

# Neuromorphic Engineering I

**Time and day :** Lecture Mondays, 14:00-16:00 ~~13:15 – 14:45~~, at <https://ethz.zoom.us/j/94419667014>

**Lab exercise location:** Online, via Zoom sessions with your TAs, <https://ethz.zoom.us/j/98109684953>

**Credits:** 6 ECTS credit points

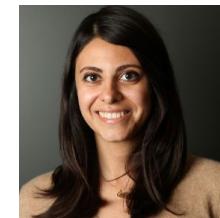
**Exam:** Oral 20-30 minutes at INI

**Labs:** Reports (**max 2 persons**). You must successfully **complete at least 9 lab exercises**. These exercises should include **the first 3 labs (mandatory)** and **at least one of the last 2 labs**. If you do all lab exercises, we will drop your 3 lowest lab grades.

**Grade:** 70% exam + 30% lab exercises

**Lectures from:** Tobi Delbrück, Giacomo Indiveri, Shih-Chii Liu, Melika Paywand

**Teaching assistants:** Elisa Donati, Giorgia Dellaferreira, Chenxi Wu, Carsten Nielsen



Tobi Delbrück

Giacomo Indiveri

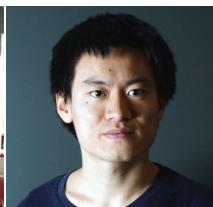
Shih-Chii Liu

Elisa

Giorgia

Chenxi

Carsten



[tobi,giacomo,shih@ini.uzh.ch](mailto:tobi,giacomo,shih@ini.uzh.ch)

# To do today

- Introduce book
- Arrange lab times (by doodle) and introduce new classchip and exercises via JupyterHub
- Introduce device physics
- Demo lab setup and class-chip use in JupyterHub

# Class composition (2020) 50 registered

## Count of Direction

UZH MNF Biology

6.0%

Special Student UZH

14.0%

Physics MSc

6.0%

Physics BSc

2.0%

Neural Syst.+Comp. MS.

20.0%

Mechanical Engineering

2.0%

## Count of Programme

Mob Biology

6.0%

Sp. Student Uni

14.0%

Physics MSc

6.0%

Physics BSc

2.0%

NSC MSc

20.0%

Mech. Engin MSc

2.0%

## Count of Language

Slovenian

2.0%

English

10.0%

Latvian

2.0%

Russian

4.0%

other

6.0%

Chinese

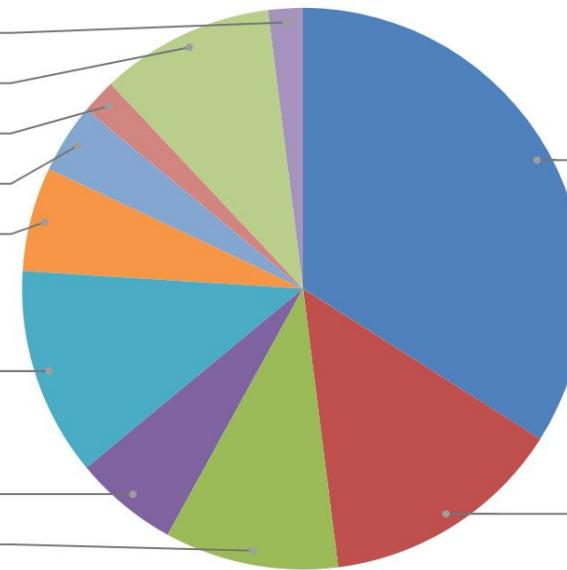
12.0%

French

6.0%

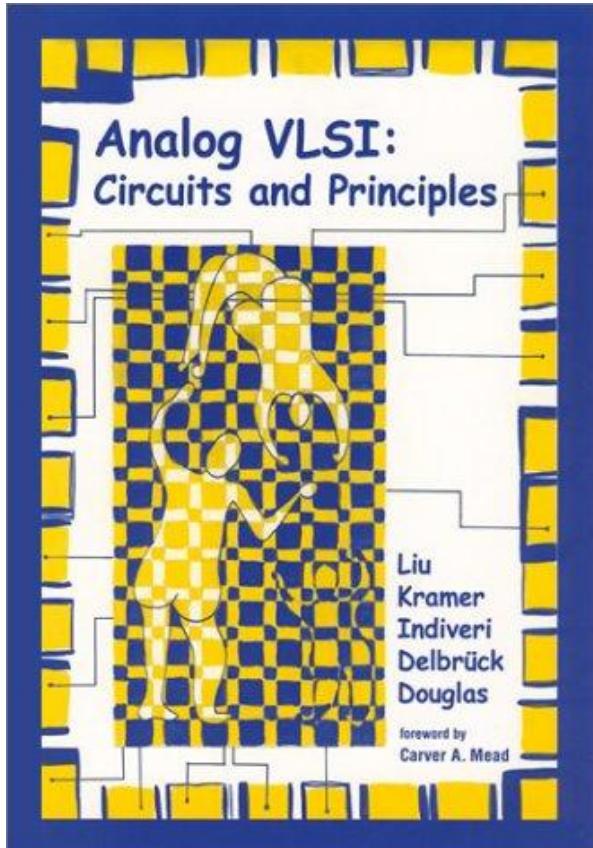
Spanish

10.0%

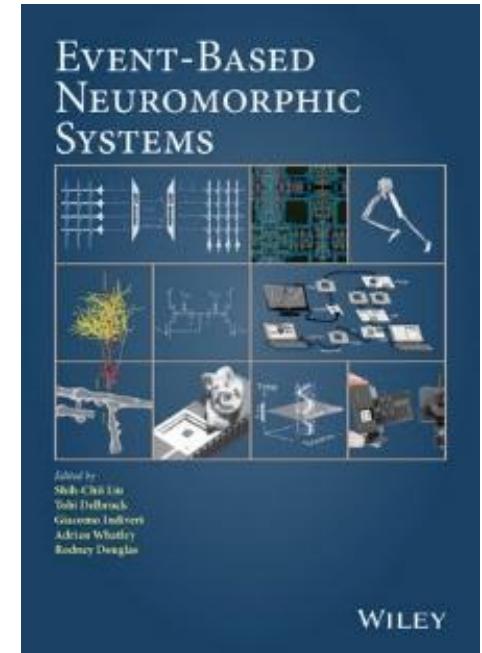


# Book(s)

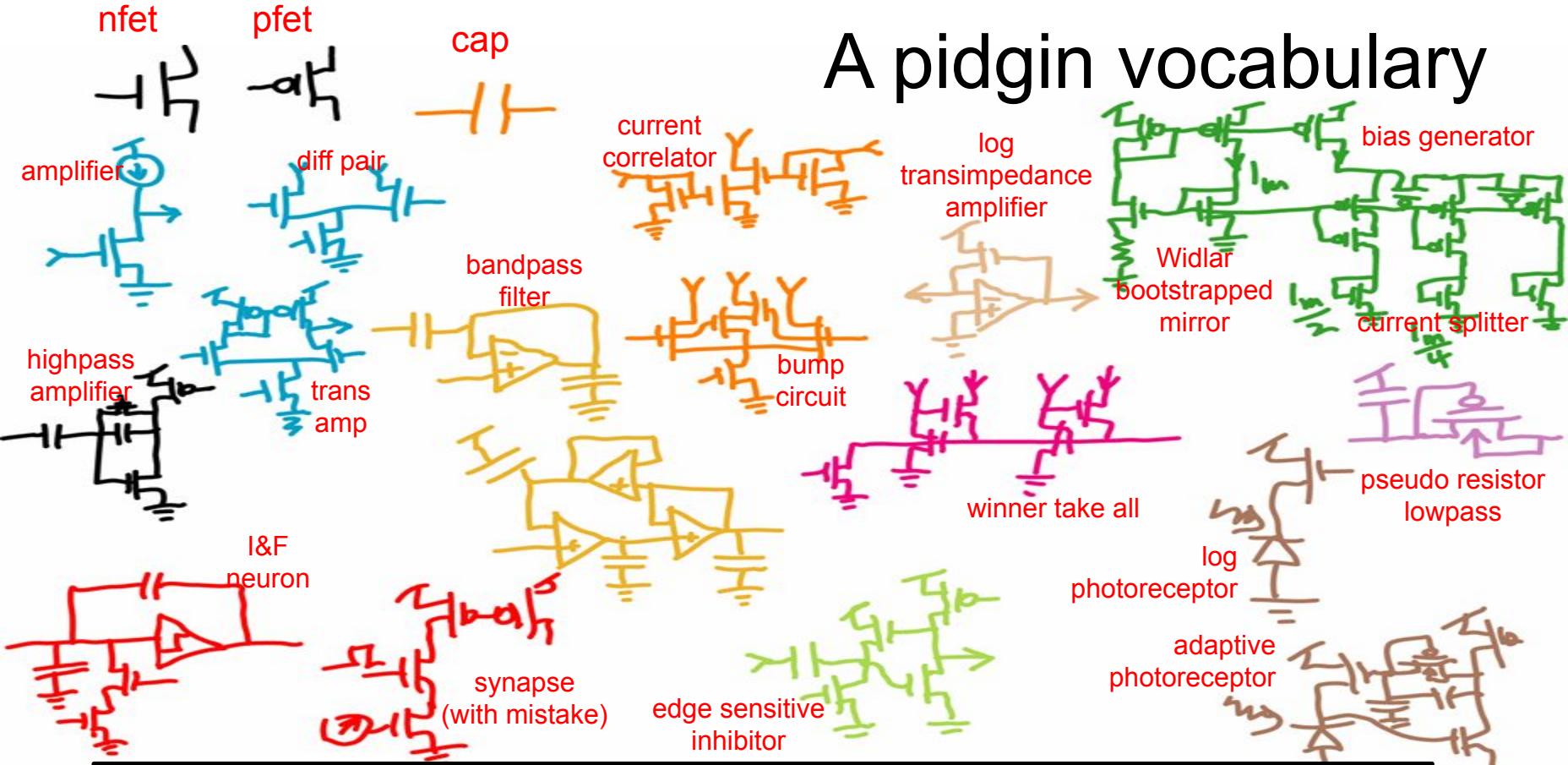
Introductory  
textbook  
(2002)  
[Amazon](#)



System examples  
(2015)  
[Amazon](#)



# A pidgin vocabulary



By the end of this semester, you should recognize many of these circuits and be able to reason your way through the others.

# Neuromorphic Electronics?

What is it all about?

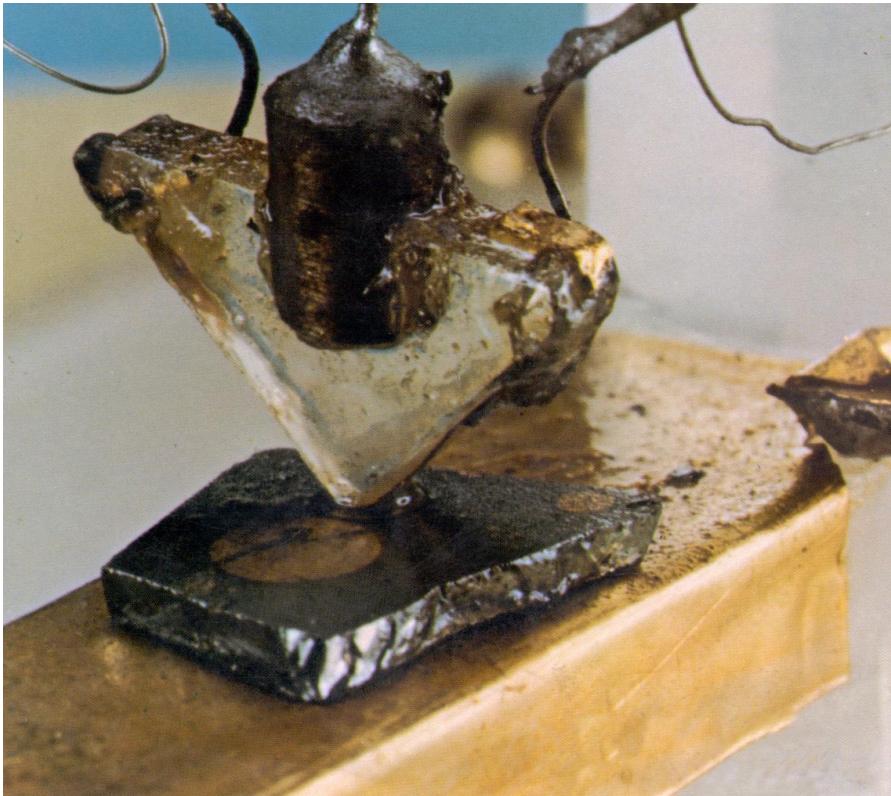
See Shih-Chii Liu talk from 2020 Telluride  
Neuromorphic Workshop:

*Neuromorphic electronics, A historical perspective*

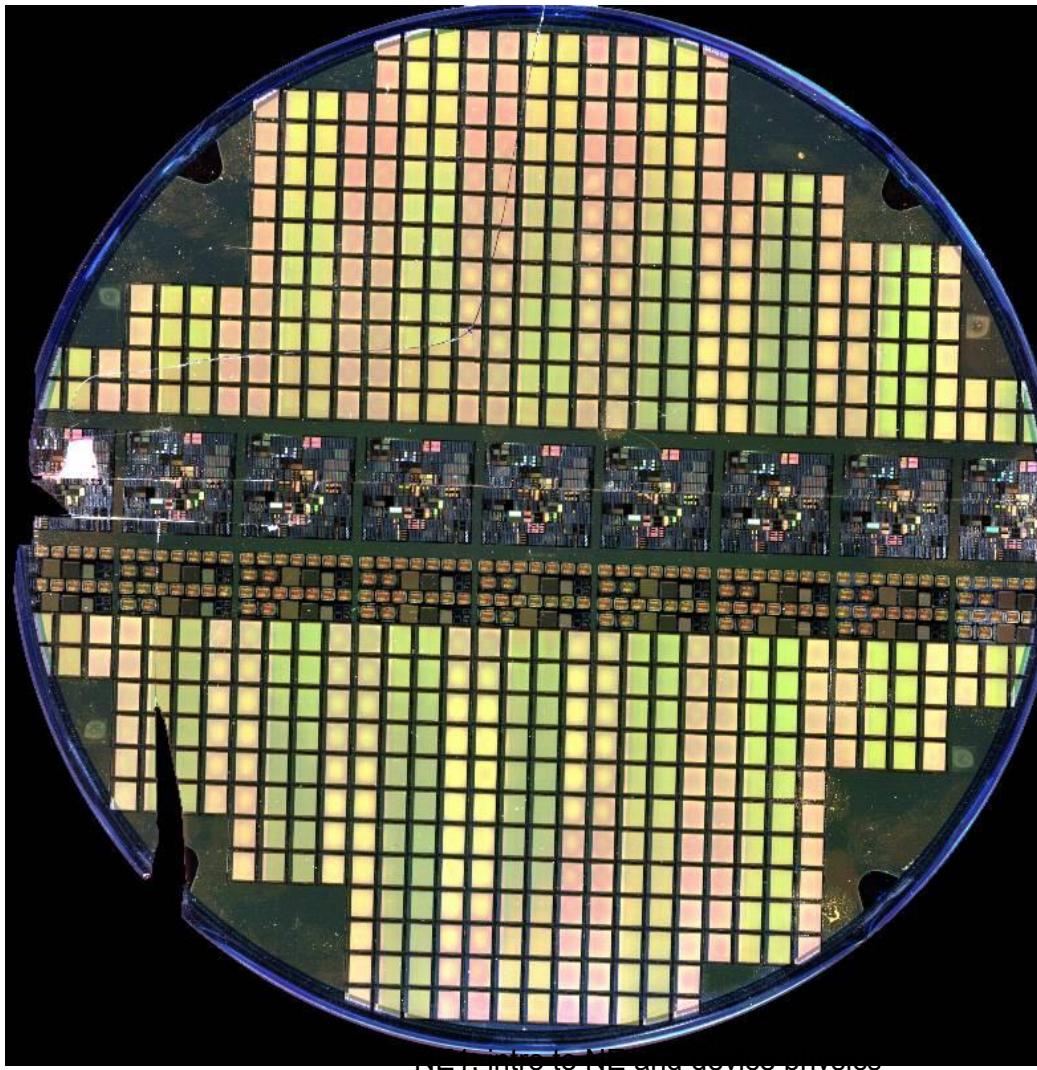
# The context

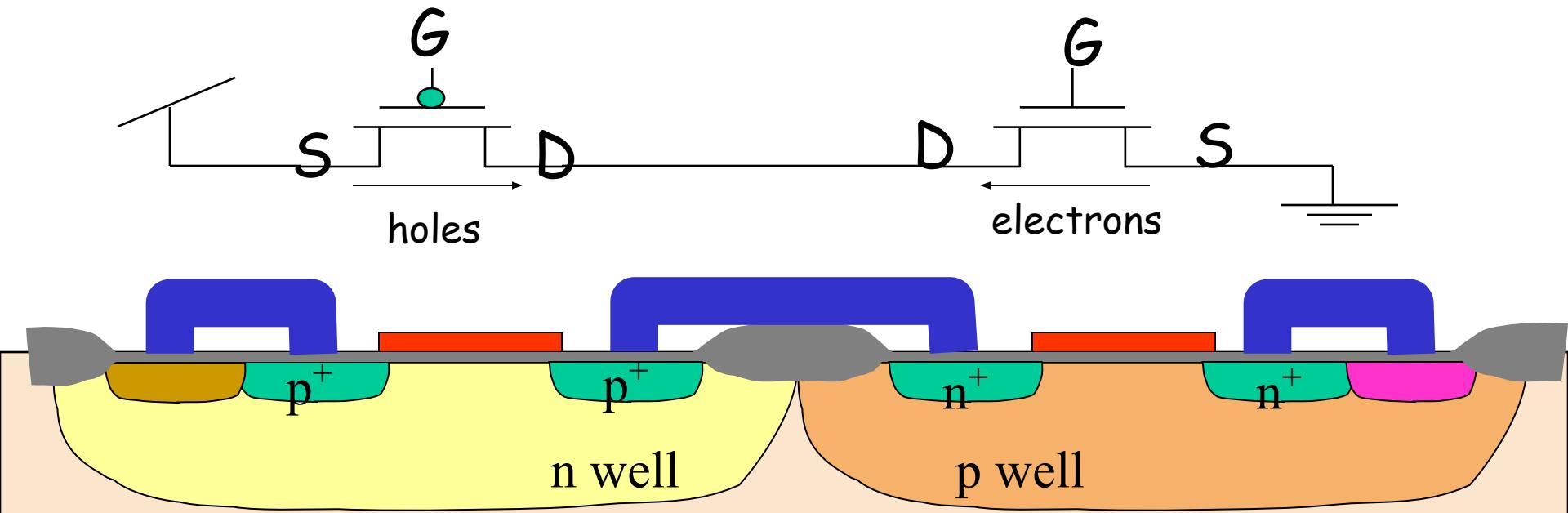
# Bardeen and Brattain

1947

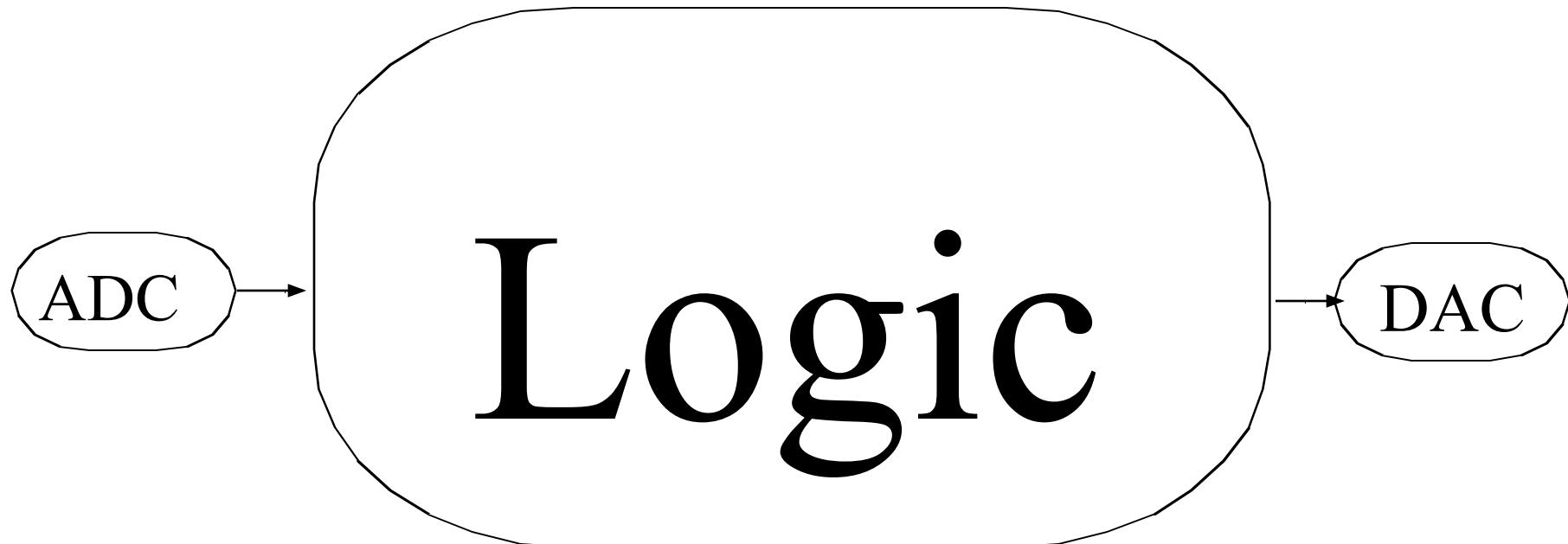


2000

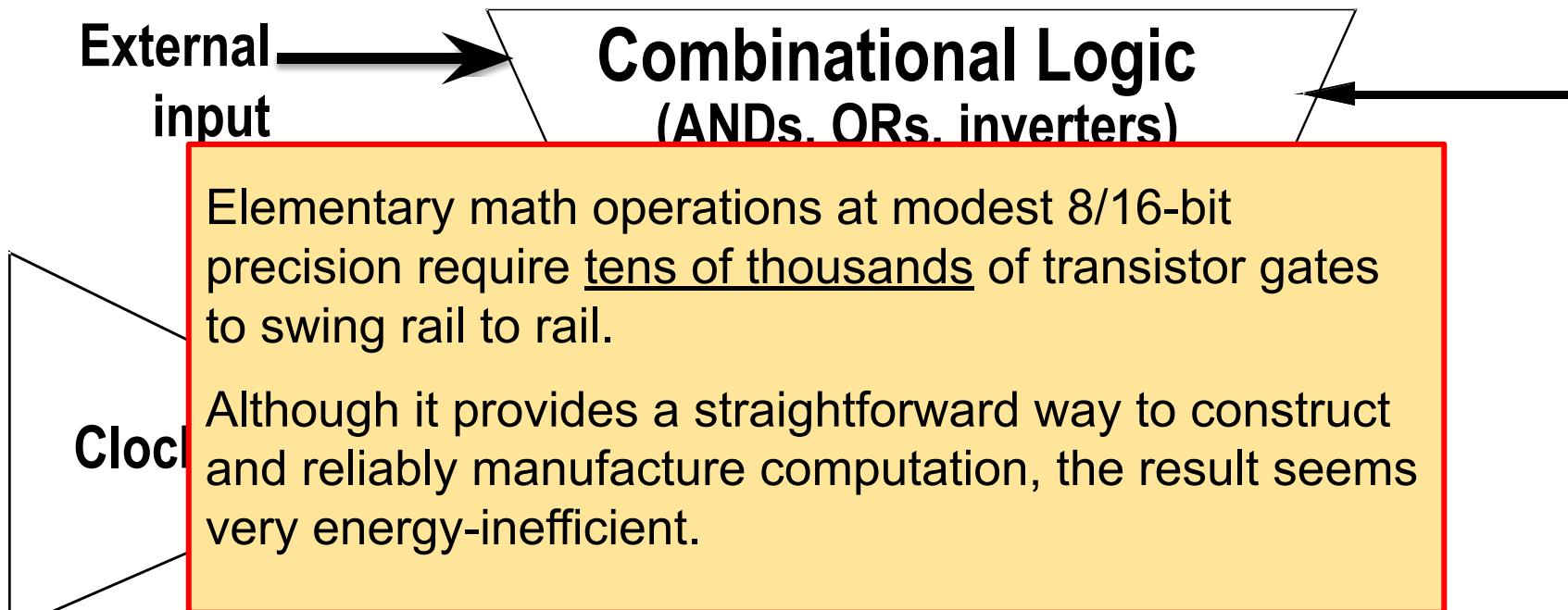




# Artificial real-world computation (or: How industry thinks of analog)



Synchronous logic is ubiquitously used to implement Finite State Machines (FSMs)



**Logic bus**  
**(many wires representing a digital symbol or state)**

# The motivation from biological computation

# Natural computation

even with 10kW computer power we cannot do this



Flies acrobatically  
Recognizes patterns  
Navigates  
Forages  
Communicates

10uW  
 $10^6$  neurons,  $10^9$  synapses  
10 op/s/synapse

$10^{-15}$  J/op  
(op=synaptic activation)

Digital silicon  $10^{-7}$  to  $10^{-13}$  J/op (MAC)

Biology is  $10^8$  to  $10^{13}$  times as efficient as digital silicon

# Sparsity

Estimate energy use and spike rate in the human brain

$$10^{11} \times 10^4 \times 10^{-1} \times 10^{-9} \times 10^{-3} \times X = 10^1$$

Neurons\*    Syn/neuron    V                  A                  sec      Avg. spike rate      W

---

J/syn. Act. =  $10^{-13}$  J = **0.1 pJ**

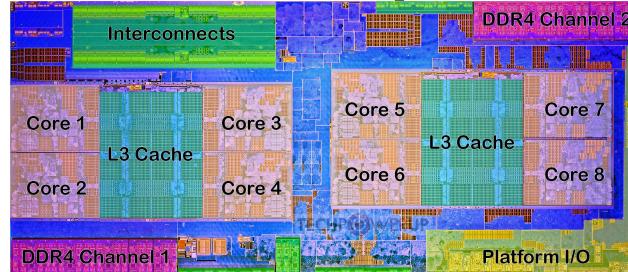
Avg. **output** spike rate = 1 Hz

10<sup>4</sup> fan-out means avg. synaptic **input** rate per neuron = 10 kHz

It is very different than conventional DNNs, where every neuron sends its messages to all recipients at the frame rate, e.g. 100Hz

# Computer vs. Brain

AMD Ryzen  
192mm<sup>2</sup>  
5B FETs  
180W



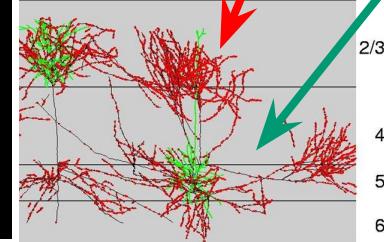
Cortex

1mm<sup>3</sup>

100k neurons

1B synapses

~1mW



dendrite

Anderson et al.  
2003

At the system level, brains are about 1 million times more power efficient than computers. Why?

Cost of elementary operation (turning on transistor or activating synapse) is about the same.  
It's not some magic about physics.

Computer	Brain
Fast global clock	Self-timed, sparse computation (avg spike rate in brain ~1Hz)
Bit-perfect deterministic logical state	Synapses are stochastic! 20% probability. Computation dances: digital→analog→digital
Memory distant in time and space to computation	Memory in synapses, at computation
Devices frozen on fabrication	Constant adaptation and self-modification

The fact that we can build devices that implement the same basic operations as those the nervous system uses leads to the inevitable conclusion that **we should be able to build entire systems based on the organizing principles used by the nervous system.**

*Carver Mead*, Physicist by inclination

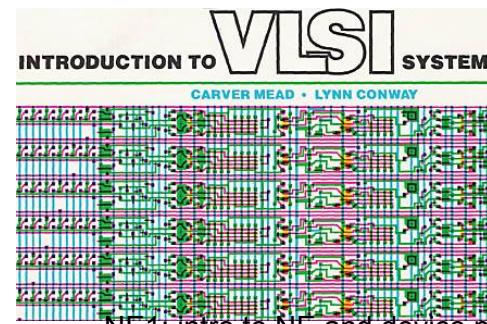
1966 Inventor of GaAs MESFET transistor

1970's: Coiner of term "Moore's Law"

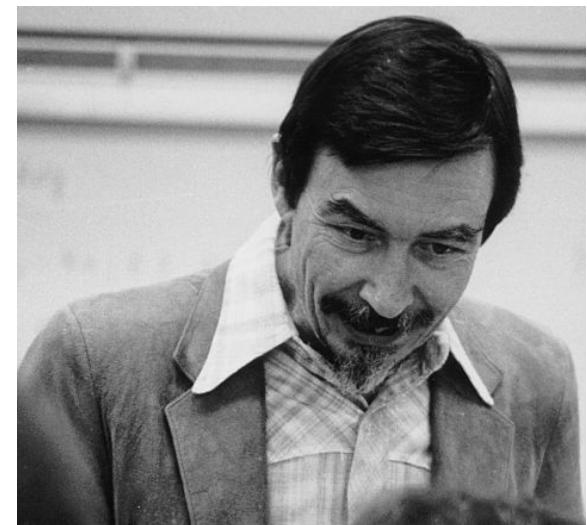
1980 Co-author of main logic design textbook for 20 years

2013: [ISSCC keynote talk](#) ([see more cool talks here](#))

"The high priest of silicon"



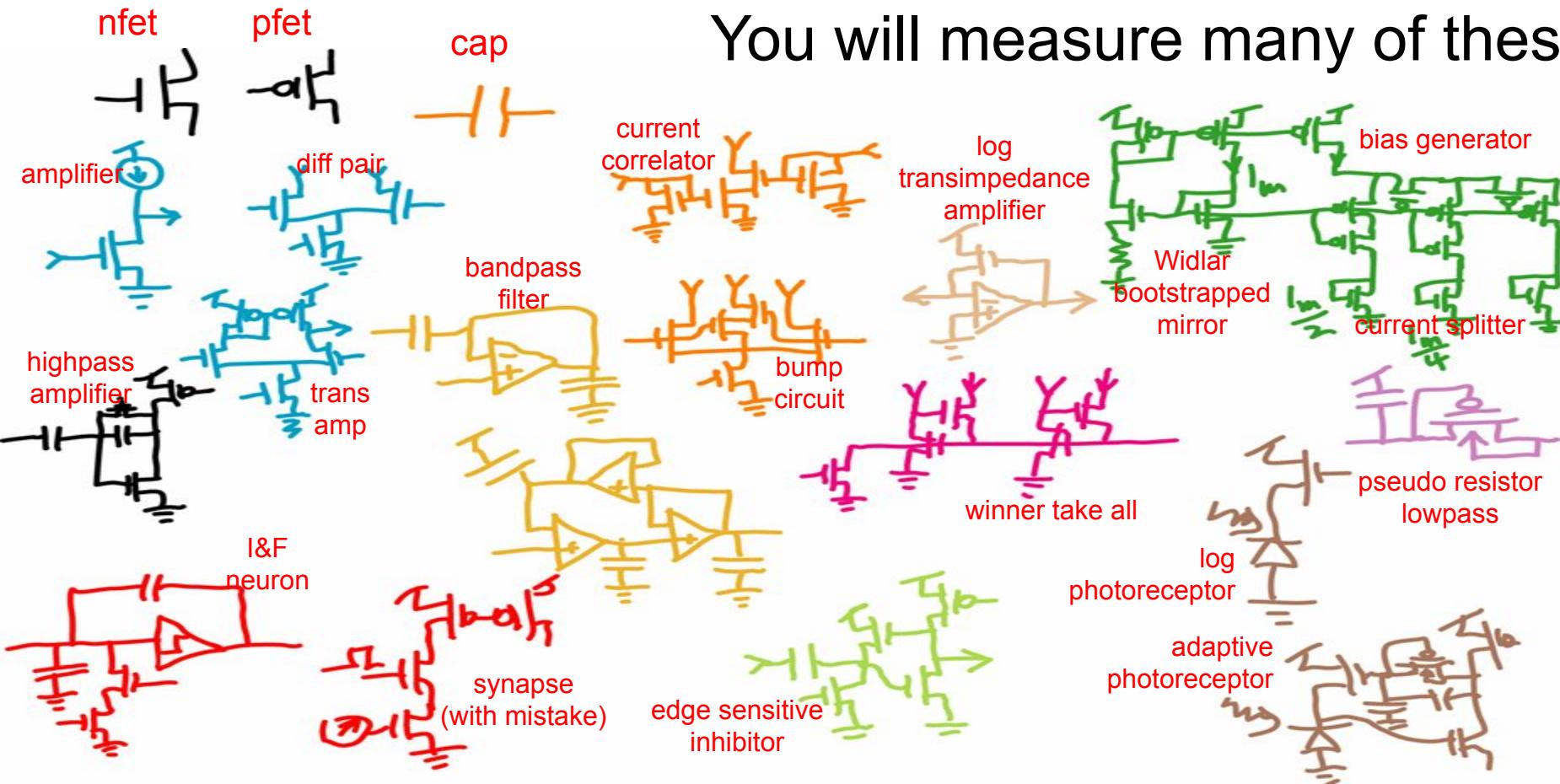
*Proc. IEEE, 1990*



T Delbruck, CNS182 class, Caltech, ca 1989

# Exercises: First look

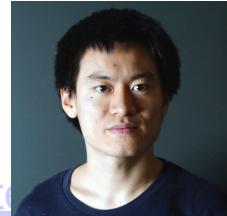
# You will measure many of these



# Lab exercises organization

- The labs are done in groups of 2 remotely via zoom and TLJH; the best way is for two to meet in person with your laptops, and use one for zoom and the other for TLJH.
- The first three labs last 2 hours, the rest are 4 hours (the whole morning/afternoon in which you sign up), the material for the corresponding week will be published at the end of the lecture.
- Please use the OLAT Forum to look for your lab partner.
- You should hand in the prelab, lab report and post-lab as a group on OLAT dropbox before your next lab starts.
- For questions regarding the labs, please contact  
[chenxi@ini.uzh.ch](mailto:chenxi@ini.uzh.ch)

TLJH= The Littlest JupyterHub



# Links for the lab exercises

lab1-scheduling: Sign up at [this lab exercise doodle](#).

Jupyter notebooks <https://code.ini.uzh.ch/CoACH/CoACH-labs/tree/patch-1/jupyter>

- [Lab 1](#): Automated Data Acquisition and Analysis (Running the classchip)
- Lab 2-3: Subthreshold Behavior of Transistors, Transistor superthreshold saturation current and drain characteristics
- Lab 4-5: Static Circuits: Current Mirror, Differential Pair, Current Correlator, Bump Circuit, and Transconductance Amplifier
- Lab 6: Winner-Take-All circuit
- Lab 7: Integrator Circuits
- Lab 8: Photoreceptors I: Phototransduction
- Lab 9: Photoreceptors II: Photoreceptor Circuits
- Lab 10: Silicon Synaptic Circuits
- Lab 11: Silicon Neuron Circuits
- Lab 12: *TBA*

Sign in

Warning: JupyterHub seems to be served over an unsecured HTTP connection. We strongly recommend enabling HTTPS for JupyterHub.

Username:

Password:

# 2020

## Class chip: COaCH

AMS (Austria Microsystems)  
 180nm technology  
 $t_{ox} = 3.75 \text{ nm}$ ,  $C_{ox} = 9 \text{ fF}/\mu\text{m}^2$ .

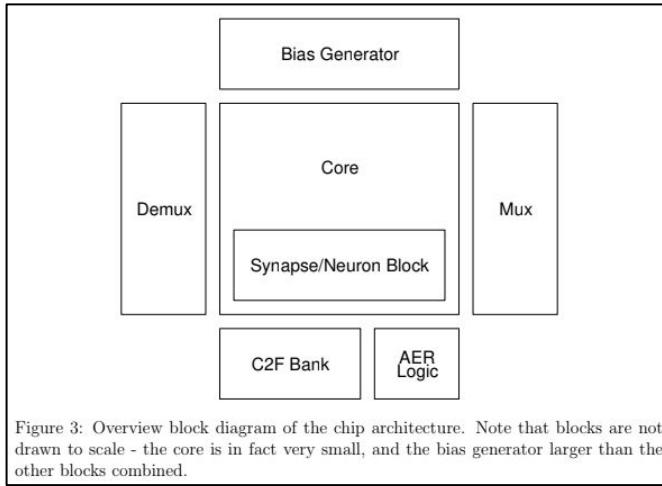
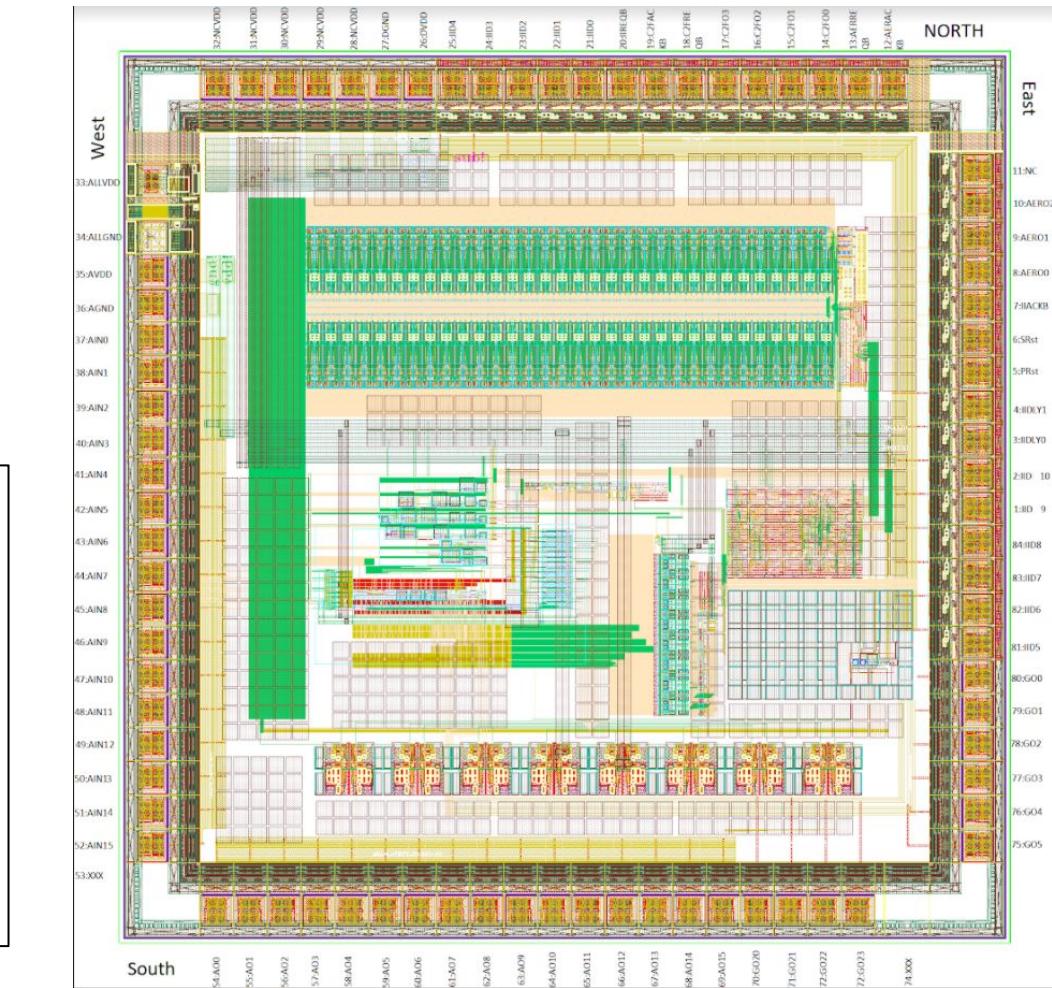


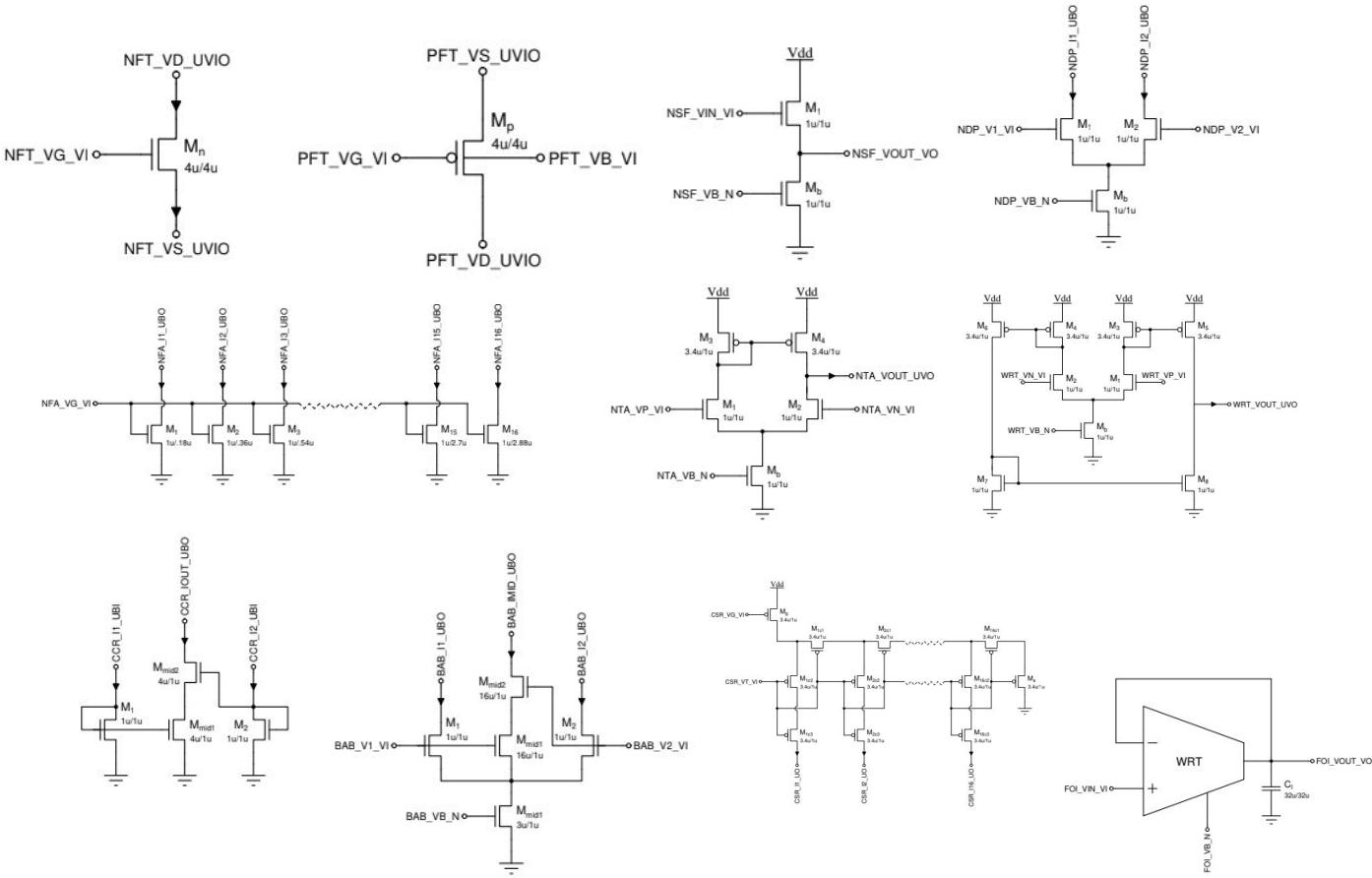
Figure 3: Overview block diagram of the chip architecture. Note that blocks are not drawn to scale - the core is in fact very small, and the bias generator larger than the other blocks combined.



# Partial contents of class chip

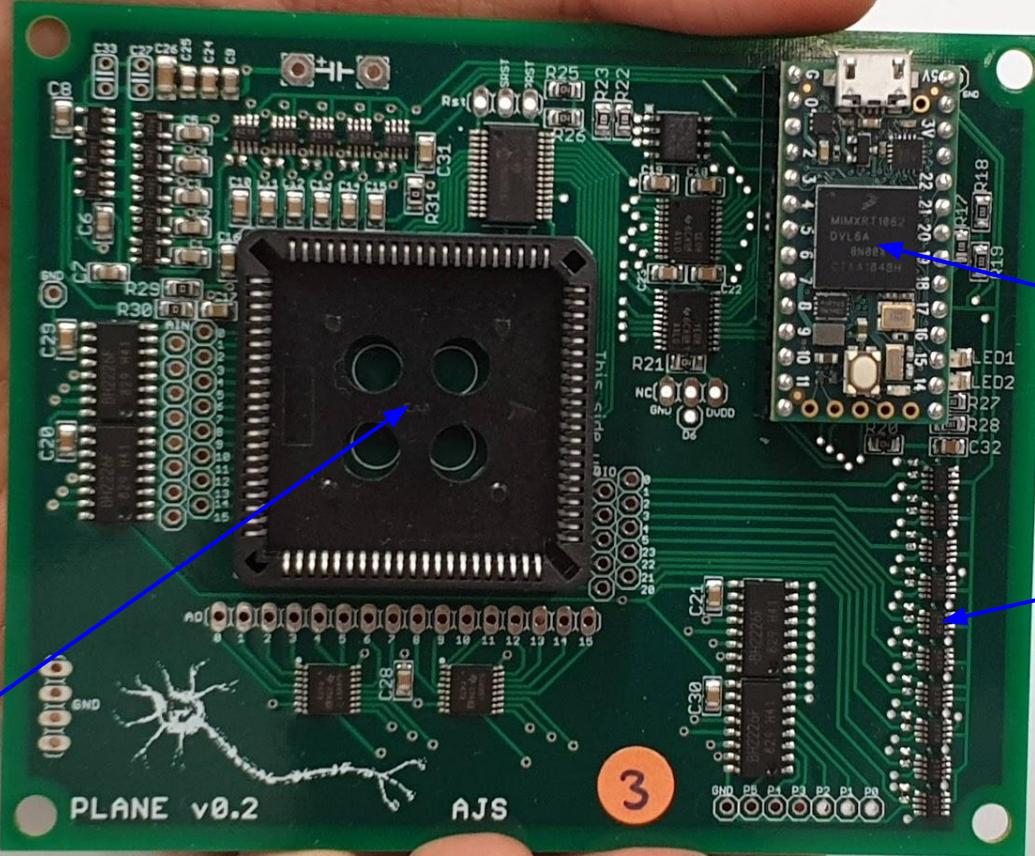
## 3 Test Circuits

- 3.1 N-FET Device . . . . .
- 3.2 P-FET Device . . . . .
- 3.3 N-FET Array . . . . .
- 3.4 P-FET Array . . . . .
- 3.5 N-Type Source-Follower . . . . .
- 3.6 P-Type Source Follower . . . . .
- 3.7 N-Type Differential Pair . . . . .
- 3.8 P-Type Differential Pair . . . . .
- 3.9 Current Correlator . . . . .
- 3.10 Bump Antibump . . . . .
- 3.11 N-Type 5T Transamp . . . . .
- 3.12 P-Type 5T Transamp . . . . .
- 3.13 Wide-Range Transamp . . . . .
- 3.14 Current-Splitter Array . . . . .
- 3.15 Winner-Take-All Array . . . . .
- 3.16 Follower-Integrator . . . . .
- 3.17 Follower-Differentiator . . . . .
- 3.18 Resistive Element . . . . .
- 3.19 Symmetric Resistive Element . . . . .
- 3.20 Source-Follower Photoreceptor . . . . .
- 3.21 DVS Pixel . . . . .
- 3.22 Second-Order Section . . . . .
- 3.23 Log Domain Synapse . . . . .
- 3.24 DPI Synapse . . . . .
- 3.25 Dual-DPI Synapse . . . . .
- 3.26 Axon-Hillock IF Neuron . . . . .
- 3.27 ADEXIF Classic Neuron . . . . .
- 3.28 ADEXIF Thresholded Neuron . . . . .
- 3.29 ADEXIF Sigma-Delta Neuron . . . . .
- 3.30 Hodgkin-Huxley Neuron . . . . .



# Classchip PCB

COACH  
classchip

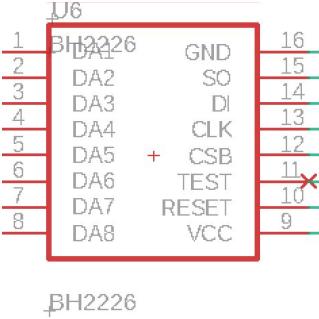


Teensy 32-bit  
Arduino uC  
with 10-bit ADC

Current monitor  
transimpedance  
ADCs

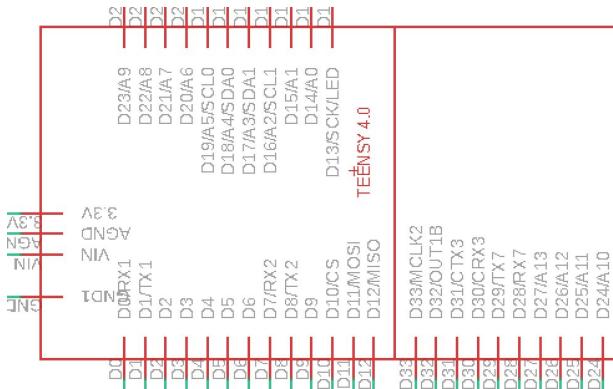
# Measuring currents and voltages

Set voltages using  
8-bit [2226](#) DAC

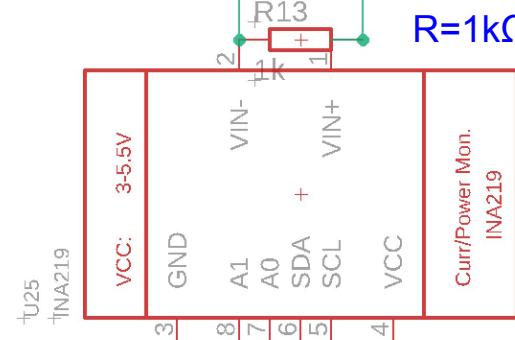
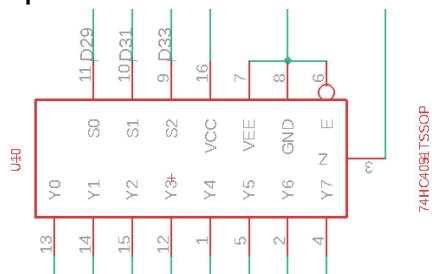


Measure voltages using [Teensy](#)

[10-bit ADC](#):  $V_{ref}=V_{dd}=3.3\text{ V}$ .

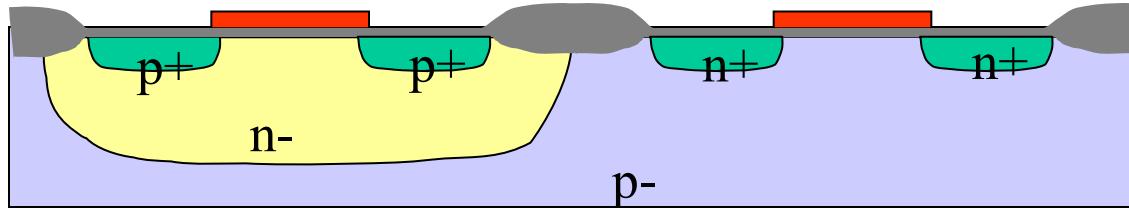


Select circuit pins with on-chip  
multiplexers



# First look at semiconductors and transistors

# MOS transistors – semiconductor device physics



We need to understand enough about semiconductors and junctions to understand how MOS transistors work

- Insulators, conductors, semiconductors
- Crystal structure of silicon
- Band structure (valence, conduction, and forbidden bands)
- Holes and electrons
- Mechanisms of charge transport (diffusion & drift)
- Doping with donors and acceptors
- Fermi-Dirac distribution
- Law of mass action ( $np=n_i^2$ )
- p-n junction
- Reverse biased junction and its capacitance

# Donors and Acceptors in the periodic table

I	II	III	IV	V	VI	VII	Zero
H							He
Li	Be	(B)	C	N	O	F	Ne
Na	Mg	Al	Si	(P)	S	Cl	Ar
K	Zn	Ga	Ge	(As)	Se	Br	Kr
Rb	Cd	In	Sn	Sb	Te	I	Xe



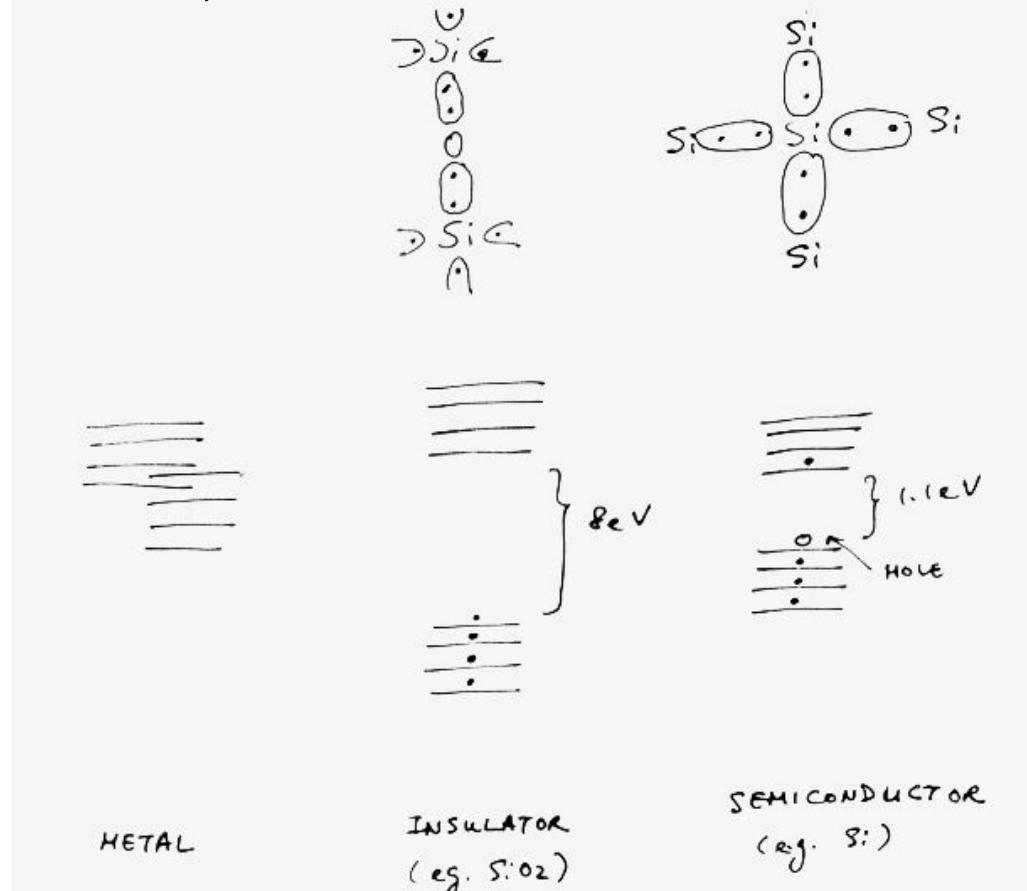
Acceptors

Donors

1 missing electron

1 extra electron

# Conductors, Semiconductors and Insulators



Mead, ca 1989, from  
Andy Grove

# Donors and Acceptors in the periodic table

I	II	III	IV	V	VI	VII	Zero
H							He
Li	Be	(B)	C	N	O	F	Ne
Na	Mg	Al	Si	(P)	S	Cl	Ar
K	Zn	Ga	Ge	(As)	Se	Br	Kr
Rb	Cd	In	Sn	Sb	Te	I	Xe



Acceptors

Donors

1 missing electron

1 extra electron

# The silicon lattice with an electron donor atom

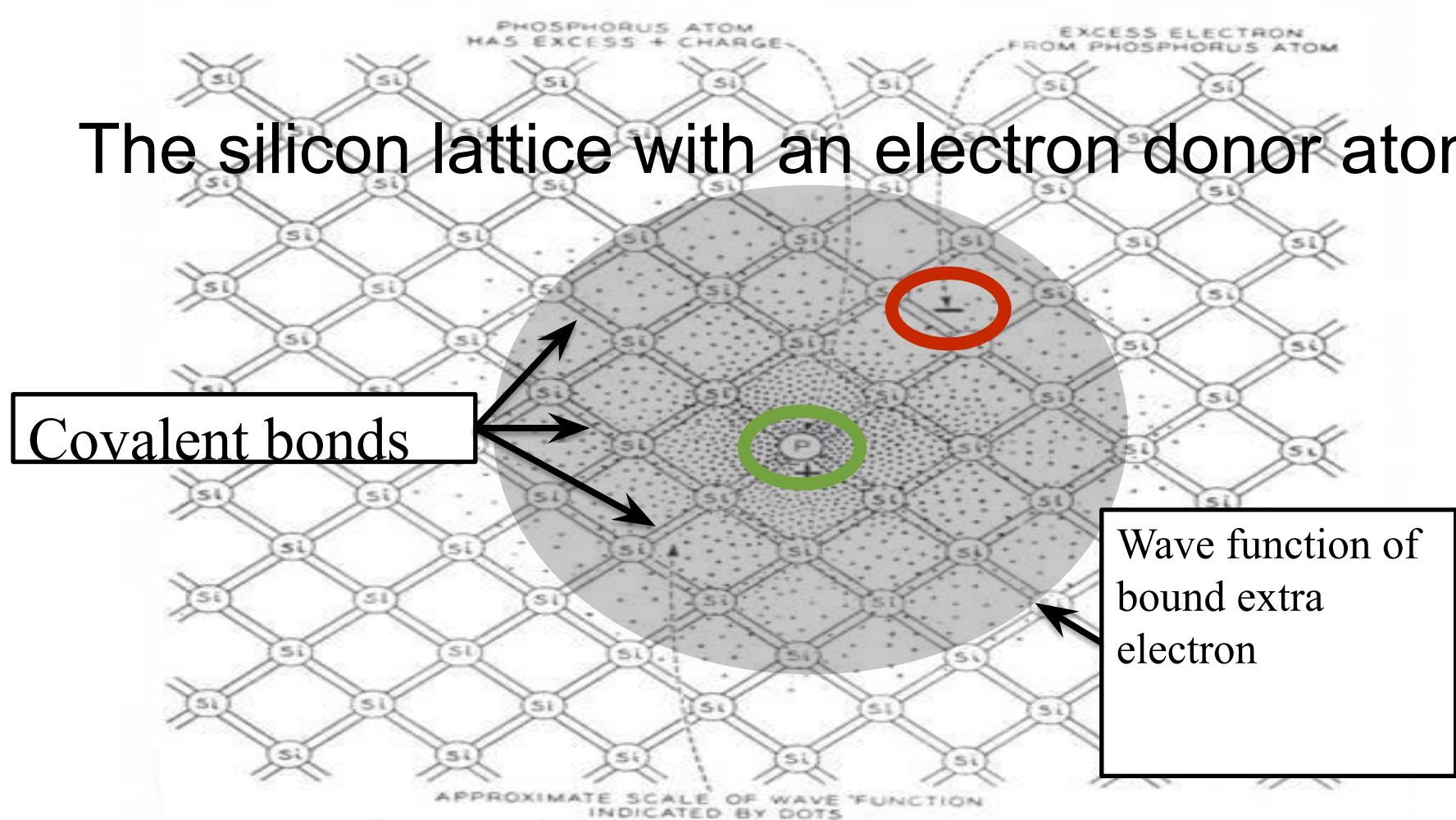
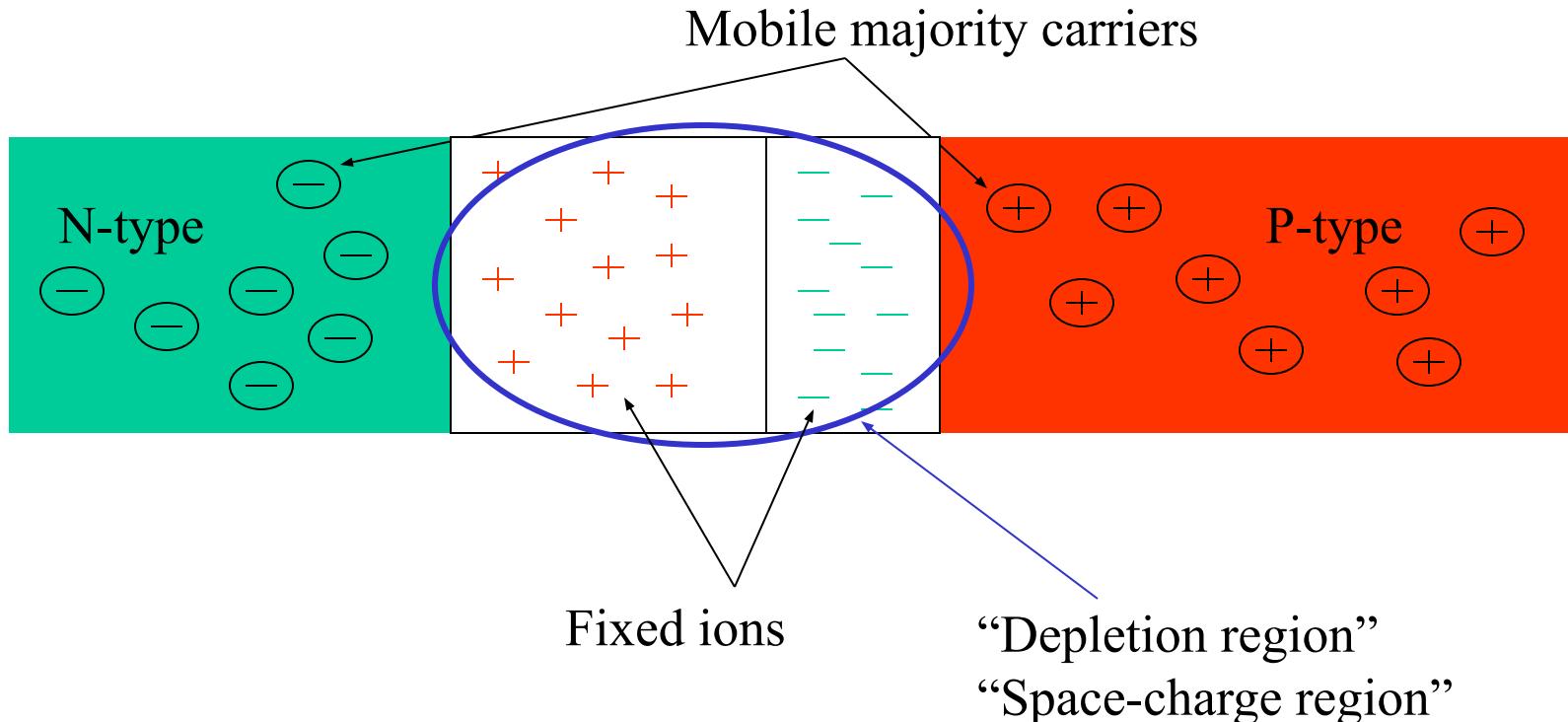
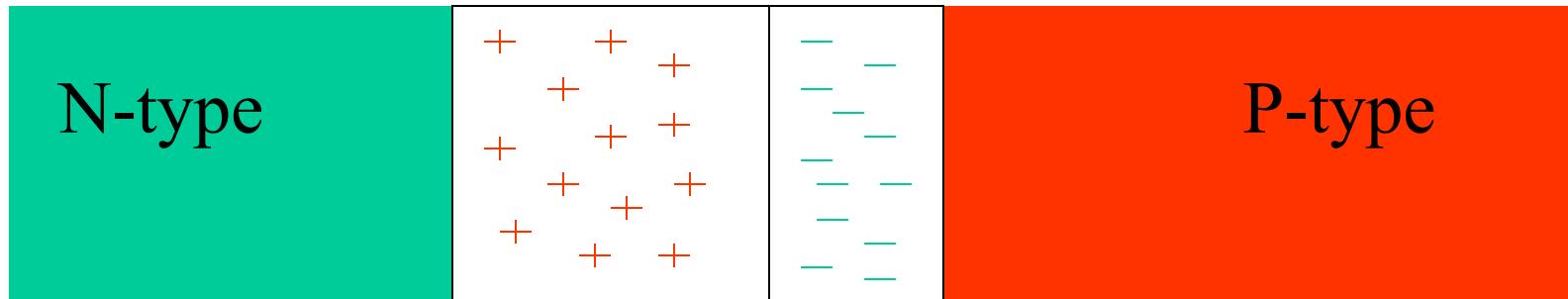


FIG. 1-14—Wave Function of Electron Bound to Phosphorous Atom in Silicon.

# A P-N junction



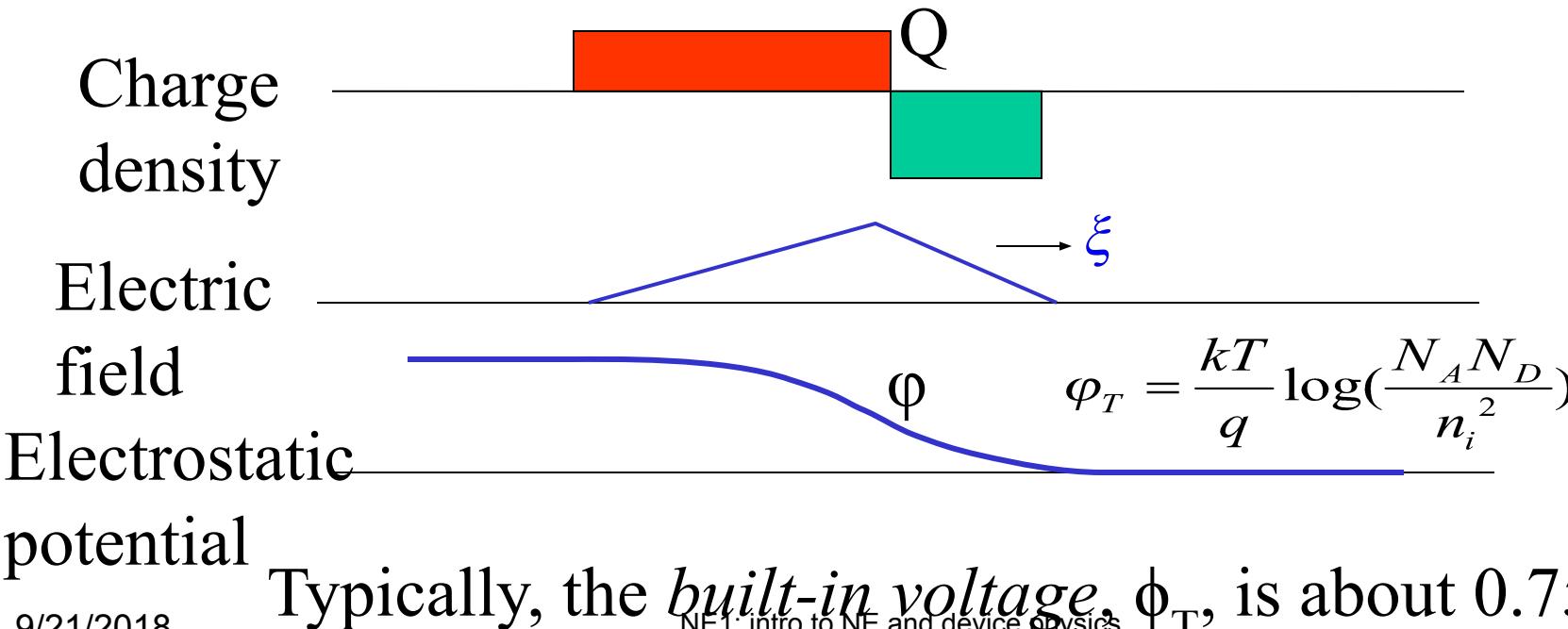
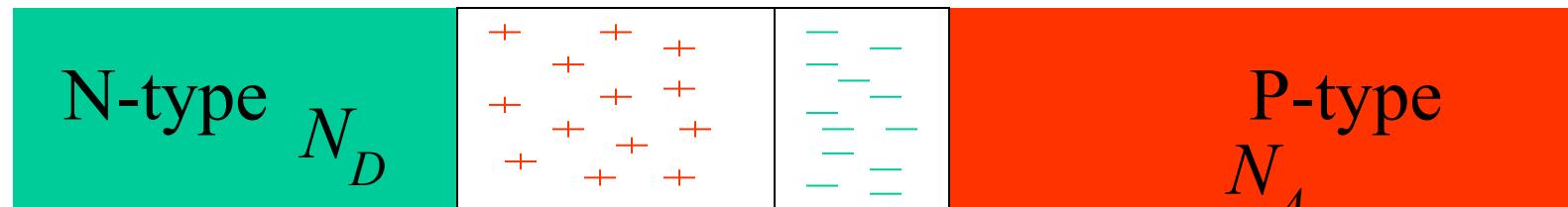
# A P-N junction



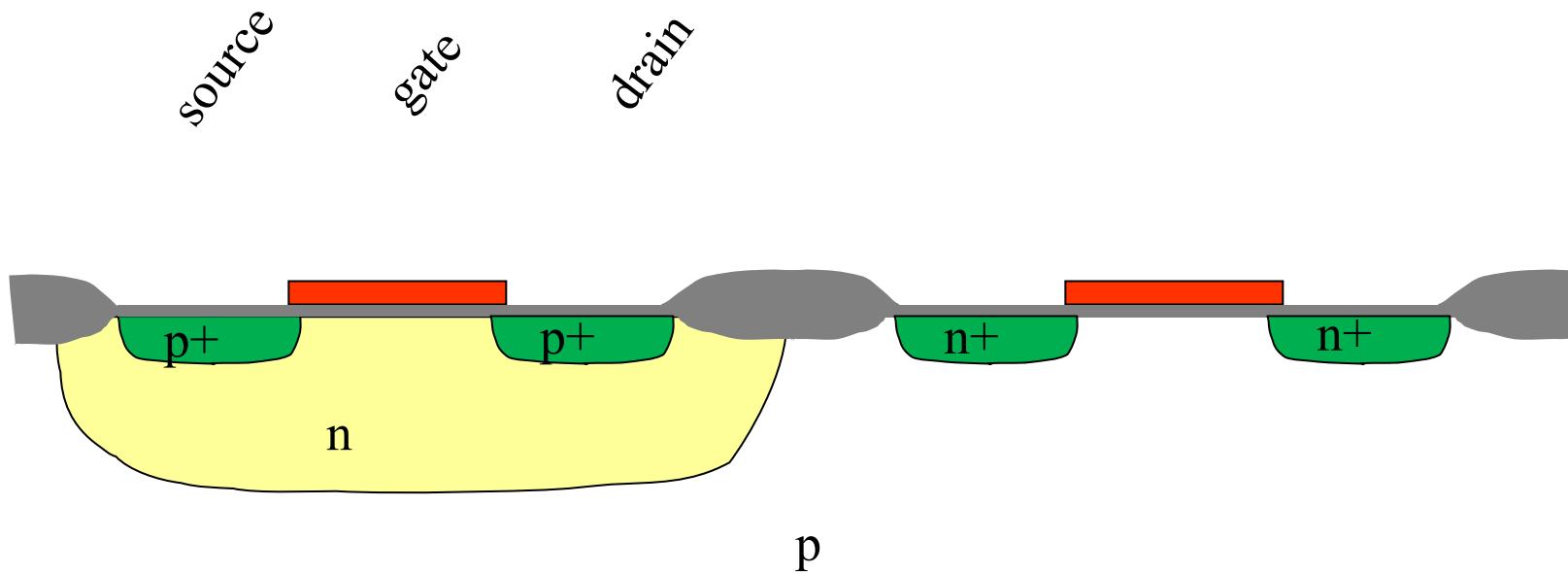
$\xleftarrow{\text{Diffusion of holes from } p \text{ region}}$   
 $\xleftarrow{\text{Diffusion of electrons from } n \text{ region}}$

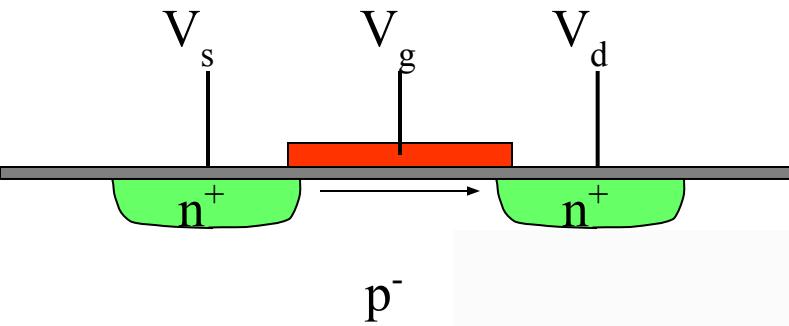
In equilibrium, *Drift* = *Diffusion* for electrons *and* holes

# Charges, fields, and potentials in a PN junction

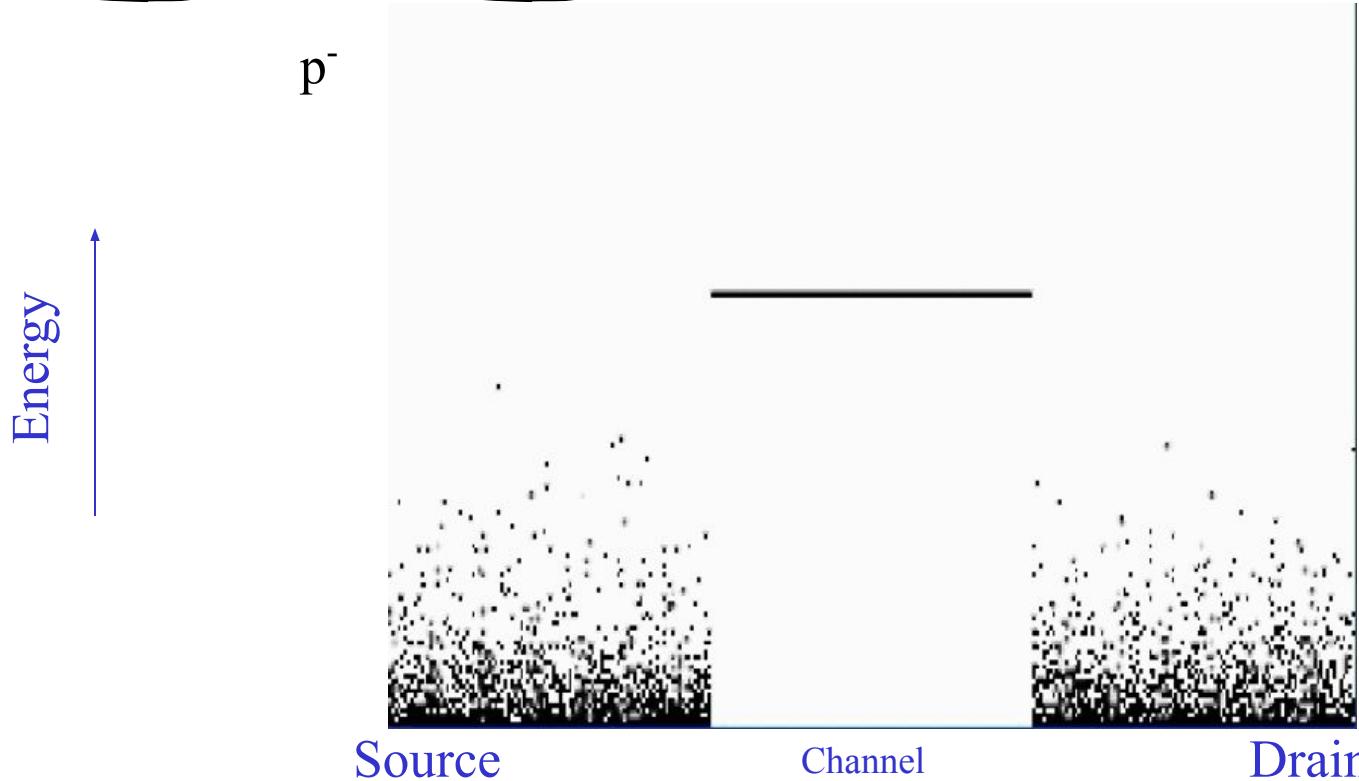


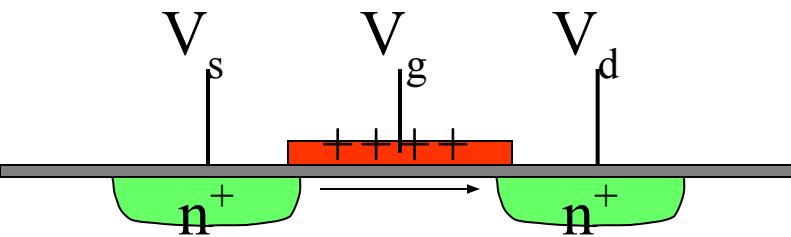
MOS transistors use insulated gates to control barrier energies at PN surface junctions at source and drain



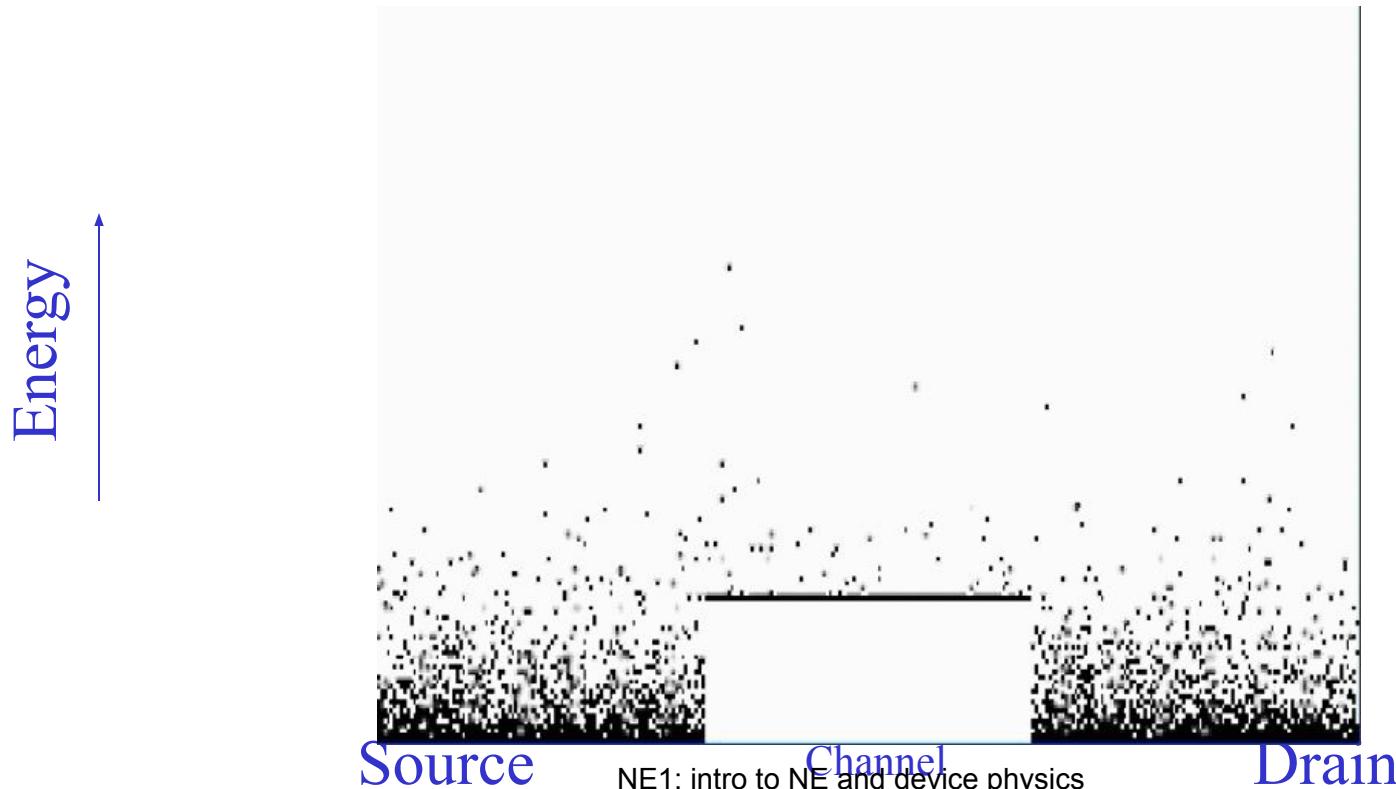


Small  $V_{gs}$ ,  $V_{ds}=0$





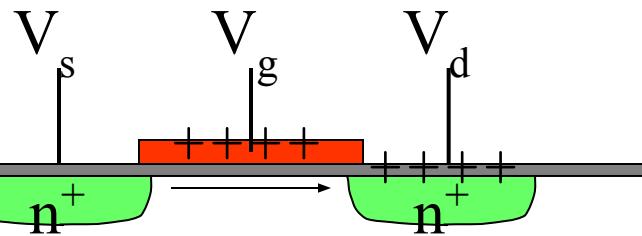
Larger  $V_{gs}$ ,  $V_{ds}=0$



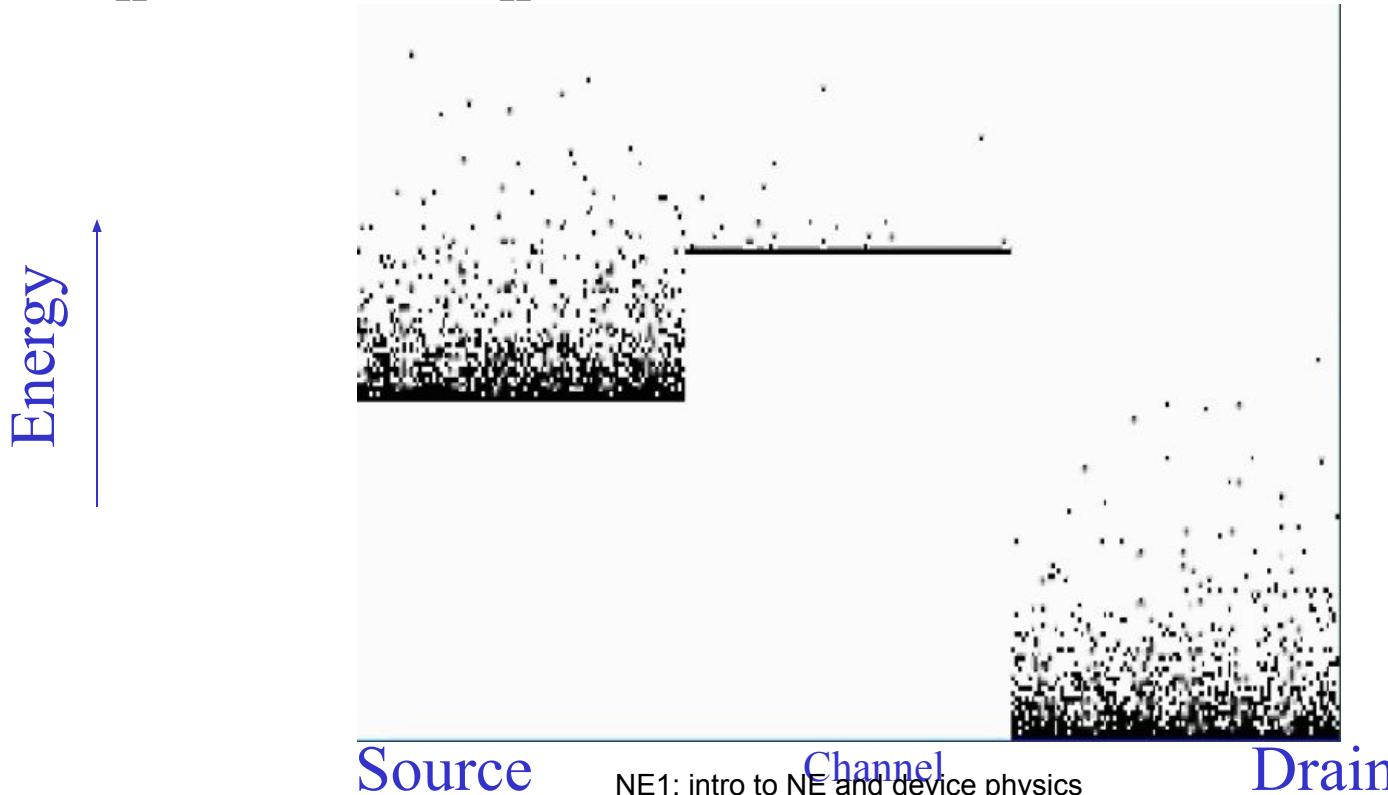
Source

Channel

Drain



Larger  $V_{gs}$ ,  
Large  $V_{ds}$



# Closer look at silicon crystal structure and energy bands

# The Diamond Structure of Silicon

Each atom is  
covalently  
bonded to 4  
neighbors

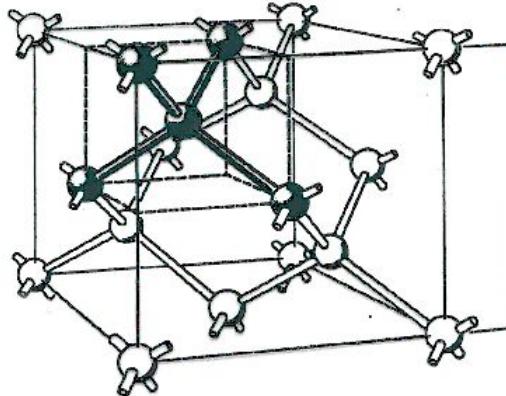


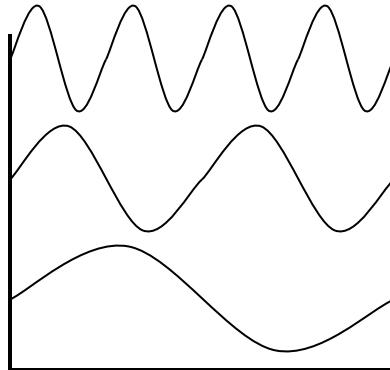
FIG. 1-3—The Diamond Structure, Showing How Each Atom Forms Four Bonds with Its Nearest Neighbors.

c GeSi bats

Si dominates because it has a clean oxide interface:  $\text{SiO}_2$

# Bands arise from periodic structure of crystal

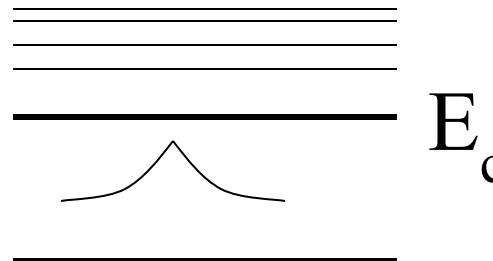
Wavefunctions of electron in a box



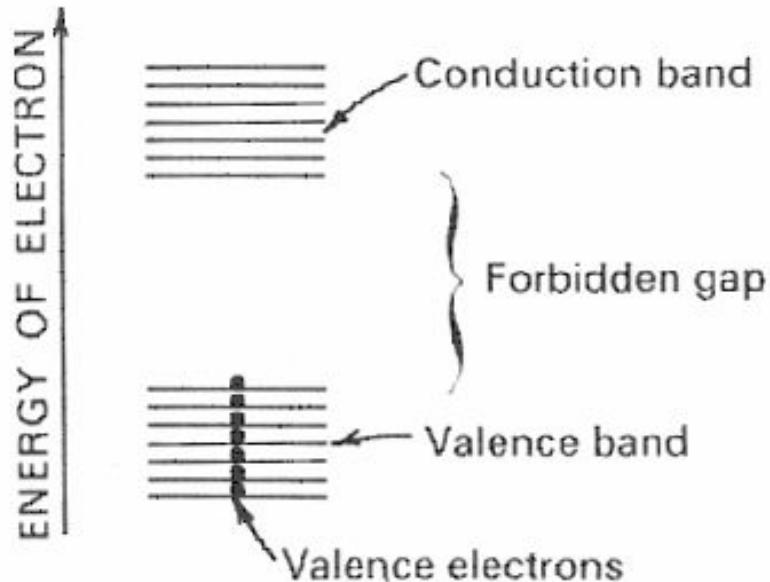
Energy levels

A crystal is like a periodic box

- Only wavefunctions with discrete nonzero energies act like free particles
- Wavefunctions at forbidden energies die off exponentially



# Schematic energy band representation for electrons in a solid

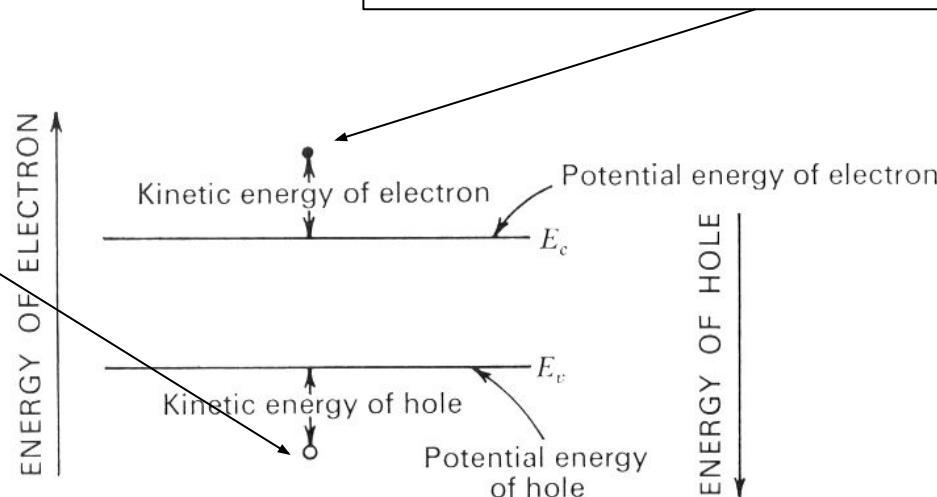


# Electrons and Holes

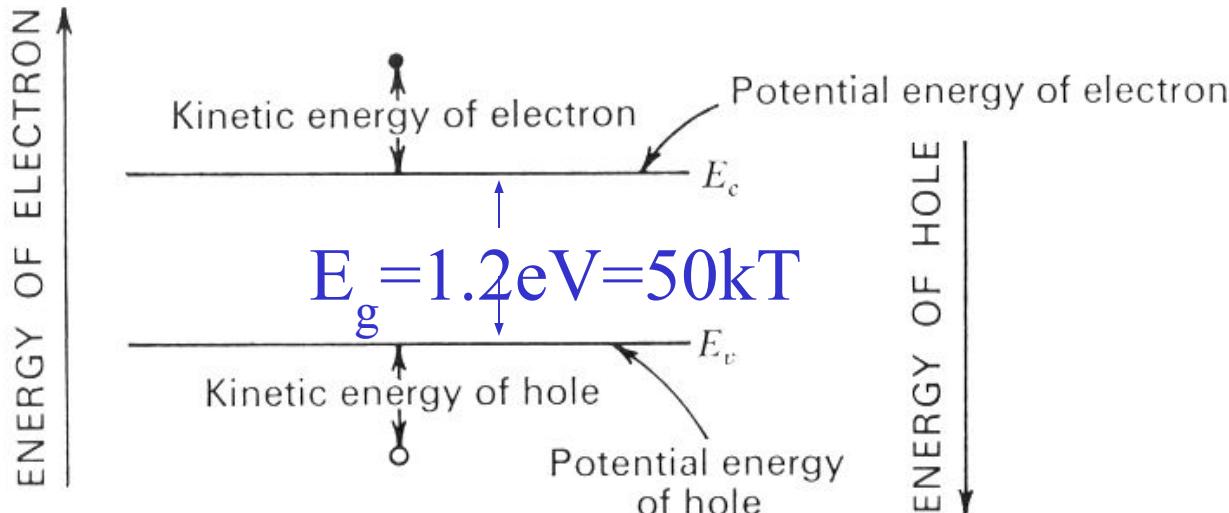
Holes are bubbles in the valence band

- The electrons move, but it is easier to talk about the vacancy (the hole) moving, just like it is easier to talk about a bubble moving than about the water around it moving
- Holes have positive charge and the **effective mass** in silicon is 2.5 times larger for a hole than for an electron

When electrons are broken loose from the lattice and enter the *conduction band*, they become *mobile*, and move almost as if in vacuum



# The meaning of energy in the band diagram



The *band gap* of silicon is about 1.2eV at room temperature

# The *Thermal Energy*

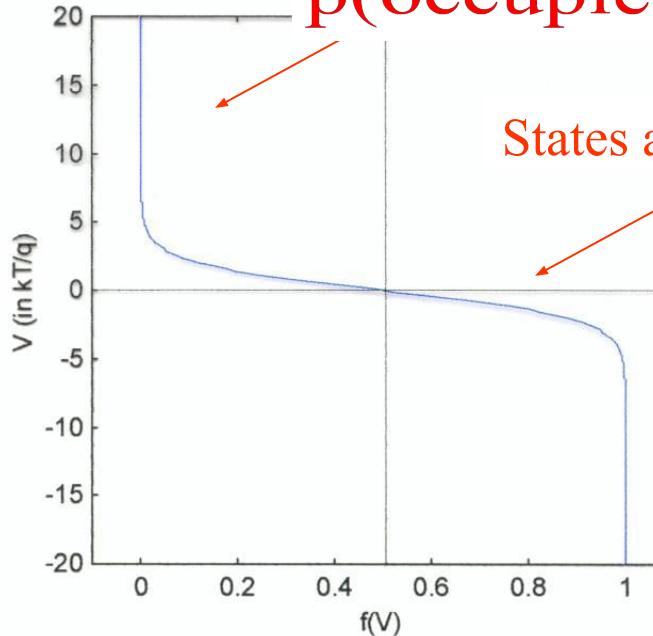
- Each *degree of freedom* of a system in thermal equilibrium has average energy  $kT/2$ , where  $k=1.38 \times 10^{-23}$  J/K is **Boltzmann's constant** and  $T$  is absolute temperature. I.e. at 300C,  $kT=4.1 \times 10^{-21}$  J
- The thermal voltage  $kT/q$  is the voltage a single charge falls through to pick up the thermal energy  $kT$
- $q$  is the **elementary charge**  $1.6 \times 10^{-19}$  C
- $U_T \equiv kT/q = 25\text{mV} = 1/40\text{V}$  at room temperature
- **$kT/q$  is the natural scale of voltage for electronic systems in thermal equilibrium**

# The Fermi-Dirac distribution

States above Fermi level are **occupied** with Boltzmann distribution

$$p(\text{occupied}) \approx e^{-(E-E_f)/kT}$$

Energy  
relative to  
Fermi level  
in  $kT$  units



States at the Fermi level are  $\frac{1}{2}$  occupied

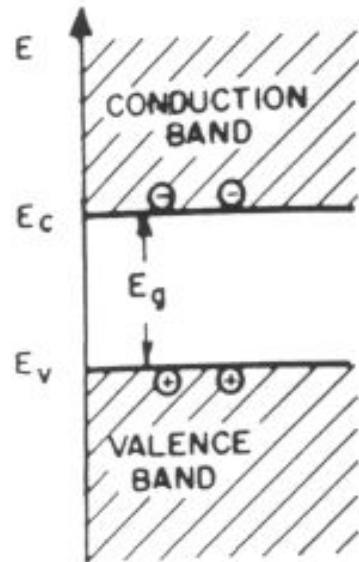
$E_f$

States below Fermi level  
are **unoccupied** with  
Boltzmann distribution

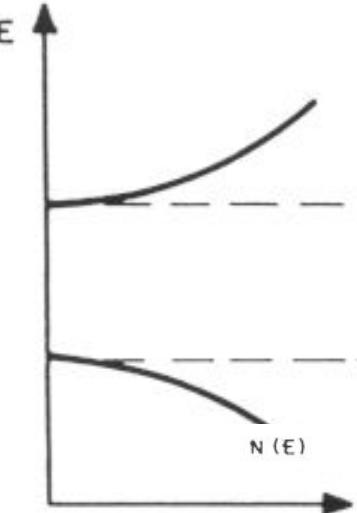
$$p(\text{unoccupied}) \approx e^{-(E_f-E)/kT}$$

Probability of occupation of a state

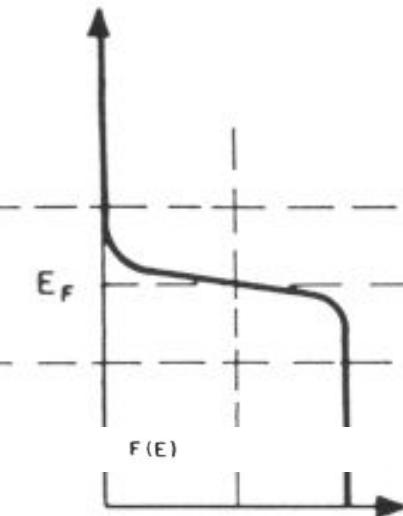
# An *intrinsic* (undoped) semiconductor



Band  
diagram

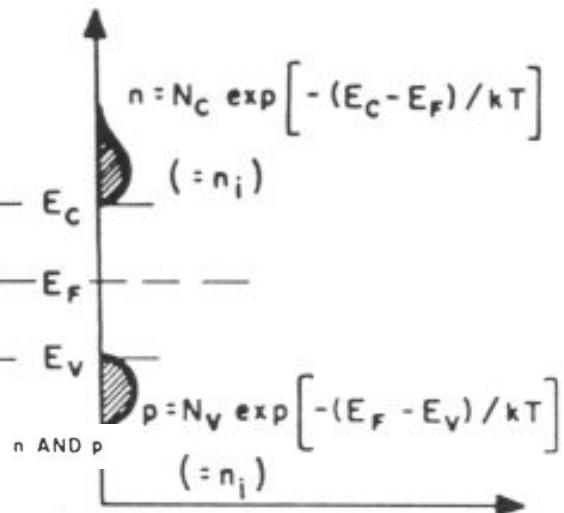


Density  
of states



(a)

Fermi-Dirac  
distribution



Carrier  
concentrations

# Donors and Acceptors in the periodic table

I	II	III	IV	V	VI	VII	Zero
H							He
Li	Be	(B)	C	N	O	F	Ne
Na	Mg	Al	Si	(P)	S	Cl	Ar
K	Zn	Ga	Ge	(As)	Se	Br	Kr
Rb	Cd	In	Sn	Sb	Te	I	Xe



Acceptors

Donors

1 missing electron

1 extra electron

# Doping levels

- Concentration (density) of Si is about  $10^{23}/\text{cm}^3$
- Doping can vary from about  $10^{15}/\text{cm}^3$  to  $10^{19}/\text{cm}^3$
- These doping levels still represent only a tiny fraction of the total atoms, from  $10^{-8}$  to  $10^{-4}$

# A donor atom in the silicon lattice

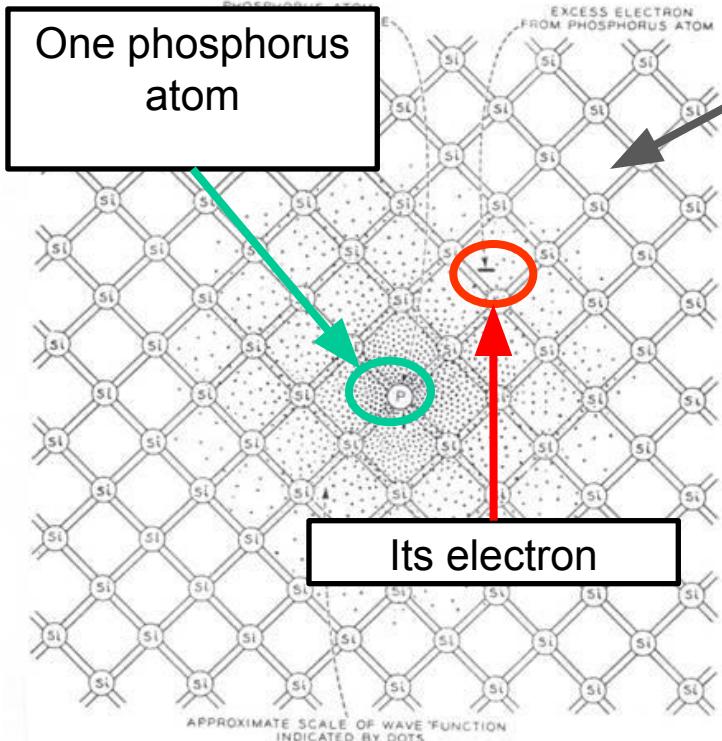


FIG. 1-14—Wave Function of Electron Bound to Phosphorous Atom in Silicon.

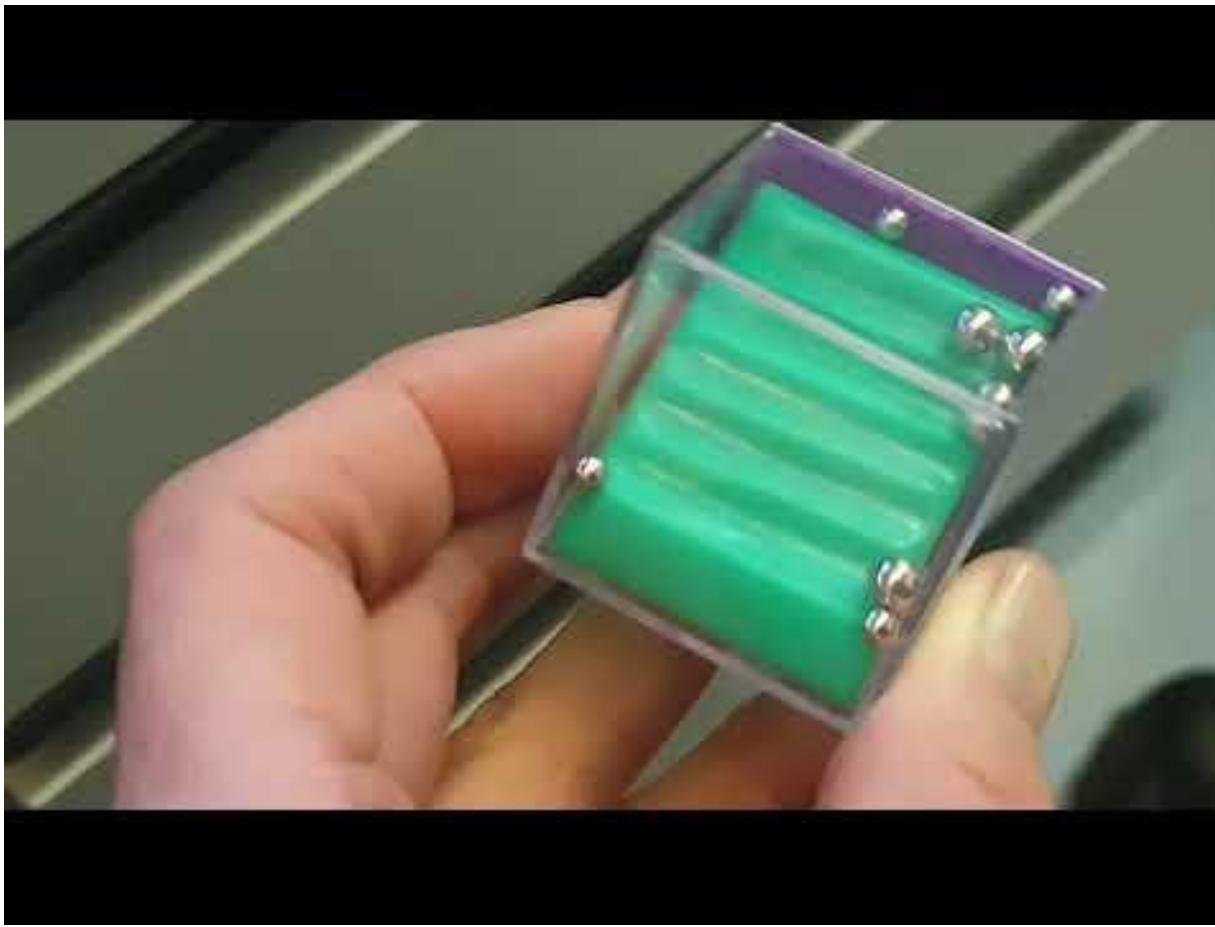
Binding energy of phosphorus donor electron is reduced from free atom binding energy (~0.5 eV) approximately by silicon *dielectric constant*

$$\epsilon_{Si} \approx 12\epsilon_0$$

$$E_{binding} \approx \frac{0.5eV}{12} \approx 0.05eV \approx 2kT$$

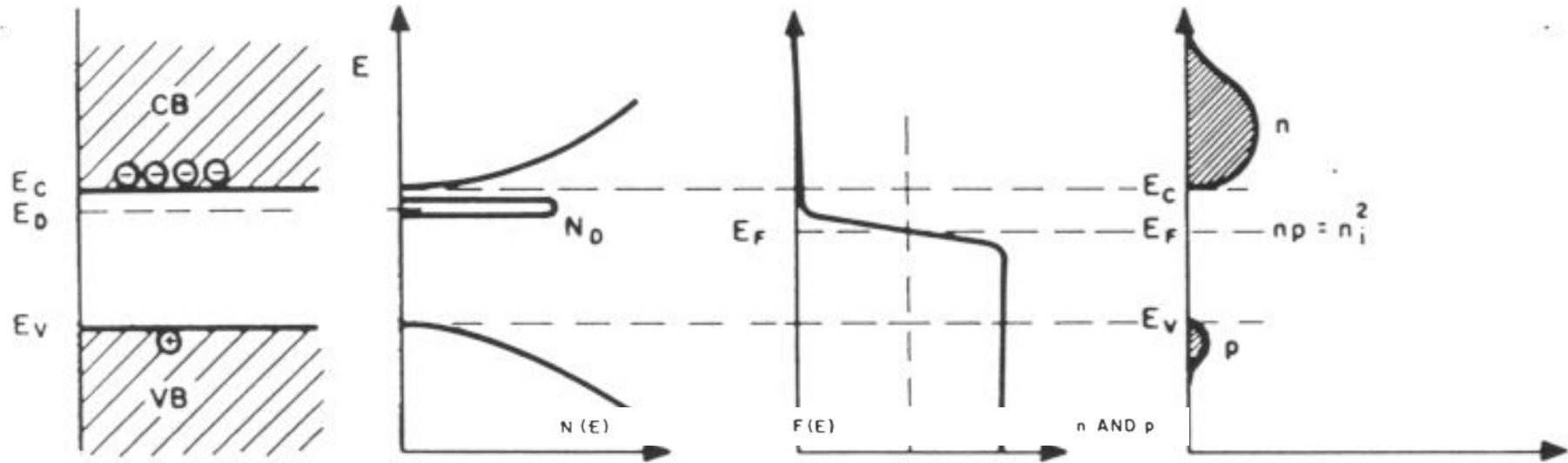
**So why does it donate a free electron?** It is still bound with twice the thermal energy.

**Answer:** There are many more ways (states) to be free than bound. Practically all donor electrons are *mobile electrons* at room temperature

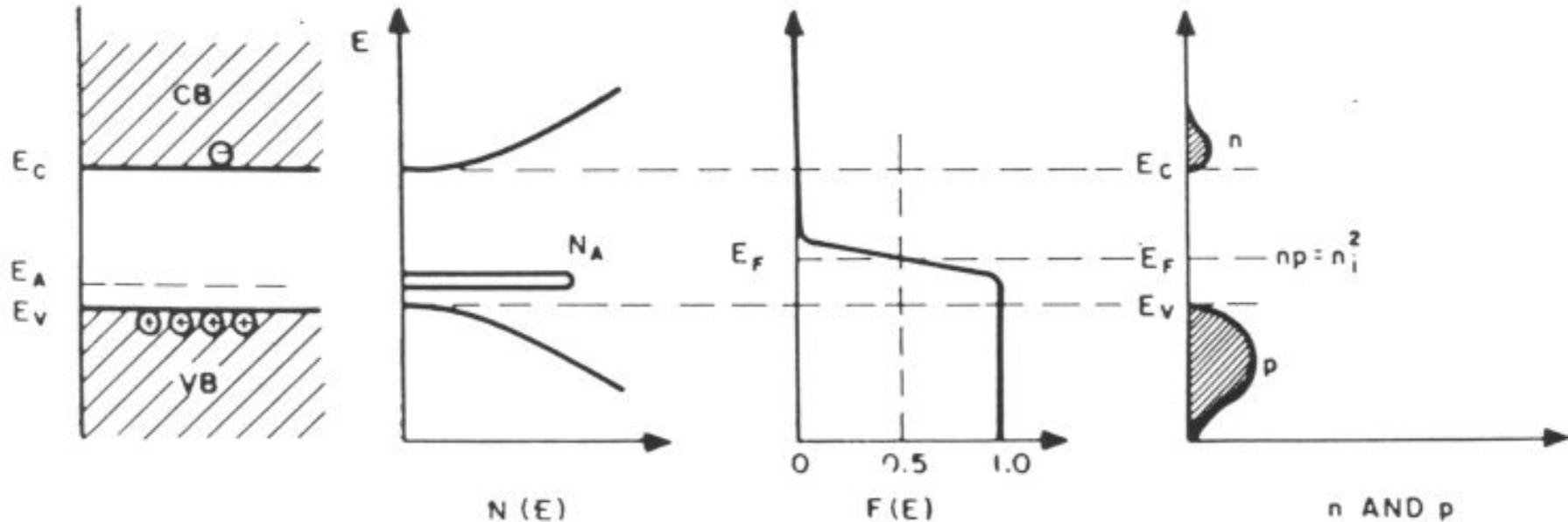


Ball “binding energy” is substantial, but there are so many other possible unbound states that it is very unlikely to be in the correct configuration

# An *n*-type semiconductor



# A *p*-type semiconductor



# *Law of mass action: $np=n_i^2$*

- In equilibrium, more holes means less electrons, and vice-versa.
- $n_i$  is the *intrinsic carrier density*
- At room temperature  $n_i$  is  $10^{10}/\text{cm}^3$ , or about  $1/10^{13}$  Si atoms.
- $n_i$  increases with temperature

# Electron transport

1. *Drift and Diffusion*
2. *Mobility*
3. The *Einstein relation*

# An electric field causes carriers to drift

Velocity

$$\overrightarrow{J} = qn\overrightarrow{v} = qn\mu(\xi) \quad \overrightarrow{\xi}$$

Current Flux

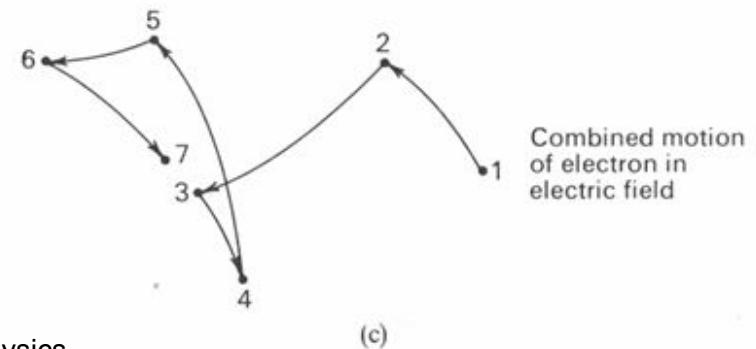
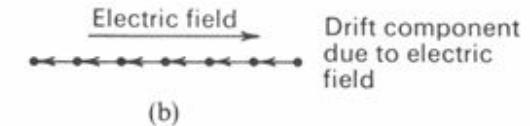
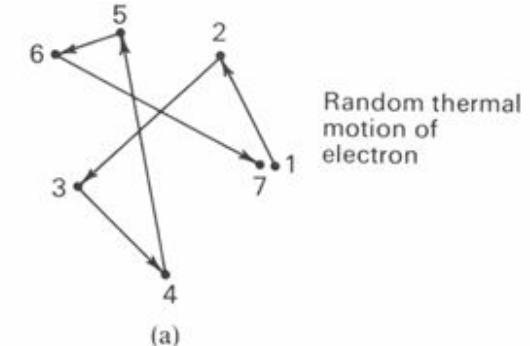
Electric field

**Mobility**

Charge density

$$\overrightarrow{J} \approx qn\mu \overrightarrow{\xi}$$

for  $\xi$  that causes velocities  
much less than the thermal velocity  
of  $\approx 100$  km/s



# Mobility is a function of electric field

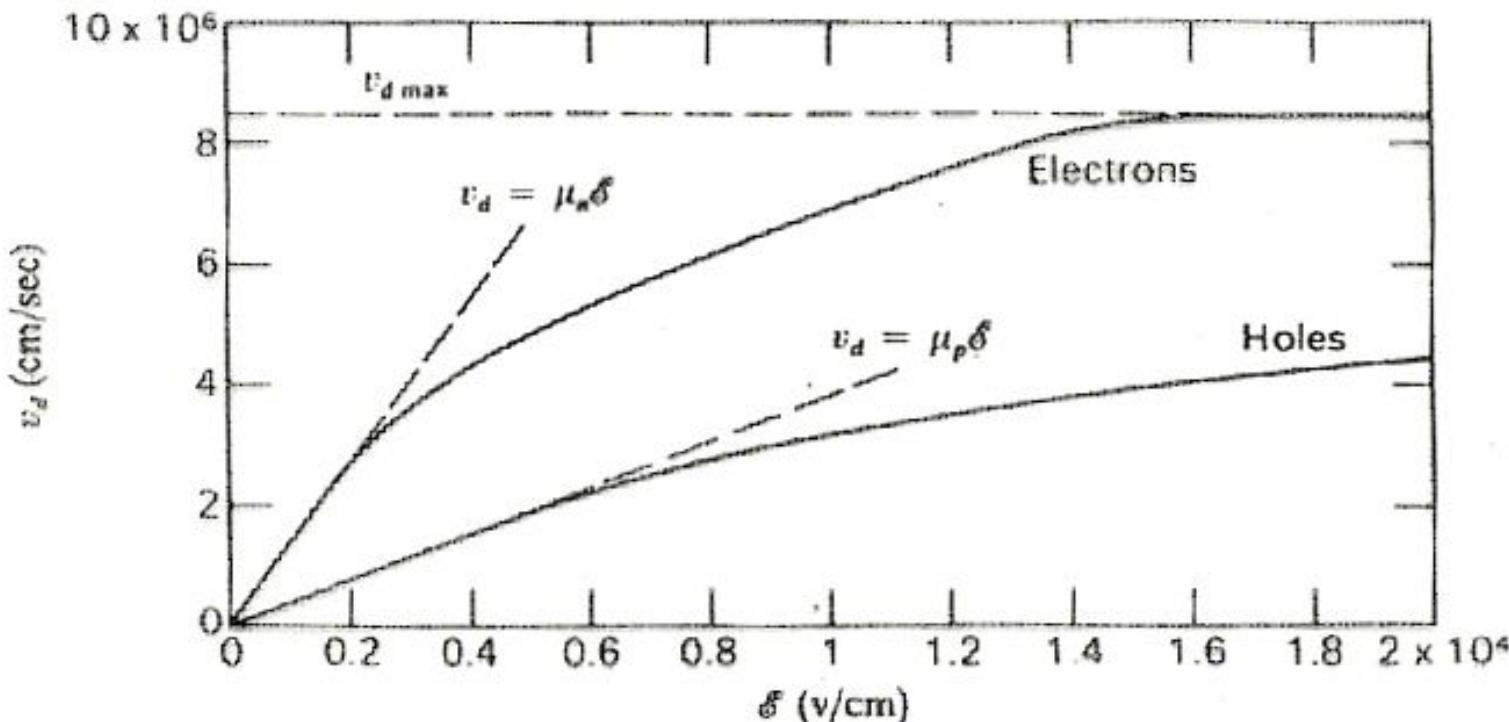
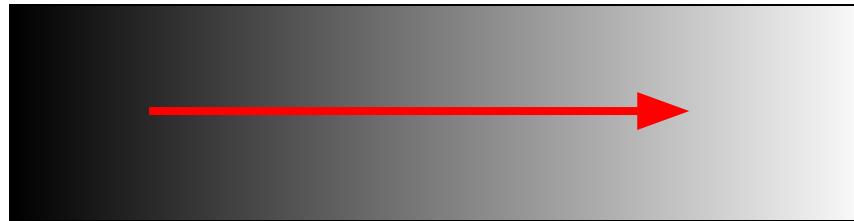


Fig. 4.10 Effect of electric field on the magnitude of the drift velocity of carriers in silicon.<sup>3</sup>

# A density gradient causes carriers to diffuse



## Diffusion current

$$\vec{J} = -Dq \nabla n$$

Current Flux

Diffusion constant

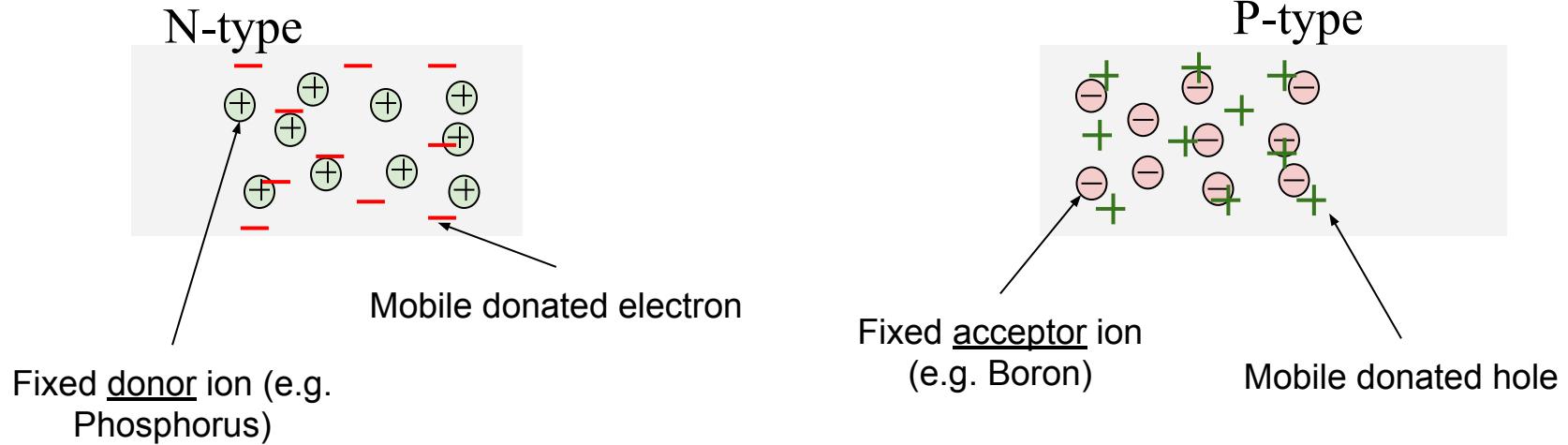
Spatial gradient of  
charge density

# Drift and diffusion are related by the *Einstein Relation*

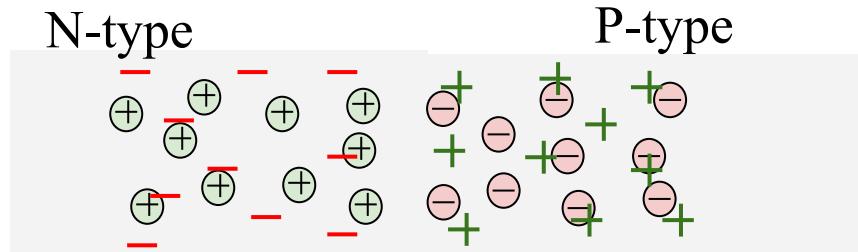
$$J_{\text{diffusion}} = -Dq\Delta n \quad J_{\text{drift}} = \mu q n \xi$$

$$D = \frac{kT}{q} \mu$$

# Charges, fields, and potentials in a PN junction



# What happens at a junction between P and N?



Lots of mobile electrons

Lots of mobile holes

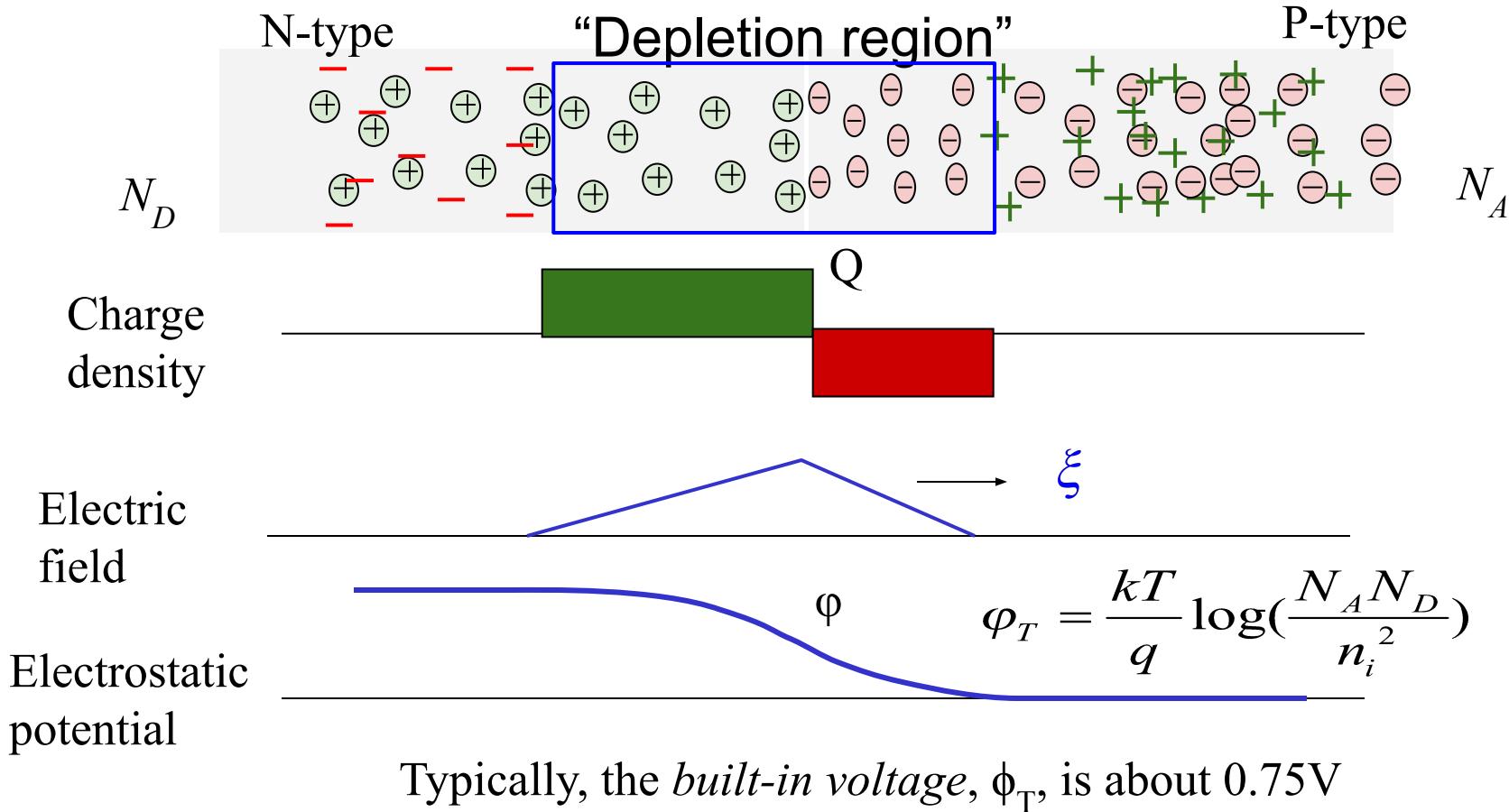
Electron density gradient:  
Electrons diffuse rightwards

Hole density gradient:  
Holes diffuse leftwards

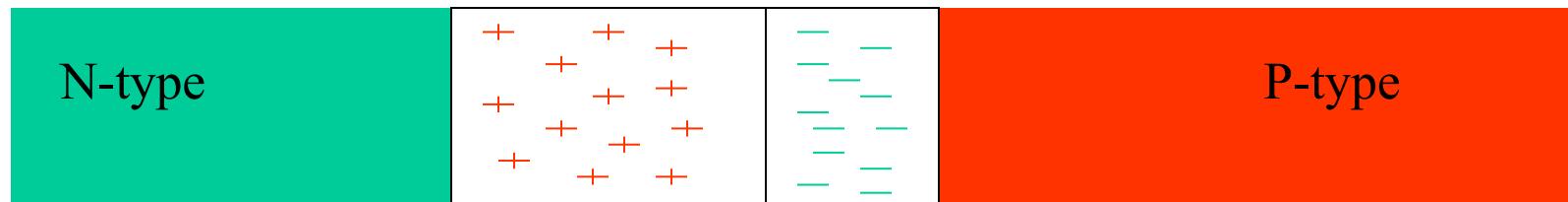
The charge separation builds up an electric field to pull the carries “back home”

In a PN junction with no applied voltage, drift and diffusion are balanced everywhere

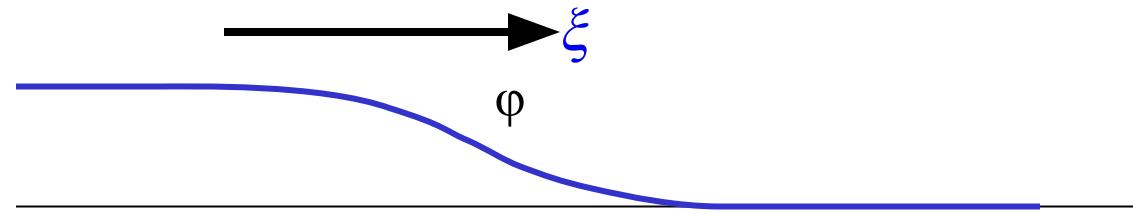
# Charges, fields, and potentials in a PN junction



# Electrostatic potentials in a PN junction



Electrostatic Potential:  
potential energy of  
**positive** charge



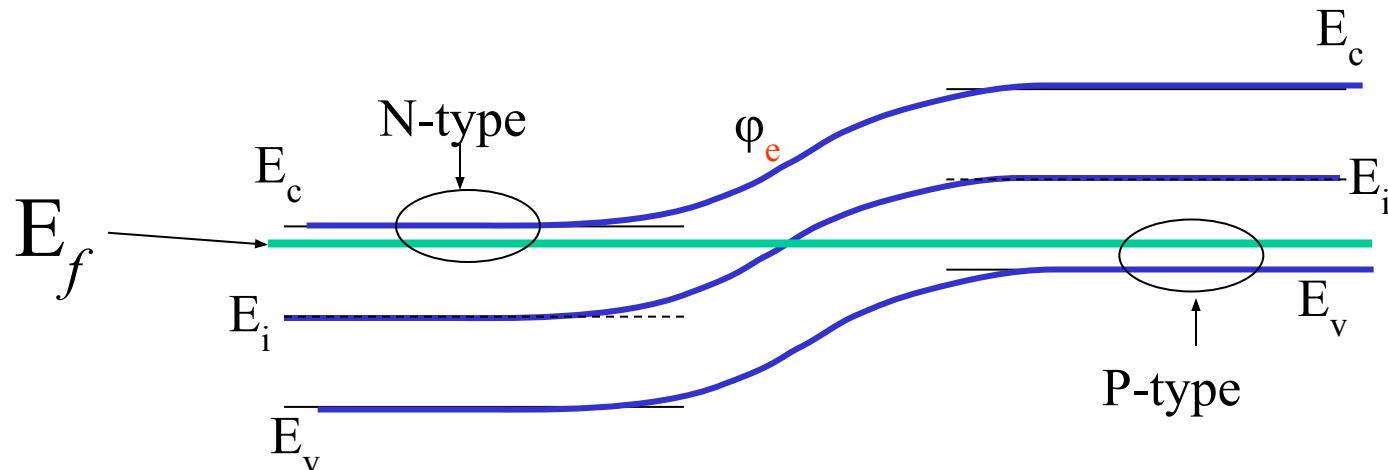
Potential energy of  
**negatively** charged  
electron



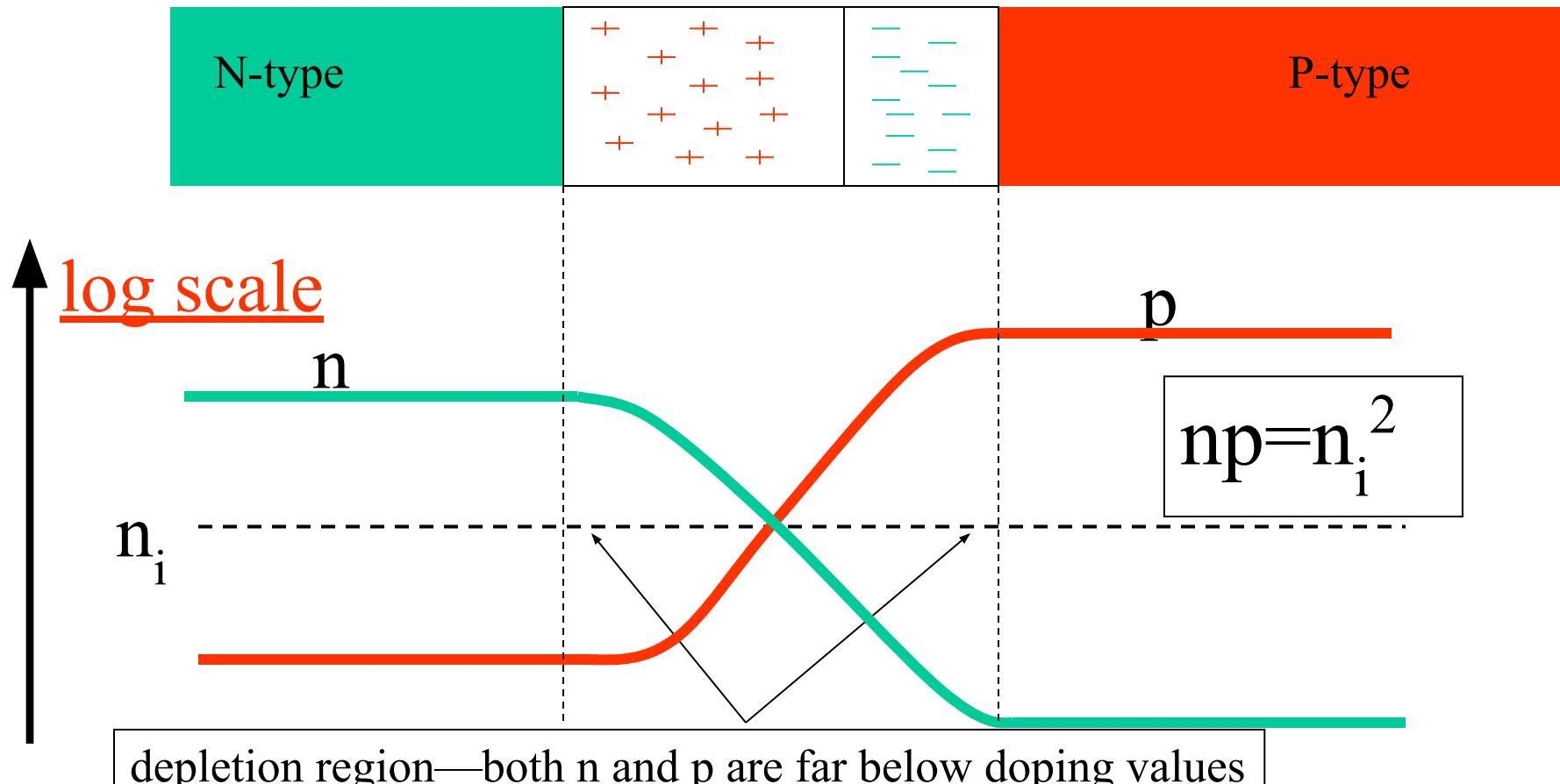
# Band structure of a PN junction



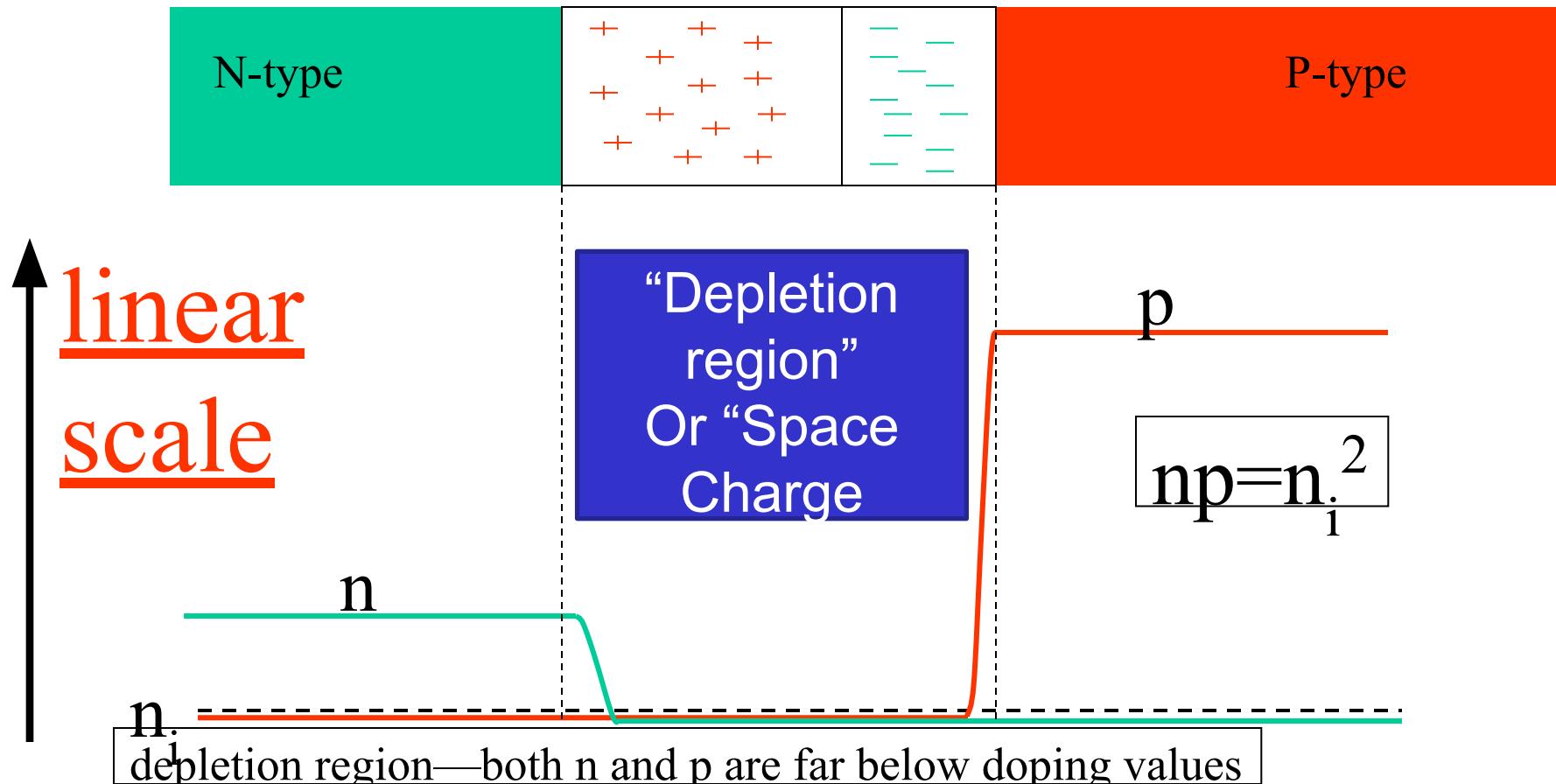
Remember electron energy is UP in a band diagram



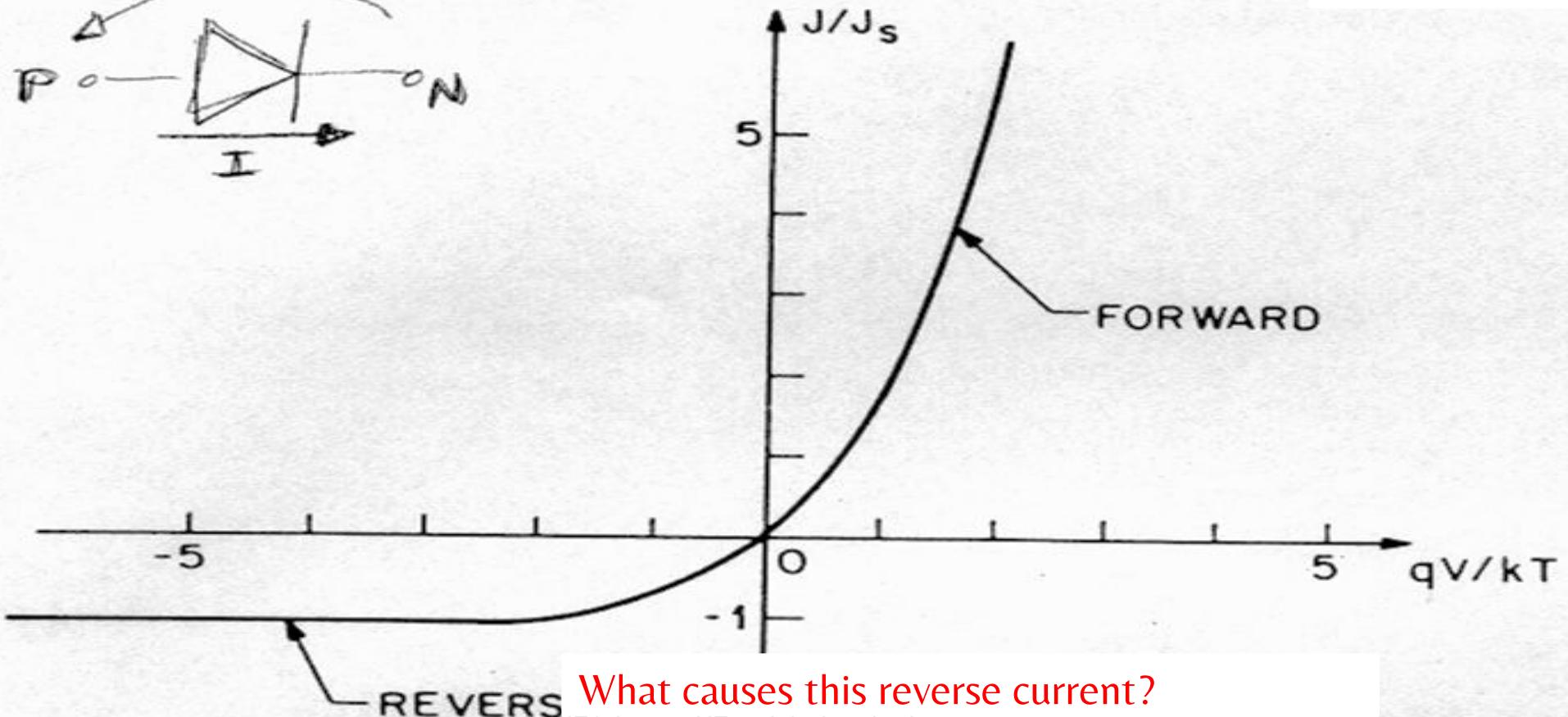
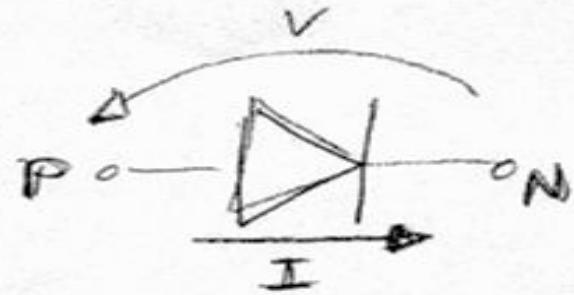
# Carrier densities in a PN junction



# Carrier densities in a PN junction

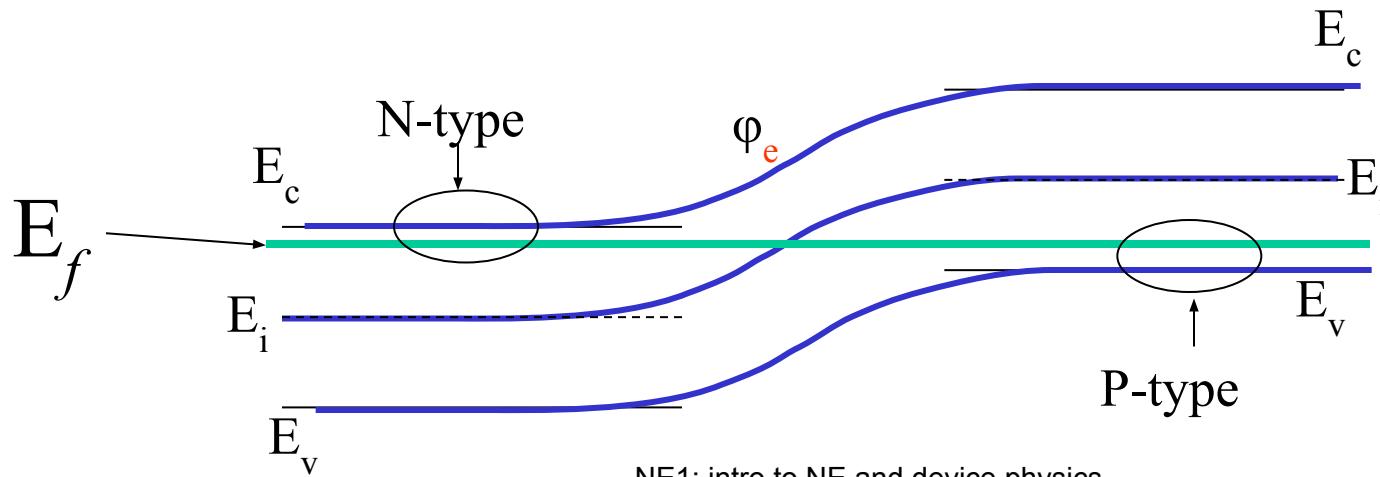
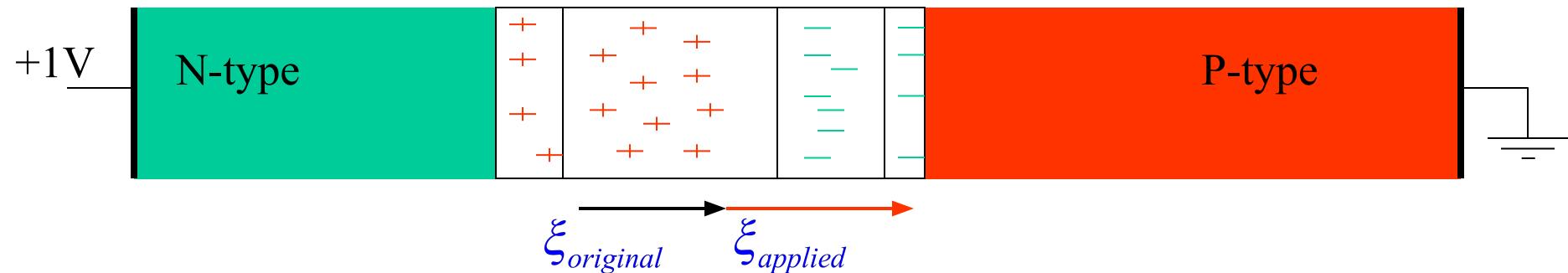


# I-V characteristics of a PN junction “rectifier”

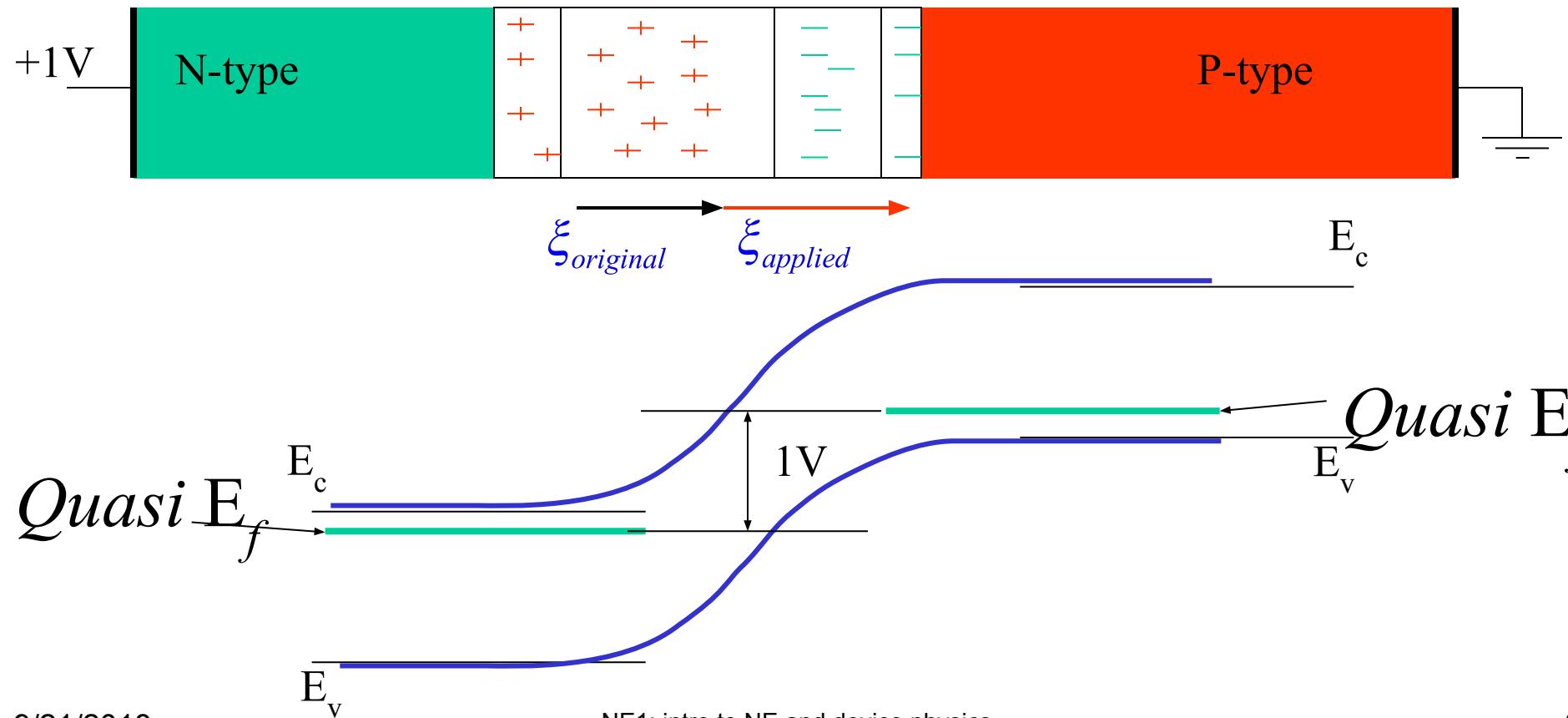


What causes this reverse current?

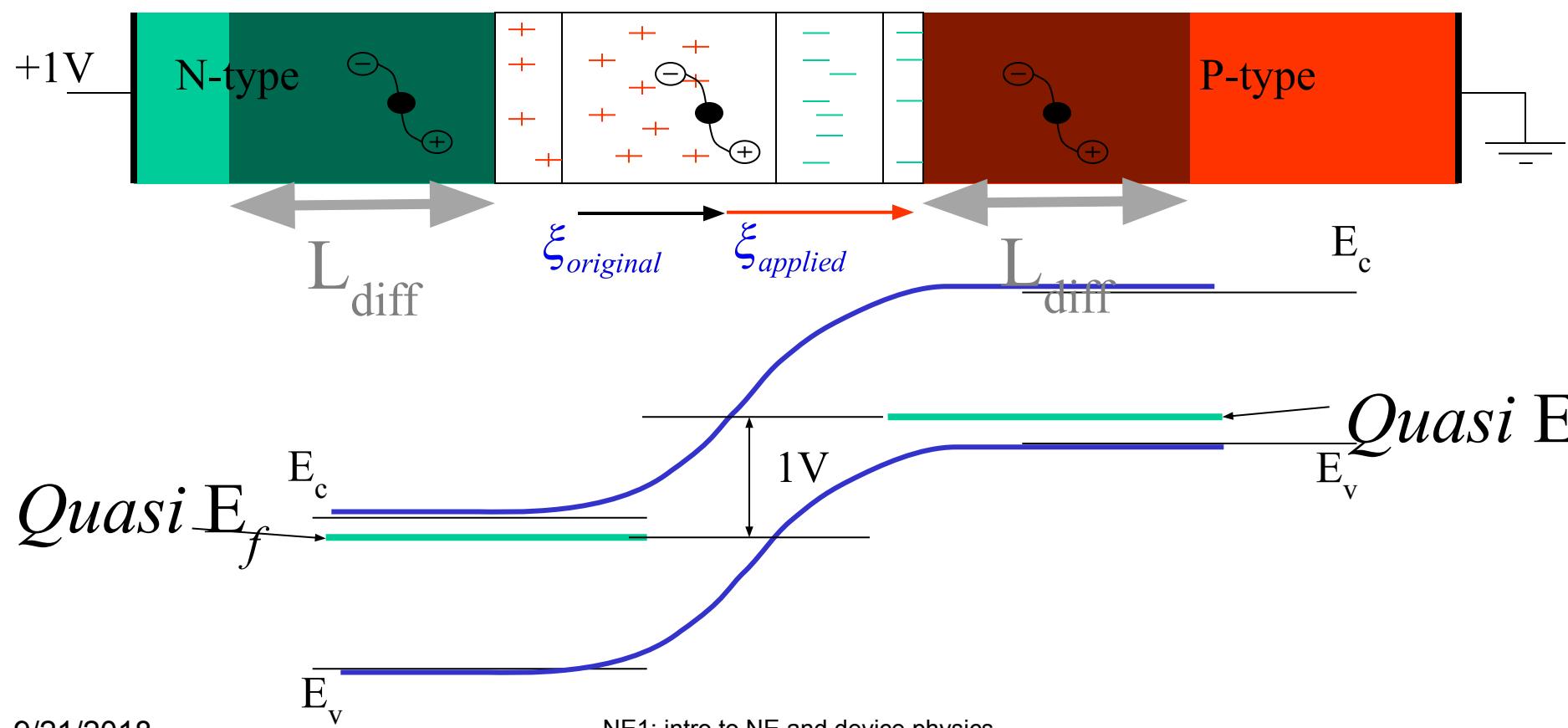
# A reverse-biased PN junction



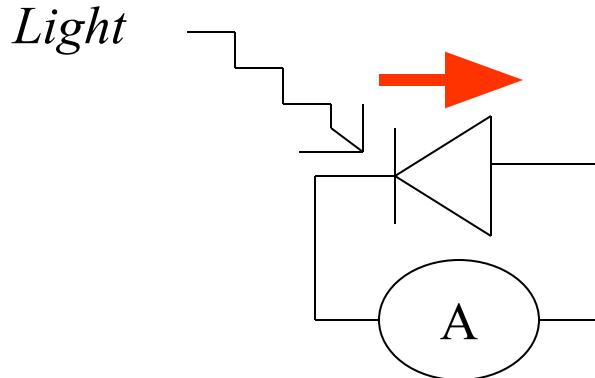
# A reverse-biased PN junction



# Reverse current comes from generated electron hole pairs in 3 regions

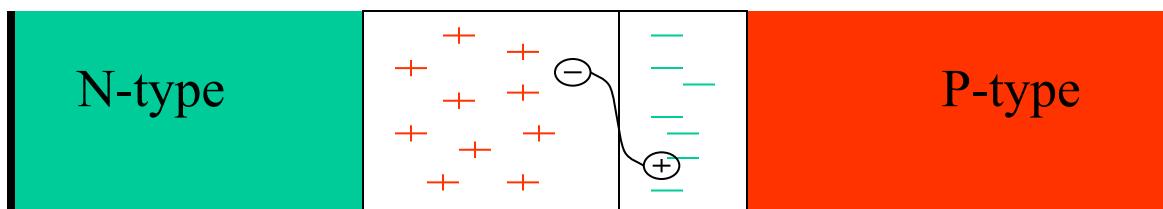


# Question



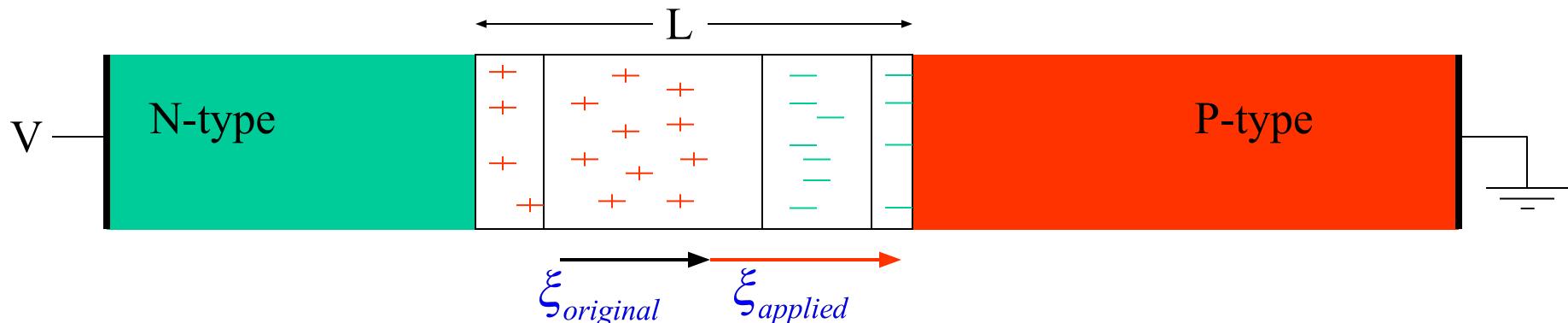
What happens when light shines on the junction?

Which way does current flow?



Answer: light tries to forward bias the junction.

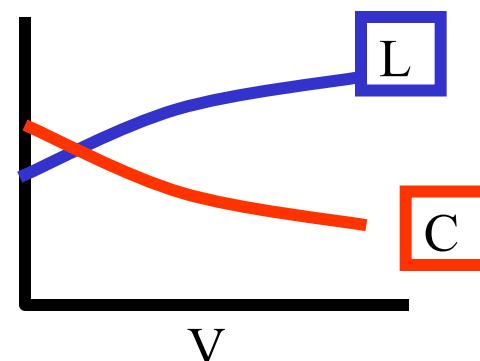
# What is capacitance of reverse-biased PN junction?



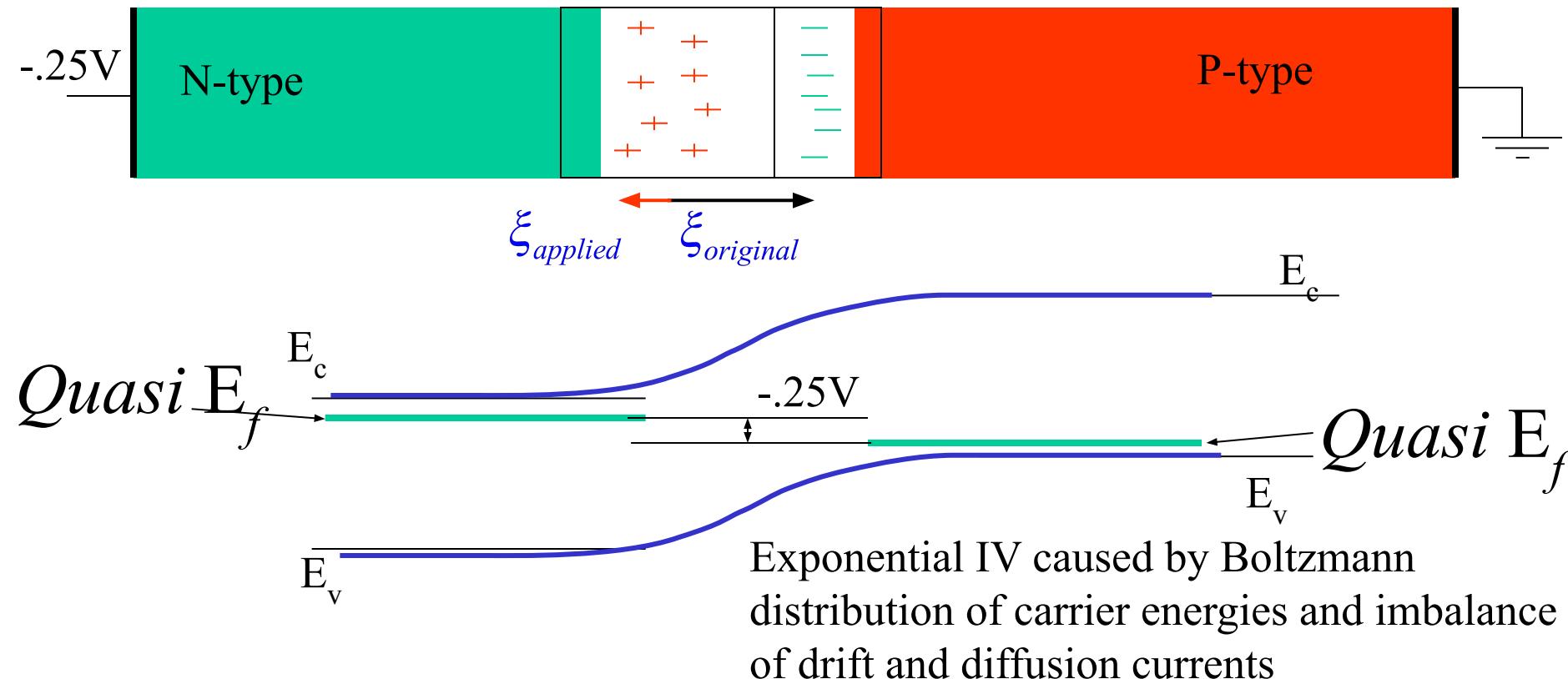
$$C = \epsilon_{Si} / L$$

As  $V$  increases,  $L$  increases.

So, as  $V$  increases,  $C$  decreases



# A forward-biased PN junction

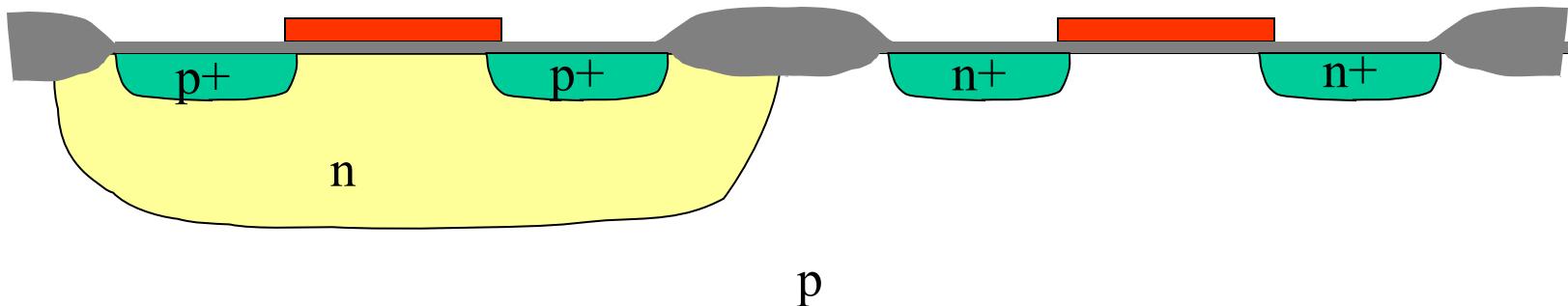


# What was covered

- Insulators, conductors, semiconductors
- Crystal structure of silicon
- Band structure (valence, conduction, and forbidden bands)
- Holes and electrons
- Mechanisms of charge transport (diffusion & drift)
- Doping with donors and acceptors
- Fermi-Dirac distribution
- Law of mass action ( $np=n_i^2$ )
- p-n junction
- Reverse biased junction and its capacitance in reverse bias

# Next week:

## Understanding how MOS transistors work in the subthreshold/weak inversion regime



# Properties of Materials (Si and SiO<sub>2</sub>)

TABLE 4.1 IMPORTANT PROPERTIES OF GERMANIUM, SILICON, GALLIUM ARSENIDE, AND OF SILICON DIOXIDE AT 27°C.

	Ge	Si	GaAs	SiO <sub>2</sub>
Atomic or molecular weight	72.60	28.09	144.63	60.08
Atoms or molecules/cm <sup>3</sup>	$4.42 \times 10^{22}$	$5.00 \times 10^{22}$	$2.21 \times 10^{22}$	$2.3 \times 10^{22}$
Crystal structure	Diamond, 8 atoms/unit cell	Diamond, 8 atoms/unit cell	Zinc-blende, 8 atoms/unit cell	Random network of SiO <sub>4</sub> tetrahedra. 50% covalent, 50% ionic bonding
Lattice constant (Å)	5.66	5.43	5.65	...
Density, $\rho$ (g/cm <sup>3</sup> )	5.32	2.33	5.32	2.27
Energy gap (eV)	0.67	1.11	1.40	~8
Effective density of states conduction band $N_c$ (cm <sup>-3</sup> ) valence band $N_v$ (cm <sup>-3</sup> )	$1.04 \times 10^{19}$ $6.0 \times 10^{18}$	$2.8 \times 10^{19}$ $1.04 \times 10^{19}$	$4.7 \times 10^{17}$ $7.0 \times 10^{18}$	...
Intrinsic carrier concentration $n_i$ (cm <sup>-3</sup> )	$2.4 \times 10^{13}$	$1.45 \times 10^{10}$	$\sim 9 \times 10^6$	...
Lattice (intrinsic) mobilities (cm <sup>2</sup> /v sec) electrons holes	3900 1900	1350 480	8600 250	Insulator; $\rho > 10^{16} \Omega\text{-cm}$ at 300°K.
Dielectric constant	16.3	11.7	12	3.9
Breakdown field (v/ $\mu$ )	~8	~30	~35	~600
Melting point (°C)	937	1415	1238	~1700

# A forward-biased PN junction

