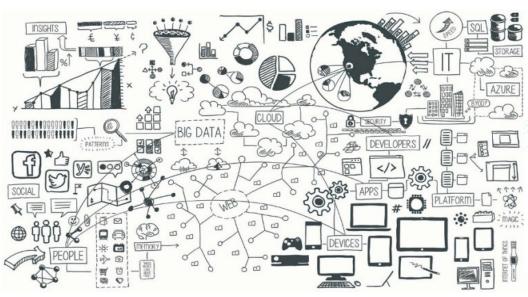
Data Mining (Minería de Datos)

Técnicas de Segmentación: Clustering





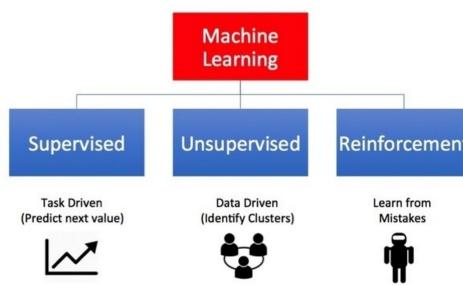
Sixto Herrera Joaquín Bedia Grupo de Meteorología Univ. de Cantabria – CSIC MACC / IFCA



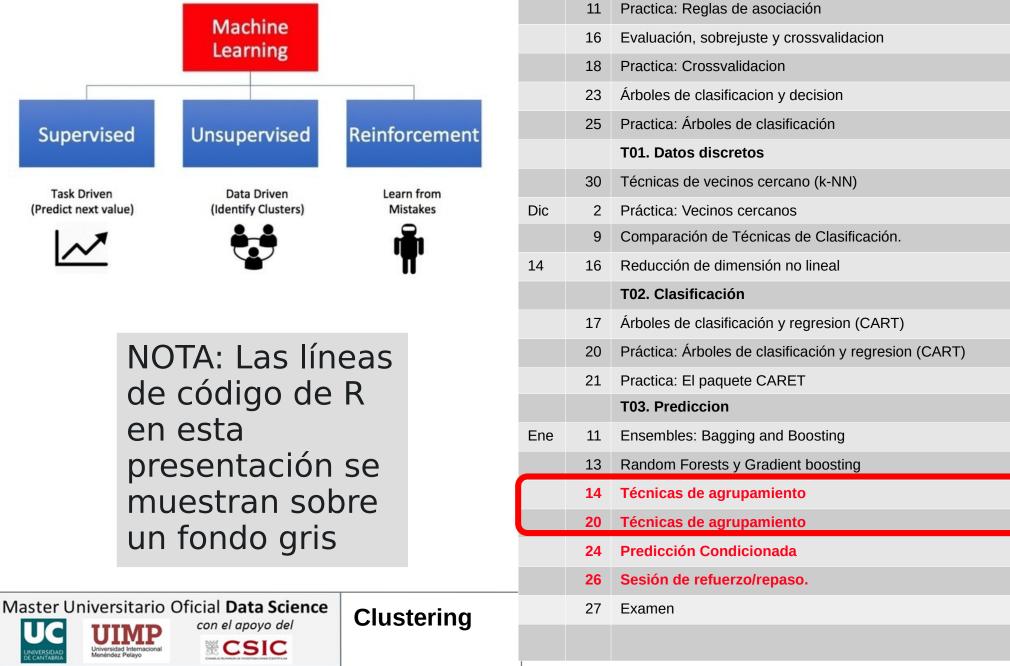




Types of Machine Learning



NOTA: Las líneas de código de R en esta presentación se muestran sobre un fondo gris



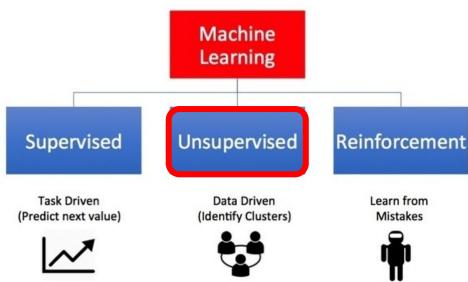
Nov

Presentación, introducción y perspectiva histórica

Reglas de asociación

Paradigmas, problemas canonicos y data challenges

Types of Machine Learning



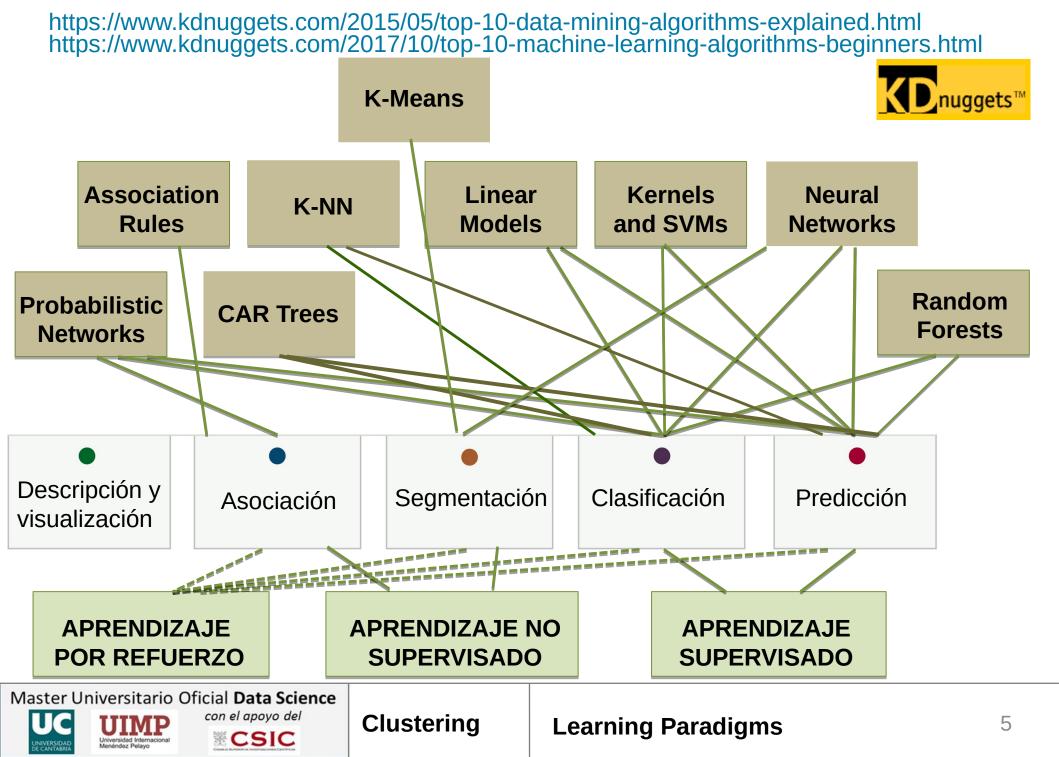
NOTA: Las líneas de código de R en esta presentación se muestran sobre un fondo gris

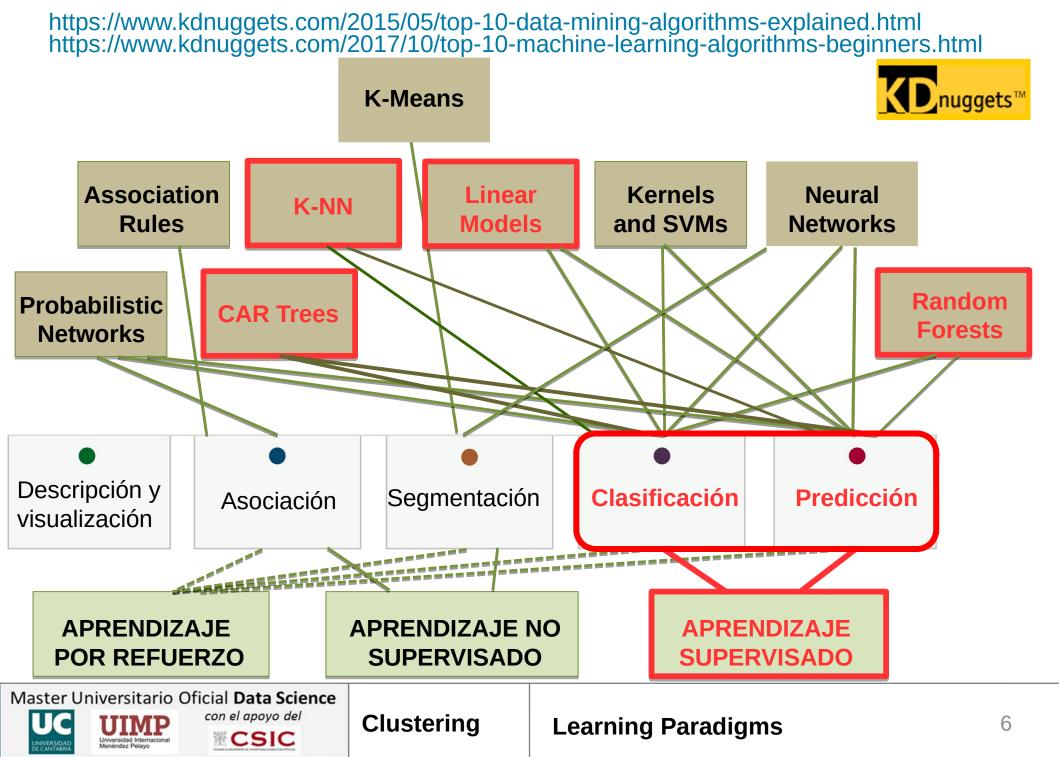


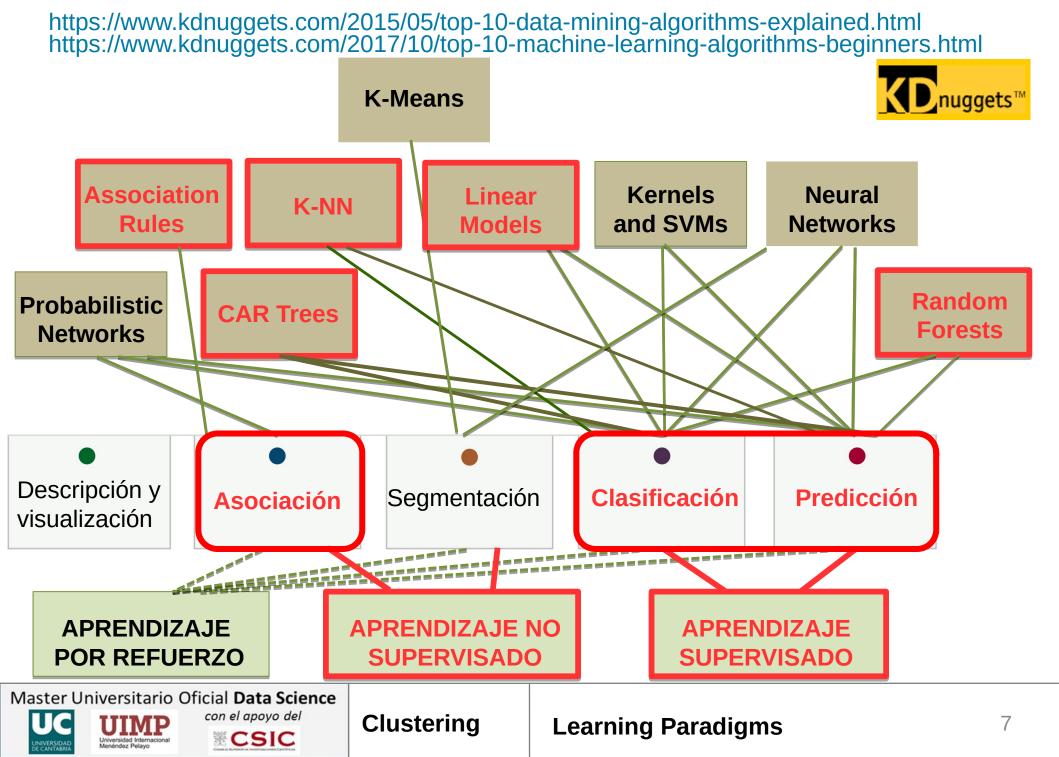
Master Universitario Oficial **Data Science**

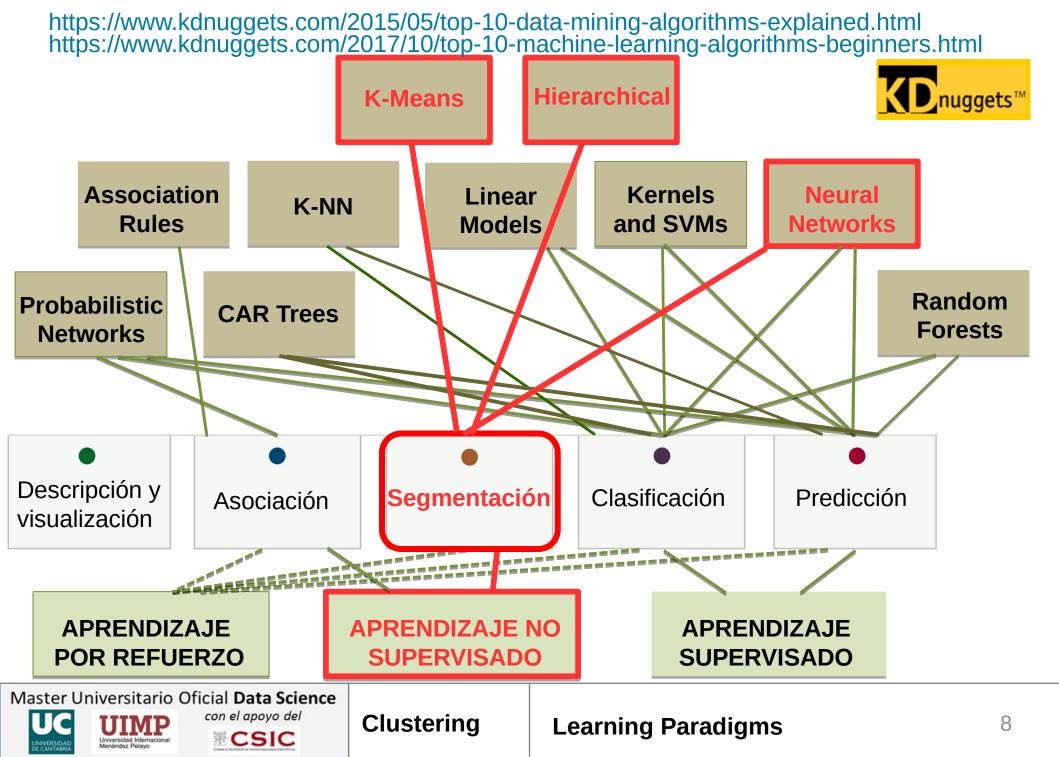
UNIVERSIDAD Universidad Internacional Menéndez Pelayo

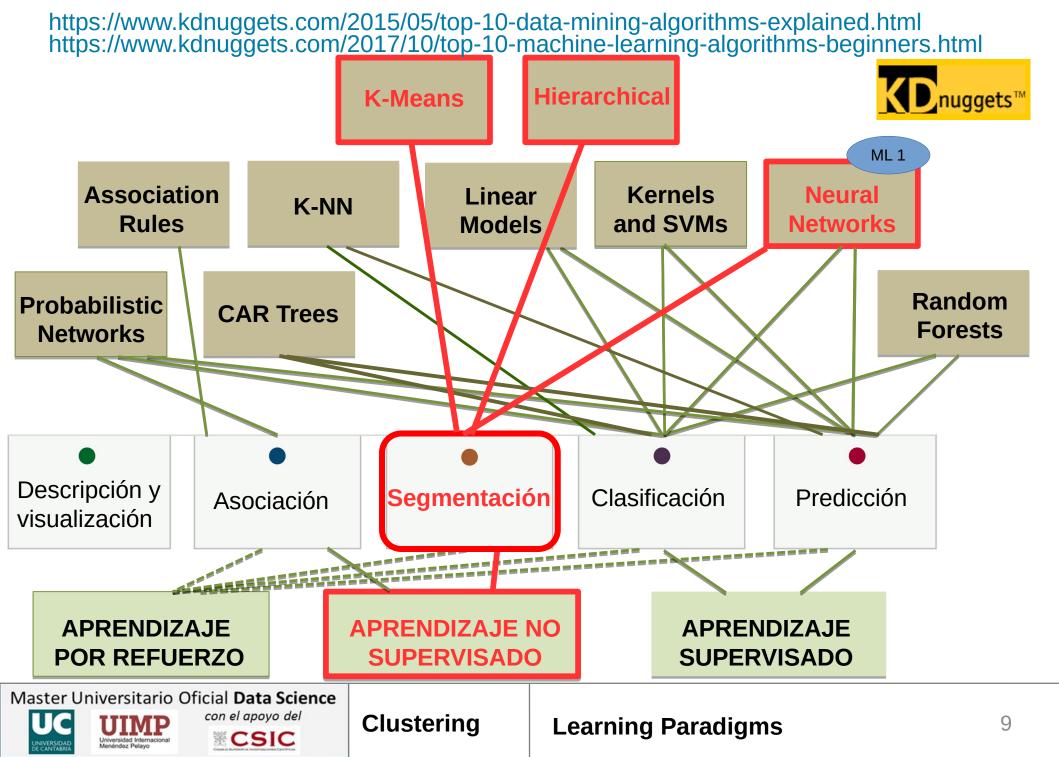
Clustering

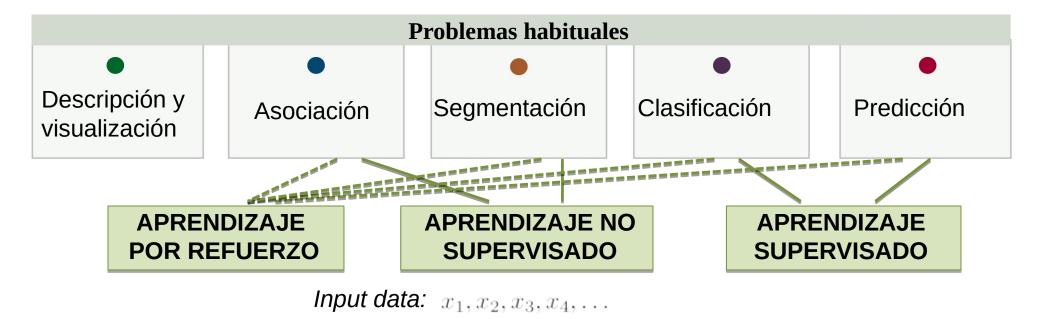








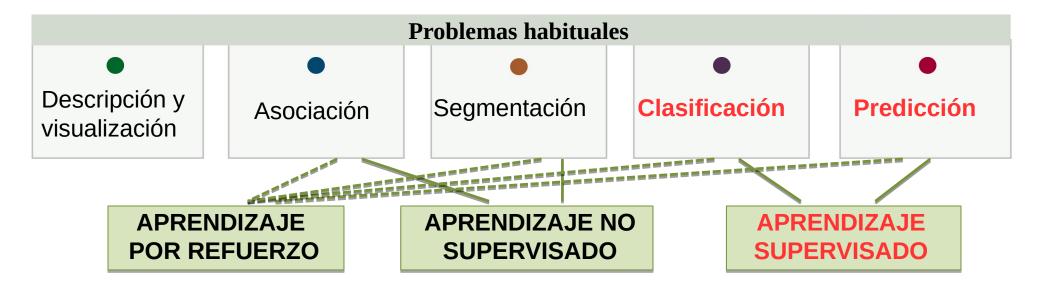




Supervised learning: The machine is also given desired outputs y_1, y_2, \ldots , and its goal is to learn to produce the correct output given a new input.

Unsupervised learning: The goal of the machine is to build representations of x that can be used for reasoning, decision making, predicting things, communicating etc.

Reinforcement learning: The machine can also produce actions a_1, a_2, \ldots which affect the state of the world, and receives rewards (or punishments) r_1, r_2, \ldots Its goal is to learn to act in a way that maximises rewards in the long term.



Target Variable: *Y: discrete/factor* or *continuous*

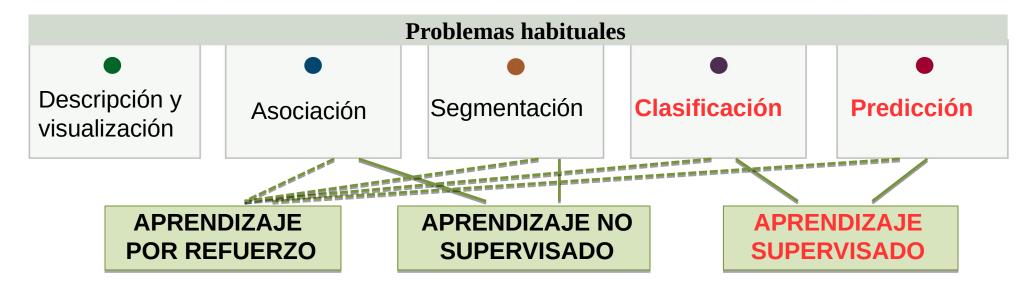
What we are trying to predict.

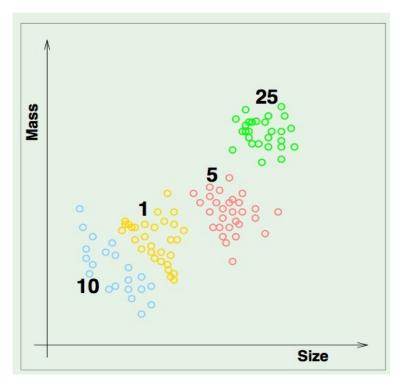
Predictive Variables: $\{X_1, X_2, \dots, X_N\}$: *continuous*

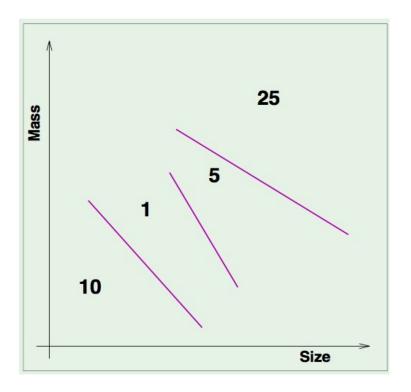
"Covariates" used to make predictions.

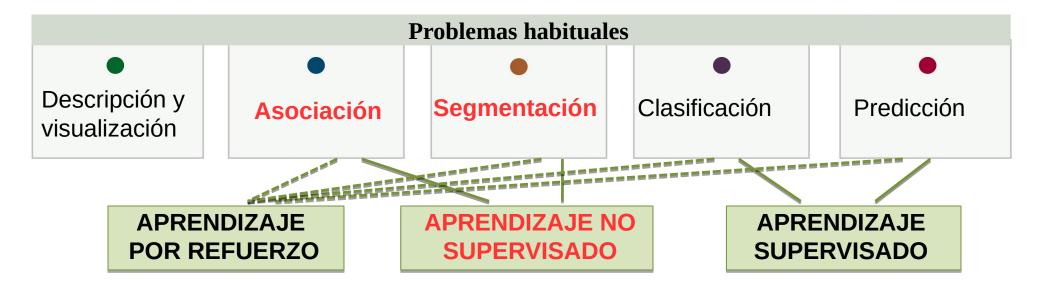
Predictive Model: $Y = f(X_1, X_2, ..., X_N)$

"Learning engine" that estimates the f (or the parameters defining f).









Target Variable: There is no target variable (association)

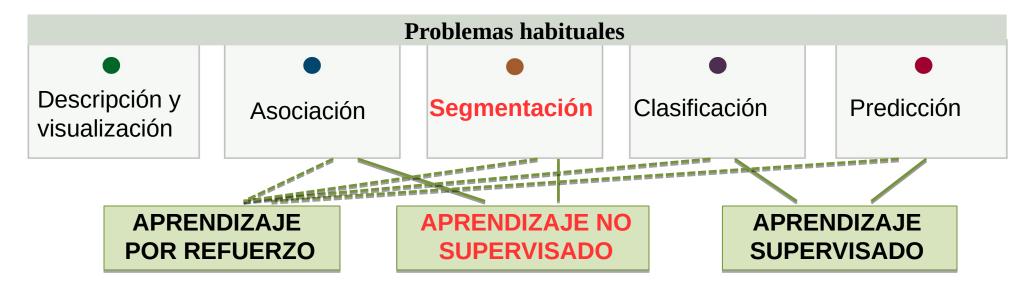
K (cluster), discrete: #clusters (segmentation)

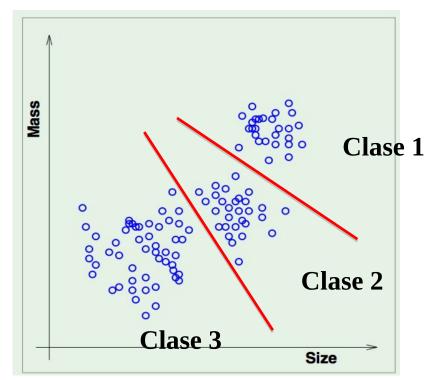
Predictive Variables: $\{X_1, X_2, \dots, X_N\}$: continuous or discrete

"Covariates" used to make predictions.

Predictive Model: Algorithmic, based on $(X_1, X_2, ..., X_N)$.

Ad-hoc "learning" and "prediction" engine.







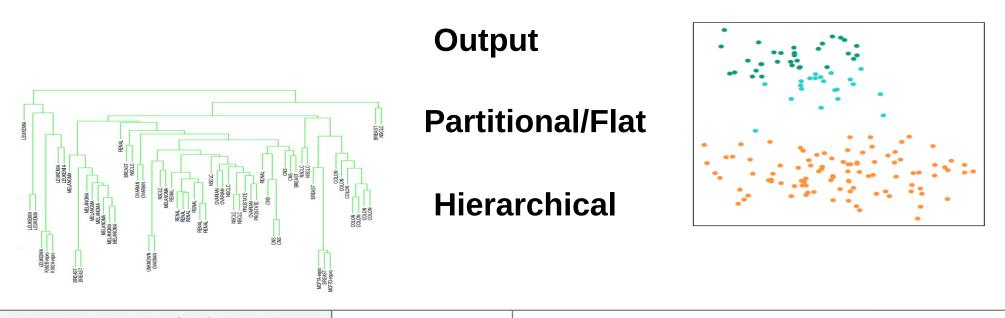


Input

Similarity-based → NxN distance matrix D

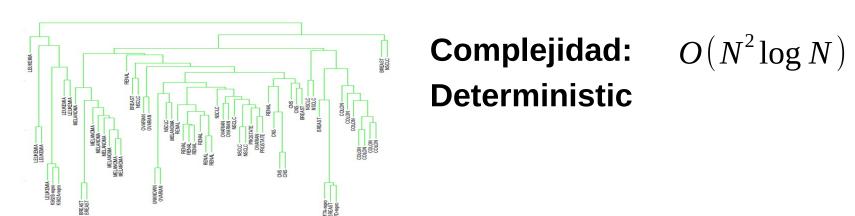
Feature-based → **NxD feature matrix X**





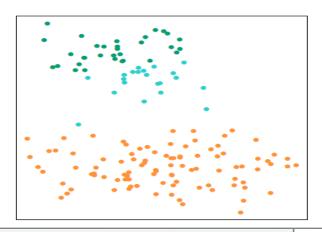


Hierarchical





Partitional/Flat



Complejidad: O(ND)

Depends on the number of clusters Sensitivity to initial conditions



Input

Output

Similiraty-based

Partitional/Flat

Feature-based

Hierarchical

To this aim, an assessment of the **degree of difference (dissimilarity)** between the objects assigned to the respective clusters is required.

Similarity and distance measures are obtained/defined considering the predictors. Therefore, strongly depend on the nature of these variables:

Quantitative Qualitative Ordinals etc...







Similarity and distance measures are obtained/defined considering the predictors. Therefore, strongly depend on the nature of these variables:

Quantitative

Minkowsky:

Manhattan / city-block:

$$D(x,y) = \left(\sum_{i=1}^{m} |x_i - y_i|^r\right)^{\frac{1}{r}} \qquad D(x,y) = \sqrt{\sum_{i=1}^{m} (x_i - y_i)^2} \qquad D(x,y) = \sum_{i=1}^{m} |x_i - y_i|$$

$$D(x,y) = \sqrt{\sum_{i=1}^{m} (x_i - y_i)^2}$$

$$D(x,y) = \sum_{i=1}^{m} |x_i - y_i|$$

$$D(x,y) = \sum_{i=1}^{m} \frac{|x_i - y_i|}{|x_i + y_i|}$$

$$D(x,y) = \sum_{i=1}^{m} \frac{|x_i - y_i|}{|x_i + y_i|}$$
 Chebychev:
$$D(x,y) = \max_{i=1}^{m} |x_i - y_i|$$

Quadratic:
$$D(x,y) = (x - y)^T Q(x - y) = \sum_{j=1}^{m} \left(\sum_{i=1}^{m} (x_i - y_i) q_{ji} \right) (x_j - y_j)$$

definite $m \times m$ weight matrix

Mahalanobis:

$$D(x,y) = [\det V]^{1/m} (x - y)^{\mathrm{T}} V^{-1} (x - y)$$

V is the covariance matrix of $A_1..A_m$, and A_i is the vector of values for attribute j occuring in the training set instances 1..n.

orrelation:
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$$\overline{x}_i = \overline{y}_i$$
 and is the average value for attribute *i* occurring in the training set.

Chi-square: $D(x,y) = \sum_{i=1}^{m} \frac{1}{sum_i} \left(\frac{x_i}{size_{ix}} - \frac{y_i}{size_{ix}} \right)^2$

 sum_i is the sum of all values for attribute i occuring in the training set, and sizex is the sum of all values in the vector x.

sign(x)=-1, 0 or 1 if x < 0,

x = 0, or x > 0, respectively.

Kendall's Rank Correlation:
$$D(x,y) = 1 - \frac{2}{n(n-1)} \sum_{i=1}^{m} \sum_{j=1}^{i-1} \operatorname{sign}(x_i - x_j) \operatorname{sign}(y_i - y_j)$$

? dist dEuc<-dist(iris[,-5],method="euclidean")</pre> dMin<-dist(iris[,-5], method="minkowski",p=4)

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Similarity and distance measures are obtained/defined considering the predictors.

Therefore, strongly depend on the nature of these variables:

Quantitative

Ordinals → redefine as the rank or the order (e.g. {low, medium, high} \rightarrow {1/3,2/3,3/3}).

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$$D(x,y) = \sum_{i=1}^{m} |x_i - y_i|$$

$$D(x,y) = \sum_{i=1}^{m} \frac{|x_i - y|}{|x_i + y|}$$

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Quadratic:
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? dist

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Similarity and distance measures are obtained/defined considering the predictors.

Therefore, strongly depend on the nature of these variables:

Quantitative

Ordinals → redefine as the rank or the order (e.g. {low, medium, high} \rightarrow {1/3,2/3,3/3}).

Qualitative – Categorical → assign a distance of 1 if the features are different and 0 otherwise.

$$D(x,y) = \sum_{j=1}^{D} I(x_j \neq y_j)$$

Manhattan / city-block:

kowsky: Euclidean: Manhattan / city-b
$$D(x,y) = \left(\sum_{i=1}^{m} |x_i - y_i|^r\right)^{1/r} \qquad D(x,y) = \sqrt{\sum_{i=1}^{m} (x_i - y_i)^2} \qquad D(x,y) = \sum_{i=1}^{m} |x_i - y_i|$$

$$D(x,y) = \sqrt{\sum_{i=1}^{m} (}$$

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Q is a problem-specific positive definite $m \times m$ weight matrix

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dNom<-daisy(iris, metric="gower")</pre>



? dist

?daisy



library(cluster)

con el apoyo del CSIC

dEuc<-dist(iris[,-5],method="euclidean")</pre>

dMin<-dist(iris[,-5],method="minkowski",p=4)</pre>

Clustering

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Defined the distance:

$$D(x_i, x_{i'}) = \sum_{j=1}^{p} w_j \cdot d_j(x_{ij}, x_{i'j}); \quad \sum_{j=1}^{p} w_j = 1. \qquad D_I(x_i, x_{i'}) = \sum_{j=1}^{p} w_j \cdot (x_{ij} - x_{i'j})^2$$

The objective of the clustering algorithms is to:

$$T = \frac{1}{2} \sum_{i=1}^{N} \sum_{i'=1}^{N} d_{ii'} = \frac{1}{2} \sum_{k=1}^{K} \sum_{C(i)=k} \left(\sum_{C(i')=k} d_{ii'} + \sum_{C(i')\neq k} d_{ii'} \right),$$

$$T = W(C) + B(C), \quad W(C) = \frac{1}{2} \sum_{k=1}^{K} \sum_{C(i)=k} \sum_{C(i')=k} d(x_i, x_{i'}). \quad \text{Minimizes the distance intragroup}$$

$$B(C) = \frac{1}{2} \sum_{k=1}^{K} \sum_{C(i)=k} \sum_{C(i')\neq k} d_{ii'} \quad \text{Maximizes the distance between clusters.}$$

? kmeans

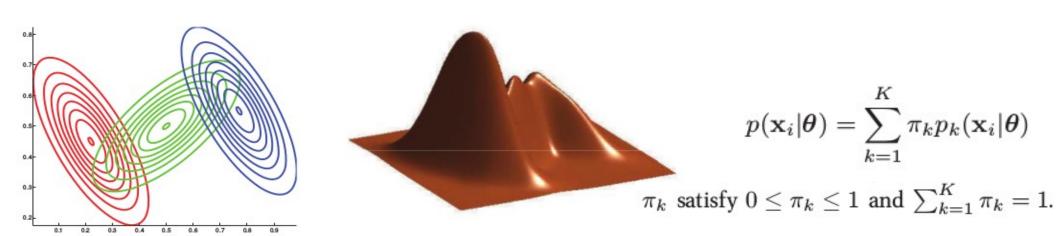
kmModel < -kmeans(iris[,-5],3,nstart = 1)

kmModel\$withinss ## Vector of within-cluster sum of squares, one component per cluster kmModel\$betweenss ## The between-cluster sum of squares

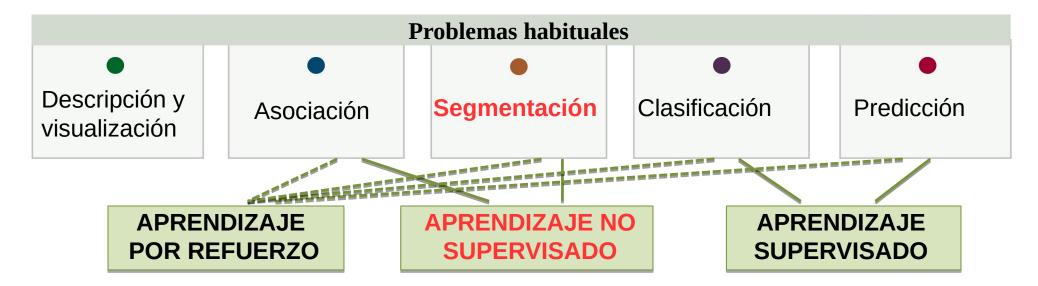








Source: Machine Learning A Probabilistic Perspective, Kevin P. Murphy, The MIT Press, Cambridge, Massachusetts, London, England



Gaussian Mixtures (EM-algorithm)

library (MASS) library (mclust)
$$p(\mathbf{x}_i|\boldsymbol{\theta}) = \sum_{k=1}^K \pi_k \mathcal{N}(\mathbf{x}_i|\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k) \qquad \pi_k \text{ satisfy } 0 \leq \pi_k \leq 1 \text{ and } \sum_{k=1}^K \pi_k = 1.$$

- **Expectation step (E):** Calculate the expected value of the log likelihood under the current estimate of the parameters.

$$r_{ik} = \frac{\pi_k p(\mathbf{x}_i | \boldsymbol{\theta}_k^{(t-1)})}{\sum_{k'} \pi_{k'} p(\mathbf{x}_i | \boldsymbol{\theta}_{k'}^{(t-1)})}$$

- Maximization step (M): Find the parameters that maximize the log likelihood.

$$\mu_k = \frac{\sum_i r_{ik} \mathbf{x}_i}{r_k}$$

$$\boldsymbol{\Sigma}_k = \frac{\sum_i r_{ik} (\mathbf{x}_i - \boldsymbol{\mu}_k) (\mathbf{x}_i - \boldsymbol{\mu}_k)^T}{r_k} = \frac{\sum_i r_{ik} \mathbf{x}_i \mathbf{x}_i^T}{r_k} - \boldsymbol{\mu}_k \boldsymbol{\mu}_k^T$$





Iris Data Set

Download: Data Folder, Data Set Description

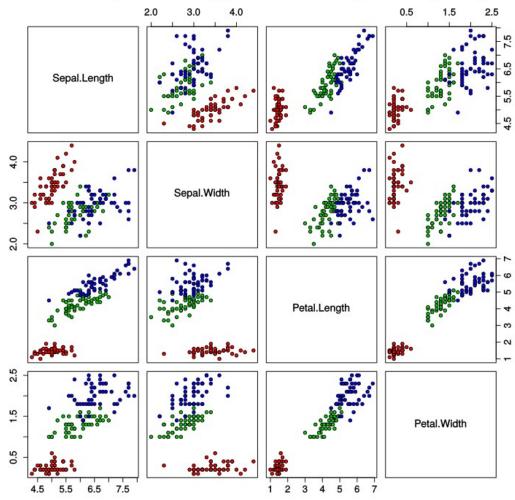
Abstract: Famous database; from Fisher, 1936

Data Set Characteristics:	Multivariate	Number of Instances:	150
Attribute Characteristics:	Real	Number of Attributes:	4
Associated Tasks:	Classification	Missing Values?	No



http://archive.ics.uci.edu/ml/datasets/Iris

Iris Data (red=setosa,green=versicolor,blue=virginica)



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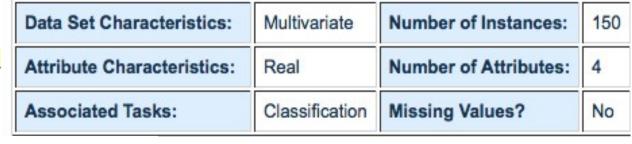


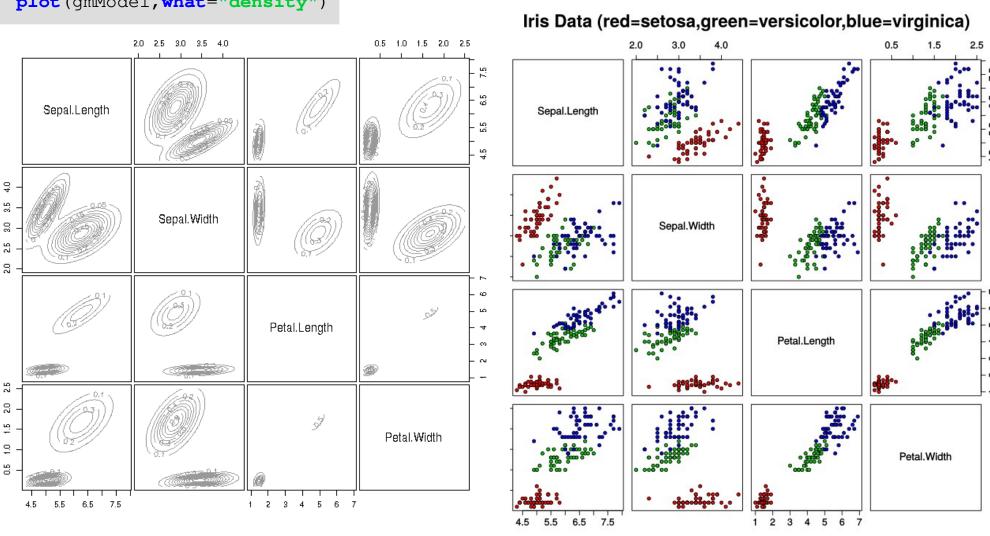
Iris Data Set

Download: Data Folder, Data Set Description

Abstract: Famous database; from Fisher, 1936

plot (gmModel, what="density")





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con el apoyo del CSIC

Clustering

Example

Iris Data Set

Download: Data Folder, Data Set Description

Abstract: Famous database; from Fisher, 1936

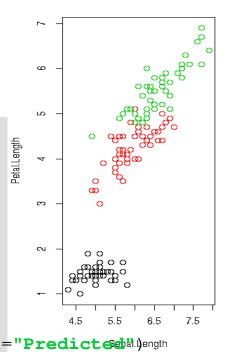
http://archive.ics.uci.edu/ml/datasets/Iris

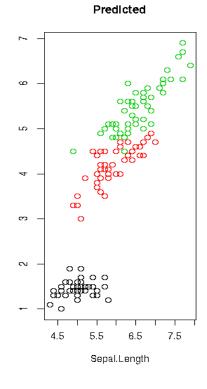
Data Set Characteristics:	Multivariate	Number of Instances:	150
Attribute Characteristics:	Real	Number of Attributes:	4
Associated Tasks:	Classification	Missing Values?	No

Observed



```
library(caret)
gmModel<-Mclust(iris[,-5])</pre>
summary(gmModel)
plot (qmModel, what="density")
## Defining the number of G-M
gmModel<-Mclust(iris[,-5],G=3)</pre>
summary(gmModel)
## Comparing observation and prediction
plot (qmModel, what="density")
par(mfrow=c(1,2))
plot (iris[,c(1,3)],col=iris[,5],main="Observed")
plot (iris[,c(1,3)], col=gmModel$classification, main="Predict@dal.)ength
confusionMatrix(as.numeric(iris[,5]),qmModel$classification)
```





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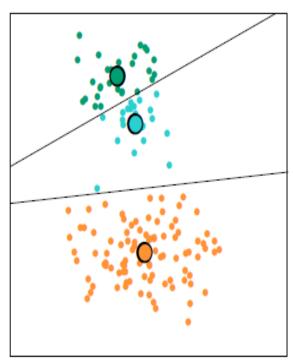


con el apoyo del CSIC



Centroid-based clustering: Non-overlapping (e.g. K-Means)

```
library(stats)
? kmeans
kmModel<-kmeans(iris[,-5],3,nstart=1)
summary(kmModel)
## Point center of two attributes
plot(iris[,c(1,3)],col=kmModel$cluster,main="K-Means")
points(kmModel$centers[,c(1,3)],col=1:3,pch=8,cex=2)
confusionMatrix(as.numeric(iris[,5]),kmModel$cluster)</pre>
```







K-Means is one of the most used iterative algorithms. It usually considers the Euclidean distance:

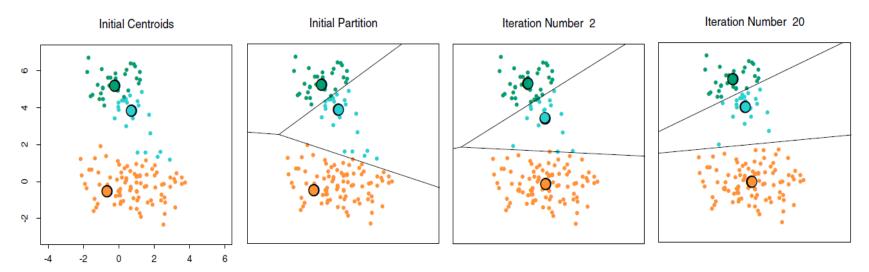
$$d(x_i, x_{i'}) = \sum_{j=1}^{p} (x_{ij} - x_{i'j})^2 = ||x_i - x_{i'}||^2 \longrightarrow W(C) = \frac{1}{2} \sum_{k=1}^{K} \sum_{C(i)=k} \sum_{C(i')=k} ||x_i - x_{i'}||^2 = \sum_{k=1}^{K} N_k \sum_{C(i)=k} ||x_i - \bar{x}_k||^2,$$

The objective is to find **K** centroids solution of the following optimization problem:

$$\min_{C,\{m_k\}_1^K} \sum_{k=1}^K N_k \sum_{C(i)=k} ||x_i - m_k||^2.$$

Once the parameter **K** is defined:

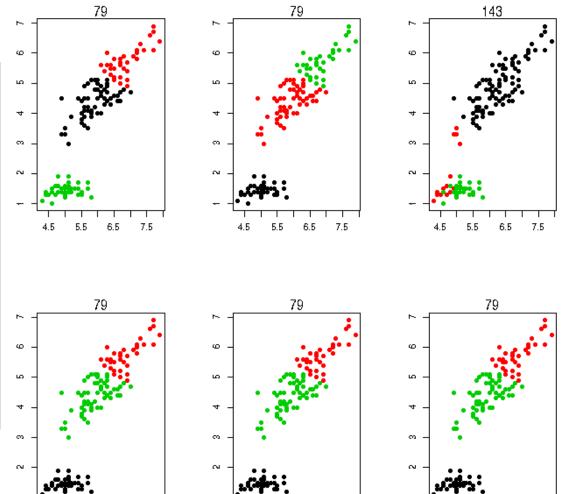
- First assignation randomly defined.
- Repeat until converge or reach the maximum number of iterations:
 - Estimate the centroid for each cluster.
 - Re-define the clusters considering the new centroids.







```
k<-3
par(mfrow=c(2,3))
i<-6
while (j>0) {
  set.seed(j)
  j<-j-1
  km<-kmeans(iris[,-5],centers=k)</pre>
  plot (iris[,c(1,3)],type="n")
  for(i in 1:k) {
    points(iris[km$cluster==i,c(1,3)],
            pch=19, col=i)
  mtext (format (km$tot.withinss, digits=2))
```



The main problems of this algorithm are:

- How to define the parameter **K**.
- The initialization could lead to different clusters.
- The clusterization is not incremental.

Example: https://www.kaggle.com/xvivancos/tutorial-clustering-wines-with-k-means



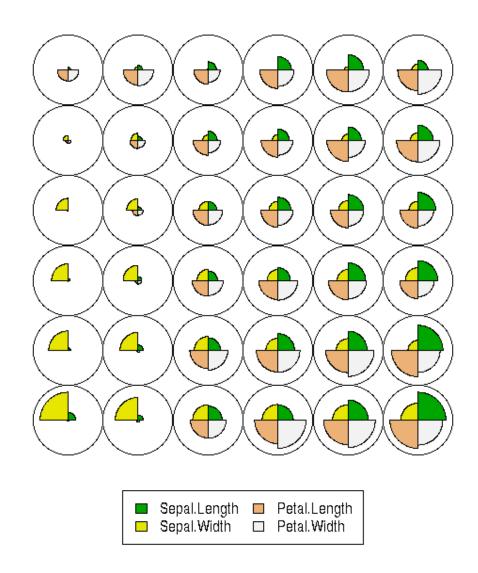




7.5

Self-Organising Maps can be considered a modification of the K-means algorithm including **topological constrains**

```
library(kohonen)
? som ## Clustering function.
? somgrid ## Definition of the topology.
som<-som(as.matrix(scale(iris[,-5])),</pre>
  somgrid(xdim=6, ydim=6, topo="rectangular"))
## Should be used to visualize the data:
plot (som)
## Considering 3 classes
somR<-som(as.matrix(scale(iris[,-5])),
  somgrid(xdim=1, ydim=3, topo="rectangular"))
somH<-som(as.matrix(scale(iris[,-5])),
  somgrid(xdim=3, ydim=1, topo="hexagonal"))
plot (somR)
plot (somH)
## We obtain the classification:
confusionMatrix(as.numeric(iris[,5]),
  somH$unit.classif)
```





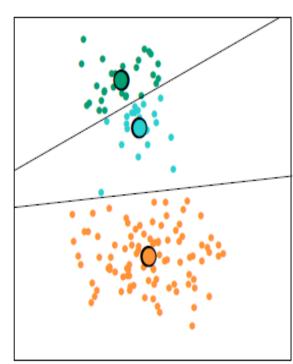






Centroid-based clustering: Non-overlapping (e.g. K-Means)

```
library(stats)
? kmeans
kmModel<-kmeans(iris[,-5],3,nstart=1)
summary(kmModel)
## Point center of two attributes
plot(iris[,c(1,3)],col=kmModel$cluster,main="K-Means")
points(kmModel$centers[,c(1,3)],col=1:3,pch=8,cex=2)
## How much clusters should we use?
totWithinss<-c(1:15)
for(i in 1:15){
   kmModel<-kmeans(iris[,-5],centers=i,nstart=1)
   totWithinss[i]<-kmModel$tot.withinss
}
plot(x=1:15,y=totWithinss,type="b",
   xlab="N. Of Cluster",ylab="Within groups sum of squares")</pre>
```



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Centroid-based clustering: Non-overlapping (e.g. K-Means)

Centroid-based clustering: Fuzzy clustering (e.g. C-Means)

```
library(e1071)
? cmeans
cmModel<-cmeans(iris[,-5],3,iter.max=1,m=2,method="cmeans")
summary(cmModel)
## Point center of two attributes
plot(iris[,c(1,3)],col=cmModel$cluster,main="K-Means")
points(cmModel$centers[,c(1,3)],col=1:3,pch=8,cex=2)
confusionMatrix(as.numeric(iris[,5]),cmModel$cluster)</pre>
```

Centroid

$$c_k = rac{\sum_x w_k(x)^m x}{\sum_x w_k(x)^m}.$$

Weights

$$egin{aligned} rg \min_{C} \sum_{i=1}^{n} \sum_{j=1}^{c} w_{ij}^{m} \|\mathbf{x}_{i} - \mathbf{c}_{j}\|^{2}, \ w_{ij} &= rac{1}{\sum_{k=1}^{c} \left(rac{\|\mathbf{x}_{i} - \mathbf{c}_{j}\|}{\|\mathbf{x}_{i} - \mathbf{c}_{k}\|}
ight)^{rac{2}{m-1}}}. \end{aligned}$$







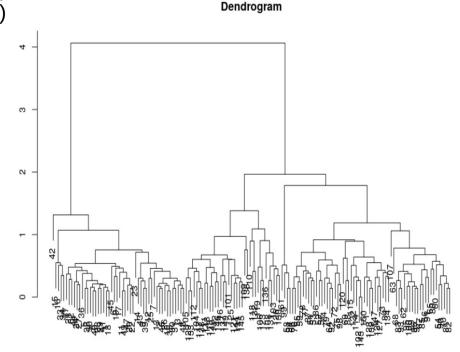


Centroid-based clustering: Non-overlapping (e.g. K-Means)

Centroid-based clustering: Fuzzy clustering (e.g. C-Means)

Hierarchical clustering

```
library(stats)
require(sparcl)## Include colours for the leaves.
? hclust
d<-dist(iris[,-5],method="euclidean")
hcModel<-hclust(d,method="average")
summary(hcModel)
plot(hcModel,main="Dendrogram")</pre>
```

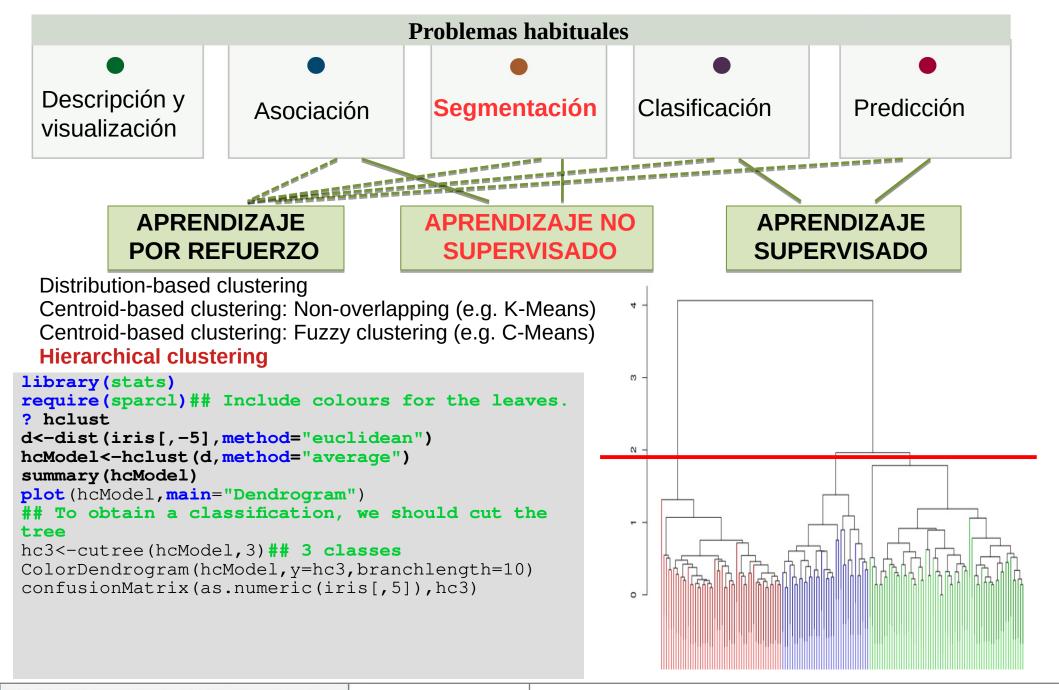


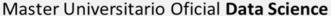
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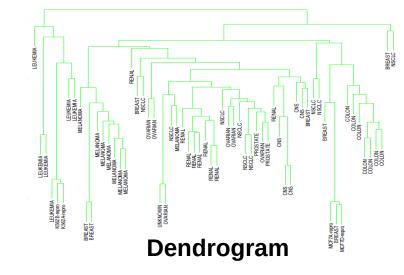






Hierarchical clustering is based on the similarity between members of the different groups/clusters to build the **dendrogram**. There are two approaches:

- Agglomerative: bottom up approach.
- Divisive: top down approach.









Hierarchical clustering is based on the similarity between members of the different groups/clusters to build the **dendrogram**. There are two approaches:

- Agglomerative: bottom up approach.
- **Divisive:** top down approach.

Linkage criterion determines the distance between the clusters and the agglomeration method:

- Complete-linkage: maximum of the distances.
- **Single-linkage:** minimum of the distances.
- Average-linkage (UPGMA): mean of the distances.
- Centroid-linkage (UPGMC): distances between centroids.

```
d<-dist(iris[,-5],method="euclidean")</pre>
## Available linkage criterion: "ward.D", "ward.D2", "single", "complete", "average",
## "mcquitty", "median" or "centroid".
par(mfrow=c(2,2))
plot (hclust (d, method="complete"), main="Complete-Linkage", col="blue", axes=FALSE)
plot (hclust (d, method="single"), main="Single-Linkage", col="red", axes=FALSE)
plot (hclust (d, method="average"), main="Average-Linkage", col="green", axes=FALSE)
plot (hclust (d, method="centroid"), main="Centroid-Linkage", col="black", axes=FALSE)
```







Dendrogram

Hierarchical clustering is based on the similarity between members of the different groups/clusters to build the **dendrogram**. There are two approaches:

- Agglomerative: bottom up approach.
- Divisive: top down approach.
 - Iteratively apply the K-means algorithm with K=2.
 - At each stage, the cluster with the largest diameter is selected, where the diameter of a cluster is the largest dissimilarity between any two of its observations (Macnaughton Smith et al. (1965), Kaufman and Rousseeuw (1990)).

```
library(cluster)
? diana ## Divisive clustering algorithm.
d<-dist(iris[,-5],method="euclidean")
diModel<-diana(d,diss=TRUE,metric="euclidean")
plot(diModel)
di3<-cutree(diModel,3)## 3 classes
confusionMatrix(as.numeric(iris[,5]),di3)
confusionMatrix(as.numeric(iris[,5]),hc3)</pre>
```

