Hierarchical Dirichlet Regression Model for Benthic Cover in the Abrolhos Bank

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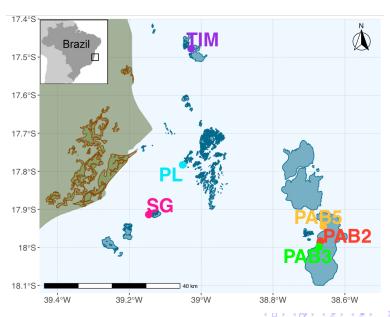
This work was done in collaboration with Mariana S. Sá and Larissa M. Martins.

11st of August, 2021

Framework

- Multivariate regression with constraint response.
- Challenge:
 - ▶ Unbalanced;
 - Lot of missing data;
 - Identificability issues
- Problem: To understand the variability by localization

Objective



Model

Maier (2014) and Holger (2018)

Alternative parametrization

- $\mathbf{Y}_l \sim D(\mu_l, \phi_l)$ with parameter $\alpha_{cl} = \mu_{cl}\phi_l$
- μ_{cl} : level term
- ϕ_l : precision term

Reference component: c^*

 c^* should be chosen

Sharing information equation

$$\beta_{cl} = \beta_c + \epsilon_{\beta_l}, \quad \epsilon_{\beta_l} \sim \mathcal{N}(0, V_{\beta})$$

$$\theta_l = \theta + \epsilon_{\theta_l}, \quad \epsilon_{\theta_l} \sim \mathcal{N}(0, V_{\theta})$$

Inference procedure

Let $\Theta = (\beta, \phi)$ be the vector of parameters

Proper independent prior distribution for the parametric vector Θ are Normal with zero mean and precision 1/K (one over K) for all effects of the model.

The joint posterior distribution does not have a known closed form

$$\pi(\boldsymbol{\Theta} \mid \mathbf{y}) \propto L(\boldsymbol{\Theta} \mid \mathbf{y}) \prod_{l}^{L} \pi(\phi_{l}) \prod_{c}^{C} \pi(\beta_{cl})$$
 (1)

Sampling from the posterior distribution

by Markov chain Monte Carlo (MCMC) via the Stan software.

Results and Conclusions

The results validate the original hypotheses

Sites near the coast (inshore) are more variable than the offshore sites.

Main conclusions

- The proposed model quantifies the heteroscedasticity through precision effects via hierarchical structures by site;
- The method is flexible;
- The reference component has been chosen using objective criteria;
- The proposal allows to obtain adequate predictions.
- This work contributes to the United Nations's Sustainable Development Goal 14 "Life Under Water".

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Thank you pamela@dme.ufrj.br