



# !!! TITLE

## USING CLUSTERING TO IDENTIFY 3 MILLION NEW ASTEROIDS

PREPARED BY

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# MILLIONS OF MISSING ASTEROIDS!

## CONNECTING PARTIAL ASTEROID TRACKLETS

Mandate from Congress:  
>90% of potentially hazardous asteroids  
must be tracked

Currently, we have 170m observations of  
known asteroids

### NATIONAL NEAR-EARTH OBJECT PREPAREDNESS STRATEGY

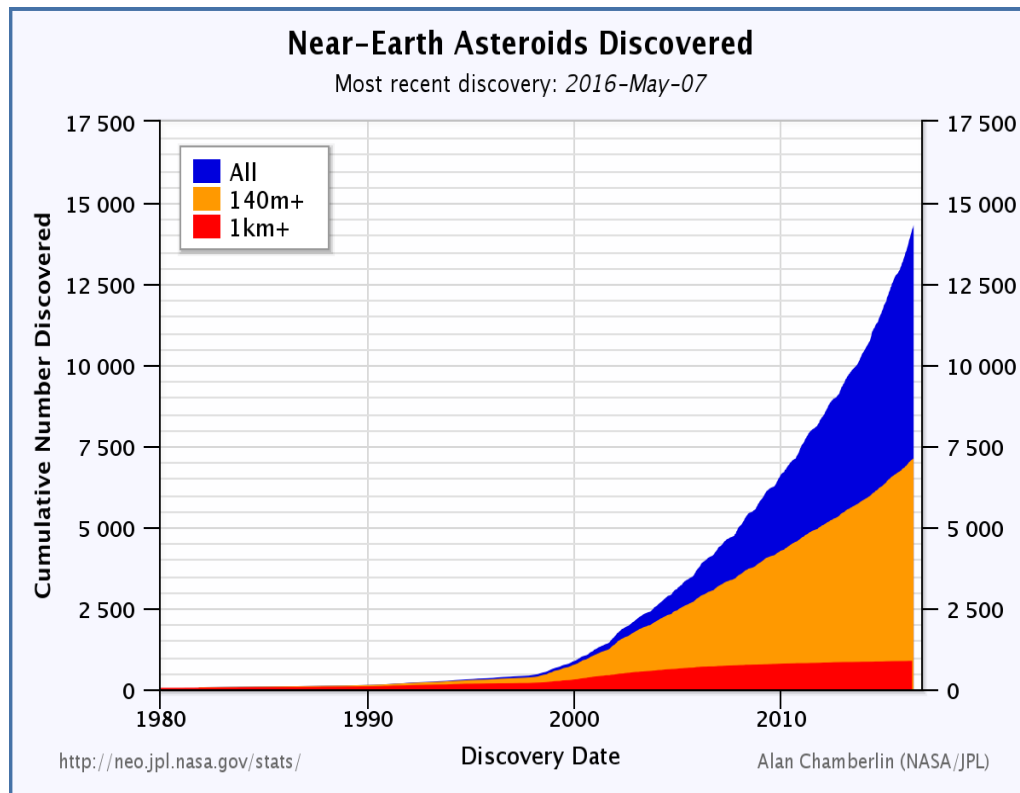
PRODUCT OF THE  
INTERAGENCY WORKING GROUP FOR DETECTING AND  
MITIGATING THE IMPACT OF EARTH-BOUND NEAR-  
EARTH OBJECTS (NEOS) (DAMIEN)  
OF THE NATIONAL SCIENCE AND TECHNOLOGY COUNCIL



DECEMBER 2016

# MILLIONS OF MISSING ASTEROIDS!

## CONNECTING PARTIAL ASTEROID TRACKLETS



However, some observations cannot be matched into an asteroid.

There are currently:

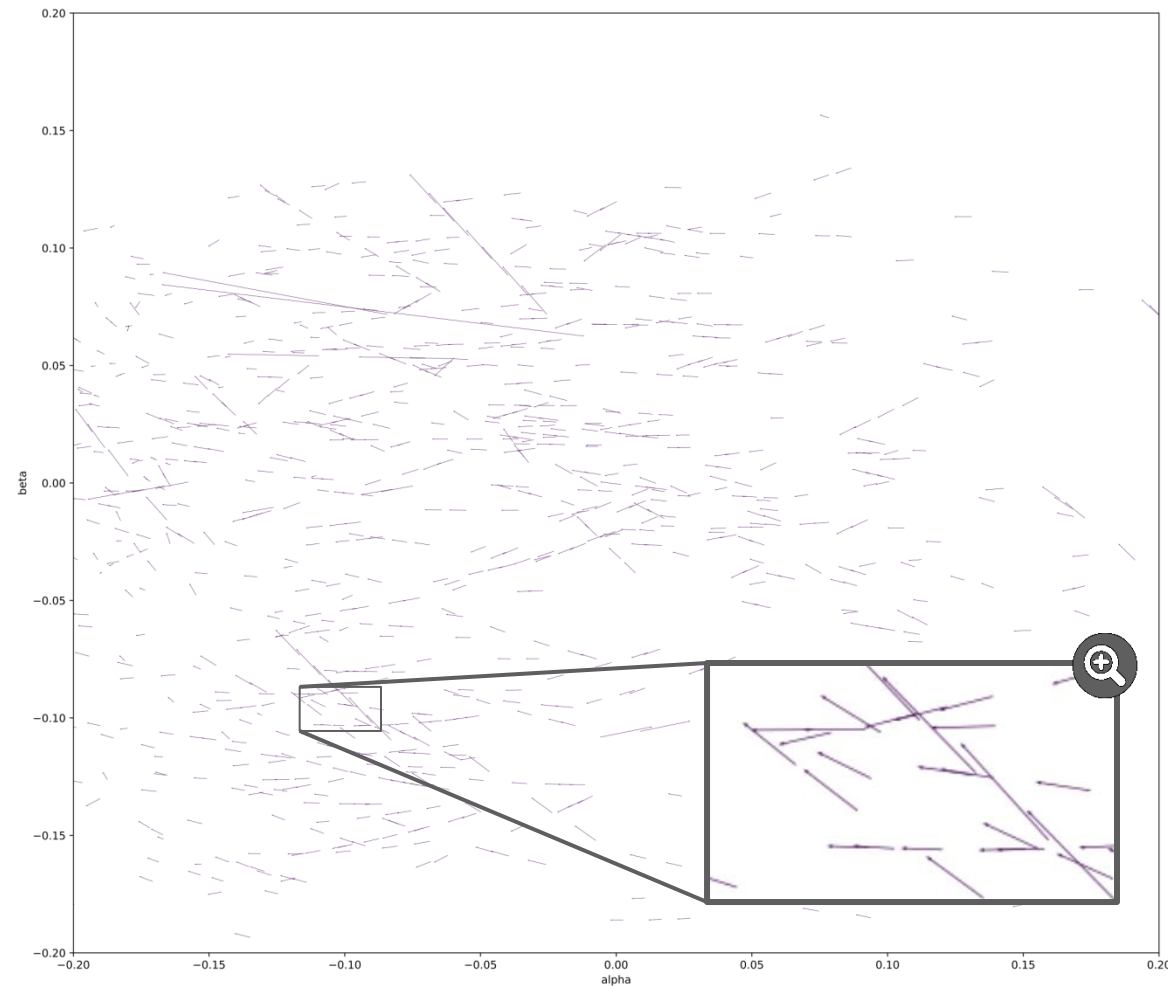
- **14 million** unmatched tracklets,
- **~3 million** total asteroids.

Growing quickly as telescope resolution increases

# A HARD PROBLEM...

- **High asteroid density** makes clustering difficult
- From Earth, asteroids trajectories are **highly non-linear**
- **Missing data** (cannot tell asteroid movement/velocity in the z direction)
- Sparse observations can be **months or years apart**
- **Brute force is impossible** with 14m observations

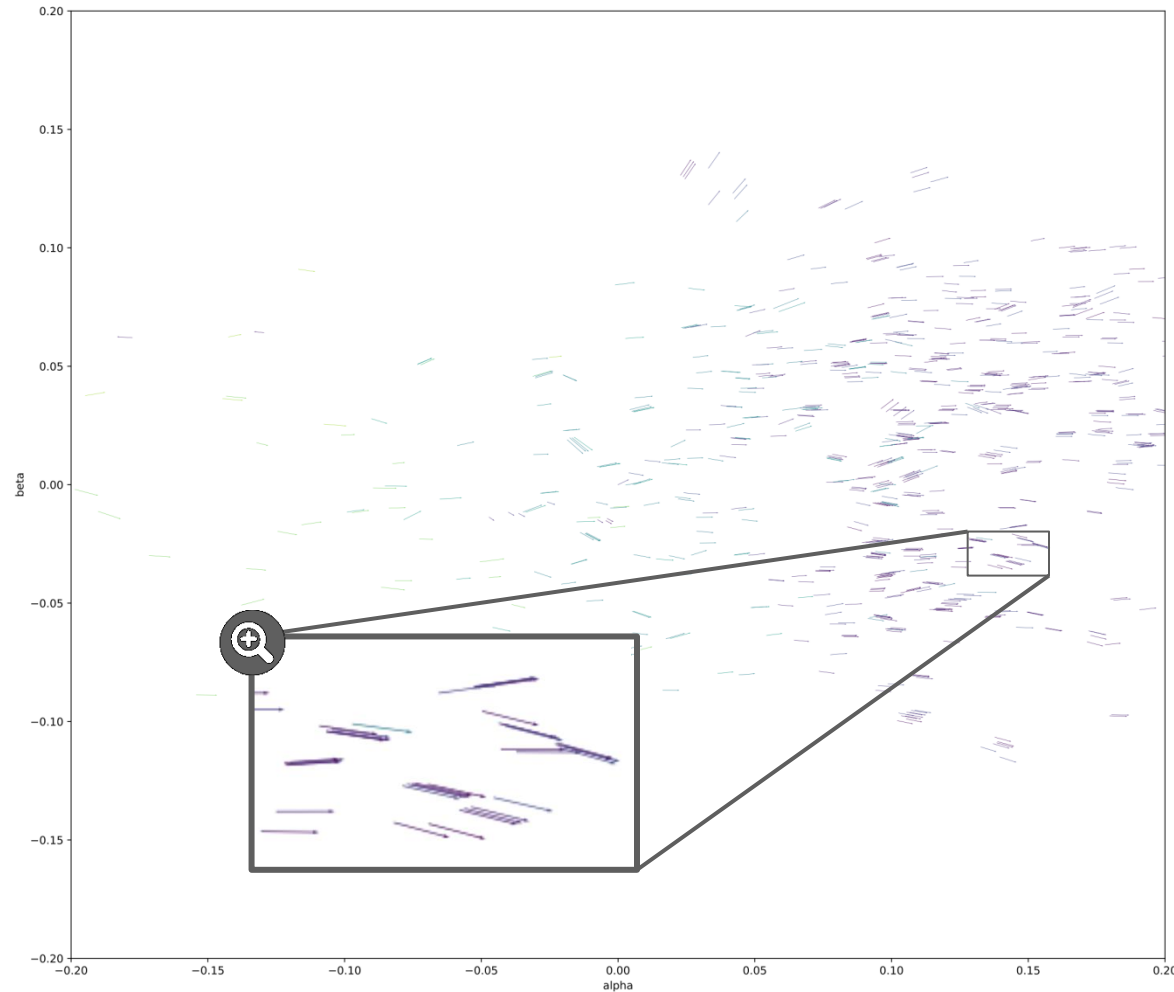
Partial asteroid tracklets (from Earth's perspective)



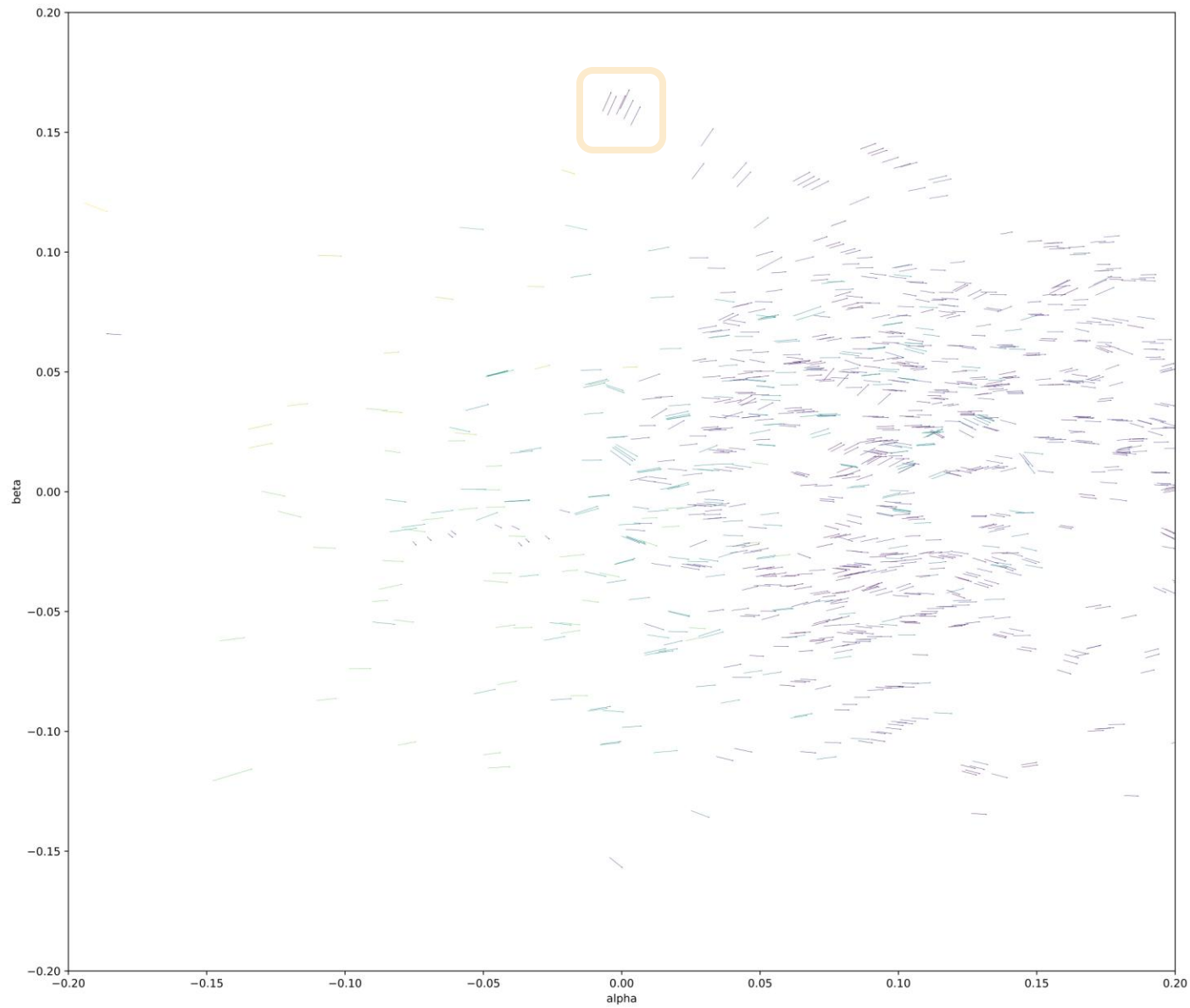
# PROPOSED SOLUTION

- When we apply a **heliocentric transformer**, the trajectories become clear!
- Similar to applying **the kernel trick in 3-dimensional space**
- Can then set a '**focal distance**' by inferring z-distance

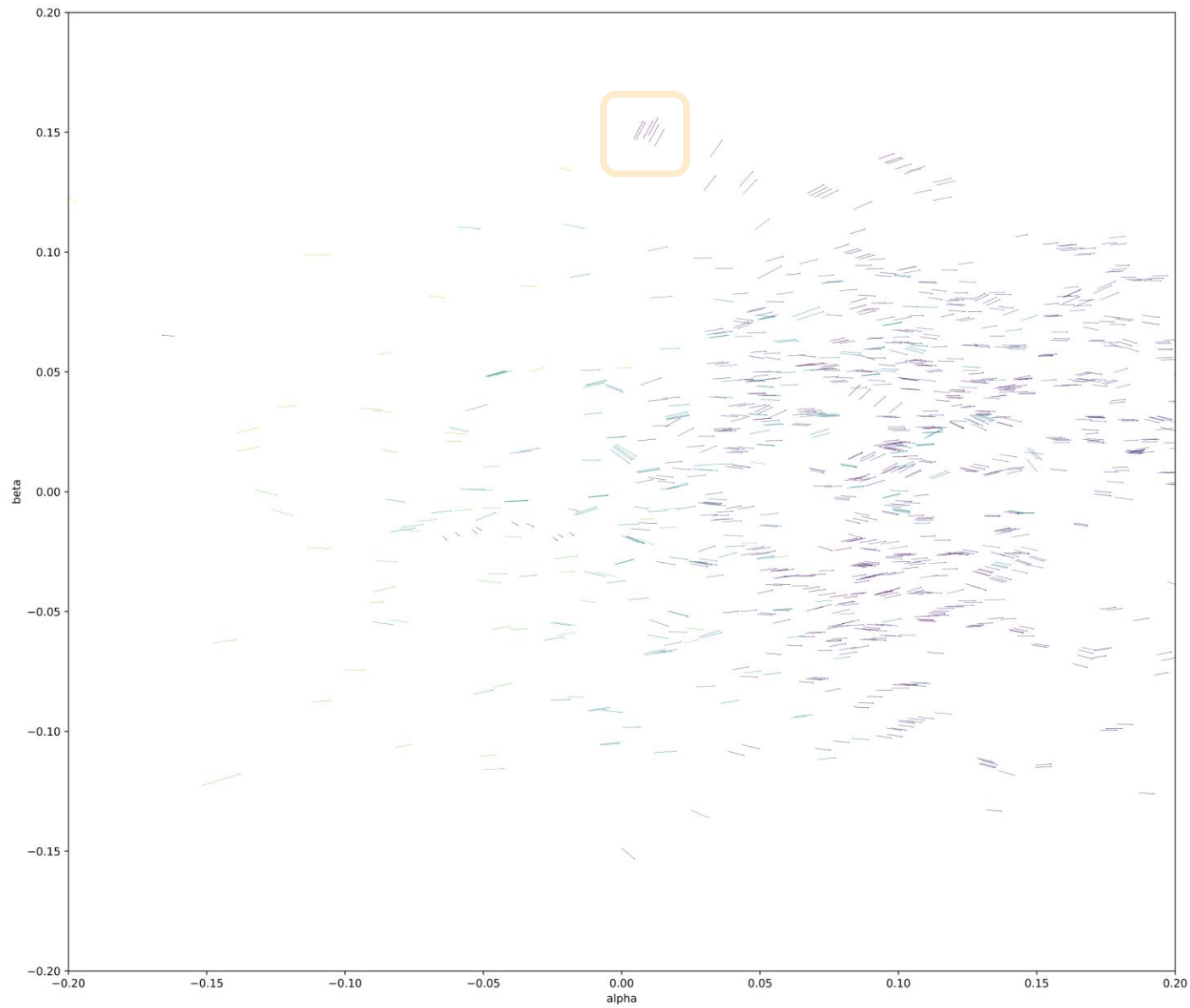
Partial asteroid tracklets (from the Sun's perspective)



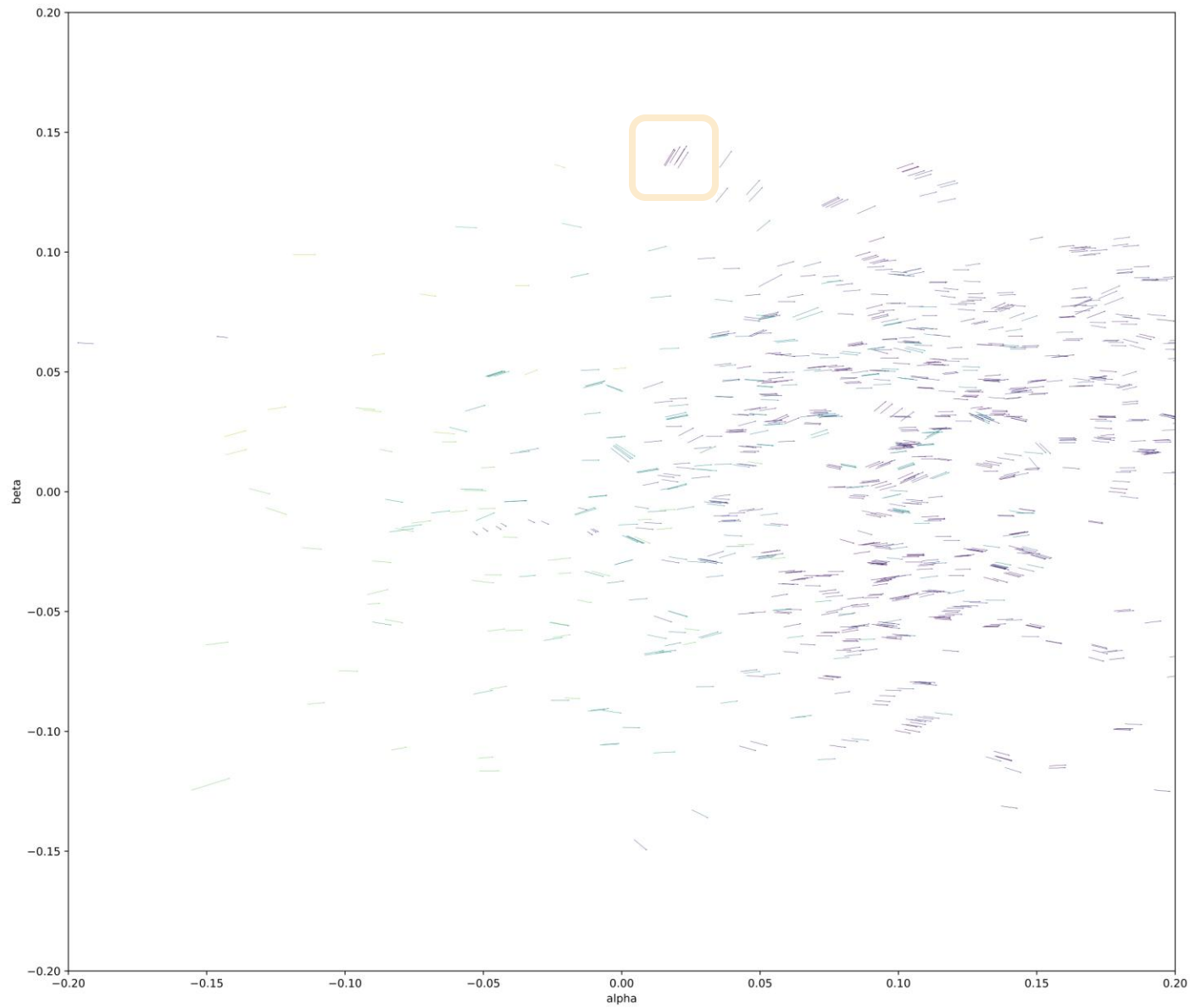
# THE VIEW FROM THE SUN



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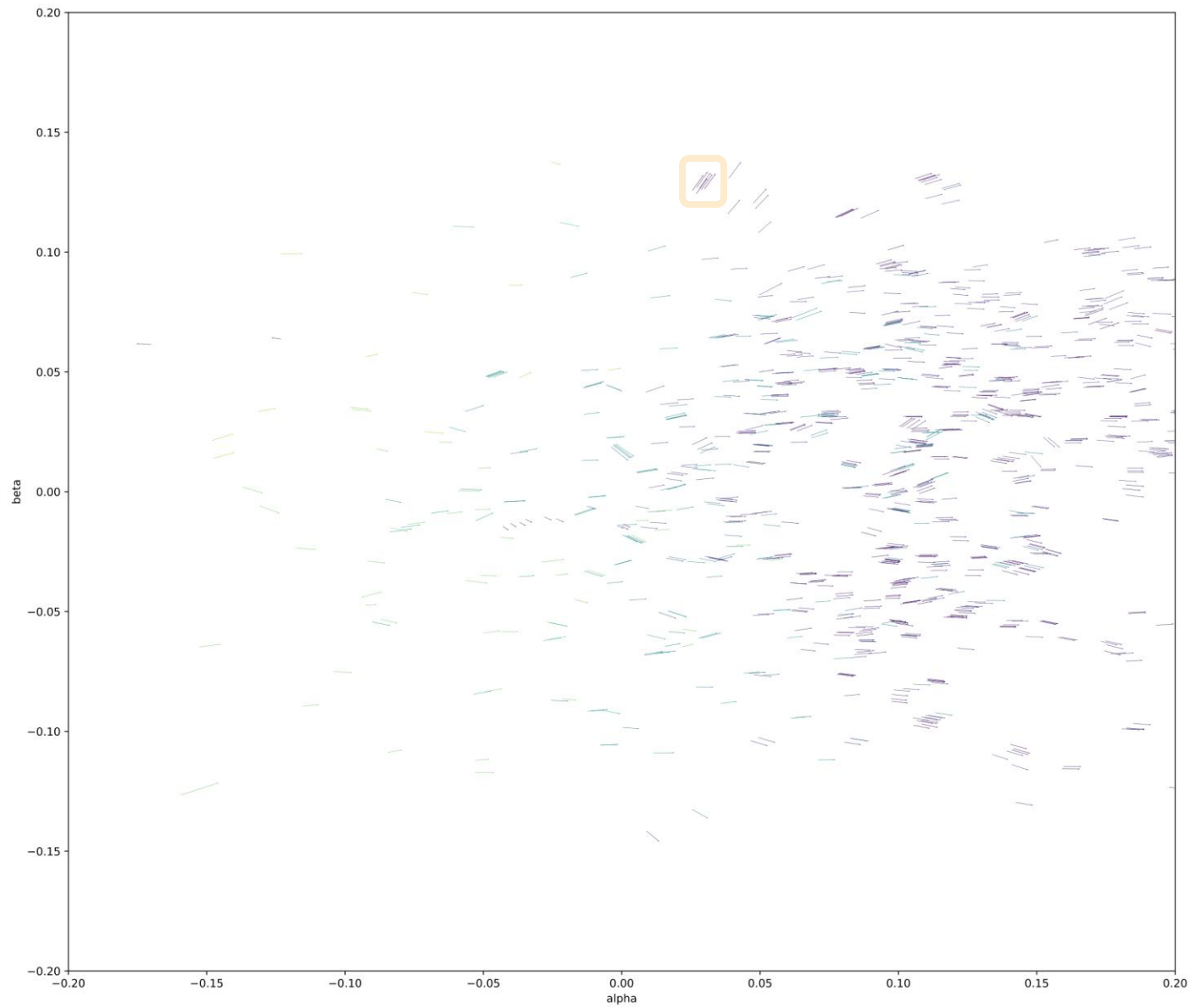


# THE VIEW FROM THE SUN

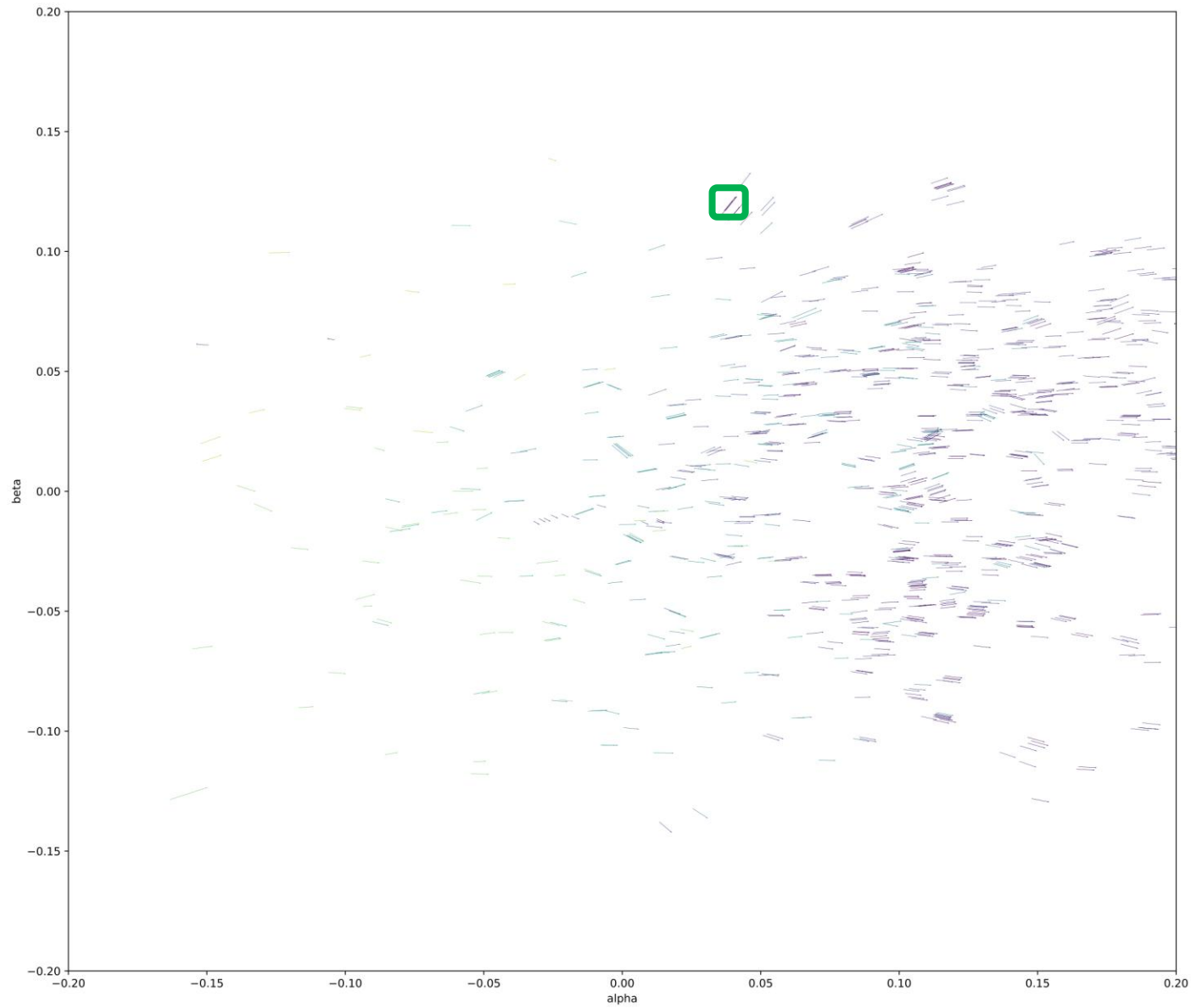




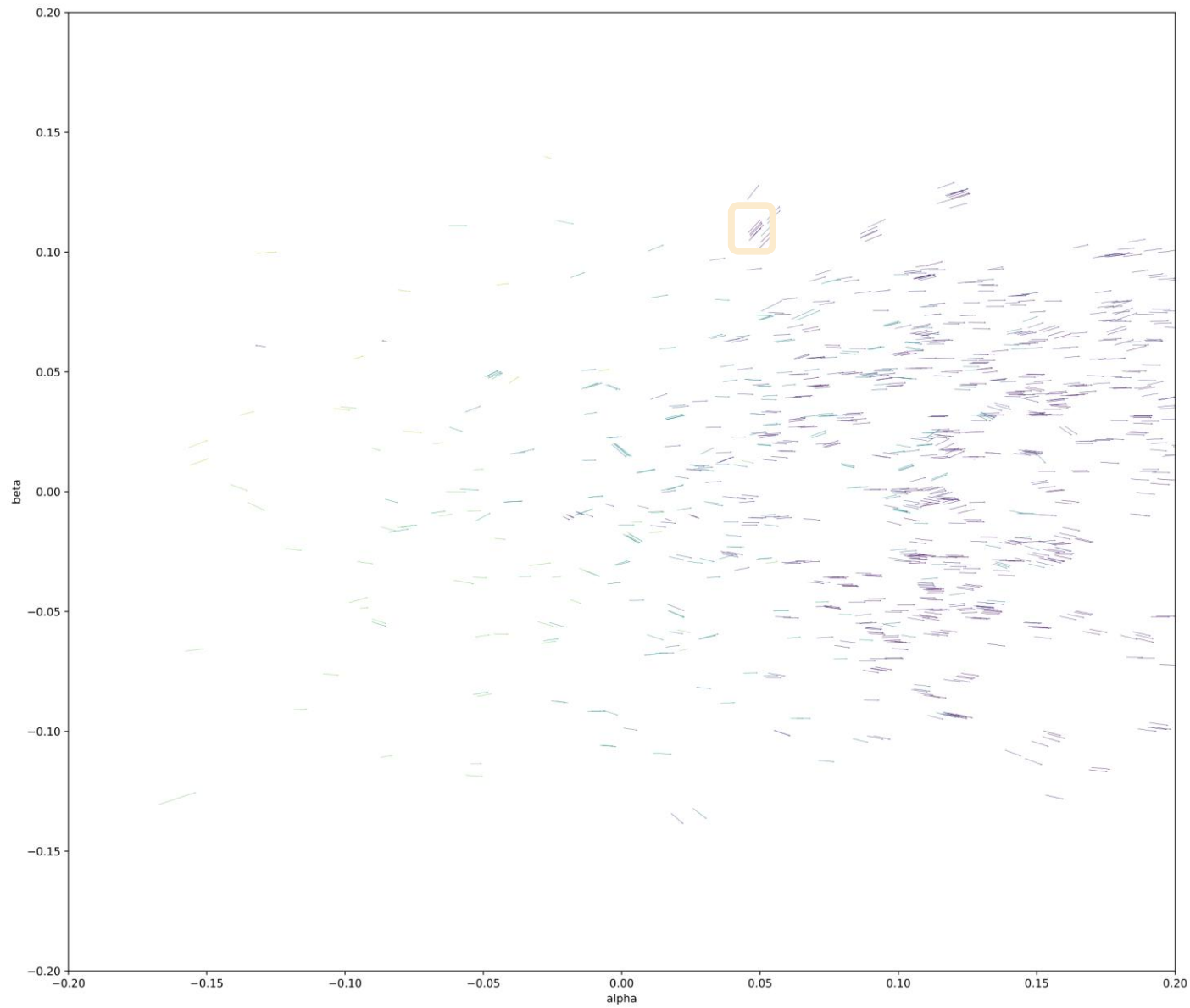
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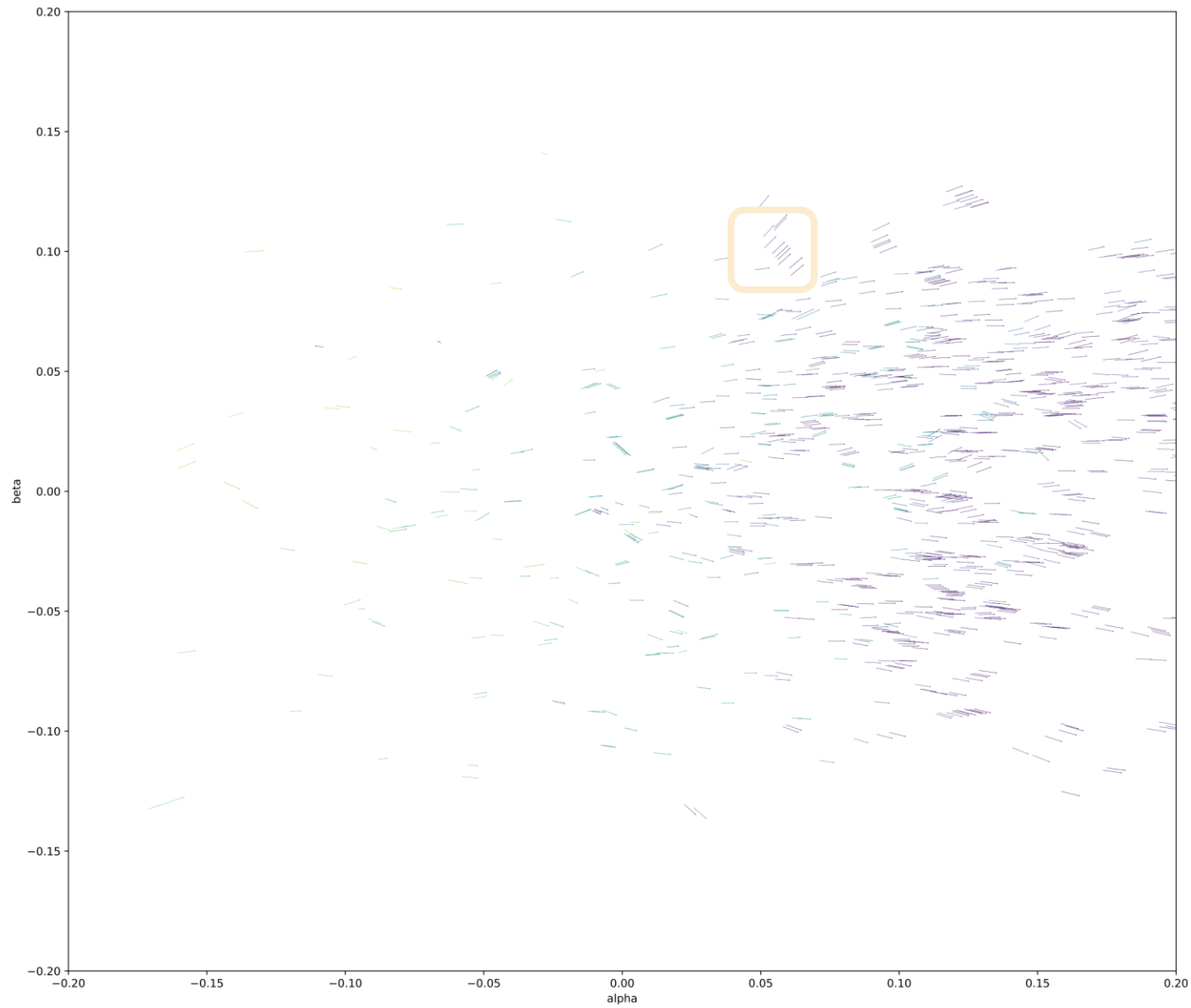
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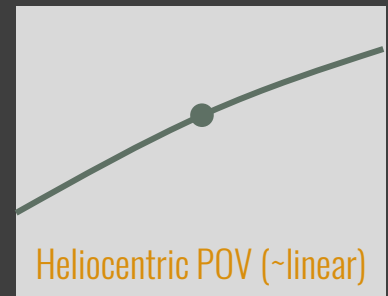
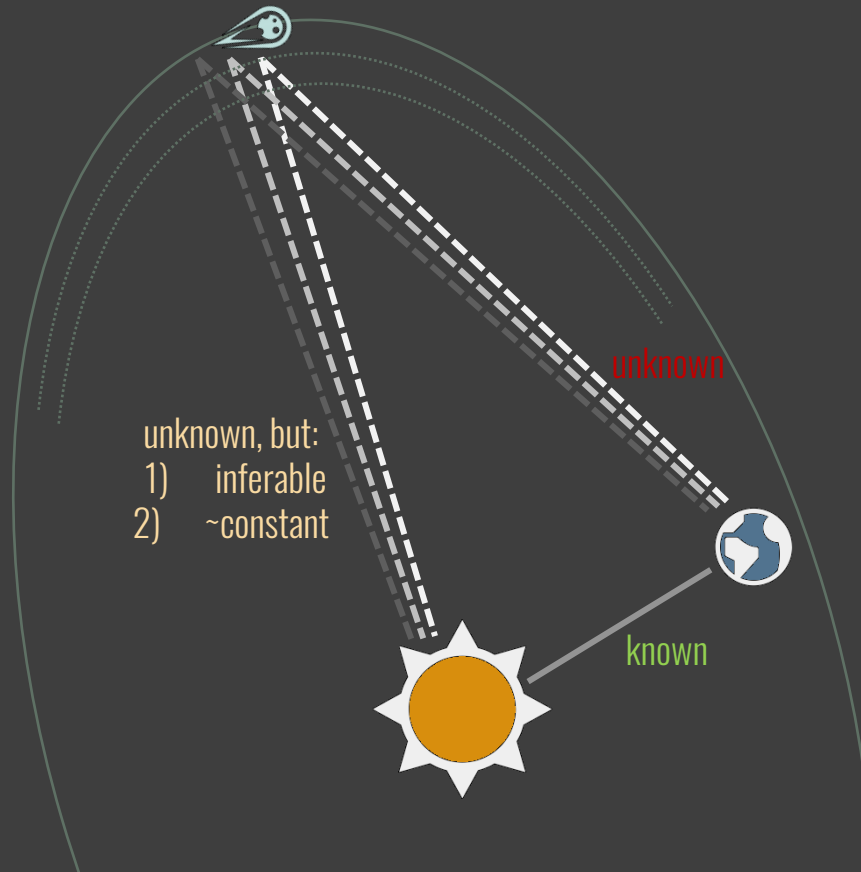
# THE VIEW FROM THE SUN



# CORE INTUITION

## WHY DOES HELIOCENTRICITY WORK?

- Heliocentric transform allows us to infer **a constant distance from the sun**
- Also helps us compare asteroid tracklets **linearly, and in common time**
- Enables **clustering** over small radii



\*not to scale  
(...obviously)

# OUR METHODOLOGY

1. **DIVIDE** SKY INTO !!! PLANES  
AND 300 TIME SLICES

2. **ASSERT** THE (UNKNOWN)  
Z-DISTANCE FROM THE SUN

Running full sky in a  
single cluster is  
computationally  
intractable [ $O(n \log n)$ ]

# OUR METHODOLOGY

1. **DIVIDE** SKY INTO !!! PLANES  
AND 300 TIME SLICES

2. **ASSERT** THE (UNKNOWN)  
Z-DISTANCE FROM THE SUN

3. **ITERATE** OVER Z-VELOCITIES, SOLVE  
OTHER MOTION PARAMS

4. **CLUSTER** BASED ON 6 PARAMS:  
X/Y/Z POSITION, X/Y/Z - VELOCITY

4 of our 6 motion  
parameters are  
known, and 1 is  
relatively constant

Model is linear in  
the parameters

# OUR METHODOLOGY

TUNE CLUSTERING HYPERPARAMETERS OVER KNOWN TRAINING SET (THANKS TO MINOR PLANET CENTER!)

TRAIN CLUSTER RADIUS/WEIGHTING

1. **DIVIDE** SKY INTO !!! PLANES AND 300 TIME SLICES
2. **ASSERT** THE (UNKNOWN) Z-DISTANCE FROM THE SUN
3. **ITERATE** OVER Z-VELOCITIES, SOLVE OTHER X/Y MOTION PARAMS
4. **CLUSTER** BASED ON 6 PARAMS: X/Y/Z POSITION, X/Y/Z - VELOCITY

We tune two hyper-parameters:

- 1) OPTIMAL **CLUSTER RADIUS**
- 2) **WEIGHTING** OF VELOCITY VS. POSITION



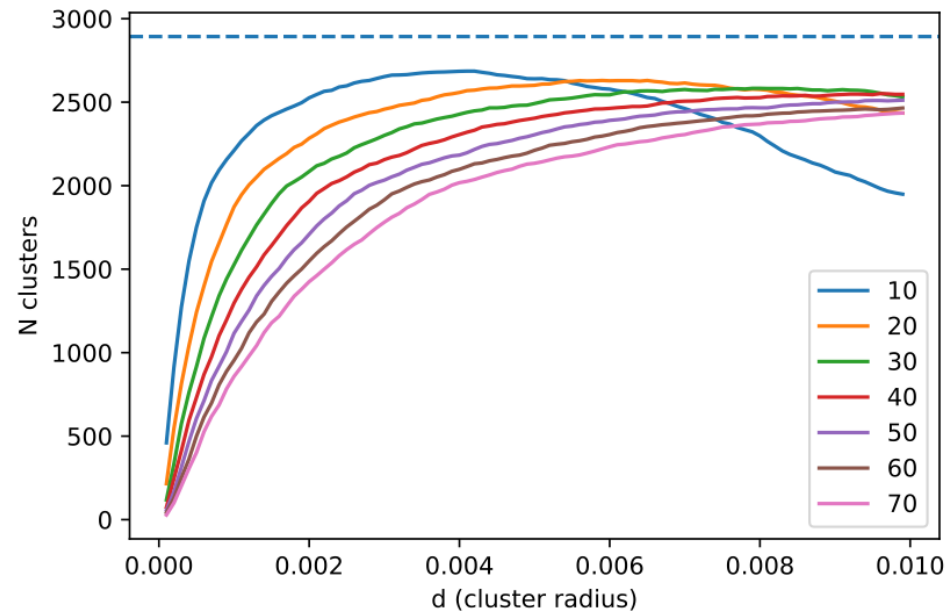
# TUNING PERFORMANCE

OPTIMAL CLUSTER  
RADIUS: 0.005-0.010AU

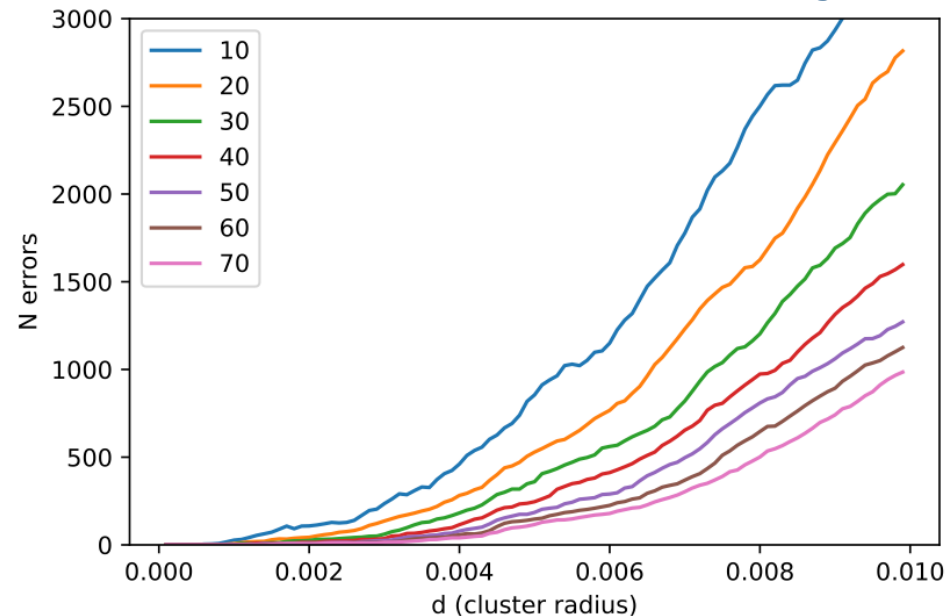
Selected KD-tree  
clustering for optimal  
speed (!!!)

Also had good results  
with agglomerative  
clustering

Total clusters detected vs. KD-tree cluster radius (training set)



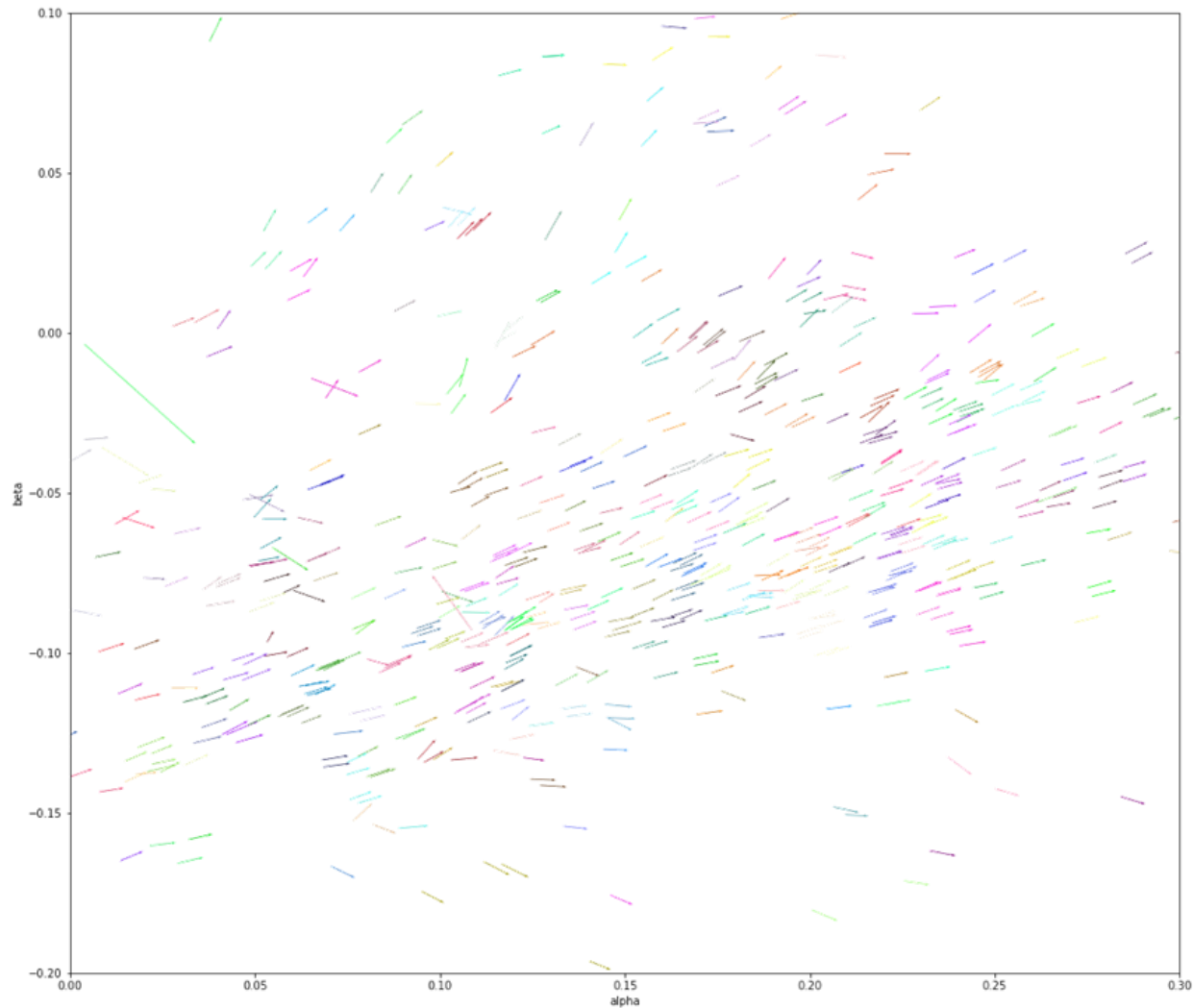
Error rate vs. KD-tree cluster radius (training set)



# CLUSTERING RESULTS

90% OF ASTEROIDS DETECTED  
WITH ZERO ERROR!

Identified Asteroids (common colors = a single asteroid)



!!! COPY HERE?

# CONCLUSIONS

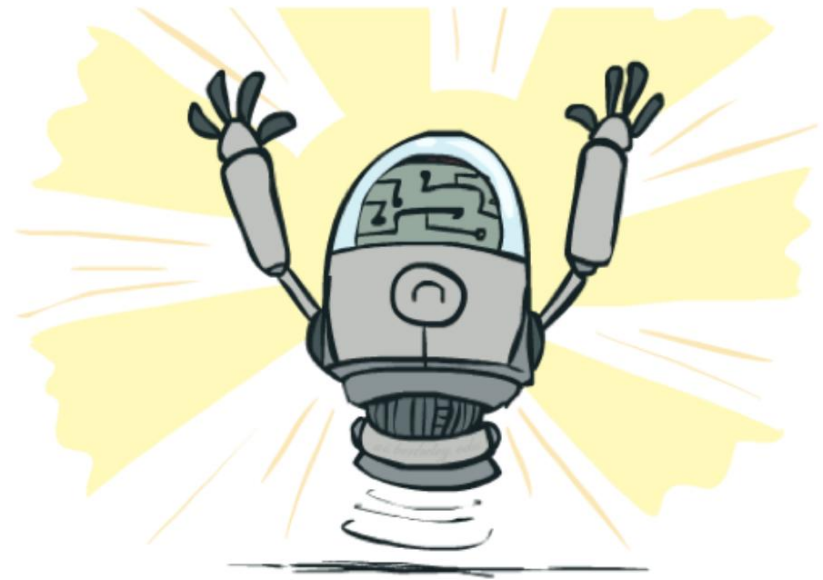
**Conclusion:** Successful tracklet matching using the heliocentric transform and KD-Trees

Also able to do so in just  $O(n \log n)$  time,  
a scalable solution!!

**Limitations:** possible improvement in a  
more accurate clustering method

**Next Steps:** Run the algorithm over all 14m  
partial observations!

**Thanks To:** The Minor Planet Center for training data, Scott and Brian for project support!

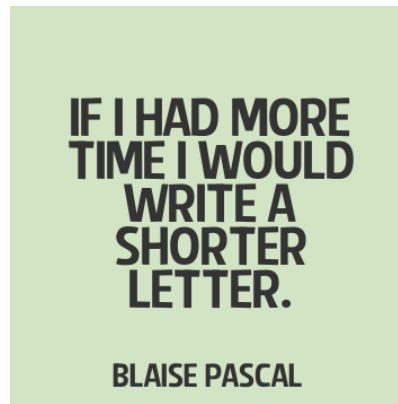




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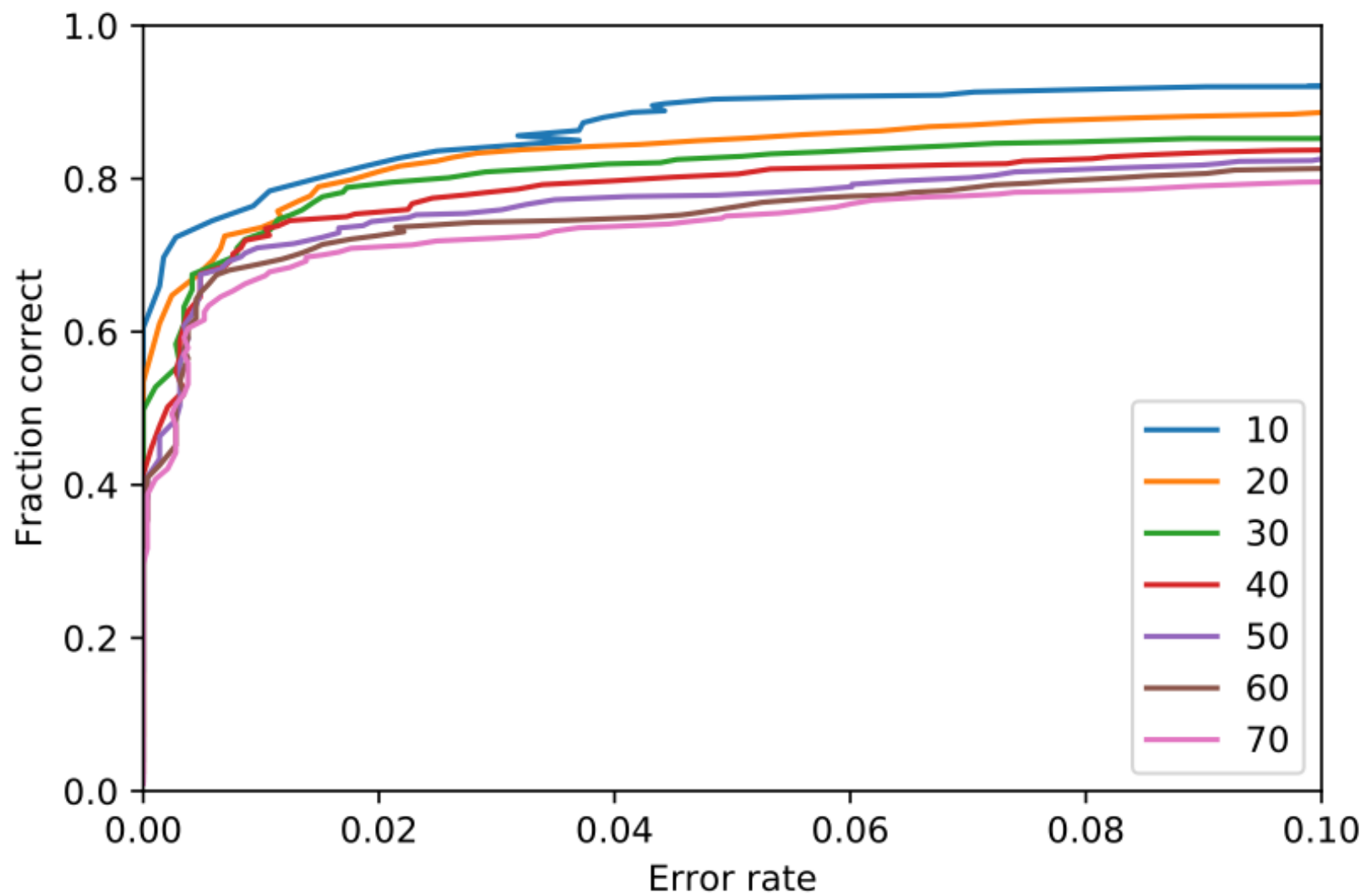
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# APPENDIX/SUPPORTING SLIDES



[QuotePixel.com](http://QuotePixel.com)

Training AUC



## Agglomerative Clustering Dendrogram (Truncated)

