

Solutions to J. Peter May's
A Concise Course in Algebraic Topology

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ABSTRACT. This document contains solutions to the problems of J. Peter May's *A Concise Course in Algebraic Topology*.

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