Guide to R package

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## Chapter 1

## Introduction

One of the greatest advantages of R: getting your work done better and in less time.

— Frank Harrell, Biostatistics, Vanderbilt University

This chapter presents basic information related to R software and is aimed at readers who have never heard about R, do not know how to work with it, or are perhaps not sure whether R is worth the effort.

We will begin by presenting the advantages of R. Next, we will discuss its history and development, followed by a presentation of what it feels like to work with R. We will use a simple example to show you how to read data, process it and create plots. After that, we will find out how to configure the environment and how to install its necessary components. Finally, we will list sources with further information related to R.

## 1.1 Data science, or why we should learn R

Data science is a dynamically growing discipline which combines data analysis and programming. There is an ever-increasing need for people who can analyse newly emerging data streams. In order to keep pace with the contemporary digital tsunami, we need robust tools to analyse data. One of such tools is the R language.

There are numerous programming languages, but R allows you to analyse data much quicker than any other language. You can go to <a href="http://bit.ly/2fXfWV2">http://bit.ly/2fXfWV2</a> (Video Introduction to R by Microsoft) to see a 90-second video which presents the potential of R software.

Why? R was created to facilitate working with data. The R language is a dialect of the S language developed by John Chambers from Bell Labs around 1976. The S language was developed for interactive data analysis. Numerous solutions were introduced to it to simplify data processing.

The first version of R was developed in 1991 by Robert Gentleman and Ross Ihaka (also known as R&R) who worked in the Department of Statistics at the University of Auckland. Initially, the R package was meant as a teaching resource at that university. At the same time, it was an open project, which is why it quickly gained in popularity. Since 1997, over twenty people worked on the development of R, thus constituting the so-called core team. The team comprises experts from various fields (statistics, mathematics, numerical methods, and computer science in a broad sense) from all over the world. The number of people developing R grew quickly. Today, the project is developed by "The Foundation for Statistical Computing" that has hundreds of members. Apart from that, there are thousands of people all around the world who share their own packages with various functions. The number of R libraries grows rapidly. In 2016, there were over 10,000 packages in the main CRAN repository (see Figure 1.1). Apart from that, there are thousands of packages that are private or placed in other repositories.

plot(1:5)

To tylko robocze odwołanie do rozdziału 1.2.1

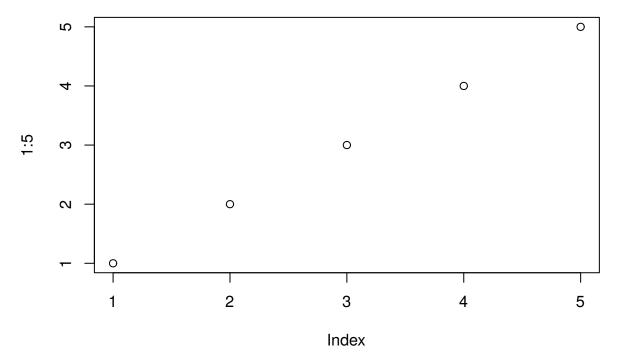


Figure 1.1: plot bar

To tylko robocze odwołanie do artykułu (Hettmansperger and Sheather, 1986) zamieszczonego w bibliografii.

$$f(k) = \binom{n}{k} p^k (1-p)^{n-k}$$
(1.1)

To tylko robocze odwołanie do równania (1.1).

R is a GNU project based on the GNU GPL license, which means it is free of charge for both educational and commercial use. More information about GNU GPL can be found at [53]. The R platform has excellent documentation available as PDF files or HTML pages. The documentation is mostly in English, but some files have other language versions as well.

The R language has been developed for people dealing with data from the very beginning. This is why it was frequently treated as a domain-specific language (DSL) by many computer scientists rather than a full-featured language. As time went by, however, the capabilities of R expanded and more solutions outside the field of data analysis appeared. Today, R is one of the most popular programming languages.

One evidence of this is the ranking created based on the votes by the IEEE committee members (Institute of Electrical and Electronics Engineer). In 2016, R ranked as the fifth most popular language, outrunning such languages as PHP or JavaScript.

There are multiple reasons behind the popularity of R. Below, we present those we consider the most significant ones.

- Because of its elasticity, R is nowadays the most basic language used when teaching statistics and data analysis, present at practically any good university.
- R software allows us to create and share packages that contain new functions. Currently, there are over 10,000 packages for multiple purposes, such as rgl for 3D graphics, lima for microarray data analysis, seqinr for genomics data analysis, psy with statistical functions commonly used in psychometry, geoR with geostatistical functions, Sweave for report generation using LaTeX, and many others. Everyone can create and share their own packages.
- The R software allows us to use functions written in other languages (C, C++, Fortran). What is more, we can execute functions available in R from other languages (Java, C, C++, Statistica packages, SAS,

and many others). Thanks to that, we can write most of our application in Java, and use R as a big external library with statistical functions.

• R software facilitates creating high-quality plots, which is of vital importance when presenting results. Even with their default settings, those plots look much better than their counterparts in other packages.

More about the history and development of R can be found at http://bit.ly/2domniT ("R Programming" at https://www.coursera.org/).

## 1.2 What working with R looks like

We work with R in an interactive way. The R software itself is often associated with a console that has a blinking cursor used to enter commands and read results.

We wanted to reflect this work style in this book, which is why we present sample code alongside the output generated by the software. Both R instructions and their results are presented against a grey background so that you can find them quickly. Results are presented on lines that start with a double hash sign (##).

For example, the substr() function cuts out a substring with the coordinates provided in the parentheses. When you run the R software, you only need to type the instruction below to see the result in the same console window. Here, the result will be a string containing a single R letter.

```
substr("What is supeR?", start = 13, stop = 13)
```

```
## [1] "R"
```

When we write about functions, packages, and language elements, we use a fixed-width font. Some key English terms are written in italics. When we first mention a function name from an untypical package, we mention the package name.

The ggplot2::qplot() notation signifies function qplot() in the ggplot2 package. Sometimes, there are multiple functions in different packages that have the same name. In this case, we can precisely specify the function by providing the name of the package in front of it. When we need to install or turn on an uncommon package to use a given function, it is better to know which package offers the given function. At the end of this book, there is an index of functions – they are presented both alphabetically and by packages.

## 1.2.1 Example: Poland in the FIFA ranking

Let us find out what "serious" work with R looks like based on the example below.

- We will use some functions from the rvest package to directly read Poland's FIFA rank from Wikipedia.
- We will use some functions from the tidyr and dplyr packages to transform the data into the appropriate form.
- We will use some functions from the ggplot2 package to graphically present the data.

The entire R code which deals with those 3 stages is quite short and easy to analyse in a step-by-step manner. Some elements may seem familiar while others will appear surprising. We will explain the meaning of each element in subsequent sections.

All R instructions contained in this book can be downloaded from <a href="http://biecek.pl/R">http://biecek.pl/R</a>. The R instructions provided will always yield the same results. The only exception from this rule are some plots that have been modified to increase their readability in print.

#### 1.2.1.1 Loading data

The code snippet below loads a data table from the Polish version of *Poland national football team* available on Wikipedia. We used rvest, a package which is very useful for downloading data from websites.

There are multiple tables on the site we are interested in. We get them all, and then choose the one with 14 columns. Having loaded the data, we show the first 6 rows.

```
library("rvest")
wikiPL <- "https://pl.wikipedia.org/wiki/Reprezentacja_Polski_w_piłce_nożnej_mężczyzn"
webpage <- read_html(wikiPL)
table_links <- html_nodes(webpage, '.wikitable')
tables <- html_table(table_links, fill=TRUE)
FIFA_table <- which(sapply(tables, ncol) == 14)
tab <- tables[[FIFA_table]]
head(tab)</pre>
```

#### 1.2.1.2 Data transformation

Another step after loading the data is cleaning and transforming it. To that end, we can use functions from the tidyr and dplyr packages. We will explain them in detail shortly. For the time being, we will provide an abbreviated explanation.

We change the data from the wide format, in which months are stored in different columns, into the narrow format, where all months are stored in a single column. Then, we change Roman numerals used for months into Arabic numerals. At this point, our data is ready to be presented graphically.

#### 1.2.1.3 Graphical data presentation

Now that we have loaded the data, it is time we looked at it. We can use the ggplot2 package for graphical presentation purposes. Below, we present instructions that will generate the chart visible in Figure 1.3, which is called a box plot. It presents the minimal, maximal, mid-range and interquartile rank of Poland in each year of the ranking. We can see when the most prominent changes took place and when Poland reached its best ranks.

```
library("ggplot2")
ggplot(data_long, aes(factor(Year), Rank)) +
geom_boxplot() + ggtitle("Rank of Poland in FIFA Ranking")
```

## 1.3 Setting up the environment

To enjoy a convenient R environment, we should follow the three steps below.

• Install the basic R environment, which comprises an interpreter and a basic set of packages. This set alone offers enormous capabilities. It will be enough for most users to analyse data, draw plots and perform other typical tasks.

- Install RStudio. It is a tool which facilitates working with the R software. It is not the only R editor out there, but seems to be the best solution. Similarly to R itself, the basic version of RStudio is free of charge.
- Install additional packages with useful functions. There are over 7,000 packages available now! You do not have to install them all at once. You will sometimes need new functions from new packages as you work with R, and it is only then that you should install them.

Below, we present a short summary related to each installation stage.

## 1.3.1 Installing basic R environment

The source and binary R files are available for most operating systems, including all Linux and Unix distributions, Windows 95 or higher, and Mac OS.

At the time of this writing, the latest R version is 3.3.2. Each year in April, there is another major 3.x version appearing, which means that we will soon enjoy version 3.4.0. During the year, further subversions are released as need be. R is being developed quickly and we should update it at least once a year to get its latest version.

In order to install R, go to <a href="https://cran.r-project.org/">https://cran.r-project.org/</a>, choose the operating system and download the binary file. The installation itself is as simple as clicking Next a few times. You can have a few versions of R installed at the same time. Keeping older versions of R may be useful when we want to reproduce the exactly same results in the future.

If you install R on a less typical platform, you can use the installation manual available at [49].

One useful feature of the R environment is that you can run it without installation. This means you can copy your R environment onto a CD, pendrive or external hard drive and run it on any other computer.

It is hard to estimate the minimal system requirements for R. Its basic version runs without problems on older computers with 256 MB of RAM, Pentium processors and a few dozen MB of space on the hard drive. However, even though the basic version is "lightweight", the installation of additional packages may require a few more GBs of RAM or hard drive space. Packages with big genomic data are particularly "heavy-weight".

Those using R for compute-intensive analyses should rather use the R version for OS X, Linux or Unix. These systems manage memory more efficiently, which means that R works (slightly) faster. Unix-based systems also provide additional tools that allow multiple threads and other system mechanisms (such us fork()).

## 1.3.2 Installing RStudio

You can work with the basic R software alone, but working with an editor is much more convenient, especially when R is our main tool at work. Currently, the best editor available free of charge is RStudio – a tool developed by a company under the same name. This editor is available for Windows, Linux and OS X alike, supports many advanced packages and functions of R.

RStudio is a tool which makes working with R easier. It is an editor, version manager, and debugger that makes creating packages, applications or reports easier. You can live without it, but it certainly helps much. The latest version of RStudio Desktop can be found at <a href="https://www.rstudio.com/">https://www.rstudio.com/</a>.

An example screenshot from the program is shown in Figure 1.5.

RStudio is very intuitive. Some of its interesting functions are:

- Ability to automatically send the whole script or a piece of it to the R console. After selecting a given code snippet and pressing Ctrl-Enter, it will be executed in the R console.
- Ability to manage multiple files and/or projects.

- Support for knitr, Sweave and shiny packages, easy navigation among code fragments.
- Support for R Notebooks, which allows interactive work with reports and running/updating code snippets.
- Showing objects (names, classes, dimensions) available in the namespace.
- Editor for data, functions and other R objects. When we click the name of a set present in the namespace, we can edit that object. It is often more convenient than using fix() or edit().
- A simplified way to load data using a graphical interface.
- Highlighting keywords and function names.
- Contextual name auto-completion for functions, variables, properties, function arguments (when we start typing names, a list with matches appears).
- Showing/hiding the code of functions or loops.
- Support for creating and testing new packages.
- Closing open brackets and quotes along with intelligent content highlighting.
- Intelligent insertion of indentation combined with syntax recognition (i.e. indentation is added in loops, functions, etc.).
- Interactive debugger.

RStudio Server is an interesting extension of RStudio Desktop. After installing it on a server, we can use R via our web browser. With the paid version, multiple users may open R at the same time.

Work in RStudio is much easier when you know some basic shortcuts. Below are those I personally find the most interesting. A very good description of RStudio alongside all keyboard shortcuts can be found at <a href="http://bit.ly/2d4B0Ix">http://bit.ly/2d4B0Ix</a> (so-called RStudio IDE cheatsheets). In the description below, Ctrl/Cmd means Ctrl for Windows/Linux and Cmd for OS X.

- Ctrl/Cmd+Shift+C, comment a line or multiple lines.
- Ctrl/Cmd+Enter, execute the highlighted code in the console.
- Ctrl/Cmd+Up, show the history of commands.
- Ctrl+L, clear the console.
- Ctrl+1-9, switch between application windows.
- Tab, autocomplete code a very useful feature indeed.
- Ctrl/Cmd+Shift+K, compile the current document.

## 1.3.3 Installing additional packages

Once we have the basic R environment in place, we already have access to various features. The real power, however, lies in the thousands of additional packages that contain further thousands of functions.

In order to use additional packages, we should follow these two steps:

- 1. Install a new package on the hard drive. You only need to do this once, the necessary files will be copied into the directory with packages. You can check the path to the directory with .libPaths().
- 2. Turn on the installed package in an active R session. This step must be performed every time we run the R environment. This will make the functions and datasets from the package available in the current session.

There are a few ways to install packages. We usually install them from the official CRAN repository (The Comprehensive R Archive Network). If the package we are interested in is available in CRAN, we can install it using install.packages().

For instance, the instruction below installs the Przewodnik package (Polish for *Guide*) directly from the CRAN repository alongside all the dependencies and datasets that we will use in this book. In order to install it, you only need to type the following code in the R console:

install.packages("Przewodnik")

Or choose Tools/Install packages... in RStudio.

Some packages are missing from the CRAN repository or are available in some older versions. For example, packages in CRAN are required to be 10 MB in size at most. Because of this limitation, greater packages must be stored elsewhere, typically in GitHub repositories. In order to install packages from GitHub, you can use the devtools:install\_github() instruction.

For example, if you want to install the latest version of our Przewodnik package from the pbiecek Github repository, you can use:

devtools::install\_github("pbiecek/PrzewodnikPakiet")

Apart from these two repositories, there are repositories for special purposes. For instance, many packages used in bioinformatical analyses can be found in the Bioconductor repository available at https://www.bioconductor.org/.

When we install a new package with data, functions and auxiliary files, they are stored on the hard drive of our computer. Before we can use them, however, we need to turn the package on. Each time we run the R platform, some basic packages such as base, graphics or stats are loaded. In order to use additional functions or datasets, we need to load (turn on) the package which contains them (assuming that the package is already installed). We use the library() instruction to turn packages on.

The instruction below turns on the devtools package. Once we execute this instruction, we can use the package without the need to add the devtools:: prefix.

library("devtools")

As we mentioned before, there are over 10,000 packages in the CRAN repository. It is difficult to find the feature we need in such a broad set. This is why we will use the following notation when using new functions: packageName::functionName(). ggplot2::qplot() means that the qplot() function can be found in the ggplot2 package. The index at the back of the book lists all functions both alphabetically and grouped by packages.

If we know the name of a function and want to find out the package that contains it, given that we do not have this book at hand, we can use the help.search() function. It will search through all installed packages and try to find the given name, or a function whose description contains the given search phrase. More information about this function and other means of searching information can be found in Section 1.4.

Once we have loaded the respective package, we can use its functions by providing their names. We can also explicitly name the package a function should come from. This might be useful when we have multiple functions with the same name in different packages. For example, both <code>epitools</code> and <code>vcd</code> packages contain an <code>oddsratio()</code> function, but each of them works in a different way. In order to specify the package, we can see the <code>:: operators</code>. The <code>:: operator</code> only allows referring to public functions of a package, whereas the <code>::: operator</code> also accepts references to private functions. Both lines of code below use the <code>seq()</code> function from the base package. The second method is useful when there are conflicting names of functions coming from different packages.

seq(10)
base::seq(10)

If we do not use the :: operator while there are multiple functions with the same name in different packages, R will use the function from the package loaded most recently.

## 1.4 Further information

In further parts of this book, we discuss libraries for data transformation, statistical modelling or visualisations. We are sure, however, that you will encounter problems or doubts not mentioned in this book. Where can you look for other types of information?

The easiest and quickest way is to ask someone who knows the answer and wants to help us.

It turns out that there is a large group of R enthusiasts who organise recurring meetups with presentations. In Poland, there are currently three major groups for R enthusiasts in three different cities. They meet once a month, more or less.

- SER: Warsaw R User Group Meetups. http://bit.ly/2epbNb9.
- eRka: Cracow Alternative for R Enthusiasts. http://bit.ly/2fJ5N9o.
- PAZUR: Poznan R User Group. http://bit.ly/2fKnTJE.

There are also substantial groups for R users in Wroclaw, Lodz and other cities where enthusiasts exchange information in data science meetups.

If we do not have an experienced friend, we can use the rich support system offered by R. First of all, there are built-in R functions that facilitate information lookup. The most useful ones among them are:

- The help() function which shows the welcome page of R's support system. The page describes the functions mentioned below in detail.
- Functions help("sort") and ?sort show a help page devoted to the sort function. Take a look at the example shown below as well. The format of descriptions is unified for ease of use. In RStudio, you can use the F1 button to activate help for a specific function. Further help sections contain the following information: concise function description (Description section), function declarations (Usage section), explanation of all arguments (Arguments section), detailed function description (Details section), literature (References section), links to other functions (See Also section) as well as usage examples (Examples section). If we provide the package argument, we will get help related to the given package. For instance, help(package=MASS) will show the description of the MASS package.
- args("functionName") shows the list of arguments of functionName.
- apropos("regression") and find("regression") list functions (and objects) whose names contain the regression substring.
- example("plot") runs a script with usage examples of plot function. Examples allow us to quickly find out how to use a function and what results we can expect.
- help.search("keyword") browses the descriptions of functions contained in the packages we have
  installed and shows those functions where keyWord was found. In this case, keyWord may also contain
  multiple words or a phrase. The result list will additionally provide information about which package
  contains the functions it found.

The code below presents a sample session in R. We are looking for information about the plot() function and functions to test hypotheses. On the first line, we show help related to the plot function, followed by usage examples. The next line shows all functions with the "test" word in their names, and the last one shows functions with the phrase "normality test" in their descriptions.

```
?plot
example(plot)
apropos("test")
help.search("normality test")
```

The functions shown above look for information on a given topic by browsing packages that are already installed on the hard drive. If this proves insufficient (chances are we do not have packages with potentially interesting functions installed), we can use the resources available on the Internet. Particularly useful are the following resources:

- Internet course in Polish called Pogromcy Danych (*Data Busters*), available at http://pogromcydanych. icm.edu.pl. The course is divided into a dozen or so short blocks with exercises, allowing us to check our level of expertise.
- StackExchange, a forum with numerous questions and hundreds of people eager to answer them. This forum often shows up in Google search results. It is available at <a href="https://stackexchange.com/">https://stackexchange.com/</a>.
- Manuals devoted to various aspects of programming in R or data analyses in R. They are available directly from R's Help menu, and at https://cran.r-project.org/manuals.html.
- *R-bloggers*, and aggregator of blogs devoted to R, which is often a source of interesting information: http://www.r-bloggers.com.
- Books devoted to R and data analysis using R. An up-to-date list of relevant books can be found at https://www.r-project.org/doc/bib/R-books.html.
- Websites with questions and answers related to statistics and programming. For instance, http://stats.stackexchange.com (questions related to statistics) or http://stackoverflow.com/questions/tagged/r (questions related to programming).

There are multiple materials available in the Polish language on the Internet. One of the first publications was *Wprowadzenie do środowiska R* by Łukasz Komsta [17], but new resources appear every year. A current list of Polish materials is available at https://pl.wikipedia.org/wiki/R.

John Chambers [5] published a useful book for those who wish to master the R language. If you want to learn statistical functions, in turn, we recommend a book by Brian Everitt [8]. Both books deal with the S language. However, it is almost identical with R from the user's point of view. There are also numerous books, websites, and electronic documents that deal with various aspects of the software and the R language itself. At the end of 2007, a comprehensive book by Michael Crawley [6] was published which is worth recommending. It presents both R itself, as well as multiple statistical procedures implemented in R. Besides, there are more and more books devoted to R software for special purposes, some examples being: a book prepared by Paul Murell devoted to graphics [21], a book by Julian Faraway about linear models [10], or another work by Brian Everitt which deals with statistics basics [9]. Springer has published over 45 books devoted to R in a series called Use R!, and each of them deals with a single subject, such as spatial data analysis, data visualisation, social or genomic data etc.

## **Chapter 2**

## R Basics

This chapter presents basic information necessary to start working with R. The first four sections introduce data loading from text files, discuss key data structures in R, and present selected descriptive statistics – both numerical and graphical. We will go back to data loading in Section 2.6, where we show how to load and save data in various formats.

Next, we will discuss the dplyr and tidyr packages. They allow us to perform most transformations and data aggregations such as filtering, grouping and aggregate creation. The last subchapter discusses how we can create automatic reports. It shows how we can use the knitr package and RStudio to immediately create easily readable reports.

## 2.1 Loading data

The two most popular formats to store data are text files and Excel/OpenOffice files. Both formats can be loaded into RStudio with just a few mouse clicks. You only need to choose File/Import Dataset, and a graphical interface for data import will appear – see Figure 2.1.

If we encounter an untypical file formatting, we can use a few control buttons to specify what the separator is, whether the first row contains headers etc.

If we do not use RStudio, we can use function read.table() to load data. An example of this function is given below.

File http://www.biecek.pl/R/auta.csv contains data on 2400 sales offers for cars of different makes. This data is stored in a file with .csv extension. Each offer contains 8 parameters which are separated with semicolons in the text file.

A fragment of the file is shown below.

```
"Make"; "Model"; "Price"; "HP"; "Capacity"; "Mileage"; "Fuel"; "Production"
"Peugeot"; "206"; 8799; 60; 1100; 85000; "gasoline"; 2003
"Peugeot"; "206"; 15500; 60; 1124; 114000; "gasoline"; 2005
"Peugeot"; "206"; 11900; 90; 1997; 215000; "diesel"; 2003
"Peugeot"; "206"; 10999; 70; 1868; 165000; "diesel"; 2003
"Peugeot"; "206"; 11900; 70; 1398; 146000; "diesel"; 2005
"Peugeot"; "206"; 19900; 70; 1398; 86400; "diesel"; 2006
```

The first argument of read.table() is the path to the file with the data. The file can be located on a hard drive, or on the Internet.

The next two arguments in the function execution below specify that the values in subsequent columns are separated with semicolons, and that the first row contains variable names.

The result of function read.table() – the table with data – is assigned to the vehicles symbol using the <- operator.

```
##
                   Cena KM Pojemnosc Przebieg Paliwo Produkcja
       Marka Model
## 1 Peugeot
              206 8799 60
                                 1100
                                         85000 benzyna
                                                            2003
## 2 Peugeot
                                 1124
                                                            2005
              206 15500 60
                                        114000 benzyna
## 3 Peugeot
                                 1997
                                                            2003
              206 11900 90
                                        215000 diesel
                                 1868
## 4 Peugeot
              206 10999 70
                                        165000 diesel
                                                            2003
## 5 Peugeot
               206 11900 70
                                 1398
                                        146000 diesel
                                                            2005
## 6 Peugeot
              206 19900 70
                                                            2006
                                 1398
                                         86400 diesel
```

The head() function shows the first 6 rows from the data set. This function allows us to quickly find out what the table contains.

In Section 2.6 we discuss more methods of data loading using various formats.

Once we have our data in place, it is time to work with it.

### 2.2 Data structures

The data we are going to work with is usually stored as a table or a vector of values. One of the basic operations on tables and vectors is selecting a subset of rows, columns or values. More information about various methods of data processing can be found in Section 2.5.

#### 2.2.1 Vectors

Vectors, or sequences of values of the same type, are the basic data structure in R. We can create sequences of numbers, strings, or logical values. For R, even a single number is a one-element vector.

Vectors can be created from smaller vectors using the c() function.

```
c(2, 3, 5, 7, 11, 13, 17)
## [1] 2 3 5 7 11 13 17
```

One particular group of vectors are sequences of consecutive numbers. The easiest way to create such sequences is by using the : operator.

```
-3:3
## [1] -3 -2 -1 0 1 2 3
```

If we need sequences of numbers with a step value other than 1, we may use the seq() function.

```
seq(from = 0, to = 100, by = 11)
## [1] 0 11 22 33 44 55 66 77 88 99
```

Many useful vectors are available in basic packages. Some examples are month names or subsequent letters.

```
month.name

## [1] "January" "February" "March" "April" "May"

## [6] "June" "July" "August" "September" "October"

## [11] "November" "December"
```

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```
LETTERS
```

```
## [1] "A" "B" "C" "D" "E" "F" "G" "H" "I" "J" "K" "L" "M" "N" "O" "P" "Q" ## [18] "R" "S" "T" "U" "V" "W" "X" "Y" "Z"
```

#### 2.2.1.1 Indexing vectors

You can use the [] operator to refer to the elements of a vector. Inside the square brackets, provide the vector of indices to read. Vector elements are numbered from 1. We can easily show indexing by selecting a subset of letters from the LETTERS vector.

```
LETTERS[ 5:10 ]

## [1] "E" "F" "G" "H" "I" "J"

LETTERS[ c(1, 2, 9:14) ]

## [1] "A" "B" "I" "J" "K" "L" "M" "N"
```

The length() function returns the number of elements in a vector. For example, it may prove useful when we want to select every second element from the vector. In the code below, we use seq() to build a sequence of indices made up of every second letter from the LETTERS vector.

```
every_second <- seq(from = 1, to = length(LETTERS), by = 2)
LETTERS[ every_second ]</pre>
```

```
## [1] "A" "C" "E" "G" "I" "K" "M" "O" "Q" "S" "U" "W" "Y"
```

Indices also accept negative numbers. This way, we can select all values except those with the indices provided.

```
month.name[ -(5:9) ]

## [1] "January" "February" "March" "April" "October" "November"
## [7] "December"
```

Vector elements can be assigned names when constructing a vector with the c() function, or at a later time with the names() function. If a given vector has names, then its elements can be referred to with those names instead of the indices.

```
value <- c(pawn = 1, knight = 3, bishop = 3,
rook = 5, queen = 9, king = Inf)</pre>
```

Getting a subvector is not the only aim of indexing. Often enough, we want to change the order of elements in a vector. In the sample code below, we reverse the order of elements by providing a new set of indices.

```
value[ 6:1 ]
## king queen rook bishop knight pawn
## Inf 9 5 3 3 1
```

Logical values are another useful method to select a subsequence of elements from a vector. The code below presents how we can choose all elements of a vector whose values are less than 6.

```
value[ value < 6 ]

## pawn knight bishop rook
## 1 3 3 5</pre>
```

#### 2.2.1.2 Changing vector elements

Vector indices are also useful when we only want to change some of the elements. We can choose a subset of vector elements, and then assign a value to it using the <- operator. In the example below, we change the value of the fourth and fifth elements of the value vector.

```
value[ c(4,5) ] <- c(6,7)
value

## pawn knight bishop rook queen king
## 1 3 3 6 7 Inf</pre>
```

In order to add new elements to the vector, we can use the c() function.

```
(value <- c(value, new_piece = 5))
## pawn knight bishop rook queen king new_piece
## 1 3 3 6 7 Inf 5</pre>
```

### 2.2.2 Data frames

The most widely used data structure in data analysis is called a data frame. Each data frame is a set of columns (variables), and each column is a vector of equal length. Columns may have values of different types. We will show you how to work with data frames using a small dataset called cats\_birds. The seven columns represent various traits of selected cats and birds.

```
library("PogromcyDanych")
head(koty_ptaki)
     gatunek waga dlugosc predkosc habitat zywotnosc druzyna
##
## 1 Tygrys 300
                      2.5
                                60
                                       Azja
                                                   25
                                                          Kot.
## 2
         Lew 200
                      2.0
                                80 Afryka
                                                   29
                                                          Kot
                                                   15
## 3
     Jaguar 100
                      1.7
                                90 Ameryka
                                                          Kot.
## 4
        Puma
               80
                                70 Ameryka
                                                   13
                                                          Kot
                      1.7
## 5 Leopard
               70
                      1.4
                                85
                                       Azja
                                                   21
                                                          Kot
## 6 Gepard
               60
                      1.4
                               115 Afryka
                                                   12
                                                          Kot.
```

#### 2.2.2.1 Indexing data frames

Data frames are structured as two-dimensional tables. In order to specify their elements, we must provide both the row and the column. To that end, we can use the [] or \$ operators. The latter will be discussed at the end of the current section.

When using the [] operator, we should separately specify the indices of rows and columns, and separate them with "," (commas). If indices of rows or columns are not specified, then all rows/columns will be selected.

The example below shows how to choose three rows from the cats\_birds data frame.

```
cats_birds[ c(1, 3 , 5) , ]
```

We can use indices for both rows and columns at the same time.

```
cats_birds[ c(1, 3, 5) , 2:5]
```

Each dimension can be indexed using the same rules that are applied to vectors. This means that (1) logical conditions can be indices, (2) we can refer to names, and (3) we can use negative indices.

In the example below, we only select animals that develop a velocity greater than 100 km/h. For each row that satisfies this condition, we show the species, velocity and length of the animal.

Individual columns of the data frame are vectors. If we refer to a single column, we will get a vector instead of a data frame. This is a very convenient property which makes the code much shorter on many occasions. However, there are situations where this notation leads to mistakes, which is why we need to be careful when selecting a single column.

We can choose a column by providing its number or name. The command below has the same meaning as cats\_birds[,4].

```
cats_birds[, "velocity"]
```

When we want to select a single column from a data frame, we can also use the \$ operator. It shortens the code by 4 characters. At the same time, it becomes much clearer that the result is a vector.

After the \$ operator, we can provide a full variable name, or just a part of it. If we only provide a part of it, we will get a column whose name starts with the part we provide.

```
cats_birds$velocity
```

The \$ operator also comes in handy when we add a new column to our data frame. We can add a new column with the given name at the end of the given data frame. Below, we change the unit, bearing in mind that 1 mile/h = 1.6 km/h.

```
cats_birds$velocity_miles <- cats_birds$velocity * 1.6
head(cats_birds, 2)</pre>
```

Another way to add a column is by using the cbind() or data.frame() function.

The rbind() function binds two data frames row by row, thus allowing us to add new rows. The dplyr package provides quicker versions of both functions. Their names are bind\_cols() and bind\_rows().

#### 2.2.3 Lists

The third most popular data structure used in R are lists. A list, just like a vector, is a sequence of values. Unlike a vector, however, a list can store elements of multiple types. A list element may be another complex structure, such as a data frame or another list.

Lists are created with list(). The example below shows how to create a list that contains a vector with numbers, letters and logical values.

```
triplet <- list(numbers = 1:5, letters = LETTERS, logic = c(TRUE, TRUE, TRUE, FALSE))
triplet</pre>
```

You can access list elements with [[]]. You can only select a single element.

If a list has a name, its elements can be referred to with the \$ operator in a way similar to data frames. Internally, data frames are represented as lists of equally long vectors.

```
triple[[2]]
triple[["logic"]]
triple$numbers
```

Lists are very useful when we need to process multiple data sets or when we want to generate multiple models. Both data sets and models can become list elements.

R contains many useful functions to work with lists. We will discuss them in Section 3.9.1.

## 2.3 Descriptive statistics

R is mainly used for data processing, analysis and visualisation. Subsequent parts of the present work are devoted to these three typical applications.

Before we discuss those complex applications, we will present some basic cases here. Variables in data analyses are usually characterised according to the classification by Stanley Stevens:

- Qualitative variables (also referred to as factors or categorical variables) are variables which can take
  on a limited number of values (usually non-numerical). They can be further divided into the following
  groups:
  - Binary variables (also known as dichotomous or binomial variables), such as gender (female/male).
  - Nominal variables (also known as unordered qualitative variables), such as car make: there is no specific order for car makes.
  - Ordinal variables (also known as ordered qualitative variables), such as education (primary/secondary/tertiary).
- Quantitative variables, which can be further divided into:
  - Count variables (count of occurrences of a given phenomenon expressed as a natural number), such as the number of education years.
  - Interval variables, measured on a scale where values can be subtracted, but not divided by each other, such as temperature in Celsius degrees, or A.D. year.
  - Ratio variables, measured on a scale where proportions are kept. This means that values can be
    divided by one another and there is a clear definition of 0.0. Examples include temperature in
    Kelvin degrees or height in centimetres.

In R, quantitative variables are represented with a numerical type called numeric. There are no separate types to describe numbers on a ratio scale or an interval scale.

Qualitative data in R are represented with a type called factor. factor variables can be additionally marked as ordered. In such cases, they have an additional class called ordered.

Binary variables can be represented with a logical type called logical. Table 2.1 presents some functions which calculate the most popular descriptive statistics. We will practice calculating descriptive statistics on a data set called socData from the Przewodnik package.

```
library("Przewodnik")
head(socData, 4)
```

### 2.3.1 Quantitative variables

Let us take a look at the values in the age column. We can refer to that column with socData\$age.

Age is a quantitative ratio variable (ratios make sense in this case; for example, we can say that someone is twice as old as someone else).

Our first question is: what are the lowest and greatest values that the age variable can take on? It is always a good idea to check boundary values as they may help us identify errors in data.

```
range(socData$age)

What is the mean age?

mean(socData$age)
```

And what is the trimmed mean calculated for the middle 60% of observations?

```
mean(socData$age, trim=0.2)
```

The median turns out to be close to the mean – that could mean there is no skewness.

median(socData\$age)

We can use the summary() function to quickly calculate the most important characteristics. In the case of quantitative variables, the result is given as a vector with the following values: the minimum, maximum, mean, median, first and third quartiles (also called lower and upper quartiles).

All of these values, apart from the mean, are always returned by the fivenum() function (the so-called fivenumber summary that divides the values observed into four equal parts). If there are missing observations in the variable, their count is also given.

```
summary(socData$age)
   Standard deviation:
sd(socData$age)
   Kurtosis / measure of tailedness:
kurtosis(socData$age)
   Skewness:
skewness(socData$age)
   Selected quantiles of the age variable:
quantile(socData$age, c(0.1, 0.25, 0.5, 0.75, 0.9))
```

One statistic which is frequently computed for multiple variables is called correlation. We can use the cor() function to calculate it. A correlation matrix is given below for three selected columns:

```
cor(socData[,c(1,6,7)])
```

### 2.3.2 **Qualitative variables**

Let us now take a look at the education column. We can refer to it by typing socData\$education.

Education is a qualitative variable. It can take on four different values and there is a natural order for

A contingency table is the most frequent statistic for qualitative variables. The example below uses the table() function:

```
table(socData$education)
```

This function defines a contingency table for one, two or more count variables. Contingency tables can also be obtained with xtabs() and ftable().

```
table(socData$education, socData$employment)
```

In the case of qualitative variables, the summary() function has a similar effect to the table() function. The only difference is that table() ignores NA data, whereas summary() provides their count.

```
summary(socData$education)
```

The summary() function can also take an argument of data.frame type. In this case, summaries are given for each column of the data frame.

```
summary(socData[,1:4])
```

Table 2.1: Descriptive statistics for a vector or matrix

Function	Description
•	base package
max()/min()	Maximal/minimal value in the sample.
mean()	Arithmetic mean, $\bar{x} = \sum_i x_i / n$ trim is an optional argument. When it is different
	than 0, a trimmed mean is calculated. A trimmed mean is calculated just like the
	arithmetic mean after removing 200% * trim of edge observations.
length()	Count of elements in the sample.
range()	Variability range of the sample, calculated as $[\min_i x_i, \max_i x_i]$ .
•	stats package
weighted.mean	Weighted mean, calculated as $\frac{1}{n}\sum_{i}w_{i}x_{i}$ . The weight vector $w_{i}$ is the second argument.
median()	Median (middle value).
quantile()	Q-quantile. The second argument of quantile() is the vector of quantiles to find. This function implements 9 different algorithms to find quantiles, see the description of type argument for more information.
IQR()	Interquartile range, i.e. the difference between the upper and lower quartile, $IQR = q_{0.75} - q_{0.25}$ .
var()	Variation in the sample. The unbiased estimator of variance is calculated as
	$S^2 = \frac{1}{n-1} \sum_i (x - \bar{x})^2$ . For two vectors, the covariance of these two vectors will be calculated. For a matrix, the covariance matrix for its columns will be calculated instead.
sd()	Standard deviation, calculated as $\sqrt{S^2}$ , where $S^2$ is the estimator of variance.
cor(), cov()	Correlation and covariance matrix. The arguments may be a pair of vectors, or a matrix.
mad()	Median absolute deviation, calculated as $1.4826 * median( x_i - median(x_i) )$ .
	other packages
kurtosis()	Kurtosis, measure of concentration, $\frac{n\sum_i(x_i-\bar{x})^4}{(\sum_i(x_i-\bar{x})^2)^2} - 3$ . The normal distribution has a kurtosis of 0. This function comes from the e1071 package.
	a kurtosis of 0. This function comes from the e1071 package.
skewness()	Skewness, measure of asymmetry, $\frac{\sqrt{n}\sum_i(x_i-\bar{x})^3}{(\sum_i(x_i-\bar{x})^2)^{3/2}}$ . The symmetric distribution has
	a skewness of 0. This function comes from the e1071 package.
<pre>geometric.mean()</pre>	Geometric mean, calculated as $(\prod_i x_i)^{1/n}$ . This function comes from the psych package.
harmonic.mean()	Harmonic mean, calculated as $n/\sum_i x_i^{-1}$ . This function comes from the psych package.
moda()	Mode, i.e. the most frequent value. This function comes from the dprep package.
moua()	In Linux, we can also use the mod() function from RVAideMemoire.
	" " " " " " " " " " " " " " " " " " " "

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## 2.4 Visual statistics

Below, we present the most popular plots used in data visualisation. Some less popular, yet equally interesting plots can be found in Section 5.5.

The examples below use the socData dataset from the Przewodnik package.

## 2.4.1 Bar plot, barplot() function

Bar plots are among the most popular data visualisation forms. When looking at the bars, we usually compare their relative length, which is why this data visualisation form is best suited for ratio variables.

The barplot() function (see Figures 2.2 and 2.3) is used to present data as horizontal or vertical bars. We can use a vector of values, or a two-dimensional matrix as its argument.

The horiz argument specifies whether bars should be drawn horizontally or vertically. The las argument denotes the direction in which axes descriptions should be written. The legend() function can be used to add a legend – more information can be found in Section 5.5.5.

The col argument allows us to pick colours for bars and legends. If add=TRUE is selected, bars are added to the existing plot instead of creating a new one.

The code below generates bars shown in Figures 2.2 and 2.3. The table() function calculates the frequency matrix, which is then drawn with barplot().

```
library("Przewodnik")
tab <- table( socData$education )
barplot(tab, horiz = TRUE, las = 1)
tab2 <- table( socData$sex, socData$education )
barplot(tab2, las=1, beside = TRUE)
legend("topright",c("female","male"),fill=c("grey","black"))</pre>
```

## 2.4.2 Histogram, hist() function

A histogram is undoubtedly one of the most popular visual statistics which presents the distribution of values for quantitative variables.

The hist() function (see Figures 2.4 and 2.5) is used to present the count of observations in certain ranges with bars. The first argument is a vector of numbers.

The breaks argument specifies how the data is broken into intervals. It can be a single number that depicts how many intervals should be created, or a string with the name of the algorithm that sets the intervals (as described below). The freq and probability arguments are used to specify whether representations of frequencies or probability densities should be plotted. The right argument specifies whether intervals should be treated as left-open or right-open.

If we do not specify the number of intervals, that number will be calculated based on the count of observations and the variance of our variable. To describe the number or width of the intervals, we can use the breaks argument. If we provide a single number as the argument, it will be treated as a suggestion as to the expected number of automatically created intervals (it is merely a suggestion, because hist() may slightly increase or decrease this number). If a vector of numbers is provided, it will be treated as a vector of points that separate the intervals (intervals do not need to be equally wide). If a string is provided as the argument, it will be interpreted as the name of the algorithm that should be used to specify the intervals (possible values are: "Sturges", "Scott", "FD" and "Freedman-Diaconis"). Below, we present two sample hist() function calls. You can see the results in Figures 2.4 and 2.5. We will start by presenting a histogram of the age variable. Since we have many rows in the data, we will suggest 15 intervals/boxes with the breaks argument. The other arguments in the code below describe the axes and the bar title.

```
hist(socData$age, breaks = 15, main="Age histogram", las=1,
    ylab="Count", xlab="Age")
```

By changing the colours of borders and bars, we can obtain a visually appealing histogram. We can also change the vertical axis to present frequencies instead of counts.

## 2.4.3 Box plot: boxplot()

One advantage of histograms is that they make it easy to identify regions of high or low density of values. On the other hand, they make it difficult to compare observation groups, because each group contains much information.

A box plot is a very popular way to compare distributions of values in groups.

The boxplot() function (see Figures 2.6 and 2.7) is used to present the distribution of a random variable with boxes. A single plot may be used to present the results for multiple variables (in order to compare their distributions), or to visualise a single variable split into observation groups (to compare its distributions in the groups).

The first argument of boxplot() denotes a vector, list of vectors, data frame, or formula with the variables that should appear in the box plot. Alternatively, multiple vectors of variables can be provided as subsequent arguments. If a vector of numbers is provided as an argument, a single box will be drawn. If multiple vectors are provided, multiple boxes will be drawn. If a formula that depicts the relation between a quantitative and qualitative variable is provided, a separate box will be created for each level of the qualitative variable.

Other arguments of boxplot() are:

- range specifies the range of an interval; observations outside this interval are treated as outliers,
- varwidth specifies whether the width of the box should be proportional to the square root of the count of observations in the vector,
- outline specifies whether outliers should be drawn.

Below, we present two examples of boxplot(). The results are shown in Figures 2.6 and 2.7.

Further vectors of numbers can be provided as subsequent arguments of boxplot(). The names argument can be used to specify axes labels. The horizontal argument is used to rotate the plot.

The first argument might be a formula. It is a convenient way to specify which groups should be compared. Below, we compare age within education groups. Additionally, with the vardwith argument, the box width reflects the count in the group that is compared.

Box plots resemble boxes with whiskers, thus they are sometimes referred to as box-and-whisker plots. Almost all observations are located between the whiskers (apart from outliers). Outliers are considered observations that are further away from the quartiles than 1.5 IQR (1.5 is the default value of the range argument). The box specified by the quartiles contains 50% of all observations. The diagram below explains the meaning of each element.

## 2.4.4 Kernel density estimator, density() function

Both histograms and boxplots present value distributions for vectors of numbers. Two other statistics which are often used to that end are called the kernel density estimator (a smooth version of a histogram; calculated with the density() function) and empiric distribution function (calculated with the ecdf() function).

The concept of kernel density estimation is to find the estimator of density in a given point based on the concentration of observations in its vicinity. The observations that lie closer to the point of interest influence the estimator with greater weights than those located further away. The template of weights is specified by a parameter called the kernel. Bandwidth, in turn, specifies which weights are considered close.

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The density() function (see Figures 2.8 and 2.9) finds the kernel density estimator for a vector of numbers. The first argument is the vector of values for which we want to calculate the density.

The from and to arguments specify the beginning and end of the range in which the density is calculated. The n argument denotes the number of points in which the density value should be calculated (the density is calculated for a regular point grid). The kernel and bw parameters are used to specify the kernel type and the bandwidth. The density() function returns a density class object whose components store the density values in the specified points. The objects of this class can be visualised with the plot() function.

The default density estimate value is calculated using a Gaussian kernel. You can browse the help for density() to find out about other kernel types and the differences between them. Many options are possible, for instance square or triangular kernels. See the kernel parameter for more information.

The bandwidth can be specified manually. Alternatively, you can specify a rule that will automatically set the best bandwidth. The stats package implements five different methods of automatic bandwidth selection.

The default rule is the "rule of thumb" (used when bw="nrd0"), as suggested by Silverman. According to this rule, the bandwidth h is calculated as follows:

$$h_{bw,nrd0} = 0.9 \min(\hat{\sigma}, IQR/1.34)n^{-1/5},$$
 (2.1)

where  $\delta$  is the standard deviation estimation , IQR is the interquartile range from the sample, and n is the number of observations. The "magical" constant 1.34 stems from the fact that  $IQR/1.34 \approx \sigma$  for a normal distribution. Another popular rule is the Scott's rule which is used when bw="nrd". The bandwidth is then calculated as follows:

$$h_{bw,nrd} = 1.06\hat{\sigma}n^{-1/5}. (2.2)$$

You can also choose other rules of bandwidth selection. For instance, you can choose some rules based on cross validation: unbiased - when bw="ucv", and biased - when bw="bcv". In most cases, the best bandwidth estimation is obtained with the Sheather-Jones method.

Below, we present examples of two density estimations calculated for different bandwidth parameters (the former was selected automatically, the latter - manually). You can see the results of those instructions in Figures 2.8 and 2.9.

```
plot(density(socData$age), main="Age distribution")
```

If we consider the smoothing bandwidth too wide, we can adjust it manually. The example below shows how to reduce it to the value of 1.5.

```
plot(density(socData$age, bw=1.5), main="Age distribution", type="h")
```

Another statistic which is helpful when we describe the distribution of a observation vector is the empirical distribution function. It can be calculated with the ecdf() function.

The empirical distribution function is a function which describes what percentage of observations have values which are less than x.

The ecdf() function returns an object of the ecdf class. An overloaded version of the plot() function is implemented for this class to visualise the empirical distribution (see the example in Figure 2.11).

```
plot(ecdf(socData$age), main="Age distribution function")
```

The distribution function can also be used to compare multiple observation groups. You only need to show distribution functions for different groups in a single plot (the add argument).

The example below shows two distribution functions in a single plot, one for men, the other for women.

```
library("dplyr")
men <- filter(socData, sex == "male")
women <- filter(socData, sex == "female")
plot(ecdf(men$age), main="Age / sex", pch=21)
plot(ecdf(women$age), add=TRUE, col = "grey")</pre>
```

## 2.4.5 Scatter plot, scatterplot() function

To show the relation between two numerical variables, scatter plots are frequently used.

R offers multiple ways of creating scatter plots. The easiest method is to use the plot() function. Below, however, we present the car::scatterplot() function, which provides some additional options. Among those options, there are: data presentation in groups, and the possibility to add a trend line or a curve to the data

The first argument can contain either two vectors representing variables to be shown in the diagram, or a formula specifying two variables from a given dataset.

By default, boxplots are also drawn in the axes. They visualise variable distributions. This behaviour can be changed by modifying the boxplots argument, e.g. boxplots="x" makes the boxplots appear only in the Ox axis. The car library features a copy of scatterplot() which is called sp(). It yields the same results, but is much quicker to type.

A scatter plot can also feature a linear regression line (the line is drawn based on the reg.line value, which is reg.line=TRUE by default; setting reg.line=FALSE will make the line disappear) and a smooth regression curve (the curve is only drawn when smooth=TRUE, which is the default value). In our example (Figure 2.13), the scatter plot for two variables (systolic and diastolic blood pressure) is presented in two subpopulations specified by the sex variable. The scatter plot allows us to see whether there is a clear relation between the variables studied, and whether that relation remains the same in the subpopulations.

The results of the instructions presented below are shown in Figures 2.12 and 2.13. The first argument of sp() is a formula which specifies which variable should be shown in the Ox axis, and which one in the Oy axis. The pch argument specifies the shape of the points drawn.

```
library("car")
sp(diastolic.pressure~systolic.pressure, data=socData,
    smooth=FALSE, reg.line=FALSE, pch=19)
```

After the | sign in the formula, we can also specify a conditioning variable. In the example below, each sex is drawn in the plot with a different shape and colour. Additionally, a trend line is added to each set of points.

```
sp(diastolic.pressure~systolic.pressure|sex, data=socData,
smooth=FALSE, lwd=3, pch=c(19,17))
```

Scatter plots are a very useful way to detect and describe linear or monotonic relations between pairs of variables.

When we have more variables, we can use the pairs(), scatterplot.matrix() or YaleToolkit::gpairs() functions. They draw a relation matrix between each pair of the variables analysed.

## 2.4.6 Mosaic plot, mosaicplot() function

How can we show a relation between two or more qualitative variables? One possibility is to use a bar plot (barplot()). Another method is to use a mosaic plot, which is less known, yet very powerful.

The mosaicplot() function (see Figures 2.14 and 2.15) presents the count of values in a dataset using rectangular areas. Those rectangles are placed in such a way that it is easy to notice (1) whether two variables correlate, and (2) what the frequencies for individual values and pairs of values are.

Let us present this kind of plot with two examples. The results of the instructions below are shown in Figures 2.14 and 2.15.

The first plot presents the relative frequency of various education groups. The rectangles have a fixed height, but they differ in width. The wider the rectangle, the more frequent the group.

```
mosaicplot(~education, data=socData, main="", border="white")
```

The other plot presents the relation between education and employment. Again, the width of a rectangle corresponds to the relative frequency of the given education group. The height, in turn, signifies the relative frequency of those employed in different education groups.

Importantly, the mosaic plot resembles a regular squared pattern when two variables are independent. Any kind of correlation is visible at first sight. The plot below shows that highest percentage of people employed is present among those with tertiary education.

One mosaic plot can show results for two or more enumerated variables. Still, attention should be given when selecting multiple variables - the higher the number of variables or the number of their values, the lower the readability of the plot.

## 2.5 How to process data with the dplyr package

R has thousands (thousands!) of functions to process data. Fortunately, we only need a few of them to start working with data in a convenient way.

The 80/20 principle (i.e. the Pareto principle, named after Wilfred Pareto) applies to data processing. This means that we only need to know a small portion of all available functions to work with the majority of data sets (i.e. 80% of all possible data).

Hadley Wickham prepared two packages, dplyr and tidyr, which provide only those really important functions. Each function performs an elementary operation, but various functions can be combined to perform all typical data operations.

Wickham calls functions from those packages verbs, and compares the analysis process to sentence construction. The basic verbs in this data analysis are:

- filter() choose the selected rows from the dataset,
- select() choose only the selected columns from the dataset,
- arrange() sort the selected rows based on the selected columns,
- mutate() add a new column with data or change an existing column,
- group\_by() / ungroup() group data based on the selected factor / remove grouping,
- summarise() find specific aggregates in each group,
- gather() / spread() transform data between wide and long formats.

Those basic verbs are described in subsequent sections of this chapter. More functions to explore data are presented in a cheat sheet developed by RStudio, available at their website [26] or at http://bit.ly/1LaYWBd.

#### 2.5.1 How to filter rows

Filtering rows that satisfy a given condition or conditions is one of the most frequent data operations.

The filter() function from the dplyr package performs filtering. Its first argument is the dataset, and further arguments define logical conditions.

The result of this function contains rows the satisfy all of the conditions specified. When specifying the conditions, we can use column names from the dataset without additional links.

We will present that with an example. Below is an instruction that chooses only those offers where Model == "Corsa" from the vehicles dataset:

```
library("dplyr")
CorsaOnly <- filter(vehicles, Model == "Corsa")
head(CorsaOnly)</pre>
```

We can specify multiple conditions simultaneously. The example below finds rows with Corsa vehicles and Diesel engines that were manufactured in 2010.

#### 2.5.2 How to choose columns

Sometimes, we only need a portion of all columns from a dataset. We can remove the unnecessary columns to make our work quicker.

Another advantage of choosing only those columns that we really need is that it is easier to show data. Instead of showing all columns, even those that are unnecessary, it is better to only show those that are important to us.

The select() function from the dplyr package allows us to choose one or more variables from the data source. The first argument is the data source, and subsequent arguments define the columns that we want to choose.

The example below selects only three columns: make, model and price.

```
threeColumns <- select(vehicles, Make, Model, Price)
head(threeColumns)</pre>
```

We can use names to select columns, but also use the negation operator "-" (minus sign), which selects all columns except those specified, or functions matches(), starts\_with() and ends\_with(), which choose only those rows that satisfy the respective conditions.

In the example below, we select only those columns that start with an M.

```
head(select(vehicles, starts_with("M")))
```

#### 2.5.3 How to create and transform variables

Data modelling and processing frequently requires creating new variables based on existing ones. Sometimes, based on the price, we create the logarithm of price (a single variable from a single variable). Sometimes, based on the weight and height, we create the BMI (a single variable from multiple variables).

The mutate() function from the dplyr package is used to conveniently create additional columns in a dataset by transforming existing columns.

We will show this function using the vehicles dataset from the Przewodnik package. It is a dataset with car offers from the otomoto.pl website from 2012.

We will start the example by specifying the age of the cars offered. Since the offers come from 2012, and the manufacture year is placed in the Production column, the age of the car can be calculated as 2013 - Production.

In the next step, we calculate the average mileage in a single year. We will need data from two columns.

Column processing can be more complex than arithmetic transformations and can involve any variables, not just numerical ones. In further chapters, we will discuss operations on strings, logical values and factors.

### 2.5.4 How to sort rows

Sorting data by a given column makes it much easier to analyse values in that column. First of all, we can immediately identify outliers. Sorting rows is therefore useful when exploring data.

We can use the arrange() function from the dplyr package to sort by one or more variables. When there are equal values in the first criterion, further criteria influence the order.

In the example below, the data is first sorted by the Model column. When there are identical values in the Model column, the order is decided based on the Price variable.

```
sortedVehicles <- arrange(vehicles, Model, Price)
head(sortedVehicles)</pre>
```

To reverse the sorting order, the variable should be surrounded with a desc() function execution.

```
sortedVehicles <- arrange(vehicles, Model, desc(Price))
head(sortedVehicles, 2)</pre>
```

#### 2.5.5 How to work with streams

We usually process data in multiple steps. We perform operation A, then B, then C, etc.

When we look at some R code, we should be able to easily grasp what operations are performed. This makes code analysis quicker - be it when we look for errors, or when we want to show our code to other people.

Streams are a mechanism introduced to R recently, but they are quickly gaining supporters. They have three main advantages: make our code shorter, increase its readability, and make it easy to add further processing steps.

### Onion problem

To present streams, we will first consider a series of fours instructions:

```
KiaOnly <- filter(vehicles, Make == "Kia")
sorted <- arrange(KiaOnly, Price)
fourColumns <- select(sorted, Model, Price, Mileage, Production)
head(fourColumns, 4)</pre>
```

In R, the result of one function can be directly passed as an argument to another function. To make the code shorter, the "big onion" syntax is often introduced.

Such an "onion" should be read from the inside. First, we apply filtering, then sorting, then selecting four columns. Finally, we select the first four rows.

The problem is that this syntax does not read easily, particularly when we look at the outer functions. In the example above, the head() function takes two arguments, but the first argument is six lines of code long, and the other one is only mentioned on line seven. With longer "onions", it is even more difficult to find out which arguments belong to which functions.

#### How the stream operator works

To get rid of the "onion", we can use a special operator for stream processing: %>%. This operator comes from the magrittr package, but is also available when we turn on the dplyr package.

To remember what this operator does, we can use a simple example of a function with two arguments. The following code:

```
a %>% function(b)
  means:
function(a,b)
```

We can also use this operator with functions that take more than two arguments. The %>% operator passes the left-hand side as the first operator of the function specified on the right.

If we want to pass a value to the second or a subsequent argument, we can specify this argument with a dot ".", as shown in the example below:

```
a %>% function(b, data=.)
```

#### Streams in action

The "onion" shown above can be rewritten in the following way:

```
vehicles %>%
  filter(Make == "Kia") %>%
  arrange(Price) %>%
  select(Model, Price, Mileage, Production) ->
  sorted
head(sorted)
```

In the example above, we also used the -> assignment operator. Thanks to this, we can consequently read the elements of the stream from left to right.

The -> operator works like <-, the only difference being that it assigns the result to the variable on the right, not on the left.

The functions from the dplyr package are defined in such a way that their first argument is always a dataset. Thanks to this, the default behaviour of the %>% operator makes our code much shorter and more understandable even with big sequences of function calls.

In the case of functions that take datasets as the second or even further arguments, we also need to use the "." symbol (dot). This symbol denotes where the left side of the %% operator should be placed. Let us take a look at an example with the lm() function which builds a linear model. This function expects the data to be passed as the second argument. This means we need to use the "." symbol.

```
vehicles %>%
  lm(Price~Mileage, data = .) %>%
  summary()
```

In the example above, we do not need to specify the argument using data=, but we did so nevertheless to increase code readability.

Notice that streams are not only easier to read, but they are also easier to comment. A comment line can be placed before each line of a stream to describe what happens in the specific place.

## 2.5.6 How to compute aggregates/statistics in groups

A frequent operation on datasets, particularly on the big ones, is the calculation of statistics/summaries/aggregates on subsets of data.

To find such aggregates with the dplyr package, we can use the summarise() and group\_by() functions. The first function specifies the statistics that we want to calculate, whereas the second function describes the groups we want to create.

We present those functions below one after another.

#### Aggregates

We can use summarise() to find aggregates in datasets.

For instance, the instruction below calculates the mean price, median mileage, and mean age in the vehicles dataset.

An aggregate is not always related with value transformation in a column. For instance, the count of rows is a useful statistic which does not depend on the values in the dataset. An aggregate like shown above is set with the n() function.

#### Grouping

The group\_by() function is used to define groups for further processing. The function itself does not modify data. It only adds a tag which specifies the grouping variable. Further functions of a stream use this tag to perform processing in groups.

The group\_by function influences other functions from the dplyr package in an intuitive way.

- The summarise() function, which computes statistics, will find statistics for each possible combination of grouping variables.
- The arrange() function, which sorts rows, will first sort rows by the grouping variable.
- The sample\_n() functions, which filters rows, will sample data independently in each group.
- The mutate() function finds each aggregate within a group, which makes it easy to normalise variables in groups.

The example below calculates four statistics (mean price, median mileage, mean vehicle age, and count of offers) in groups specified by the make.

Aggregates are an ordinary data frame, which means we can perform subsequent operations on them, such as sorting.

The example below modifies the Mileage variable. It divides Mileage by the mean mileage for the given make.

```
vehicles %>%
  select(Make, Price, Mileage, Model) %>%
  group_by(Make) %>%
  mutate(Mileage = Mileage/mean(Mileage, na.rm=TRUE))
```

## 2.5.7 Wide and long formats

Many functions assume that data is structured as tables in which rows are subsequent observations and columns are variables describing those observations. This data format is expected by packages such as dplyr, ggplot2 and others.

However, data is sometimes given in other formats. Sometimes, the same variable is described by many columns, or multiple variables are provided a single column. Some functions from the tidyr package are used to transform various data formats.

We will present those data formats and the functions used to transform them on some sample data from Eurostat. We will get this data using the eurostat package. Below, we load data from the tsdtr210 table in which Eurostat gathers information about the popularity of various means of transport in various countries.

```
library("eurostat")
tsdtr210 <- get_eurostat("tsdtr210", time_format="num")
head(tsdtr210, 4)</pre>
```

The data is given in the long format. What this means will become clear once we present the wide format. In this example, the geo column specifies the country, the time column specifies the year, the vehicle column specifies the means of transport, and the values column specifies the popularity of a given means of transport in the given country and year.

#### Spread onto columns

To transform data from the long format to the wide format, we can use the spread() function. The name wide format comes from the fact that it contains more columns. New columns in the wide format correspond to the values of a single column in the long format.

The spread() function expects three arguments. The first argument is, naturally, the dataset. The second argument is the key corresponding to column names, and the last argument are the values to be written into the specific columns. Rows in the new table are chosen as unique values in the other columns.

In the example below, the time function is changed from the long format to the wide format in which names correspond to subsequent years - values from the time column. The values in new columns are copies from the values column in the long data format.

```
library("tidyr")
wideFormat <- spread(tsdtr210, time, values)
wideFormat %>% filter(geo == "PL")
```

The data in the tsdtr210 table describes values in intersections through four dimensions (unit, vehicle type, country, year). Each dimension can be used to create new columns in the wide format.

In the example below, subsequent columns are created based on the goo column in the long format.

```
wideFormat2 <- spread(tsdtr210, geo, values)</pre>
```

We can show the rows for year 2010 (some columns are omitted).

```
wideFormat2 %>% filter(time == "2010")
```

#### Gather into columns

The opposite of spreading a single column into multiple columns is gathering multiple columns into a single column. This can be accomplished with the gather() function.

This function takes a dataset as the first argument. Further two arguments specify column names with keys and values, while the other arguments point to those columns from the old dataset that should be gathered together in the new dataset. We can use the minus sign notation "-" which means "everything except…".

In the example below, we transform the wideFormat data frame into the long format in such a way that all columns except for geo and vehicle are transformed into a column called value. This is why the result

contains the geo and vehicle columns (skipped when gathering) as well as year and value (results of gathering).

```
wideFormat %>%
  gather(year, value, -geo, -vehicle) %>%
  tail()
```

To show an example of 4 rows, we used the tail() function which shows the last 6 rows, because the first six rows are NA values.

## 2.5.8 Uniting/separating columns

When we work with data, we often want to unite multiple columns into one, or split a column into multiple columns.

#### **Uniting columns**

We can use the unite() function to merge a few columns into a single column.

The code below unites values from columns geo and time into a single string column geo\_time.

```
unite(tsdtr210, geo_time, geo, time, sep=":") %>%
head(4)
```

Uniting columns is frequently useful when we want to group rows by multiple variables. We can then unite such columns, and group rows by the new, united column.

#### Separating columns

The opposite of uniting is separating. Here, we can use the separate() function.

We will show an example of an artificial dataset with two columns: data and identifier.

In the example below, the separate() function creates three new columns based on the dates column. The columns are filled with parts of the old column separated with the - sign.

The length of the into vector specifies the number of columns to be created after separation. If the column that is being split contains too few or too many values (e.g. only two elements separated with a separator), then separate() will produce warnings by default. Additional extra and fill arguments can be used to specify what should happen when some data is missing.

### 2.6 How to load and save data in various formats

In this subchapter, we will present how to load tabular data from various sources. We will discuss all kinds of formats, since we understand that people who use R have various needs. For typical cases, you will only need to read the first three sections that explain how to load data from packages, text files and Excel files.

Generally speaking, data sets can have various structures. They can be expressed as graphs, trees, they may describe photos or multimedia files. All of these structures can be loaded into R and analysed. Most of the time, however, the data sets that we work this have a tabular structure with columns and rows clearly marked. We will put focus on this sort of structure in the following subchapter.

## 2.6.1 Loading data from text files

Loading data from packages is the easiest case. You only need to turn the given package on using library(), and then use data() to load a given file. A single package can store multiple datasets, which is why packages are often used as storages of useful data.

One of such packages is the PogromcyDanych package (Polish for Data Busters). It contains various datasets which we use in the present book, such as cats\_birds. Once we install the PogromcyDanych package, we only need two lines of code to use this dataset:

```
library("PogromcyDanych")
data("cats_birds")
```

A new symbol for the dataset should appear in the Environment of RStudio. We can see the first few rows using the head() function.

```
library("Przewodnik")
head(cats_birds)
```

The cats\_birds dataset contains 7 columns that describe various parameters of sample animals. To show the list of all datasets in a given package, we can also use the data() function:

```
data(package="PogromcyDanych")
```

## 2.6.2 Loading data from text files

Text files are a very popular format to store data. Their contents can be displayed in any text file, or in RStudio. They usually have the .txt, .csv (comma separated values) or .tsv (tab separated values) extension. In such files, subsequent column values are separated with some sort of separators, such as tabs, commas, semicolons, or other characters.

We will now analyse an example data set available on-line at http://biecek.pl/R/dane/cats\_birds.csv. The file contents is presented below:

```
species; weight; length; velocity; habitat; lifespan; team
Tiger; 300; 2, 5; 60; Asia; 25; Cat
Lion; 200; 2, 0; 80; Africa; 29; Cat
Jaguar; 100; 1, 7; 90; America; 15; Cat
Puma; 80; 1, 7; 70; America; 13; Cat
Panthera; 70; 1, 4; 85; Asia; 21; Cat
Cheetah; 60; 1, 4; 115; Africa; 12; Cat
Snow leopard; 50; 1, 3; 65; Asia; 18; Cat
Swift; 0, 05; 0, 2; 170; Eurasia; 20; Bird
Ostrich; 150; 2, 5; 70; Africa; 45; Bird
Golden eagle; 5; 0, 9; 160; North; 20; Bird
Peregrine falcon; 0, 7; 0, 5; 110; North; 15; Bird
Gerfalcon; 2; 0, 7; 100; North; 20; Bird
Albatross; 4; 0, 8; 120; South; 50; Bird
```

We can see that the file contains a table of values separated with semicolons. The first row is the header with column (variable) names:

```
species; weight; length; velocity; habitat; lifespan; team
```

Further rows contain the values of these variables. A description of the logical structure of this file is presented in Figure 2.16.

To load data in this format into R, we can use the read.table() function. It has many parameters which are described in detail later. In the example below, the table of values that we loaded is assigned to the cats\_birds symbol using the <- symbol.

Data can be loaded from a file located on a hard drive, or downloaded directly from the Internet. In this case, we need to specify the following arguments:

- file="http://biecek.pl/R/cats\_birds.csv", i.e. text file path,
- sep=";", which defines the separator character,
- dec=",", which defines the decimal point; usually a dot, but can also be a comma, as shown in this file,
- header=TRUE, which informs that the first row contains headers and not values.

To find out whether data has been loaded correctly, we can again use the head() function. Alternatively, you can also use the Environment tab in RStudio, as shown in Figure 2.18.

```
head(cats_birds)
```

Loading big files with read.table() can take a lot of time. In such cases, you may consider using the data.table::fread() function, which is much faster and has a similar number of parameters.

#### 2.6.2.1 read.table() in detail

Unfortunately, there is no single universal format to store data in text files. Separators, decimal points, comment lines or strings can be defined with various characters.

The read.table() function is able to load data written in virtually any format. It is, however, only possible with a major number of additional options. The declaration of read.table() is as follows:

In the utils package, there are four other functions that work in the same way, but have other default values.

If we saved the data in the CSV format using the Polish version of Excel, semicolons will be used as separators, and commas as decimal points. In such cases, the read.csv2() function is most suitable. If we use the English version of Excel, dots will be used as decimal points, and the read.csv() function will be a better solution.

Table 2.2 presents the descriptions of read.table() arguments. The English version of these descriptions can be found in the help file: ?read.table. As can be seen, there are many arguments, and we suggest you read about each of them at least once.

Table 2.2: Arguments of 'read.table()'

Function	Description
file	String value. It is the only obligatory argument which must be explicitly provided. Its value is the file path where the data is stored. We can provide a local file, or a file from the Internet by providing the URL that specifies the server and directory of the file. This field can also specify a connection or a socket. If we provide "clipboard" instead of a file name, data will be read from the system clipboard, which is a convenient way of loading data from various MS Office programs.
header	Logical value. If it is TRUE, the first argument will be treated as a list of columns. If this argument is not provided, and the first line contains one field less than other lines, R will automatically treat this line as the header.
sep	String value. The given string will be treated as the field separator. The default "" value treats each whitespace (single space, multiple spaces, tabulator, new line) as a separator.
quote	String value. It defines the character that represents the decimal point. If data is saved according to Polish standards, the comma sign "," is the decimal point.
row.names	A vector of strings or a single number. If a vector of strings is provided, it will be treated as the names of subsequent rows. If this argument is a number, it will be treated as the ordinal number of the column in the loaded file that contains row names. If the data contains a header (i.e. header=TRUE) and the first line has one field less than other lines, then the first line is automatically treated as a vector with row names.
col.names	Vector of strings. Column names can be specified with this argument. If it is not provided, and the file does not contain a header, then subsequent column names start with the letter "V", followed by increasing integer numbers.
nrows	Numerical field. Specifies the maximal number of rows to be read.
skip	Numerical value. Specifies the number of initial lines that should be ignored when reading the file.
check.names	Logical value. Specifies whether column names should be checked for correctness (i.e. without illegal characters or repetitions).
as.is	Vector of logical or numerical variables. By default, each field which is not converted into a real number or logical value is converted into a factor type variable. If the as.is parameter is a vector of logical values, then it indicates which columns can be converted into the factor type, and which cannot. A vector of numbers, instead, is treated as indexes of columns which should not be converted.
na.strings	Vector of strings. Indicates which values should be treated as NA, i.e. which values are used for missing observations. Additionally, empty fields in columns with numerical or logical values are marked as missing observations.
colClasses	Vector of characters. Each character specifies the type of a single variable (column). Possible values are: (1) NA - default value, signifies automatic conversion, (2) NULL - a column will be skipped, (3) one of atomic classes (logical, integer, numeric, complex, character, raw, factor, Date or POSIXct).
fill	Logical value. If subsequent lines have different numbers of values, and fill=FALSE (default value), then read.table() will throw an error. If fill=TRUE, shorter lines will be complemented with NA values to get the same line length.
blank.lines.s	Logical value. When TRUE, empty lines will be skipped while reading the file.
comment.char	Character value. This character is treated as a comment character. All remaining characters in a given line after this character will be ignored.
allowEscapes	Logical value. When TRUE, special escape characters are recognised. For instance, or are changed into tabulators or new line characters, respectively. FALSE (default value) means the text will be read literally, without any escape characters.
stringsAsFactors	Logical value. If TRUE, strings will be converted into factor types. If FALSE, they will be represented as strings. The default value is TRUE.

### 2.6.3 Saving data into text files

#### 2.6.3.1 write.table() function

The write.table() function saves the values of a variable (atomic variable, vector, matrix or data frame) into a text file with a given formatting style. Below, we present the full declaration of this function:

Similarly to read.table(), the utils package features two functions that work in the same way as write.table(), but use other parameterisation of default arguments. Both functions are used to save data in the csv format.

```
write.csv(x, file = "", sep = ",", dec=".", ...)
write.csv2(x, file = "", sep = ";", dec=",", ...)
```

Table 2.3 describes all parameters of write.table() based on the help file: ?write.table. Below, we show a few examples of how to save a vector, number or a data frame into a file.

This instruction prints a vector of numbers onto the screen instead of saving it into a file:

```
write.table(runif(100),"")
```

This instruction will write a vector into the clipboard:

```
write.table(1:100,"clipboard",col.names=FALSE, row.names=FALSE)
```

This instruction will write a string into a text file:

```
write.table("Monday","c:/worstWeekday.txt")
```

This instruction will save data in the CSV format into a file:

```
write.csv2(iris, file="forExcel.csv")
```

Writing big objects of data.frame type into text files may be time-consuming. This happens due to the fact that formatting is switched between various columns that can present data of various types. R checks the type of each column and row, and formats the values based on their types. To speed up the process, it is sometimes better to convert the data into a matrix using as.matrix().

## 2.6.4 Loading and saving JSON data

Previously, we mainly discussed tabular data, but not all data can be saved as tables.

A universal and very flexible format used to transport various data sets is JSON (*JavaScript Object Notation*). It is frequently found in solutions that use Internet communication, such as REST services.

JSON is a text format (which means it is human-readable), describes data with a hierarchical structure (which is a very flexible solution), and is lightweight (does not take much space).

Below, we present a sample JSON file. It describes a two-element list whose first value is a string, and the second value is a table.

```
{ "source": "Przewodnik",
   "indicators": [
          {"year": "2010", "value": 15.5},
          {"year": "2011", "value": 10.1},
          {"year": "2012", "value": 12.2}
] }
```

Function	Description
X	Object to save. Obligatory field. This object is usually a matrix or a data frame.
file	String value. Represents the path to the file in which the data should be written.  This field can also represent a connection or a socket, just like read.table().
	Similarly, if we provide "clipboard" instead, the data will be saved into the clipboard. The "" value will print the object to the console.
qmethod	String value. Indicates how special characters should be marked. "escape"
1	value is a C-style marking (with a backslash sign), while "double" value means
	a double backslash should be used instead.
sep	String value. This string will be treated as the separator of subsequent fields (the
_	separator does not need to be a single character).
eol	String value. This string will be used as a line ending string. In Windows, the
	default value is eol=" ".
quote	Logical value. TRUE means that factor types and strings will be surrounded
	with quotes "".
dec	String value. This field defines the decimal point. By default, it is a "." (dot). If
	the data is written in accordance with Polish standards, then the decimal point
	should be a "," (comma).
row.names	Vector of strings or logical value. If a vector of strings is provided, it will be used
	to name subsequent rows. If a logical value is provided, it will specify whether
	row names should be written or not.
col.names	Vector of strings or logical value. If a vector of strings is provided, it will be used
	to name subsequent columns. If a logical value is provided, it will specify
	whether column names should be written or not.

Table 2.3: Arguments of 'write.table()'

In R, there are a few packages to read or write JSON files. The three most popular ones are RJSONIO, rjson and jsonlite. Each of them contains a toJSON() function which converts data into JSON, and a from JSON() function which loads data from JSON.

The most stable option is the <code>jsonlite</code> package. Below, we only present some examples for this package. From JSON to R: The data we load is initially a list. The structure is simplified into a data frame or a vector, where possible.

```
fromJson({"source": "Przewodnik","indicators": [{"year": "2010", "
  value": 15.5},{"year": "2011", "values": 10.1},{"year": "2012", "
  value": 12.2}]})
```

From R to JSON: The example below shows how to convert the first two rows of the cats\_birds data frame:

```
toJSON(cats_birds[1:2,])
```

# References

Hettmansperger, T. P. and Sheather, S. J. (1986). Confidence intervals based on interpolated order statistics. *Statistics and Probability Letters*, 4(2):75–79.