Disturbance Estimation
And Cancellation
for
Linear Uncertain Systems

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Summary

disturbance without a priori knowledge in order to cancel their effect on system of the most important problems is that of robustness of the controlled system, from the view point of the theory of control? In this work, it is assumed that one motivation of this study comes from the following questions. Is it really possible application, namely a smart structural system. More specifically, the primary

to estimate and cancel out any bounded disturbance and/or uncertainty. behaviour. This study provides a method, including its theoretical foundation, and it is supposed that one of the solution would be to estimate uncertainty and to use smart structural system in a practical situation? What is the problem This thesis was born on the boundary of the theory of control and a particular

external disturbances. Thus, this type of system model would include many In addition, such system models would suffer from parametric uncertainty and models will inevitably generate uncertainty, representing unmodelled dynamics. and, hence, a high order finite dimensional model is obtained. Such approximate In practice, however, a model is obtained by using the Finite Element Method, infinite dimensional models if it were modelled by ordinary differential equations. to the host materials. The modelling of smart structural systems gives rise to host materials, sensing and actuating layers, which are attached or embedded structural systems cannot escape from this problem. Such systems consist of mechanical or structural system, contain some form of uncertainty. Even smart of the controlled system. It is known that almost all physical systems, such as One of the most important problems in control systems is the robustness

is the case, what can be said about the robustness of controlled system without even impossible, to obtain such a priori knowledge of any disturbance. It this deterministically. However, for smart structural systems, it may be difficult, or per bound to uncertainty and disturbance, and robust controllers are determined tor the robust control problem. The majority of this work assumes a known up-In past decades, much research has been done using a deterministic approach types of uncertainties.

be found in this thesis. a priori knowledge of any disturbance? Part of the answer to this question can

can be designed based on the information from the known nominal model only the advantage that, if further design objectives are to be realized, the controls can then be used to cancel the effect of the disturbance in the system. This has novel and the adaptive control algorithm is easy to implement. This information mate the bounded disturbance. The design of the adaptive control algorithm is main contribution is that an adaptive feedback control law is designed to estiand/or disturbance is known to be bounded, but its bound is unknown. The This thesis considers a linear uncertain system in which the uncertainty

and not on the model with uncertainty.

are provided. disturbances. In Chapter 4, conclusion remarks and suggestions for future works it is demonstrated that parameter variations can be extracted from estimated that the method can be used only by outputs of a system. At last, in Section 3.6, disturbance by the method proposed. In Section 3.5, the method is extended so it is shown that under appropriate assumptions, it is possible to treat residual and unmodelled dynamics is discussed. In the following section, Section 3.4, a controlled system is presented. In Section 3.3, treatment of input uncertainty presented. In Section 3.2, an adaptive algorithm which guarantees robustness of of Chapter 2, some applications of the method of disturbance estimation are linear systems, and multi-input linear systems. In Chapter 3, based on the works examined are second-order single-input linear systems, n^{th} order single-input lemmas, theorem, and simulation examples are provided. The class of systems required for analysis. Then, for each class of systems, an adaptive algorithm, of the problem is provided. It is followed by some preliminary works which are I, the method of disturbance estimation is introduced. Firstly, the statement robust control. In Chapter 2, motivated by the limitation discussed at Chapter of that chapter, it is implied that there is some limitation of that approach of of systems and deterministic approach of robust control are recalled. At the end This thesis is organized as follows. In Chapter 1, firstly, concept of stability

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Chapter 4

Conclusions and further research

4.1 Concluding remarks

As it is shown in previous chapters, in this study, the following topics are investigated.

- I. For both single-input and multi-input systems, estimation and cancellation of bounded disturbance/uncertainty can be performed without a priori knowledge of bounded disturbance/uncertainty (see Theorem 3, 4, 5, and related remarks).
- 2. Estimation and cancellation can be achieved, even in the presence of residual uncertainty/disturbance under appropriate conditions (see Section 3.4).
- 3. Using the disturbance estimation method, a tracking controller can be designed with respect to the nominal model (see Theorem 7).
- 4. Estimation and cancellation of unknown bounded disturbance/uncertainty can, also, be achieved by using only output measurement, even in the presence of sensor noise (see Section 3.5).
- 5. For both the stabilization and tracking problems, the system to be controlled is robust against parametric uncertainty, input uncertainty, unmodelled dynamics, external disturbance and/or sensor noise using the disturbance estimation/cancellation method (see Theorem 7, 8, and Section 3.5.3).
- 6. The parameter variations for the nominal model can be estimated from the estimated disturbance under certain assumptions (see Section 3.6).

In addition, numerical simulations are presented to demonstrate the methods developed.

4.2 Recommendations for further work

Topics which are not studied, but are suggested for further work, are listed as follows.

- 1. Implementation of the methods in some practical application.
- 2. Treatment of the case when there are input constraints.

The author believes that theory is enhanced as a result of interaction with various applications. Although the primary motivation of this study comes from one specific area of application and the assumptions developed are constructed so that these assumptions are realistic in the specific practical situation, it is uncertain what kind of problems exist when the theory is implemented for applications. The author believes that almost exact estimation of such uncertainty plications. Thus, to make clear and resolve such problems, it is recommended that the methods to make clear and resolve such problems, it is recommended that the methods be implemented in a number of applications.

In relation to Treatment of input constraint, improvements of the adaptive algorithms and a better understanding of the nominal model and modelling is encouraged. The method proposed gives an engineering solution for the worst case situation regarding uncertainty and disturbance, as well as control of a nonlinear and time-varying system, by cancelling out their effect. However, due to input constraints, there is a limit on the amount of estimation error of uncertainty and uncertainty that can be tolerated as modelling errors. Thus, improvements and uncertainty that can be tolerated as modelling errors. Thus, improvements of the adaptive algorithms and a better understanding of modelling and the

Sonstraines, where is a mare on the amount of cashinana crious and uncertainty that can be tolerated as modelling errors. Thus, improvements of the adaptive algorithms and a better understanding of modelling and the characteristics of the nominal model, which are fundamental characteristics of nonlinear system and time-varying system, are required.

Since the methods developed do not require any a priori knowledge of dissince the methods developed do not require any a priori knowledge of dissince the methods.

turbance and the methods can be applied using only output measurement, the methods will be relatively easy to implement in a practical situation. The author believes that the method proposed will contribute to the development of bigh parformance dealings.

high performance/reliable systems.

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