class in 28.1   | intersection with the first Chern class of            |
| ind-étale in 7.1   | $\mathcal{L}$ in 25.1                                 |
| ind-quasi-affine in 66.1   | intersection with the first Chern class of            |
| ind-quasi-affine in 66.1   | $\mathcal{L}$ in 18.1                                 |
| ind- $Zariski$ in 4.1  | inverse image $f^{-1}(Z)$ of the closed sub-          |
| indecomposable in 5.5  | $scheme\ Z\ in\ 17.7$                                 |
| induced filtration in 19.1   | inverse image $f^{-1}(Z)$ of the closed sub-          |
| induced filtration in 23.4   | space Z in 13.2                                       |
| induced filtration in 24.5   | inverse image in 36.1                                 |
| inductive system over I in $C$ in 21.2                                       | inverse system over $I$ in $C$ in $21.2$              |
| inertia fibred category $\mathcal{I}_{\mathcal{S}}$ of $\mathcal{S}$ in 34.2 | invertible $\mathcal{O}_X$ -module in 25.1            |
| inertia group of $\mathfrak{m}$ in 112.3                                     | invertible $\mathcal{O}_X$ -module in 40.1            |
| initial in 12.1  | invertible module $M$ in $40.4$                       |
| initial in 17.3  | invertible module in 22.1                             |
| injective hull in 5.1  | invertible sheaf $\mathcal{O}_S(D)$ associated to $D$ |
| injective resolution of $A$ in 18.1  | in 14.1   |
| injective resolution of $K^{\bullet}$ in 18.1                                | invertible sheaf $\mathcal{O}_X(D)$ associated to $D$ |
| injective-amplitude in $[a,b]$ in 69.1                                       | in 7.1  |
| injective in 16.2  | invertible in 43.4                                    |
| injective in 16.2  | invertible in 117.1                                   |
| injective in 3.1   | invertible in 32.1                                    |
| injective in 11.1  | irreducible component in 8.1                          |
| injective in 5.3   | irreducible component in 6.18                         |
| injective in 27.1  | irreducible in 8.1                                    |
| injective in 55.1  | irreducible in 120.1                                  |
| inseparable degree in 14.7   | irreducible in 6.9                                    |
| integral closure of $\mathcal{O}_X$ in $\mathcal{A}$ in 53.2                 | irreducible in 6.9                                    |
| integral closure of $\mathcal{O}_X$ in $\mathcal{A}$ in 48.2                 | isolated point in 27.2                                |
| integral closure in 36.9   | isomorphism in 2.4                                    |
| integral domain in 2.2   | J-0  in  47.1   |
| $integral\ over\ I\ in\ 38.1$  | J-1  in  47.1   |
| integral over $R$ in $36.1$  | J-2  in  47.1   |
| integrally closed in 36.9  | J-2 in 19.1   |
| integral in 36.1   | $Jacobson\ ring\ in\ 35.1$                            |
| integral in 3.1  | Jacobson in 18.1                                      |
| integral in 44.1   | Jacobson in 6.1                                       |
| integral in 45.2   | Japanese in 161.1                                     |
| integral in 4.1  | Japanese in 13.1                                      |
| integral in 10.1   | K-flat in 59.1  |
| integral in $50.1$   | K-flat in 26.2  |
| integral in 33.12  | K-flat in 17.2  |
|  |   |

| K-injective in 31.1                             | lies over in 29.1                                  |
|---|--|
| K-injective in 25.7                             | lies over in 9.1                                   |
| Kähler different in 7.1                         | lift of $x$ along $f$ in 17.1                      |
| Kan complex in 31.1                             | lift in 32.2                                       |
| Kan fibration in 31.1                           | lift in 32.2                                       |
| Kaplansky dévissage in 84.1                     | limit preserving in 3.1                            |
| Karoubian in 4.1                                | limit preserving in 3.1                            |
| kernel of $F$ in 6.5                            | limit preserving in 11.1                           |
| kernel of $H$ in 6.5                            |  |
| · · · · · · · · · · · · · · · · · · ·           | limit preserving in 3.1<br>limit in 14.1           |
| kernel of the functor $F$ in 10.5 kernel in 3.9 | limit in 20.2                                      |
| Kolmogorov in 8.6                               |  |
| Koszul at $x$ in 62.2                           | linear series of degree d and dimension            |
|   | r in 3.1   |
| Koszul at x in 48.1                             | linearly adequate in 3.2                           |
| Koszul complex on $f_1, \ldots, f_r$ in 28.2    | linearly disjoint over $k$ in $\Omega$ in 27.2     |
| Koszul complex on $f_1, \ldots, f_r$ in 24.2    | linearly topologized in 36.1                       |
| Koszul complex in 28.1                          | linearly topologized in 36.1                       |
| Koszul complex in 24.1                          | lisse-étale site in 14.1                           |
| Koszul morphism in 62.2                         | lisse in 28.1                                      |
| Koszul morphism in 48.1                         | lisse in 18.1                                      |
| Koszul-regular ideal in 32.1                    | local complete intersection morphism in            |
| Koszul-regular immersion in 21.1                | 62.2   |
| Koszul-regular immersion in 44.2                | local complete intersection morphism in            |
| Koszul-regular in 30.1                          | 48.1   |
| Koszul-regular in 20.2                          | local complete intersection morphism in            |
| Koszul in 44.1                                  | 44.1   |
| Krull dimension of $X$ at $x$ in 10.1           | $local \ complete \ intersection \ over \ k \ in$  |
| Krull dimension in 10.1                         | 135.1  |
| Krull dimension in 60.2                         | local complete intersection over $k$ in 30.1       |
| lattice in V in 121.3                           | local complete intersection in 33.2                |
| left acyclic for $F$ in 15.3                    | local complete intersection in 8.5                 |
| left adjoint in 24.1                            | local homomorphism of local rings in 18.1          |
| left admissible in 40.9                         | local in the $\tau$ -topology in 15.1              |
| left derivable in 14.9                          | local isomorphism in 3.1                           |
| left derived functor LF is defined at in        | local Lefschetz number in 14.2                     |
| 14.2  | local on the base for the $\tau$ -topology in      |
| left derived functors of $F$ in 15.3            | 22.1   |
| $left \ dual \ in \ 43.5$                       | local on the base for the $\tau$ -topology in      |
| $left\ exact\ in\ 23.1$                         | 10.1   |
| left multiplicative system in 27.1              | local on the source for the $\tau$ -topology in    |
| $left\ orthogonal\ in\ 40.1$                    | 26.1   |
| Leibniz rule in 131.1                           | local on the source for the $\tau$ -topology in    |
| Leibniz rule in 28.1                            | 14.1   |
| Leibniz rule in 33.1                            | local ring map $\varphi: R \to S$ in 18.1          |
| length in $10.1$                                | local ring of $X$ at $x$ in $2.1$                  |
| length in $52.1$                                | local ring of the fibre at $\mathfrak{q}$ in 112.5 |
| length in $60.1$                                | local ring in 18.1                                 |
| length in 9.1                                   | $localization\ morphism\ in\ 25.1$                 |
|   |  |

| localization morphism in 30.4                                   | locally Noetherian in 36.5                                       |
|---|--|
| localization morphism in 19.1                                   | locally of finite presentation over $S$ in $3.1$                 |
| localization morphism in 21.2                                   | locally of finite presentation in 21.1                           |
| localization of A with respect to S in 9.2                      | locally of finite presentation in 28.1                           |
| localization of the ringed site $(C, O)$ at                     | locally of finite presentation in 3.1                            |
| the object $U$ in 19.1  | locally of finite presentation in 3.1                            |
| localization of the ringed topos                                | locally of finite presentation in 27.1                           |
| $(Sh(\mathcal{C}), \mathcal{O})$ at $\mathcal{F}$ in 21.2       | locally of finite type in 15.1                                   |
| localization of the site C at the object U                      |  |
| in 25.1   | locally of finite type in 23.1<br>locally of finite type in 24.1 |
| localization of the topos $Sh(\mathcal{C})$ at $\mathcal{F}$ in | locally of finite type in 17.1                                   |
| 30.4  | locally of type P in 14.2  |
| localization in 9.6   | locally principal closed subscheme in 13.1                       |
| localized pth Chern class in 50.3                               | locally principal closed subspace in 6.1                         |
| localized Chern character in 50.3                               | locally projective in 21.1                                       |
| locally P in 4.2  | locally projective in 43.1                                       |
| locally acyclic at $\overline{x}$ relative to $K$ in 93.1       | locally projective in 31.2                                       |
| locally acyclic relative to $K$ in 93.1                         | locally quasi-coherent in 11.1                                   |
| locally acyclic in 93.1   | locally quasi-coherent in 12.1                                   |
| $locally\ adic^*$ in 20.7                                       | locally quasi-compact in 13.1                                    |
| locally algebraic $k$ -scheme in 20.1                           | locally quasi-finite in 20.1                                     |
| locally closed immersion in $10.2$                              | locally quasi-finite in 27.1                                     |
| locally closed subspace in 12.1                                 | locally quasi-finite in 23.2                                     |
| locally closed substack in 9.9                                  | locally quasi-projective in 40.1                                 |
| locally connected in 7.10                                       | locally ringed site in 40.4                                      |
| locally constant in 43.1  | locally ringed space $(X, \mathcal{O}_X)$ in 2.1                 |
| locally constant in 64.1  | locally ringed in 40.6   |
| locally constant in 64.1  | locally separated over $S$ in 13.2                               |
| locally constant in 64.1  | locally separated in 3.1   |
| locally constructible in 15.1                                   | locally separated in 3.1   |
| locally countably indexed and classical in                      | locally separated in 4.2   |
| 20.7  | locally trivial in 11.3  |
| locally countably indexed in 20.7                               | locally trivial in 9.3   |
| locally finite in 28.4  | locally weakly adic in 20.7                                      |
| locally finite in 24.2  | local in 4.1   |
| locally finite in 26.2  | local in 14.1  |
| locally free in 78.1  | maximal Cohen-Macaulay in 103.8                                  |
| locally free in 14.1  | McQuillan  in  9.7   |
| locally free in 23.1  | meromorphic function in 23.1                                     |
| locally generated by $r$ sections in 23.1                       | meromorphic function in 10.1                                     |
| locally generated by sections in 8.1                            | meromorphic section of $\mathcal{F}$ in 23.3                     |
| locally generated by sections in 23.1                           | meromorphic section of $\mathcal{F}$ in 10.3                     |
| locally has finite tor dimension in 48.1                        | minimal model in 8.4   |
| locally has finite tor dimension in 46.1                        | minimal polynomial in 9.1  |
| locally nilpotent in 32.1                                       | minimal in 3.12  |
| locally Noetherian in 9.1                                       | minimal in 14.4  |
| locally Noetherian in 5.1                                       | minimal in 27.1  |
| locally Noetherian in 20.7                                      | miniversal in 14.4   |

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Mittag-Leffler condition in 31.2
Mittag-Leffler directed system of mod-
ules in 88.1
Mittag-Leffler in 86.1
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module of principal parts of order k in
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16.4
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moduli stack of stable curves in 22.4
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jects in 19.1
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morphism (U, R, s, t, c) \rightarrow (U', R', s', t', c') morphism from U to V in 8.1
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morphism \psi: (\mathcal{F}_i, \varphi_{ij}) \to (\mathcal{F}'_i, \varphi'_{ij}) of
descent data in 2.1
morphism \psi: (\mathcal{F}_i, \varphi_{ij}) \to (\mathcal{F}'_i, \varphi'_{ij}) of
descent data in 3.1
morphism \psi : (G,m) \rightarrow (G',m') of
group algebraic spaces over B in 5.1
morphism \psi : (G,m) \rightarrow (G',m') of
group schemes over S in 4.1
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morphism \psi: (V_i, \varphi_{ij}) \to (V'_i, \varphi'_{ij}) of de-
scent data in 34.3
morphism \psi: (V_i, \varphi_{ij}) \to (V'_i, \varphi'_{ij}) of de-
scent data in 22.3
morphism \psi: (X_i, \varphi_{ij}) \to (X'_i, \varphi'_{ij}) of
descent data in 3.1
morphism \varphi: \mathcal{F} \to \mathcal{G} of presheaves of
\mathcal{O}-modules on \mathcal{B} in 30.11
morphism \varphi: \mathcal{F} \to \mathcal{G} of presheaves of
\mathcal{O}-modules in 6.1
morphism \varphi: \mathcal{F} \to \mathcal{G} of presheaves of
\mathcal{O}-modules in 9.1
morphism \varphi: \mathcal{F} \to \mathcal{G} of presheaves of
sets on \mathcal{B} in 30.1
morphism \varphi: \mathcal{F} \to \mathcal{G} of presheaves of
sets \ on \ X \ in \ 3.1
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value in C in 5.1
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morphism a: \xi \to \eta of formal objects in
morphism f
                           (U,R,s,t,c)
(U', R', s', t', c') of groupoid schemes
over S in 13.1
morphism f
                           (U,R,s,t,c)
(U', R', s', t', c') of groupoids in algebraic
spaces over B in 11.1
morphism f:(V/X,\varphi)\to (V'/X,\varphi') of
descent data relative to X \to S in 34.1
morphism f: (V/Y, \varphi) \to (V'/Y, \varphi') of
descent data relative to Y \to X in 22.1
morphism f: F \to F' of algebraic spaces
over S in 6.3
morphism f: p \to p' in 37.2
morphism f: X \to Y of schemes over S
in 18.1
morphism of \delta-functors from F to G in
12.2
morphism of G-torsors in 4.1
morphism of \mathcal{G}-torsors in 4.1
morphism of G-modules in 57.1
morphism of G-sets in 2.1
morphism of n-truncated simplicial ob-
jects in 12.1
morphism of R-G-modules in 57.1
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morphism of étale neighborhoods in 19.2 morphism of sheaves of  $\mathcal{O}$ -modules in morphism of étale neighbourhoods in 35.1 morphism of abelian presheaves over Xin 4.4 morphism of affine formal algebraic spaces in 9.1morphism of affine schemes in 5.5 morphism of cones in 7.2 morphism of cosimplicial objects  $U \rightarrow$ U' in 5.1 morphism of differential objects in 22.1 morphism of divided power schemes in morphism of divided power thickenings of X relative to  $(S, \mathcal{I}, \gamma)$  in 8.1 morphism of dotted arrows in 44.1 morphism of dotted arrows in 39.1 morphism of elementary étale neighbourhoods in 11.5 morphism of exact couples in 21.1 morphism of extensions in 6.1 morphism of families of maps with fixed target of  $\mathcal{C}$  from  $\mathcal{U}$  to  $\mathcal{V}$  in 8.1 morphism of formal algebraic spaces in  $\tau$ -coverings in 36.1 11.1 morphism in 2.2morphism of formal objects in 9.1 morphism in 18.1 morphism of functors in 2.15 morphism of germs in 20.1 morphism of groupoid schemes cartesian over (U, R, s, t, c) in 21.1 morphism of lifts in 17.1  $tion\ I$  in 15.1 morphism of locally ringed sites in 40.9 morphism of locally ringed spaces in 2.1 morphism of locally ringed topoi in 40.9 morphism of module-valued functors in morphism of Postnikov systems in 41.1 through  $x_0$  in 4.3 morphism of predeformation categories multiplicity in 2.2 in 6.2 multiplicity in 3.4 morphism of presheaves on  $\mathcal{X}$  in 3.1 *N-1* in 161.1 N-2 in 161.1 morphism of pseudo  $\mathcal{G}$ -torsors in 4.1 morphism of ringed sites in 6.1 morphism of ringed spaces in 25.1 Nagata in 13.1 morphism of ringed topoi in 7.1 morphism of schemes in 9.1 morphism of sheaves of O-modules in 10.1

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| naive cotangent complex in 35.1  | number of geometric branches of $X$ at $x$            |
|--|---|
| naive cotangent complex in 35.4  | in 13.1   |
| naive obstruction theory in 23.5   | number of $geometric$ $branches$ of $A$ in            |
| naively rig-flat in 15.2   | 106.6   |
| $natural\ transformation\ in\ 2.15$  | number of geometric branches of $X$ at $x$            |
| nilpotent in $32.1$  | in 15.4   |
| node  in  16.2   | $number\ of\ geometric\ branches\ of\ X\ at\ x$       |
| node  in  19.1   | in 23.4   |
| Noetherian in 9.1  | numerical polynomial in 58.3                          |
| Noetherian in 9.3  | numerical polynomial in 26.1                          |
| Noetherian in 9.3  | numerical type associated to $X$ in 11.4              |
| Noetherian in 5.1  | numerical type of genus $g$ in $3.4$                  |
| Noetherian in 24.1   | numerical type in 3.1                                 |
| Noetherian in 9.7  | obstruction modules in 22.1                           |
| Noetherian in 8.1  | obstruction theory in 22.1                            |
| Noetherian in 6.16   | obstruction in 22.1                                   |
| Noetherian in 36.5   | of finite presentation relative to $S$ in $58.1$      |
| nondegenerate in 26.2  | of finite presentation in 23.1                        |
| nonsingular projective model of $X$ in 2.7   | of finite presentation in 28.1                        |
| nonsingular in 9.1   | of finite presentation in 27.1                        |
| nontrivial solution in 67.5  | of finite type in 23.1                                |
| normal at $x$ in 20.1  | of finite type in 23.1                                |
| normal bundle in 19.5  | of finite type in 17.1                                |
| normal bundle in 6.5   | *               |
|  | Oka family in 28.2                                    |
| normal closure E over F in 16.4  | one step dévissage of $\mathcal{F}/X/S$ at $x$ in 4.2 |
| normal cone $C_ZX$ in 19.5   | one step dévissage of $\mathcal{F}/X/S$ over s in     |
| normal cone $C_Z X$ in 6.5   | 4.1   |
| normal crossings divisor in 21.4   | open immersion in 43.7                                |
| normal morphism in 20.1  | open immersion in 3.1                                 |
| normalization of $X$ in $Y$ in 53.3  | open immersion in 10.2                                |
| normalization of $X$ in $Y$ in 48.3  | open immersion in 12.1                                |
| normalization in 54.1  | open immersion in 9.1                                 |
| normalization in 49.6  | open subgroup scheme in 4.3                           |
| normalization in 46.3  | open subscheme in 10.2                                |
| normalized blowup of $X$ at $x$ in 5.1   | open subspace of $(X, \mathcal{O})$ associated to $U$ |
| normalized blowup of $X$ at $x$ in 5.1   | in 31.2   |
| normalized in 27.1   | open subspace of $X$ associated to $U$ in             |
| normal in 15.1   | 3.3   |
| normal in $28.1$   | open subspace in 12.1                                 |
| normal in $37.1$   | open substack in 9.9                                  |
| normal in $37.11$  | open subtopos in 43.4                                 |
| normal in 7.1  | openness of versality in 13.1                         |
| norm in $20.1$   | openness of versality in 13.1                         |
| nowhere dense in 21.1  | open in 23.1  |
| number field in 7.8  | open in 27.1  |
| number of branches of A in 106.6   | open in 6.2   |
| number of branches of $X$ at $x$ in 15.4   | open in 11.2  |
| number of branches of $X$ at $x$ in 16.4<br>number of branches of $X$ at $x$ in 24.4 | opposite algebra in 2.5                               |
| number of brunches of A at a III 24.4  | opposite atycora in 2.9                               |

| opposite category in 3.1                    | point p of the site $C$ in $32.2$  |
|---|--|
| opposite differential graded algebra in     | point $p$ in 52.1  |
| 11.1  | point of the topos $Sh(\mathcal{C})$ in 32.1                                 |
| orbit space for $R$ in $5.18$               | point in 4.1   |
| orbit in 5.1                                | point in 4.2   |
| orbit in 5.4                                | pondération in 75.2  |
| order of vanishing along $R$ in 121.2       | Postnikov system in 41.1   |
| order of vanishing of $f$ along $Z$ in 26.3 | pre-adic in $36.1$   |
| order of vanishing of $f$ along $Z$ in 6.4  | pre-admissible in 36.1   |
| order of vanishing of s along $Z$ in 27.1   | pre-equivalence relation in 3.1  |
| order of vanishing of s along $Z$ in 7.1    | pre-equivalence relation in 4.1  |
| ordered Čech complex in 23.2                | pre-relation in 3.1  |
| ordinary double point in 16.2               | pre-relation in 4.1  |
| ordinary double point in 19.1               | pre-triangulated category in 3.2   |
| p-basis of $K$ over $k$ in 46.1             | pre-triangulated subcategory in 3.4  |
| p-independent over $k$ in 46.1              | preadditive in 3.1   |
| parasitic for the $\tau$ -topology in 12.1  | predeformation category in 6.2   |
| parasitic in 12.1                           | preordered set in 21.1   |
| parasitic in 9.1                            | preorder in 21.1   |
| partial order in 21.1                       | presentation of $\mathcal{F}$ by $(U, R, s, t, c)$ in 25.1                   |
| partially ordered set in 21.1               | presentation in 9.3  |
| partition in 28.1                           | presentation in 16.5   |
| parts in 28.1                               | preserved under arbitrary base change in                                     |
| perfect at $x$ in 47.1                      | 18.3   |
| perfect closure in 45.5                     | preserved under arbitrary base change in                                     |
| perfect relative to R in 83.1               | 18.3   |
| perfect relative to S in 35.1               | preserved under base change in 18.3  |
| perfect relative to Y in 52.1               | preserved under base change in 18.3  |
| perfect ring map in 82.1                    | presheaf $\mathcal{F}$ of sets on $\mathcal{B}$ in 30.1                      |
| perfect in 45.1                             | presheaf $\mathcal{F}$ of sets on $X$ in 3.1                                 |
| perfect in 74.1                             | presheaf $\mathcal{F}$ on $X$ with values in $\mathcal{C}$ in 5.1            |
| perfect in 74.1                             | presheaf $\mathcal{F}$ with values in $\mathcal{C}$ on $\mathcal{B}$ in 30.8 |
| perfect in 49.1                             | presheaf of $\mathcal{O}$ -modules $\mathcal{F}$ on $\mathcal{B}$ in 30.11   |
| perfect in 49.1                             | presheaf of $\mathcal{O}$ -modules in 6.1                                    |
| perfect in 47.1                             | presheaf of $\mathcal{O}$ -modules in 9.1                                    |
| perfect in 47.1                             | presheaf of abelian groups on $X$ in 4.4                                     |
| perfect in 61.2                             | presheaf of isomorphisms from $x$ to $y$ in                                  |
| perfect in 10.1                             | 2.2  |
| perfect in 47.1                             | presheaf of modules on $\mathcal{X}$ in 7.1                                  |
| ph covering of $T$ in 8.4                   | presheaf of morphisms from $x$ to $y$ in 2.2                                 |
| $ph \ covering \ of \ X \ in \ 8.1$         | presheaf of sets on $C$ in 3.3   |
| Picard functor in 4.1                       | presheaf of sets in 2.1  |
| Picard group of A in 22.3                   | presheaf of sets in 9.1  |
| Picard group of $T$ in 4.1                  | presheaf on $\mathcal{X}$ in 3.1   |
| Picard group of $X$ in 40.7                 | presheaf in 3.3  |
| Picard group in 25.9                        | presheaf in 2.2  |
| Picard group in 32.6                        | prestable family of curves in 20.1   |
| PID in 120.12                               | prime divisor in 26.2  |
|   | *  |

| prime divisor in 6.2 prime divisor in 49.1 prime subfield of $F$ in 5.1 prime in 120.1 principal divisor associated to $f$ in 17.1 principal divisor associated to $f$ in 13.1 principal homogeneous $G$ -space over $B$ in 9.3 principal homogeneous space in 11.3 principal homogeneous space in 9.3 principal homogeneous space in 9.3 principal ideal domain in 120.12 principal Weil divisor associated to $f$ in 26.5 principal Weil divisor associated to $f$ in 6.7 pro-étale covering of $T$ in 12.1 product $U \times V$ exists in 13.1 product $U \times V$ of $U$ and $V$ in 13.1 product category in 2.20 product of $U$ and $V$ in 6.1 product of $U$ and $V$ in 9.1 product in 4.1 | proper in 40.1 proper in 31.1 proper in 37.1 prorepresentable in 6.1 prorepresentable in 22.1 pseudo G-torsor in 4.1 pseudo G-torsor in 11.1 pseudo G-torsor in 9.1 pseudo functor in 29.5 pseudo torsor in 4.1 pseudo-catenary in 5.14 pseudo-coherent at x in 46.1 pseudo-coherent relative to R in 81.4 pseudo-coherent relative to S in 59.2 pseudo-coherent relative to S in 59.2 pseudo-coherent relative to Y in 45.3 pseudo-coherent relative to Y in 45.3 pseudo-coherent ring map in 82.1 pseudo-coherent in 64.1 pseudo-coherent in 64.1 pseudo-coherent in 47.1 |
|---|---|
| $\begin{array}{l} \textit{product } U \times V \;\; \textit{exists} \; \text{in} \; 13.1 \\ \textit{product } U \times V \;\; \textit{of} \; U \;\; \textit{and} \; V \; \text{in} \; 13.1 \end{array}$   | pseudo-coherent relative to $Y$ in 45.3 pseudo-coherent relative to $Y$ in 45.3   |
| product of $U$ and $V$ in 9.1   | pseudo-coherent in 64.1   |
| profinite group in 30.5<br>profinite in 22.1<br>projective n-space over <b>Z</b> in 13.2<br>projective n-space over R in 13.2   | pseudo-coherent in 45.1<br>pseudo-coherent in 45.1<br>pseudo-coherent in 60.2<br>pseudo-coherent in 46.1  |
| projective n-space over S in 13.2<br>projective bundle associated to $\mathcal{E}$ in 21.1<br>projective cover in 4.1<br>projective dimension in 109.2  | pullback $x^{-1}\mathcal{F}$ of $\mathcal{F}$ in 9.2<br>pullback functor in 33.6<br>pullback functor in 3.4<br>pullback functor in 34.7   |
| projective envelope in 4.1<br>projective resolution of $A$ in 19.1<br>projective resolution of $K^{\bullet}$ in 19.1<br>projective system over $I$ in $C$ in 21.2   | pullback functor in 34.9 pullback functor in 22.7 pullback functor in 22.9 pullback of S along f in 12.9  |
| projective variety in 26.1<br>projective-amplitude in [a, b] in 68.1<br>projective in 77.1<br>projective in 28.1  | pullback of D by f is defined in 13.12<br>pullback of D by f is defined in 6.10<br>pullback of S by f in 47.4<br>pullback of the effective Cartier divisor  |
| projective in 43.1<br>projective in 7.1<br>proper relative cycle in 9.1<br>proper variety in 26.1<br>property $\mathcal{P}$ in 5.1  | in 13.12  pullback of the effective Cartier divisor in 6.10  pullbacks of meromorphic functions are defined for f in 23.4   |
| property $\mathcal{P}$ in 4.1<br>property $\mathcal{P}$ in 10.1<br>proper in 17.2<br>proper in 41.1   | pullbacks of meromorphic functions are defined for f in 10.6 pullback in 26.1 pullback in 13.1  |

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| pullback in 3.3  | quasi-compact in 12.1                     |
| pullback in 36.1   | quasi-compact in 12.1                     |
| pullback in 4.3  | quasi-compact in 17.1                     |
| pure above y in 3.1  | quasi-compact in $17.4$                   |
| pure above $y$ in $3.1$                                    | quasi-compact in 17.4                     |
| pure along $X_s$ in 16.1                                   | quasi-compact in 19.1                     |
| pure along $X_s$ in 16.1                                   | quasi-compact in $5.1$                    |
| pure extension module in 8.8                               | quasi-compact in $8.2$                    |
| pure injective resolution in 8.5                           | quasi-compact in $17.2$                   |
| pure injective in 8.1                                      | quasi-compact in $17.4$                   |
| pure projective resolution in 8.5                          | quasi-compact in 6.1                      |
| pure projective in 8.1                                     | quasi-compact in $7.2$                    |
| pure relative to $S$ in 16.1                               | quasi-compact in $6.4$                    |
| pure relative to $S$ in 16.1                               | $quasi-DM \ over \ S \ in \ 4.2$          |
| pure relative to $Y$ in $3.1$                              | quasi-DM in $4.1$                         |
| pure relative to $Y$ in $3.1$                              | quasi-DM in $4.2$                         |
| purely inseparable in 14.1                                 | quasi-excellent in $52.1$                 |
| purely inseparable in 14.1                                 | quasi-finite at $\mathfrak{q}$ in 122.3   |
| purely inseparable in 28.1                                 | quasi-finite at $x$ in 27.1               |
| purely transcendental extension in 26.1                    | quasi-finite at a point $x \in X$ in 20.1 |
| <i>pure</i> in 108.1                                       | quasi-finite in 122.3                     |
| pushforward of $S$ along $f$ in 12.4                       | quasi-finite in 20.1                      |
| pushforward in 26.1  | quasi-finite in 27.1                      |
| pushforward in 44.1  | quasi-finite in 24.1                      |
| pushforward in 13.1  | quasi-inverse in 2.17                     |
| pushforward in 12.1  | quasi-isomorphism in 13.4                 |
| pushforward in 35.1  | quasi-isomorphism in 13.10                |
| pushforward in 35.3  | quasi-isotrivial in 11.3                  |
| pushforward in 8.1   | quasi-isotrivial in 9.3                   |
| pushout of $V$ and $W$ over $U$ in 8.1                     | quasi-projective variety in 26.1          |
| pushout in 9.1   | quasi-projective in 40.1                  |
| qc covering in 31.2  | quasi-proper in 17.2                      |
| quasi-affine in 18.1                                       | quasi-regular ideal in 32.1               |
| quasi-affine in 13.1                                       | quasi-regular immersion in 21.1           |
| quasi-affine in 21.2                                       | quasi-regular immersion in 44.2           |
| quasi-coherent $\mathcal{O}_{\mathcal{X}}$ -module in 11.1 | quasi-regular sequence in 69.1            |
| quasi-coherent module on $(U, R, s, t, c)$ in              | quasi-regular in 20.2                     |
| 14.1   | quasi-separated over S in 13.2            |
| quasi-coherent module on $(U, R, s, t, c)$ in              | quasi-separated over $S$ in 4.2           |
| 12.1   | quasi-separated in 21.3                   |
| quasi-coherent module on $\mathcal{X}$ in 11.1             | quasi-separated in 21.3                   |
| quasi-coherent sheaf of $\mathcal{O}_X$ -modules in        | quasi-separated in 3.1                    |
| 10.1   | quasi-separated in 3.1                    |
| quasi-coherent in 23.1                                     | quasi-separated in 4.2                    |
| quasi-coherent in 17.2                                     | quasi-separated in 16.3                   |
| quasi-coherent in 11.1                                     | quasi-separated in 30.1                   |
| quasi-coherent in 29.1                                     | quasi-separated in 4.1                    |
| quasi-coherent in 36.1                                     | quasi-separated in 4.2                    |
| quast controlled III ou.1                                  | quasi ocpanaica in 4.2                    |

| quasi-sober in 8.6  | refinement in 8.1  |
|---|--|
| quasi-split over u in 15.1  | refines in 28.1  |
| quasi-splitting of $R$ over $u$ in 15.1                                   | reflexive hull in 23.9   |
| quotient category $\mathcal{D}/\mathcal{B}$ in 6.7                        | reflexive hull in 12.1   |
| quotient category cofibered in groupoids                                  | reflexive in 23.1  |
| [ $U/R$ ] $\rightarrow \mathcal{C}$ in 21.9                               | reflexive in 12.1  |
| quotient filtration in 19.1   | regular at x in 21.1   |
| quotient functor in 6.7   | regular ideal in 32.1  |
| quotient functor in 0.7<br>quotient morphism $U \to [U/R]$ in 21.9        | regular immersion in 21.1  |
| quotient morphism $U \to [U/H]$ in 21.9<br>quotient of $U$ by $G$ in 14.4 | regular in codimension $\leq k$ in 157.1   |
| quotient of 0 by G in 14.4 quotient representable by an algebraic         | regular in codimension $k \in \mathbb{N}$ in 137.1 regular in codimension $k \in \mathbb{N}$ in 12.1 |
| space in 19.3   | regular local ring in 60.10  |
| quotient representable by an algebraic                                    | regular locus in 14.1  |
| space in 19.3   | regular morphism in 21.1   |
| quotient sheaf $U/R$ in 20.1  | regular section in 14.6  |
| quotient sheaf $U/R$ in 19.1  | regular section in 7.4   |
| quotient stack in 20.1  | regular sequence in 68.1   |
| quotient stack in 20.1  | regular system of parameters in 60.10  |
| quotient in 5.3   | regular in 110.7   |
| radicial in 10.1  | regular in 24.7  |
| radicial in 3.1   | regular in 41.1  |
| ramification index in 111.1   | regular in 9.1   |
| rank r in 32.1  | regular in 20.2  |
| rank in 102.5   | regular in 23.7  |
| rank in 48.1  | regular in 10.9  |
| rank in $46.2$  | relation in 11.2   |
| rational function on $X$ in 49.3  | relation in 3.1  |
| rational function on $X$ in 47.2  | relation in 4.1  |
| rational map from $X$ to $Y$ in 49.1                                      | relative $H_1$ -regular immersion in 22.2  |
| rational map from $X$ to $Y$ in 47.1                                      | relative r-cycle on $X/S$ in 6.1   |
| rationally equivalent to zero in 19.1                                     | relative assassin of $\mathcal{F}$ in $X$ over $S$ in 7.1  |
| rationally equivalent to zero in 15.1                                     | relative assassin of N over $S/R$ in 65.2  |
| rationally equivalent in 19.1   | relative cotangent space in 3.6  |
| rationally equivalent in 15.1   | relative dimension $\leq d$ at $x$ in 29.1   |
| reasonable in 6.1   | relative dimension $\leq d$ in 29.1  |
| reasonable in 17.1  | relative dimension $\leq d$ in 33.2  |
| reduced induced algebraic space structure                                 | relative dimension $d$ in 29.1   |
| in 12.5   | relative dimension d in 33.2   |
| reduced induced algebraic stack structure                                 | relative dimension of $S/R$ at $\mathfrak{q}$ in 125.1   |
| in 10.4   | relative dimension of in 125.1   |
| reduced induced scheme structure in 12.5                                  | relative dimension in 5.7  |
| reduced in 12.1   | relative dualizing complex in 27.1   |
| reduction $\mathcal{X}_{red}$ of $\mathcal{X}$ in 10.4                    | relative dualizing complex in 28.1   |
| reduction $X_{red}$ of $X$ in 12.5  | relative dualizing complex in 9.1  |
| reduction $X_{red}$ of $X$ in 12.5  | relative dualizing sheaf in 19.2   |
| reduction to rational singularities is pos-                               | relative effective Cartier divisor in 18.2   |
| sible for A in 8.3  | relative effective Cartier divisor in 9.2  |
| Rees algebra in 70.1  |  |
| <i></i>   |  |

| relative Frobenius morphism of $X/S$ in                 | residual gerbe of $\mathcal{X}$ at $x$ in 11.8                     |
|---|--|
| 36.4  | residual space of $X$ at $x$ in 13.6                               |
| relative global complete intersection in                | residue degree in 111.1  |
| 136.5   | residue degree in 123.1  |
| relative homogeneous spectrum of $A$ over               | residue field of $X$ at $x$ in $2.1$                               |
| S in 16.7   | residue field of $X$ at $x$ in 11.2                                |
| relative homogeneous spectrum of $A$ over               | resolution functor in 23.2   |
| X in 11.3   | resolution of M by finite free R-modules                           |
| relative inertia of $S$ over $S'$ in 34.2               | in 71.2  |
| relative Proj of $\mathcal{A}$ over $S$ in 16.7         | resolution of $M$ by free $R$ -modules in                          |
| relative Proj of $A$ over $X$ in 11.3                   | 71.2   |
| relative quasi-regular immersion in 22.2                | resolution of singularities by normalized                          |
| relative sheaf of automorphisms of $x$ in               | blowups in 14.2  |
| 5.3   | resolution of singularities by normalized                          |
| relative sheaf of isomorphisms from $x_1$               | blowups in $8.2$   |
| to $x_2$ in 5.3   | resolution of singularities in 14.1                                |
| relative spectrum of $A$ over $S$ in 4.5                | resolution of singularities in 8.1                                 |
| relative spectrum of $A$ over $X$ in 20.8               | resolution property in 36.1  |
| relative weak assassin of $\mathcal{F}$ in $X$ over $S$ | resolution property in 28.1  |
| in 8.1  | resolution in 71.2   |
| relative weak assassin of $\mathcal{F}$ in $X$ over $Y$ | restriction $(U, R, s, t, c) _{\mathcal{C}'}$ of $(U, R, s, t, c)$ |
| in 4.5  | $to \ \mathcal{C}' \ \text{in} \ 21.7$                             |
| relatively ample in 37.1                                | restriction of $(U, R, s, t, c)$ to $U'$ in 18.2                   |
| relatively ample in 14.1                                | restriction of $(U, R, s, t, c)$ to $U'$ in 17.2                   |
| relatively limit preserving in 3.1                      | restriction of $\mathcal{F}$ to $\mathcal{C}/U$ in 25.1            |
| relatively prime in 11.1                                | restriction of $\mathcal{F}$ to $\mathcal{C}/U$ in 19.1            |
| relatively very ample in 38.1                           | restriction of $\mathcal{F}$ to $U_{\acute{e}tale}$ in 9.2         |
| representable by a scheme in 15.1                       | restriction of $\mathcal{G}$ to $U$ in 31.2                        |
| representable by algebraic spaces in 3.1                | restriction of $\mathcal{G}$ to $U$ in 31.2                        |
| representable by algebraic spaces in 9.1                | restriction of $\mathcal{G}$ to $U$ in $31.2$                      |
| representable by an algebraic space over                | restriction to the small étale site in 4.15                        |
| S  in  8.1  | restriction to the small étale site in 4.9                         |
| representable by open immersions in 15.3                | restriction to the small pro-étale site in                         |
| representable quotient in 20.2                          | 12.14  |
| representable quotient in 20.2                          | restriction to the small Zariski site in                           |
| representable quotient in 19.3                          | 3.15   |
| representable quotient in 19.3                          | restriction in 3.3   |
| representable sheaves in 12.3                           | restriction in 4.3   |
| representable in 3.6                                    | retrocompact in 12.1   |
| representable in 6.4                                    | rig-étale over $(A, I)$ in 8.1                                     |
| representable in 8.2                                    | rig-étale in 20.1  |
| representable in 40.1                                   | rig-closed in 14.2   |
| representable in 42.3                                   | rig-etale in 19.2  |
| representable in 15.1                                   | rig-flat in 15.4   |
| representable in 21.4                                   | rig-flat in 16.1   |
| residual degree in 111.1                                | rig-smooth over $(A, I)$ in 4.1                                    |
| residual degree in 123.1                                | rig-smooth in 17.2   |
| residual gerbe of $\mathcal{X}$ at $x$ exists in 11.8   | rig-smooth in 18.1   |
|   |  |

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|---|---|
| rig-surjective in 21.1  | scheme theoretic image in 16.2                    |
| right acyclic for F in 15.3   | scheme theoretic image in 38.1                    |
| right adjoint in 24.1   | scheme theoretic intersection in 4.4              |
| right admissible in 40.9  | scheme theoretic intersection in 14.4             |
| right derivable in 14.9   | scheme theoretic support of $\mathcal{F}$ in 5.5  |
| right derived functor RF is defined at in                             | scheme theoretic support of $\mathcal{F}$ in 15.4 |
| 14.2  | scheme theoretic union in 4.4                     |
| right derived functors of $F$ in 15.3                                 | scheme theoretic union in 14.4                    |
| right dual in 43.5  | scheme theoretically dense in $X$ in 7.1          |
| right exact in 23.1   | scheme theoretically dense in $X$ in 17.3         |
| right multiplicative system in 27.1                                   | scheme in 9.1                                     |
| right orthogonal in 40.1  | sections with compact support in 3.7              |
| ring of rational functions on $X$ in 49.4                             | semi-representable objects over X in 2.1          |
| ring of rational functions on $X$ in 47.3                             | semi-representable objects in 2.1                 |
| ringed site in 6.1  | seminormalization of $X$ in $Y$ in 55.6           |
| ringed site in 17.2   | seminormalization in 47.8                         |
| ringed space in 25.1  | seminormal in 47.1                                |
| ringed topos in 7.1   | seminormal in 47.3                                |
| satisfies the existence part of the valua-                            | semistable family of curves in 21.2               |
| tive criterion in 20.3  | semistable reduction in 14.6                      |
| satisfies the existence part of the valua-                            | separable degree in 12.6                          |
| tive criterion in 41.1  | separable degree in 14.7                          |
| satisfies the sheaf property for the fpqc                             | separable over $k$ in 42.1                        |
| topology in 9.12  | separable solution in 115.1                       |
| satisfies the sheaf property for the fpqc                             | separable in 12.2                                 |
| topology in 15.5  | separable in 12.2                                 |
| satisfies the sheaf property for the given                            | separable in 12.2                                 |
| family in 9.12  | separable in 28.1                                 |
| satisfies the sheaf property for the V                                | separably generated over k in 42.1                |
| topology in 10.11   | separated group scheme in 4.5                     |
| satisfies the sheaf property for the                                  | separated over $S$ in 13.2                        |
| Zariski topology in 15.3  | separated over S in 4.2                           |
| satisfies the uniqueness part of the valu-<br>ative criterion in 20.3 | separated presheaf in 11.1                        |
| satisfies the uniqueness part of the valu-                            | separated in 4.1<br>separated in 11.2             |
| ative criterion in 41.1   | separated in 10.9                                 |
| satisfies the valuative criterion in 41.1                             | separated in 49.2                                 |
| saturated in 27.20  | separated in 19.1                                 |
| saturated in 6.1  | separated in 21.3                                 |
| scheme over $R$ in 18.1   | separated in 21.3                                 |
| scheme over $S$ in 18.1   | separated in 3.1                                  |
| scheme structure on $Z$ in 12.5                                       | separated in 3.1                                  |
| scheme theoretic closure of $U$ in $X$ in 7.1                         | separated in 4.2                                  |
| scheme theoretic closure of $U$ in $X$ in                             | separated in 4.2<br>separated in 16.3             |
| 17.3  | separated in 30.1                                 |
| scheme theoretic fibre $X_s$ of $f$ over $s$ in                       | separated in 4.1                                  |
| 18.4  | separated in 4.1<br>separated in 4.2              |
| scheme theoretic image in 6.2   | separates R-orbits in 5.8                         |
| solvenide incorevice invage in 0.2                                    | 50pura000 10 010000 III 0.0                       |

| separates orbits in                        | n 5.8                                   | sheaf of meromorphic functions on $X$ in           |
|--|---|--|
| Serre functor in 3                         |   | 23.1   |
| Serre subcategory                          |   | sheaf of meromorphic functions on $X$ in           |
|  | valence relation in 5.13                | 10.1   |
|  | equivalence relation in                 | sheaf of total quotient rings $K_S$ in 49.1        |
| 5.13                                       | 1                                       | sheaf theoretically empty in 42.1                  |
|  | <i>R-invariant</i> in 19.1              | sheaf in 9.1                                       |
| set-theoretically R                        |   | sheaf in 7.1                                       |
| setoid in 39.1                             | 0.0000000000000000000000000000000000000 | sheaf in 7.6                                       |
|  | lules on $\mathcal{B}$ in 30.11         | sheaf in 47.10                                     |
| sheaf $\mathcal F$ of sets or              |   | sheaf in 11.1                                      |
| sheaf $\mathcal F$ of sets or              |   | sheaf in 4.3                                       |
|  | $es \ in \ C \ on \ B \ in \ 30.8$      | shift in 16.4                                      |
|  |   | short exact sequence in 5.7                        |
| sheaf associated to                        |   |  |
| sheaf associated to                        |   | siblings in 10.1                                   |
|  | the module M and the                    | siblings in 12.1                                   |
| ring map $\alpha$ in 10.                   |   | sibling in 10.1                                    |
|  | to the module $M$ in 10.6               | sibling in 12.1                                    |
| sheaf for the étale                        |   | sieve on U generated by the morphisms              |
| sheaf for the fppf                         |   | $f_i \text{ in } 47.3$                             |
|  | oth topology in 4.3                     | sieve $S$ on $U$ in 47.1                           |
|  | omic topology in 4.3                    | similar in 61.3                                    |
| sheaf for the Zari                         |   | simple in 52.9                                     |
|  | es associated to $\mathcal{F}$ in 8.2   | simple in 2.3                                      |
|  | es associated to $\mathcal{F}$ in 8.2   | simple in 2.3                                      |
| sheaf of $\mathcal{O}$ -module             |   | simple in 9.1                                      |
| sheaf of $\mathcal{O}$ -module             |   | simplicial $\mathcal{A}_{\bullet}$ -module in 41.1 |
| sheaf of $\mathcal{O}_{\mathcal{X}}$ -modu |   | simplicial abelian group in 3.1                    |
|  | ant functions on $X$ in                 | simplicial object $U$ of $C$ in $3.1$              |
| 8.1  |   | simplicial scheme associated to $f$ in 27.3        |
| sheaf of abelian gr                        |   | simplicial set in 3.1                              |
| sheaf of automorp                          |   | simplicial sheaf of $A_{\bullet}$ -modules in 41.1 |
|  | al graded $\mathcal{O}$ -algebras in    | simplicial system of the derived category          |
| 12.1                                       |   | of modules in 14.1                                 |
| sheaf of different                         | tial graded algebras in                 | simplicial system of the derived category          |
| 12.1                                       |   | in 13.1  |
|  | Tals $\Omega_{X/S}$ of X over S         | singular ideal of $A$ over $R$ in $2.1$            |
| in 28.10                                   |   | singular locus in 14.1                             |
| sheaf of differenti                        | Tals $\Omega_{X/S}$ of X over S         | singularities of X are at-worst-nodal in           |
| in $32.1$                                  |   | 19.1   |
| sheaf of differenti                        | als $\Omega_{X/Y}$ of X over Y          | site in 6.2  |
| in 33.10                                   | ,                                       | site in 10.2                                       |
| sheaf of differenti                        | als $\Omega_{X/Y}$ of X over Y          | size in 11.2                                       |
| in 7.2                                     | ,                                       | skew field in 2.2                                  |
| sheaf of graded $\mathcal{O}$              | -algebras in 3.1                        | skyscraper sheaf at $x$ with value $A$ in 27.1     |
| sheaf of graded al                         | _                                       | skyscraper sheaf in 27.1                           |
|  | $aisms from x_1 to x_2 in$              | skyscraper sheaf in 27.1                           |
| 5.3  | v ± <u>=</u>                            | skyscraper sheaf in 27.1                           |
|  |   | ~ <b>* *</b>                                       |

| skyscraper sheaf in 27.1                                   | spectral sequence associated to $(A, d, \alpha)$ |
|--|--|
| skyscraper sheaf in 32.6                                   | in 22.5  |
| small $\tau$ -site of $S$ in 20.2                          | spectral sequence associated to the exact        |
| small étale site $X_{\text{étale}}$ in 18.1                | couple in 21.3                                   |
| small étale site of $S$ in $4.8$                           | spectral sequence in $A$ in 20.1                 |
| small étale site over $S$ in $27.3$                        | spectral in 23.1                                 |
| small étale site in 34.1                                   | spectral in 23.1                                 |
| small étale topos in 21.1                                  | spectrum of $A$ over $S$ in 4.5                  |
| small étale topos in 18.7                                  | spectrum of $A$ over $X$ in 20.8                 |
| small affine étale site of $S$ in 4.8                      | spectrum in 17.1                                 |
| small affine Zariski site of S in 3.7                      | spectrum in 5.3                                  |
| small extension in 141.1                                   | split category fibred in groupoids in 37.2       |
| small extension in 3.2                                     | split equalizer in 4.2                           |
| small pro-étale site of $S$ in 12.8                        | split fibred category in 36.2                    |
| small Zariski site $F_{Zar}$ in 12.6                       | split node in 19.10                              |
| small Zariski site of S in 3.7                             | split over $u$ in 15.1                           |
| small Zariski sites in 27.3                                | splits in 8.1                                    |
| small Zariski topos in 21.1                                | splitting field of $P$ over $F$ in 16.2          |
| smooth at $\mathfrak{q}$ in 137.11                         | splitting field in 8.1                           |
| smooth at $x \in X$ in 34.1                                | splitting of $R$ over $u$ in 15.1                |
| smooth at $x \in X$ in 34.1<br>smooth at $x$ in 37.1       | split in 5.9                                     |
| smooth at $x$ in $37.1$<br>smooth covering of $T$ in $5.1$ | split in 18.1                                    |
|  |  |
| smooth covering of X in 5.1                                | split in 18.1                                    |
| smooth group scheme in 4.5                                 | stabilizer of the groupoid in algebraic          |
| smooth groupoid in 16.4                                    | spaces $(U, R, s, t, c)$ in 16.2                 |
| smooth local on source-and-target in 20.1                  | stabilizer of the groupoid scheme                |
| smooth local in 21.1                                       | (U,R,s,t,c) in 17.2                              |
| smooth of relative dimension d in 34.13                    | stable family of curves in 22.2                  |
| smooth sheaf in 4.3  | stable under base change in 14.1                 |
| smooth variety in 26.1                                     | stable under composition in 14.1                 |
| smooth in 137.1  | stable under generalization in 19.1              |
| smooth in $34.1$   | stable under specialization in 19.1              |
| smooth in 20.2   | stably free in 3.1                               |
| smooth in $37.1$   | stably isomorphic in 3.1                         |
| smooth in $8.1$  | stack in discrete categories in 6.1              |
| smooth in $9.1$  | stack in groupoids in 5.1                        |
| smooth in 23.1   | stack in setoids in 6.1                          |
| smooth in $33.1$   | stack in sets in 6.1                             |
| smooth in $4.3$  | stack in 4.1                                     |
| sober in 8.6   | stalk in 29.6                                    |
| solution for $A \subset B$ in 115.1                        | stalk in 18.6                                    |
| special cocontinuous functor $u$ from $C$ to               | stalk in 19.6                                    |
| $\mathcal{D}$ in 29.2                                      | standard $\tau$ -covering in 20.4                |
| specializations lift along $f$ in 19.4                     | standard étale covering in 4.5                   |
| specialization in 19.1                                     | standard étale in 144.1                          |
| specialization in 6.22                                     | standard étale in 36.1                           |
| specialization in 36.2                                     | standard étale in 26.3                           |
| specializing in 19.4                                       | standard fppf covering in 7.5                    |
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| standard fpqc covering in 9.9<br>standard h covering in 34.11<br>standard open covering in 5.2<br>standard open covering in 5.2                          | strongly $C$ -cartesian morphism in 33.1<br>strongly cartesian morphism in 33.1<br>strongly split over $u$ in 15.1<br>strongly transcendental over $R$ in 123.7 |
|--|---|
| standard open covering in 8.2<br>standard opens in 17.3  | structure morphism in 18.1<br>structure of site on $S$ inherited from $C$   |
| standard ph covering in 8.1<br>standard pro-étale covering in 12.6<br>standard resolution of $\mathcal{B}$ over $\mathcal{A}$ in 18.1                    | in 10.2<br>structure sheaf $\mathcal{O}_{\mathrm{Spec}(R)}$ of the spectrum<br>of $R$ in 5.3  |
| $standard\ resolution\ of\ B\ over\ A\ in\ 3.1$ $standard\ shrinking\ in\ 4.6$   | structure sheaf $\mathcal{O}_{Proj(S)}$ of the homogeneous spectrum of $S$ in 8.3   |
| standard shrinking in 5.5<br>standard smooth algebra over R in 137.6   | structure sheaf of $\mathcal{X}$ in 6.1<br>structure sheaf of the big site $(Sch/S)_{\tau}$   |
| standard smooth covering in 5.5<br>standard smooth in 34.1<br>standard syntomic covering in 6.5  | in 8.2<br>structure sheaf of the small site in 8.2<br>structure sheaf in 6.1  |
| $standard\ syntomic\ in\ 30.1$ $standard\ V\ covering\ in\ 10.1$   | structure sheaf in 7.1<br>structure sheaf in 23.3   |
| standard Zariski covering in 3.4<br>strata in 28.3<br>stratification in 28.3   | structure sheaf in 21.2<br>sub 2-category in 29.2<br>subbase for the topology on X in 5.4   |
| strict henselization of $\mathcal{O}_{S,s}$ in 33.2<br>strict henselization of $R$ with respect to   | subbasis for the topology on $X$ in 5.4 subcanonical in 12.2  |
| $\kappa \subset \kappa^{sep}$ in 155.3<br>strict henselization of $S$ at $\overline{s}$ in 33.2<br>strict henselization of $X$ at $\overline{x}$ in 22.2 | subcategory in 2.10<br>subfield in 2.1<br>subfunctor $H \subset F$ in 15.3  |
| strict henselization in 155.3<br>strict map of topological spaces in 6.3   | submersive in 6.3<br>submersive in 24.1   |
| strict morphism of thickenings in 3.2<br>strict morphism of thickenings in 9.2   | submersive in 7.2<br>submersive in 12.2   |
| strict normal crossings divisor in 21.1 strict transform of M along $R \to R[\frac{I}{a}]$ in 26.1   | subobject in 5.3<br>subpresheaf in 16.2<br>subpresheaf in 3.3   |
| $strict\ transform\ {\rm in}\ 33.1$ $strict\ transform\ {\rm in}\ 33.1$  | subsheaf generated by the $s_i$ in 4.5<br>subsheaf of sections annihilated by $\mathcal{I}$ in  |
| strict transform in 18.1<br>strict transform in 18.1<br>strictly commutative in 3.3  | 24.3 subsheaf of sections annihilated by $\mathcal{I}$ in 14.3  |
| strictly full in 2.10<br>strictly henselian in 153.1   | subsheaf of sections supported on $T$ in $24.6$   |
| strictly henselian in 32.6<br>strictly perfect in 46.1<br>strictly perfect in 44.1   | subsheaf of sections supported on T in 14.6 subsheaf in 16.2  |
| strictly standard in A over R in 2.3 strict in 19.3  | subtopos in 43.2<br>sum of the effective Cartier divisors $D_1$   |
| strong generator in 36.3<br>strong splitting of $R$ over $u$ in 15.1<br>stronger in 47.8   | and $D_2$ in 13.6<br>sum of the effective Cartier divisors $D_1$<br>and $D_2$ in 6.6  |
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| sum of the effective Cartier divisors in 23.9 support of $\mathcal{F}$ in 5.1 support of $\mathcal{F}$ in 31.3 support of $\sigma$ in 31.3 support of $\sigma$ in 20.3 support of $\sigma$ in 20.3 support of $\sigma$ in 20.3 support of $\sigma$ in 5.1 supported on $\sigma$ in 6.1 supported on $\sigma$ in 6.1 supported on $\sigma$ in 3.2 support in 8.3 surjective in 16.2 surjective in 16.2 surjective in 3.1 surjective in 5.3 surjective in 9.1 | tangent vector in 16.3<br>tangent vector in 35.3<br>tautologically equivalent in 8.2<br>taut in 5.1<br>tensor power in 25.6<br>tensor product differential graded algebra<br>in 3.4<br>tensor product in 4.7<br>termwise split exact sequence of com-<br>plexes of $\mathcal{A}$ in 9.9<br>termwise split injection $\alpha: A^{\bullet} \to B^{\bullet}$ in 9.4<br>termwise split surjection $\beta: B^{\bullet} \to C^{\bullet}$ in 9.4<br>the fibre of $f: X \to Y$ at $y$ is geometri-<br>cally reduced in 29.2<br>the fibre of $f$ over $y$ is locally Noetherian<br>in 4.2 |
|---|--|
| surjective in 5.2<br>surjective in 25.1<br>surjective in 5.1<br>symbol associated to M, a, b in 68.29<br>symbolic power in 64.1   | the fibre of $X$ over $z$ is flat at $x$ over the fibre of $Y$ over $z$ in 23.2 the fibre of $X$ over $z$ is flat over the fibre of $Y$ over $z$ in 23.2 the fibres of $f$ are locally Noetherian in   |
| symbol in 68.2<br>symmetric monoidal category in 43.9<br>syntomic at $x \in X$ in 30.1<br>syntomic at $x$ in 36.1<br>syntomic covering of $T$ in 6.1  | the Fourier-Mukai kernel of a relative equivalence from X to Y over S in 15.1 the functions on X are the R-invariant functions on U in 8.1   |
| syntomic covering of X in 6.1<br>syntomic of relative dimension d in 30.15<br>syntomic sheaf in 4.3<br>syntomic in 136.1<br>syntomic in 30.1  | the gysin map for $f$ exists in 59.4<br>the relative dimension in 5.2<br>the restriction of $\mathcal{F}$ to its fibre over $z$ is<br>flat at $x$ over the fibre of $Y$ over $z$ in 23.2<br>thickenings over $\mathcal{Z}$ in 3.1  |
| syntomic in 36.1<br>system $(\mathcal{F}_i, \varphi_{i'i})$ of sheaves on $(X_i, f_{i'i})$<br>in 51.1<br>system $(M_i, \mu_{ij})$ of R-modules over I in<br>8.1   | thickenings over $B$ in 9.1<br>thickenings over $S$ in 2.1<br>thickening in 2.1<br>thickening in 9.1<br>thickening in 3.1  |
| system of parameters of $R$ in 60.10 system of rings in 2.1 system over $I$ in $\mathcal{C}$ in 21.2 tame inertia group of $\mathfrak{m}$ in 112.6 tame symbol in 68.31 tamely ramified with respect to $A$ in 111.7 tangent space $T\mathcal{F}$ of $\mathcal{F}$ in 12.1 tangent space $T\mathcal{F}$ of $F$ in 11.9 tangent space of $X$ over $S$ at $x$ in 16.3 tangent space of $X$ over $S$ in 35.3   | topological genus of $T$ in 3.11<br>topological group in 30.1<br>topological module in 30.10<br>topological module in 36.1<br>topological ring in 30.7<br>topological ring in 36.1<br>topological space in 4.7<br>topological space in 4.8<br>topologically nilpotent in 4.8<br>topologically of finite type over in 29.1  |

| topology associated to $\mathcal{C}$ in 48.2                           | triangulated subcategory in 3.4                      |
|--|--|
| topology on $C$ in 47.6  | $trivial \mathcal{G}$ - $torsor$ in 4.1              |
| topos in 15.1  | $trivial \ \mathcal{G}$ - $torsor \ in \ 4.1$        |
| $tor\ dimension \le d \text{ in } 66.1$                                | trivial descent datum in 3.5                         |
| $tor\ dimension \leq d\ in\ 48.1$                                      | trivial descent datum in 2.3                         |
| $tor\ dimension \leq d\ in\ 46.1$                                      | trivial descent datum in 34.10                       |
| Tor independent over $B$ in $20.2$                                     | trivial descent datum in 3.3                         |
| Tor independent over $R$ in $61.1$                                     | trivial descent datum in 22.10                       |
| Tor independent over $S$ in $22.2$                                     | trivial Kan fibration in 30.1                        |
| tor-amplitude in $[a, b]$ in $66.1$                                    | trivial in 117.1                                     |
| tor-amplitude in $[a, b]$ in $48.1$                                    | trivial in 25.1                                      |
| tor-amplitude in $[a, b]$ in 46.1                                      | trivial in 11.1                                      |
| torsion free in 22.1   | trivial in 9.1                                       |
| torsion free in 11.2   | trivial in $40.4$                                    |
| torsion in 22.1  | $twist\ of\ the\ structure\ sheaf\ of\ Proj(S)$ in   |
| torsion in 11.2  | 10.1   |
| torsion in 18.6  | twist of the structure sheaf in 21.1                 |
| torsor in 4.1  | two-sided admissible in 40.9                         |
| torsor in 4.1  | type of algebraic structure in 15.1                  |
| <i>Tor</i> in 26.15  | <i>UFD</i> in 120.4                                  |
| <i>Tor</i> in 17.14  | underlying presheaf of sets of $\mathcal{F}$ in 5.2  |
| total Chern class of $\mathcal{E}$ on $X$ in 37.1                      | unibranch at $x$ in 15.1                             |
| total Chern class of $\mathcal{E}$ in 28.2                             | $unibranch \ at \ x \ in \ 24.2$                     |
| total Chern class in 38.8  | unibranch in 106.1                                   |
| total left derived functor of $G$ in 6.4                               | unibranch in 15.1                                    |
| total right derived functor of $F$ in 6.4                              | unibranch in $24.2$                                  |
| totally acyclic in 13.4  | uniform categorical moduli space in $C$ in           |
| totally disconnected in 7.8  | 12.1   |
| totally ramified with respect to $A$ in 111.7                          | uniform categorical moduli space in 12.1             |
| tower in 6.3   | uniform categorical quotient in 4.4                  |
| trace element in 4.1   | uniformizer in 119.8                                 |
| trace pairing in 20.6  | uniformly in 7.1                                     |
| trace in 20.1  | unique factorization domain in 120.4                 |
| trace in $66.1$  | $uniqueness\ part\ of\ the\ valuative\ criterion$    |
| trace in 4.1   | in 39.6  |
| transcendence basis in 26.1  | universal $\delta$ -functor in 12.3                  |
| $transcendence\ degree\ of\ x/f(x)\ in\ 33.1$                          | universal $\varphi$ -derivation in 28.3              |
| transcendence degree in 26.4   | universal $\varphi$ -derivation in 33.3              |
| $transition \ maps \ in \ 21.2$  | $universal\ S$ - $derivation\ in\ 32.1$              |
| triangle associated to 0 $\rightarrow$ K $\rightarrow$ L $\rightarrow$ | $universal\ Y$ - $derivation\ in\ 33.10$             |
| $M \to 0 \text{ in } 8.2$  | $universal\ Y$ - $derivation\ in\ 7.2$               |
| $triangle\ associated\ to\ the\ termwise\ split$                       | universal categorical quotient in 4.4                |
| sequence of complexes in 9.9   | universal effective epimorphism in 12.1              |
| triangle in 3.1  | universal first order thickening in 149.2            |
| $triangulated\ category\ of\ quasi-coherent$                           | universal first order thickening in 7.2              |
| objects in the derived category in 26.1                                | universal first order thickening in 15.5             |
| triangulated category in 3.2   | universal flattening of $\mathcal{F}$ exists in 21.1 |
| $triangulated\ functor\ in\ 3.3$                                       | universal flattening of $\mathcal{F}$ exists in 11.1 |
|  |  |

| universal flattening of $X$ exists in 21.1                               | unramified in 3.5  |
|--|--|
| universal flattening of $X$ exists in 11.1                               | unramified in 38.1   |
| universal homeomorphism in 45.1  | unramified in 36.1   |
| universal homeomorphism in 53.2  | V covering of T in 10.7  |
| universal homeomorphism in 15.2  | valuation ring in 50.1   |
| universally S-pure in 16.1   | valuation in 50.13   |
| universally Y-pure in 3.1  | value group in 50.13   |
| universally catenary in 105.3  | value of LF at X in 14.2   |
| universally catenary in 17.1   | value of $RF$ at $X$ in 14.2                                       |
| universally catenary in 25.4   | value in 22.1  |
| universally closed in 17.2   | value in 22.1  |
| universally closed in 20.1   | variety in 3.1   |
| universally closed in 9.2  | variety in 67.9  |
| universally closed in 13.2   | vector bundle $\pi: V \to S$ over $S$ in 6.2                       |
| universally exact in 82.1  | vector bundle associated to $\mathcal{E}$ in 6.1                   |
| *  |  |
| universally injective in 82.1  | versal ring to $\mathcal{X}$ at $x_0$ in 2.2<br>versal in 8.9      |
| universally injective in 10.1  | versal in 12.1   |
| universally injective in 4.5   | versal in 12.1<br>versal in 12.2                                   |
| universally injective in 19.3  | versai in 12.2<br>vertical in 29.1                                 |
| universally injective in 14.2<br>universally Japanese in 162.1           |  |
| universally Japanese in 13.1   | very ample on $X/S$ in 38.1<br>very reasonable in 6.1              |
| universally locally acyclic relative to $K$                              | very reasonable in 17.1  |
| in 93.1  |  |
|  | viewed as an algebraic space over $S'$ in $16.2$                   |
| universally locally acyclic in 93.1                                      |  |
| universally open in 23.1<br>universally open in 6.2                      | viewed as an algebraic stack over $S'$ in 19.2                     |
|  | w-contractible in 11.1   |
| universally open in 11.2   |  |
| universally pure above y in 3.1  | w-local in 2.3 $w$ -local in 2.3                                   |
| universally pure along $X_s$ in 16.1                                     | weak R-orbit in 5.4  |
| universally pure relative to S in 16.1                                   |  |
| universally pure relative to Y in 3.1                                    | weak dimension $\leq d$ in 104.3                                   |
| universally submersive in 24.1   | weak functor in 29.5   |
| universally submersive in 7.2  | weak generator in 36.3   |
| universally submersive in 12.2   | weak ideal of definition in 4.8                                    |
| universally in 7.1<br>unobstructed in 9.1                                | weak normalization of X in Y in 55.6<br>weak normalization in 55.8 |
|  | weak normalization in 55.8<br>weak orbit in 5.4                    |
| unramified at $\mathfrak{q}$ in 151.1<br>unramified at $x \in X$ in 35.1 |  |
| *  | weak Serre subcategory in 10.1                                     |
| unramified at x in 3.5   | weak solution for $A \subset B$ in 115.1                           |
| unramified at $x$ in 38.1  | weaker than the canonical topology in                              |
| unramified cusp form on $GL_2(\mathbf{A})$ with                          | 12.2   |
| values in $\Lambda$ in 31.1  | weaker in 47.8   |
| unramified homomorphism of local rings                                   | weakly R-equivalent in 5.4   |
| in 3.1   | weakly étale in 104.1  |
| unramified with respect to A in 111.7                                    | weakly étale in 64.1   |
| unramified in 151.1  | weakly adic in 7.1   |
| unramified in 35.1   | weakly adic in 9.7   |
|  |  |

| Weil divisor associated to s in 7.4 Weil divisor associated to s in 17.1 Weil divisor associated to a Cartier divisor in 49.1 Weil divisor associated to a rational function $f \in K(X)^*$ in 49.1 Weil divisor class associated to $\mathcal{L}$ in 27.4 Weil divisor class group in 26.7  Zeroth K-group of $\mathcal{D}$ in 28.1 | Weil divisor $[D]$ associated to an effective Cartier divisor $D \subset X$ in 49.1 Zariski in 17.3  Weil divisor associated to $\mathcal{L}$ in 24.1 zero object in 3.3  Weil divisor associated to $\mathcal{L}$ in 17.1 zero scheme in 14.8  Weil divisor associated to $\mathcal{L}$ in 27.4 zero scheme in 7.6  Weil divisor associated to $\mathcal{L}$ in 24.1 zero has a zero | weakly associated in 5.1 weakly associated in 2.2 weakly contractible in 40.2 weakly converges to $H(K)$ in 23.6 weakly converges to $H^*(K^{\bullet})$ in 24.9 weakly converges to $H^n(Tot(K^{\bullet,\bullet}))$ in 25.2  weakly normal in 55.9 weakly pre-adic in 7.1 weakly pre-admissible in 4.8 weakly unramified in 111.1 weakly unramified in 123.1 weakly unramified in 123.1 weighting in 75.2 Weil cohomology theory in 11.4 Weil divisor [D] associated to an effective which associates a presheaf to a semi-representable object in 2.2 which associates a presheaf to a semi-representable object in 2.2 which associates a presheaf to a semi-representable object in 2.2 wild inertia group of $\mathfrak{m}$ in 112.6 Yoneda extension in 27.4  Zariski covering of $X$ in 3.1 Zariski covering in 12.5 Zariski locally quasi-separated over $S$ in 3.2 Zariski locally quasi-separated in 3.1 Zariski pair in 10.1 Zariski sheaf in 4.3 Zariski topos in 21.1 Zariski, étale, smooth, syntomic, or fppf covering in 8.4 | weakly admissible in 4.8Weil divisor class group in 6.9weakly associated points of X in 5.1Weil divisor in 26.2weakly associated points of X in 2.2Weil divisor in 6.2weakly associated in 66.1Weil divisor in 49.1 |
|--|--|---|---|
|--|--|---|---|

## 2. Definitions listed per chapter

| Introduction  | In 2.8: functor<br>In 2.9: faithful, fully faithful, essentially                   |
|---|--|
| Conventions   | surjective   |
| Set Theory  | In 2.10: subcategory, full subcategory, strictly full                              |
| Categories  | In 2.15: natural transformation, morphism of functors                              |
| In 2.1: category In 2.4: isomorphism In 2.5: groupoid | In 2.17: equivalence of categories, quasi-<br>inverse<br>In 2.20: product category |

In 3.1: opposite category

In 3.2: contravariant

In 3.3: presheaf of sets on C, presheaf

In 3.6: representable

In 4.1: product

In 4.2: has products of pairs of objects

In 5.1: coproduct, amalgamated sum

In 5.2: has coproducts of pairs of objects

In 6.1:  $fibre\ product$ 

In 6.2: cartesian

In 6.3: has fibre products

In 6.4: representable

In 8.2: representable, F is relatively rep

 $resentable\ over\ G$ 

In 9.1: pushout In 9.2: cocartesian

In 10.1: equalizer

In 11.1: coequalizer

In 12.1: initial, final

In 13.1: monomorphism, epimorphism

In 14.1: *limit* 

In 14.2: colimit

In 14.6: product

In 14.7: coproduct

In 16.1: connected

In 17.1:  $\mathcal{I}$  is cofinal in  $\mathcal{J}$ , cofinal

In 17.3:  $\mathcal{I}$  is initial in  $\mathcal{J}$ , initial

In 19.1: directed, filtered, directed, filtered

In 20.1: codirected, cofiltered, codirected, cofiltered

In 21.1: preorder, preordered set, directed set, partial order, partially ordered set, directed partially ordered set

In 21.2: system over I in C, inductive system over I in C, inverse system over Iin C, projective system over I in C, transition maps

In 21.4: directed system, directed inverse system

In 22.1: essentially constant, value, essentially constant, value

In 22.2: essentially constant system, essentially constant inverse system

In 23.1: left exact, right exact, exact In 24.1: left adjoint, right adjoint

In 26.1: categorically compact

In 27.1: left multiplicative system, right multiplicative system, multiplicative system

In 27.4:  $s^{-1}f$ 

In 27.12:  $fs^{-1}$ 

In 27.20: saturated

In 28.1: horizontal

In 29.1: 2-category, 1-morphisms, 2-morphisms, vertical, composition, hori-

zontal In 29.2: sub 2-category

In 29.4: equivalent

In 29.5: functor, weak functor, pseudo

functor

In 30.1: (2,1)-category

In 31.1: final object

In 31.2: 2-fibre product of f and g

In 32.1: 2-category of categories over  $\mathcal{C}$ 

In 32.2: fibre category, lift, x lies over U,

lift,  $\phi$  lies over f

In 33.1: strongly cartesian morphism,

strongly C-cartesian morphism In 33.5: fibred category over C

In 33.6: choice of pullbacks, pullback

functor

In 33.9: 2-category of fibred categories

over C

In 34.2: relative inertia of S over S', inertia fibred category  $I_S$  of S

In 35.1: fibred in groupoids

In 35.6: 2-category of categories fibred in groupoids over  $\mathcal{C}$ 

In 36.2: split fibred category,  $S_F$ 

In 37.2: split category fibred in groupoids,  $S_F$ 

In 38.1: discrete

In 38.2: category fibred in sets, category

fibred in discrete categories

In 38.3: 2-category of categories fibred in sets over C

In 39.1: setoid

In 39.2: category fibred in setoids

In 39.3: 2-category of categories fibred in setoids over C

In 40.1: representable

In 42.3: representable,  ${\mathcal X}$  is relatively rep-

resentable over  $\mathcal{Y}$ 

In 43.1: monoidal category

In 43.2: functor of monoidal categories

In 43.4: invertible

In 43.5: left dual, right dual

In 43.9: symmetric monoidal category

In 43.11: functor of symmetric monoidal categories

In 44.1: morphism of dotted arrows

### Topology

In 4.1: separated

In 5.1: base for the topology on X, basis for the topology on X

In 5.4: subbase for the topology on X, subbasis for the topology on X

In 6.3: strict map of topological spaces, submersive

In 7.1: connected, connected component

In 7.8: totally disconnected

In 7.10: locally connected

In 8.1: irreducible, irreducible component

In 8.6: generic point, Kolmogorov, quasisober, sober

In 9.1: Noetherian, locally Noetherian

In 10.1: chain of irreducible closed subsets, length, dimension, Krull dimension, Krull dimension of X at x

In 10.5: equidimensional

In 11.1: codimension

In 11.4: catenary

In 12.1: quasi-compact, quasi-compact, retrocompact

In 13.1: locally quasi-compact

In 15.1: constructible, locally constructible

In 17.2: closed, Bourbaki-proper, quasi-proper, universally closed, proper

In 18.1: Jacobson

In 19.1: specialization, generalization, stable under specialization, stable under generalization

In 19.4: specializations lift along f, specializing, generalizations lift along f, generalizing

In 20.1: immediate specialization, dimension function

In 21.1: interior, nowhere dense

In 22.1: profinite

In 23.1: spectral, spectral

In 26.1: extremally disconnected

In 27.2: isolated point

In 28.1: partition, parts, refines

In 28.2: good stratification

In 28.3: stratification, strata

In 28.4: locally finite

In 30.1: topological group, homomorphism of topological groups

In 30.5: profinite group

In 30.7: topological ring, homomorphism of topological rings

In 30.10: topological module, homomorphism of topological modules

# Sheaves on Spaces

In 3.1: presheaf  $\mathcal{F}$  of sets on X, morphism  $\varphi: \mathcal{F} \to \mathcal{G}$  of presheaves of sets on X

In 3.2: constant presheaf with value A

In 4.4: presheaf of abelian groups on X, abelian presheaf over X, morphism of abelian presheaves over X

In 5.1: presheaf  $\mathcal{F}$  on X with values in  $\mathcal{C}$ , morphism  $\varphi: \mathcal{F} \to \mathcal{G}$  of presheaves with value in  $\mathcal{C}$ 

In 5.2: underlying presheaf of sets of  $\mathcal{F}$ 

In 6.1: presheaf of  $\mathcal{O}$ -modules, morphism  $\varphi: \mathcal{F} \to \mathcal{G}$  of presheaves of  $\mathcal{O}$ -modules

In 7.1: sheaf  $\mathcal{F}$  of sets on X, morphism of sheaves of sets

In 7.4: constant sheaf with value A

In 8.1: abelian sheaf on X, sheaf of abelian groups on X

In 9.1: sheaf

In 10.1: sheaf of  $\mathcal{O}$ -modules, morphism of sheaves of  $\mathcal{O}$ -modules

In 11.2: separated

In 15.1: type of algebraic structure

In 16.2: subpresheaf, subsheaf, injective, surjective, injective, surjective

In 21.7: f-map  $\xi: \mathcal{G} \to \mathcal{F}$ 

In 21.9: composition of  $\varphi$  and  $\psi$ 

In 25.1:  $ringed\ space,\ morphism\ of\ ringed\ spaces$ 

In 25.3: composition of morphisms of ringed spaces

In 26.1: pushforward, pullback

In 27.1: skyscraper sheaf at x with value A, skyscraper sheaf, skyscraper sheaf, skyscraper sheaf

In 30.1: presheaf  $\mathcal{F}$  of sets on  $\mathcal{B}$ , morphism  $\varphi: \mathcal{F} \to \mathcal{G}$  of presheaves of sets

In 30.2: sheaf  $\mathcal{F}$  of sets on  $\mathcal{B}$ , morphism of sheaves of sets on  $\mathcal{B}$ 

In 30.8: presheaf  $\mathcal{F}$  with values in  $\mathcal{C}$  on  $\mathcal{B}$ , morphism  $\varphi: \mathcal{F} \to \mathcal{G}$  of presheaves with values in C on B, sheaf F with values in C on B

In 30.11: presheaf of  $\mathcal{O}$ -modules  $\mathcal{F}$  on  $\mathcal{B}$ , morphism  $\varphi: \mathcal{F} \to \mathcal{G}$  of presheaves of  $\mathcal{O}$ -modules on  $\mathcal{B}$ , sheaf  $\mathcal{F}$  of  $\mathcal{O}$ -modules

In 31.2: restriction of  $\mathcal{G}$  to U, restriction of  $\mathcal{G}$  to U, open subspace of  $(X,\mathcal{O})$  associated to U, restriction of  $\mathcal{G}$  to U

In 31.3: extension of  $\mathcal{F}$  by the empty set  $j_{n!}\mathcal{F}$ , extension of  $\mathcal{F}$  by the empty set  $j_!\mathcal{F}$ In 31.5: extension  $j_{p!}\mathcal{F}$  of  $\mathcal{F}$  by 0, extension  $j_!\mathcal{F}$  of  $\mathcal{F}$  by 0, extension  $j_{p!}\mathcal{F}$  of  $\mathcal{F}$ by e, extension  $j_!\mathcal{F}$  of  $\mathcal{F}$  by e, extension by 0, extension by 0

### Sites and Sheaves

In 2.1: presheaf of sets, Morphisms of presheaves

In 2.2: presheaf, morphism

In 3.1: injective, surjective

In 3.3: subpresheaf

In 3.5: image of  $\varphi$ 

In 6.1: family of morphisms with fixed target

In 6.2: site, coverings of C

In 7.1: sheaf

In 7.5:  $Sh(\mathcal{C})$ In 7.6: sheaf

In 8.1: morphism of families of maps with fixed target of C from U to V, morphism from  $\mathcal{U}$  to  $\mathcal{V}$ , refinement

In 8.2: combinatorially equivalent, tautologically equivalent

In 10.9: separated

In 10.11: sheaf associated to  $\mathcal{F}$ 

In 11.1: injective, surjective

In 12.1: effective epimorphism, universal effective epimorphism

In 12.2: weaker than the canonical topology, subcanonical

In 12.3: representable sheaves, U

In 13.1: continuous

In 14.1: morphism of sites

In 14.5: composition

In 15.1: topos, morphism of topoi, composition  $f \circ q$ 

In 17.1: quasi-compact

In 17.4: quasi-compact, quasi-compact

In 20.1: cocontinuous

In 25.1: localization of the site C at the object U, localization morphism, direct image functor, restriction of  $\mathcal{F}$  to  $\mathcal{C}/U$ , extension of G by the empty set

In 29.2: special cocontinuous functor u from C to D

In 30.4: localization of the topos  $Sh(\mathcal{C})$  at

 $\mathcal{F}$ , localization morphism In 32.1: point of the topos  $Sh(\mathcal{C})$ 

In 32.2: point p of the site C

In 32.6: skyscraper sheaf

In 36.1: 2-morphism from f to q

In 37.2: morphism  $f: p \to p'$ 

In 38.1: conservative, has enough points In 40.2: weakly contractible, enough weakly contractible objects, enough P ob*jects* 

In 42.1: sheaf theoretically empty

In 42.3: almost cocontinuous

In 43.1: embedding In 43.2: subtopos

In 43.4: open subtopos

In 43.6: closed subtopos

In 43.7: open immersion, closed immersion

In 44.1: pushforward

In 45.1: qlobal sections

In 47.1: sieve S on U

In 47.3: sieve on U generated by the morphisms  $f_i$ 

In 47.4: pullback of S by f

In 47.6: topology on C

In 47.8: finer, stronger, coarser, weaker

In 47.10: *sheaf* 

In 47.12: canonical topology

In 48.2: topology associated to C

In 49.2: separated

In 49.4: sheaf associated to  $\mathcal{F}$ 

In 52.1: point p

#### Stacks

In 2.2: presheaf of morphisms from x to y, presheaf of isomorphisms from x to y In 3.1: descent datum  $(X_i, \varphi_{ij})$  in S relative to the family  $\{f_i : U_i \to U\}$ , cocycle condition, morphism  $\psi : (X_i, \varphi_{ij}) \to (X'_i, \varphi'_{ij})$  of descent data

In 3.4: pullback functor

In 3.5: trivial descent datum, canonical descent datum, effective

In 4.1: stack

In 4.5: 2-category of stacks over C

In 5.1: stack in groupoids

In 5.5: 2-category of stacks in groupoids over  $\mathcal{C}$ 

In 6.1: stack in setoids, stack in sets, stack in discrete categories

In 6.5: 2-category of stacks in setoids over C

In 10.2: structure of site on S inherited from C, S is endowed with the topology inherited from C

In 11.1: gerbe

In 11.4: gerbe over

In 12.4:  $f_*S$ , pushforward of S along f In 12.9:  $f^{-1}S$ , pullback of S along f

# Fields

In 2.1: field, subfield

In 2.2: domain, integral domain

In 5.1: characteristic, prime subfield of F

In 6.2: field extension

In 6.3: tower

In 6.6: generates the field extension, finitely generated field extension

In 7.1: degree, finite

In 7.8: number field

In 8.1: algebraic, algebraic extension

In 9.1: minimal polynomial

In 10.1: algebraically closed

In 10.3: algebraic closure

In 11.1: relatively prime

In 12.2: separable, separable, separable

In 12.6: separable degree

In 14.1: purely inseparable, purely inseparable

In 14.7: separable degree, inseparable degree, degree of inseparability

In 15.1: normal

In 15.8: automorphisms of E over F, automorphisms of E/F

In 16.2: splitting field of P over F

In 16.4:  $normal\ closure\ E\ over\ F$ 

In 20.1: trace, norm

In 20.6: trace pairing

In 20.8: discriminant of L/K

In 21.1: Galois

In 21.3: Galois group

In 26.1: algebraically independent, purely transcendental extension, transcendence basis

In 26.4: transcendence degree

In 26.9: algebraic closure of k in K, al-

 $gebraically\ closed\ in\ K$ 

In 27.1: compositum of K and L in  $\Omega$ 

In 27.2: linearly disjoint over k in  $\Omega$ 

In 28.1: algebraic, separable, purely inseparable, normal, Galois

### Commutative Algebra

In 5.1: finite R-module, finitely generated R-module, finitely presented R-module, R-module of finite presentation

In 6.1: finite type, S is a finite type Ralgebra, finite presentation

In 7.1: finite

In 8.1: system  $(M_i, \mu_{ij})$  of R-modules over I, directed system

In 8.6: homomorphism of systems

In 9.1: multiplicative subset of R

In 9.2: localization of A with respect to S

In 9.6: localization

In 11.2: relation

In 12.1: R-bilinear

In 12.6: (A, B)-bimodule

In 14.1: base change, base change

In 17.1: spectrum

In 17.3: Zariski, standard opens

In 18.1: local ring, local homomorphism of local rings, local ring map  $\varphi: R \to S$ 

In 28.2: Oka family

In 32.1: locally nilpotent, nilpotent

In 35.1: Jacobson ring

In 36.1: integral over R, integral

In 36.9: integral closure, integrally closed

In 37.1: normal

In 37.3: almost integral over R, completely normal

sequence

affine blowup algebra

In 70.1: blowup algebra, Rees algebra,

In 37.11: normal In 71.2: resolution, resolution of M by In 38.1: integral over I free R-modules, resolution of M by finite In 39.1: flat, faithfully flat, flat, faithfully free R-modules In 72.1: I-depth, depth In 40.1: support of MIn 77.1: projective In 78.1: locally free, finite locally free, fi-In 40.3: annihilator of m, annihilator of nite locally free of rank r MIn 41.1: going up, going down In 82.1: universally injective, universally In 42.1: separably generated over k, sep $arable\ over\ k$ In 84.1: direct sum dévissage, Kaplansky In 43.1: geometrically reduced over k $d\acute{e}vissage$ In 45.1: perfect In 86.1: Mittag-LefflerIn 45.5: perfect closure In 88.1: Mittag-Leffler directed system of In 47.4: geometrically irreducible over kmodulesIn 48.3: geometrically connected over k In 88.2: dominates In 49.1: geometrically integral over kIn 88.7: Mittag-Leffler In 50.1: dominates, valuation ring, cen-In 90.1: coherent module, coherent ring In 96.2: I-adically complete, I-adically teredIn 50.13: value group, valuation, discrete completeIn 102.5: rankvaluation ring In 52.1: length In 103.1: Cohen-Macaulay In 52.9: simple In 103.8: maximal Cohen-Macaulay In 53.1: Artinian In 103.12: Cohen-Macaulay In 54.1: essentially of finite type, essen-In 104.1: Cohen-Macaulay tially of finite presentation In 104.6: Cohen-Macaulay In 57.1: homogeneous spectrum In 105.1: catenary In 58.3: numerical polynomial In 105.3: universally catenary In 59.1: an ideal of definition of R In 108.1: pure In 59.6: Hilbert polynomial In 109.2: finite projective dimension, pro-In 59.8: d(M)jective dimension In 60.1: chain of prime ideals, length In 109.10: finite global dimension, global In 60.2: Krull dimension dimensionIn 60.3: height In 110.7: regularIn 60.10: system of parameters of R, req-In 112.5: local ring of the fibre at  $\mathfrak{q}$ ular local ring, regular system of param-In 119.8: uniformizer In 120.1: associates, irreducible, prime etersIn 120.4: unique factorization domain, In 63.1: associated In 64.1: symbolic power UFDIn 65.2: relative assassin of N over S/RIn 120.12: principal ideal domain, PID In 120.14: Dedekind domain In 66.1: weakly associated In 67.1: embedded associated primes, em-In 121.2: order of vanishing along R bedded primes of R In 121.3: lattice in VIn 68.1: M-regular sequence, M-regular In 121.5: distance between M and M'sequence in I, regular sequenceIn 122.3: quasi-finite at  $\mathfrak{q}$ , quasi-finite In 69.1: M-quasi-regular, quasi-regular In 123.7: strongly transcendental over R

In 125.1: relative dimension of S/R at  $\mathfrak{q}$ ,

relative dimension of

In 131.1: derivation, R-derivation,  $Leibniz\ rule$ In 131.2: module of Kähler differentials, module of differentials
In 133.1: differential operator  $D:M\to N$  of order kIn 133.4: module of principal parts of order kIn 134.1: naive cotangent complex

In 135.1: global complete intersection over k, local complete intersection over k

In 135.5: complete intersection (over k) In 136.1: syntomic, flat local complete intersection over R

In 136.5: relative global complete intersection

In 137.1: smooth

In 137.6:  $standard\ smooth\ algebra\ over\ R$ 

In 137.11: smooth at  $\mathfrak{q}$ 

In 138.1: formally smooth over R

In 141.1:  $small\ extension$ In 143.1:  $\acute{e}tale$ ,  $\acute{e}tale\ at\ \mathfrak{q}$ In 144.1:  $standard\ \acute{e}tale$ 

In 148.1: formally unramified over R In 149.2: universal first order thickening,

conormal module,  $C_{S/R}$ 

In 150.1: formally étale over R

In 151.1: unramified, G-unramified, unramified at  $\mathfrak q$  , G-unramified at  $\mathfrak q$ 

In 153.1: henselian, strictly henselian

In 155.3: henselization, strict henselization of R with respect to  $\kappa \subset \kappa^{sep}$ , strict henselization

In 157.1:  $(R_k)$ , regular in codimension  $\leq k$ ,  $(S_k)$ 

In 160.1: complete local ring In 160.4: coefficient ring In 160.5: Cohen ring

In 161.1: N-1, N-2, Japanese

In 162.1: universally Japanese, Nagata ring

In 162.9: analytically unramified, analytically unramified

In 165.2: geometrically normal In 166.2: geometrically regular

#### Brauer groups

In 2.1: finite

In 2.2: skew field

In 2.3: simple, simple

In 2.4: central

In 2.5: opposite algebra In 5.2: Brauer group

In 8.1: splits, splitting field

# Homological Algebra

In 3.1: preadditive, additive

In 3.3: zero object In 3.5: direct sum

In 3.8: additive In 3.9: kernel, cokernel, coimage of f, im-

age of f

In 4.1: Karoubian

In 5.1: abelian

In 5.3: injective, surjective, subobject, quotient

In 5.7: complex, exact at y, exact at  $x_i$ , exact, exact sequence, exact complex, short exact sequence

In 5.9: split

In 6.1:  $extension\ E\ of\ B\ by\ A,\ morphism$ 

of extensions In 6.2: Ext-group

In 9.1: simple

In 9.2: Artinian, Artinian

In 9.3: Noetherian, Noetherian

In 10.1: Serre subcategory, weak Serre subcategory

In 10.5: kernel of the functor FIn 11.1: zeroth K-group of A

In 12.1: cohomological  $\delta$ -functor,  $\delta$ -functor

In 12.2: morphism of  $\delta$ -functors from F to G

In 12.3: universal  $\delta$ -functor

In 13.2: homotopy equivalence, homotopy equivalent

In 13.4: quasi-isomorphism, acyclic

 $\begin{array}{l} \text{In 13.8: } homotopy \ equivalence, homotopy \\ equivalent \end{array}$ 

In 13.10: quasi-isomorphism, acyclic

In 14.1: k-shifted chain complex  $A[k]_{\bullet}$ 

In 14.2:  $H_{i+k}(A_{\bullet}) \to H_i(A[k]_{\bullet})$ 

In 14.7: k-shifted cochain complex  $A[k]^{\bullet}$ 

In 14.8:  $H^{i+k}(A^{\bullet}) \longrightarrow H^{i}(A[k]^{\bullet})$ 

In 16.1: category of graded objects of A

In 16.4: shift

In 17.1: additive monoidal category

In 18.1: double complex

In 18.3: associated simple complex, associated total complex

In 19.1: decreasing filtration, filtered object of A, morphism  $(A, F) \rightarrow (B, F)$  of filtered objects, induced filtration, quotient filtration, finite, separated, exhaustive

In 19.3: strict

In 20.1: spectral sequence in A, morphism of spectral sequences

In 20.2: limit, degenerates at  $E_r$ 

In 21.1: exact couple, morphism of exact couples

In 21.3: spectral sequence associated to the exact couple

In 22.1: differential object, morphism of differential objects

In 22.3: homology

In 22.5: spectral sequence associated to  $(A, d, \alpha)$ 

In 23.1: filtered differential object

In 23.4: induced filtration

In 23.6: weakly converges to H(K), abuts to H(K)

In 24.1: filtered complex  $K^{\bullet}$  of A

In 24.5: induced filtration

In 24.7: regular, coregular, bounded, bounded below, bounded above

In 24.9: weakly converges to  $H^*(K^{\bullet})$ , abuts to  $H^*(K^{\bullet})$ , converges to  $H^*(K^{\bullet})$ 

In 25.2: weakly converges to  $H^n(Tot(K^{\bullet,\bullet}))$ , abuts to  $H^n(Tot(K^{\bullet,\bullet}))$ , converges to  $H^n(Tot(K^{\bullet,\bullet}))$ , weakly converges to  $H^n(Tot(K^{\bullet,\bullet}))$ , abuts to  $H^n(Tot(K^{\bullet,\bullet}))$ , converges to  $H^n(Tot(K^{\bullet,\bullet}))$ 

In 27.1: injective

In 27.4: enough injectives

In 27.5: functorial injective embeddings

In 28.1: projective

In 28.4: enough projectives

In 28.5: functorial projective surjections

In 31.2: Mittag-Leffler condition, ML

### **Derived Categories**

In 3.1: triangle, morphism of triangles

In 3.2: triangulated category, distinguished triangles, pre-triangulated category

In 3.3: exact functor, triangulated functor

In 3.4: pre-triangulated subcategory, triangulated subcategory

In 3.5: homological, cohomological

In 3.6:  $\delta$ -functor from A to D, image of the short exact sequence under the given  $\delta$ -functor

In 5.1: compatible with the triangulated structure

In 6.1: saturated

In 6.5: kernel of F, kernel of H

In 6.7: quotient category  $\mathcal{D}/\mathcal{B}$ , quotient functor

In 8.1: category of (cochain) complexes, bounded below, bounded above, bounded

In 9.1: cone

In 9.4: termwise split injection  $\alpha: A^{\bullet} \to B^{\bullet}$ , termwise split surjection  $\beta: B^{\bullet} \to C^{\bullet}$ 

In 9.9: termwise split exact sequence of complexes of A, triangle associated to the termwise split sequence of complexes

In 10.1: distinguished triangle of K(A)

In 11.3: derived category of A, bounded derived category

In 13.1: category of finite filtered objects of A

In 13.2: filtered quasi-isomorphism, filtered acyclic

In 13.5: filtered derived category of A

In 13.7: bounded filtered derived category In 14.2: right derived functor RF is defined at, value of RF at X, left derived functor LF is defined at, value of LF at X

In 14.9: right derivable, everywhere defined, left derivable, everywhere defined

In 14.10: computes, computes

In 15.3: right derived functors of F, left derived functors of F, right acyclic for F, acyclic for RF, left acyclic for F, acyclic for LF

In 16.2: ith right derived functor  $R^iF$  of F

In 18.1: injective resolution of A, injective resolution of  $K^{\bullet}$ 

In 19.1: projective resolution of A, projective resolution of  $K^{\bullet}$ 

In 21.1: Cartan-Eilenberg resolution

In 23.2: resolution functor

In 26.1: filtered injective

In 27.1: ith extension group

In 27.4: Yoneda extension, equivalent

In 28.1: zeroth K-group of  $\mathcal{D}$ 

In 31.1: K-injective

In 33.1: derived colimit, homotopy colimit

In 34.1: derived limit, homotopy limit

In 36.3: classical generator, strong generator, weak generator, generator

In 37.1: compact object

In 37.5: compactly generated

In 40.1: right orthogonal, left orthogonal

In 40.9: right admissible, left admissible, two-sided admissible

In 41.1: Postnikov system, morphism of Postnikov systems

### Simplicial Methods

In 2.1:  $\delta_j^n : [n-1] \to [n], \ \sigma_j^n : [n+1] \to [n]$ 

In 3.1: simplicial object U of C, simplicial set, simplicial abelian group, morphism of simplicial objects  $U \to U'$ , category of simplicial objects of C

In 5.1: cosimplicial object U of C, cosimplicial set, cosimplicial abelian group, morphism of cosimplicial objects  $U \rightarrow U'$ , category of cosimplicial objects of C

In 6.1: product of U and V

In 7.1: fibre product of V and W over U

In 8.1: pushout of V and W over U

In 9.1: product of U and V

In 10.1: fibre product of V and W over

In 11.1: n-simplex of U, face of x, degeneracy of x, degenerate

In 12.1: n-truncated simplicial object of C, morphism of n-truncated simplicial objects

In 13.1:  $product \ U \times V \ of \ U \ and \ V$ ,  $product \ U \times V \ exists$ 

In 14.1:  $\operatorname{Hom}(U, V)$ 

In 15.1:  $\operatorname{Hom}(U, V)$ 

In 17.1:  $\operatorname{Hom}(U, V)$ 

In 18.1: split, split

In 20.1: augmentation  $\epsilon: U \to X$  of U towards an object X of C

In 22.3: Eilenberg-Maclane object K(A, k)

In 26.1: homotopy from a to b, homotopic, in the same homotopy class

In 26.6: homotopy equivalence, homotopy equivalent

In 28.1: homotopy from a to b, homotopic, in the same homotopy class

In 30.1: trivial Kan fibration

In 31.1: Kan fibration, Kan complex

# More on Algebra

In 3.1: stably isomorphic, stably free

In 8.3:  $kth\ Fitting\ ideal$ 

In 10.1: Zariski pair

In 11.1: henselian pair

In 14.1: absolutely integrally closed

In 15.1: auto-associated

In 22.1: torsion, torsion free

In 23.1: reflexive

In 23.9: reflexive hull

In 24.1: content ideal of x

In 26.1: strict transform of M along  $R \to R[\frac{I}{a}]$ 

In 28.1:  $Koszul\ complex$ 

In 28.2: Koszul complex on  $f_1, \ldots, f_r$ 

In 30.1: M-Koszul-regular, M- $H_1$ -regular, Koszul-regular,  $H_1$ -regular

In 32.1: regular ideal, Koszul-regular ideal,  $H_1$ -regular ideal, quasi-regular ideal

In 33.2: local complete intersection

In 36.1: topological ring, topological module, homomorphism of topological modules, homomorphism of topological rings, linearly topologized, linearly topologized, ideal of definition, pre-admissible, admissible, pre-adic, adic

In 37.1: formally smooth over R

In 37.3: formally smooth for the  $\mathfrak{n}$ -adic topology

In 41.1: regular

In 46.1: p-independent over  $k,\ p$ -basis of

K over k

In 47.1: *J-0*, *J-1*, *J-2* 

In 50.1: *G-ring* 

In 52.1: quasi-excellent, excellent

In 55.1: injective

In 55.5:  $M \mapsto M^{\vee}$ , free module

In 59.1: K-flat

In 59.13: derived tensor product

In 61.1: Tor independent over R

In 64.1: m-pseudo-coherent, pseudo-coherent, m-pseudo-coherent, pseudo-coherent

In 66.1: tor-amplitude in [a,b], finite tor dimension, tor dimension  $\leq d$ , finite tor dimension

In 68.1: finite projective dimension, projective-amplitude in [a, b]

In 69.1: finite injective dimension, injective-amplitude in [a, b]

In 70.4: *I-projective* 

In 74.1: perfect, perfect

In 80.2: finitely presented relative to R In 81.4: m-pseudo-coherent relative to R, p-seudo-coherent relative to R, m-pseudo-coherent relative to R, p-seudo-coherent relative to R

In 82.1: pseudo-coherent ring map, perfect ring map

In 83.1: R-perfect, perfect relative to R In 88.1: I-power torsion module, an fpower torsion module

In 91.4: derived complete with respect to I, derived complete with respect to I

In 104.1: absolutely flat, weakly étale, absolutely flat

In 104.3: weak dimension  $\leq d$ 

In 106.1: unibranch, geometrically unibranch

In 106.6: number of branches of A, number of geometric branches of A

In 109.1: formally catenary

In 111.1: extension of discrete valuation rings, ramification index, weakly unramified, residual degree, residue degree

In 111.7: unramified with respect to A, tamely ramified with respect to A, totally ramified with respect to A

In 112.3: decomposition group of  $\mathfrak{m}$ , inertia group of  $\mathfrak{m}$ 

In 112.6: wild inertia group of  $\mathfrak{m}$ , tame inertia group of  $\mathfrak{m}$ 

In 113.3: mixed characteristic, absolute ramification index

In 115.1: weak solution for  $A \subset B$ , solution for  $A \subset B$ , separable solution

In 117.1: invertible, trivial

In 123.1: extension of valuation rings, weakly unramified, residual degree, residue degree

In 124.5: Bézout domain, elementary divisor domain

# Smoothing Ring Maps

In 2.1: singular ideal of A over R In 2.3: elementary standard in A over R, strictly standard in A over R

#### **Sheaves of Modules**

In 4.1: generated by global sections, generate

In 4.5: subsheaf generated by the  $s_i$ 

In 5.1: support of  $\mathcal{F}$ , support of s

In 8.1: locally generated by sections

In 9.1: finite type

In 10.1: quasi-coherent sheaf of  $\mathcal{O}_X$ -modules

In 10.6: sheaf associated to the module M and the ring map  $\alpha$ , sheaf associated to the module M

In 11.1: finite presentation

In 12.1: coherent  $\mathcal{O}_X$ -module

In 13.1: closed immersion of ringed spaces

In 14.1: locally free, finite locally free, finite locally free of rank r

In 17.1: flat

In 17.3: flat at x

In 20.1: flat at x, flat

In 20.3: flat over Y at a point  $x \in X$ , flat over Y

In 23.1: annihilator

In 24.1: Koszul complex

In 24.2: Koszul complex on  $f_1, \ldots, f_r$ 

In 25.1: invertible  $\mathcal{O}_X$ -module, trivial

In 25.6: tensor power

In 25.7: associated graded ring

In 25.9: Picard group

In 28.1:  $\mathcal{O}_1$ -derivation,  $\varphi$ -derivation, Leibniz rule

In 28.3: module of differentials, universal  $\varphi$ -derivation

In 28.10: S-derivation, sheaf of differentials  $\Omega_{X/S}$  of X over S

In 29.1: differential operator  $D: \mathcal{F} \to \mathcal{G}$  of order k

In 29.4: module of principal parts of order k

In 29.8: differential operator of order k on X/S

In 30.1: de Rham complex of  $\mathcal{B}$  over  $\mathcal{A}$ 

In 30.4: de Rham complex

In 31.1: naive cotangent complex

In 31.6: naive cotangent complex

### Modules on Sites

In 4.1: free abelian presheaf In 5.1: free abelian sheaf

In 6.1: ringed site, structure sheaf, morphism of ringed sites, composition of morphisms of ringed sites

In 7.1: ringed topos, structure sheaf, morphism of ringed topoi, composition of morphisms of ringed topoi

In 8.1: 2-morphism from f to q

In 9.1: presheaf of  $\mathcal{O}$ -modules, morphism  $\varphi: \mathcal{F} \to \mathcal{G}$  of presheaves of  $\mathcal{O}$ -modules

In 10.1: sheaf of  $\mathcal{O}$ -modules, morphism of sheaves of  $\mathcal{O}$ -modules

In 13.1: pushforward, pullback

In 16.1:  $g_{p!}\mathcal{F}, g_!\mathcal{F} = (g_{p!}\mathcal{F})^{\#}$ 

In 17.1: free O-module, finite free, generated by global sections, generated by r global sections, generated by finitely many global sections, global presentation, global finite presentation

In 19.1: localization of the ringed site  $(C, \mathcal{O})$  at the object U, localization morphism, direct image functor, restriction of  $\mathcal{F}$  to C/U, extension by zero

In 21.2: localization of the ringed topos  $(Sh(C), \mathcal{O})$  at  $\mathcal{F}$ , localization morphism In 23.1: locally free, finite locally free, locally generated by sections, locally generated by r sections, of finite type, quasicoherent, of finite presentation, coherent In 28.1: flat, flat, flat, flat

In 31.1: flat, flat

In 31.3: flat over  $(Sh(\mathcal{D}), \mathcal{O}')$ 

In 32.1: rank r, invertible,  $\mathcal{O}^*$ 

In 32.6: Picard group

In 33.1:  $\mathcal{O}_1$ -derivation,  $\varphi$ -derivation, Leibniz rule

In 33.3: module of differentials, universal  $\varphi$ -derivation

In 33.10: Y-derivation, sheaf of differentials  $\Omega_{X/Y}$  of X over Y, universal Y-derivation

In 34.1: differential operator  $D: \mathcal{F} \to \mathcal{G}$  of order k

In 34.4: module of principal parts of order k

In 35.1: naive cotangent complex

In 35.4: naive cotangent complex

In 40.4: locally ringed site

In 40.6: locally ringed

In 40.9: morphism of locally ringed topoi, morphism of locally ringed sites

In 43.1: constant sheaf, locally constant, finite locally constant

#### **Injectives**

In 2.4:  $\alpha$ -small with respect to I

In 10.1: generator, Grothendieck abelian category

In 11.2: *size* 

### Cohomology of Sheaves

In 4.1: torsor, G-torsor, morphism of G-torsors, trivial G-torsor

In 9.1:  $\check{C}ech\ complex,\ \check{C}ech\ cohomology$  groups

In 12.1: flasque, flabby

In 23.1: alternating Čech complex

In 23.2: ordered Čech complex

In 24.2: locally finite

In 26.2: K-flat

In 26.14: derived tensor product

In 26.15: *Tor* 

In 46.1: strictly perfect

In 47.1: m-pseudo-coherent, pseudo-coherent, m-pseudo-coherent, pseudo-coherent

In 48.1: tor-amplitude in [a, b], finite tor dimension, locally has finite tor dimension, tor dimension  $\leq d$ 

In 49.1: perfect, perfect

### Cohomology on Sites

In 4.1: pseudo torsor, pseudo  $\mathcal{G}$ -torsor, morphism of pseudo  $\mathcal{G}$ -torsors, torsor,  $\mathcal{G}$ -torsor, morphism of  $\mathcal{G}$ -torsors, trivial  $\mathcal{G}$ -torsor

In 8.1: Čech complex, Čech cohomology groups

In 13.4: totally acyclic

In 17.2: K-flat

In 17.13: derived tensor product

In 17.14: Tor

In 31.2: qc covering

In 41.1: simplicial  $A_{\bullet}$ -module, simplicial sheaf of  $A_{\bullet}$ -modules

In 43.1:  $QC(\mathcal{O})$ 

In 44.1: strictly perfect

In 45.1: m-pseudo-coherent, pseudo-coherent, m-pseudo-coherent, pseudo-coherent

In 46.1: tor-amplitude in [a,b], finite tor dimension, locally has finite tor dimension, tor dimension  $\leq d$ 

In 47.1: perfect, perfect

## Differential Graded Algebra

In 3.1: differential graded algebra over R In 3.2: homomorphism of differential graded algebras

In 3.3: commutative, strictly commutative

In 3.4: tensor product differential graded algebra

In 4.1: differential graded module, homomorphism of differential graded modules In 4.3: k-shifted module

In 5.1: homotopy between f and g, homotopic

In 5.3: homotopy category

In 6.1: cone

In 7.1: admissible monomorphism, admissible epimorphism, admissible short exact sequence

In 8.2: triangle associated to  $0 \to K \to L \to M \to 0$ , distinguished triangle

In 11.1: opposite differential graded algebra

In 11.3: kth shifted A-module, kth shifted A-module

In 22.2: derived category of (A, d)

In 24.1: R-linear category A

In 24.2: functor of R-linear categories, R-linear functor

In 25.1: graded category A over R

In 25.2: functor of graded categories over R, graded functor

In 25.3:  $A^0$ 

In 25.4: graded direct sum

In 26.1: differential graded category A over R

In 26.2: functor of differential graded categories over R

In 26.3: category of complexes of A, homotopy category of A

In 26.4: differential graded direct sum In 28.1: (A, B)-bimodule, graded (A, B)-bimodule, differential graded (A, B)-bimodule

# Divided Power Algebra

In 2.1: divided power structure

In 3.1: divided power ring, homomorphism of divided power rings

In 4.1: extends

In 6.1: divided power structure

In 6.5: compatible with the differential graded structure

In 8.5: complete intersection, local complete intersection

#### Differential Graded Sheaves

In 3.1: sheaf of graded O-algebras, sheaf of graded algebras, homomorphism of graded O-algebras

In 4.1: graded A-module, graded module, homomorphism of graded A-modules

In 8.1: graded (A, B)-bimodule, homomorphism of graded (A, B)-bimodules

In 12.1: sheaf of differential graded O-algebras, sheaf of differential graded algebras, homomorphism of differential graded O-algebras

In 13.1: differential graded A-module, differential graded module, homomorphism of differential graded A-modules In 17.1: differential graded (A, B)bimodule, homomorphism of differential
graded (A, B)-bimodules

In 21.1: homotopy between f and g, homotopic

In 21.2: homotopy category

In 22.2: cone

In 25.2: graded injective

In 25.7: K-injective

In 26.4: derived category of (A, d)

In 28.2: derived tensor product, derived pullback

In 29.2: derived internal hom, derived pushforward

In 33.1:  $QC(\mathcal{A}, d)$ 

### Hypercoverings

In 2.1: semi-representable objects, semi-representable objects over X

In 2.2: which associates a presheaf to a semi-representable object

In 3.1: covering, covering

In 3.3: hypercovering of X

In 4.1: homology of K

In 6.1: hypercovering of  $\mathcal{G}$ , hypercovering

## Schemes

In 2.1: locally ringed space  $(X, \mathcal{O}_X)$ , local ring of X at x, residue field of X at x, morphism of locally ringed spaces

In 3.1: open immersion

In 3.3: open subspace of X associated to II

In 4.1: closed immersion

In 4.4: closed subspace of X associated to the sheaf of ideals  $\mathcal{I}$ 

In 5.2: standard open covering, standard open covering

In 5.3: structure sheaf  $\mathcal{O}_{\operatorname{Spec}(R)}$  of the spectrum of R, spectrum

In 5.5: affine scheme, morphism of affine schemes

In 9.1: scheme, morphism of schemes In 10.2: open immersion, open subscheme, closed immersion, closed subscheme, immersion, locally closed immersion

In 12.1: reduced

In 12.5: scheme structure on Z, reduced induced scheme structure, reduction  $X_{red}$  of X

In 15.1:  $representable\ by\ a\ scheme,\ representable$ 

In 15.3: satisfies the sheaf property for the Zariski topology, subfunctor  $H \subset F$ , representable by open immersions, covers F

In 17.1:  $fibre\ product$ 

In 17.7: inverse image  $f^{-1}(Z)$  of the closed subscheme Z

In 18.1: scheme over S, structure morphism, scheme over R, morphism  $f: X \to Y$  of schemes over S, base change, base change hase change

In 18.3: preserved under arbitrary base change, preserved under base change, preserved under arbitrary base change, preserved under base change

In 18.4: scheme theoretic fibre  $X_s$  of f

over s, fibre of f over s

In 19.1: quasi-compact In 20.1: universally closed

In 20.3: satisfies the existence part of the valuative criterion, satisfies the uniqueness part of the valuative criterion

In 21.3: separated, quasi-separated, separated, quasi-separated

In 23.1: monomorphism

#### Constructions of Schemes

In 4.5: relative spectrum of A over S, spectrum of A over S

In 5.1: affine n-space over S, affine n-space over R

In 6.1: vector bundle associated to  $\mathcal{E}$ 

In 6.2: vector bundle  $\pi: V \to S$  over S, morphism of vector bundles over S

In 7.1: cone associated to A, affine cone associated to A

In 7.2: cone  $\pi: C \to S$  over S, morphism of cones

In 8.2: standard open covering

In 8.3: structure sheaf  $\mathcal{O}_{Proj(S)}$  of the homogeneous spectrum of S, homogeneous spectrum

In 10.1: twist of the structure sheaf of Proj(S)

In 13.2: projective n-space over  $\mathbb{Z}$ , projective n-space over S, projective n-space over R

In 16.7: relative homogeneous spectrum of A over S, homogeneous spectrum of A over S, relative Proj of A over S

In 21.1: projective bundle associated to  $\mathcal{E}$ , twist of the structure sheaf

In 22.2: Grassmannian over  $\mathbf{Z}$ , Grassmannian over S, Grassmannian over R

### Properties of Schemes

In 3.1: integral

In 4.1: local

In 4.2: locally P

In 5.1: locally Noetherian, Noetherian

In 6.1: Jacobson

In 7.1: normal

In 8.1: Cohen-Macaulay

In 9.1: regular, nonsingular

In 10.1: dimension, dimension of X at x

In 11.1: catenary

In 12.1: regular in codimension k,  $(R_k)$ ,  $(S_k)$ 

In 13.1: Japanese, universally Japanese, Nagata

In 14.1: regular locus, singular locus

In 15.1: unibranch at x, geometrically unibranch at x, unibranch, geometrically unibranch

In 15.4: number of branches of X at x, number of geometric branches of X at x

In 18.1: quasi-affine

In 21.1: locally projective

In 23.1:  $\kappa$ -generated

In 24.3: subsheaf of sections annihilated by  $\mathcal{I}$ 

In 24.6: subsheaf of sections supported on T

In 26.1: *ample* 

## Morphisms of Schemes

In 4.4: scheme theoretic intersection, scheme theoretic union

In 5.5: scheme theoretic support of  $\mathcal{F}$ 

In 6.2: scheme theoretic image

In 7.1: scheme theoretic closure of U in X, scheme theoretically dense in X

In 8.1: dominant

In 9.1: surjective

In 10.1: universally injective, radicial

In 11.1: affine

In 12.1: ample family of invertible modules on X

In 13.1: quasi-affine

In 14.1: local, stable under base change, stable under composition

In 14.2: locally of type P

In 15.1: finite type at  $x \in X$ , locally of finite type, finite type

In 16.3: finite type point

In 17.1: universally catenary

In 19.1: J-2

In 20.1: quasi-finite at a point  $x \in X$ , locally quasi-finite, quasi-finite

In 21.1: finite presentation at  $x \in X$ , locally of finite presentation, finite presentation

In 23.1: open, universally open

In 24.1: submersive, universally submersive

In 25.1: flat at a point  $x \in X$ , flat over S at a point  $x \in X$ , flat, flat over S

In 26.3: canonical scheme structure on T In 29.1: relative dimension  $\leq d$  at x, relative dimension  $\leq d$ , relative dimension d

In 30.1: syntomic at  $x \in X$ , syntomic, local complete intersection over k, standard syntomic

In 30.15:  $syntomic\ of\ relative\ dimension\ d$ 

In 31.1: conormal sheaf  $C_{Z/X}$  of Z in X, conormal sheaf of i

In 32.1: sheaf of differentials  $\Omega_{X/S}$  of X over S, universal S-derivation

In 34.1: smooth at  $x \in X$ , smooth, standard smooth

In 34.13: smooth of relative dimension dIn 35.1: unramified at  $x \in X$ , G-unramified at  $x \in X$ , unramified, G-unramified

In 36.1: étale at  $x \in X$ , étale, standard étale

In 37.1: relatively ample, f-relatively ample, ample on X/S, f-ample

relatively very ample, very ample on X/S, f-very ample

In 40.1: quasi-projective, H-quasiprojective, locally quasi-projective

In 41.1: proper

In 43.1: projective, H-projective, locally projective

In 44.1: integral, finite

In 45.1: universal homeomorphism

In 47.1: seminormal, absolutely weakly normal

In 47.3: seminormal, absolutely weakly normal

In 47.8: seminormalization, absolute weak normalization

In 48.1: finite locally free, rank, degree

In 49.1: equivalent, rational map from X

to Y, S-rational map from X to Y

In 49.3: rational function on X

In 49.4: ring of rational functions on X

In 49.6: function field, field of rational functions

In 49.8: defined in a point  $x \in X$ , domain of definition

In 49.10: dominant

In 49.11: birational, S-birational

In 50.1: birational

In 51.8: degree of X over Y

In 51.11: modification of X

In 51.12: alteration of X

In 53.2: integral closure of  $\mathcal{O}_X$  in  $\mathcal{A}$ 

In 53.3: normalization of X in Y

In 54.1: normalization

In 55.6: seminormalization of X in Y, weak normalization of X in Y

In 55.8: weak normalization

In 55.9: weakly normal

In 57.1: bounds the degrees of the fibres of f, fibres of f are universally bounded

#### Cohomology of Schemes

In 11.1:  $depth \ k$  at a point,  $depth \ k$  at a point,  $(S_k)$ ,  $(S_k)$ 

In 11.4: Cohen-Macaulay

In 26.2: Z is proper over S

# **Divisors**

In 2.1: associated, associated points of X

In 38.1: relatively very ample, f- In 4.1: embedded associated point, embedded point, embedded component

> In 5.1: weakly associated, weakly associated points of X

> In 7.1: relative assassin of  $\mathcal{F}$  in X over

In 8.1: relative weak assassin of  $\mathcal{F}$  in Xover S

In 11.2: torsion, torsion free

In 12.1: reflexive hull, reflexive

In 13.1: locally principal closed subscheme, effective Cartier divisor

In 13.6: sum of the effective Cartier divisors  $D_1$  and  $D_2$ 

In 13.12: pullback of D by f is defined, pullback of the effective Cartier divisor

In 14.1: invertible sheaf  $\mathcal{O}_S(D)$  associated to D, canonical section

In 14.6: regular section

In 14.8: zero scheme

In 18.2: relative effective Cartier divisor In 19.1: conormal algebra  $C_{Z/X,*}$  of Z in X, conormal algebra of f

In 19.5: normal cone  $C_ZX$ , normal bundle

In 20.2: regular, Koszul-regular,  $H_1$ regular, quasi-regular

In 21.1: regular immersion, Koszulregular immersion,  $H_1$ -regular immersion, quasi-regular immersion

In 22.2: relative quasi-regular immersion, relative  $H_1$ -regular immersion

In 23.1: sheaf of meromorphic functions on X,  $\mathcal{K}_X$ , meromorphic function

In 23.3: meromorphic section of  $\mathcal{F}$ 

In 23.4: pullbacks of meromorphic functions are defined for f

In 23.7: regular

to f

In 23.10:  $ideal\ sheaf\ of\ denominators\ of$ 

In 26.2: prime divisor, Weil divisor

In 26.3: order of vanishing of f along ZIn 26.5: principal Weil divisor associated

In 26.7: Weil divisor class group

In 27.1: order of vanishing of s along Z

In 27.4: Weil divisor associated to s, Weil divisor class associated to  $\mathcal{L}$ 

In 32.1: blowing up of X along Z, blowing up of X in the ideal sheaf  $\mathcal{I}$ , exceptional divisor, center

In 33.1:  $strict\ transform,\ strict\ transform$ 

In 34.1: U-admissible blowup

### Limits of Schemes

#### Varieties

In 3.1: variety

In 6.1: geometrically reduced at x, geometrically reduced

In 7.1: geometrically connected

In 8.1: geometrically irreducible

In 9.1: geometrically pointwise integral at x, geometrically pointwise integral, geometrically integral

In 10.1: geometrically normal at x, geometrically normal

In 12.1: geometrically regular at x, geometrically regular over k

In 16.1: dual numbers

In 16.3: tangent space of X over S at x, tangent vector

In 20.1: algebraic k-scheme, locally algebraic k-scheme

In 26.1: affine variety, projective variety, quasi-projective variety, proper variety, smooth variety

In 33.1: Euler characteristic of  $\mathcal{F}$ 

In 35.7: m-regular

In 35.15: Hilbert polynomial In 36.1: absolute frobenius of X

In 36.4: relative Frobenius morphism of X/S

In 39.3:  $\delta$ -invariant of A

In 39.7:  $\delta$ -invariant of X at x

In 40.4: A is a wedge of  $A_1, \ldots, A_n$ 

In 43.1: curve

In 44.1: degree, degree

In 45.3: intersection number

In 45.10: degree of Z with respect to  $\mathcal{L}$ 

In 46.1: embedding dimension of X at x

In 46.2: embedding dimension of X/k at

### Topologies on Schemes

In 3.1: Zariski covering of T

In 3.4: standard Zariski covering

In 3.5: biq Zariski site

In 3.7: big Zariski site of S, small Zariski site of S, big affine Zariski site of S, small affine Zariski site of S

In 3.15: restriction to the small Zariski site

In 4.1: étale covering of T

In 4.5: standard étale covering

In 4.6: big étale site

In 4.8: big étale site of S, small étale site of S, big affine étale site of S, small affine étale site of S

In 4.15: restriction to the small étale site

In 5.1: smooth covering of T

In 5.5: standard smooth covering

In 5.6: big smooth site

In 5.8: big smooth site of S, big affine smooth site of S

In 6.1: syntomic covering of T

In 6.5: standard syntomic covering

In 6.6: big syntomic site

In 6.8: big syntomic site of S, big affine syntomic site of S

In 7.1: fppf covering of T

In 7.5: standard fppf covering

In 7.6: big fppf site

In 7.8: big fppf site of S, big affine fppf site of S

In 8.1: standard ph covering

In 8.4: ph covering of T

In 8.9: big ph site

In 8.11: big ph site of S, big affine ph site of S

In 9.1: fpqc covering of T

In 9.9: standard fpqc covering

In 9.12: satisfies the sheaf property for the given family, satisfies the sheaf property for the fpqc topology

In 10.1: standard V covering

In 10.7: V covering of T

In 10.11: satisfies the sheaf property for the V topology

### Descent

In 2.1: descent datum  $(\mathcal{F}_i, \varphi_{ij})$  for quasicoherent sheaves, cocycle condition, morphism  $\psi : (\mathcal{F}_i, \varphi_{ij}) \to (\mathcal{F}'_i, \varphi'_{ij})$  of descent data descent datum, effective

In 3.1: descent datum  $(N, \varphi)$  for modules with respect to  $R \to A$ , cocycle condition, morphism  $(N,\varphi) \to (N',\varphi')$  of descent data

In 3.4: effective

In 4.2: split equalizer

In 4.5: universally injective

In 4.9: C

In 4.15: base extension along f, descent morphism for modules, effective descent morphism for modules

In 4.19:  $f_*$ 

In 8.2: structure sheaf of the big site  $(Sch/S)_{\tau}$ , structure sheaf of the small site, sheaf of  $\mathcal{O}$ -modules associated to  $\mathcal{F}$ , sheaf of  $\mathcal{O}$ -modules associated to  $\mathcal{F}$ 

In 12.1: parasitic, parasitic for the  $\tau$ topology

In 15.1: local in the  $\tau$ -topology

In 20.1:  $germ \ of \ X \ at \ x, \ morphism$ of germs, composition of morphisms of *qerms* 

In 20.2: étale, smooth

In 21.1: étale local, smooth local

In 22.1:  $\tau$  local on the base,  $\tau$  local on the target, local on the base for the  $\tau$ -topology In 26.1:  $\tau$  local on the source, local on the

source for the  $\tau$ -topology

In 32.3: étale local on source-and-target In 33.1: étale local on the source-andtarget

In 34.1: descent datum for V/X/S, cocycle condition, descent datum relative to  $X \to S$ , morphism  $f: (V/X, \varphi) \to$  $(V'/X,\varphi')$  of descent data relative to  $X \to S$ 

In 34.3: descent datum  $(V_i, \varphi_{ij})$  relative to the family  $\{X_i \to S\}$ , morphism  $\psi$ :  $(V_i, \varphi_{ij}) \to (V'_i, \varphi'_{ij})$  of descent data

In 34.7: pullback functor

In 34.9: pullback functor

In 34.10: trivial descent datum, canonical descent datum, effective

In 34.11: canonical descent datum, effective

In 2.3: trivial descent datum, canonical In 36.1: morphisms of type P satisfy descent for  $\tau$ -coverings

### **Derived Categories of Schemes**

In 6.1: supported on T

In 14.1: approximation holds for the triple

In 14.2: approximation by perfect complexes holds

In 22.2: Tor independent over S

In 35.1: perfect relative to S, S-perfect

In 36.1: resolution property

In 38.2: Grothendieck group of X, Grothendieck group of coherent sheaves on X

### More on Morphisms

In 2.1: thickening, first order thickening, morphism of thickenings, thickenings over S, morphisms of thickenings over S

In 5.1: first order infinitesimal neighbourhood

In 6.1: formally unramified

In 7.2: universal first order thickening, conormal sheaf of Z over X

In 8.1: formally étale

In 11.1: formally smooth

In 13.1: naive cotangent complex of f

In 20.1: normal at x, normal morphism

In 21.1: regular at x, regular morphism

In 22.1: Cohen-Macaulay at x, Cohen-Macaulay morphism

In 35.1: étale neighbourhood of (S, s), morphism of étale neighbourhoods, elementary étale neighbourhood

In 58.1: finitely presented relative to S, of finite presentation relative to S

In 59.2: m-pseudo-coherent relative to S, pseudo-coherent relative to S, m-pseudocoherent relative to S, pseudo-coherent relative to S

In 60.2: pseudo-coherent

In 61.2: perfect

In 62.2: Koszul at x, Koszul morphism, local complete intersection morphism

In 64.1: weakly étale, absolutely flat

In 66.1: ind-quasi-affine, ind-quasi-affine

In 73.1: affine stratification

In 73.4: affine stratification number

In 75.2: weighting, pondération

In 78.1: completely decomposed, completely decomposed

### More on Flatness

In 4.1: one step dévissage of  $\mathcal{F}/X/S$  over s

In 4.2: one step dévissage of  $\mathcal{F}/X/S$  at x

In 4.6: standard shrinking

In 5.1: complete dévissage of  $\mathcal{F}/X/S$  over s

In 5.2: complete dévissage of  $\mathcal{F}/X/S$  at x

In 5.5: standard shrinking

In 6.1: elementary étale localization of the ring map  $R \to S$  at  $\mathfrak{q}$ 

In 6.2: complete dévissage of N/S/R over  $\mathfrak r$ 

In 6.4: complete dévissage of N/S/R at  $\mathfrak{q}$ 

In 15.2: impurity of  $\mathcal{F}$  above s

In 16.1: pure along  $X_s$ , universally pure along  $X_s$ , pure along  $X_s$ , universally S-pure, universally pure relative to S, S-pure, pure relative to S, S-pure, pure relative to S

In 20.10:  $\mathcal{F}$  is flat over S in dimensions  $\geq n$ 

In 21.1: universal flattening of  $\mathcal{F}$  exists, universal flattening of X exists

In 21.3: flattening stratification, flattening stratification

In 34.2: h covering of T

In 34.10:  $big\ h\ site$ 

In 34.11: standard h covering

In 34.13: big h site of S, big affine h site of S

### Groupoid Schemes

In 3.1: pre-relation, relation, preequivalence relation, equivalence relation on U over S

In 3.3: restriction, pullback

In 4.1: group scheme over S, morphism  $\psi:(G,m)\to(G',m')$  of group schemes over S

In 4.3: closed subgroup scheme, open subgroup scheme

In 4.5: smooth group scheme, flat group scheme, separated group scheme

In 9.1: abelian variety

In 10.1: action of G on the scheme X/S, equivariant, G-equivariant

In 10.2: free

In 11.1: pseudo G-torsor, formally principally homogeneous under G, trivial

In 11.3: principal homogeneous space, G-torsor, G-torsor in the  $\tau$  topology,  $\tau$  G-torsor,  $\tau$  torsor, quasi-isotrivial, locally trivial

In 12.1: G-equivariant quasi-coherent  $\mathcal{O}_X$ -module, equivariant quasi-coherent  $\mathcal{O}_X$ -module

In 13.1: groupoid scheme over S, groupoid over S, morphism f:  $(U,R,s,t,c) \rightarrow (U',R',s',t',c')$  of groupoid schemes over S

In 14.1: quasi-coherent module on (U, R, s, t, c)

In 17.2: stabilizer of the groupoid scheme (U, R, s, t, c)

In 18.2: restriction of (U, R, s, t, c) to U'In 19.1: set-theoretically R-invariant, R-invariant, R-invariant

In 20.1: quotient sheaf U/R

In 20.2: representable quotient, representable quotient

In 21.1: cartesian, (U', R', s', t', c') is cartesian over (U, R, s, t, c), morphism of groupoid schemes cartesian over (U, R, s, t, c)

### More on Groupoid Schemes

#### Étale Morphisms of Schemes

In 3.1: unramified homomorphism of local rings

In 3.5: unramified at x, unramified

In 9.1: flat, faithfully flat, flat (resp. faithfully flat)

In 9.3: flat over Y at  $x \in X$ , flat at  $x \in X$ , flat, faithfully flat

In 11.1: étale homomorphism of local rings

In 11.4: étale at  $x \in X$ , étale

In 21.1: strict normal crossings divisor In 21.4: normal crossings divisor

### **Chow Homology and Chern Classes**

In 2.1: 2-periodic complex, cohomology modules, exact, (2,1)-periodic complex, cohomology modules

In 2.2: multiplicity, (additive) Herbrand quotient

In 7.6:  $\delta$ -dimension of Z

In 8.1:  $cycle\ on\ X,\ k\text{-}cycle$ 

In 8.3: support

In 8.4: effective

In 9.2: multiplicity of Z' in Z, k-cycle associated to Z

In 10.2: multiplicity of Z' in  $\mathcal{F}$ , k-cycle associated to  $\mathcal{F}$ 

In 12.1: pushforward

In 14.1: flat pullback of  $\alpha$  by f

In 17.1:  $principal\ divisor\ associated\ to\ f$ 

In 19.1: rationally equivalent to zero, rationally equivalent, Chow group of k-cycles on X, Chow group of k-cycles modulo rational equivalence on X

In 22.1: envelope

In 24.1: Weil divisor associated to s, Weil divisor associated to  $\mathcal{L}$ 

In 25.1: intersection with the first Chern class of  $\mathcal{L}$ 

In 29.1: Gysin homomorphism

In 33.1: bivariant class c of degree p for f

In 34.1: Chow cohomology

In 34.4: first Chern class

In 37.1: Chern classes of  $\mathcal{E}$  on X, total Chern class of  $\mathcal{E}$  on X

In 38.1: intersection with the jth Chern class of  $\mathcal{E}$ 

In 38.8: ith Chern class, total Chern class

In 41.1: degree of a zero cycle

In 46.3: Chern classes of E are defined

In 50.3: localized Chern character, localized pth Chern class

In 59.4: the gysin map for f exists, gysin map

In 68.2: admissible, symbol, admissible relation, determinant of the finite length R-module M

In 68.13: determinant of  $(M, \varphi, \psi)$ 

In 68.29: symbol associated to M, a, b

In 68.31:  $tame\ symbol$ 

# Intersection Theory

In 13.5: intersect properly, intersect properly

In 15.1: multiplicity of M for the ideal of definition I

#### Picard Schemes of Curves

In 4.1: Picard functor

In 6.3: genus

# Weil Cohomology Theories

In 5.1:  $ith\ Chow\ group\ of\ M$ 

In 7.3: classical Weil cohomology theory

In 11.4: Weil cohomology theory

### **Adequate Modules**

In 3.1: module-valued functor, morphism of module-valued functors

In 3.2: adequate, linearly adequate

In 5.1: adequate

In 5.7:  $Adeq(\mathcal{O})$ ,  $Adeq((Sch/S)_{\tau}, \mathcal{O})$ , Adeq(S)

In 8.1: pure projective, pure injective

In 8.5: pure projective resolution, pure injective resolution

In 8.8: pure extension module

### **Dualizing Complexes**

In 2.1: essential, essential extension of, essential

In 4.1: projective cover, projective envelope

In 5.1: injective hull

In 5.5: indecomposable

In 15.1: dualizing complex

In 21.1: Gorenstein, Gorenstein

In 27.1: relative dualizing complex

### **Duality for Schemes**

In 2.2: dualizing complex

In 20.5: dualizing complex normalized relative to  $\omega_{S}^{\bullet}$ 

In 24.1: Gorenstein

In 25.2: Gorenstein at x, Gorenstein morphism

In 28.1: relative dualizing complex

#### Discriminants and Differents

In 4.1: trace element In 7.1: Kähler different

In 9.1: different

# de Rham Cohomology

In 7.1: Hodge filtration

In 15.1: de Rham complex of log poles is defined for  $Y \subset X$  over S

In 15.3: de Rham complex of log poles for  $Y \subset X \ over S$ 

### Local Cohomology

In 4.2: cohomological dimension of I in

In 13.1: I-depth, depth

# Algebraic and Formal Geometry

In 6.4: derived complete with respect to

In 16.5:  $(\mathcal{F}_n)$  extends to X

In 16.7:  $(\mathcal{F}_n)$  canonically extends to X In 19.1:  $(\mathcal{F}_n)$  satisfies the (a,b)inequalities,  $(\mathcal{F}_n)$  satisfies the strict (a,b)-inequalities

#### Algebraic Curves

In 2.7: nonsingular projective model of XIn 3.1: linear series of degree d and dimension r,  $\mathfrak{g}_d^r$ 

In 8.1: genus

In 11.1: geometric genus

In 16.2: multicross singularity, node, ordinary double point, defines a nodal sinqularity

In 19.1: node, ordinary double point, defines a nodal singularity, singularities of X are at-worst-nodal

In 19.10: split node

In 20.2: at-worst-nodal of relative dimension 1

#### Resolution of Surfaces

In 5.1: normalized blowup of X at x

In 8.3: defines a rational singularity, reduction to rational singularities is possible for A

In 14.1: resolution of singularities

In 14.2: resolution of singularities by normalized blowups

#### Semistable Reduction

In 3.1: numerical type

In 3.2: equivalent types

In 3.4: numerical type of genus g

In 3.8: (-1)-index

In 3.11: topological genus of T

In 3.12: minimalIn 3.16: (-2)-index

In 4.1: Picard group of T

In 8.4: minimal model

In 11.4: numerical type associated to X

In 14.6: semistable reduction

In 14.8: good reduction

# **Functors and Morphisms**

# **Derived Categories of Varieties**

In 3.2: a Serre functor exists, Serre func-

In 8.1: Fourier-Mukai functor, Fourier-Mukai kernel

In 10.1: siblings, sibling

In 12.1: siblings, sibling

In 15.1: the Fourier-Mukai kernel of a relative equivalence from X to Y over S

In 18.1: derived equivalent

### **Fundamental Groups of Schemes**

In 2.1: G-set, discrete G-set, morphism of G-sets, G-Sets

In 3.6: Galois category

In 6.1: fundamental group, base point

### Étale Cohomology

In 4.1: étale covering

In 9.1: presheaf of sets, abelian presheaf

In 10.1: family of morphisms with fixed taraet

In 10.2: site, coverings

In 11.1: separated presheaf, sheaf

In 11.4: category of sheaves of sets,  $abelian\ sheaves$ 

In 13.1: zeroth Čech cohomology group

In 15.1: fpqc covering

In 15.5: satisfies the sheaf property for the fpqc topology

In 16.1: descent datum, cocycle condition, effective

In 16.5: descent datum

In 16.6: effective

In 17.2: ringed site, quasi-coherent

In 18.1: Čech complex, Čech cohomology groups

In 18.4: free abelian presheaf on G

In 20.1:  $\tau$ -covering

In 20.2: big  $\tau$ -site of S, small  $\tau$ -site of S

In 20.4: standard  $\tau$ -covering

In 21.1: étale topos, small étale topos, Zariski topos, small Zariski topos, big  $\tau$ -topos

In 23.1: constant sheaf

In 23.3: structure sheaf

In 26.1: étale

In 26.3: standard étale

In 27.1: étale covering

In 27.3: big étale site over S, small étale site over S, big, small Zariski sites

In 29.1: geometric point, lies over, étale neighborhood, morphism of étale neighborhoods

In 29.6: stalk

In 31.3: support of  $\mathcal{F}$ , support of  $\sigma$ 

In 32.2: henselian

In 32.6: strictly henselian

In 33.2: étale local ring of S at  $\overline{s}$ , strict henselization of  $\mathcal{O}_{S,s}$ , henselization of  $\mathcal{O}_{S,s}$ , strict henselization of S at  $\overline{s}$ , henselization of S at s

In 35.1: direct image, pushforward

In 35.3: direct image, pushforward

In 35.4: higher direct images

In 36.1:  $inverse\ image,\ pullback$ 

In 51.1: system  $(\mathcal{F}_i, \varphi_{i'i})$  of sheaves on  $(X_i, f_{i'i})$ 

In 56.1: absolute Galois group, algebraic In 57.1: G-module, discrete G-module, morphism of G-modules, R-G-module, morphism of R-G-modules

In 57.2: continuous group cohomology groups, group cohomology groups, Galois cohomology groups, Galois cohomology groups of K with coefficients in M

In 61.3: similar, equivalent

In 61.4: Brauer group

In 64.1: constant sheaf with value E, constant sheaf, locally constant, finite locally constant, constant sheaf with value A,

constant sheaf, locally constant, finite locally constant, constant sheaf with value

M, constant sheaf, locally constant

In 66.1: *trace* 

In 67.5:  $C_r$ , nontrivial solution

In 67.9: variety, curve

In 70.1: extension by zero, extension by zero

In 71.1: constructible, constructible, constructible

In 76.1:  $D_c(X_{\acute{e}tale}, \Lambda)$ 

In 77.1:  $D_{ctf}(X_{\acute{e}tale}, \Lambda)$ 

In 93.1: locally acyclic at  $\overline{x}$  relative to K, locally acyclic relative to K, universally locally acyclic relative to K, locally acyclic, universally locally acyclic

In 95.1: cohomological dimension of XIn 96.1: cohomological dimension of f

### Crystalline Cohomology

In 2.2: divided power envelope of J in B relative to  $(A, I, \gamma)$ 

In 4.1:  $\delta$  is compatible with  $\gamma$ 

In 5.2: divided power thickening, homomorphism of divided power thickenings

In 6.1: divided power A-derivation

In 7.1: divided power structure  $\gamma$ 

In 7.2: divided power scheme, morphism of divided power schemes

In 7.3: divided power thickening

In 8.1: divided power thickening of X relative to  $(S, \mathcal{I}, \gamma)$ , morphism of divided power thickenings of X relative to  $(S, \mathcal{I}, \gamma)$ 

 $\label{eq:continuous} \begin{tabular}{ll} In 8.4: Zariski, \'etale, smooth, syntomic, \\ or fppf covering, big crystalline site \\ \end{tabular}$ 

In 9.1: crystalline site

In 11.1: locally quasi-coherent, quasi-coherent, crystal in  $\mathcal{O}_{X/S}$ -modules

In 11.3: crystal in quasi-coherent modules, crystal in finite locally free modules In 12.1: S-derivation  $D: \mathcal{O}_{X/S} \to \mathcal{F}$ 

In 26.2: F-crystal on X/S (relative to  $\sigma$ ), nondegenerate

### Pro-étale Cohomology

In 2.3: w-local, w-local

In 3.1: local isomorphism, identifies local rings

In 4.1: ind-Zariski In 7.1: ind-étale

In 11.1: w-contractible

In 12.1: pro-étale covering of T In 12.6: standard pro-étale covering

In 12.7: big pro-étale site

In 12.8: big pro-étale site of S, small pro-étale site of S, big affine pro-étale site of S

In 12.14: restriction to the small proétale site

In 26.1: extension by zero, extension by

In 27.1: constructible

In 28.1: constructible  $\Lambda$ -sheaf, lisse, adic

lisse, adic constructible In 29.1: constructible

In 29.4: adic lisse, adic constructible

### Relative Cycles

In 6.1: relative r-cycle on X/S

In 7.1: equidimensional

In 8.1: effective

In 9.1: proper relative cycle

### More Étale Cohomology

In 3.3: direct image with compact support In 3.7: sections with compact support

In 4.4: direct image with compact support

In 12.1: cohomology of K with compact support, compactly supported cohomology of K

#### The Trace Formula

In 3.4: geometric frobenius

In 3.8: arithmetic frobenius

In 3.10: geometric frobenius

In 4.1: trace

In 6.4: total right derived functor of F, total left derived functor of G

In 7.1: filtered injective, projective, filtered quasi-isomorphism

In 8.1: filtered derived functor

In 10.1: perfect

In 12.1: finite Tor-dimension

In 14.1: global Lefschetz number

In 14.2:  $local\ Lefschetz\ number$ 

In 15.2: G-trace of f on P

In 18.1:  $\mathbf{Z}_{\ell}$ -sheaf,  $\ell$ -adic sheaf, lisse, mor-

phism

In 18.6: torsion, stalk

In 18.8: ℓ-adic cohomology

In 19.1: L-function of  $\mathcal{F}$ 

In 19.3: L-function of  $\mathcal{F}$ 

In 27.1: open

In 31.1: unramified cusp form on

 $GL_2(\mathbf{A})$  with values in  $\Lambda$ 

## Algebraic Spaces

In 5.1: property  $\mathcal{P}$ 

In 6.1: algebraic space over S

In 6.3: morphism  $f: F \to F'$  of algebraic

spaces over S

In 9.2: étale equivalence relation

In 9.3: presentation

In 12.1: open immersion, open subspace, closed immersion, closed subspace, immersion, locally closed subspace

In 12.5: Zariski covering

In 12.6: small Zariski site  $F_{Zar}$ 

In 13.2: separated over S, locally separated over S, quasi-separated over S, Zariski locally quasi-separated over S

In 14.4: acts freely, quotient of U by G

In 16.2: base change of F' to S, viewed as an algebraic space over S'

## Properties of Algebraic Spaces

In 3.1: separated, locally separated, quasi-separated, Zariski locally quasi-separated, separated, locally separated, quasi-separated, Zariski locally quasi-separated

In 4.1: point

In 4.7: topological space

In 5.1: quasi-compact

In 7.2: has property  $\mathcal{P}$ 

In 7.5: has property P at x

In 8.2: étale locally constructible

In 9.1: dimension of X at x

In 9.2: dimension

In 10.2: dimension of the local ring of X

at x, x is a point of codimension d on X

In 12.5: algebraic space structure on Z, reduced induced algebraic space struc-

ture, reduction  $X_{red}$  of X

In 16.2:  $\acute{e}tale$ 

In 18.1: small étale site  $X_{\text{\'etale}}$ 

In 18.2:  $X_{spaces, \acute{e}tale}$ 

In 18.5:  $X_{affine,\acute{e}tale}$ 

In 18.7: étale topos, small étale topos

In 18.9: f-map  $\varphi : \mathcal{G} \to \mathcal{F}$ 

In 19.1: geometric point, geometric point lying over x

In 19.2: étale neighborhood, morphism of étale neighborhoods

In 19.6: *stalk* 

In 20.3: support of  $\mathcal{F}$ , support of  $\sigma$ 

In 21.2: structure sheaf

In 22.2: étale local ring of X at  $\overline{x}$ , strict henselization of X at  $\overline{x}$ 

In 23.2: geometrically unibranch at x, geometrically unibranch

In 23.4: number of geometric branches of

X at x

In 24.1: Noetherian

In 25.2: X is regular at x

In 29.1: quasi-coherent

In 31.2: locally projective

# Morphisms of Algebraic Spaces

In 4.2: separated, locally separated, quasiseparated

In 5.2: surjective

In 6.2: open, universally open

In 7.2: submersive, universally submersive

In 8.2: quasi-compact

In 9.2: closed, universally closed

In 10.1: monomorphism

In 13.2: inverse image  $f^{-1}(Z)$  of the closed subspace Z

In 14.4: scheme theoretic intersection, scheme theoretic union

In 15.4: scheme theoretic support of  $\mathcal{F}$ 

In 16.2: scheme theoretic image

In 17.3: scheme theoretic closure of U in X, scheme theoretically dense in X

In 18.1: dominant

In 19.3: universally injective

In 20.2: affine

In 20.8: relative spectrum of A over X, spectrum of A over X

In 21.2: quasi-affine

In 22.2: has property  $\mathcal{P}$ 

In 22.6: has property Q at x

In 23.1: locally of finite type, finite type

at x, of finite type

In 25.2: finite type point

In 27.1: locally quasi-finite, quasi-finite at x, quasi-finite

In 28.1: locally of finite presentation, finite presentation at x, of finite presentation

In 30.1: flat, flat at x

In 31.2:  $flat \ at \ x \ over \ Y$ ,  $flat \ over \ Y$ 

In 33.1: dimension of the local ring of the fibre of f at x, transcendence degree of x/f(x), f has relative dimension d at x

In 33.2: relative dimension  $\leq d$ , relative dimension d

In 36.1: syntomic, syntomic at x

In 37.1: smooth, smooth at x

In 38.1: unramified, unramified at x, G-unramified, G-unramified at x

In 39.1: étale at x

In 40.1: proper

In 41.1: satisfies the uniqueness part of the valuative criterion, satisfies the existence part of the valuative criterion, satisfies the valuative criterion

In 45.2: integral, finite

In 46.2: finite locally free, rank, degree

In 47.1: equivalent, rational map from X

to Y, B-rational map from X to Y

In 47.2: rational function on X

In 47.3: ring of rational functions on X

In 47.4: defined in a point  $x \in |X|$ , do-

main of definition

In 47.6: dominant

In 47.7: birational

In 48.2: integral closure of  $\mathcal{O}_X$  in  $\mathcal{A}$ 

In 48.3: normalization of X in Y

In 49.6: normalization

In 53.2: universal homeomorphism

#### Decent Algebraic Spaces

In 3.1: fibres of f are universally bounded

In 6.1: decent, reasonable, very reasonable

In 11.2: residue field of X at x

In 11.5: elementary étale neighbourhood, morphism of elementary étale neighbourhoods In 11.7: henselian local ring of X at x

In 13.6: residual space of X at x

In 17.1: has property  $(\beta)$ , has property  $(\beta)$ , decent, reasonable, very reasonable

In 22.1: birational

In 24.2: unibranch at x, unibranch

In 24.4: number of branches of X at x

In 25.1: catenary

In 25.4: universally catenary

# Cohomology of Algebraic Spaces

In 6.2: alternating Čech complex

In 12.1: coherent

## Limits of Algebraic Spaces

In 3.1: limit preserving, locally of finite presentation, locally of finite presentation over S, limit preserving, locally of finite presentation, relatively limit preserving

In 14.3: subsheaf of sections annihilated  $by \mathcal{I}$ 

In 14.6: subsheaf of sections supported on

### Divisors on Algebraic Spaces

In 2.2: weakly associated, weakly associated points of X, x is associated to  $\mathcal{F}$ , x is an associated point of X

In 4.2: the fibre of f over y is locally Noetherian, the fibres of f are locally Noetherian

In 4.5: relative weak assassin of  $\mathcal{F}$  in Xover Y

In 6.1: locally principal closed subspace, effective Cartier divisor

In 6.6: sum of the effective Cartier divisors  $D_1$  and  $D_2$ 

In 6.10: pullback of D by f is defined, pullback of the effective Cartier divisor

In 7.1: invertible sheaf  $\mathcal{O}_X(D)$  associated

In 7.4: regular section

In 7.6: zero scheme

In 9.2: relative effective Cartier divisor

In 10.1: sheaf of meromorphic functions

on X,  $\mathcal{K}_X$ , meromorphic function

In 10.3: meromorphic section of  $\mathcal{F}$ 

In 10.6: pullbacks of meromorphic functions are defined for f

In 10.9: regular

In 11.3: relative homogeneous spectrum of A over X, homogeneous spectrum of  $\mathcal{A}$  over X, relative Proj of  $\mathcal{A}$  over X

In 14.1: relatively ample, f-relatively ample, ample on X/Y, f-ample

In 17.1: blowing up of X along Z, blowing up of X in the ideal sheaf  $\mathcal{I}$ , exceptional divisor, center

In 18.1: strict transform, strict transform

In 19.1: U-admissible blowup

## Algebraic Spaces over Fields

In 4.1: integral

In 4.3: function field, field of rational *functions* 

In 5.2: degree of X over Y

In 6.2: prime divisor, Weil divisor

In 6.4: order of vanishing of f along Z

In 6.7: principal Weil divisor associated to f

In 6.9: Weil divisor class group

In 7.1: order of vanishing of s along Z

In 7.4: Weil divisor associated to s, Weil

divisor class associated to  $\mathcal{L}$ In 8.1: modification of X

In 8.3: alteration of X

In 11.1: geometrically reduced at x, geometrically reduced

In 12.1: geometrically connected

In 13.1: geometrically irreducible

In 14.1: geometrically integral

In 17.1: Euler characteristic of  $\mathcal{F}$ 

In 18.3: intersection number

#### Topologies on Algebraic Spaces

In 3.1: Zariski covering of X

In 4.1: étale covering of X

In 4.5:  $(Spaces/S)_{\acute{e}tale}$ 

In 4.6:  $(Spaces/X)_{\acute{e}tale}$ 

In 4.9: restriction to the small étale site

In 5.1: smooth covering of X

In 6.1: syntomic covering of X

In 7.1: fppf covering of X

In 7.6:  $(Spaces/S)_{fppf}$ 

In 7.7:  $(Spaces/X)_{fppf}$ 

In 8.1: ph covering of X

In 8.5:  $(Spaces/S)_{ph}$ In 8.6:  $(Spaces/X)_{ph}$ In 9.1:  $fpqc\ covering\ of\ X$ 

# Descent and Algebraic Spaces

In 3.1: descent datum  $(\mathcal{F}_i, \varphi_{ij})$  for quasicoherent sheaves, cocycle condition, morphism  $\psi : (\mathcal{F}_i, \varphi_{ij}) \to (\mathcal{F}'_i, \varphi'_{ij})$  of descent data

In 3.3: trivial descent datum, canonical descent datum, effective

In 10.1:  $\tau$  local on the base,  $\tau$  local on the target, local on the base for the  $\tau$ -topology In 14.1:  $\tau$  local on the source, local on the source for the  $\tau$ -topology

In 20.1: smooth local on source-and-target

In 21.1: étale-smooth local on sourceand-target

In 22.1: descent datum for V/Y/X, cocycle condition, descent datum relative to  $Y \to X$ , morphism  $f: (V/Y, \varphi) \to (V'/Y, \varphi')$  of descent data relative to  $Y \to X$ 

In 22.3: descent datum  $(V_i, \varphi_{ij})$  relative to the family  $\{X_i \to X\}$ , morphism  $\psi$ :  $(V_i, \varphi_{ij}) \to (V'_i, \varphi'_{ij})$  of descent data

In 22.7: pullback functor

In 22.9: pullback functor

In 22.10: trivial descent datum, canonical descent datum, effective

In 22.11: canonical descent datum, effective

### **Derived Categories of Spaces**

In 3.2: supported on T

In 5.1: derived category of  $\mathcal{O}_X$ -modules with quasi-coherent cohomology sheaves In 7.2: T is proper over Y

In 9.1: elementary distinguished square In 14.1: approximation holds for the triple

In 14.2: approximation by perfect complexes holds

In 20.2: Tor independent over B In 28.1: resolution property

### More on Morphisms of Spaces

In 3.1: radicial

In 5.1: conormal sheaf  $C_{Z/X}$  of Z in X, conormal sheaf of i

In 6.1: conormal algebra  $C_{Z/X,*}$  of Z in X, conormal algebra of i

In 6.5: normal cone  $C_ZX$ , normal bundle In 7.2: sheaf of differentials  $\Omega_{X/Y}$  of Xover Y, universal Y-derivation

In 9.1: thickening, first order thickening, morphism of thickenings, thickenings over B, morphisms of thickenings over B

In 12.1: first order infinitesimal neighbourhood

In 13.1: formally smooth, formally étale, formally unramified

In 14.1: formally unramified

In 15.5: universal first order thickening, conormal sheaf of Z over X

In 16.1: formally étale

In 19.1: formally smooth

In 21.1: naive cotangent complex of f

In 23.2: the restriction of  $\mathcal{F}$  to its fibre over z is flat at x over the fibre of Y over z, the fibre of X over z is flat at x over the fibre of Y over z, the fibre of X over z is flat over the fibre of Y over z

In 26.2: Cohen-Macaulay at x, Cohen-Macaulay morphism

In 27.2: Gorenstein at x, Gorenstein morphism

In 29.2: the fibre of  $f: X \to Y$  at y is geometrically reduced

In 44.2: Koszul-regular immersion,  $H_1$ -regular immersion, quasi-regular immersion

In 45.3: m-pseudo-coherent relative to Y, p-seudo-coherent relative to Y, m-pseudo-coherent relative to Y, p-seudo-coherent relative to Y

In 46.1: pseudo-coherent, pseudo-coherent at x

In 47.1: perfect, perfect at x

In 48.1: Koszul morphism, local complete intersection morphism, Koszul at x

In 52.1: perfect relative to Y, Y-perfect In 55.1: at-worst-nodal of relative dimension 1

### Flatness on Algebraic Spaces

In 2.2: impurity of  $\mathcal{F}$  above y

In 3.1: pure above y, universally pure above y, pure above y, universally Y-pure, universally pure relative to Y, Y-pure, pure relative to Y, Y-pure, pure relative to Y

In 11.1: universal flattening of  $\mathcal{F}$  exists, universal flattening of X exists

In 11.3:  $\mathcal{F}$  is flat over Y in dimensions  $\geq n$ 

# Groupoids in Algebraic Spaces

In 4.1: pre-relation, relation, preequivalence relation, equivalence relation on U over B

In 4.3: restriction, pullback

In 5.1: group algebraic space over B, morphism  $\psi:(G,m)\to(G',m')$  of group algebraic spaces over B

In 8.1: action of G on the algebraic space X/B, equivariant, G-equivariant

In 8.2: free

In 9.1: pseudo G-torsor, formally principally homogeneous under G, trivial

In 9.3: principal homogeneous space, principal homogeneous G-space over B, G-torsor in the  $\tau$  topology,  $\tau$  G-torsor,  $\tau$  torsor, quasi-isotrivial, locally trivial

In 10.1: G-equivariant quasi-coherent  $\mathcal{O}_X$ -module, equivariant quasi-coherent  $\mathcal{O}_X$ -module

In 11.1: groupoid in algebraic spaces over B, morphism  $f:(U,R,s,t,c)\to (U',R',s',t',c')$  of groupoids in algebraic spaces over B

In 12.1: quasi-coherent module on (U, R, s, t, c)

In 16.2: stabilizer of the groupoid in algebraic spaces (U, R, s, t, c)

In 17.2: restriction of (U, R, s, t, c) to U'In 18.1: R-invariant, R-invariant, R-invariant

In 19.1: quotient sheaf U/R

In 19.3: quotient representable by an algebraic space, representable quotient, representable quotient, quotient representable by an algebraic space

In 20.1: quotient stack, quotient stack

### More on Groupoids in Spaces

In 15.1: strongly split over u, strong splitting of R over u, split over u, splitting of R over u, quasi-split over u, quasi-splitting of R over u

### **Bootstrap**

In 3.1: representable by algebraic spaces In 4.1: property  $\mathcal{P}$ 

### Pushouts of Algebraic Spaces

# Chow Groups of Spaces

In 2.5:  $\delta$ -dimension of T

In 3.1: cycle on X, k-cycle

In 4.2:  $\mathcal{F}$  has length d at x

In 5.2: multiplicity of Z in Y, k-cycle associated to Y

In 6.1: multiplicity of Z in  $\mathcal{F}$ , k-cycle associated to  $\mathcal{F}$ 

In 8.1: pushforward

In 10.1: flat pullback of  $\alpha$  by f

In 13.1: principal divisor associated to f In 15.1: rationally equivalent to zero, rationally equivalent, Chow group of kcycles on X, Chow group of k-cycles modulo rational equivalence on X

In 17.1: Weil divisor associated to s, Weil divisor associated to  $\mathcal{L}$ 

In 18.1: intersection with the first Chern class of  $\mathcal{L}$ 

In 22.1: Gysin homomorphism

In 26.1: bivariant class c of degree p for f

In 26.2: Chow cohomology

In 28.2: ith Chern class of  $\mathcal{E}$ , total Chern class of  $\mathcal{E}$ 

In 32.1: degree of a zero cycle

### Quotients of Groupoids

In 3.1: R-invariant, G-invariant

In 3.4: base change, flat base change

In 4.1: categorical quotient, categorical quotient in C, categorical quotient in the category of schemes, categorical quotient in schemes

In 4.4: universal categorical quotient, uniform categorical quotient

In 5.1: orbit, R-orbit

In 5.4: weakly R-equivalent, R-equivalent, weak orbit, weak R-orbit, orbit, R-orbit

In 5.8: set-theoretically R-invariant, separates orbits, separates R-orbits

In 5.13: set-theoretic pre-equivalence relation, set-theoretic equivalence relation

In 5.18: orbit space for R

In 6.1: coarse quotient, coarse quotient in schemes

In 7.1: uniformly, universally

In 8.1: sheaf of R-invariant functions on X, the functions on X are the R-invariant functions on U

In  $9.1: good\ quotient$ 

In 10.1: geometric quotient

### More on Cohomology of Spaces

### Simplicial Spaces

In 12.1: cartesian, cartesian, cartesian, cartesian

In 13.1: simplicial system of the derived category, cartesian, morphism of simplicial systems of the derived category

In 14.1: simplicial system of the derived category of modules, cartesian, morphism of simplicial systems of the derived category of modules

In 27.1: cartesian, Y is cartesian over X In 27.3: simplicial scheme associated to f

### **Duality for Spaces**

In 2.2: dualizing complex

In 9.1: relative dualizing complex

# Formal Algebraic Spaces

In 4.7: tensor product, completed tensor product

In 4.8: topologically nilpotent, weak ideal of definition, weakly pre-admissible, weakly admissible

In 5.1: taut

In 6.1: adic

In 7.1: weakly pre-adic, c-adic, weakly adic

In 9.1: affine formal algebraic space, morphism of affine formal algebraic spaces In 9.7: McQuillan, classical, weakly adic,

adic, adic\*, Noetherian

In 9.9: formal spectrum

In 10.2: countably indexed

In 11.1: formal algebraic space, morphism of formal algebraic spaces

In 14.3: completion of X along T

In 16.3: quasi-separated, separated

In 17.2: quasi-compact

In 17.4: quasi-compact

In 20.7: locally countably indexed, locally countably indexed and classical, locally weakly adic, locally adic\*, locally Noetherian

In 23.2: adic morphism

In 24.1: locally of finite type, finite type

In 25.1: surjective

In 26.1: monomorphism

In 27.1: closed immersion

In 29.1: topologically of finite type over

In 30.1: separated, quasi-separated

In 31.1: proper

In 34.1:  $small\ \acute{e}tale\ site$ 

In 37.3: completion of X along T

In 38.1: completion of X along Z

### Algebraization of Formal Spaces

In 4.1: rig-smooth over (A, I)

In 8.1: rig-étale over (A, I)

In 13.4: flat

In 14.2: rig-closed

In 14.7: completed principal localization

In 15.2: naively rig-flat

In 15.4: rig-flat

In 16.1: rig-flat

In 17.2: rig-smooth

In 18.1: rig-smooth

In 19.2: rig-etale

In 20.1: rig-étale

In 21.1: rig-surjective

In 24.1: formal modification

### Resolution of Surfaces Revisited

In 4.1: blowing up  $X' \to X$  of X at x

In 5.1: normalized blowup of X at x

In 8.1: resolution of singularities

In 8.2: resolution of singularities by normalized blowups

### Formal Deformation Theory

In 3.1:  $C_{\Lambda}$ , classical case

In 3.2: small extension

In 3.6: relative cotangent space

In 3.9: essential surjection

In 4.1:  $\widehat{\mathcal{C}}_{\Lambda}$ 

In 5.1: category cofibered in groupoids over  $\mathcal{C}$ 

In 6.1: prorepresentable

In 6.2: predeformation category, morphism of predeformation categories

In 7.1: category  $\widehat{\mathcal{F}}$  of formal objects of  $\mathcal{F}$ , formal object  $\xi = (R, \xi_n, f_n)$  of  $\mathcal{F}$ , morphism  $a : \xi \to \eta$  of formal objects

In 7.3: completion of  $\mathcal{F}$ 

In 8.1: smooth

In 8.9: versal

In 9.1: smooth, unobstructed

In 10.1: conditions (S1) and (S2)

In 11.1: R-linear

In 11.9:  $tangent \ space \ TF \ of \ F$ 

In 12.1: tangent space  $T\mathcal{F}$  of  $\mathcal{F}$ 

In 12.3: differential  $d\varphi: T\mathcal{F} \to T\mathcal{G}$  of  $\varphi$ 

In 14.4: minimal, miniversal

In 16.1: condition (RS)

In 16.8: deformation category

In 17.1: lift of x along f, morphism of lifts

In 19.1: group of infinitesimal automorphisms of x' over x

In 19.2: group of infinitesimal automorphisms of  $x_0$ 

In 19.5: automorphism functor of x

In 21.1: category of groupoids in functors on C, groupoid in functors on C, morphism  $(U, R, s, t, c) \rightarrow (U', R', s', t', c')$  of groupoids in functors on C

In 21.4: representable

In 21.7: restriction  $(U, R, s, t, c)|_{\mathcal{C}'}$  of (U, R, s, t, c) to  $\mathcal{C}'$ 

In 21.9: quotient category cofibered in groupoids  $[U/R] \rightarrow \mathcal{C}$ , quotient morphism  $U \rightarrow [U/R]$ 

In 22.1: prorepresentable

In 22.2: completion  $(U, R, s, t, c)^{\wedge}$  of (U, R, s, t, c)

In 23.1: smooth

In 25.1: presentation of  $\mathcal{F}$  by (U, R, s, t, c)

In 27.1: normalized, minimal

### **Deformation Theory**

In 3.2: strict morphism of thickenings In 9.2: strict morphism of thickenings

### The Cotangent Complex

In 3.1: standard resolution of B over A

In 3.2: cotangent complex

In 13.1: A-biderivation

In 17.1: Atiyah class

In 18.1: standard resolution of  $\mathcal{B}$  over  $\mathcal{A}$ 

In 18.2: cotangent complex

In 19.1: Atiyah class

In 20.1:  $cotangent\ complex$ 

In 22.1: cotangent complex

In 24.1: cotangent complex  $L_{X/Y}$  of X

over Y

In 26.1: cotangent complex  $L_{X/Y}$  of X

over Y

#### **Deformation Problems**

### Algebraic Stacks

In 8.1: representable by an algebraic space over S

In 9.1: representable by algebraic spaces

In 10.1: property  $\mathcal{P}$ 

In 12.1: algebraic stack over S

In 12.2: Deligne-Mumford stack

In 12.3: 2-category of algebraic stacks over S

In 16.4: smooth groupoid

In 16.5: presentation

In 19.2: viewed as an algebraic stack over S'

In 19.3: change of base of  $\mathcal{X}'$ 

### **Examples of Stacks**

In 18.2: degree d finite Hilbert stack of  $\mathcal{X}$  over  $\mathcal{Y}$ 

#### Sheaves on Algebraic Stacks

In 3.1: presheaf on  $\mathcal{X}$ , morphism of presheaves on  $\mathcal{X}$ 

In 4.1: associated Zariski site, associated étale site, associated smooth site, associated syntomic site, associated fppf site In 4.3: Zariski sheaf, sheaf for the Zariski

topology, étale sheaf, sheaf for the étale

topology, smooth sheaf, sheaf for the smooth topology, syntomic sheaf, sheaf for the syntomic topology, fppf sheaf, sheaf, sheaf for the fppf topology

In 4.5: associated morphism of  $fppf\ topoi$ 

In 6.1: structure sheaf of  $\mathcal{X}$ 

In 7.1: presheaf of modules on  $\mathcal{X}$ ,  $\mathcal{O}_{\mathcal{X}}$ -module, sheaf of  $\mathcal{O}_{\mathcal{X}}$ -modules

In 9.2: pullback  $x^{-1}\mathcal{F}$  of  $\mathcal{F}$ , restriction of  $\mathcal{F}$  to  $U_{\acute{e}tale}$ 

In 11.1: quasi-coherent module on  $\mathcal{X}$ , quasi-coherent  $\mathcal{O}_{\mathcal{X}}$ -module

In 12.1: locally quasi-coherent

In 24.1: associated affine site

In 24.2: associated affine Zariski site, associated affine étale site, associated affine smooth site, associated affine syntomic site, associated affine fppf site

In 26.1: triangulated category of quasicoherent objects in the derived category

# Criteria for Representability

In 8.1: algebraic

#### Artin's Axioms

In 5.1: condition (RS)

 ${\bf In}\; 9.1: formal\; object,\; morphism\; of\; formal$ 

objects, lies over In 9.4: effective

In 11.1: limit preserving

In 12.1: versal In 12.2: versal

In 13.1: openness of versality, openness of versality

In 18.1: condition  $(RS^*)$ 

In 22.1: obstruction theory, obstruction modules, obstruction

In 23.5: naive obstruction theory

### **Quot and Hilbert Spaces**

# Properties of Algebraic Stacks

In 4.2: point

In 4.8: topological space

In 5.1: surjective

In 6.1: quasi-compact

In 7.2: has property  $\mathcal{P}$ 

In 7.5: has property P at x

In 8.1: monomorphism

In 9.1: open immersion, closed immersion, immersion

In 9.9: open substack, closed substack, locally closed substack

In 10.4: algebraic stack structure on Z, reduced induced algebraic stack structure, reduction  $\mathcal{X}_{red}$  of  $\mathcal{X}$ 

In 11.8: residual gerbe of  $\mathcal{X}$  at x exists, residual gerbe of  $\mathcal{X}$  at x

In 12.2: dimension of X at x

In 12.3: dimension

In 13.1: number of geometric branches of  $\mathcal{X}$  at x, geometrically unibranch at x

# Morphisms of Algebraic Stacks

In 4.1: DM, quasi-DM, separated, quasi-separated

In 4.2: DM over S, quasi-DM over S, separated over S, quasi-separated over S, DM, quasi-DM, separated, quasi-separated

In 5.3: relative sheaf of automorphisms of x, relative sheaf of isomorphisms from  $x_1$  to  $x_2$ , sheaf of automorphisms of x, sheaf of isomorphisms from  $x_1$  to  $x_2$ 

In 7.2: quasi-compact

In 8.1: Noetherian

In 9.1: affine

In 10.1: integral, finite

In 11.2: open, universally open

In 12.2: submersive, universally submersive

In 13.2: closed, universally closed

In 14.2: universally injective

In 15.2: universal homeomorphism

In 16.2: has property  $\mathcal{P}$ 

In 17.1: locally of finite type, of finite type

In 18.2: finite type point

In 23.2: locally quasi-finite

In 24.1: quasi-finite

In 25.1: flat

In 26.2:  $flat\ at\ x$ 

In 27.1: locally of finite presentation, of

finite presentation

In 28.1: gerbe over, gerbe

In 33.1: smooth

In 34.2: has property  $\mathcal{P}$ 

In 35.1:  $\acute{e}tale$ 

In 36.1: unramified

In 37.1: proper

In 38.1: scheme theoretic image

In 39.1: dotted arrow, morphism of dotted arrows

In 39.6: uniqueness part of the valuative criterion

In 39.10: existence part of the valuative criterion

In 44.1: local complete intersection morphism, Koszul

In 46.3: normalization

In 48.1: decent In 50.1: integral

## Limits of Algebraic Stacks

In 3.1: limit preserving

# Cohomology of Algebraic Stacks

In 7.1: flat base change property

In 9.1: parasitic

In 14.1:  $lisse-\acute{e}tale$  site, flat-fppf site

In 17.2: coherent

### **Derived Categories of Stacks**

In 5.1: derived category of  $\mathcal{O}_{\mathcal{X}}$ -modules with quasi-coherent cohomology sheaves

### **Introducing Algebraic Stacks**

In 4.3: smooth

In 5.1: algebraic stack

#### More on Morphisms of Stacks

In 3.1: thickening, morphism of thickenings, thickenings over  $\mathcal{Z}$ , morphisms of thickenings over  $\mathcal{Z}$ 

In 3.3: first order thickening

In 8.1: formally smooth

In 12.1: categorical moduli space, uniform categorical moduli space, categorical moduli space in C, uniform categorical moduli space in C

In 13.1: well-nigh affine

### The Geometry of Algebraic Stacks

In 2.2: versal ring to  $\mathcal{X}$  at  $x_0$ 

In 3.4: multiplicity

In 4.1: formal branches of  $\mathcal{X}$  through  $x_0$ 

In 4.3: multiplicity of a formal branch of

 $\mathcal{X}$  through  $x_0$ 

In 5.2: the relative dimension

In 5.7:  $relative\ dimension$ 

In 5.14: pseudo-catenary

In 6.3: dimension of the local ring of  $\mathcal{X}$ 

# Moduli Stacks

# Moduli of Curves

In 16.4: moduli stack of smooth proper curves, moduli stack of smooth proper curves of genus g

In 19.2: relative dualizing sheaf

In 20.1: prestable family of curves

In 21.2: semistable family of curves

In 22.2: stable family of curves

In 22.4: moduli stack of stable curves, moduli stack of stable curves of genus g

### Examples

#### Exercises

In 2.1: directed set, system of rings

In 2.3: colimit

In 2.8: finite presentation

In 6.4: quasi-compact

In 6.6: Hausdorff

In 6.9: irreducible, irreducible

In 6.12: generic point

In 6.16: Noetherian, Artinian

In 6.18: irreducible component

In 6.22: closed, specialization, generalization

In 6.26: connected, connected component

In 9.1: length

In 18.1: catenary, catenary

In 22.1: finite locally free, invertible mod-

In 22.3: class group of A, Picard group of A

In 24.1: going-up theorem, going-down theorem

In 26.1: numerical polynomial

In 26.2: graded module, locally finite, Euler-Poincaré function, Hilbert function, Hilbert polynomial

In 26.3: graded A-algebra, graded module M over a graded A-algebra B, homomorphisms of graded modules/rings, graded submodules, graded ideals, exact sequences of graded modules

| In 27.1: homogeneous<br>In 27.2: homogeneous spectrum Proj(R)   | In 41.2: $\delta(\tau)$<br>In 49.1: Weil divisor, prime divisor, Weil |
|---|---|
| In 27.3: $R_{(f)}$  | divisor associated to a rational function                             |
| In 28.1: Cohen-Macaulay   | $f \in K(X)^*$ , effective Cartier divisor,                           |
| In 30.3: filtered injective                                     | Weil divisor [D] associated to an effec-                              |
| In 30.4: $Fil^f(\mathcal{A})$                                   | tive Cartier divisor $D \subset X$ , sheaf of total                   |
| In 30.6: filtered quasi-isomorphism                             | quotient rings $K_S$ , Cartier divisor, Weil                          |
| In 30.7: filtered acyclic                                       | divisor associated to a Cartier divisor                               |
| In 33.12: integral  | A Guide to the Literature   |
| In 35.1: dual numbers   |   |
| In 35.3: tangent space of X over S, tangent vector              | Desirables  |
| In 36.1: quasi-coherent   | Coding Style  |
| In 36.2: specialization In 36.5: locally Noetherian, Noetherian | Obsolete  |
| In 36.6: coherent   | In 23.7: $\epsilon$ -invariant  |
| In 40.1: invertible $\mathcal{O}_X$ -module                     | In 23.9: sum of the effective Cartier di-                             |
| In 40.4: invertible module M, trivial                           | visors  |
| In 40.7: Picard group of $X$                                    | GNU Free Documentation License  |

### 3. Other chapters

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