



100,000 ASTEROIDS
DOWN THE BACK OF THE COUCH




1 COIN 1 PLAY

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CS182

ARTIFICIAL INTELLIGENCE



PREPARED BY
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WITH MATT PAYNE
MINOR PLANET CENTER

1 COIN 1 PLAY

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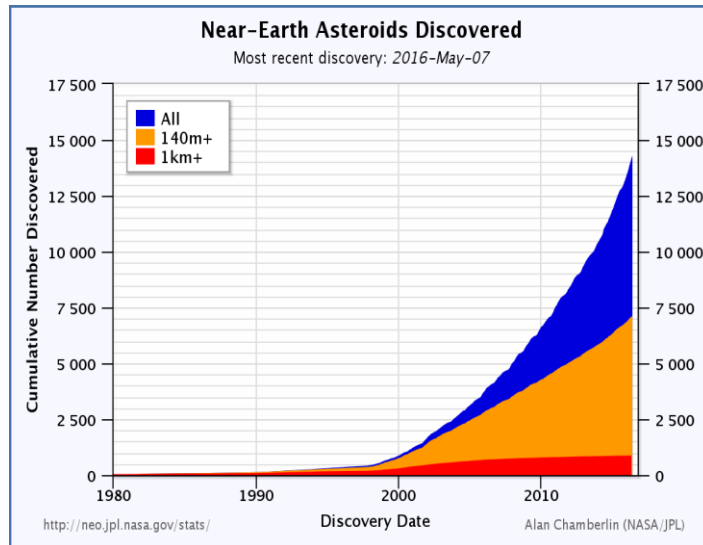
ARTIFICIAL INTELLIGENCE

30 NOVEMBER 2017

MISSING ASTEROIDS!

CONNECTING ASTEROID TRACKLETS

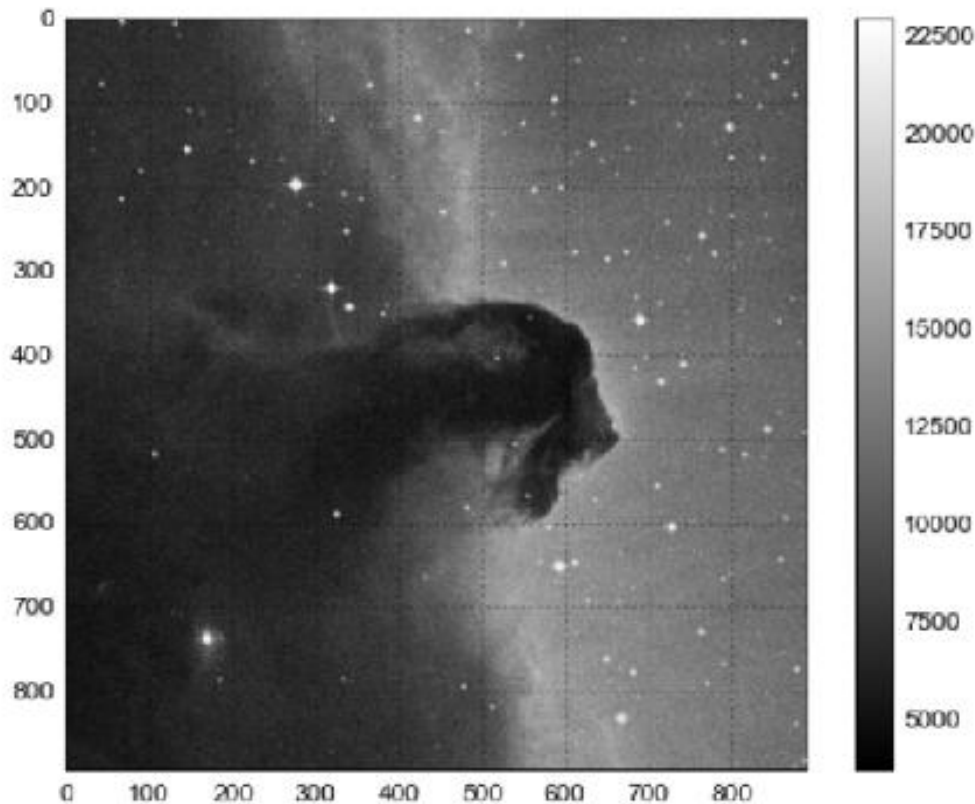
Mandate from Congress:
Discover >90% of potentially
hazardous asteroids with
diameters >140 meters



Currently, we have 170m
asteroid observations

MISSING ASTEROIDS!

CONNECTING ASTEROID TRACKLETS



Asteroids 'tracklets' are found by matching 3+ detections in digital exposures

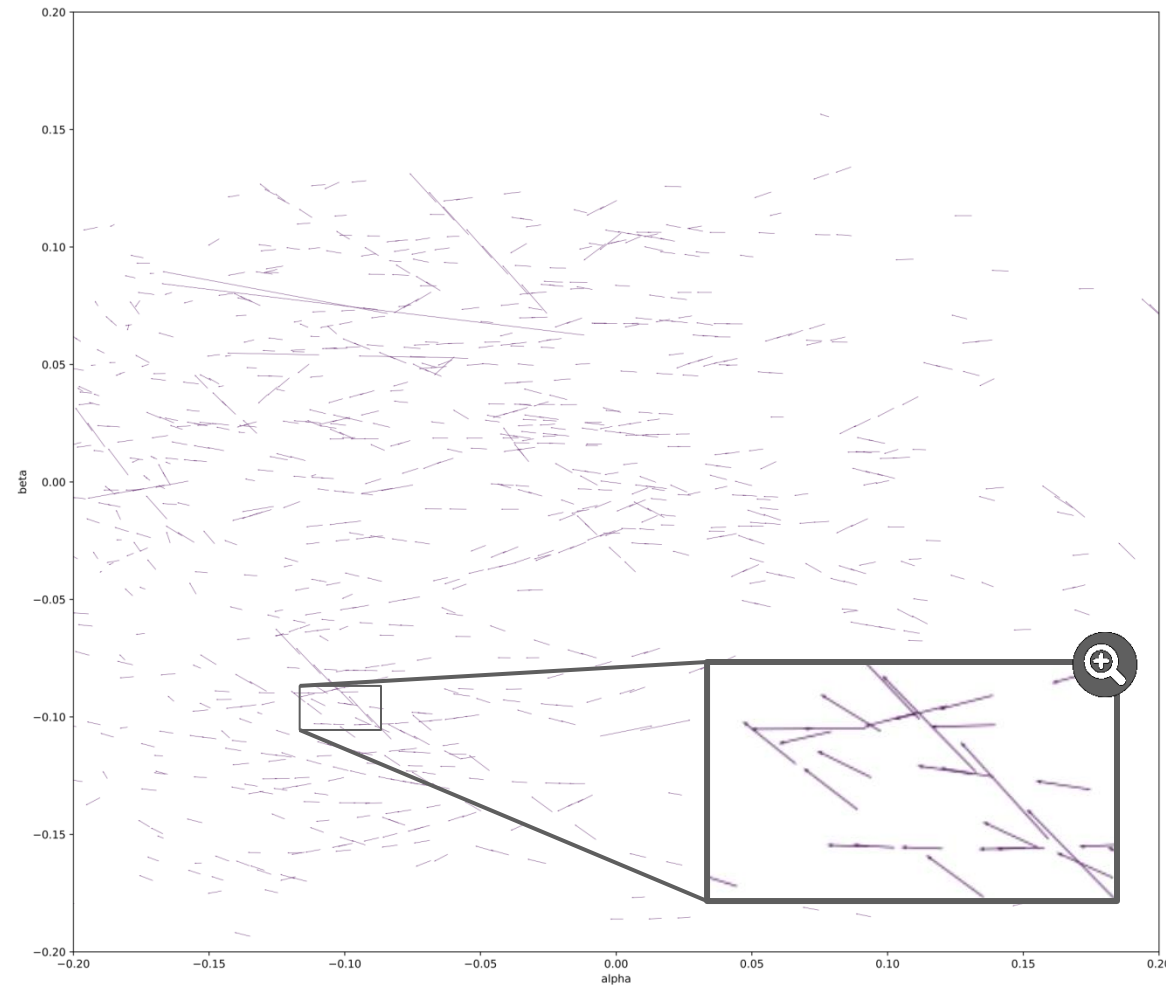
90% can be identified immediately. But there are **14 million** unmatched tracklets

Growing quickly as telescope aperture increases

A HARD PROBLEM...

- Observed from Earth, asteroid trajectories are **highly nonlinear**
- This, with the **high density of asteroids** makes naïve linking difficult
- **Missing data** (cannot tell asteroid pos'n/velocity in the radial direction)
- Sparse observations can be separated by **weeks, months, or years**
- **Brute force is impractical** with 14m observations (Current soln = $O(n^3)$!)

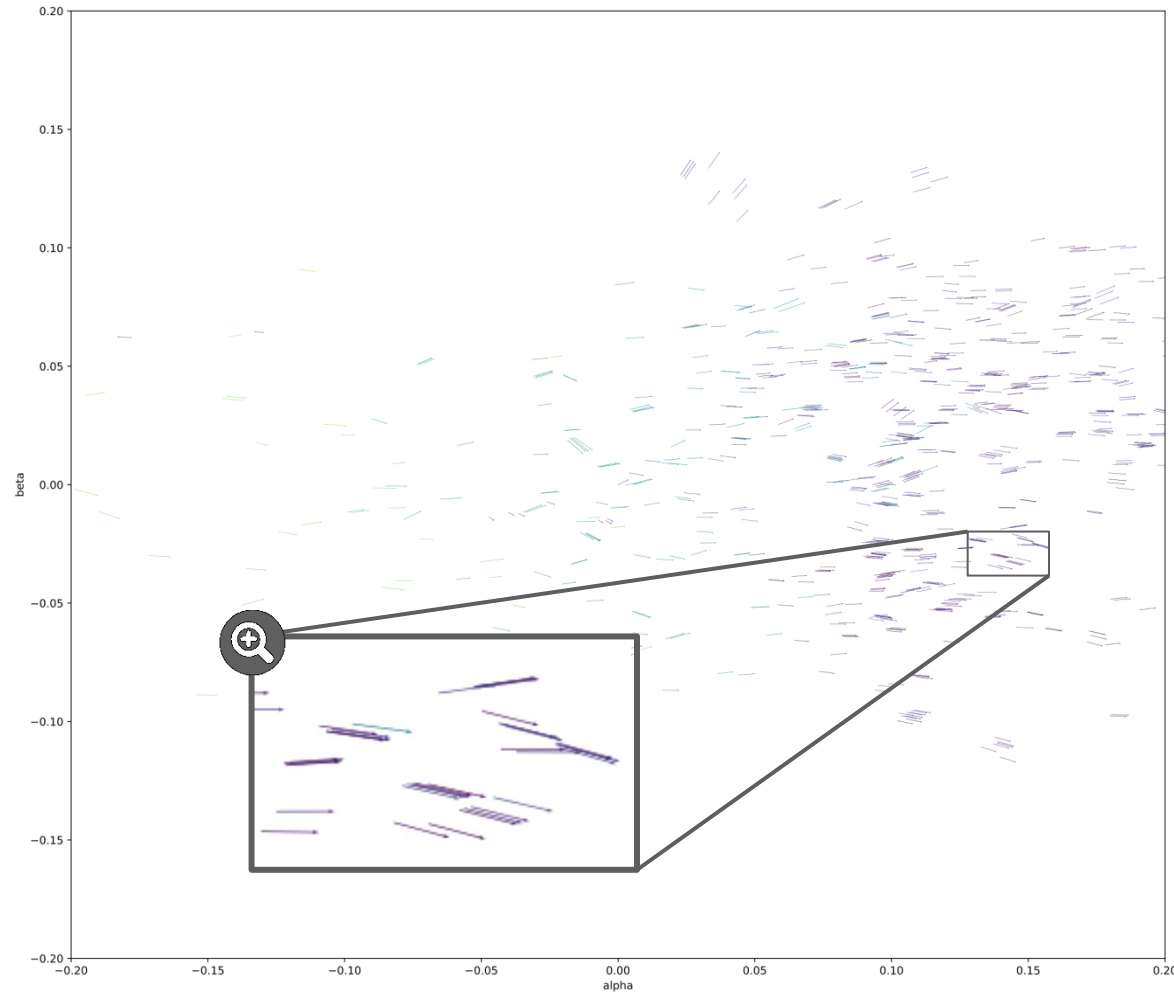
Asteroid tracklets (from Earth's perspective)



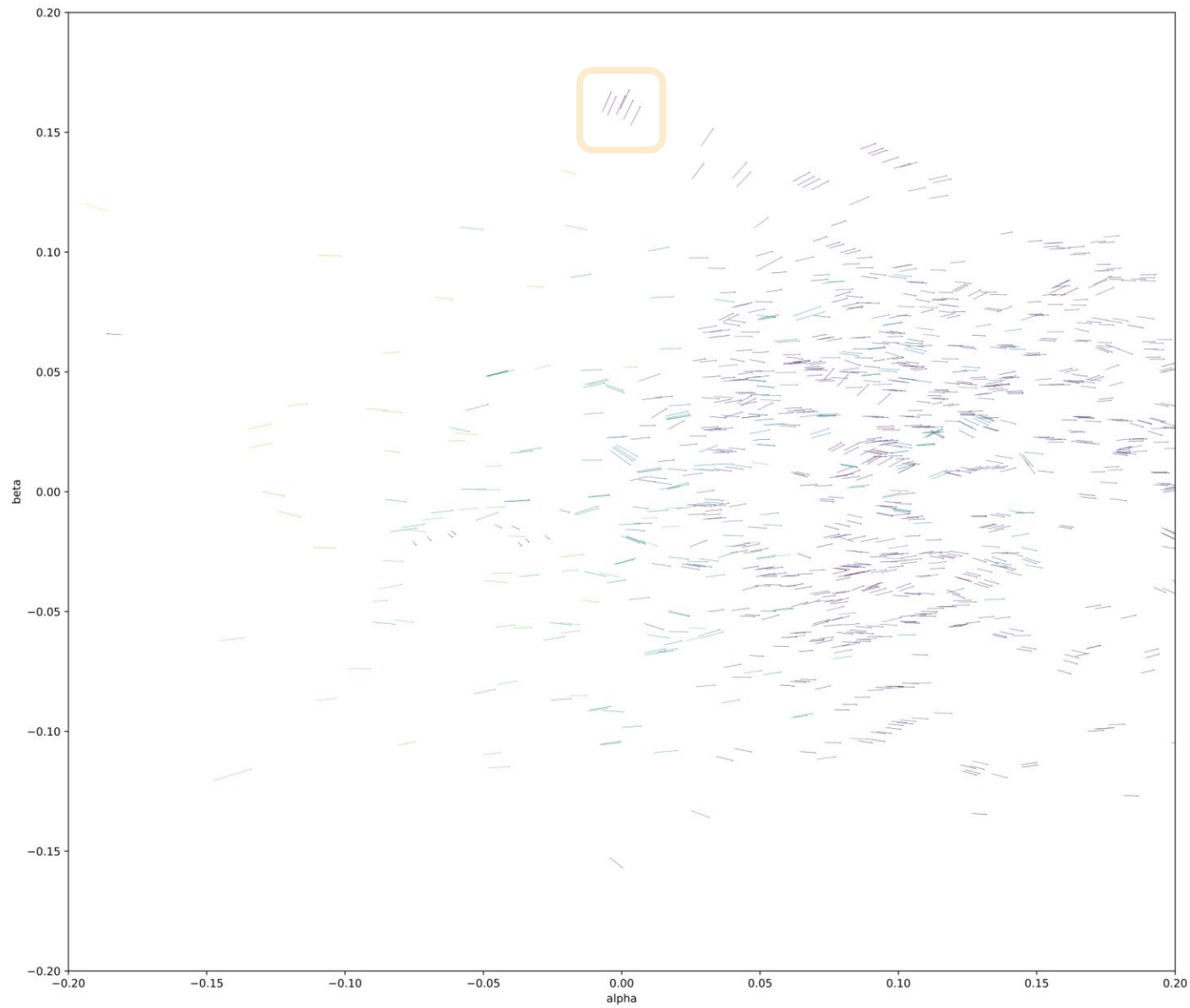
PROPOSED SOLUTION

- When we apply a **heliocentric transformation**, the trajectories become clear!
- Similar to applying **the kernel trick from 2d to 3d space**
- Can then set a '**focal distance**' by scanning radial distances/velocities

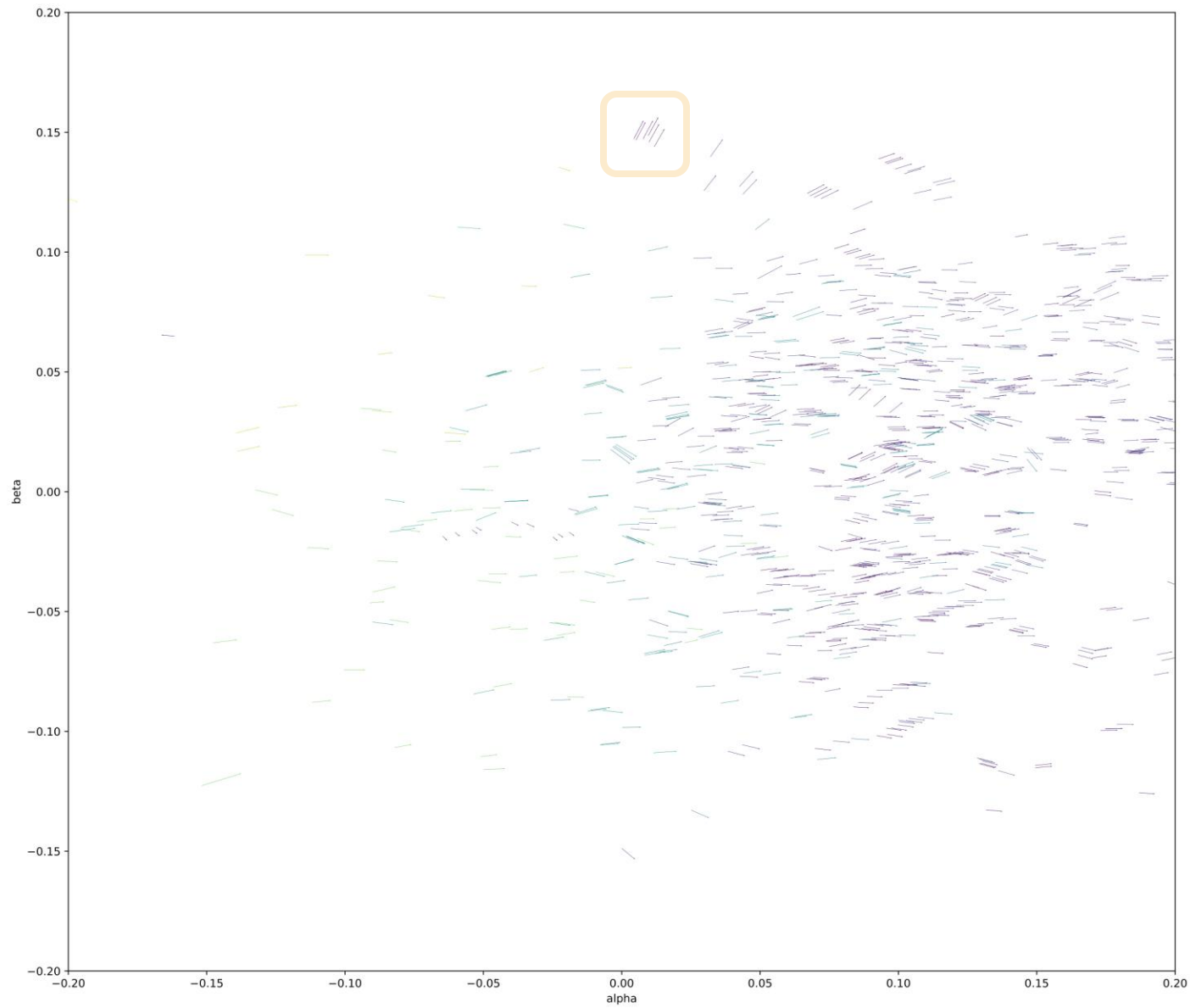
Asteroid tracklets (from the Sun's perspective)



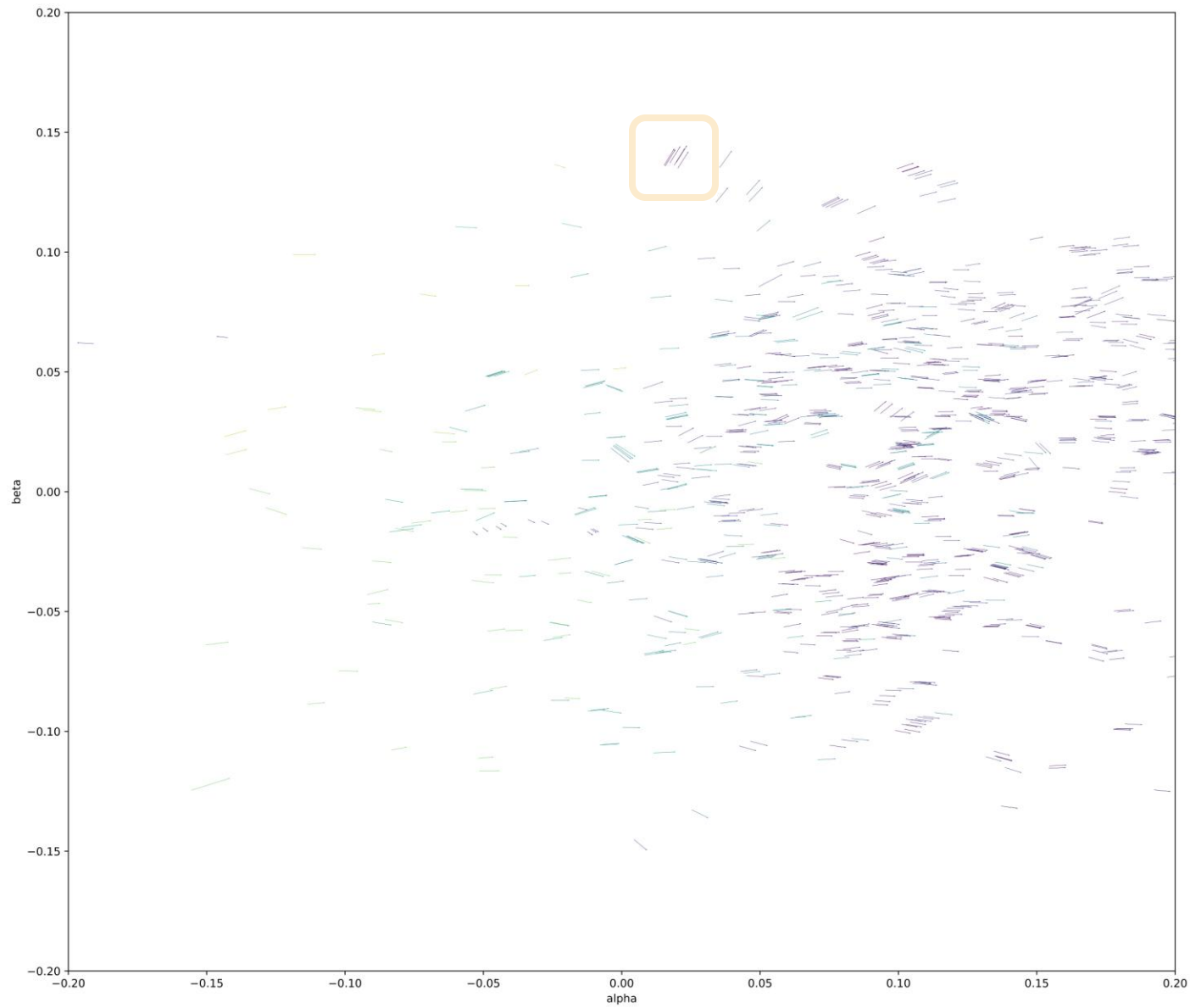
THE VIEW FROM THE SUN



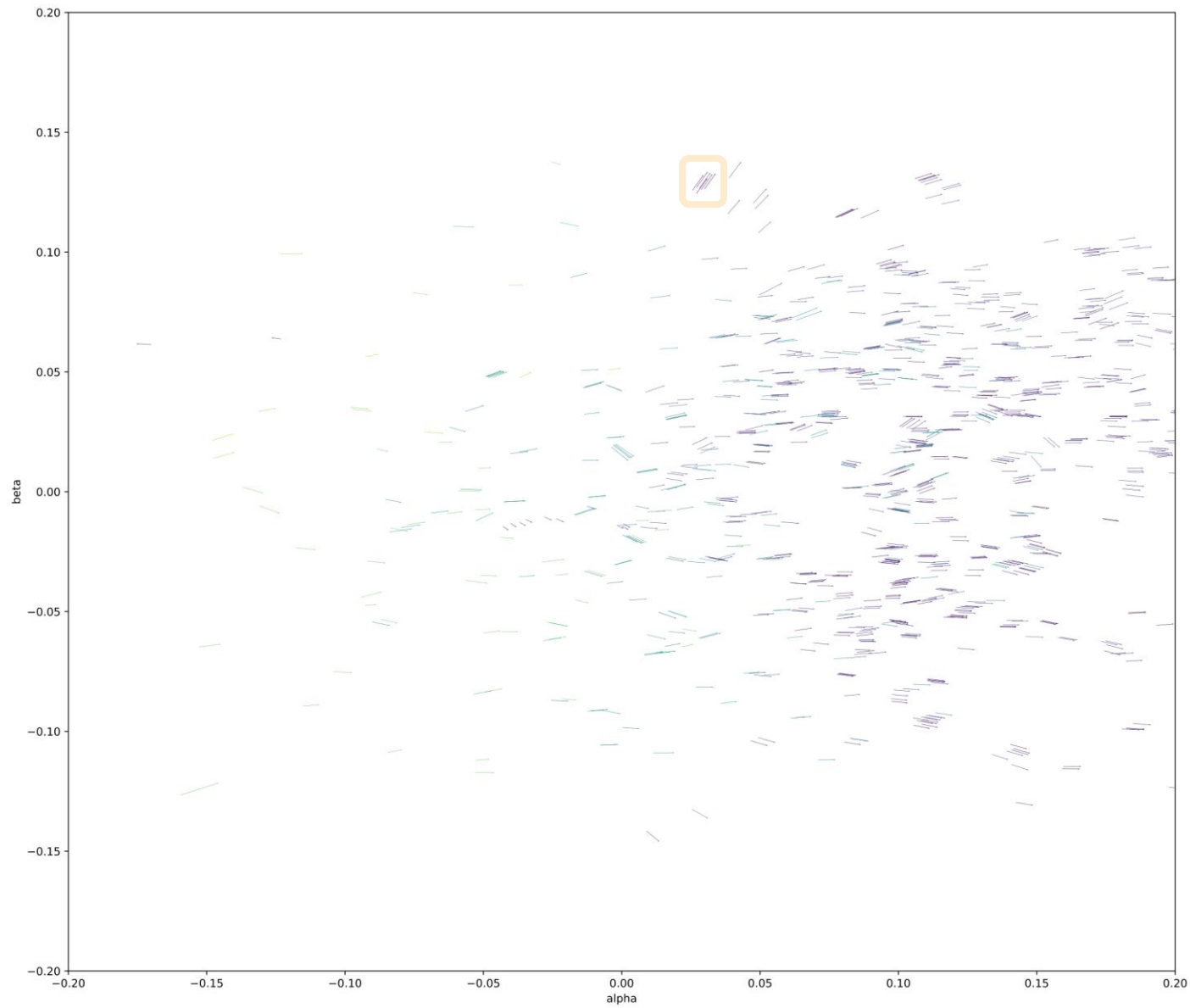
THE VIEW FROM THE SUN



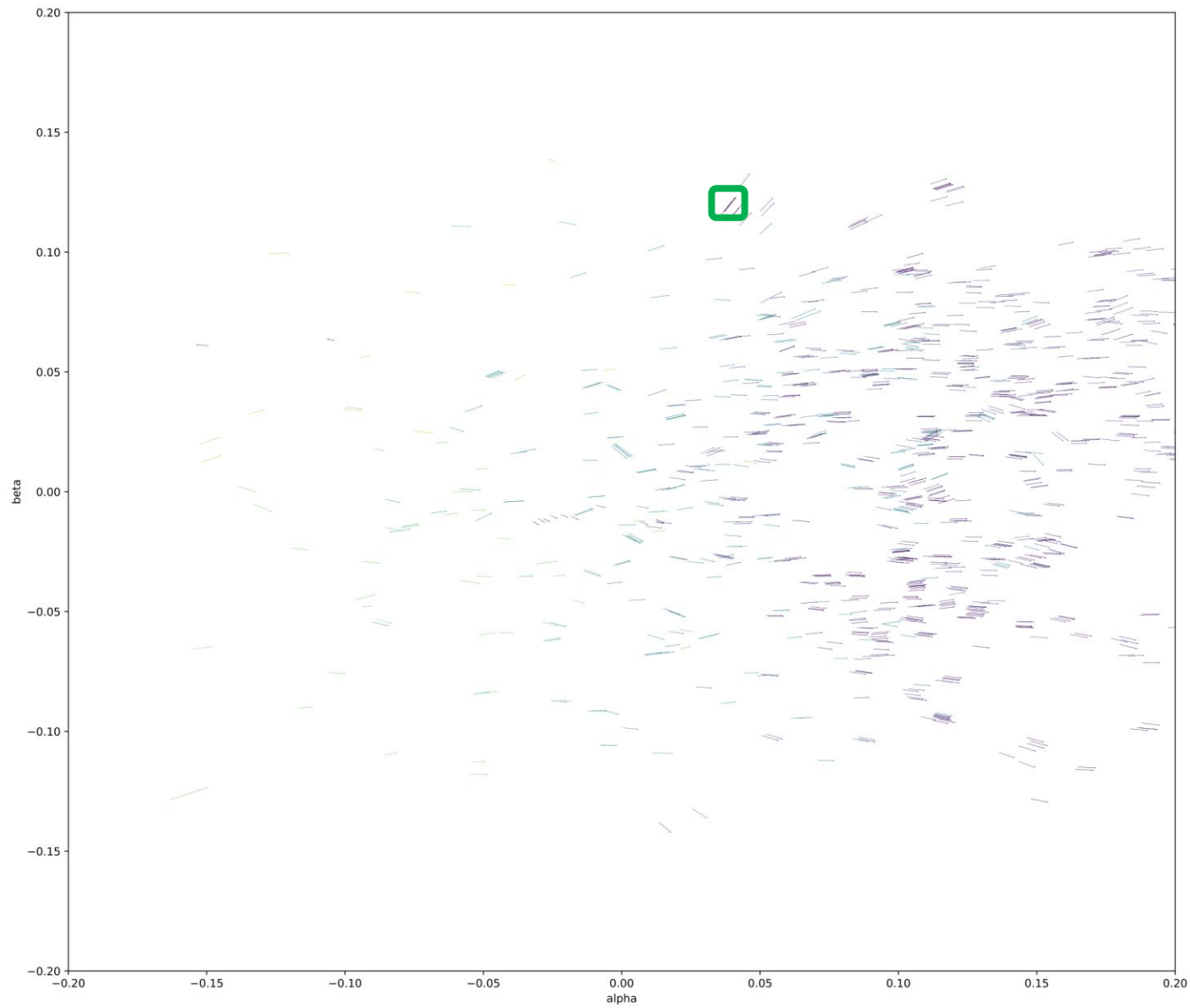
THE VIEW FROM THE SUN



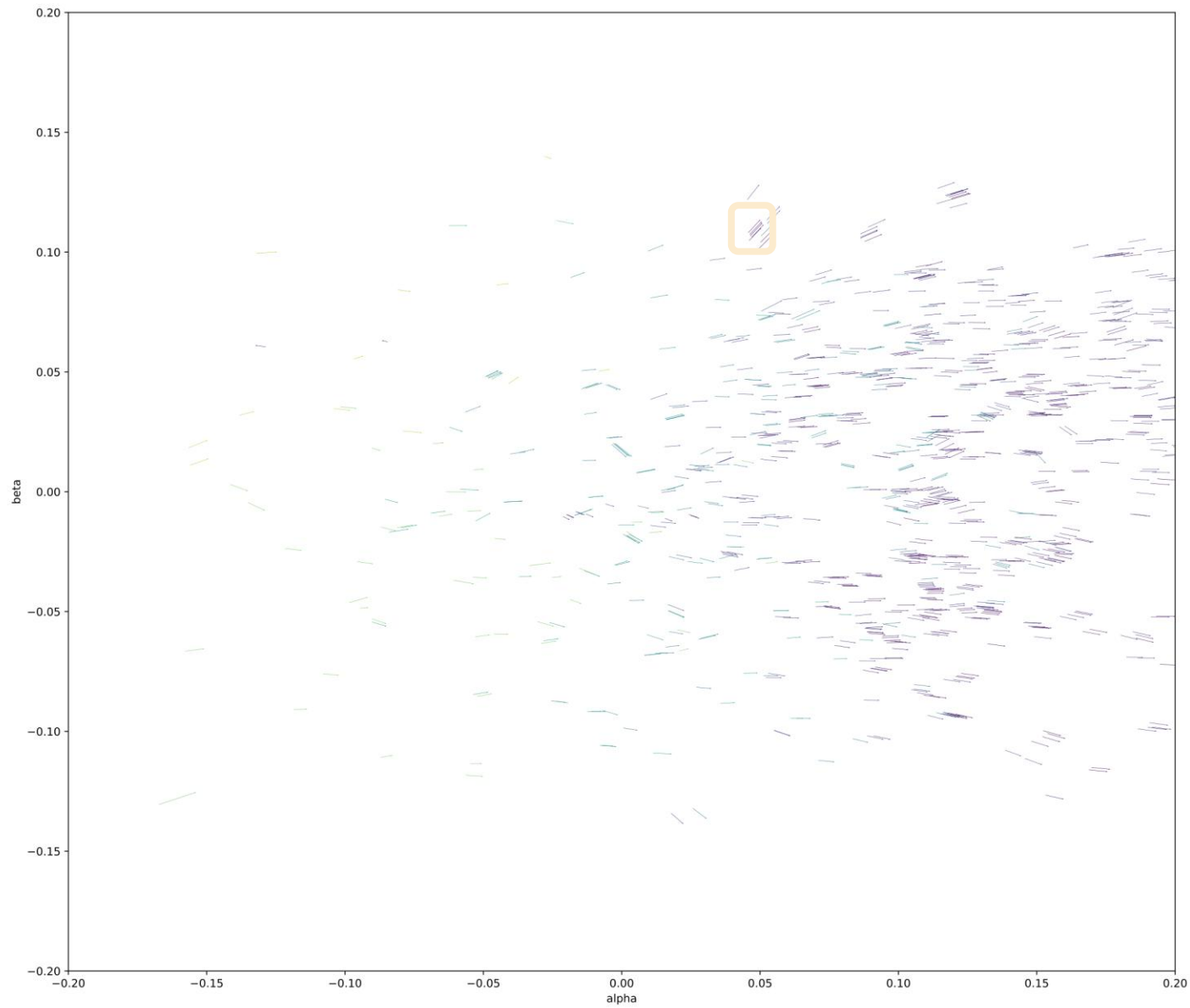
THE VIEW FROM THE SUN



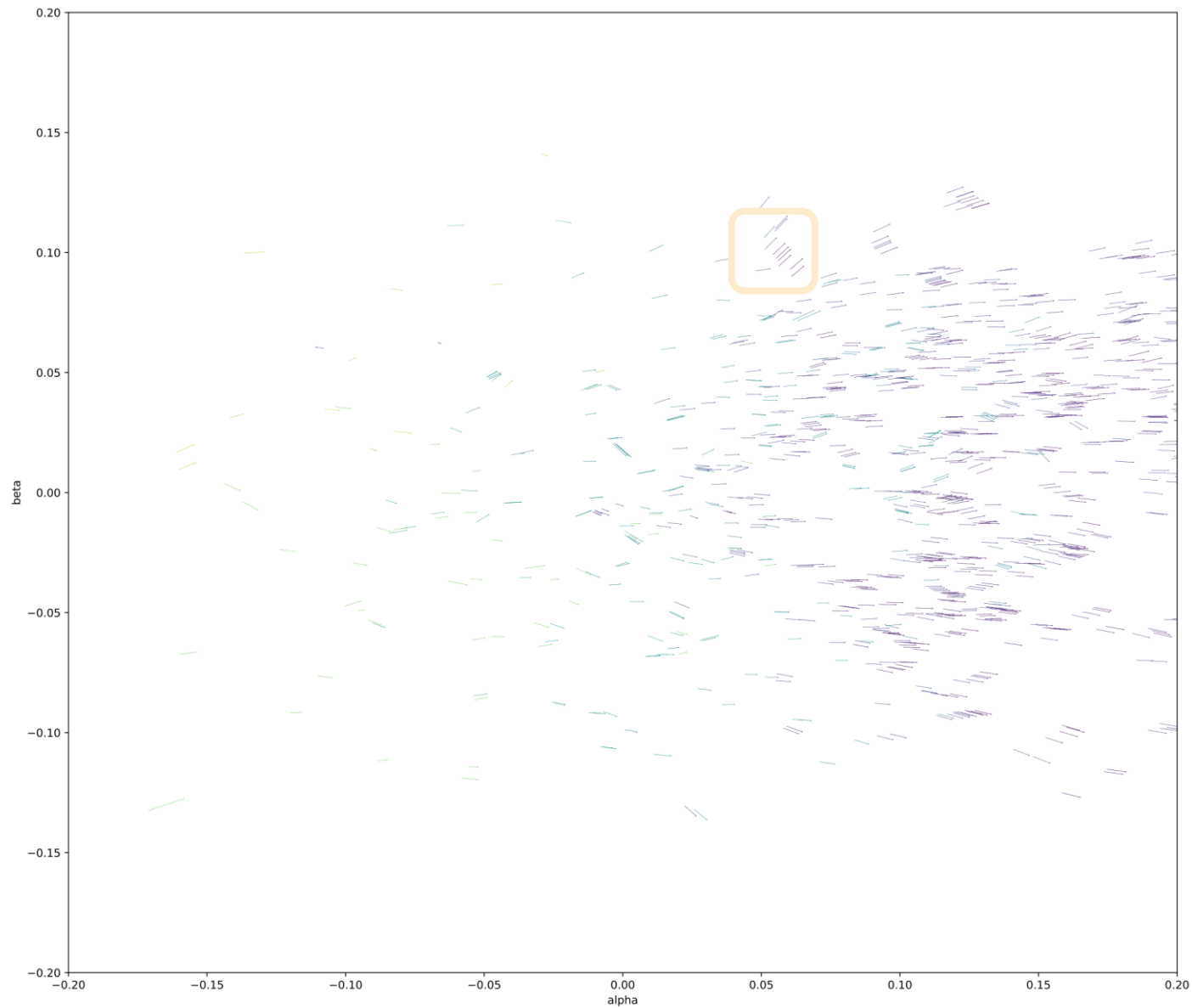
THE VIEW FROM THE SUN



THE VIEW FROM THE SUN



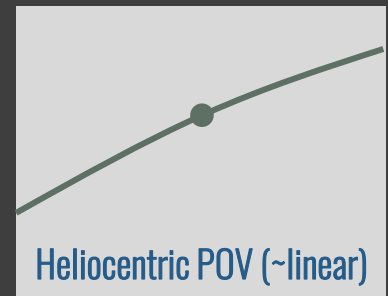
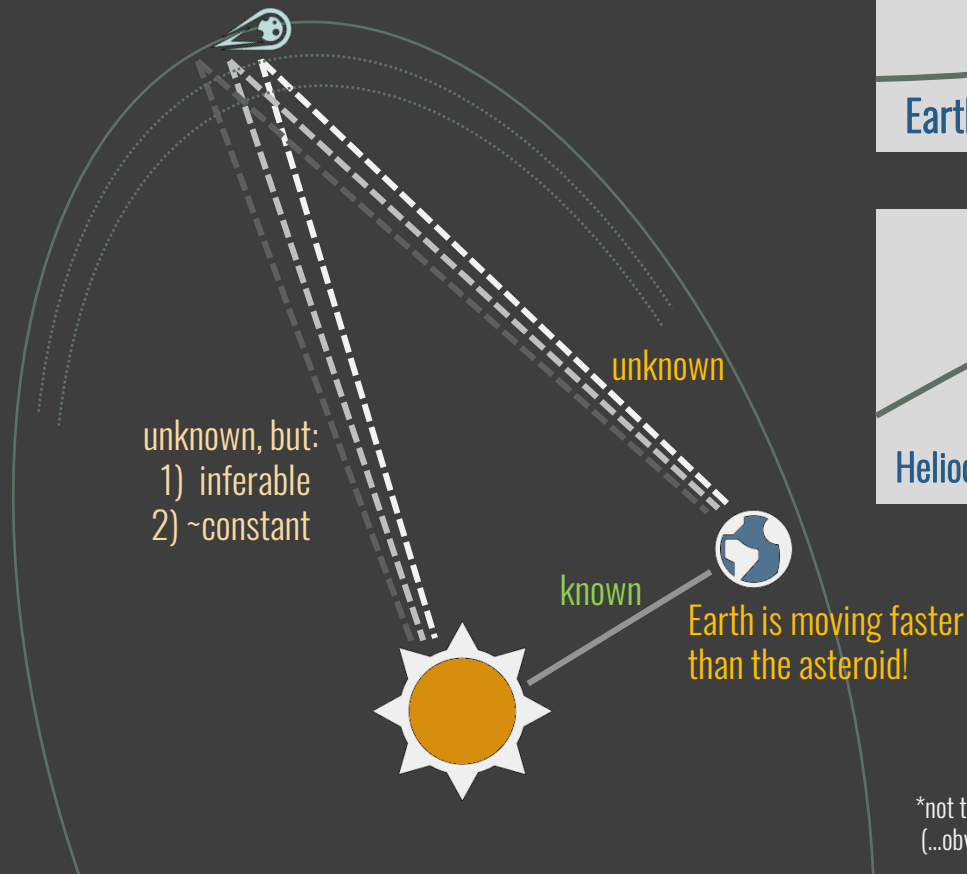
THE VIEW FROM THE SUN



CORE INTUITION

WHY DOES HELIOCENTRIC LINKING WORK?

- Heliocentric transformation allows us to infer a **near-constant distance from the sun** (we have a strong prior)
- Also helps us compare asteroid tracklets in a **linear space**, at a **common time**
- Enables **clustering** to identify observations as one object



*not to scale
(...obviously)

OUR METHODOLOGY

1. **DIVIDE** SKY INTO 300 MONTHLY
TIME SLICES, 800 SKY REGIONS

2. **ASSERT** THE (UNKNOWN)
RADIAL DISTANCE FROM THE SUN

Dividing into sky regions
allows for a more
precise clustering

OUR METHODOLOGY

1. **DIVIDE** SKY INTO 300 MONTHLY TIME SLICES, 800 SKY REGIONS
2. **ASSERT** THE (UNKNOWN) RADIAL DISTANCE FROM THE SUN
3. **ITERATE** OVER RADIAL VELOCITIES, FIT FOR OTHER MOTION PARAMS
4. **CLUSTER** BASED ON RESULTING PARAMS: X/Y/Z POSITION, VELOCITY

4 of our 6 motion parameters are known, and 1 is relatively constant

Model is linear in the parameters (least squares fit)

OUR METHODOLOGY

TUNE CLUSTERING HYPERPARAMETERS OVER KNOWN TRAINING SET (THANKS TO MATT PAYNE, MINOR PLANET CENTER!)

TRAIN CLUSTER RADIUS/WEIGHTING

1. **DIVIDE** SKY INTO 300 MONTHLY TIME SLICES, 800 SKY REGIONS
2. **ASSERT** THE (UNKNOWN) RADIAL DISTANCE FROM THE SUN
3. **ITERATE** OVER RADIAL VELOCITIES, FIT FOR OTHER MOTION PARAMS
4. **CLUSTER** BASED ON RESULTING PARAMS: X/Y/Z POSITION, VELOCITY

We tune two hyper-parameters:

- 1) OPTIMAL **CLUSTER RADIUS**
- 2) **WEIGHTING** OF VELOCITY VS. POSITION

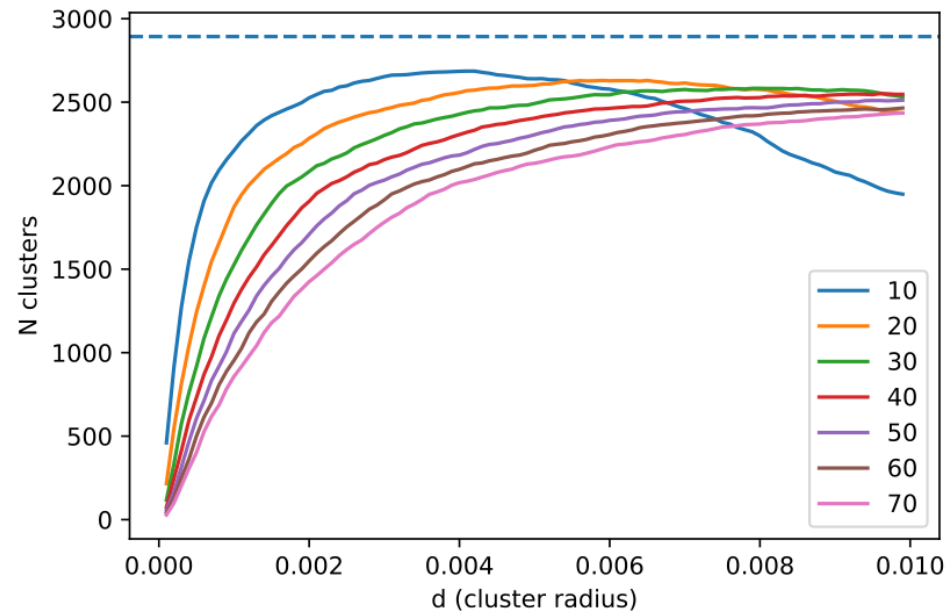
TUNING PERFORMANCE

OPTIMAL RADIUS:
 $0.0005 - 0.0010 \text{ rad}$

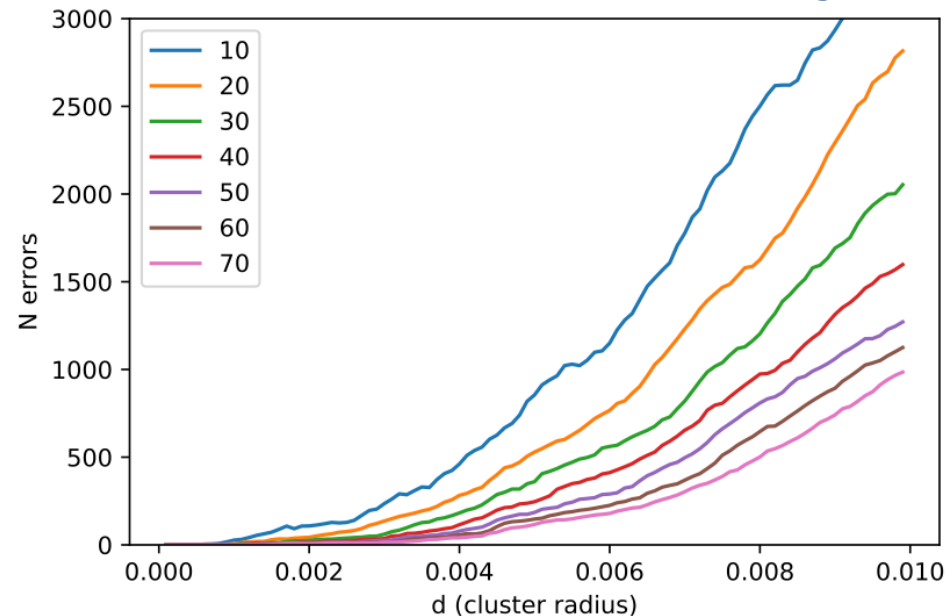
Selected KD-tree
clustering for speed
(average case $\log(n)$)

Also had good results
with agglomerative
clustering

Total clusters detected vs. KD-tree cluster radius (training set)



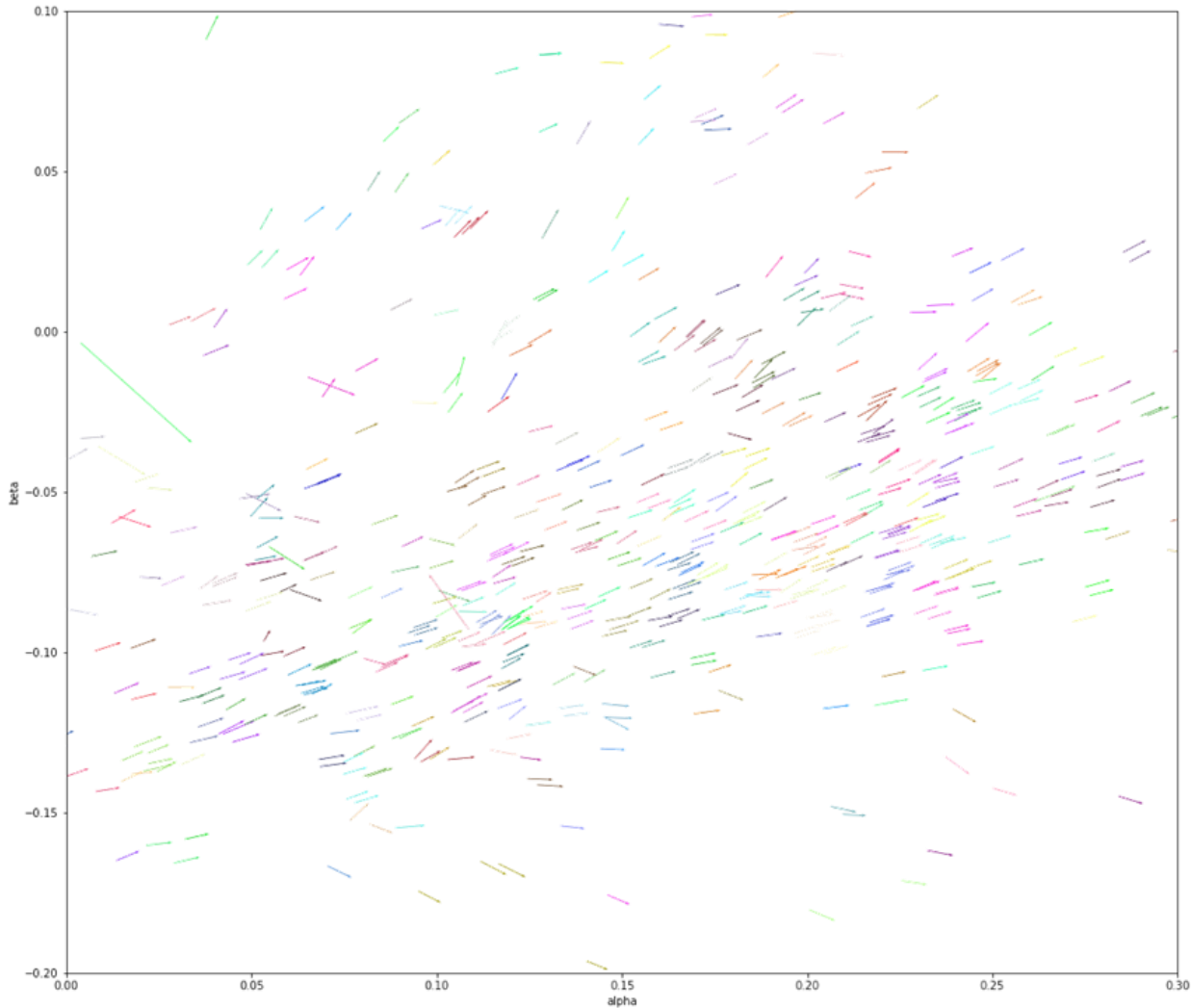
Error rate vs. KD-tree cluster radius (training set)



CLUSTERING RESULTS

90% OF ASTEROIDS DETECTED
WITH NEAR-ZERO ERROR!

Identified Asteroids (common colors = a single asteroid)



CONCLUSIONS

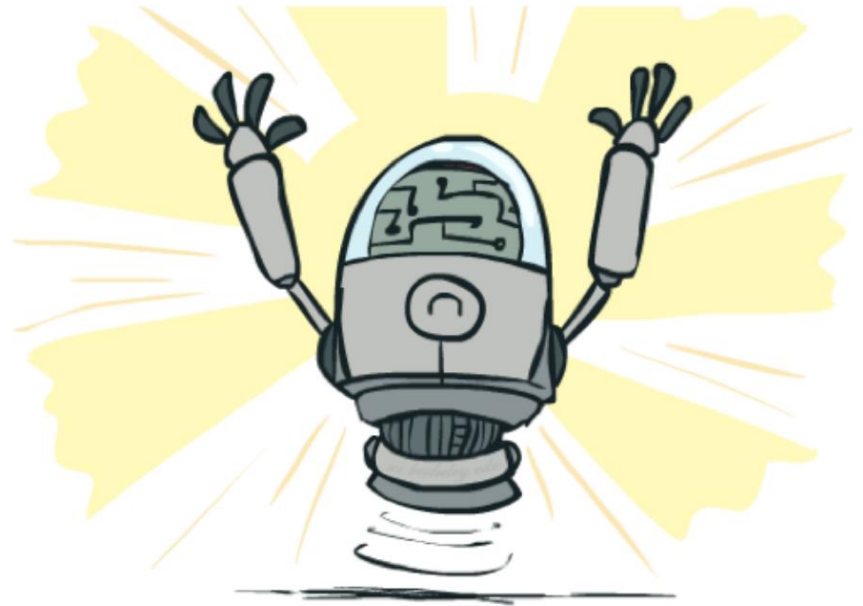
Conclusion: Strong tracklet linking with heliocentric transformation & KD-tree clustering

Also able to do so in just $O(n \log n)$ time,
a scalable solution!!

Limitations: currently restricted to small
(monthly) observation time window

Next Steps: Run the algorithm over all 14m
tracklet observations!

Thanks To: The Minor Planet Center for training data, Scott and Brian for project support!

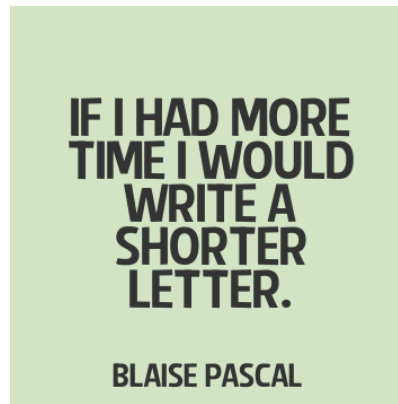




1 COIN 1 PLAY

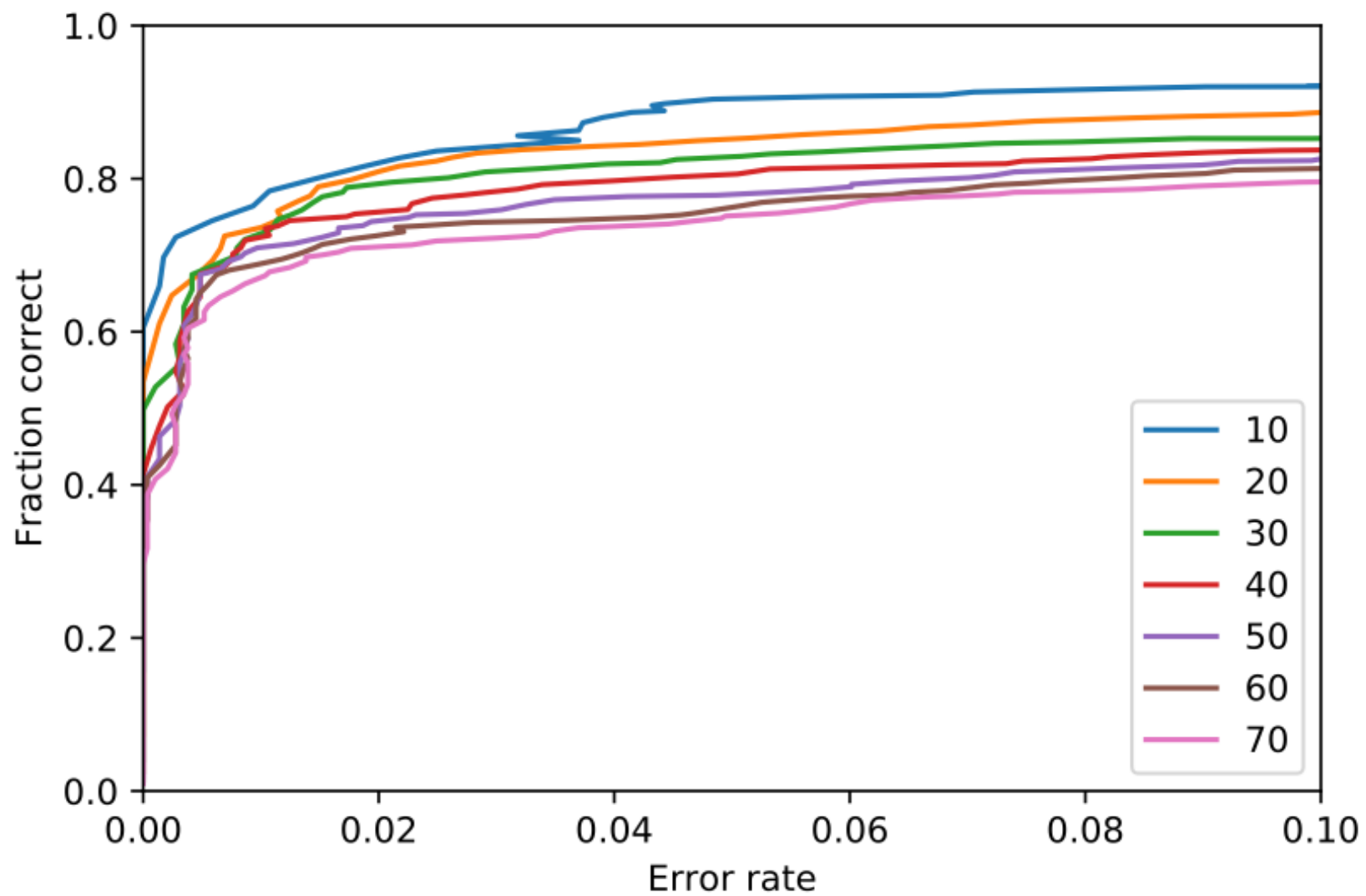
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APPENDIX/SUPPORTING SLIDES



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Training AUC



Agglomerative Clustering Dendrogram (Truncated)

