

Solutions to Walter Rudin's
Functional Analysis

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ABSTRACT. This document contains solutions to the exercises of Walter Rudin's *Functional Analysis*.

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