Solutions to Jean-Pierre Serre's
Linear Representations of Finite Groups

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ABSTRACT. This document contains solutions to the exercises of J-P. Serre's *Linear Representations of Finite Groups*.

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