Correspondance analysis (CA) with FactoMineR (Nobel prize dataset)

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Import data

Upload the Nobel prize dataset on your computer.

```
Nobel <- read.table("data_CA_NobelPrize_withMaths.csv", header=TRUE, sep=";", row.names=1, check.names=FALSE)
```

summary(Nobel)

```
##
     Chemistry
                 Economic science Literature
                                                 Medicine
   Min. : 1.00
##
                 Min. : 0.00
                                Min. : 0.00
                                              Min. : 2.00
                 1st Qu.: 1.00 1st Qu.: 5.00
   1st Qu.: 4.00
                                              1st Qu.: 4.00
## Median : 8.00
                 Median: 3.00
                                Median : 7.00
                                              Median: 9.00
## Mean :22.46
                 Mean :10.38
                                Mean :12.38
                                              Mean : 26.69
                 3rd Qu.: 6.00
## 3rd Qu.:24.00
                                3rd Qu.:10.00
                                              3rd Qu.: 26.00
## Max.
        :94.00
                Max. :47.00
                                Max. :79.00
                                              Max. :110.00
##
      Peace
                   Physics
                                Mathematics
## Min. : 0.00 Min. : 2.00
                                Min. : 1.000
## 1st Qu.: 1.00 1st Qu.: 5.00
                                1st Qu.: 1.000
                 Median : 11.00
## Median : 8.00
                                Median : 4.000
## Mean
        :11.62
                 Mean : 26.54
                                     : 7.846
                                Mean
                 3rd Qu.: 24.00
## 3rd Qu.:16.00
                                3rd Qu.:11.000
## Max. :51.00
                 Max. :103.00
                                Max. :34.000
```

Loading FactoMineR

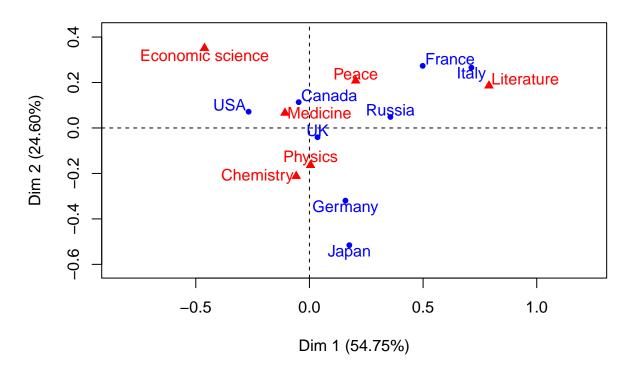
```
library(FactoMineR)
```

Correspondence Analysis

Active variables are the G8 countries and the Nobel prizes.

```
res.ca=CA(Nobel[1:8,1:6])
```

CA factor map



Outputs can be summarized with the function ${\tt summary}.$

```
summary(res.ca)
```

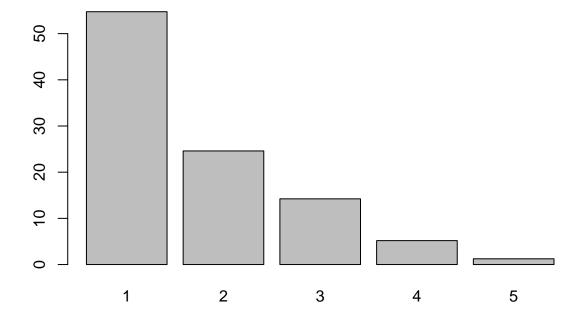
```
##
## Call:
## CA(X = Nobel[1:8, 1:6])
## The chi square of independence between the two variables is equal to 86.75919 (p-value = 2.76733e-0
##
## Eigenvalues
##
                          Dim.1
                                   Dim.2
                                           Dim.3
                                                    Dim.4
                                                            Dim.5
## Variance
                           0.083
                                   0.037
                                           0.022
                                                    0.008
                                                            0.002
## % of var.
                          54.748
                                  24.600
                                          14.227
                                                    5.180
                                                            1.245
                                  79.348
                                                   98.755 100.000
## Cumulative % of var.
                         54.748
                                          93.575
##
## Rows
##
                       Iner*1000
                                    Dim.1
                                             ctr
                                                    cos2
                                                            Dim.2
                                                                      ctr
                                                                            cos2
## Canada
                           2.040 | -0.047
                                           0.085
                                                   0.035
                                                            0.113
                                                                   1.086
                                                                           0.199
## France
                          33.080 |
                                    0.498 27.709
                                                   0.698 |
                                                            0.273 18.536
                                                                           0.210
## Germany
                          19.066
                                    0.158
                                           4.226
                                                   0.185 |
                                                           -0.320 38.296
## Italy
                          25.908 |
                                    0.713 20.316
                                                   0.653 |
                                                            0.265
                                                                   6.261
                                                                           0.090
## Japan
                          15.089 |
                                    0.176
                                           1.492
                                                   0.082 | -0.516 28.653
                                                                           0.711
## Russia
                          14.432 |
                                    0.356
                                           7.210
                                                   0.416 |
                                                            0.049
                                                                   0.298
                                                                           0.008
## UK
                          7.354 | 0.036
                                           0.249
                                                  0.028 | -0.041
                                                                   0.727
                                                                           0.037
## USA
                          35.239 | -0.267 38.713 0.915 |
                                                            0.071
                                                                   6.143
                                                                          0.065
```

```
##
                      Dim.3
                               ctr
                                     cos2
## Canada
                   0.112 1.834
                                    0.195 l
## France
                   | -0.155 10.375
                                    0.068 |
                   | -0.061 2.431
## Germany
                                    0.028
## Italy
                      0.282 12.251
                                    0.102 |
## Japan
                      0.244 11.089
                                    0.159 |
## Russia
                   0.355 27.589
                                    0.414 l
## UK
                   | -0.205 31.534
                                    0.929 |
## USA
                   | 0.037 2.897 0.018 |
##
## Columns
##
                     Iner*1000
                                  Dim.1
                                                 cos2
                                                         Dim.2
                                           ctr
                                                                  ctr
                                                                        cos2
                        13.469 | -0.058 0.862
## Chemistry
                                                0.053 | -0.212 25.471
                                                                       0.708
## Economic science |
                        38.902 | -0.462 26.916
                                                0.577 |
                                                         0.351 34.675
                                                                       0.334
## Literature
                        58.438 | 0.790 64.353
                                                0.918 |
                                                         0.186
                                                                7.942
                                                                       0.051
## Medicine
                        10.429 | -0.108
                                         3.418
                                                0.273 |
                                                         0.066
                                                                2.874
                                                                       0.103
## Peace
                        16.213 | 0.203 4.443
                                                0.228 | 0.208 10.316
                                                                      0.238
## Physics
                        14.758 | 0.005 0.008
                                                0.000 | -0.164 18.723 0.475
##
                      Dim.3
                               ctr
                                     cos2
## Chemistry
                   | -0.107 11.181
                                    0.180 |
## Economic science | 0.174 14.649
                                    0.082 |
## Literature
                   0.117 5.478
## Medicine
                   | -0.115 15.069
                                    0.313 |
## Peace
                   | -0.226 21.169
                                    0.283 l
## Physics
                   | 0.164 32.455 0.476 |
```

Bar chart of eigenvalues

```
barplot(res.ca$eig[,2],main="Eigenvalues", names.arg=1:nrow(res.ca$eig))
```

Eigenvalues



CA with supplementary elements

```
# Adding the Fields medal as supplementary element
res.ca=CA(Nobel[1:8,], col.sup=7)
```

CA factor map

