

Determinant

ZPRAC-16-17-Lab12

DETERMINANT

[40 Points]

Up to 20% marks will be allotted for good programming practice.

These include

- Comments: for non-trivial code
 - Indentation: align your code properly
 - Function use and modular programming
 - Do not include anything in the header other than what is already given in the template.
 - Pointers are to be used whenever possible.
 - Recursion is to be used. Other analytic methods of computing would not fetch marks.
 - All matrices are to be dynamically created
 - remember, you can treat matrices as an array of arrays.
- 0 marks otherwise.

Determinant is a very important property of square matrices.

Interestingly, it can be computed in a recursive fashion as follows : Let $A(n,n)$ be a matrix of size $n \times n$. Let us define $M(j,k)$ = sub-matrix of A which does not contain the row j and column k . Clearly, the matrix M would be a square matrix of size $(n-1) \times (n-1)$. We can calculate $\det(A)$ as follows : $\det(A) = \sum \text{over any row or column } (((-1)^{(j+k)}) * A[j,k] * \det(M(j,k)))$. I.e. while applying the above recursion formula, keep one of j or k fixed.

Example:

For the 3x3 matrix A we can use the above formula with j=1 fixed and varying k :-

$$\det(A) = A[1,1]*\det(M(1,1)) - A[1,2]*\det(M(1,2)) + A[1,3]*\det(M(1,3)) .$$

(Assuming A is 1 indexed)

Input : An integer n denoting the size of the square matrix.

n lines of n integers each denoting the contents of the matrix.

Output: Determinant of the matrix. Example: Input: 2 3 1 1 6 Output: 17

Constraints: $1 \leq n \leq 5$